

3D Quantum Bubble Collisions

Jonathan Braden

University College London

COSMO 2015, Warsaw, September 9, 2015

Based on work with Dick Bond and Laura Mersini-Houghton

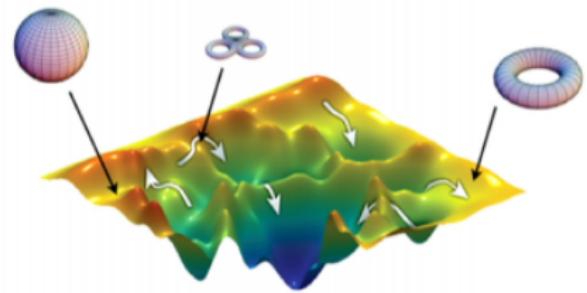
JCAP 1503 (2015) 03, 007 [arXiv:1412.5591]

JCAP 1508 (2015) 08, 048 [arXiv:1505.01857]

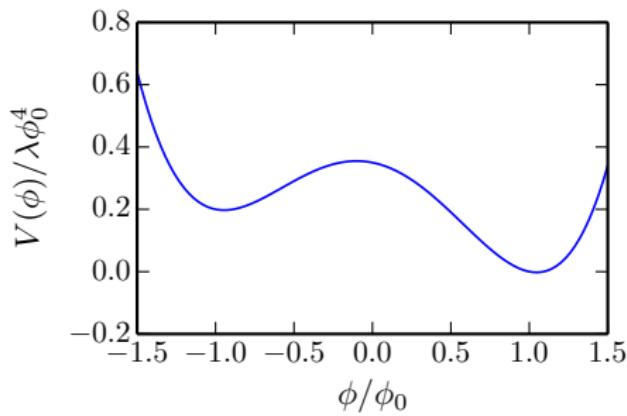
JCAP 1509 (2015) 09, 004 [arXiv:1505.02162]

Videos at www.star.ucl.ac.uk/~jbraden

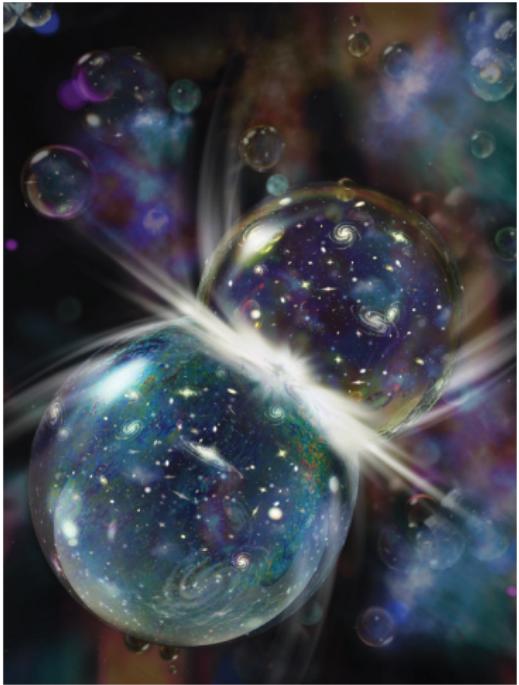
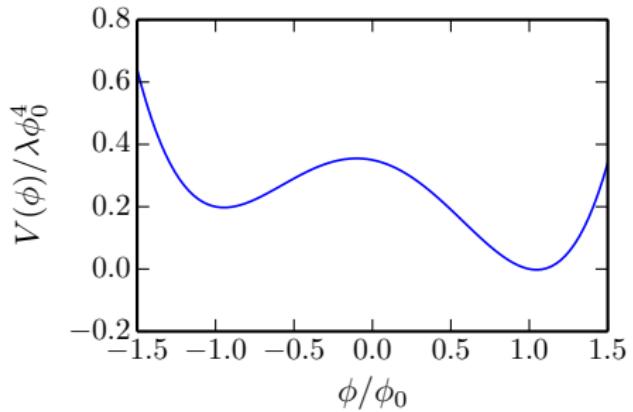
The Bubbly Universe



The Bubbly Universe



The Bubbly Universe



Outline

- ▶ Review of Standard Approach and It's Shortcomings
- ▶ Results of Collisions with Quantum Fluctuations
 - ▶ Single-field Example
 - ▶ Multi-field Example (inflation)
- ▶ Linear Parametric Resonance as Initial Stage
- ▶ Observational and Phenomenological Implications

Large Literature Starting in 1982 ...

Single Bubbles

- ▶ Coleman, deLuccia
- ▶ **Hawking, Moss**
- ▶ Turok
- ▶ Sasaki, Linde, Tanaka, Yamamoto
- ▶ Garriga, Vilenkin, Montes, Garcia-Bellido
- ▶ Guth, Guven
- ▶ Freese, Adams
- ▶ Susskind et al
- ▶ ...

Vacuum Bubble Collisions

- ▶ **Hawking, Moss, Stewart**
- ▶ Kosowski, Turner, Watkins, Kamionkowski
- ▶ **Johnson, Aguirre**, Tysanner, Larfors
- ▶ Chang, Kleban, Levy, Sigurdson, Gobbetti
- ▶ Easter, Giblin, Lim, Lau
- ▶ **Johnson, Lehner, Peiris**,... (GR)
- ▶ ...

Observations

- ▶ **Johnson, Peiris, Mortlock, McEwan, Feeney**,...
- ▶ Smith, Senatore, Osborne

... All Based on the “Canonical” $\text{SO}(2,1)$ Approach

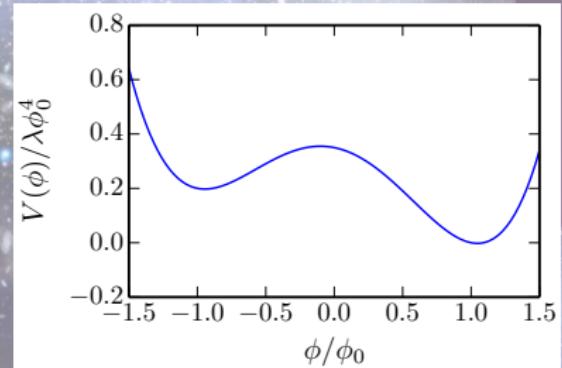
New Coordinates (Minkowski)

$$t = s \cosh \psi$$

$$x = x$$

$$y = s \sinh \psi \cos \theta$$

$$z = s \sinh \psi \sin \theta$$



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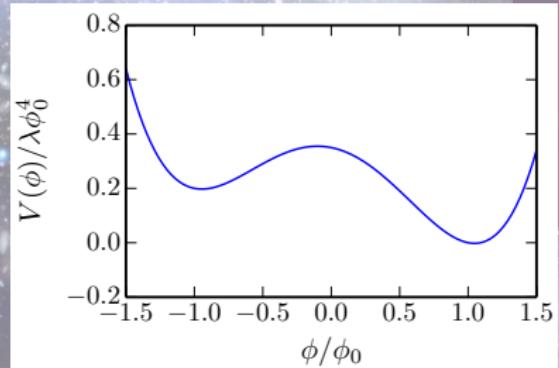
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$\text{SO}(2,1)$ Assumption: $\phi(t, x, y, z) = \phi(s, x)$

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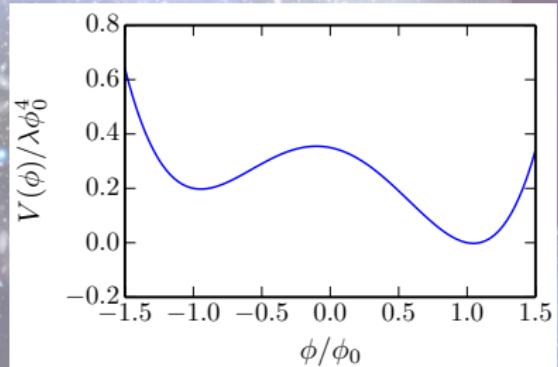
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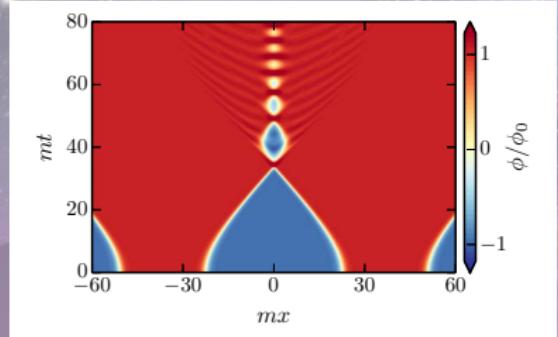
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$\text{SO}(2,1)$ Assumption: $\phi(t, x, y, z) = \phi(s, x)$

Individual Bubbles

- ▶ Perfectly Spherical
- ▶ Boost Invariant



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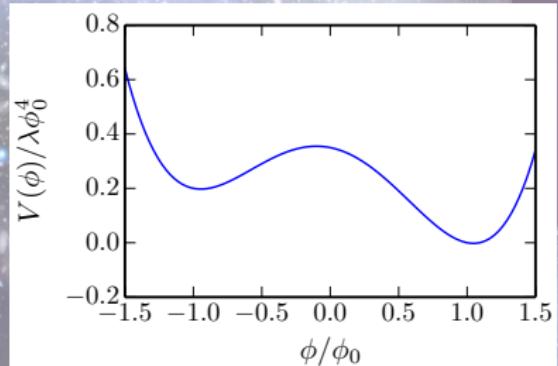
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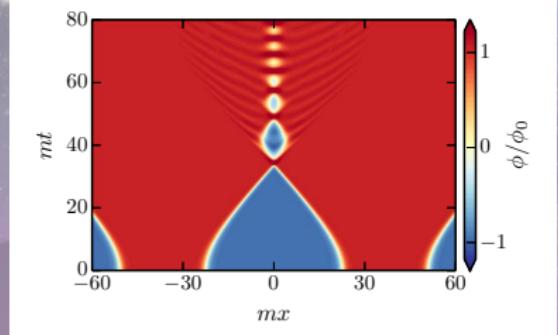
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$\text{SO}(2,1)$ Assumption: $\phi(t, x, y, z) = \phi(s, x)$

2nd Bubble Breaks

- ▶ 1 Boost
- ▶ 2 Rotations



... All Based on the “Canonical” SO(2,1) Approach

New Coordinates (Minkowski)

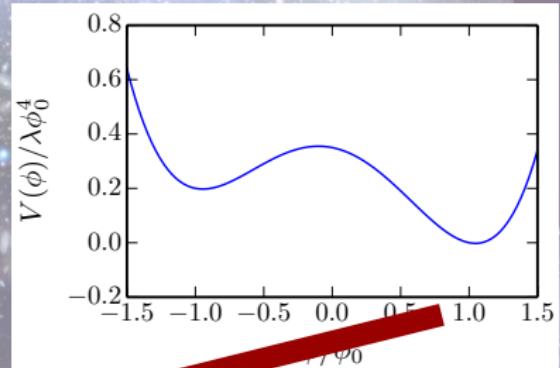
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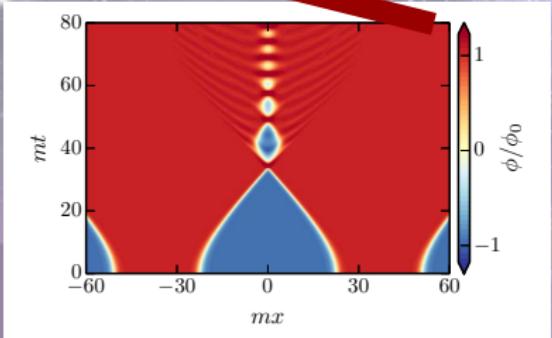
~~SO(2,1) Assumption~~



$$\phi(s, x, y, z) = \phi(s, x)$$

2nd Bubble Breaks

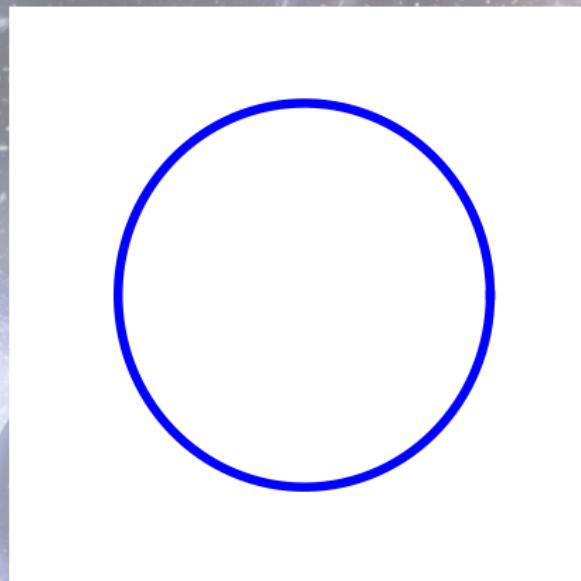
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Limitations of SO(2,1) Formalism

Quantum (or Stochastic) Fluctuations

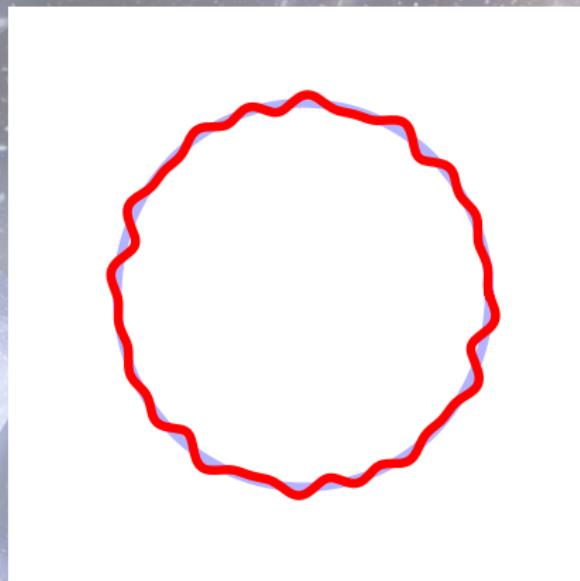
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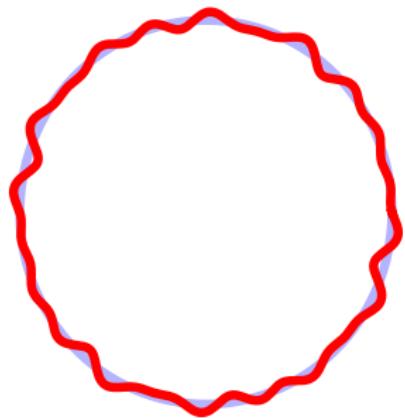
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$\delta\phi$ has dynamics not captured by SO(2,1) formalism

Ignoring $\delta\phi$ Breaks

- ▶ Quantum Mechanics
- ▶ Bubble Nucleation
- ▶ Inflationary perturbations

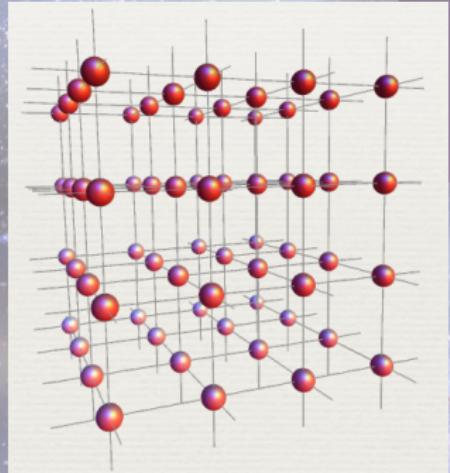


Hybrid MPI/OpenMP Lattice Code

- ▶ Solve field equation (e.g.)

$$\ddot{\phi}_i + 3\frac{\dot{a}}{a}\dot{\phi}_i - \frac{\nabla^2 \phi_i}{a^2} + V'(\vec{\phi}) = 0$$

- ▶ 10th order Gauss-Legendre integration (general) or 8th order Yoshida (nonlinear sigma models)
- ▶ Finite-difference (fully parallel) or Pseudospectral (OpenMP)
- ▶ Optional absorbing boundaries
- ▶ Quantum fluctuations → realization of random field



- ▶ Energy conservation $\mathcal{O}(10^{-9} - 10^{-14})$

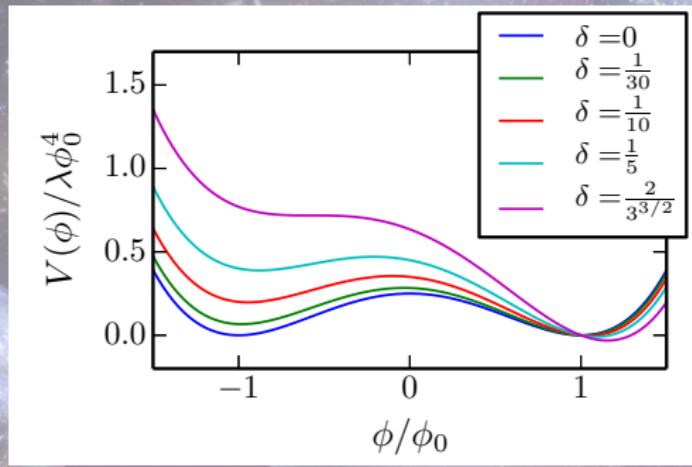
Initial Conditions I: The Bounce Solution [c.f. Coleman]

$$\frac{d^2\phi_b}{dr_E^2} + \frac{3}{r_E} \frac{d\phi_b}{dr_E} - \frac{\partial V}{\partial \phi} = 0$$

$$\phi_b(r_E = \infty) = \phi_{false} \quad \partial_{r_E} \phi_b(r_E = 0) = 0$$

$$r_E^2 \equiv \tau^2 + x^2 + y^2 + z^2 \quad \tau \equiv it$$

Pseudospectral
Approximation



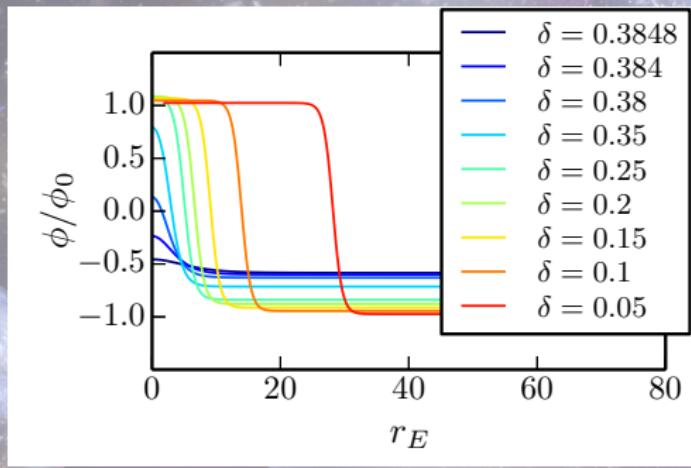
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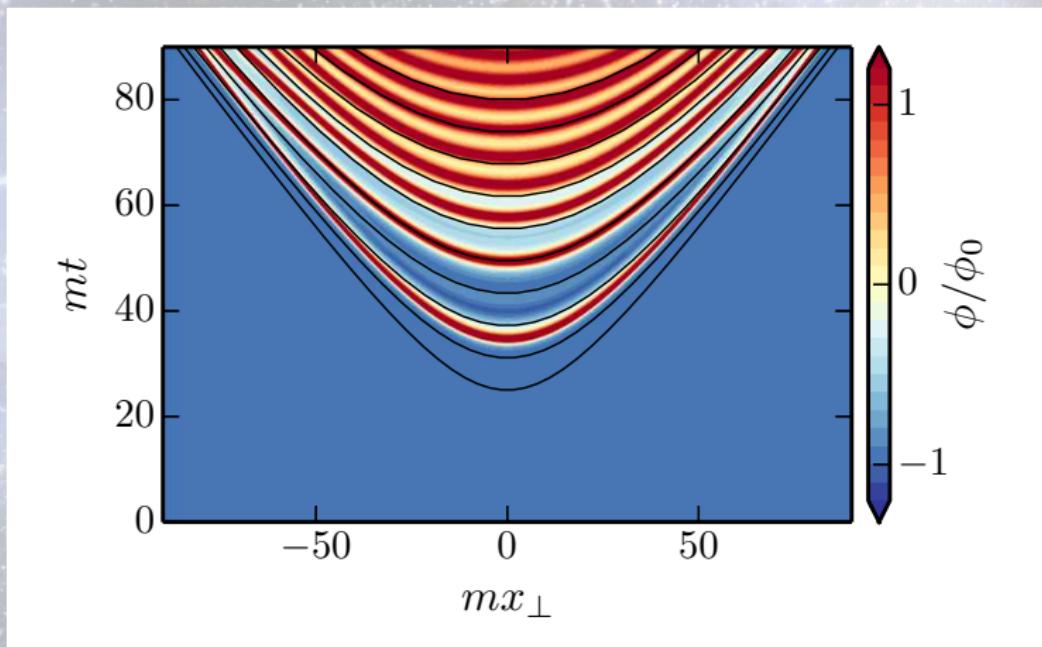


A photograph showing two people playing bumper ball on a grassy field. They are wearing large, transparent, spherical safety pods. One person's pod has the brand name "BumperBallz" printed on it. The person on the right is leaning back, performing a kick or a collision maneuver. The background shows a chain-link fence and some trees under an overcast sky.

Now Some Collisions

Three-Dimensional SO(2,1) Collision

Numerical Preservation of $\text{SO}(2,1)$ Symmetry

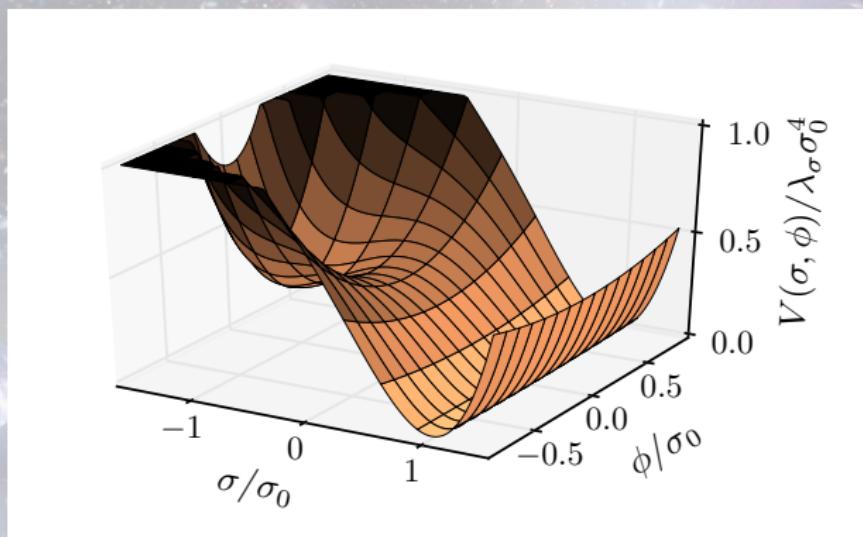


Same Collision with Fluctuations ... [JB, Bond, Mersini-Houghton, 1505.02162]

... Produces Oscillons (Visible in Energy Density)

Works for multifield models supporting inflation as well

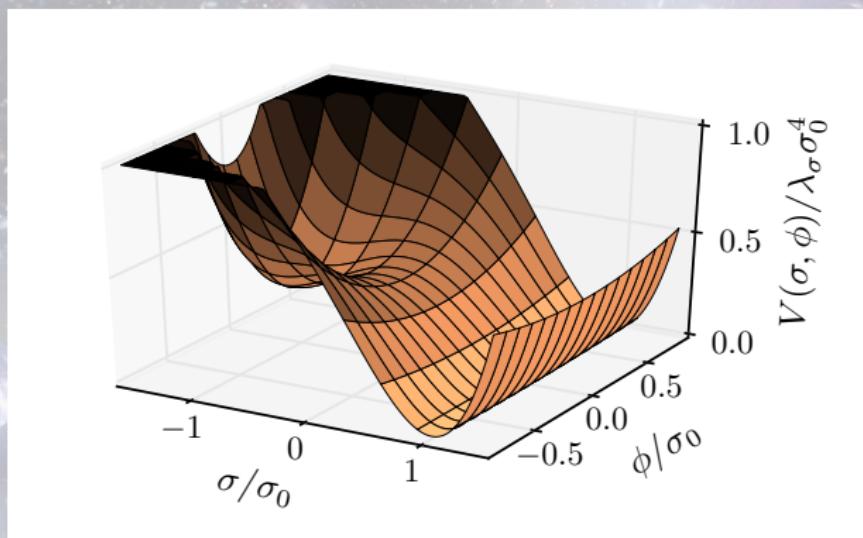
$$V(\sigma, \phi) = \frac{\lambda_\sigma \sigma_0^4}{4} \left[\left(\frac{\sigma^2}{\sigma_0^2} - 1 \right)^2 - \frac{\delta}{\lambda_\sigma} \frac{\sigma}{\sigma_0} \right] + \epsilon \phi + \frac{g^2}{2} \phi^2 \sigma^2$$



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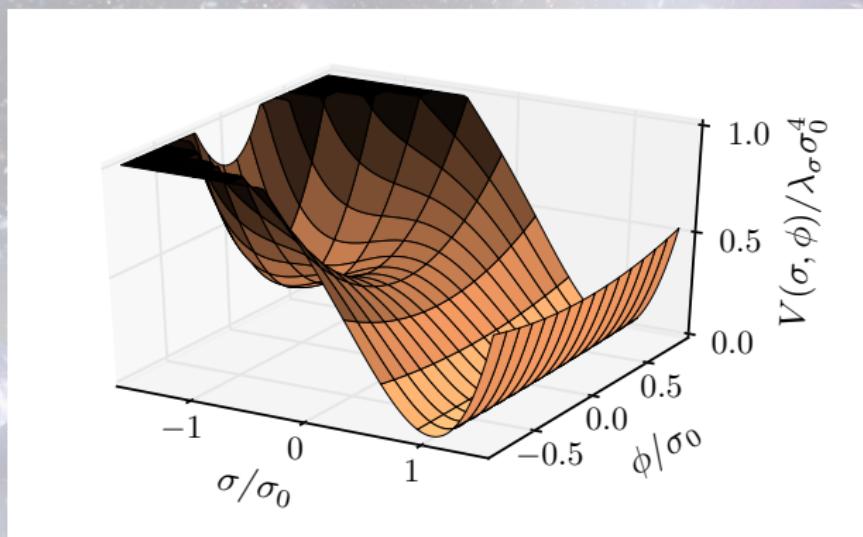
► V_{tunnel}



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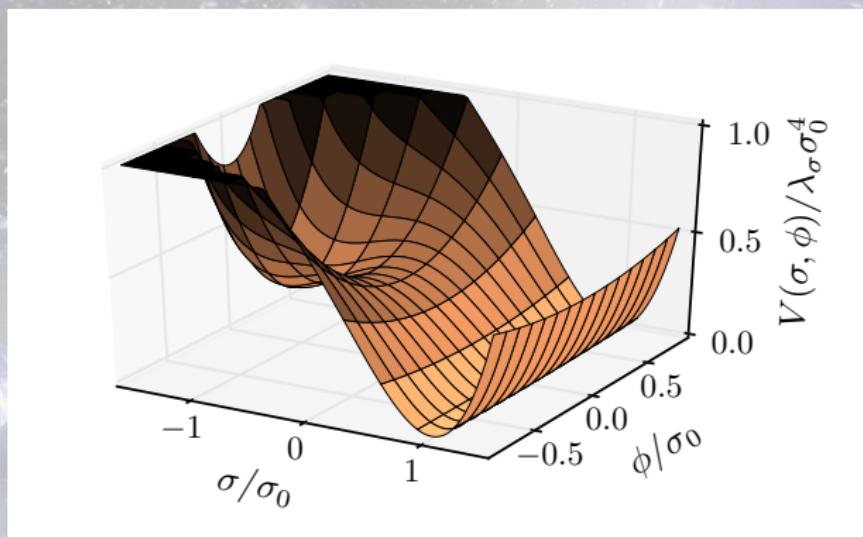
- ▶ V_{tunnel}
- ▶ $V_{inflaton}$



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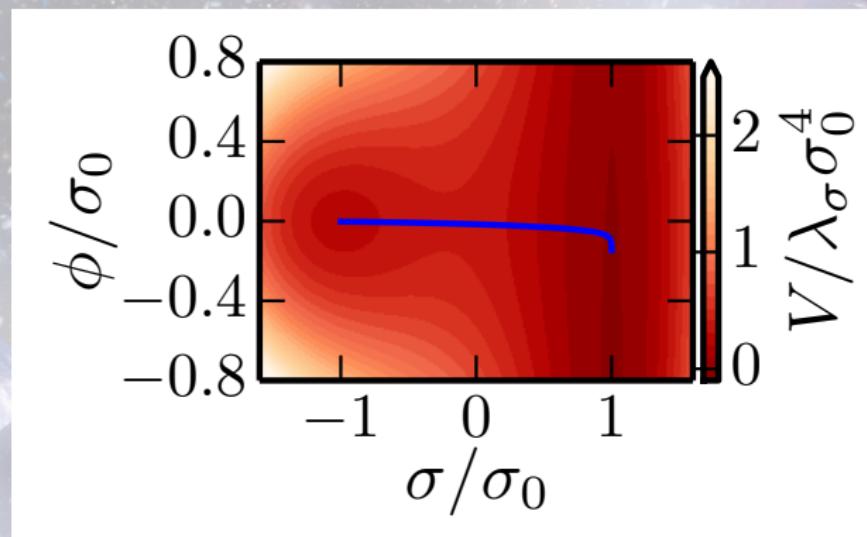
- V_{tunnel}
- $V_{inflaton}$
- $V_{coupling}$



Works for multifield models supporting inflation as well

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Evolution of σ and ϕ

σ Evolution

ϕ Evolution

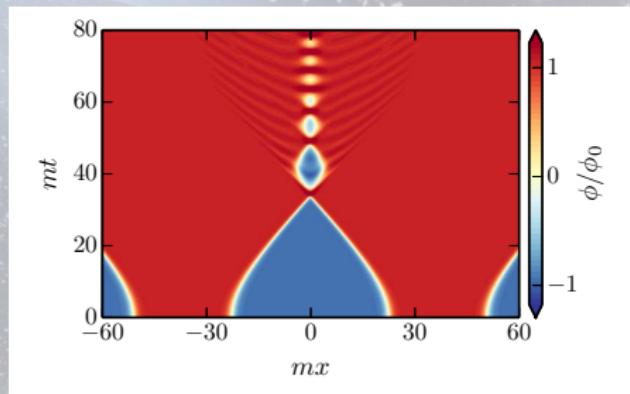
Why Does This Happen?

Linear Parametric Resonance

[JB, Bond, Mersini-Houghton, 1412.5591]

Non-SO(2,1) fluctuations evolve in the symmetric background

$$\frac{\partial^2 \phi_{bg}}{\partial s^2} + \frac{2}{s} \frac{\partial \phi_{bg}}{\partial s} - \frac{\partial^2 \phi_{bg}}{\partial x^2} + V'(\phi_{bg}) = 0$$
$$\left[\frac{\partial^2}{\partial s^2} - \frac{\partial^2}{\partial x^2} - \frac{\nabla_{H_2}^2}{s^2} + V''(\phi_{bg}) \right] (s\delta\phi) = 0$$



Floquet Theory

c.f. Preheating [Kofman,Linde,Starobinski '97]

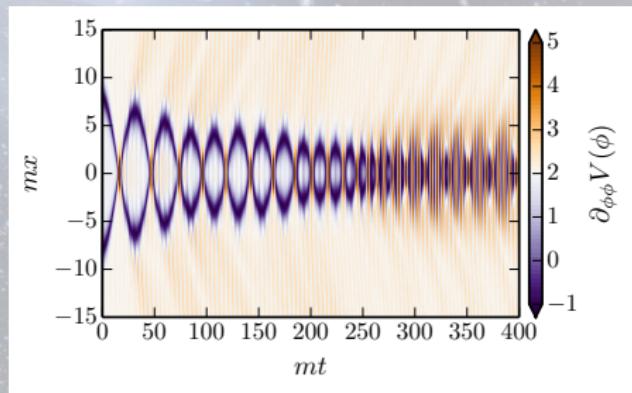
Oscillating $V''(\phi_{bg})$
⇒ $\delta\phi \sim e^{\mu t} P(x, t)$

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$$\left[\frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial x^2} + (k_\perp^2 + V''(\phi_{planar})) \right] \delta \tilde{\phi}_{k_\perp} = 0$$



Floquet Theory

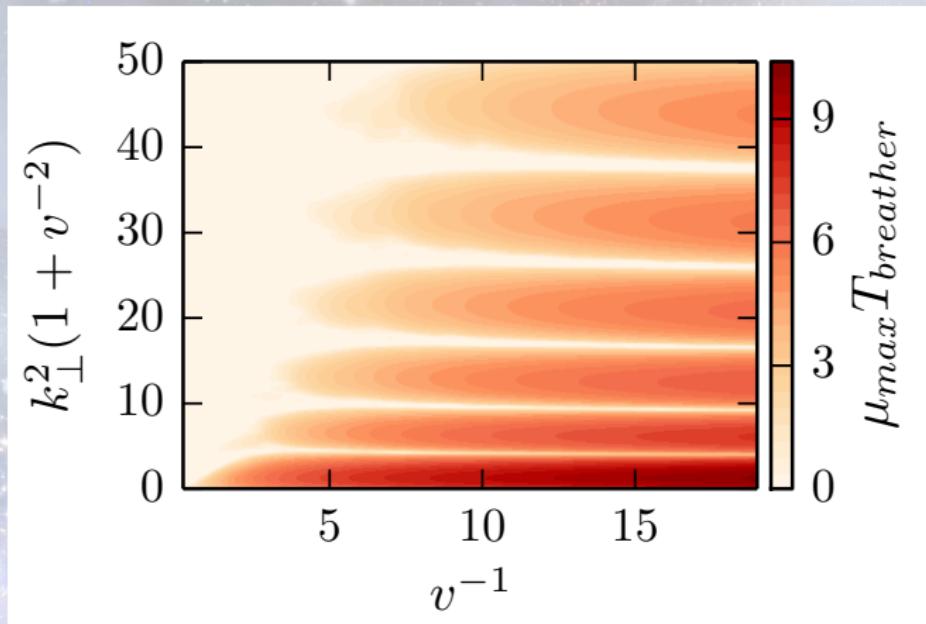
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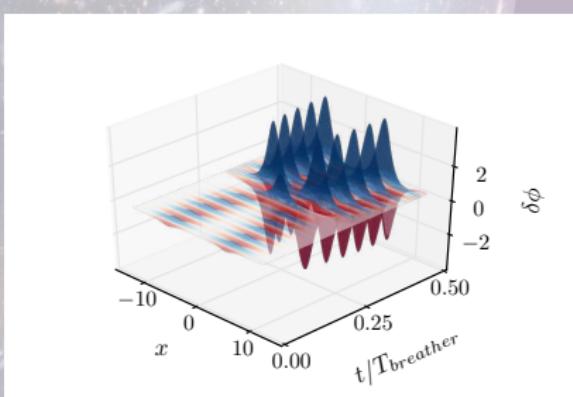
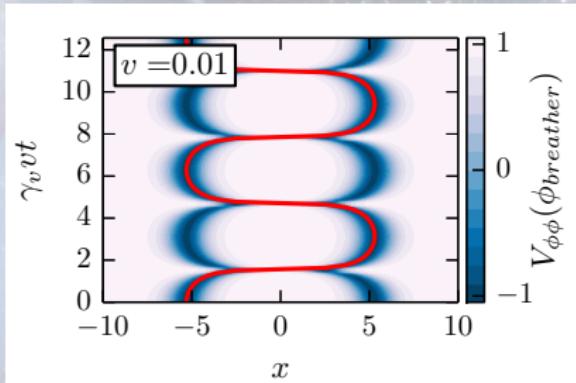
Exponentially Growing Modes Exist

$$V(\phi) = 1 - \cos(\phi)$$

$$\phi_{breather} = 4 \tan^{-1} \left(\frac{\cos(\gamma_v v t)}{v \cosh(\gamma_v x)} \right) \quad \gamma_v \equiv (1 + v^2)^{-1/2}$$



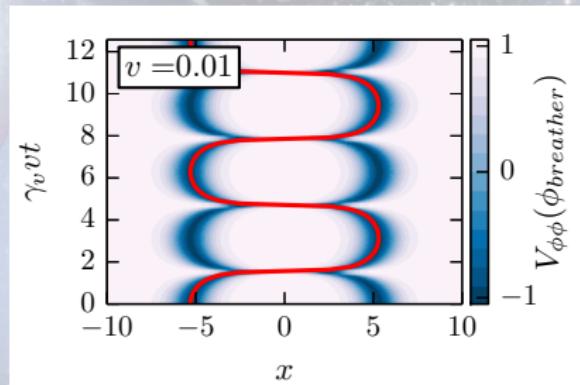
Broad Resonance for Colliding Walls



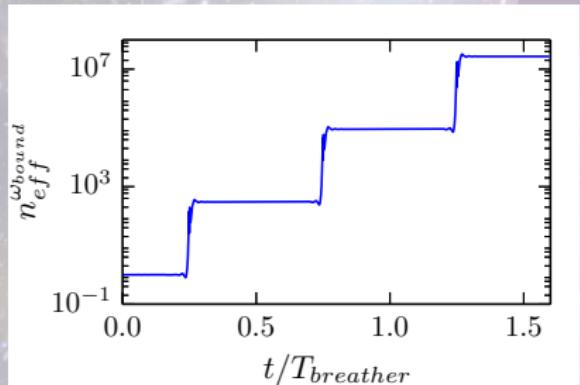
Generic Instability

- ▶ Goldstones of Spontaneously Broken Translation Invariance
- ▶ Time-dependent wall “tension”

Broad Resonance for Colliding Walls



$$n_k^{eff} \propto \frac{1}{2k_{\perp}} \int_{-\infty}^{\infty} dx \left(\delta\dot{\phi}_k^2 + k_{\perp}^2 \delta\phi^2 \right)$$



Generic Instability

- ▶ Goldstones of Spontaneously Broken Translation Invariance
- ▶ Time-dependent wall “tension”

Implications

SO(2,1) symmetry can be badly broken

Observables don't necessarily have azimuthal symmetry

- ▶ Beam smoothing versus inhomogeneity scale
- ▶ Tensor modes are produced by fracturing of walls
- ▶ Inhomogeneous start to inflation in some regions
- ▶ Sign of $\zeta = \delta \ln(a)$ in one field versus two field model

Qualitative conclusions don't depend on inflationary scenario

- ▶ Oscillons as nonequilibrium environment for baryogenesis?
- ▶ Oscillons dilute as $a^{-3} \rightarrow$ perturbed EOS during phase transition?
- ▶ Application to braneworlds with colliding walls
- ▶ Preheating in unwinding inflation?
- ▶ Bubble baryogenesis

These signals are spatially **intermittent**