



planck

Dick Bond @Stanford17\_12

# Quantum Inflation in the Planck Era & Beyond



what are the degrees of freedom / parameters of the ultra early Universe? TBD

Quantum Inflation - if quantum energy then quantum gravity (entangled) then gravitons

Phonons *density fluctuations = Trace strain = spatial 3-volume fluctuations*

=> *combined entropy-like measure*  $\zeta$  =inflaton

$$\zeta(x,t) = \int_{\text{field-path}} (dE+pdV)/3(E+pV)$$



Gravitons *tensor perturbations transverse traceless strain*  $P_{GW} = r P_{\zeta}$  *grail*  $r < .07$  now, to  $< .001$

Isocons *when multiple particle-species - orthogonal scalar degrees of freedom to inflaton/phonon*

Dilatons *4-volume fluctuations - Higgs inflation*  $L_G(R)$  *gravity - conformally-flatten potentials*

moduli, axions *connection to particle physics models "fundamental scalars" .. string theory*

fermions, vector gauge fields, *Standard model of particle physics* .. vector perturbations

begin-inflate => inflate => end-inflate => preheat => non-equilibrium heat+entropy

=> *Standard Model particle physics* QG plasma radiation dominated

=> dark matter dominated *structure via gravitational instability* => dark energy now

*fit into a UV-complete theory (ultra-high energy to the Planck scale) strings, landscape, .. & IR-complete theory (post-inflation heating -> quark/gluon plasma)???* TBD



# $\zeta$ all cosmic structure from **entropy!**

linear (*bst1983*)  $\Rightarrow$  nonlinear  $\zeta(\mathbf{x}, t) = \int_{\text{field-path}} (dE + pdV) / 3(E + pV)$   
*SBB89, SB90,91, B95, B+Braden17* **coarse-grained** horizon scale cf. fine-grained fluctuations

*system / signal*

*reservoir / noise*

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*coarse-grained* horizon scale cf. *fine-grained* fluctuations

$$\ln V / \langle V \rangle |_{\rho} = 3 \ln a(\mathbf{x}, t) / \langle a \rangle |_{\rho} = \ln \det A^{ij}(\mathbf{x}, t) / \langle a \rangle |_{\rho} \sim 1/2 \ln \det {}^{(3)}g^{ij}$$

**volume deformation = isotropic strain** SBB89, SB90,91, B95  
-> Sasaki+  $\delta N$  'formalism'

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volume deformation = **isotropic strain**

$\ln \rho(\mathbf{x},t) / \langle \rho \rangle |_v$  **phonon**

*SBB89, SB90,91, B95, B+Braden17  
B2FH, b+braden+frolov+huang*



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along coarse-grain trajectories  $d\zeta = [d\bar{\zeta}] (fg \rightarrow cg) \quad (- [d\bar{\zeta}] (cg \rightarrow fg))$

regimes: 1. stochastic inflation non-adiabatic  $[d\bar{\zeta}] (fg \rightarrow cg)$

*reduction of Langevin network for all fields, Fokker-Planck probability evolution*



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**gradient flow + stochastic jitter**, simple Hamilton principle function  $S \sim H(\phi_{cg})$

*origin of all cosmic structure from quantum noise story - nonGaussianity feedback of cg on fg*



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*classical dynamical system theory, chaos*

2. ballistic phase adiabatic thru EoI, but caustics & Kolmogorov-Sinai entropy



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3. shock-in-time,  $cg \Leftrightarrow fg$ , origin of almost all entropy  $S_{U,m+r} \sim 10^{88.6}$   
non-equilibrium S burst, slow evolution to quark/gluon plasma cf.  $S_G \sim 10^{121.9}$  asymptotic DE





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further S generation in early Unioverse: phase transitions, out-of-equilibrium decays?

further  $\mathbf{dbar} S$ : reionization epoch & beyond via nuclear/accretion, gravitational collapse **CIB**



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..7.. cf. late-time **density web** ~ strain web  **$\ln p \det \mathbf{A} / 3$**

if cold DM  $p/\rho \sim 0 \Rightarrow \zeta(\mathbf{x}, t | cdm)$  is conserved before shell crossing (preheating)

reveals primordial early universe phonons

# $\zeta$ - TOPOGRAPHY & CARTOGRAPHY

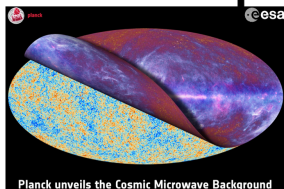
$$\langle \zeta | \text{Temp}, E \text{ pol} \rangle$$

caution: not de-lensed, but the Wiener filter does partially de-lens

Planck 2015 XVII nonG

40 arcmin fwhm

linear map



© esa

Planck unveils the Cosmic Microwave Background

=> infer structure far far earlier scale  $\sim 1/10^{55}$  in 2 numbers

visibility mask

$$\int d \text{visibility}(\text{distance}) \langle \zeta | \text{Temp}, E \text{ pol} \rangle \quad (\text{angles}, \text{distance})$$

Planck's primordial light unveiled

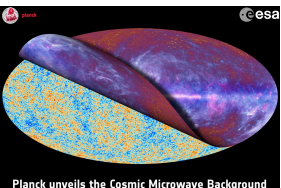
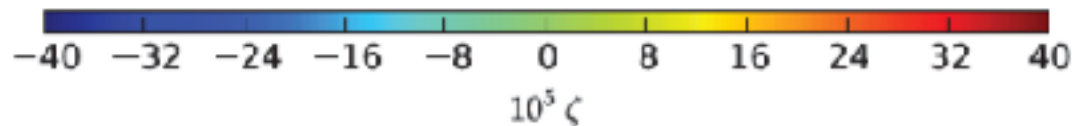
reveals **primordial sound waves** from far earlier times  
=> the inharmonious early Universe '*music of the spheres*'

## Planck's most celebrated findings

=> infer structure far far earlier *scale*  $\sim 1/10^{55}$  **in 2 numbers**

**loudness, bass/treble**  $n_s = 0.968 \pm 0.006$  noise-like *random sound*  
**5.6 $\sigma$  from 1**

we search for a 3rd number, early Universe **gravity waves**  $r (< 0.07)$



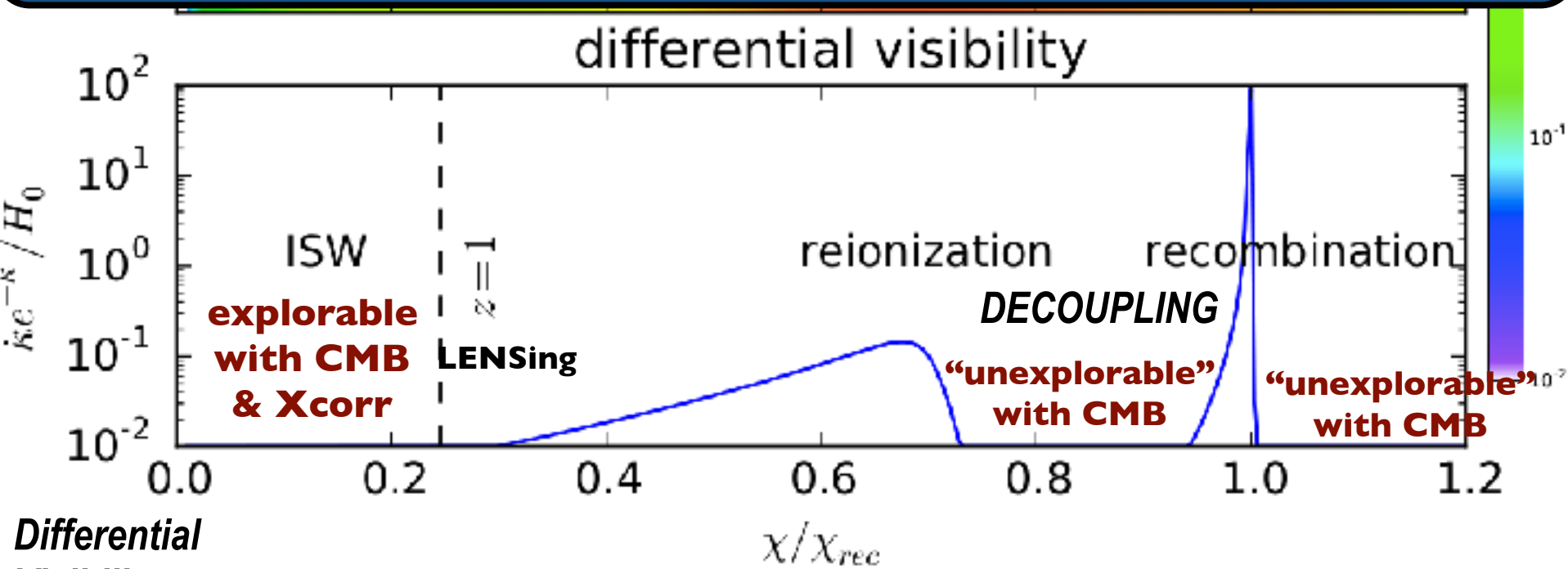
$$\langle \zeta_{LM}(\chi) | T_{LM}^{E_{LM}} \rangle$$

the unexplorable  $\zeta$ -scape,  
 explore with landscape++ ideas  
 our Hubble Bit will reveal all?

**CMB** ~10,000,000 T/E modes of  $\Lambda$ CDM  
 $\lesssim 500$  modes of anomaly  
 $\lesssim 100$  modes reionization history

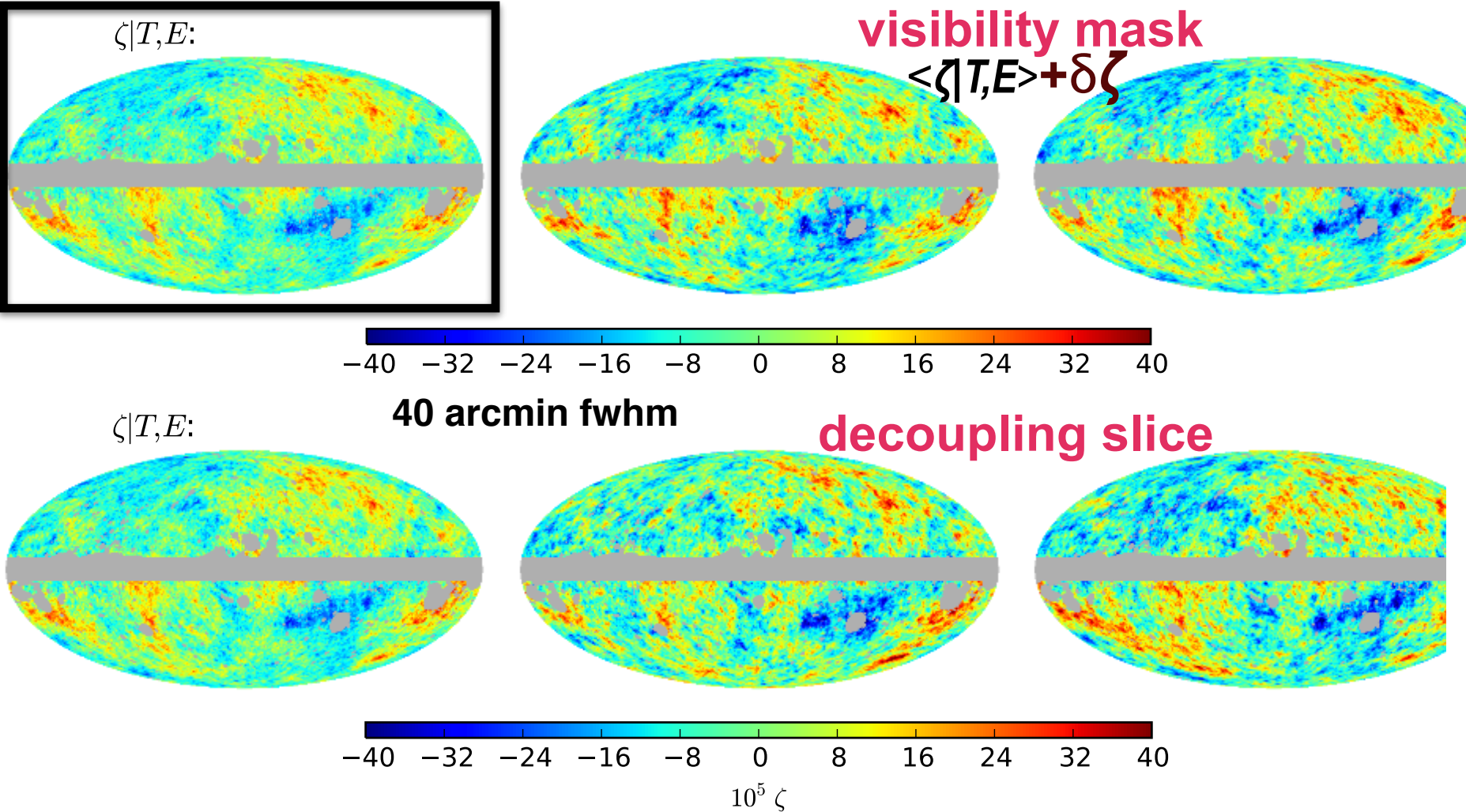
**CMB modes**  
 $\sim f_{\text{sky}} L_{\text{max}}^2$

**LSS**  
 tomography  
 $\propto k_{\text{max}} d_{\text{max}}$



Differential  
 Visibility

limits to our knowledge

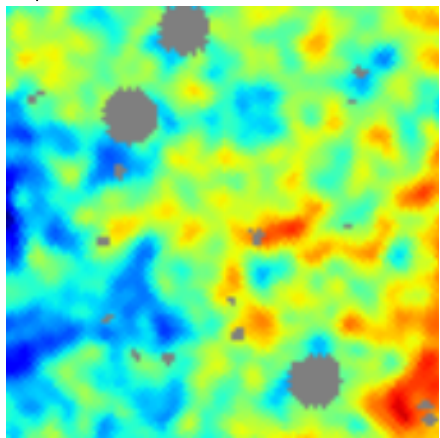


**Maps = (radical) compressions** of the *time ordered information Tol* onto a parameterized space  $q^A$ : *Linear maps, Quadratic maps (power), cosmic parameter maps*

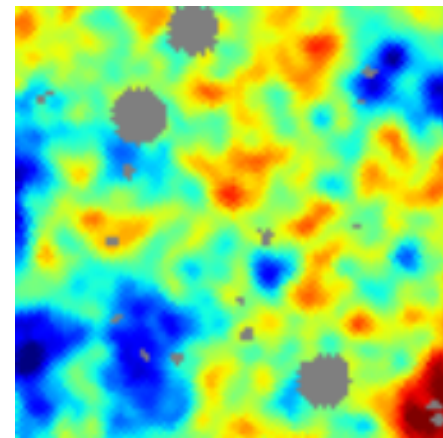
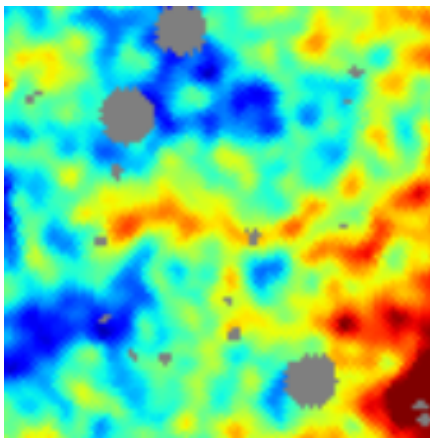
**a Map is an ensemble = mean-map + fluctuation-maps, encoding correlated errors**

**allowed fluctuations are less noisy with T +E-pol (extra mode/LM)**

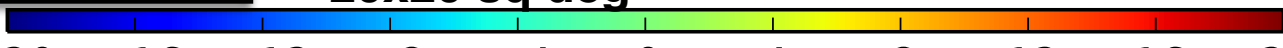
$\zeta|T,E:$



visibility mask

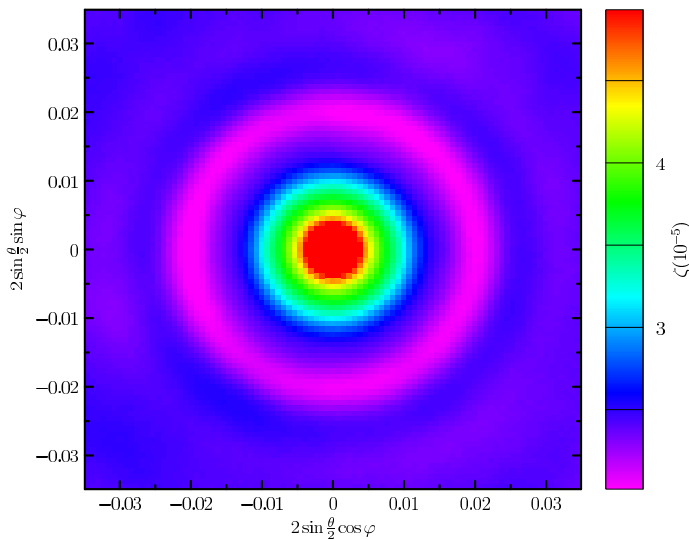


20x20 sq deg

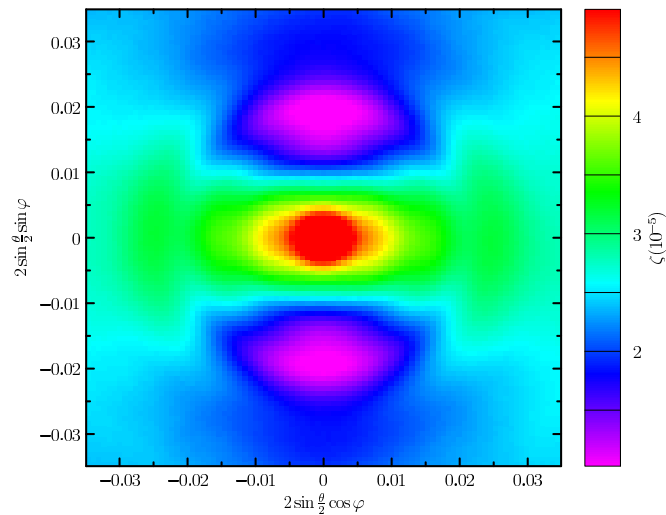


zoom in, higher res: 20 arcmin fwhm

20857 patches on  $\zeta$  maxima, random orientation, threshold  $\nu=0$



20854 patches on  $\zeta$  maxima, oriented, threshold  $\nu=0$



stack to damp fluctuations

$\langle \zeta | \zeta_p k \rangle |_{dv}$

oriented stacks, etc.



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# Dick Bond @ CAP17\_5 Quantum Inflation in the Planck Era & Beyond



*relic1:  $\zeta$  from inflaton - observable = all cosmic structure CMB&LSS & stars/humans etal  
amplitude & slope  $\leftrightarrow$  acceleration history &  $V_{\text{eff}}$  simple over observable range*



*relic2: entropy cooled remnant of particle/field plasma post-inflation  $S_{\text{tot}} = S_{\text{CMB}} + S_{\text{CnuB}}$   
 $10^{88.6}$*

*relic3: baryon asymmetry of matter over antimatter  $N_{\text{baryon}}/S_{\text{tot}}$   
 $10^{-10.06}$*

*relic4: dark matter from quark/gluon plasma - only seen gravitationally WIMPS, axions,..  
 $26.8 \pm 0.9\%$*

*relic5: big bang nucleosynthesis products  $H, He, D, Li$  (influenced by  $C_{\text{nuB}}$ )*

*relic 6: CMB with all its fluctuations & polarization*

*relic 7: galaxies & large scale clustering, flows, gravitational lensing*

*relic 8: dark energy  
 $68.8 \pm 0.9\%$*





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# Dick Bond @ CAP17\_5 Quantum Inflation in the Planck Era & Beyond



what are the degrees of freedom / parameters of the ultra early Universe? TBD

relics not yet seen: in quest of what lies Beyond *the Standard Model of cosmology* SMC

from inflation

*local nonG for  $\Phi_N = G + f_{nl} G^2$   $f_{nl} = 0.8 \pm 5.0$*

non-Gaussian features in  $\zeta$  from weak nonlinearities (*very nearly*) Gaussian random field

gravity waves (not so far - obscured by dust)

*P15+BKP  $r < 0.09$  uniform  $n_s$*

isocon relic (not so far) - Planck on CDM isocurvature, neutrino, correlated

*cf.  $0 < r < 0.11$  95% CL P15+BKP 12 knots*

bubble remnants of tunneling during inflation

*< 2% isocurvature role*

from heating

isocon memories (not so far)

strong subdominant but intermittent nonlinearities in  $\zeta$  (spikes via chaotic billiards)

curvatons oscillons strings domain walls - short lived

rare WIMPzillas as dark matter

from later quark gluon plasma

late phase transitions

*anomalies in CMB & LSS*

could be *primordial. large-scale, intermittent? statistics of just a few (modes, spatial rare events)?*

# Beyond the Standard Model of cosmology? $\text{SMc} = \text{tilted } \Lambda\text{CDM} + r (\zeta, h_{+x})$

## BSMc = SMc + primordial anomalies

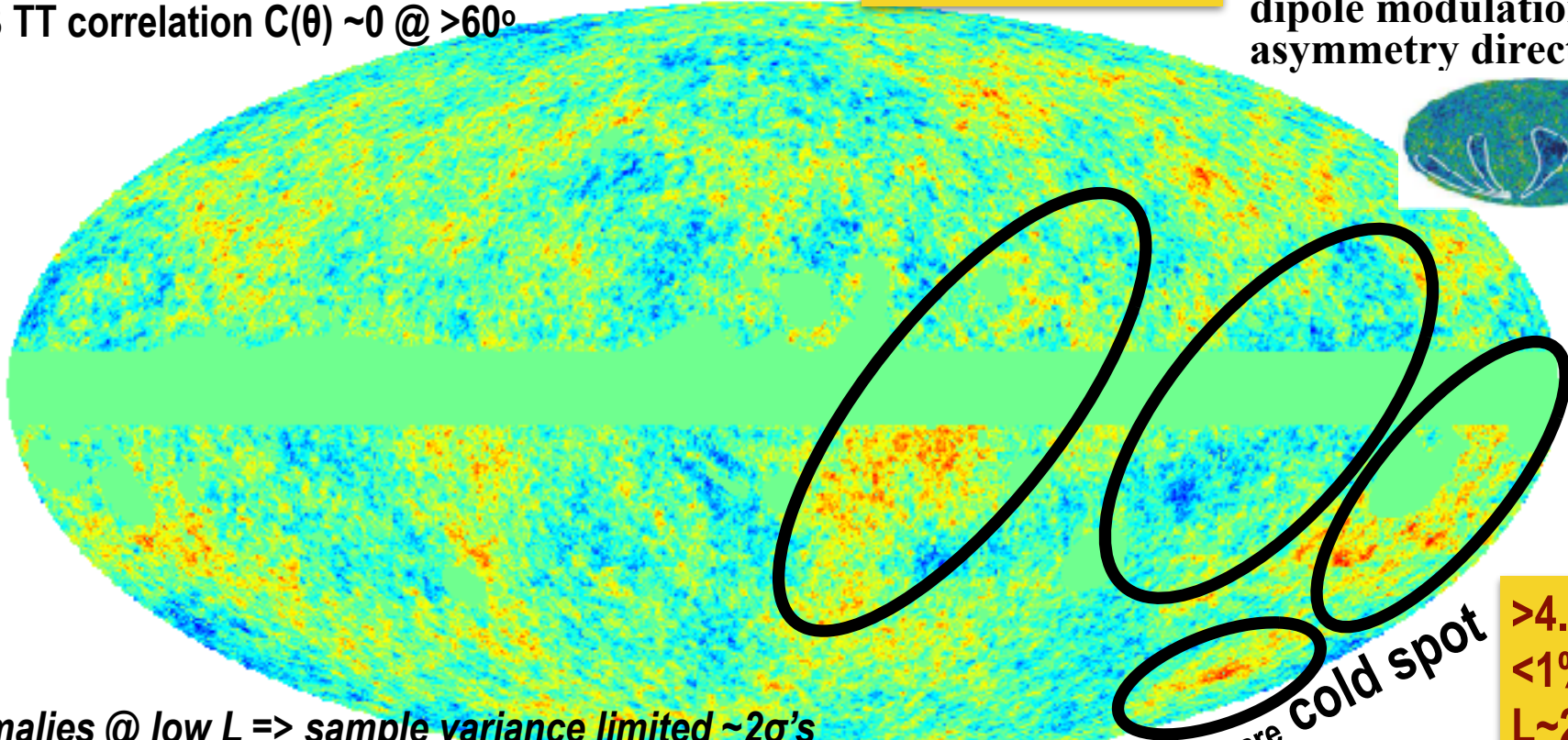
std nonG  $\zeta = \zeta_G + f_{\text{NL}} * (\zeta_G^2 - \langle \zeta_G^2 \rangle)$  local & equilateral pattern & orthogonal  
 non-std nonG  $\zeta = \zeta_{\text{inflaton}} + \text{uncorrelated } \zeta_{\text{[GRF]}}$  modulated heating intermittent

$f_{\text{NL}} = -0.52 \pm 3.0$  for  $\zeta$

CMB TT power  $L \sim 20-30$  dip  $\Rightarrow \zeta$ -Spectrum k-dip  
 hemisphere difference  $\sim 7\%$  at low resolution  
 CMB TT correlation  $C(\theta) \sim 0$  @  $>60^\circ$

$\langle \zeta | T, E\text{-pol} \rangle$

octupole/quadrupole alignment  
 dipole modulation/  
 asymmetry direction



anomalies @ low  $L \Rightarrow$  sample variance limited  $\sim 2\sigma$ 's  
 GUTA = Grand Unified Theory of Anomalies? if then maybe  $\gg 2\sigma$ ? TBD

the rare cold spot

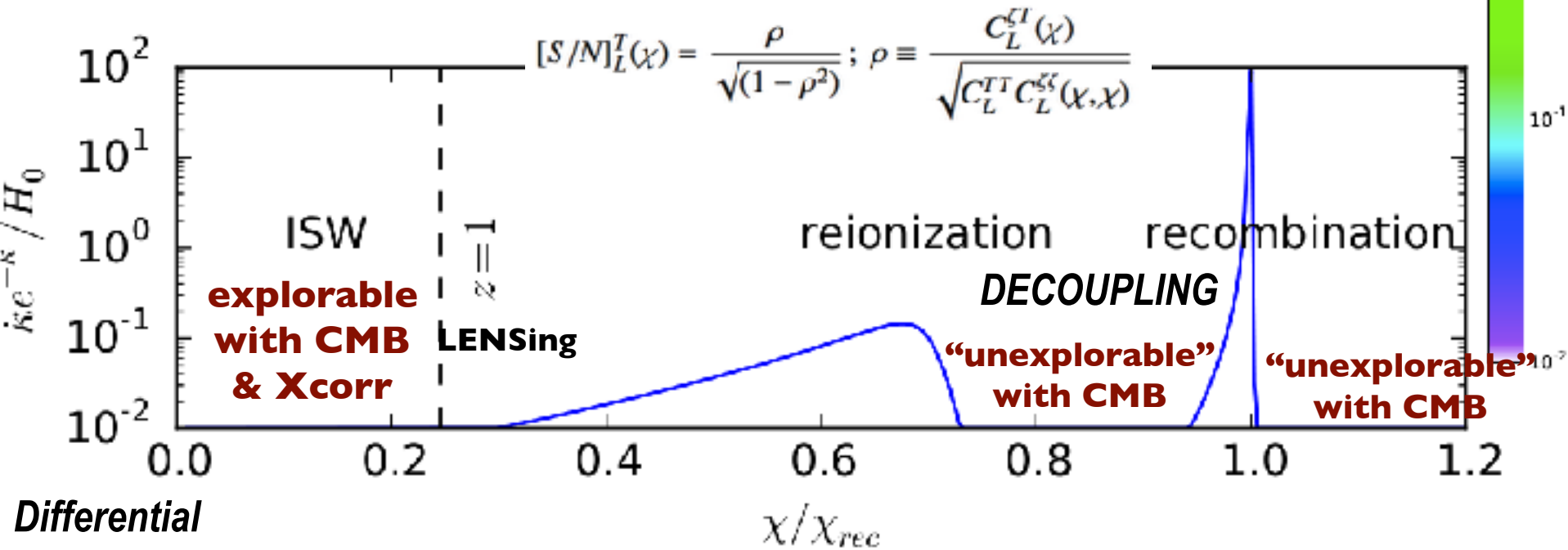
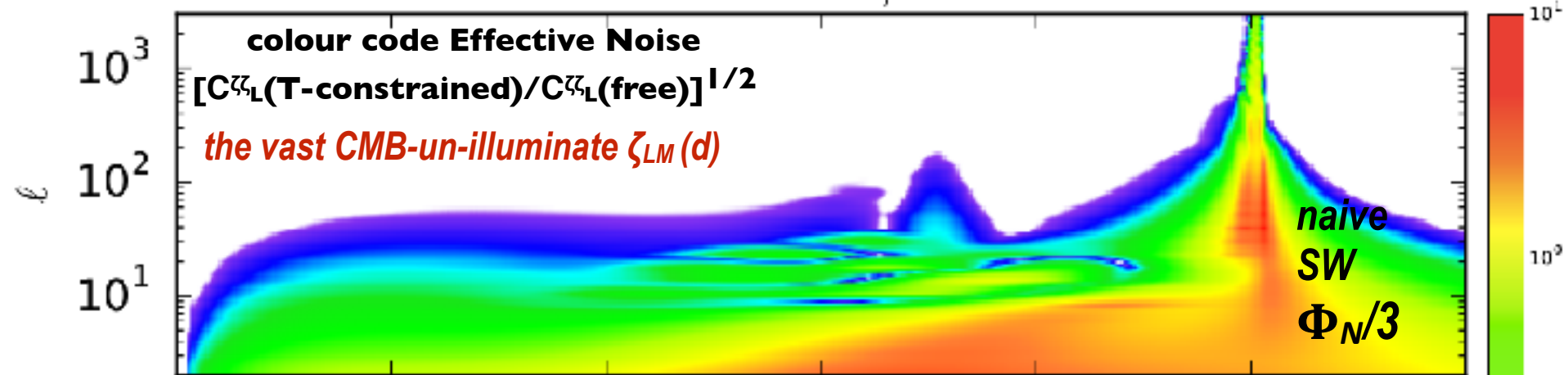
$>4.5\sigma$   
 $<1\%$   
 $L \sim 20$   
 LSS  
 void?



$$\langle \zeta_{LM}(\chi) | T_{LM}^{E_{LM}} \rangle$$

**the unexplorable  $\zeta$ -scape,**  
**explore with landscape++ ideas**  
*our Hubble Bit will reveal all?*

T + E S/N

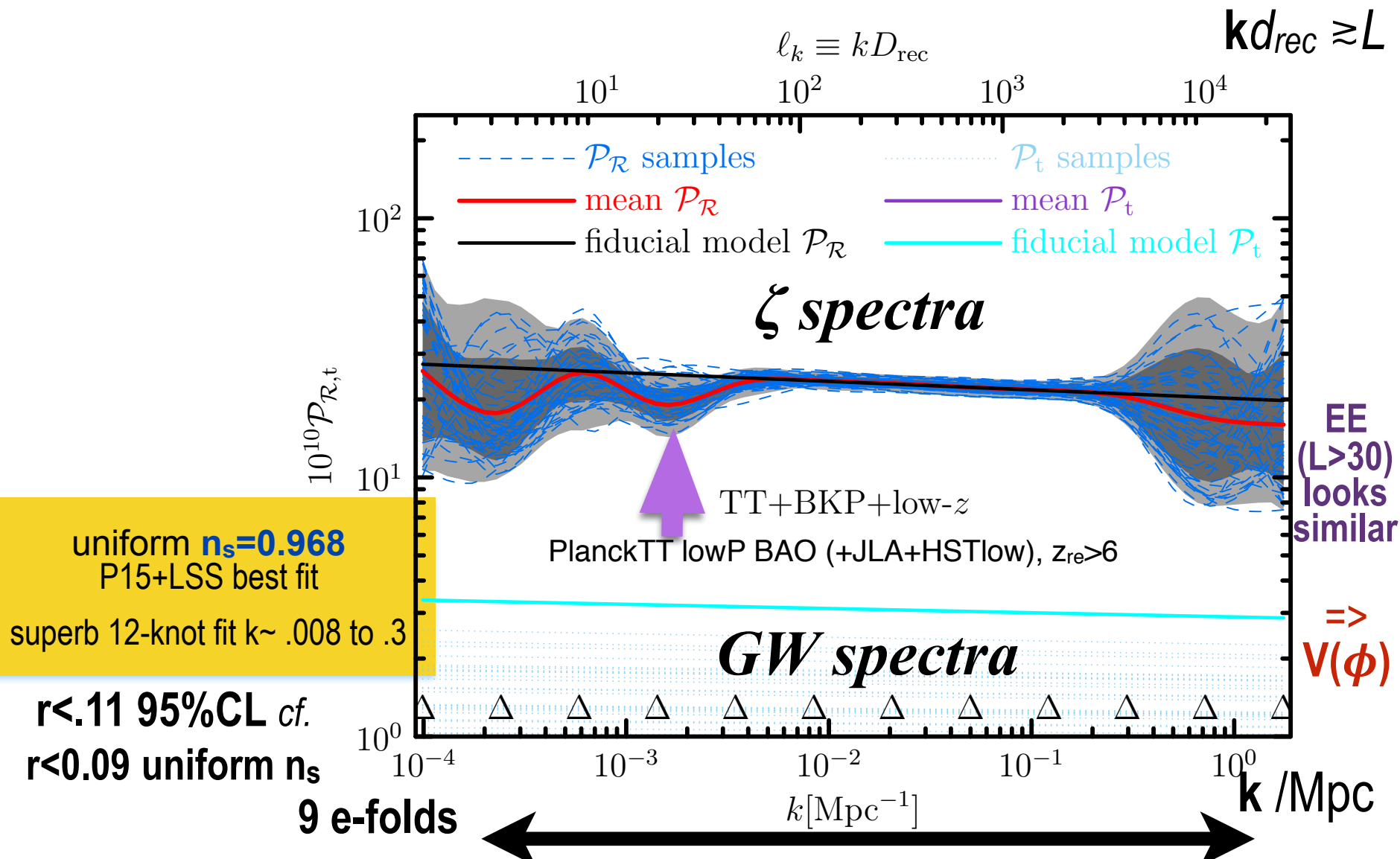


**limits to our knowledge**

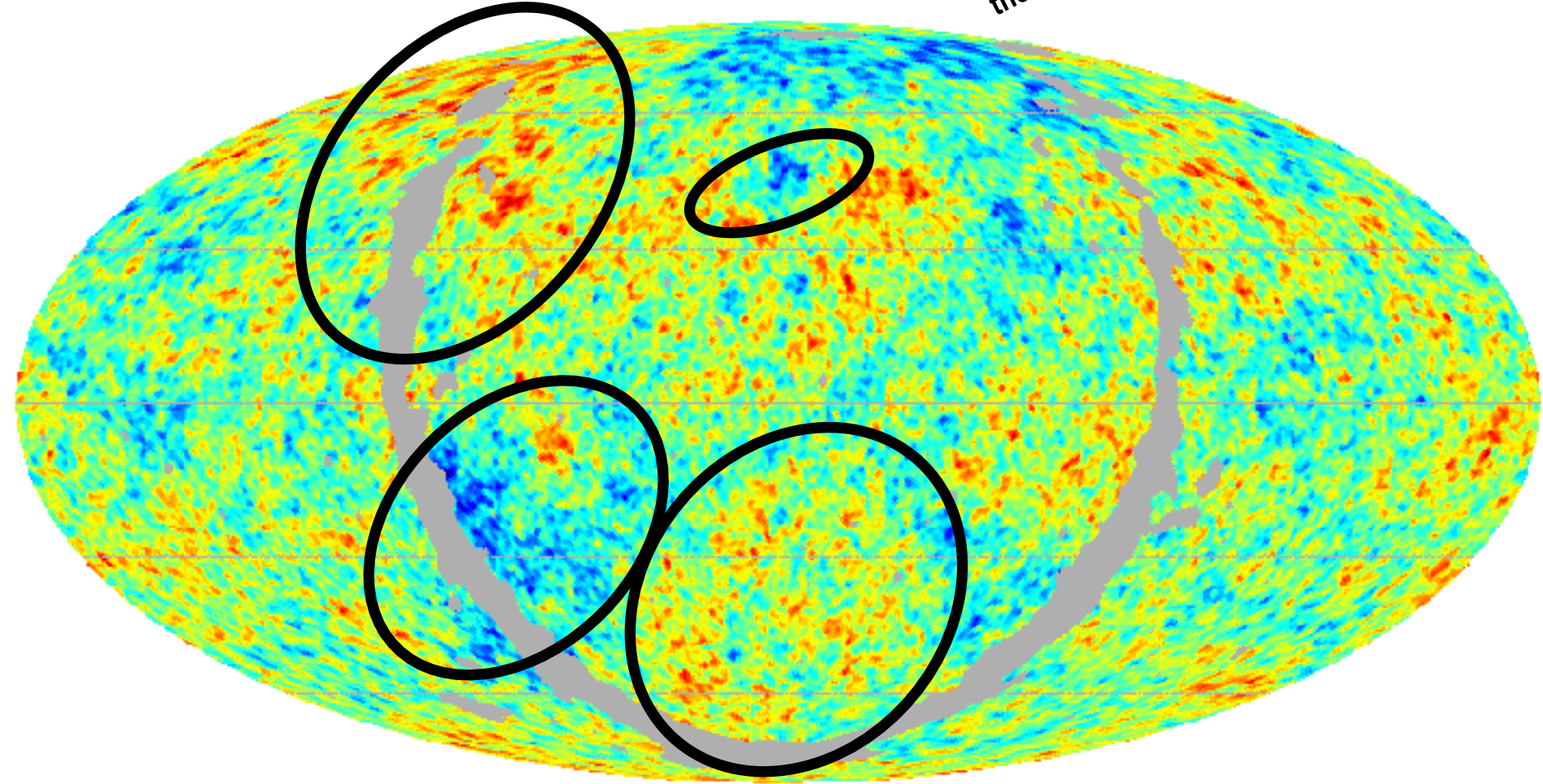
# quadratic map of the $\zeta$ -scape

Planck 2015 XX inflation

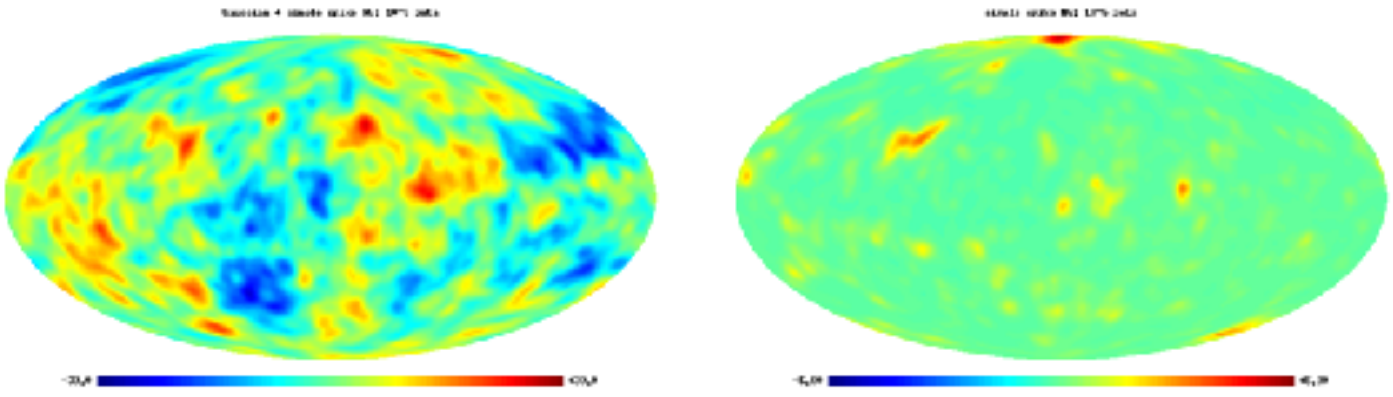
CMB TT power  $L \sim 20-30$  dip  $\Rightarrow$   $\zeta$ -Spectrum k-dip; includes CMB lensing, parameter marginalization



the rare cold spot

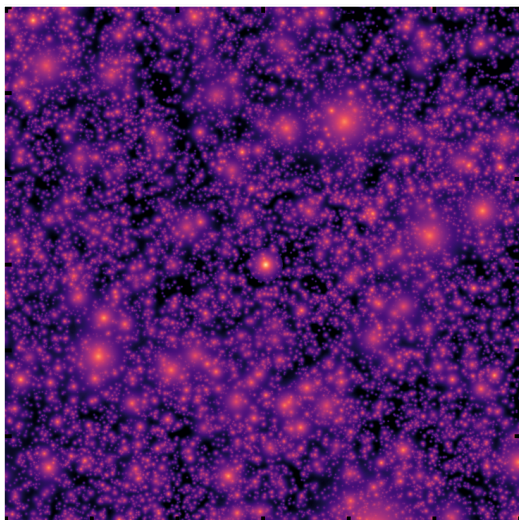


**CMB+LSS mocks to test: standard Gaussian inflaton  $\zeta_{inf}$ + subdominant uncorrelated  $\zeta_{isoc}$**   
 e.g., from modulated preheating by isocons



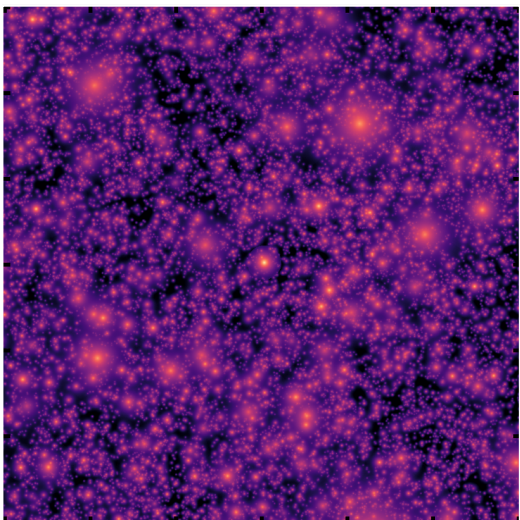
*uncorrelated nonG 'wide open' cf. usual correlated highly constrained nonG*

LSS tSZ: Gaussian std



*B2FH, b+braden+frolov+huang*

LSS tSZ: Gaussian std + subdominant uncorrelated  $\zeta$

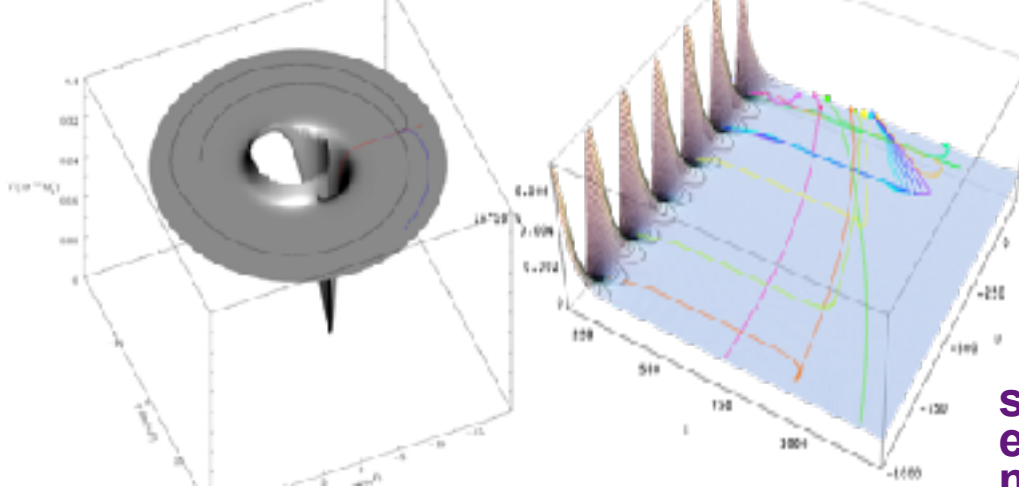


*ABSB+FH, alvarez+b+stein+frolov+huang*

single field  $V$  heating slow, oscillating  
 but shaped  $V$  can give rapid heating (roulette)

Barnaby, Bond, Huang, Kofman 09

coarse-grain cm-horizon  
 $\Rightarrow$  fine-grain fluctuations  
 =  $S$  generation



quantum  
 diffusion  
 spatial jitter  
 drift

$E_{ol}$  ★

★ let there be  
 heat

roulette oscillations  
 highly damped  
 $\Rightarrow$  no-non-G  
 if redirect by  $\chi_{cg, eoi}$ ,  $g$   
 $\Rightarrow$  non-G??

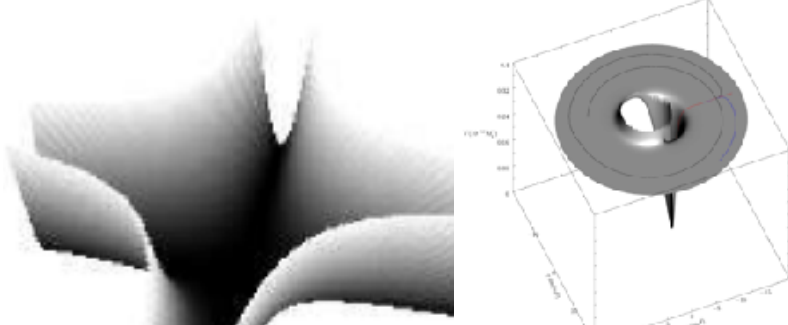
$E_{ol}$  horizon  $\sim$  1cm comoving

SEMANTIC SLATS

# what is the inflaton's potential?

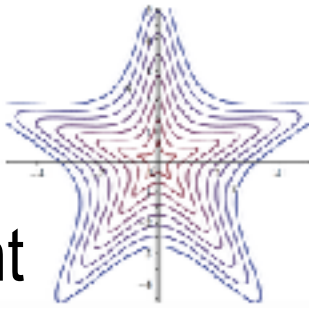
around a minimum is the **HOT /heating question**

2 filament?



4 filament

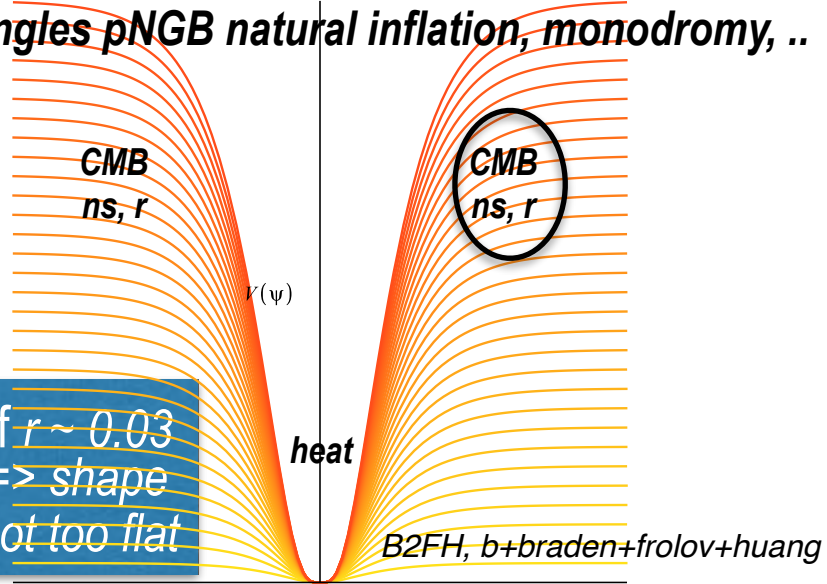
$$1/4\lambda\phi^4 + 1/2g^2\phi^2\chi^2$$



3-filament

5-filament

angles  $p$ NGB natural inflation, monodromy, ..



conformal potential-flattening eg Higgs inflation SBB89 etc

how was *matter & entropy* generated at the end of acceleration = inflation?

Relate to Higgs & standard model?

Preheating After Roulette Inflation

$$\langle \tau \rangle =$$

quantum diffusion spatial jitter

drift

$$\ln a(\mathbf{x}, \ln H)$$

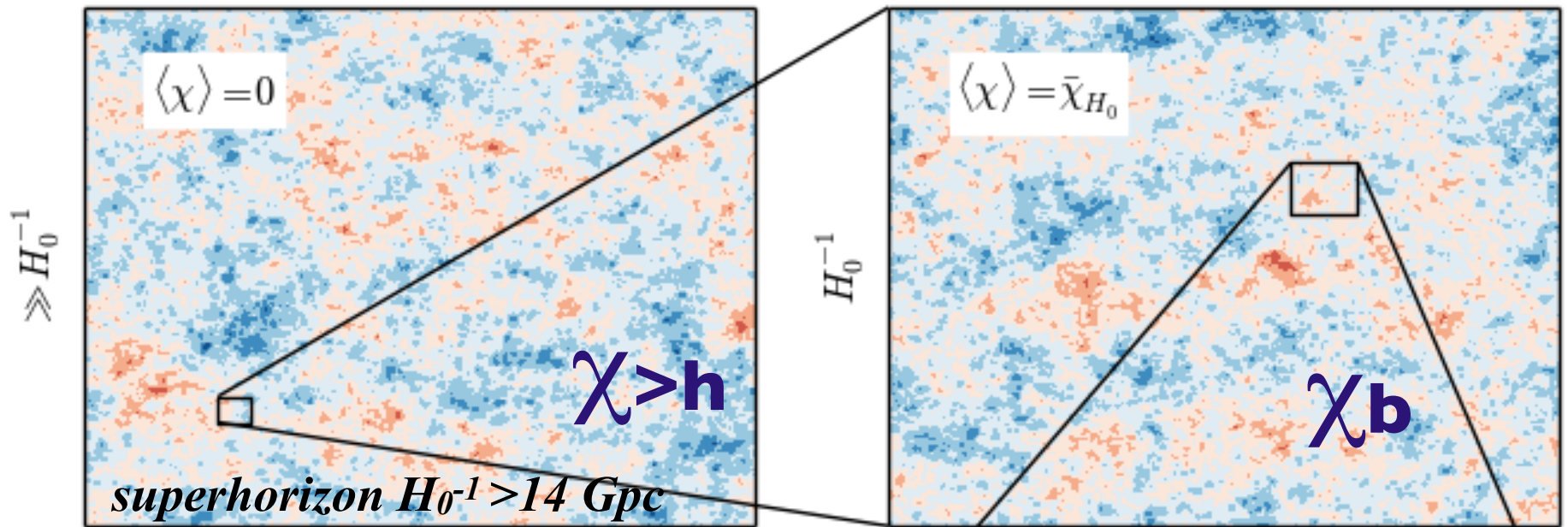
entropy generation in preheating from the coherent inflaton (origin of all matter)

let there be heat

isocon directions, e.g., axion

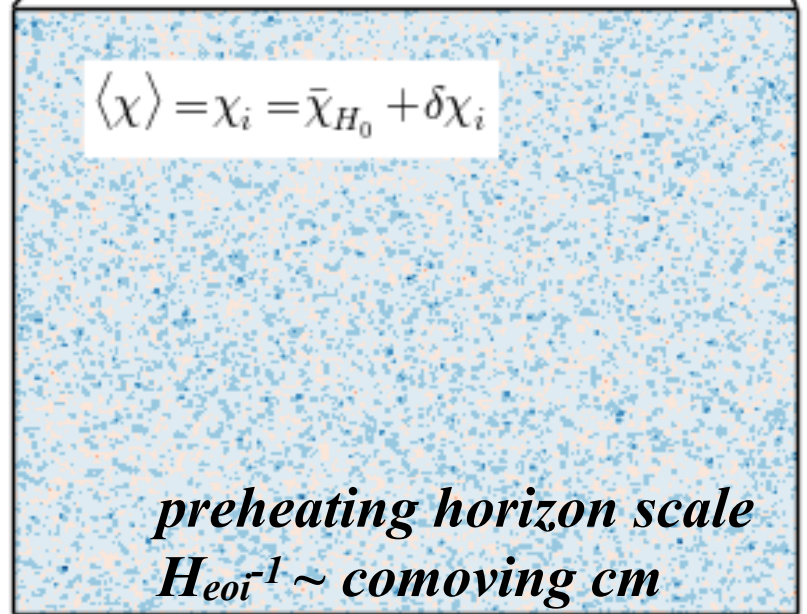
S-E-M-I-N-E-R-N-A-L I-N-F-L-A-T-I-O-N





ULSS modulation beyond our Hubble patch

LSS modulation within our Hubble patch



$\zeta (\chi_{\text{cg,eoi}}(\mathbf{x}) | g^2/\lambda)$

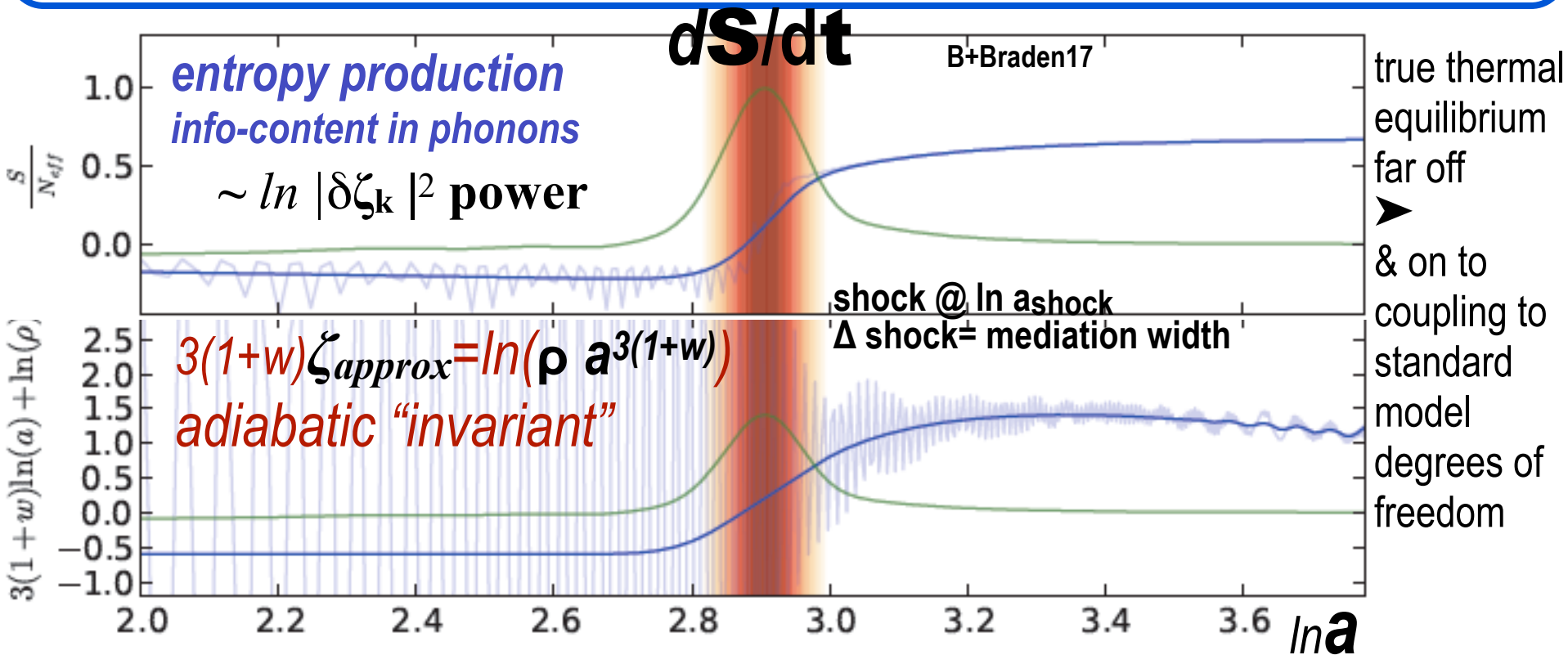
$\Rightarrow$  NonG cold spots ++

the complex preheating cm is modulated by a large scale Gaussian field

quartic inflaton  $V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$

*log-normal pdf (density aka  $\zeta$ ), in  $k$ -bands too; normal pdf (velocity)*

# nonG from large-scale modulations of the shock-in-times of preheating



coarse-grain  $\langle \zeta \rangle \Leftrightarrow$  fine-grain  $\delta\zeta_{\mathbf{k}}$  gradients,  $\delta V$

$$\zeta_{\text{final}}(\mathbf{x}, t_f | \chi_{\text{cg, eoi}}(\mathbf{x}), g^2/\lambda) \sim \zeta_{\text{shock}}$$

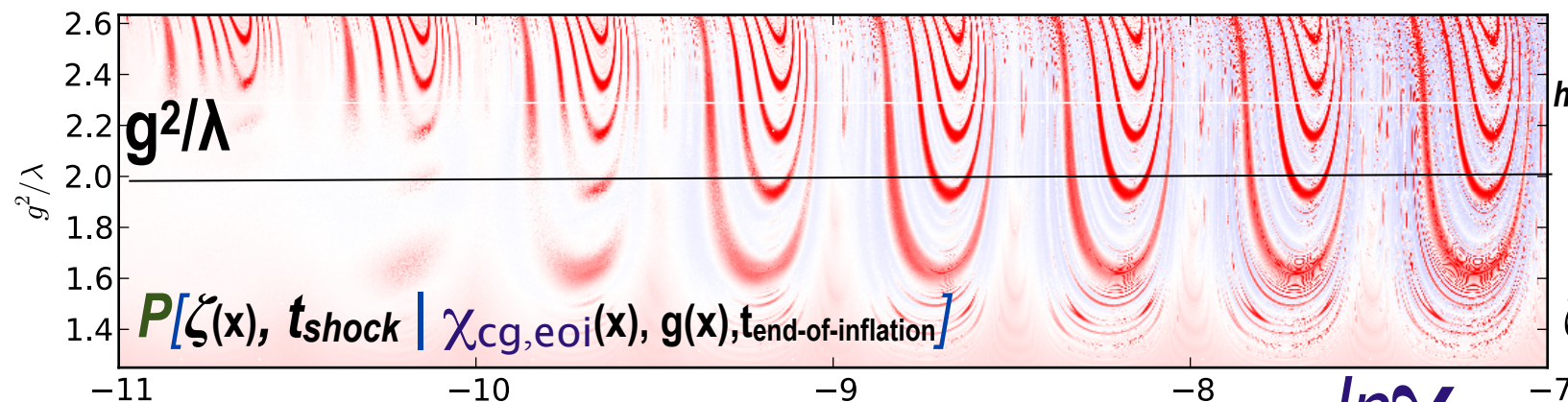
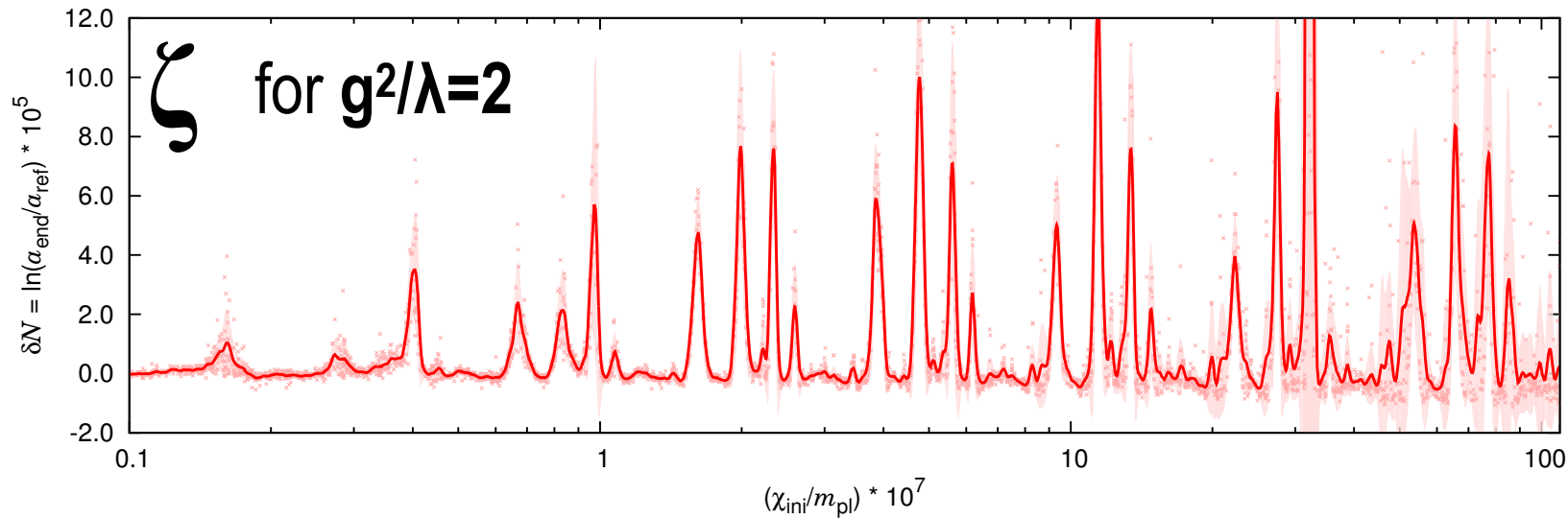
$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

$dS/dt(t, g) \Rightarrow$  the Shock-in-time: entropy production rate

$\zeta_{\text{shock}}(\chi_{\text{cg, eoi}}(x) | g^2/\lambda) \Rightarrow$  Chaotic Billiards: NonG from Parametric Resonance in Preheating

B+Frolov, Huang, Kofman 09  
B+Braden, Frolov, Huang 17

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



computational tour de force

huge number of  $64^3$  sims to show the wondrous complexity of

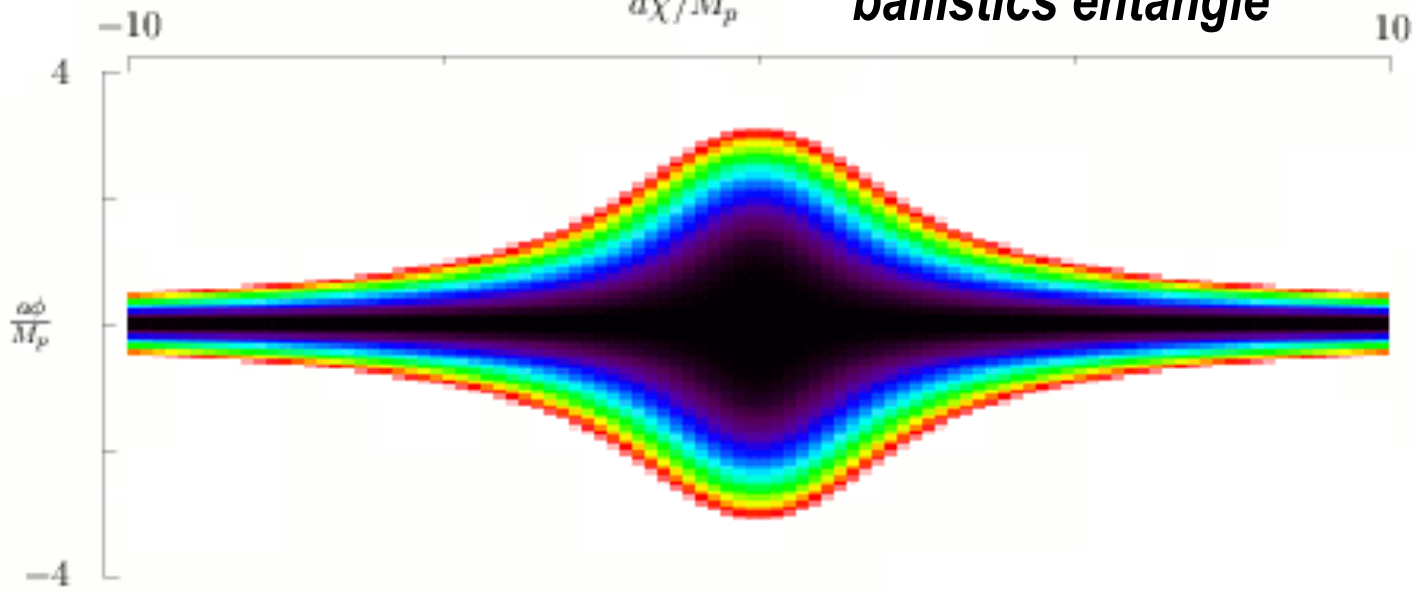
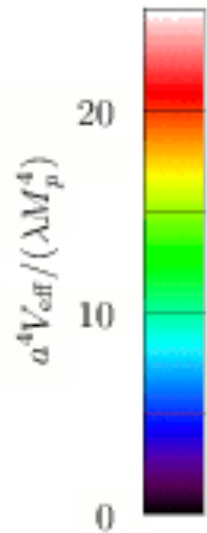
gigafigure of lattice simulations

$\ln \chi_{\text{cg, eoi}}$

full lattice simulations of coarse-grained  $k \sim 0$  trajectories ( $\chi_{\text{cg,eoi}}$ )

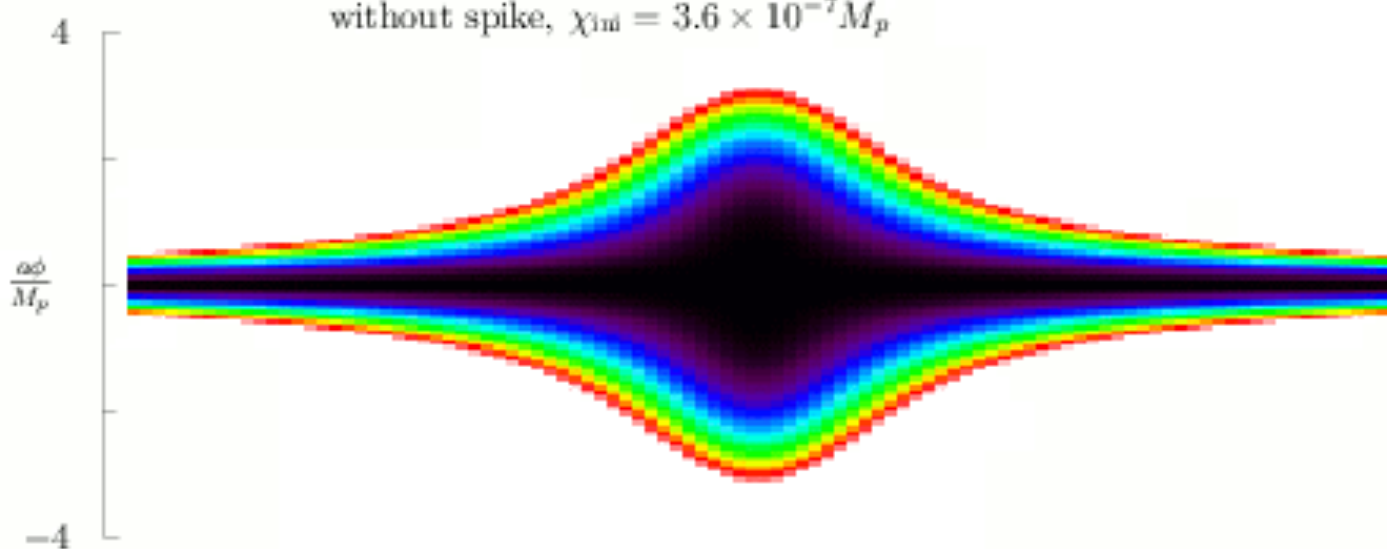
$a\chi/M_p$

ballistics entangle



without spike,  $\chi_{\text{int}} = 3.6 \times 10^{-7} M_p$

$a =$



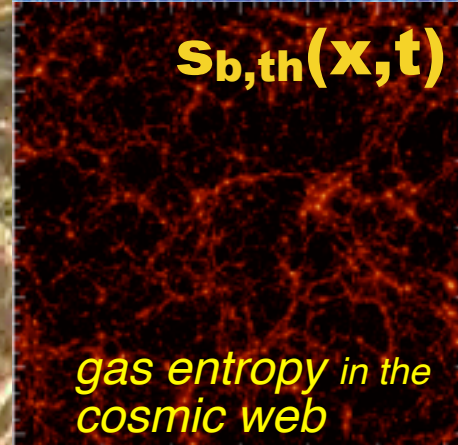
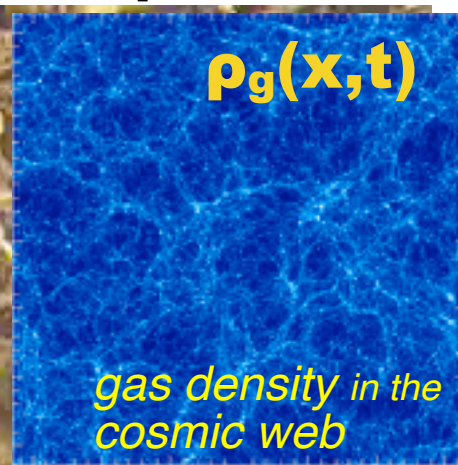
with spike,  $\chi_{\text{int}} = 3.9 \times 10^{-7} M_p$

**(nonlinear)  $V_{\text{eff}}$  is trajectory-bundle dependent**

$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$

# caustics are ubiquitous: LSS/cosmic web & preheating

Andrei Frolov movie in Banff B2FH

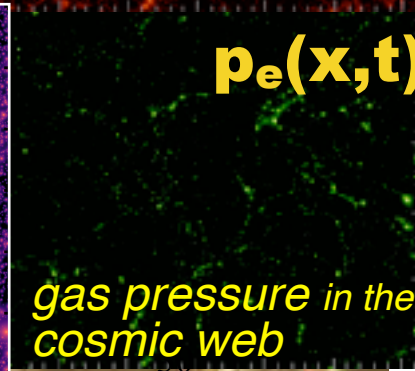
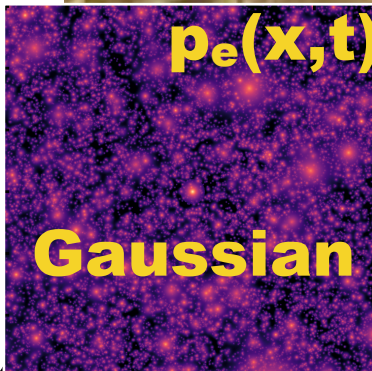
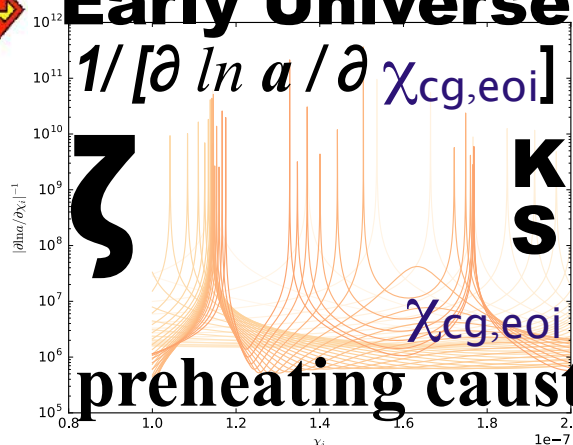


$\zeta_{dm}$   cf.  $\int \mathbf{K} \mathbf{S}_{dm}$

gas entropy in the cosmic web

gas entropy in the cosmic web

## Early Universe



gas pressure in the cosmic web

*cm-scale* **coarse-grained**  $k \sim 0$

**“ballistic” trajectories**

*become* **entangled** *with fluctuations*

*aka sub-cm* **k-modes** *in a coarse-grained*

*non-equilibrium-***entropy***-generating*

**shock-in-time**

*& on to the quark/gluon plasma* **StandardModel-pp**

$\delta\zeta_{\mathbf{k}}$  &  $\ln[\rho/\langle\rho\rangle]_{\mathbf{k}}$  are nearly Gaussian within a preheating horizon:

*shown by B+Braden17 lattice simulations for probability distribution functions in k-bands, and smallness of the 3 pt, etc. (!!!)*

# caustics in $\langle q^A \rangle$ ballistic orbits

$$\langle \delta q^A t_2 \mid \delta q^B t_1 \rangle \sim \exp(\mathcal{E}(t_2 \mid t_1)) \langle \delta q^A t_1 \mid \delta q^B t_1 \rangle$$

early U parameters: **final**  $\varphi, \Pi_\varphi, \chi, \Pi_\chi, \ln a, \ln \rho$ , **initial**  $\chi_{cg, eoi}$ , *couplings*  $g, \lambda, \dots$

parameter strain tensor  $\mathcal{E}(t_2 \mid t_1)$

**$d\mathcal{E}/dt$**  strain rate  $\sim$  local Lyapunov coefficients *Floquet instability charts*  
instability to have nearby parameters diverge  $\Rightarrow$  chaotic billiards  
**Kolmogorov-Sinai entropy**:  $\sim$  Sum of positive values of  $d\mathcal{E}/dt$

small  $\mathcal{E}$  eigenvalues  $\Rightarrow$  coherent trajectory bundles (for a time)

= caustics (inverse  $\rightarrow \infty$ )  $1/[\partial \zeta / \partial \chi_{cg, eoi}]$ ;  $\Rightarrow$  peaks in  $\zeta(\chi_{cg, eoi})$

stopping time **tstop** ( $\chi_{cg, eoi}$ ) when  $\mathcal{E}$  values get large  $\Leftrightarrow$  local gradients  $\uparrow\uparrow$

cf. LargeScaleStructure: final Eulerian position  $\Leftarrow$  initial Lagrangian position

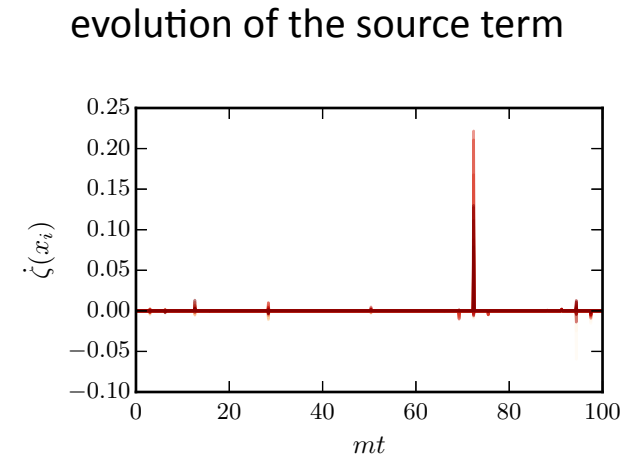
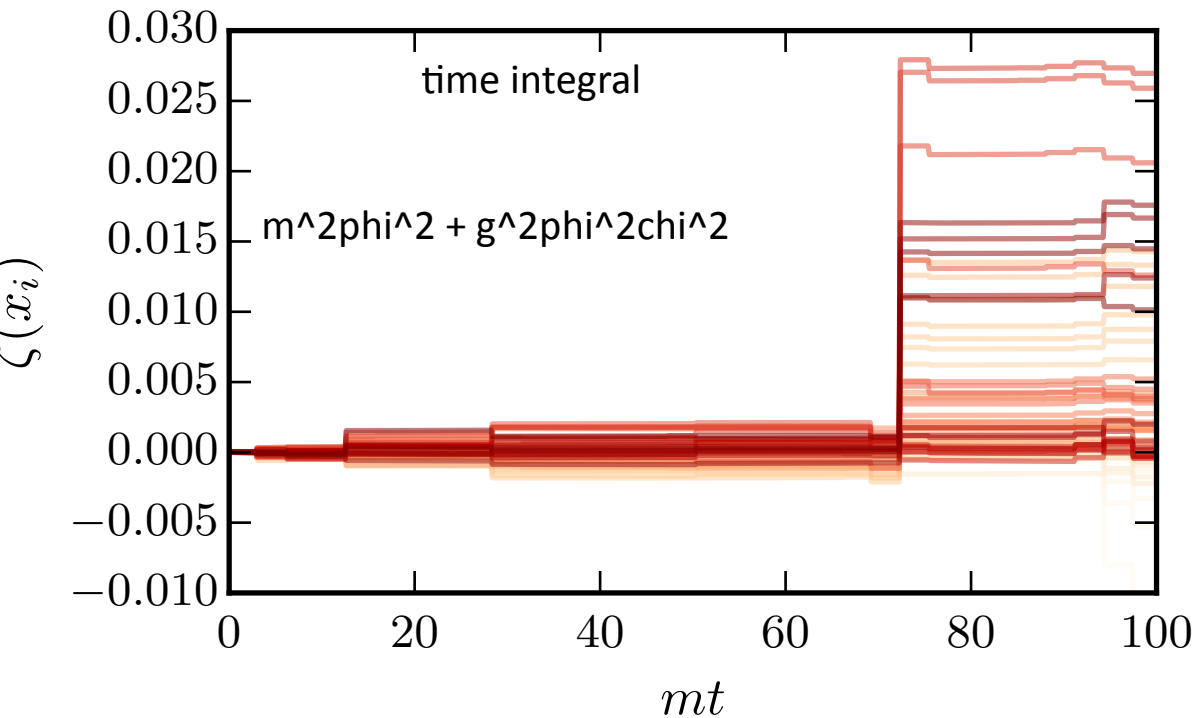
1LPT aka Zeldovich:  $\partial x / \partial r = \exp(\mathcal{E}) \rightarrow 0$  density  $\rho \sim \exp(-\text{Tr}(\mathcal{E})) \rightarrow \infty$



zeta conserved along trajectories until the “shock-in-time” when high k fluctuations (fine-grain) develop from coarse-grain, measure is  $\ln \rho \sqrt{g}$

but  $D \ln \rho = \text{Trace } \bar{d} \epsilon$  does change, KS entropy

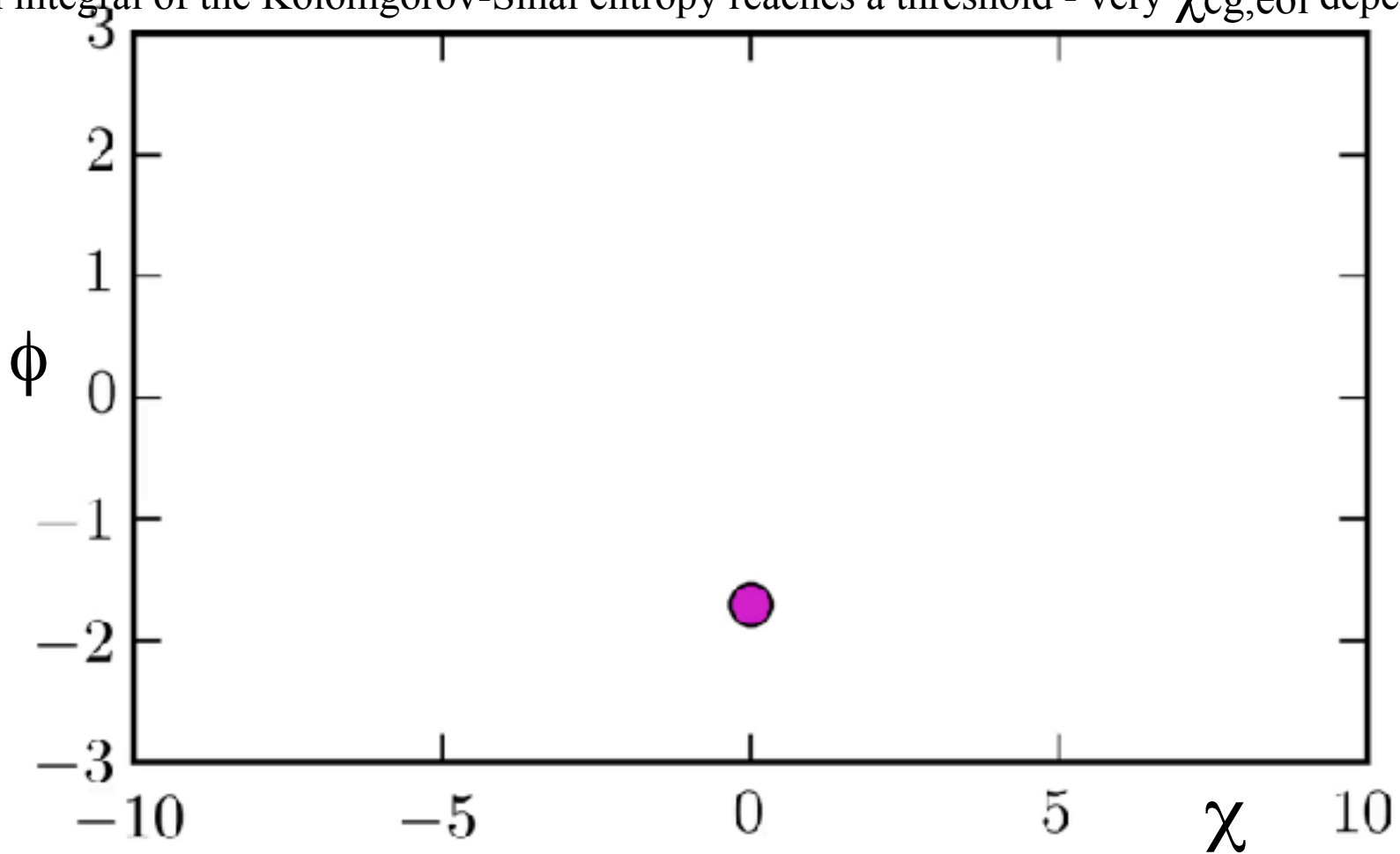
stretching of phase strings. begin with anisotropic Gaussian at EoI and watch it stretch,  $\epsilon$  grows, rotates, locally OK as distorted ellipsoid, but strain depends upon the central value  $\Rightarrow$  phase tubes



# ballistic billiards $k=0$ mode **phase space string** evolution

2D constrained distribution functions

**stopping criterion** when coarse-grained entropy of field variables rises  $\Leftrightarrow$  strain  $\mathcal{E}$  high,  
*ie* when integral of the Kolomgorov-Sinai entropy reaches a threshold - very  $\chi_{cg, eoi}$  dependent



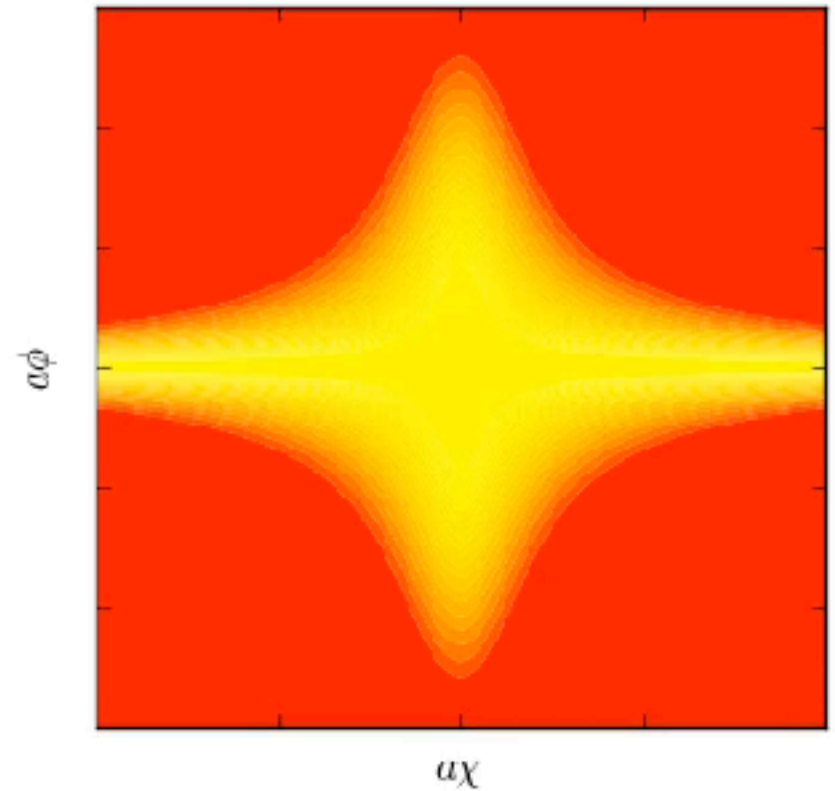
$$V = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



# phase space strings

2D constrained distribution functions

caustics are ubiquitous

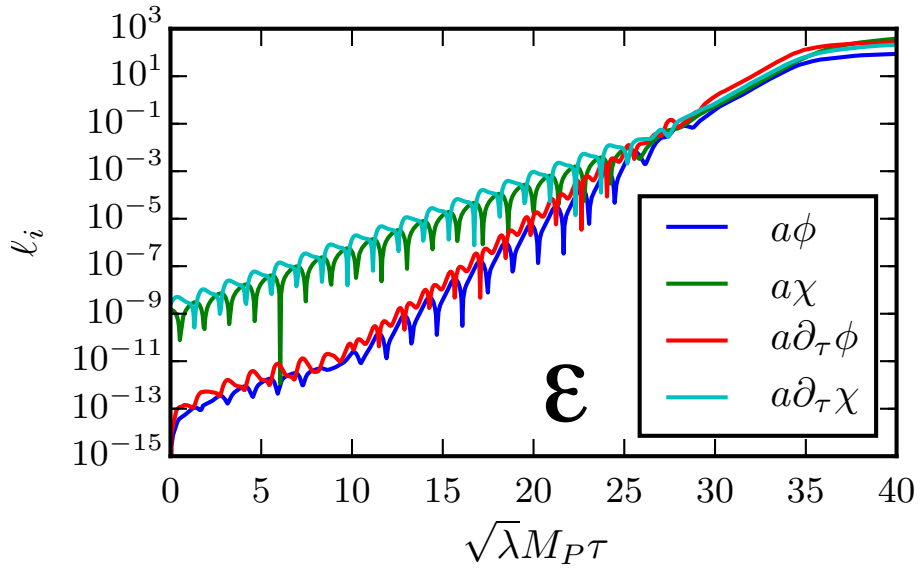


*B2FH, b+braden+frolov+huang*

# phase space strings

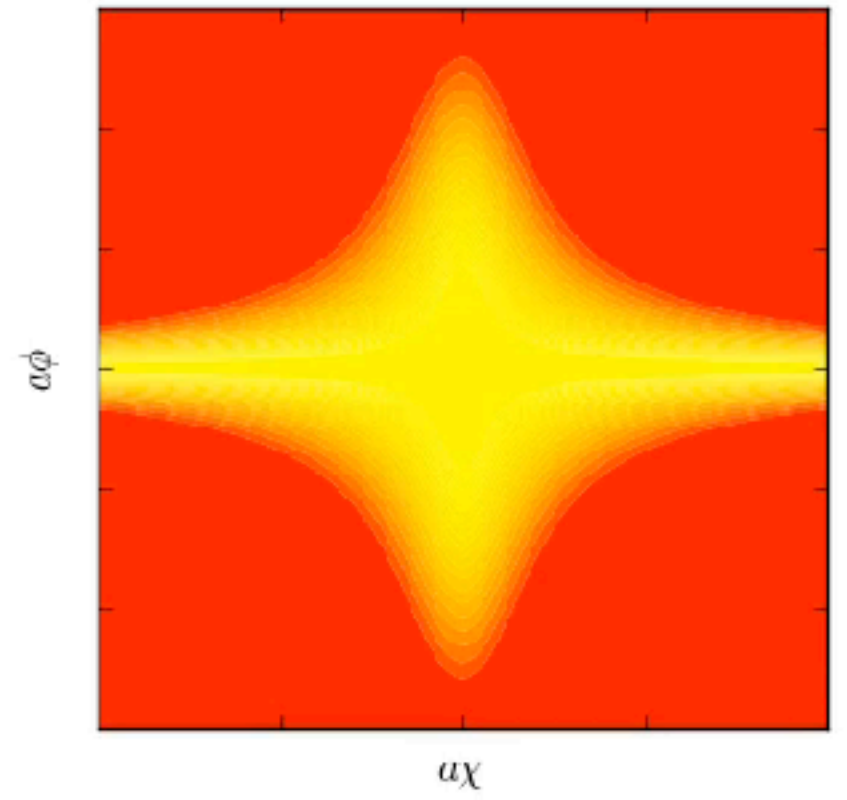
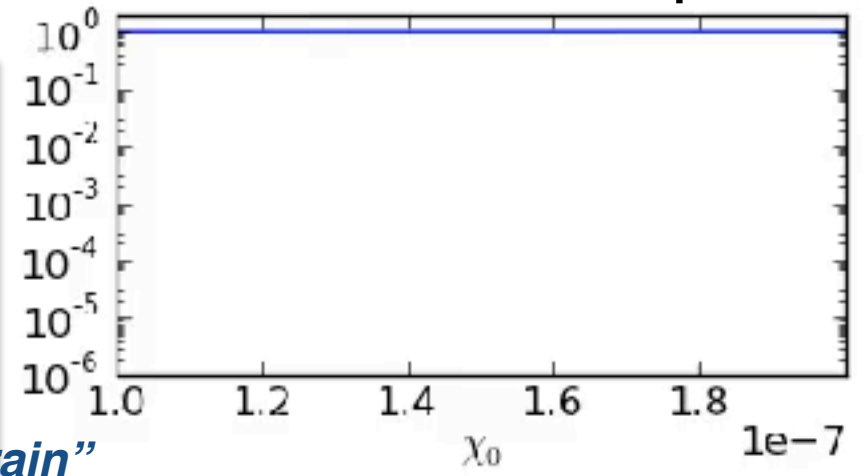
2D constrained distribution functions

*phase string growth in time “parameter strain”  
integral of Kolmogorov-Sinai entropy*

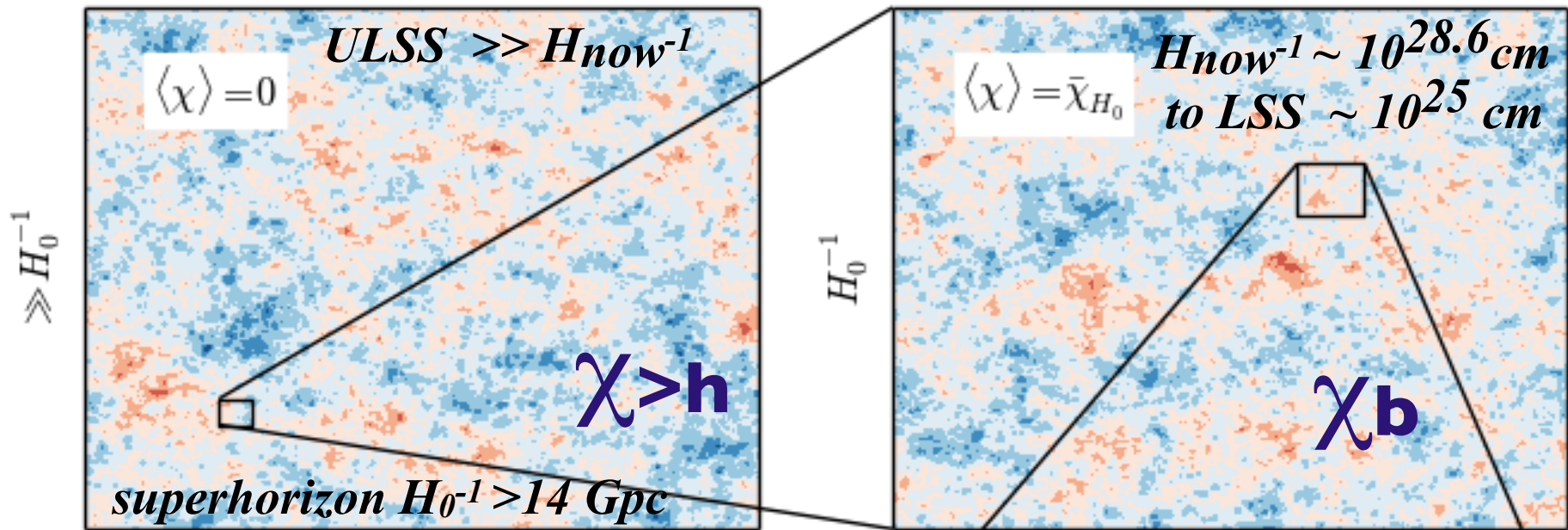


=> 3D constrained distribution functions

# caustics are ubiquitous



B2FH, b+braden+frolov+huang

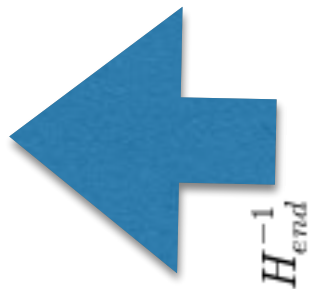


*ULSS modulation beyond our Hubble patch  
threading the patches together to make LSS*

*LSS modulation within our Hubble patch*

$$\zeta (\chi_{cg, eoi}(\mathbf{x}) | g^2/\lambda)$$

*=> NonG cold spots ++*



*the complex preheating cm is modulated  
by a large scale Gaussian field*

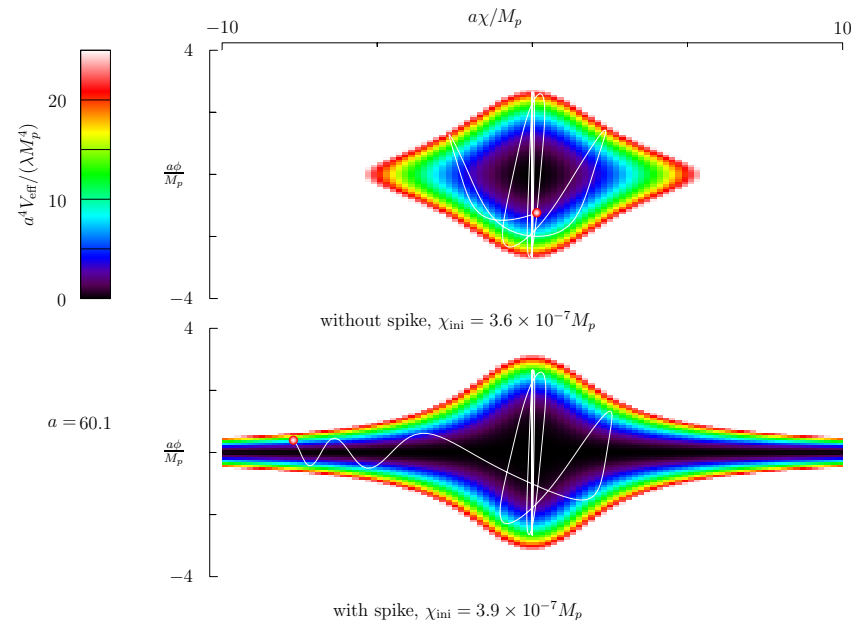
*understanding the  $\zeta$ -spike structure,* *B<sup>2</sup>FH 17*

*qualitatively YES quantitatively in Progress*

**arresting the orbits via a  
shock-in-time, incoherent  
cf. coherent (caustic)  
trajectory bundles**

*incoherent*

*coherent*



**how generic will caustic  
preheating be? structure  
around potential minima:  
=> 'filamentary' potentials**

**=> ballistic flow channels**

*multi-filaments may lead to caustics  
2 std inflaton, slow heating? roulette  $V$  is fast. 3-star*

*4 case workhorse. the 5-star... 'axionic' angles  
works with conformal flattening of  $V(\phi_A) \mp$*

*cf. filaments that join at clusters in the LSS web*

**how modulated caustics in  
preheating could give  
observable intermittency**

**via isocon power on large  
& super-horizon scales**

*=> light particles* ( $\chi_{eoi}(x)$ , couplings  $g(x)$ , ...)

***these isocons are active, NOT spectators***



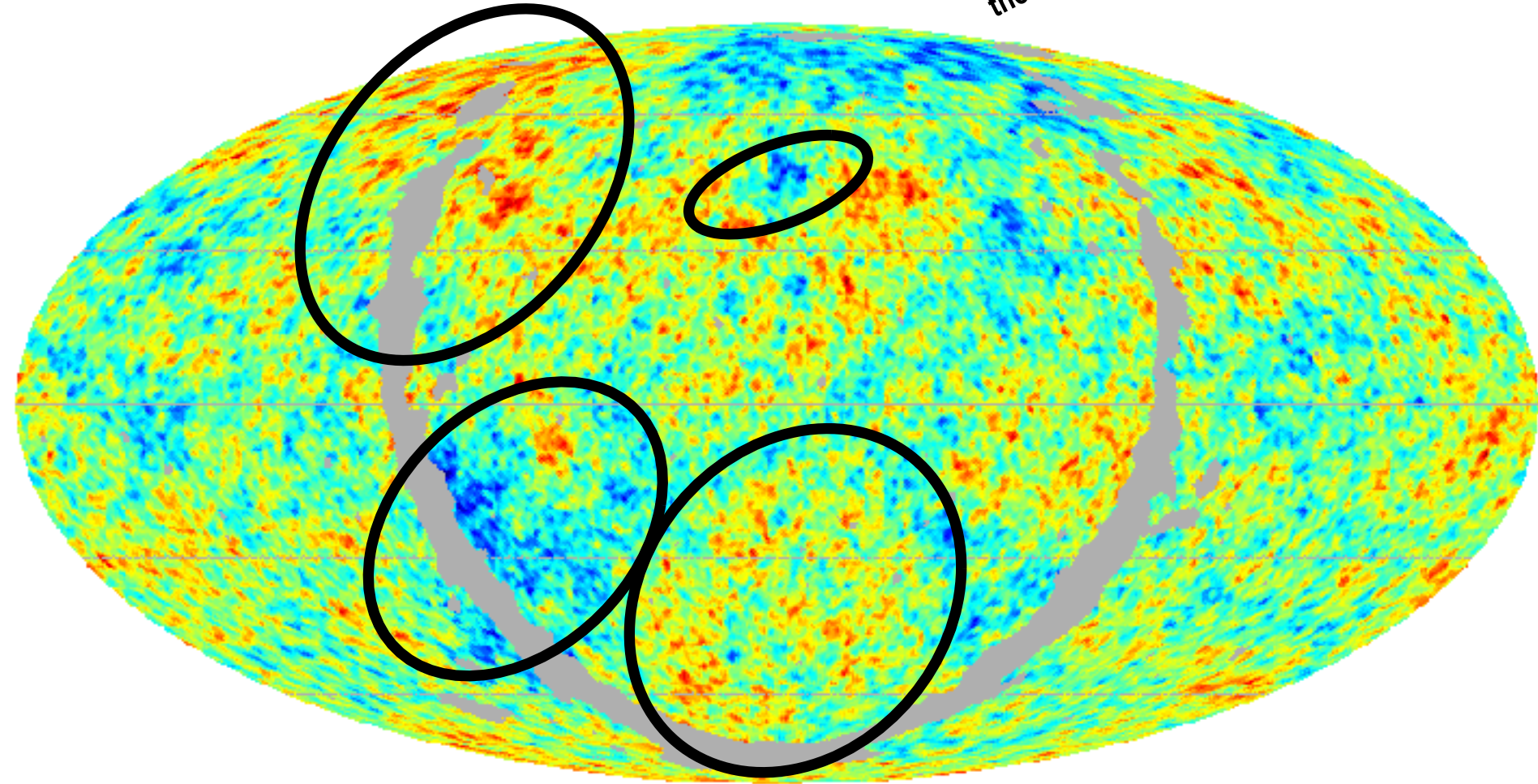
# looking at the CMB cold spot again as an anomaly example

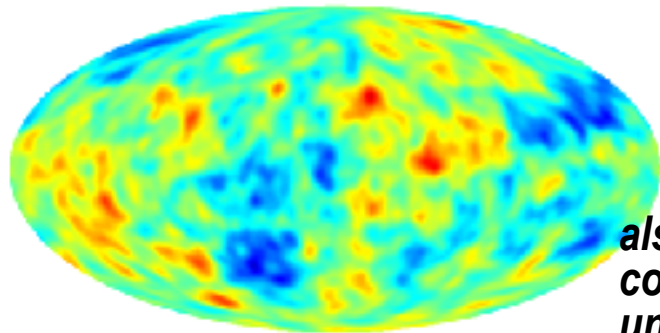
$>4.5\sigma$   $<1\%$   $L\sim 20$  ..... LSS void?

*B+Huang tried hard to make a Grand Unified Theory of Anomalies? new ways of looking at the anomalies (comparing harmonic and real space in various ways) but no GUTA ... TBD*

**CMB**  $\sim 10,000,000$  T/E modes of  $\Lambda$ CDM  
 $\approx 500$  modes of anomaly  
 $\approx 100$  modes reionization history

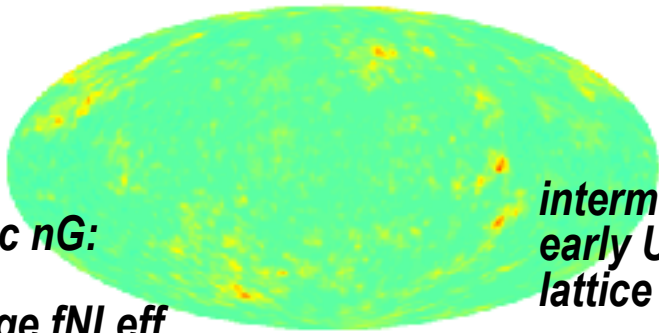
the rare cold spot



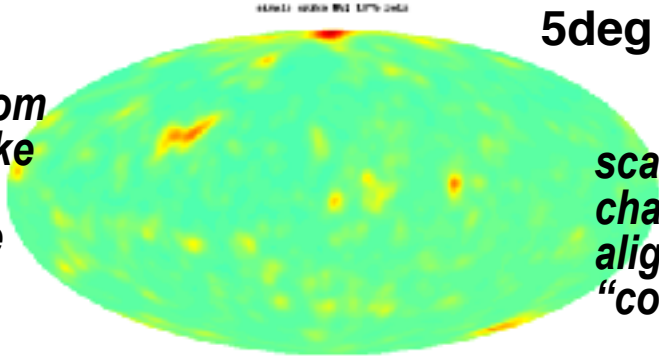


**5deg fwhm**

*also cf. quadratic nG:  
correlated fNL  
uncorrelated large fNL<sub>eff</sub>*



*intermittent nG from  
early U preheating  
lattice sims - too small*



**5deg fwhm**

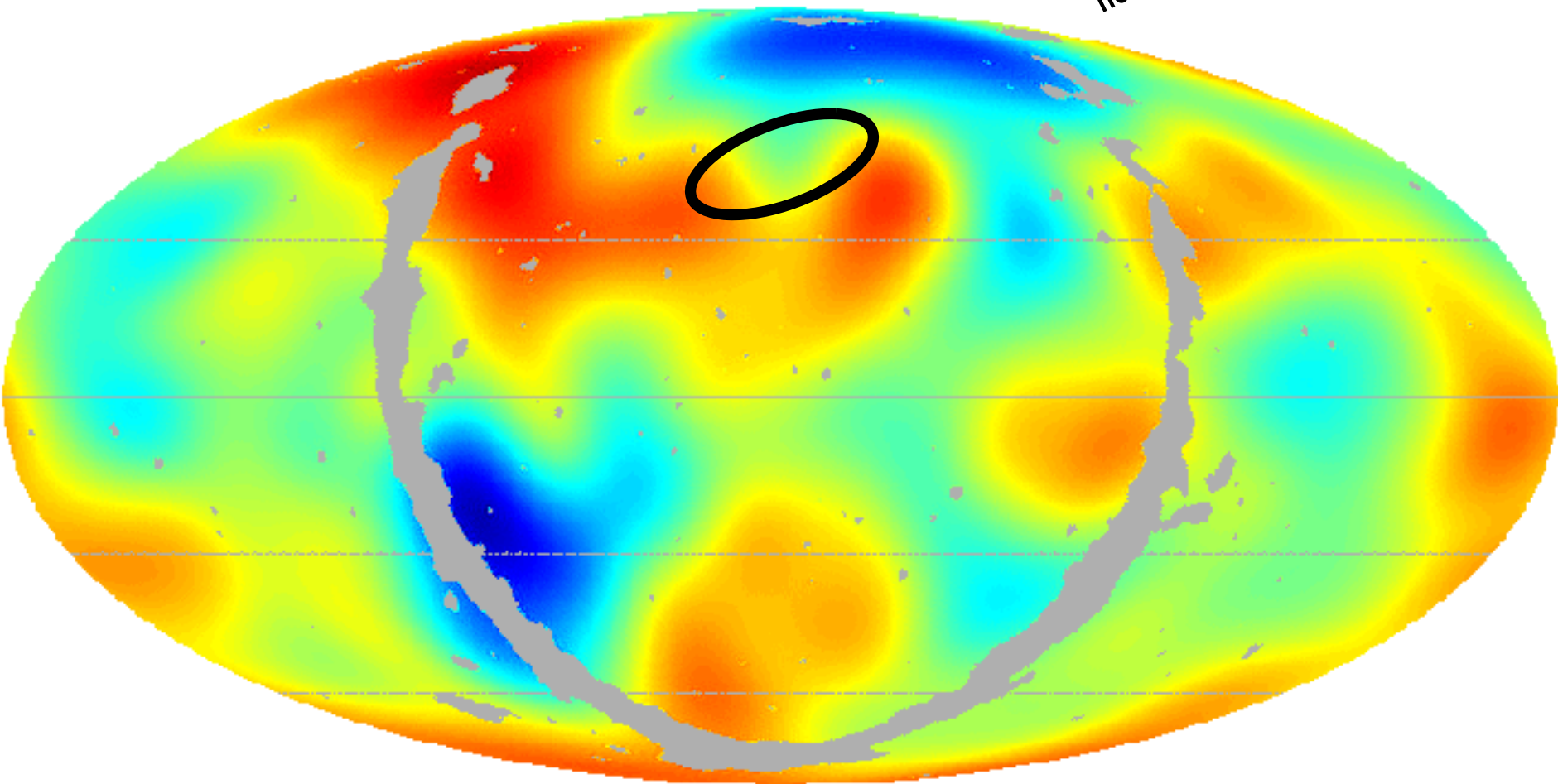
*intermittent nG from  
early U single spike  
sims - tunable  
amplitude, get the  
“cold spot”*

*scan sims to get  
chance intermittent  
alignment to get a  
“cold spot”*



Gaussian smoothing  $l = 6$  (FWHM 20.8deg)

*no cold spot*



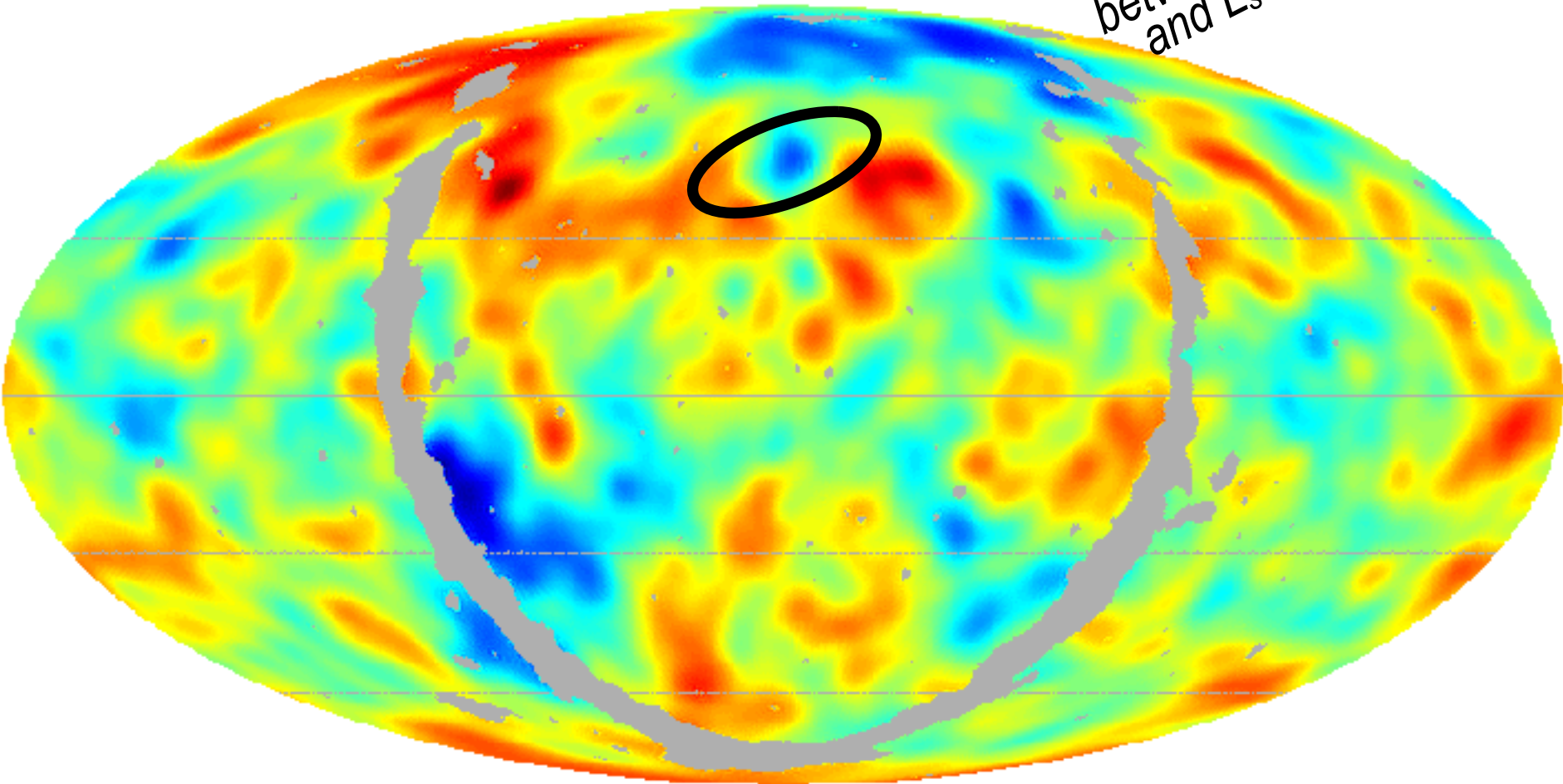
-101.



+72.5

Gaussian smoothing  $\lambda = 20$  (FWHM 6.6deg)

**cold spot**  
emerges  
between  $L_s=6$   
and  $L_s=20$

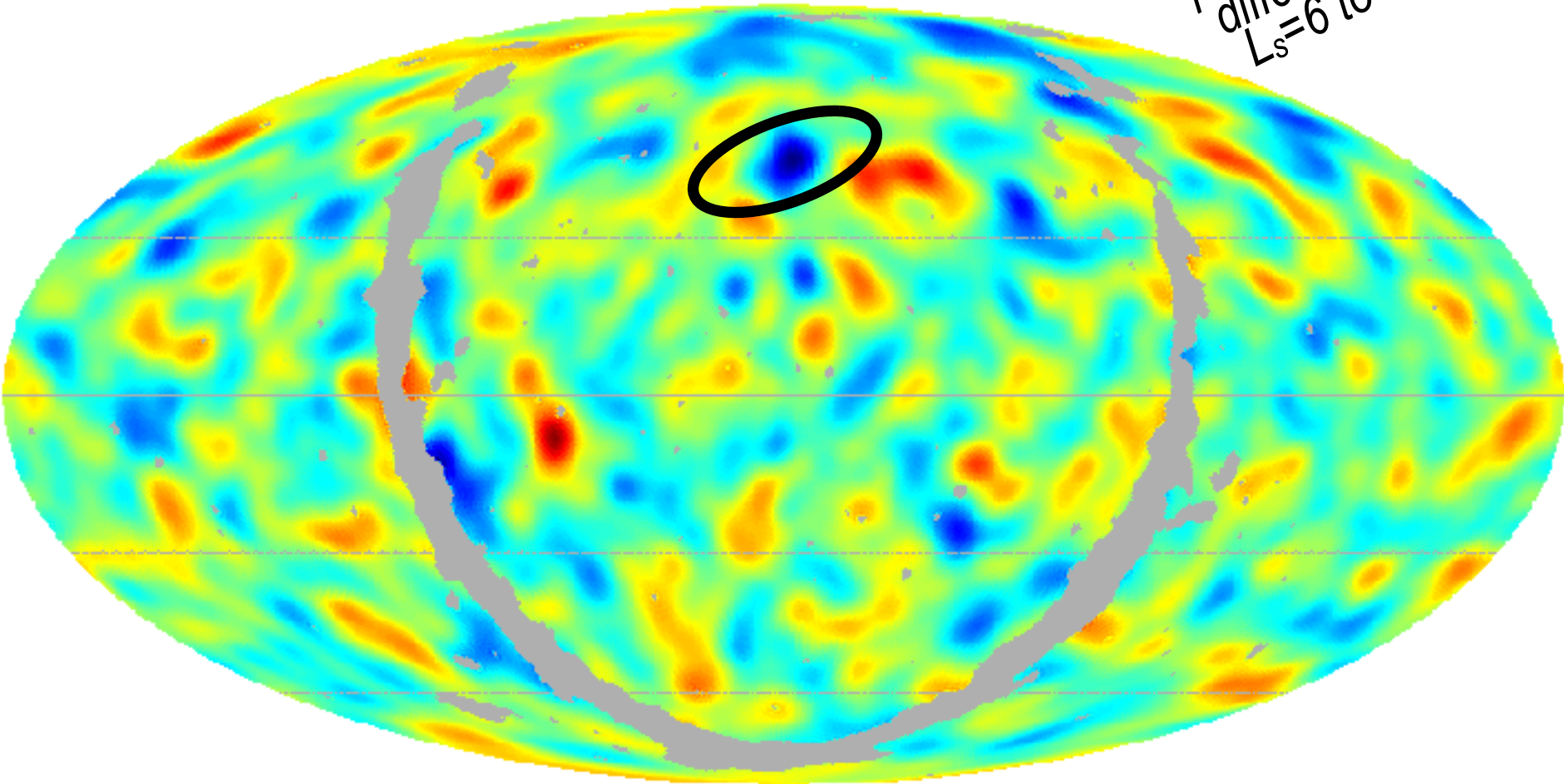


-165.

+125.

Difference map between  $l_{\text{smooth}} = 20$  and  $l_{\text{smooth}} = 6$

**cold spot**  
prominent in the  
difference map  
 $l_s=6$  to  $l_s=20$



-94.8

+90.4

$$W(\ell) = e^{-\frac{\chi(\ell|1)}{2(\ell_2+1/2)^2}} - e^{-\frac{\chi(\ell|1)}{2(\ell_1+1/2)^2}} \quad (\ell_2 > \ell_1)$$

$\ell_1$	$\ell_2$	$T_{\text{cold}}/\sigma_T$	cold-spot p value	$T_{\text{hot}}/\sigma_T$	hot-spot p value
2	20	-3.5	29.9%	3.2	60.2%
4	20	-4.0	10.1%	3.9	13.9%
6	20	-4.5	2.0%	4.2	4.7%
8	20	-4.5	2.1%	4.3	4.5%
10	20	-4.5	3.0%	4.4	3.9%

*tantalizing that the cold spot is the same L-band range as the L p spec dip, but all of our tools have not teased out a relation*

*B+Huang 2015*

0

*e.g. low L constrained fields do not make a nice low-L cavity for the cold spot to be boosted up*

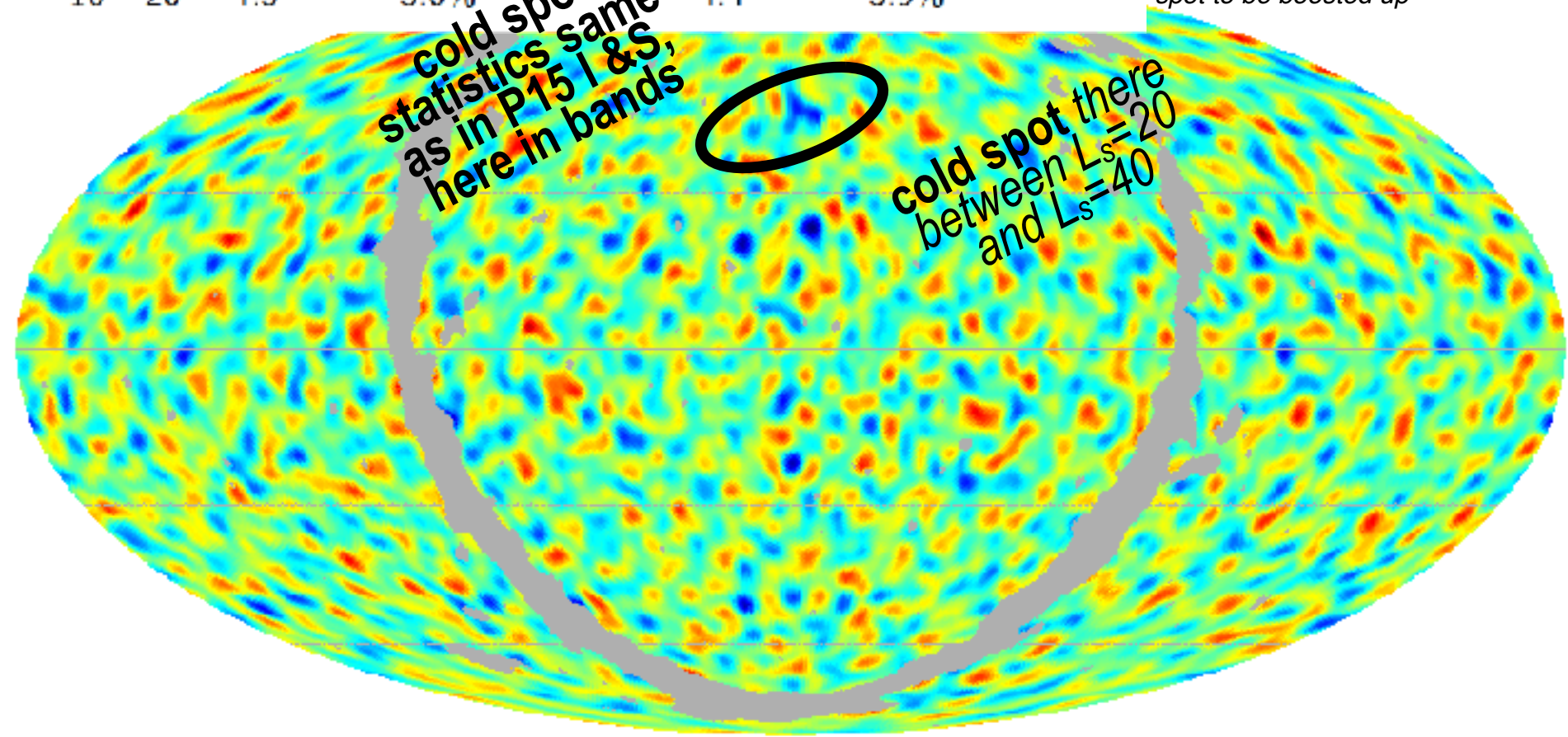
**cold spot statistics same as in P15 I & S, here in bands**

**cold spot there between  $L_s=20$  and  $L_s=40$**

-65.7



+59.7



# **how intermittency could amplify the cold spot to statistical correctness**

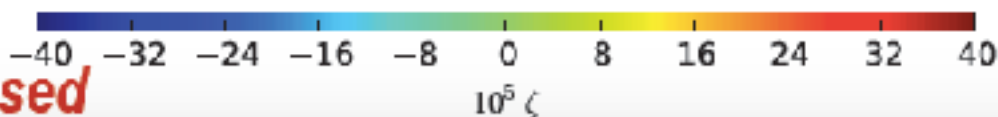
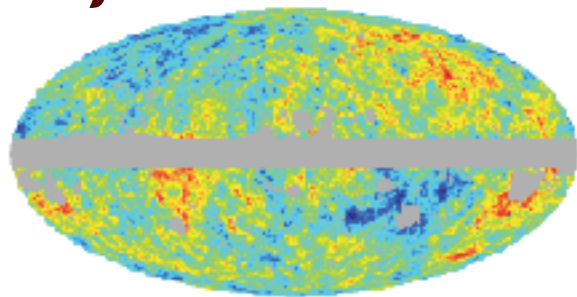
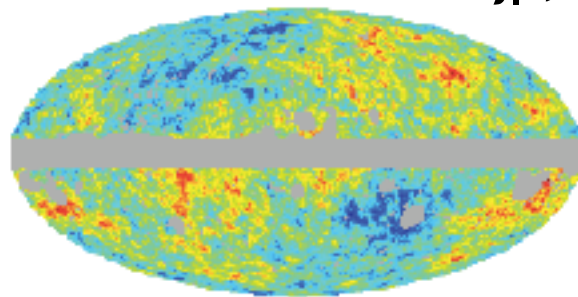
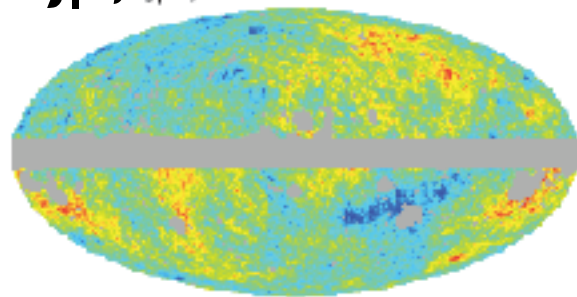
from  $>4.5\sigma$  Gaussian random field anomaly



$\langle \zeta | T, E \rangle$

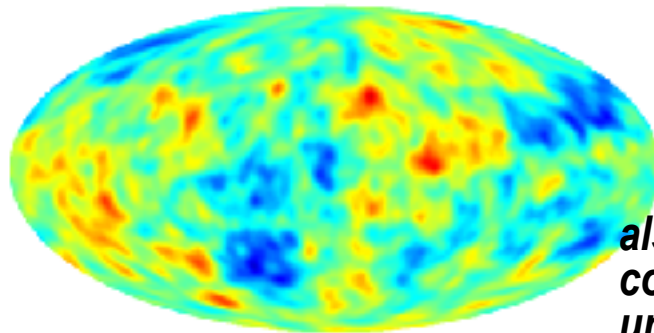
Planck 2015 XVII nonG

$\langle \zeta | T, E \rangle + \delta \zeta$



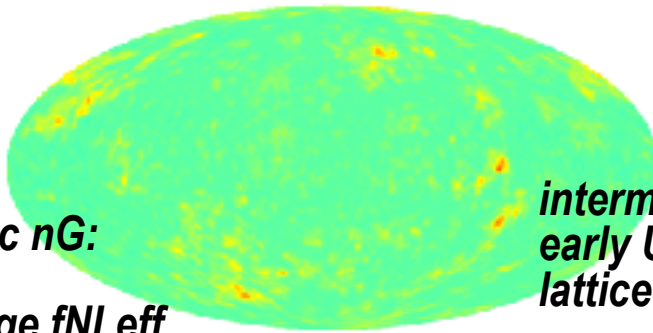
caution: not de-lensed

visibility mask



5deg fwhm

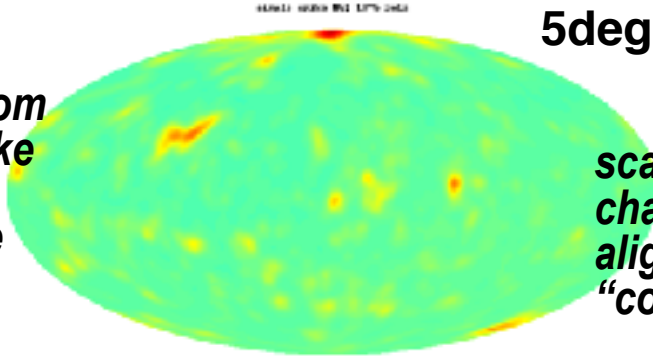
also cf. quadratic nG:  
correlated fNL  
uncorrelated large fNL<sub>eff</sub>



intermittent nG from  
early U preheating  
lattice sims - too small



intermittent nG from  
early U single spike  
sims - tunable  
amplitude, get the  
"cold spot"



5deg fwhm

scan sims to get  
chance intermittent  
alignment to get a  
"cold spot"



**mocking heaven to**  
**explore 3D intermittency**  
from **modulating preheating,**  
**bubble collisions, etc**

we are **in quest** of an **apparent**  
**breakdown of LSS**  
**homogeneity** - but NOT that

*a nonlinear (large scale) bias response to the nearly scale invariant isocon field*  
*cf. LSS bias of clusters/galaxies: threshold function acts on the linear density field*

*CMB modes  $\sim f_{\text{sky}} L_{\text{max}}^2$  LSS tomography  $\propto k_{\text{max}} d_{\text{max}}$*

**mocking heaven to**

**explore 3D intermittency**

from **modulating preheating,**

**bubble collisions, etc**

we are **in quest** of an **apparent**

**breakdown of LSS**

**homogeneity - *not really broken***

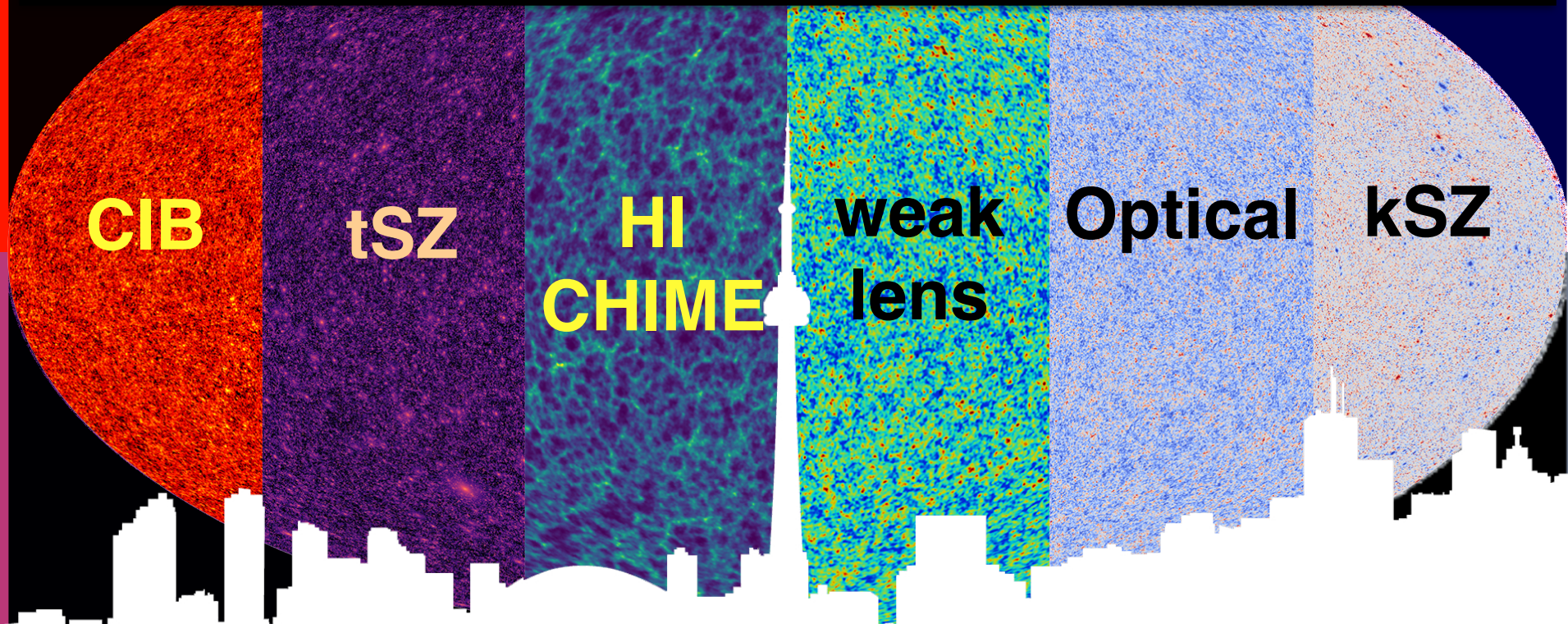
*a nonlinear (large scale) bias response to the nearly scale invariant isocon field  
cf. LSS bias of clusters/galaxies: threshold function acts on the linear density field*

# Mocking Heaven @ CITA Alvarez Bond Stein Battaglia ..



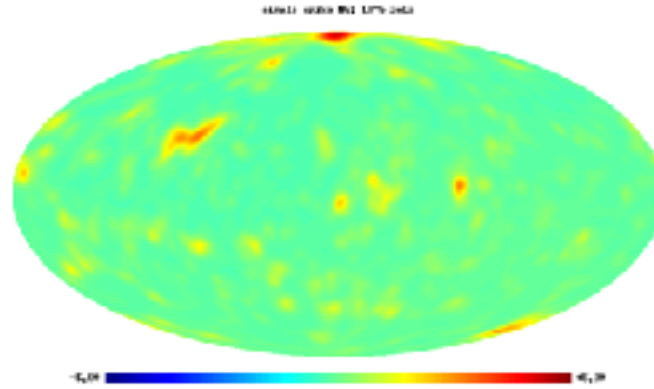
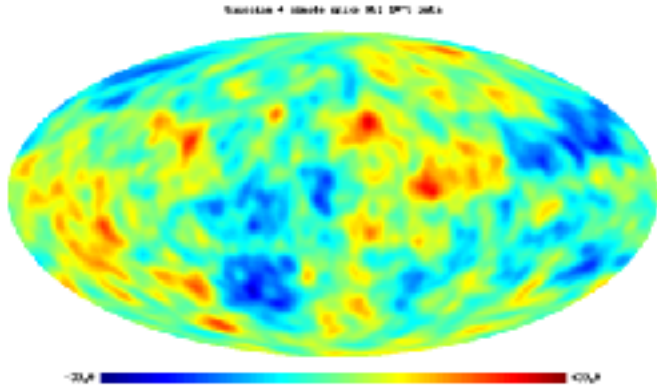
*Peak Patch Full Sky Models for Planck, AdvACT, SO, CMB-S4, CCATp, CHIME, HIRAX, SKA, COMAP, EUCLID, LSST, ...*

*need End to End mocks, fully correlated to draw out:  
BSMc, DE/modG, Mnu, nonG (correlated, uncorrelated, intermittent),...*



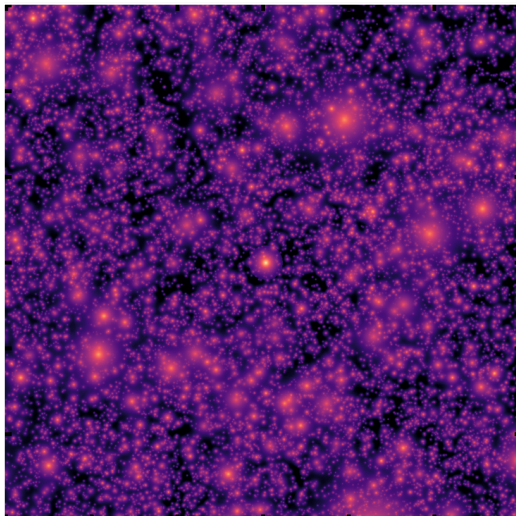
*Planck 2015 XII: Full Focal Plane Sims (Nov): FFP8 ensemble of 10K EndtoEnd mission realizations in 1M maps. instrument noise + CMB + PSM + .. (25M NERSC CPU hrs)*

**CMB+LSS mocks to test: standard Gaussian inflaton  $\zeta_{inf}$ + subdominant uncorrelated  $\zeta_{isoc}$**   
 e.g., from modulated preheating by isocons



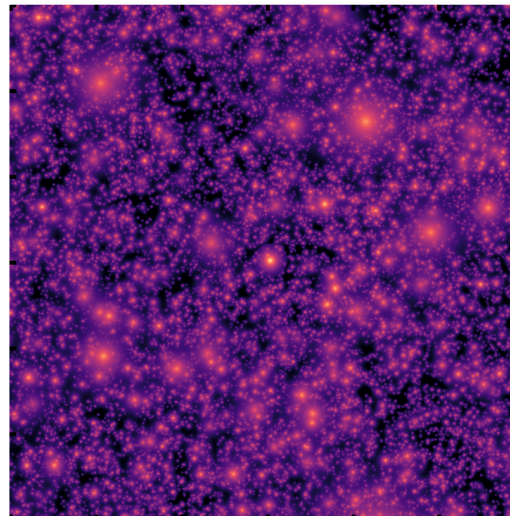
*uncorrelated nonG 'wide open' cf. usual correlated highly constrained nonG  $f_{nl}$*

LSS tSZ: Gaussian std    **Gaussian  $\zeta_{inf}$**



B2FH, b+braden+frolov+huang

LSS tSZ: Gaussian std +  
 subdominant uncorrelated  $\zeta$



ABSB+FH, alvarez+b+stein+frolov+huang

**Gaussian  $\zeta_{inf}$  +  
 uncorrelated  
 intermittent nonG  $\zeta_{isoc}$**

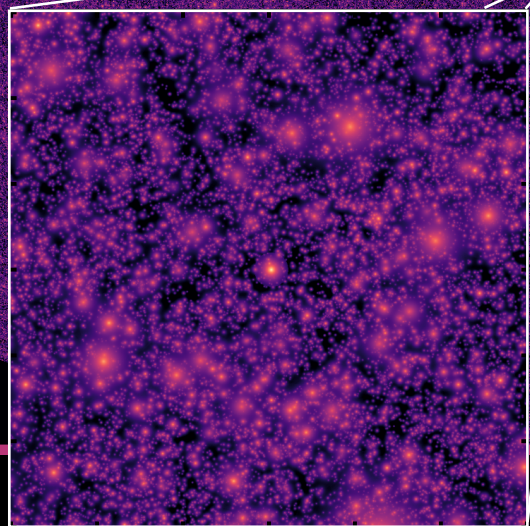
# Compton Scattering (Sunyaev-Zeldovich) Simulations for ACT, Planck, Simons Obs & CMB Stage 4 Cluster Observations Using high res Gas Hydro Sims

# HI Intensity Mapping simulations of CHIME / HIRAX .. $z=0.8-2.5$ , $\sim(8 \text{ Gpc})^3$

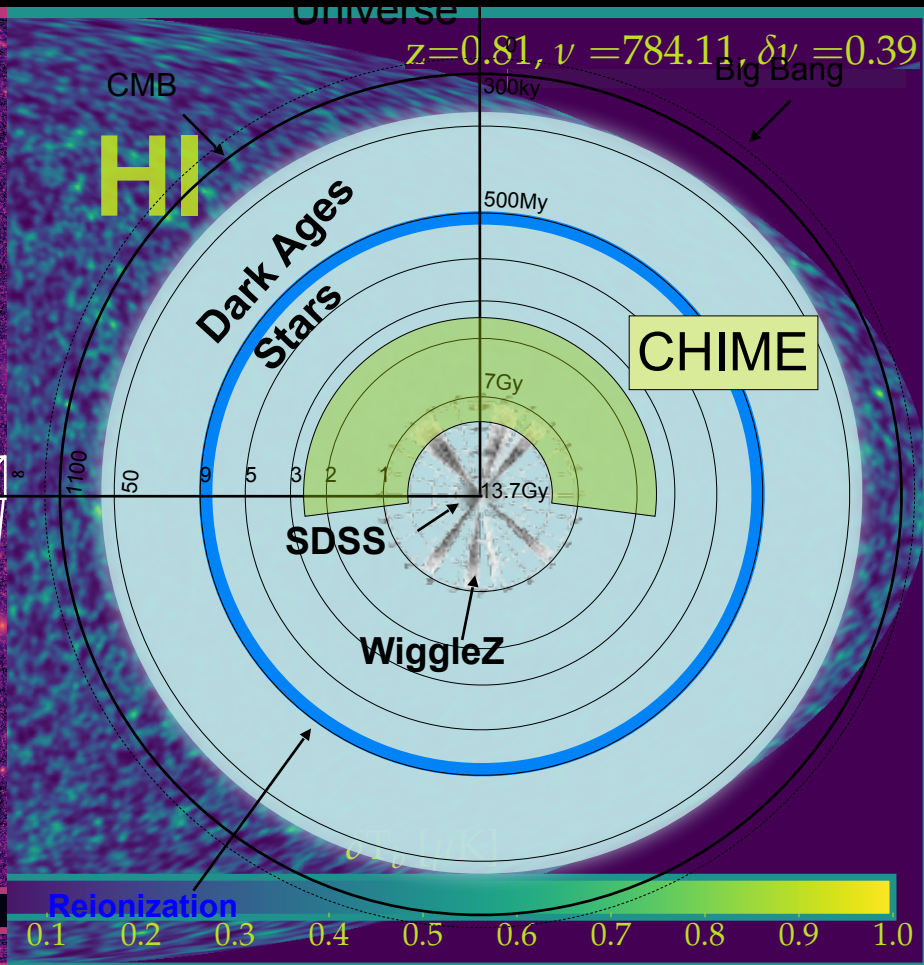
$0.00 < z < 1.25$   
8Gpc,  $4096^3$  Box

tSZ

Gaussian



6 deg



**Compton Scattering (Sunyaev-Zeldovich)**  
**Simulations for ACT, Planck, Simons Obs**  
**& CMB Stage 4 Cluster Observations**  
**Using high res Gas Hydro Sims**

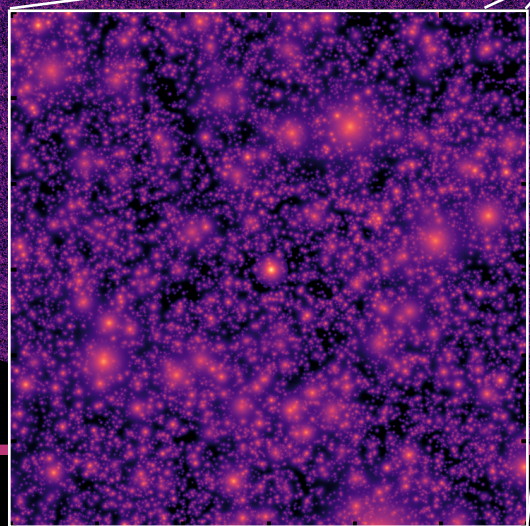
**HI Intensity Mapping**  
**simulations of CHIME / HIRAX ..**  
 **$z=0.8-2.5, \sim(8 \text{ Gpc})^3$**

$0.00 < z < 1.25$   
8Gpc,  $4096^3$  Box

$z=0.81, \nu = 784.11, \delta\nu = 0.39$

**tSZ**

**HI**



Gaussian

$\delta T_b [\mu\text{K}]$



6 deg



**Compton Scattering (Sunyaev-Zeldovich)**  
**Simulations for ACT, Planck, Simons Obs**  
**& CMB Stage 4 Cluster Observations**  
**Using high res Gas Hydro Sims**

**HI Intensity Mapping**  
**simulations of CHIME / HIRAX ..**  
 **$z=0.8-2.5, \sim(8 \text{ Gpc})^3$**

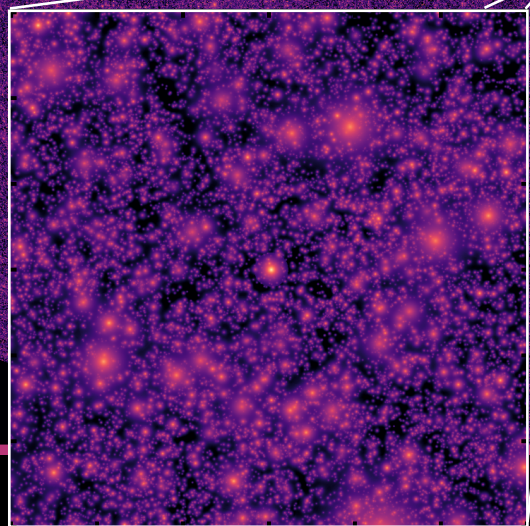
$0.00 < z < 1.25$   
8Gpc,  $4096^3$  Box

**tSZ**

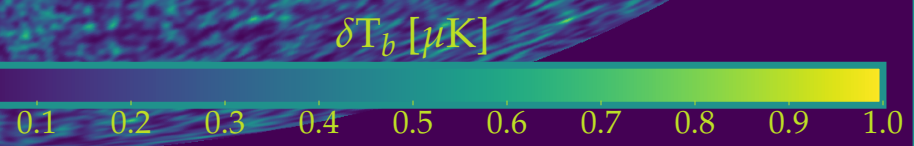
**HI**

$z=0.81, \nu = 784.11, \delta\nu = 0.39$

correlated  
Quadratic  
nonG  
 $f_{NL} = 25$



6 deg





**Compton Scattering (Sunyaev-Zeldovich)**  
**Simulations for ACT, Planck, Simons Obs**  
**& CMB Stage 4 Cluster Observations**  
**Using high res Gas Hydro Sims**

**HI Intensity Mapping**  
**simulations of CHIME / HIRAX ..**  
 **$z=0.8-2.5, \sim(8 \text{ Gpc})^3$**

$0.00 < z < 1.25$   
8Gpc,  $4096^3$  Box

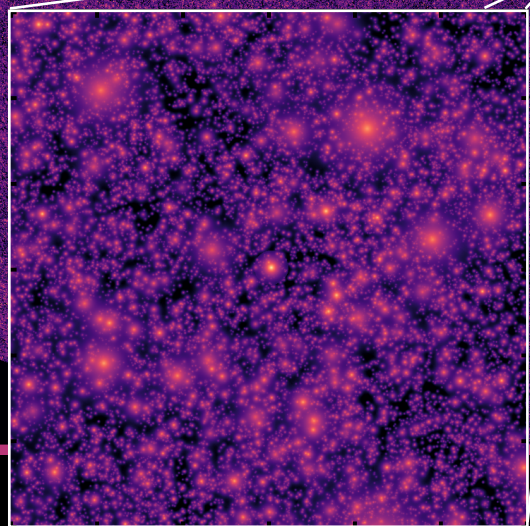
**tSZ**

**HI**

$z=0.81, \nu = 784.11, \delta\nu = 0.39$

uncorrelated  
modulated  
preheating  
intermittent  
nonG

**Gaussian Spike**

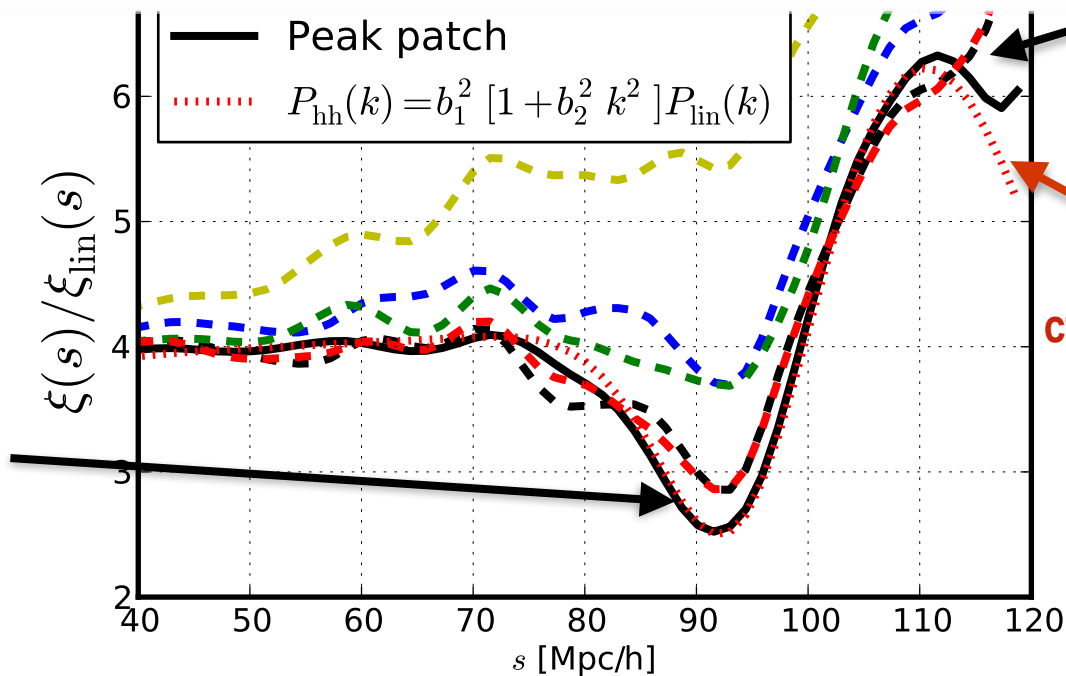
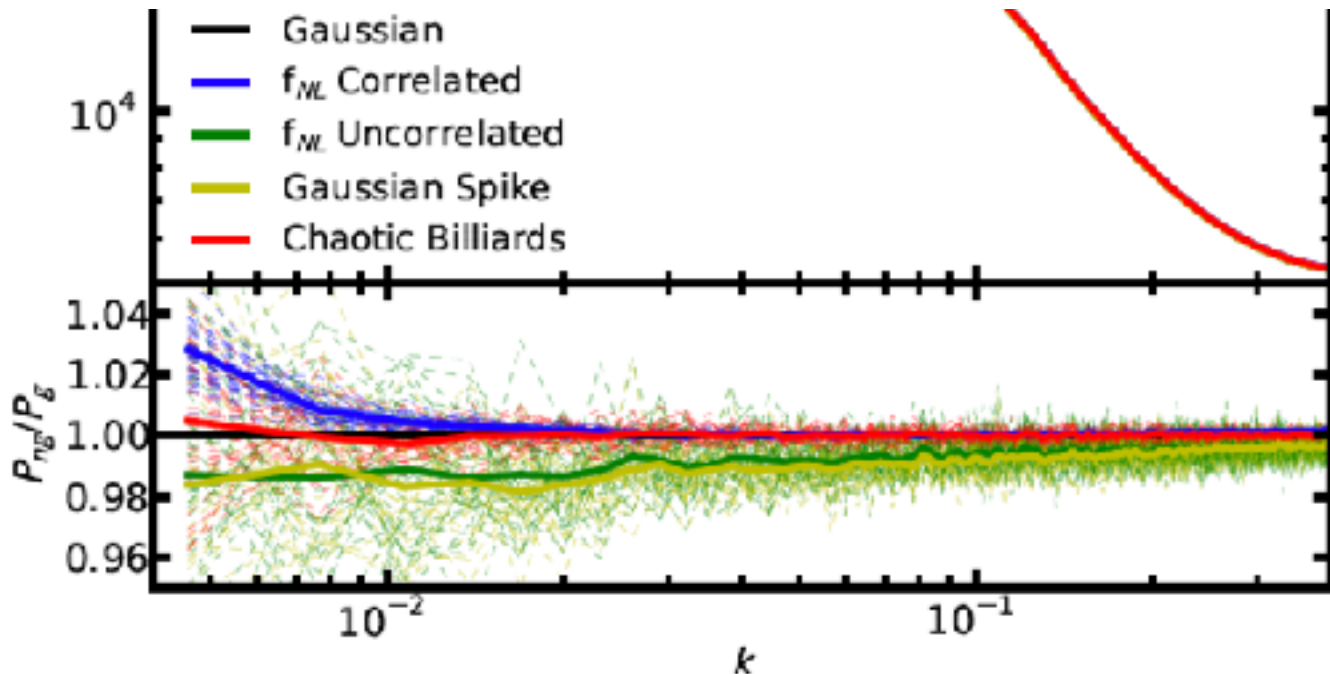


6 deg

$\delta T_b [\mu\text{K}]$



*this is a quantitative exercise* e.g.,  
**response of BAO & biasing  
of halos to forms of nonG -  
correlated cf. uncorrelated,  
intermittent cf. perturbative**  
e.g., **search for rare superBIAS  
events**  $>\sim$  supercluster-scale



Positive Curvature:  
Overabundance of  
Negative Extrema

cf. fit to N-body results:  
without any tuning it  
comes out from peak  
patches naturally

*intermittent nG from  
early U single spike*

Positive Curvature:  
Overabundance of  
Negative Extrema

## highly nonlinear field evolutions happened

(EoI caustics, bubble collisions, non-eq entropy generation)

*subdominant patterns do arise => will any be observable as rare-event CMB/LSS 'GaussianRandomField-biasing' anomalies?*

or **weak constraints** on multifield potentials,  $>$ horizon fields, nucleation rates, etc.

*B2FH17 progress in semi-analytic understanding of complex lattice sims with probability strings, caustics, trajectory stopping, shocks-in-time in the  $V(\phi)$ -web*

*light isocons cf. heavy isocons, the heavy can lighten up = original SBB  $nG$*

*isocon modulators, coupling(isocon) modulators, isocon tunneling, isocon oscillons, isocon short-lived fuzzy-strings, + very long-lived strings*

**alas a 2-number  $P_\zeta$ - $n_s$   $\zeta$ -verse so far ...  $r$  adds +1?**

intermittency frustration: statistical variance is large - cf. a 2-3 parameter search

**CMB restricts us to a projected 2D  $\zeta$ -scape to reconstruct  $\zeta$ -maps &  $\zeta$ -power, the future may look much the same as now for  $\zeta$  => potential  $V(\phi)$  => acceleration  $\epsilon(a)$ ; constrained  $r$  helps**

we mock the LSS future **end-to-end** to probe the mode-rich 3D  $\zeta$ -scape

**end**

**Cosmic standard model SMC =  $\Lambda$ CDM,  $\Lambda$ =dark energy+tilt: what is U made of?**  
Planck13-15-17 CMB, CvB, GW, dark matter, baryons, dark energy/modGravity, CIB:  
 $\rho_{\text{dm}}/\rho_{\text{b}}=5.43$   $\rho_{\text{de}}/\rho_{\text{dm}}=2.53$   $\Omega_{\text{m}}=0.32 \pm 0.009$ ,  $\Omega_{\Lambda}=0.68 \pm 0.009 \Rightarrow$

**BSMc Beyond the SMC** eg  $\Omega_{\Lambda}(t,x)$ , neutrino properties, inflation anomalies

**How Structure in the Universe Arose?: fluctuation generation in curvature from an early inflaton: reconstruct  $\ln a(x,t) \sim$  phonons, isocurvature, Gravity Waves HEAT** (coherence + quantum noise  $\Rightarrow$  incoherence via entropy generation) via nonlinear lattice simulations of multiple scalar fields at the end of inflation  $\Leftrightarrow$  dynamical systems

$\Rightarrow$  CMB/LSS Anomalies from EarlyU intermittent non-Gaussianity cf. perturbative non-Gaussianity, correlated & uncorrelated  $\Rightarrow$  CITA in CMB + LSS large surveys

**CMBology** precision cosmic parameters Planck 2013-15-17 intensity + polarization + ACTpol + BKP + SPT  $\Rightarrow$  Spider, Advanced ACTpol CCATp  $\Rightarrow$  Simons Obs  $\Rightarrow$  CMB Stage 4, ... & **LSSology** CHIME, COMAP, Euclid ... & cross correlations: CMBxLSS = webXweb

**morphs** into the nonlinear **Cosmic Web: Mocking Heaven** clusters SZ, filaments, voids; galaxies Mass-peak-patches, N-body, gas: Lens, tSZ, kSZ, CIB, CO, HI (21cm, H $\alpha$ , Ly $\alpha$ ) optical

LIM/LAM Line Intensity Mapping

constrained patch stacks

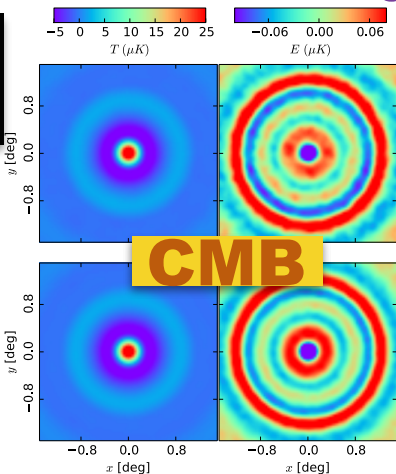
dynamical, coupled? dark energy

# Stacking @ CITA - oriented asymmetric on extrema & other points

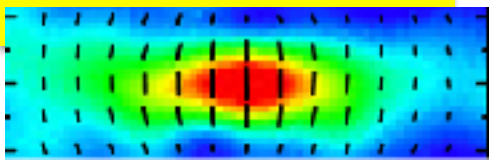
Topography of the CMB-web,  $\zeta$ -web, IQU/ E B, ISM-web,  $\gamma$ -web, LIM/LAM web  
 oriented/symmetry-broken stacking on field points peaks saddles (cols, passes)

**ACTPol stack**  
 $\langle T, E, B | T\text{-field} \rangle$

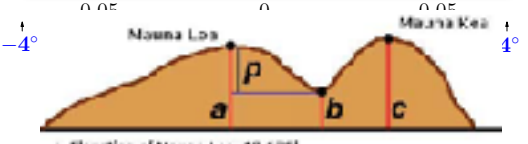
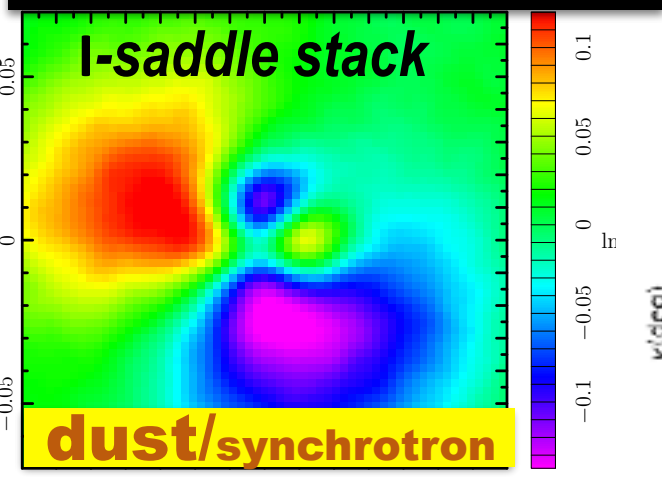
B+Frolov+Huang 17



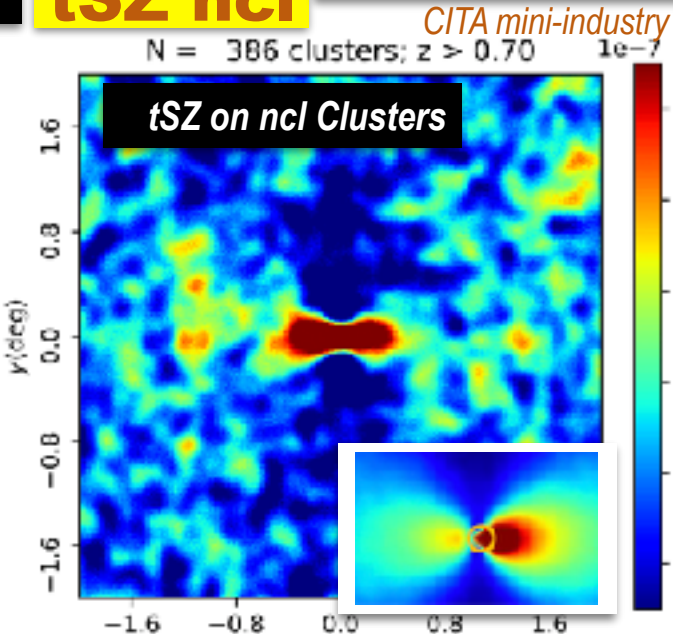
$\langle Qr | \text{oriented } l\text{-pk} \rangle$



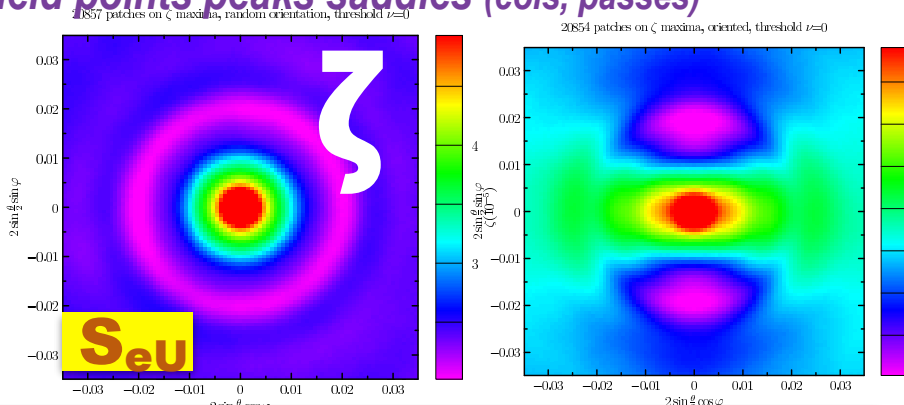
**Planck 353 GHz stacked dust**



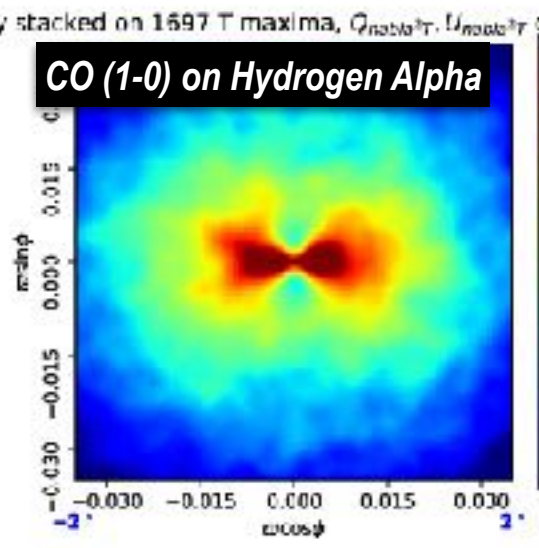
**tSZ ncl**



**earlyU SuperWeb map Planck2015 XVII**  
**stacked  $\zeta$ -map |  $\zeta$ -pk TQU** BFH17



**LIM/LAM** CITA mini-industry



# Mocking Heaven with PeakPatches++

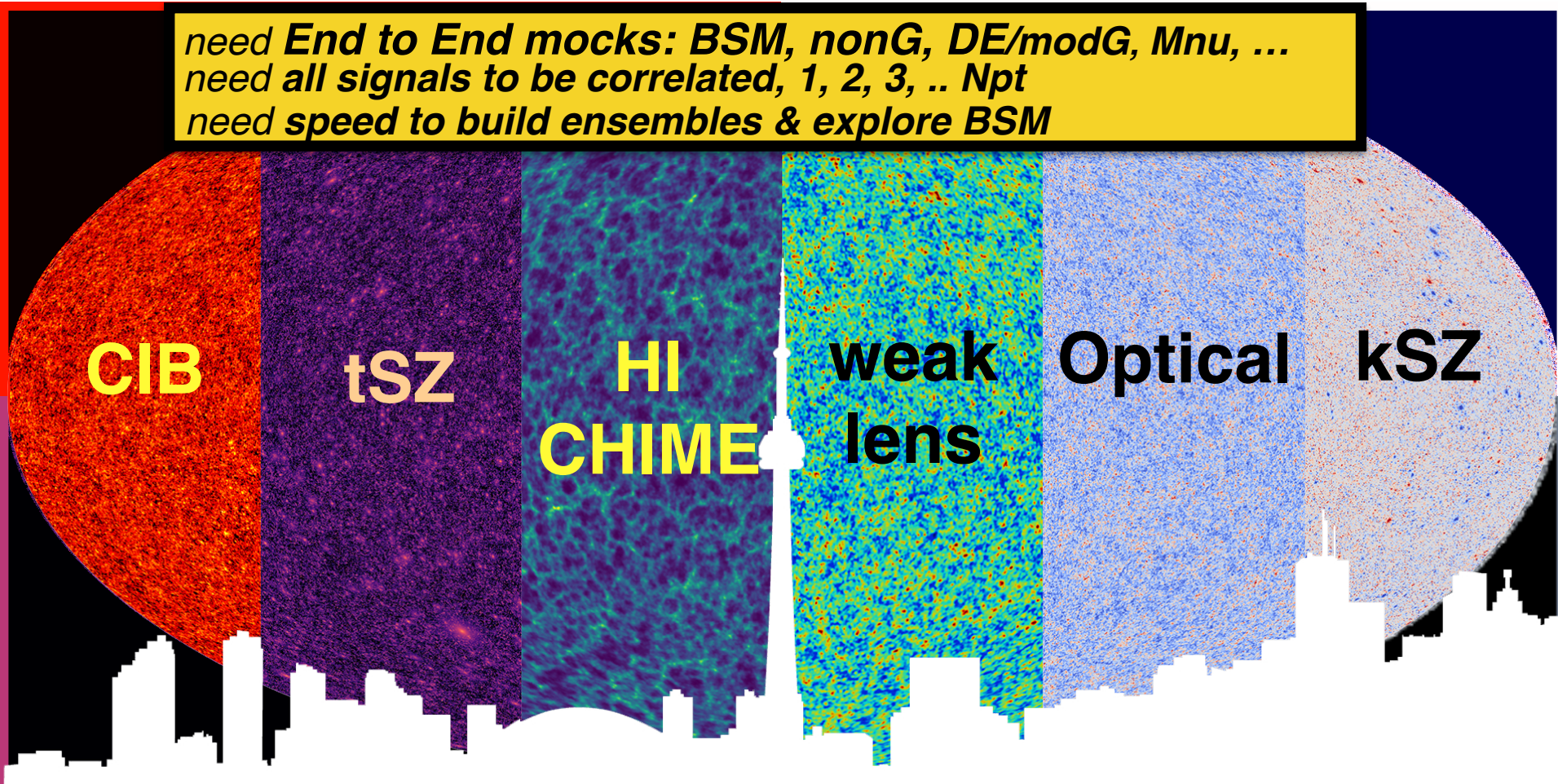


*Dick Bond @ CITA Jamboree 17*

*Planck, AdvACT, SO, CMB-S4, CCATp, EUCLID, LSST, CHIME, HIRAX, COMAP, ...SKA  
Line Intensity Mapping and Line Absorption Mapping **fLIMfLAM***

*CITA mini-industry: Marcelo Alvarez, Dick Bond, George Stein & Battaglia, Codis, van Engelen & FIRE: Lakhani + Murray + Hopkins + Berger & Connor Bevington, Bruno Régaldo-Saint Blancard, Ronan Kerr, Louis Pham*

*need **End to End** mocks: BSM, nonG, DE/modG, Mnu, ...  
need all signals to be correlated, 1, 2, 3, .. Npt  
need speed to build ensembles & explore BSM*



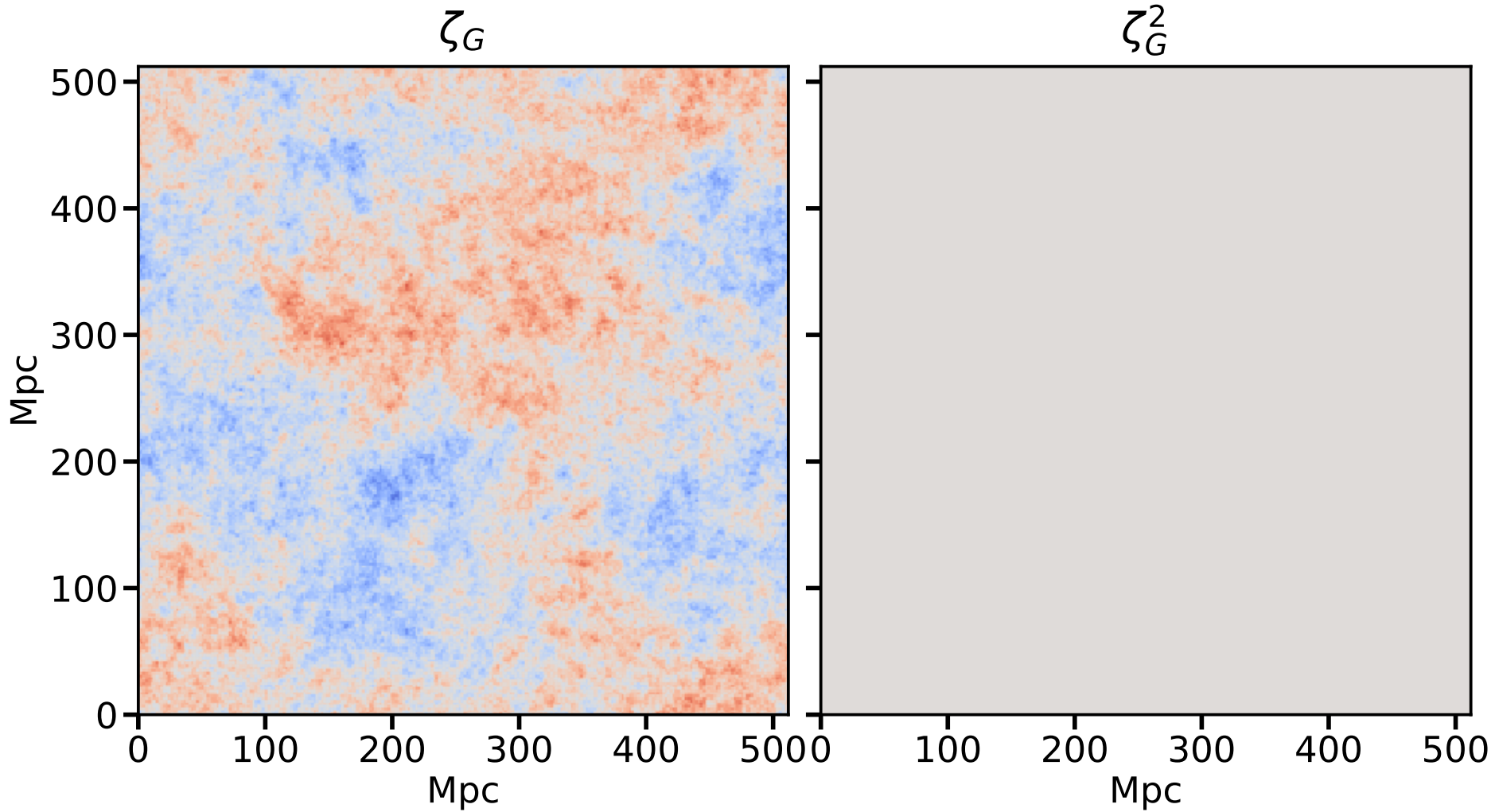
*Planck 2015 XII: Full Focal Plane Sims: FFP8 ensemble of 10K **EndtoEnd** mission realizations in 1M maps. instrument noise + CMB + PSkyModel + .. (25M NERSC CPU hrs)*



# Primordial Non-Gaussianity in the Peak Patch method:

$$\Phi_{NG} = \phi(x) + f_{NL}(\phi^2(x) - \langle \phi^2 \rangle)$$

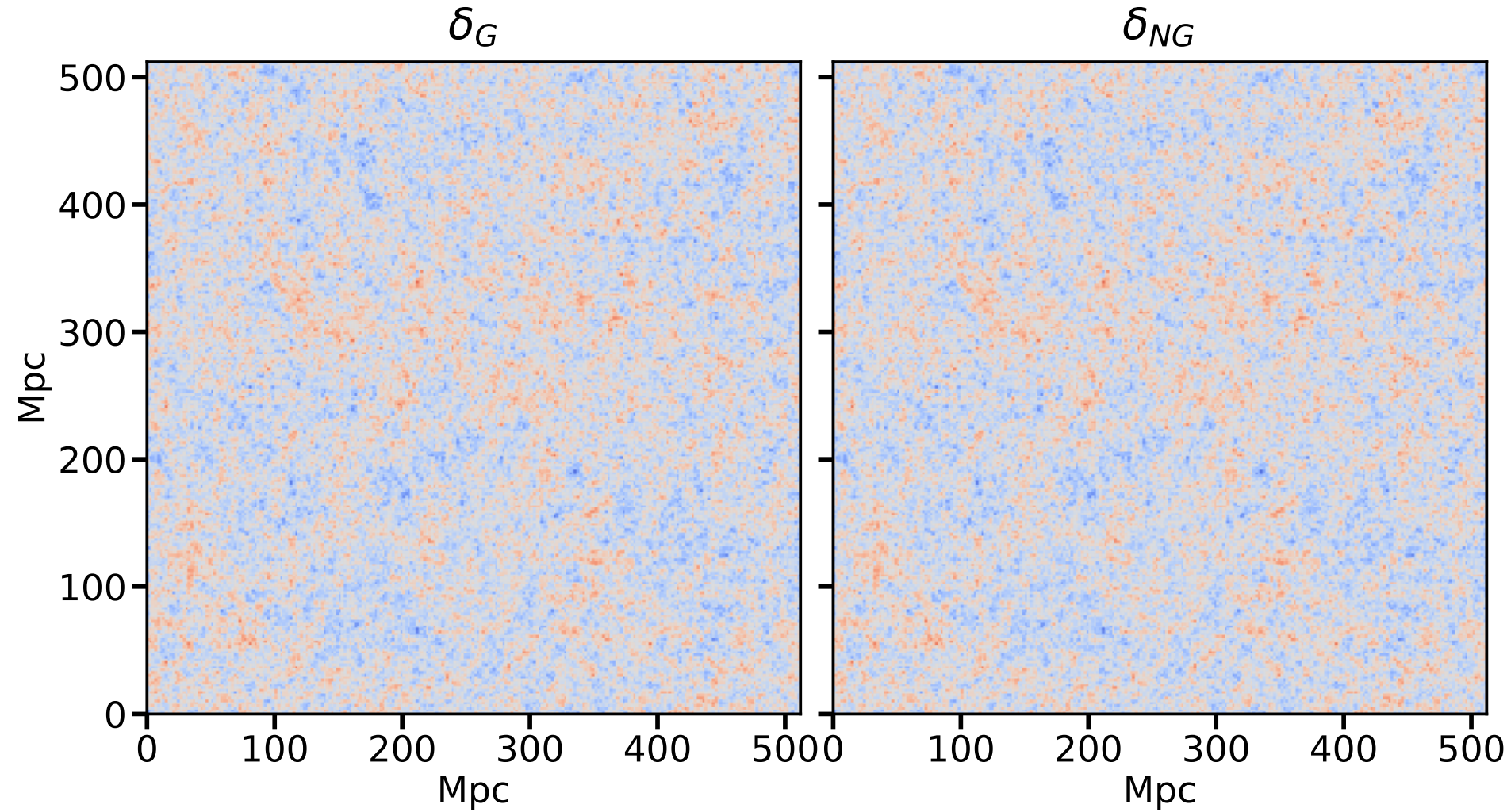
Classic Non-Gaussian case



# Primordial Non-Gaussianity in the Peak Patch method:

$$\Phi_{NG} = \phi(x) + f_{NL}(\phi^2(x) - \langle \phi^2 \rangle)$$

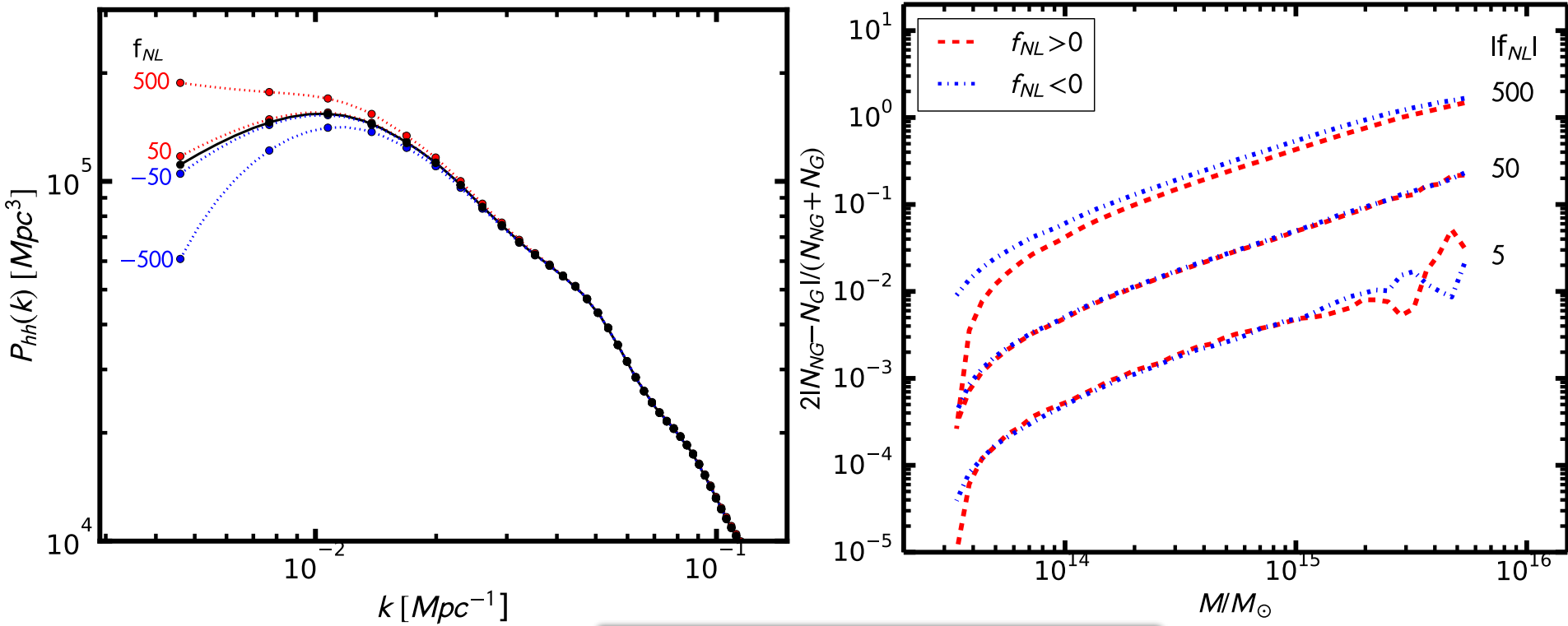
Classic Non-Gaussian case



# Primordial Non-Gaussianity in the Peak Patch method:

$$\Phi_{NG} = \phi(x) + f_{NL}(\phi^2(x) - \langle \phi^2 \rangle)$$

Validation

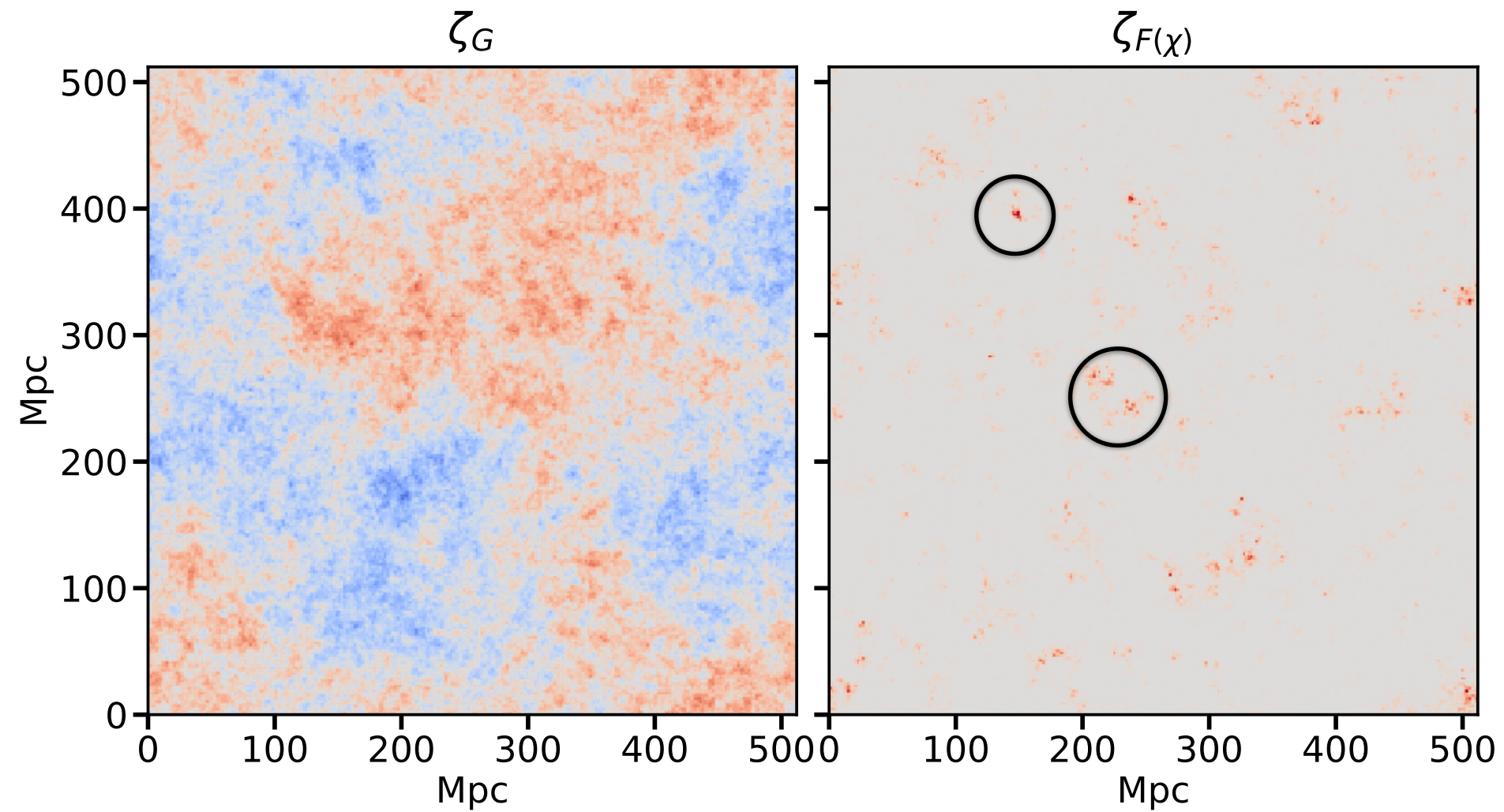


**Mean statistics from 6400  
2Gpc,  $1024^3$  runs**



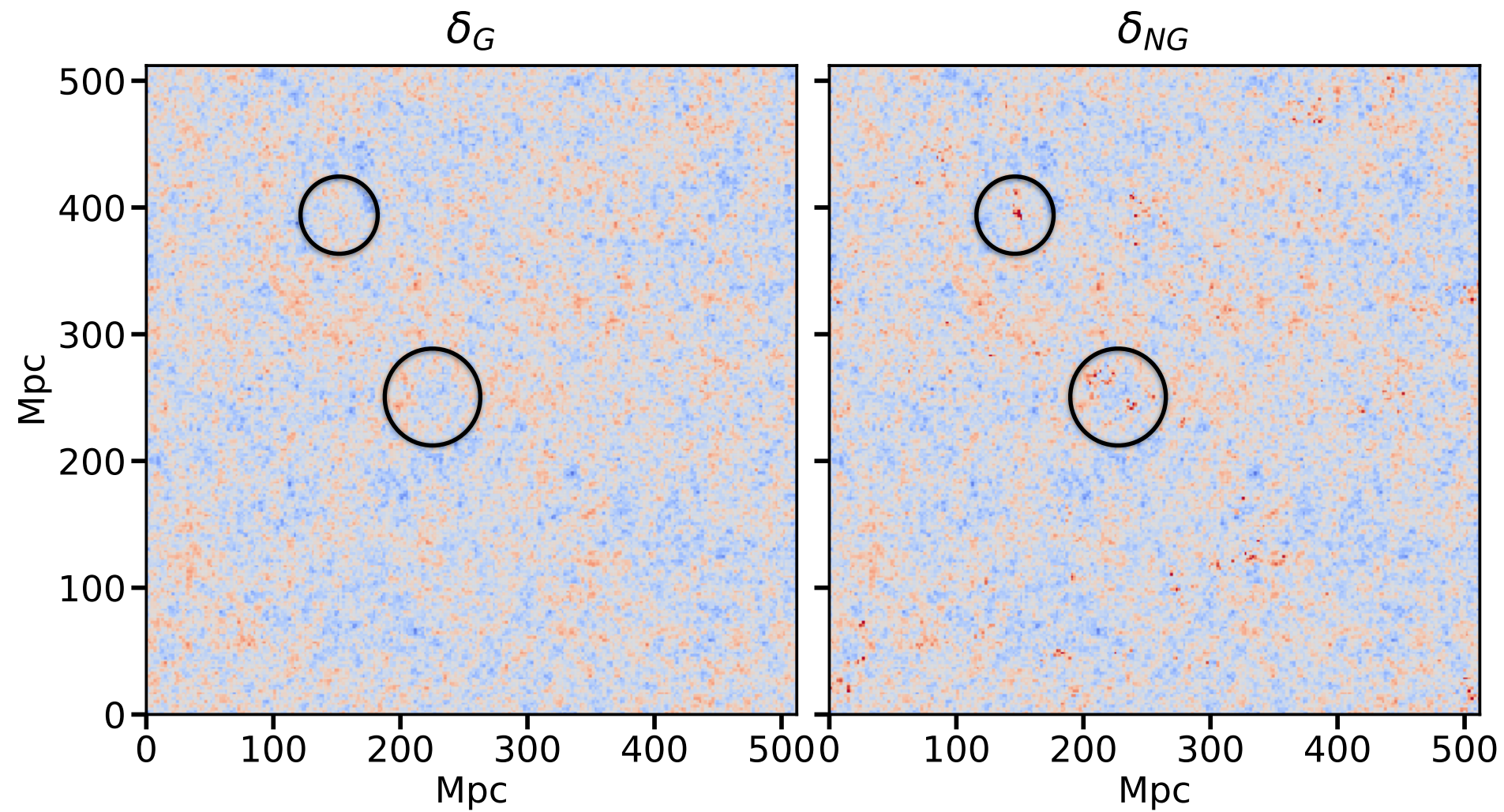
# Primordial Non-Gaussianity in the Peak Patch method:

Intermittent Non-Gaussian case

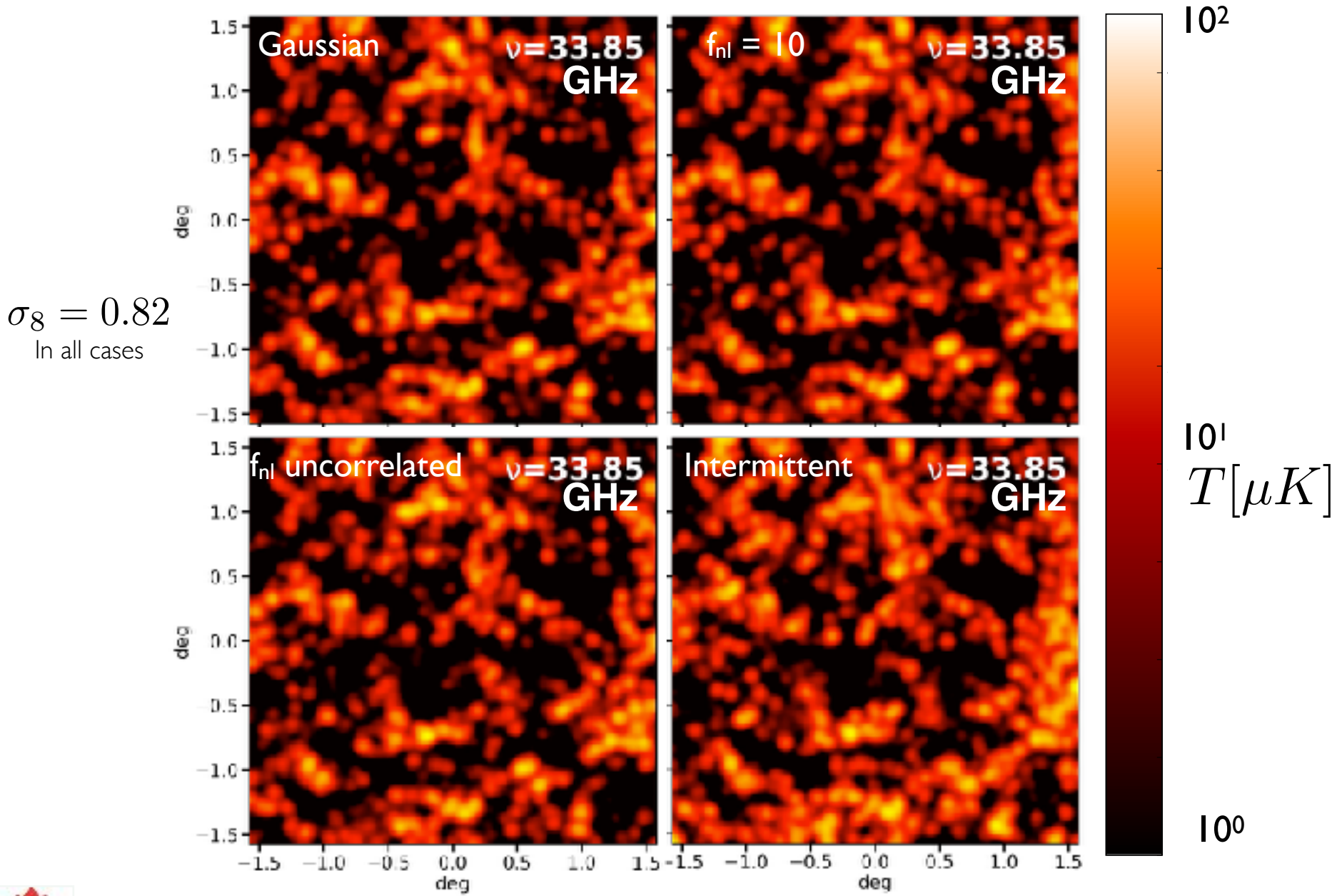


# Primordial Non-Gaussianity in the Peak Patch method:

Intermittent Non-Gaussian case

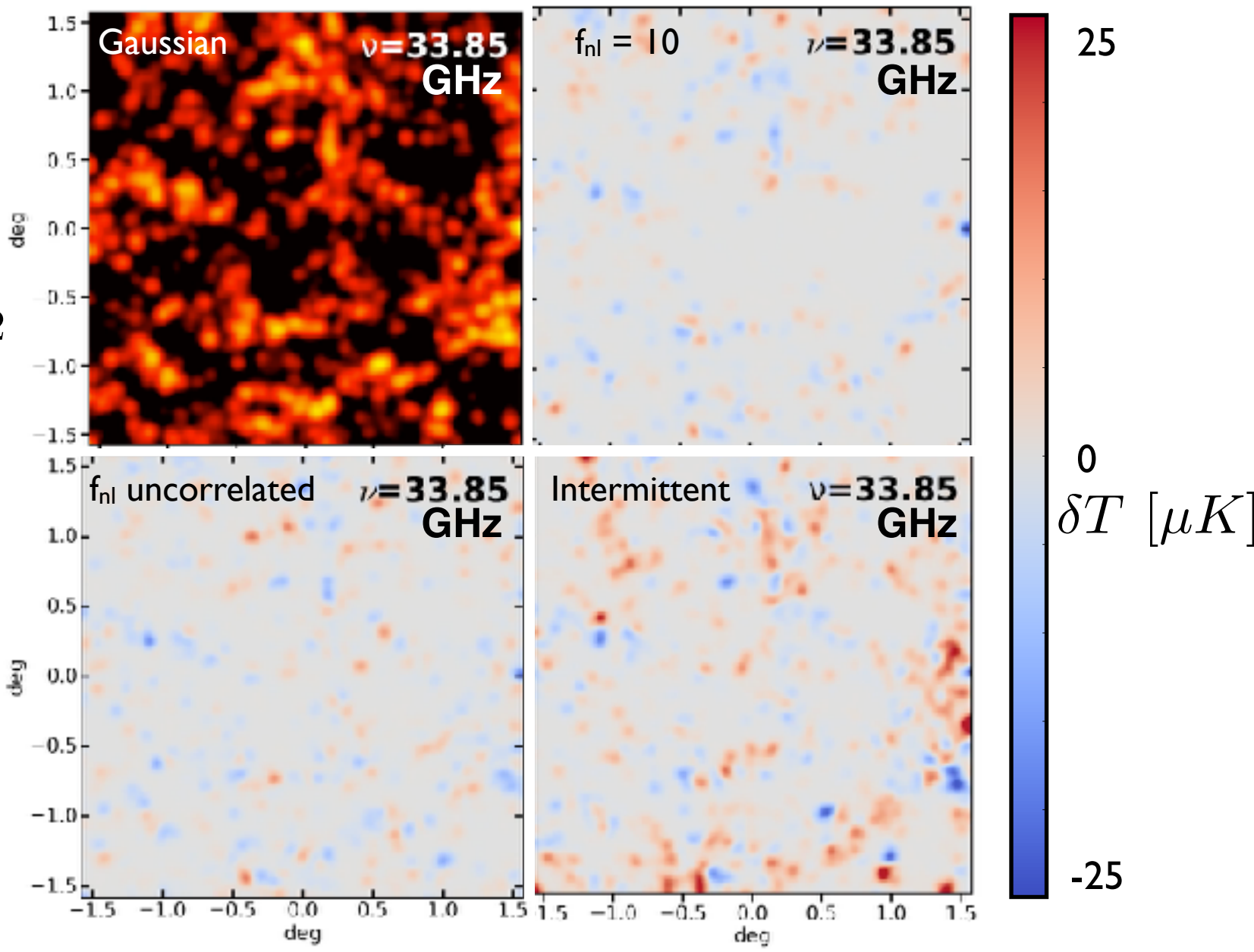


# Primordial Non-Gaussianity in CO



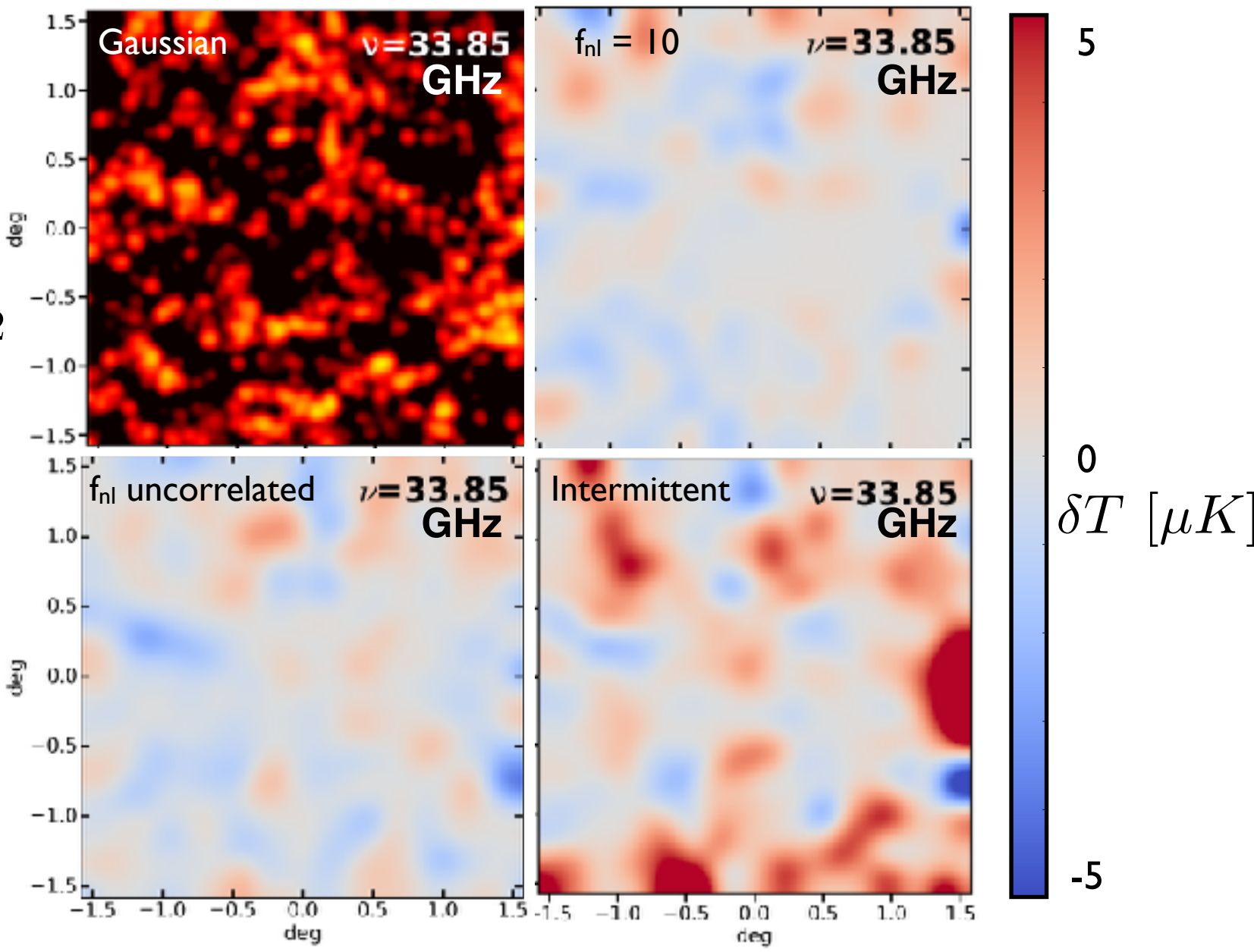
# Primordial Non-Gaussianity in CO

$\sigma_8 = 0.82$   
In all cases



# Primordial Non-Gaussianity in CO

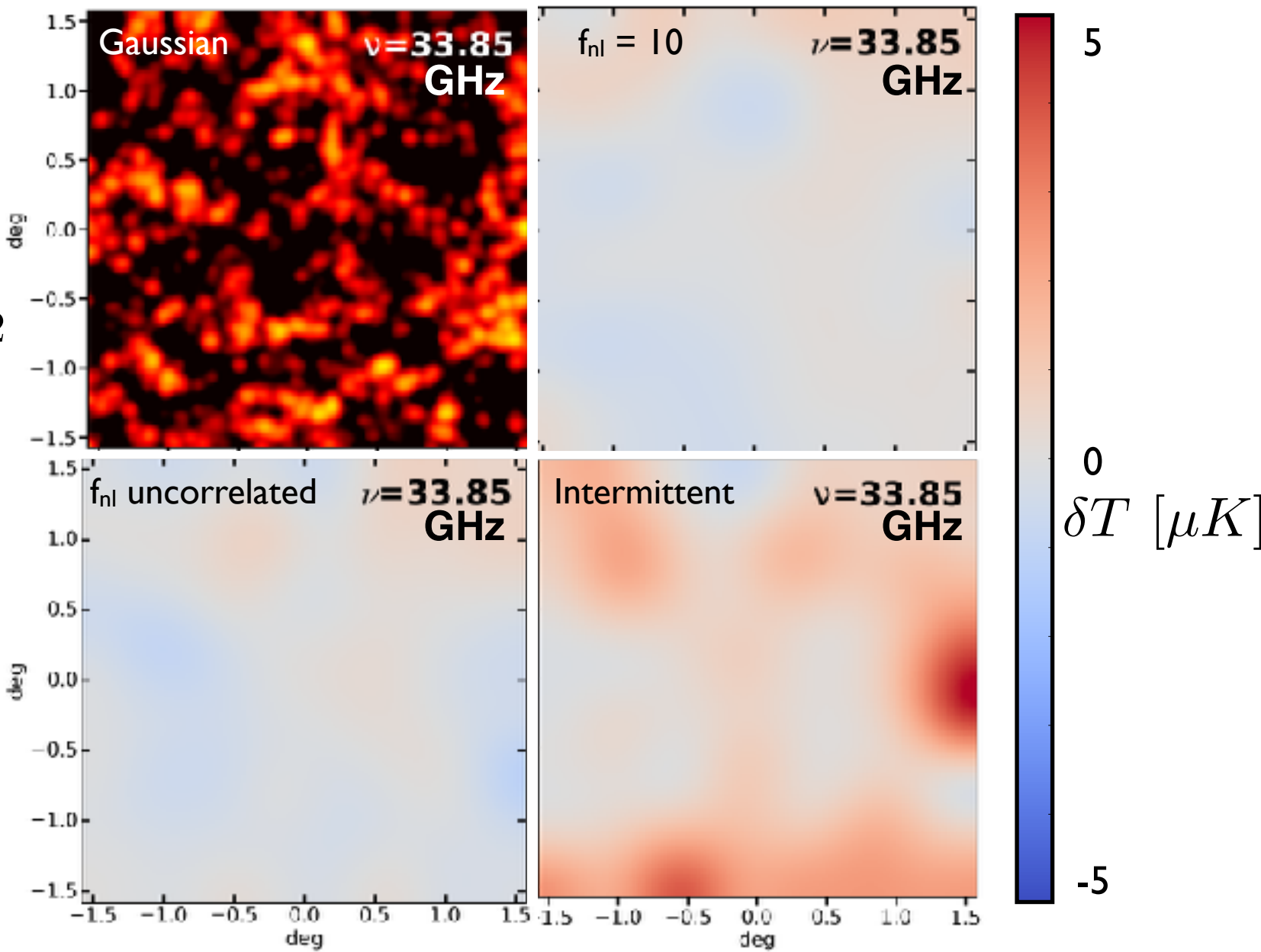
$\sigma_8 = 0.82$   
In all cases





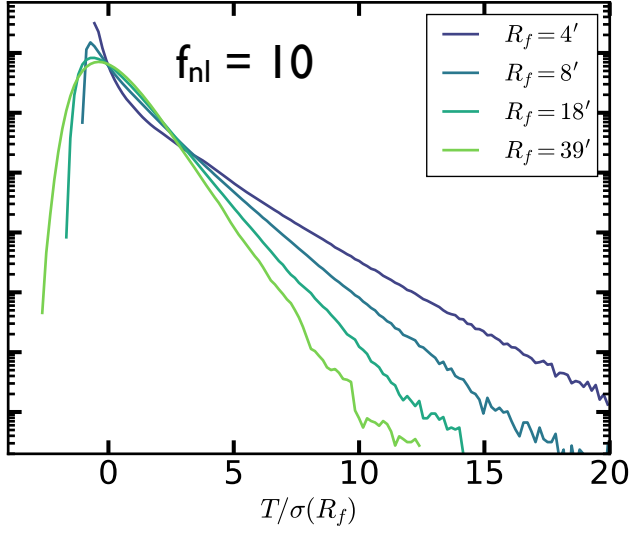
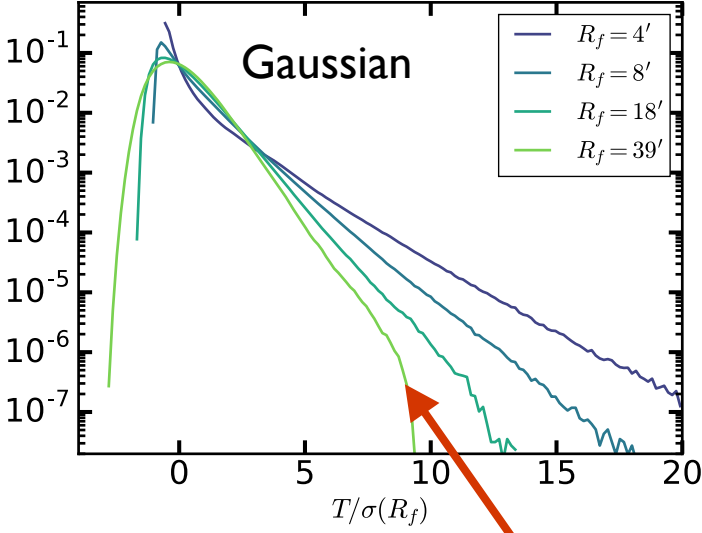
# Primordial Non-Gaussianity in CO

$\sigma_8 = 0.82$   
In all cases

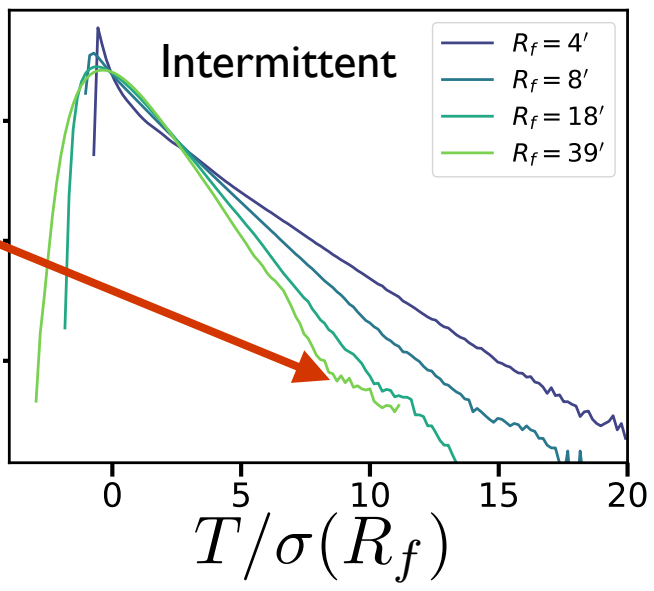
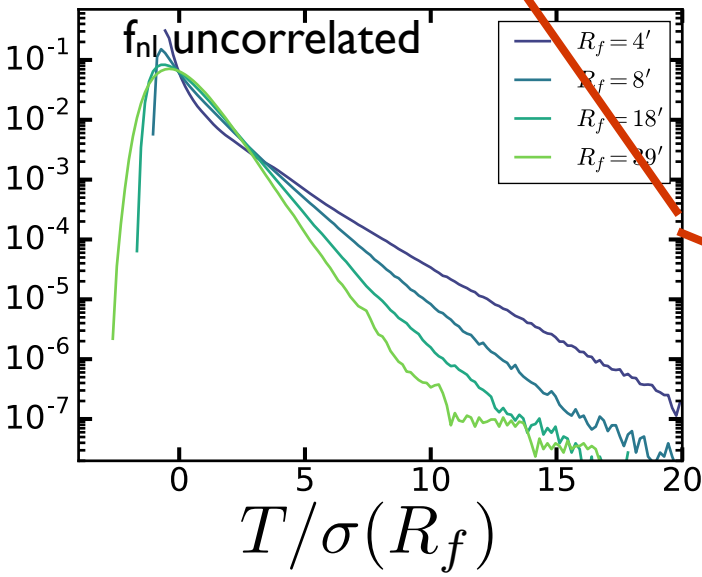


# Primordial Non-Gaussianity in CO

$P(T; R_f)$



$P(T; R_f)$



# Summary

CO at high redshift is complicated to model

- highly correlated with star formation

To **extract cosmological information** we must fully understand:

- **Intrinsic Scatter**

- eg. SFR(Mass),  $L_{\text{CO}}(\text{SFR})$  - Li et al. 2016
- **Hydro Sims** - Lakhani, Hopkins, Stein, Murray, Bond, Alvarez

- **Cosmic Scatter**

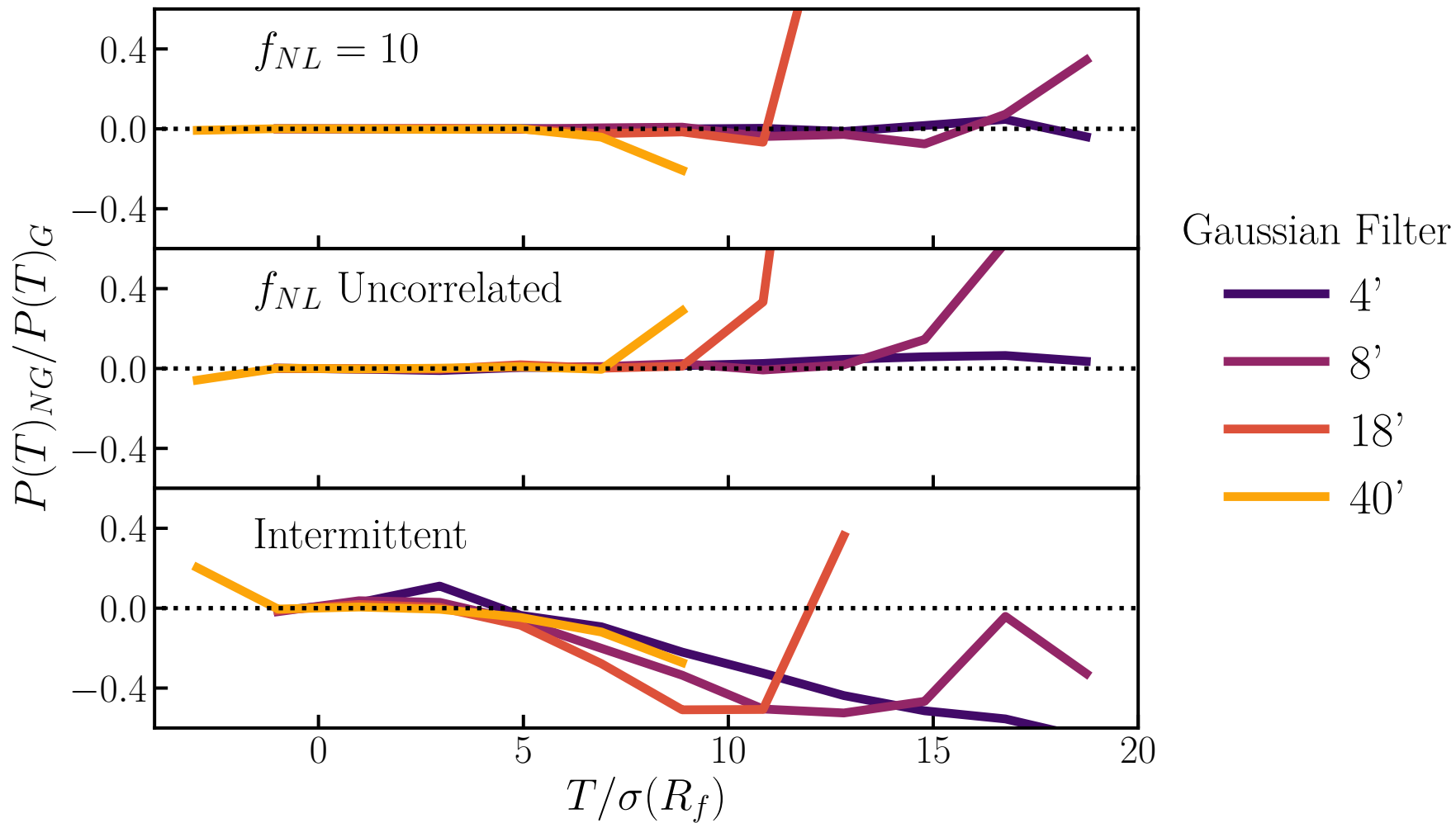
- COMAP fov subject to cosmic variance
- **Monte Carlo Peak Patch Sims** - Stein, Alvarez, Bond

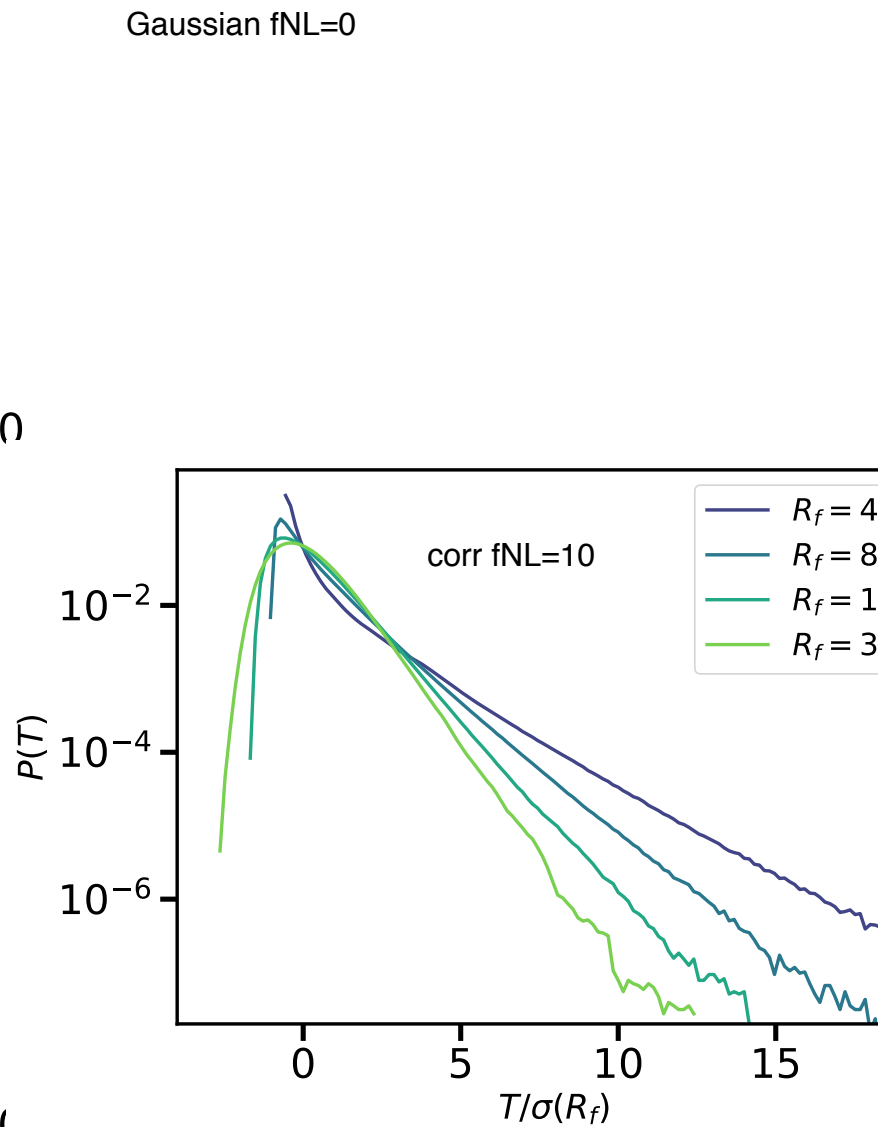
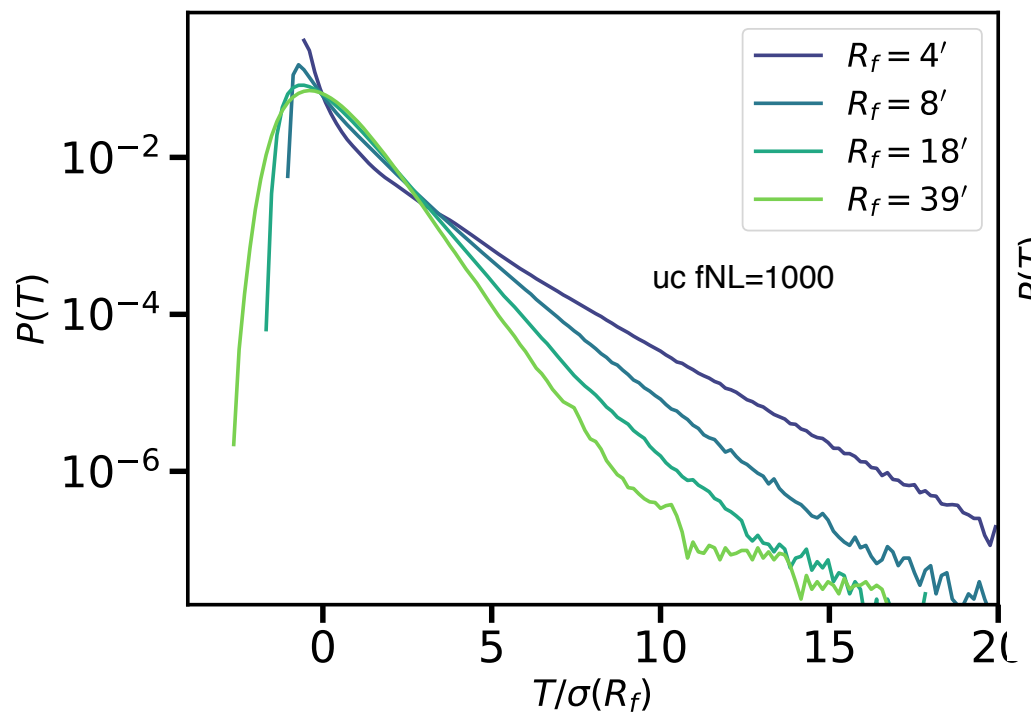
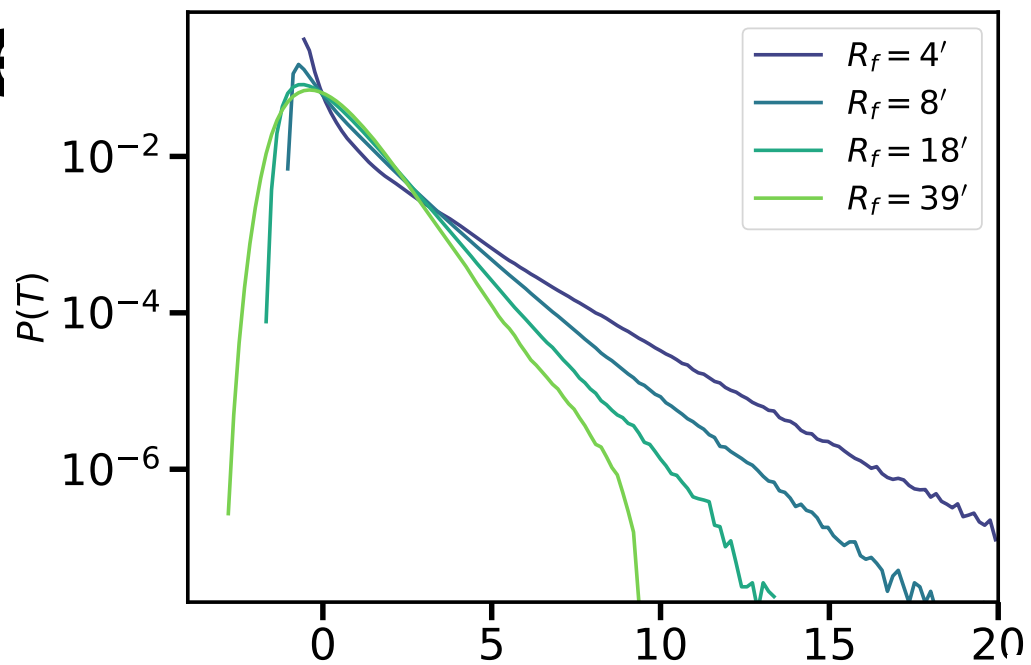
- **Beyond Powerspectrum**

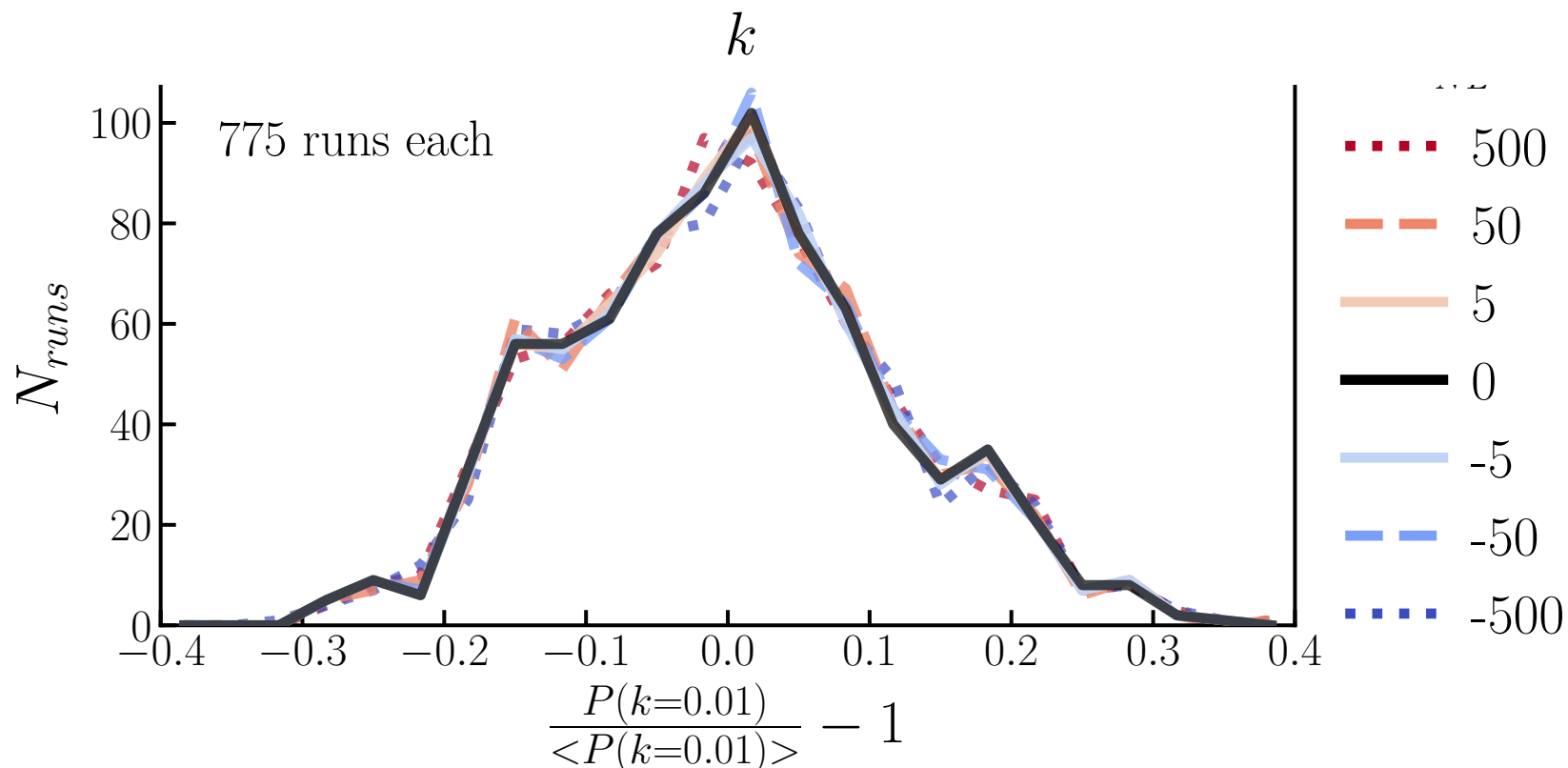
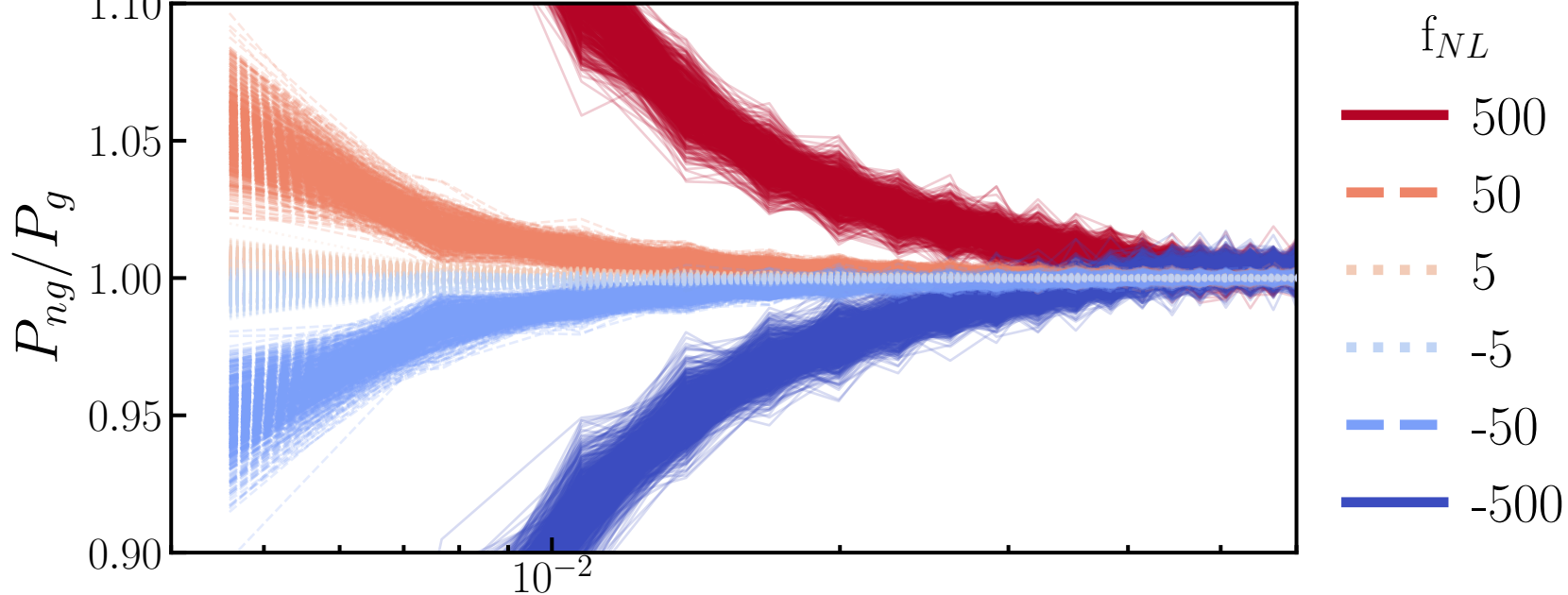
- VID analysis, line spectra, cross correlations, stacking, ...
  - Stein, Bond, Alvarez, Murray, Lakhani, Ihle, Kerr, et al.



# end



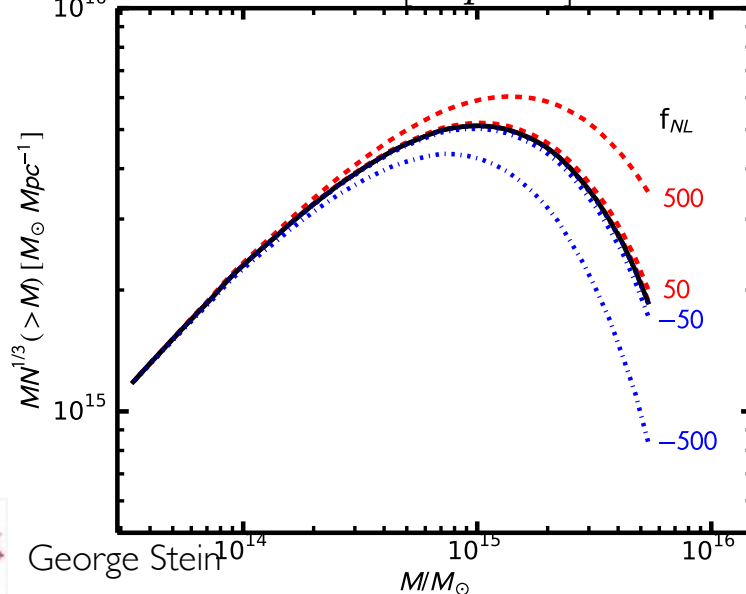
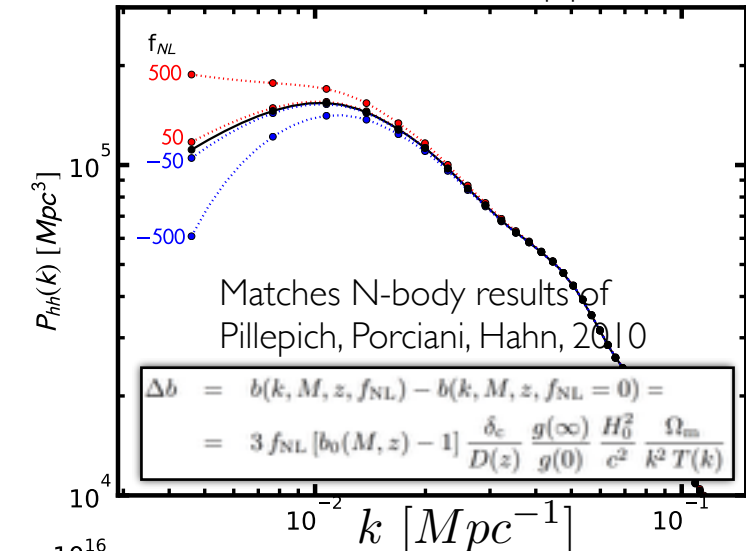


**er**

Add in:

## Primordial Non-Gaussianity

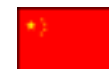
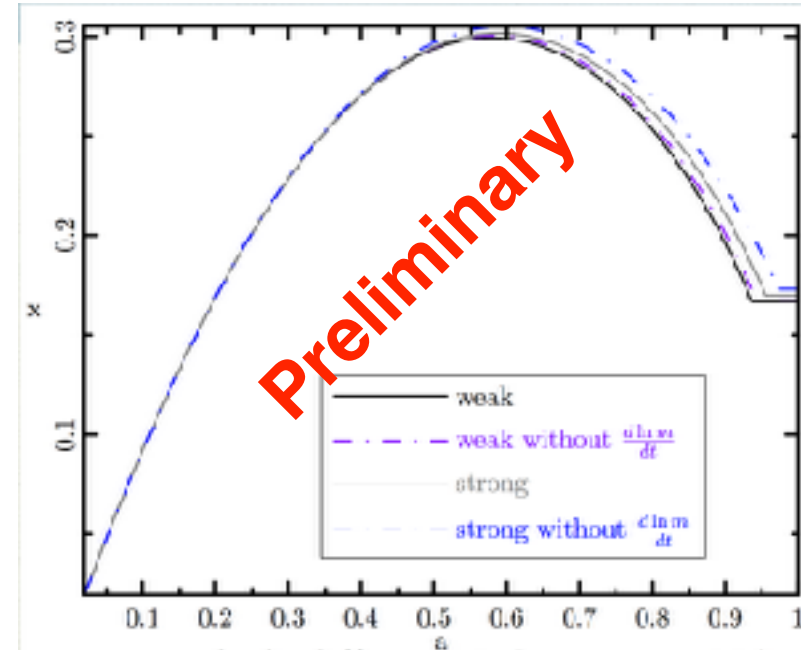
the Peak Patch method accurately reproduces the effects of primordial Non-Gaussianities  
 → Add to full mock pipeline



&

## Modified Gravity

The Effect of chameleon-like f(R) gravity On the dynamics of ellipsoidal collapse

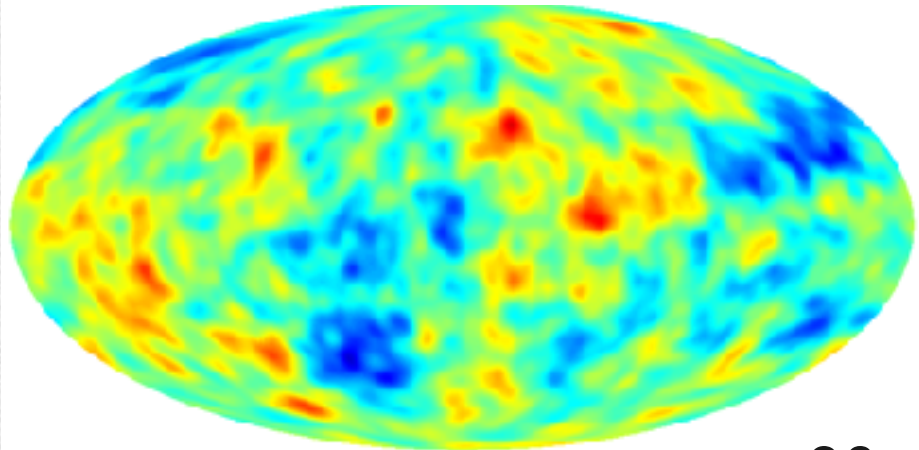


Emma Platts, Zhiqi Huang,  
Alex Lague



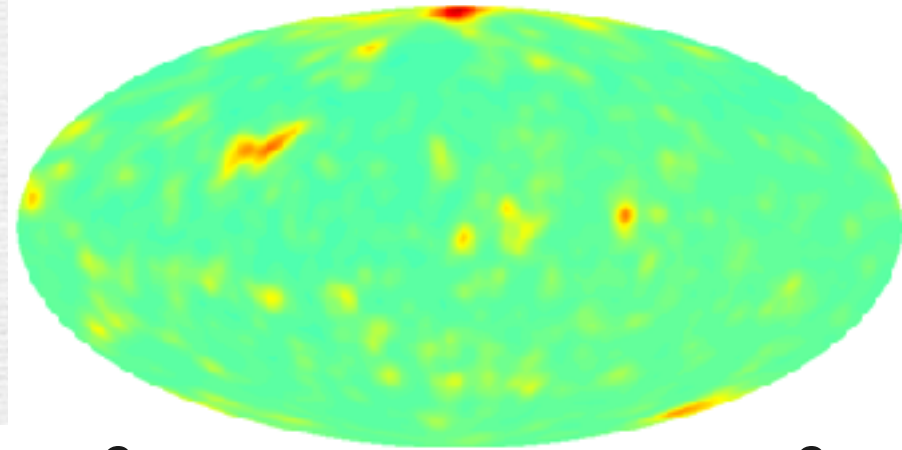
# CMB Example: Gravitational Potential Maps

Gaussian Component



-30 30

Intermittent Component

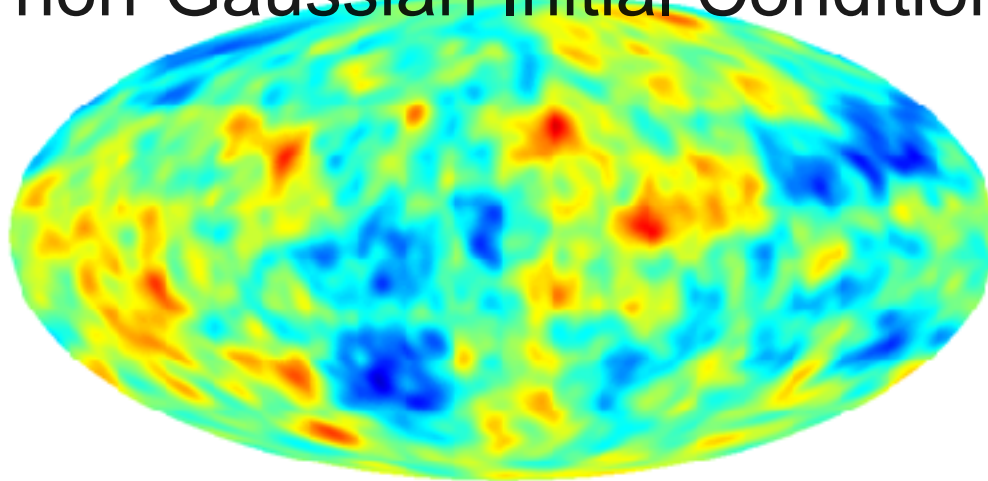


-6 6

+

non-Gaussian Initial Conditions

=



-30 30

Bond, Frolov, Huang,  
Kofman (2009)

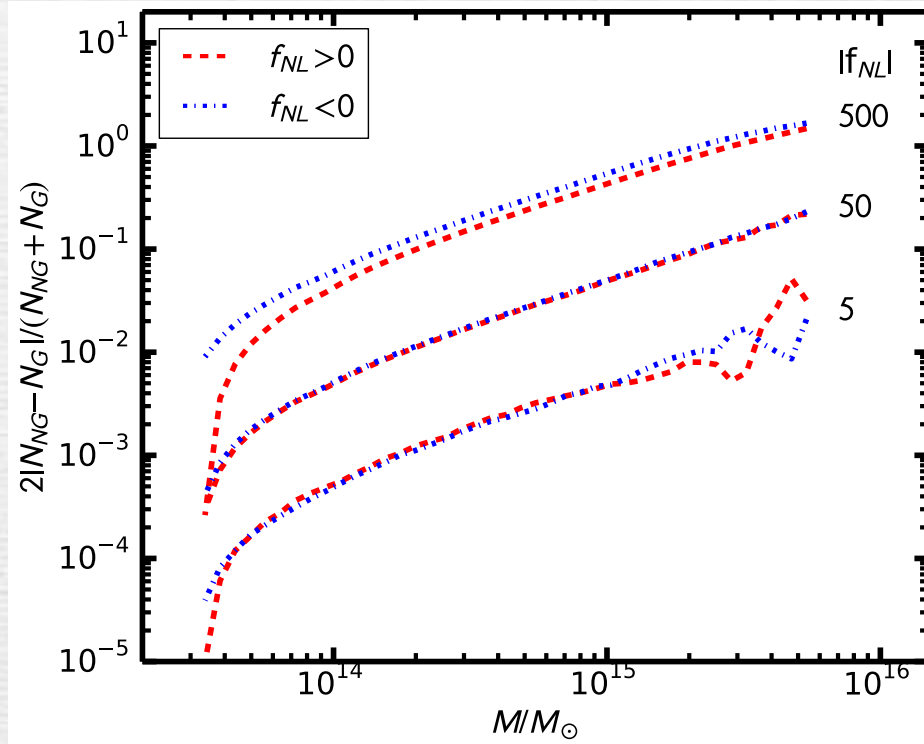
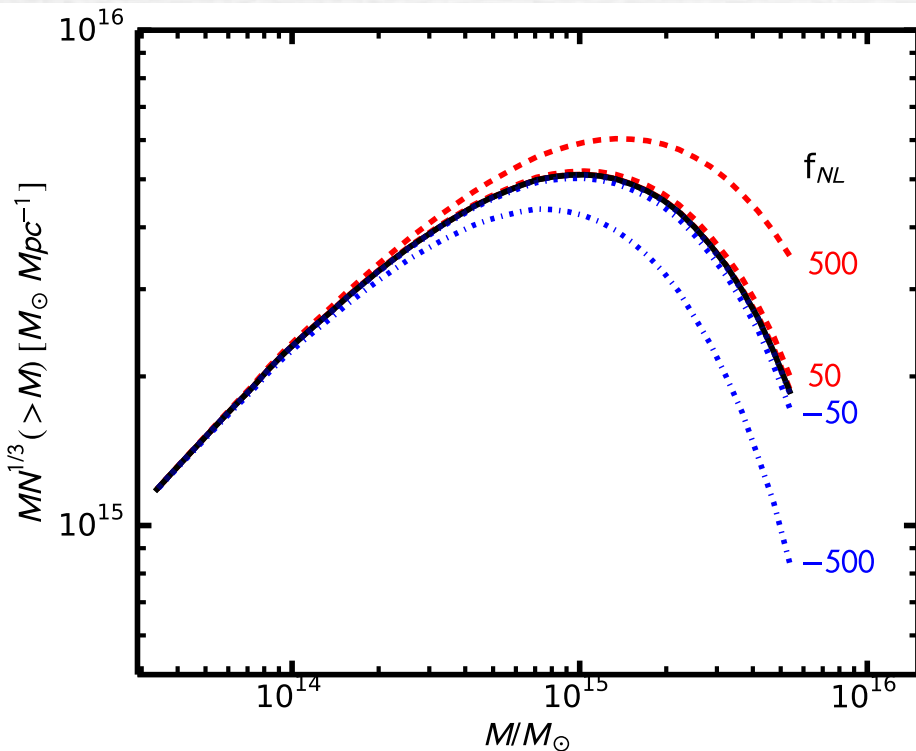




Halo Mass Function is strongly affected only for large  $f_{NL}$

Local  
non-Gaussianity  
 $\Phi(x) = \phi(x) + f_{NL}(\phi^2 - \langle \phi^2 \rangle)$

Peak Patch Sims: 2048 Mpc box,  $1024^3$  cells  
900 realizations, ~3 mins each on 64 cores

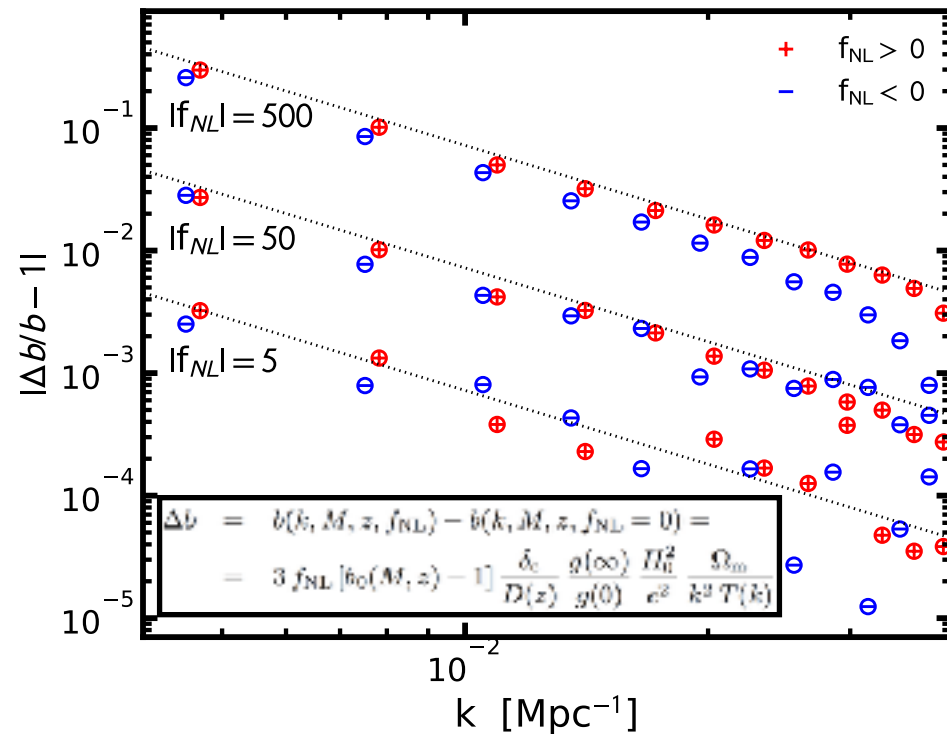
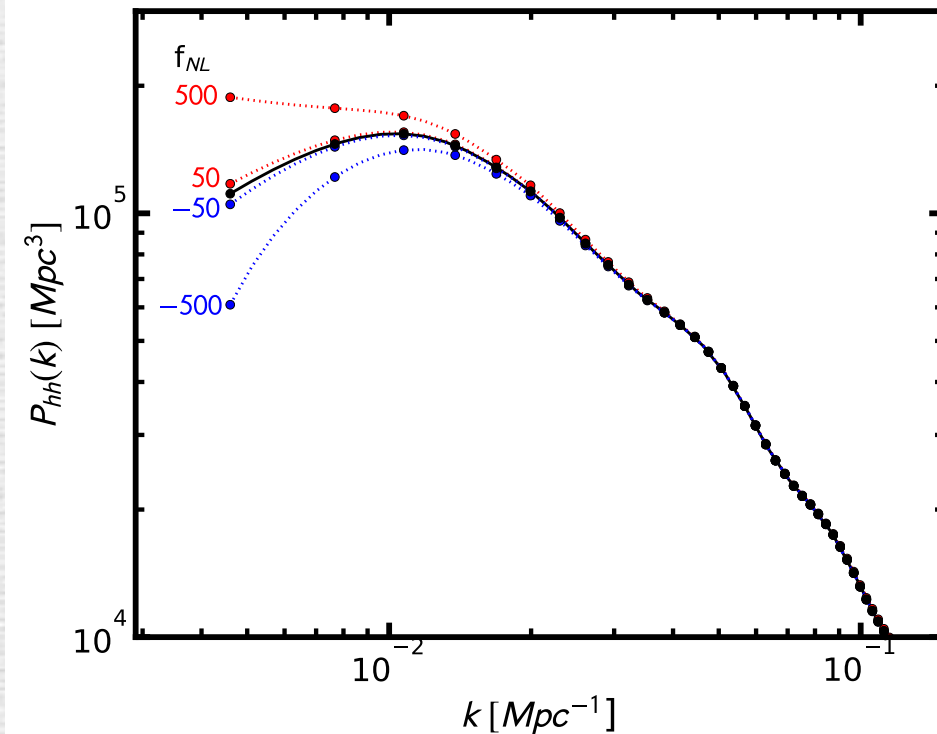


Instead look at **power spectrum**  
and **scale dependent bias**

# Local non-Gaussianity

$$\Phi(x) = \phi(x) + f_{NL}(\phi^2 - \langle \phi^2 \rangle)$$

Peak Patch Sims: 2048 Mpc box,  $1024^3$  cells  
900 realizations, ~3 mins each on 64 cores

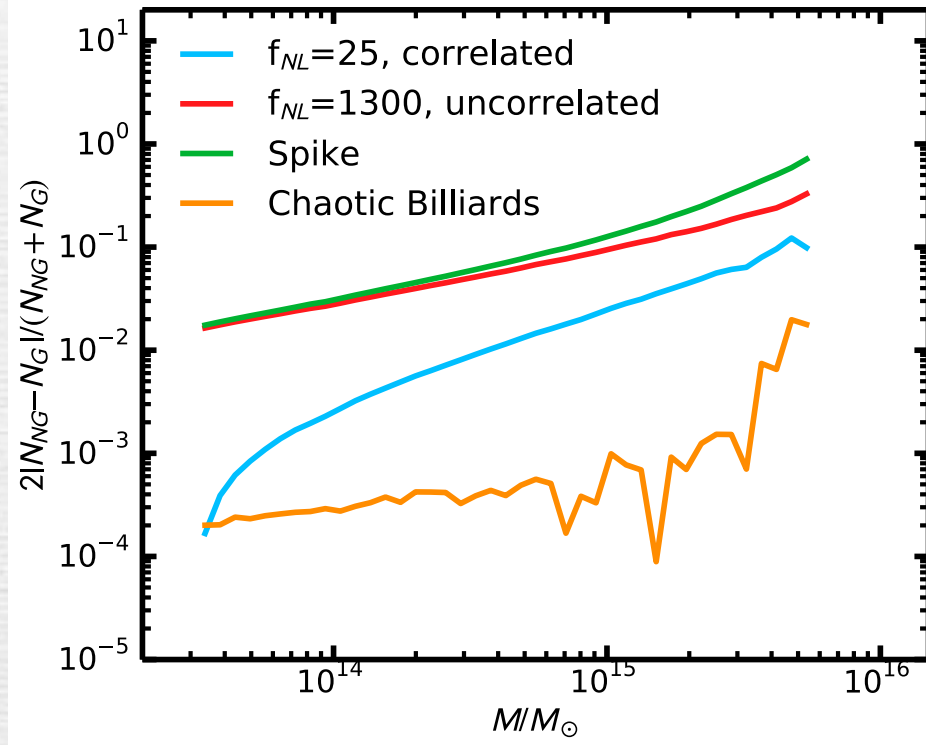
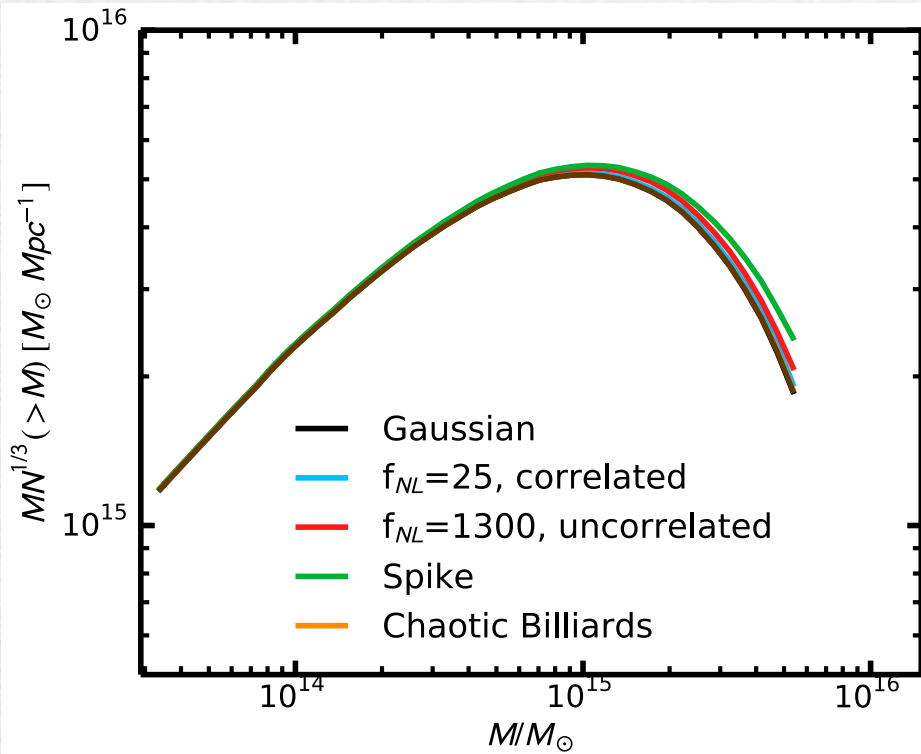


# Halo Mass Function is weakly affected for intermittent cases

# Intermittent non-Gaussianity

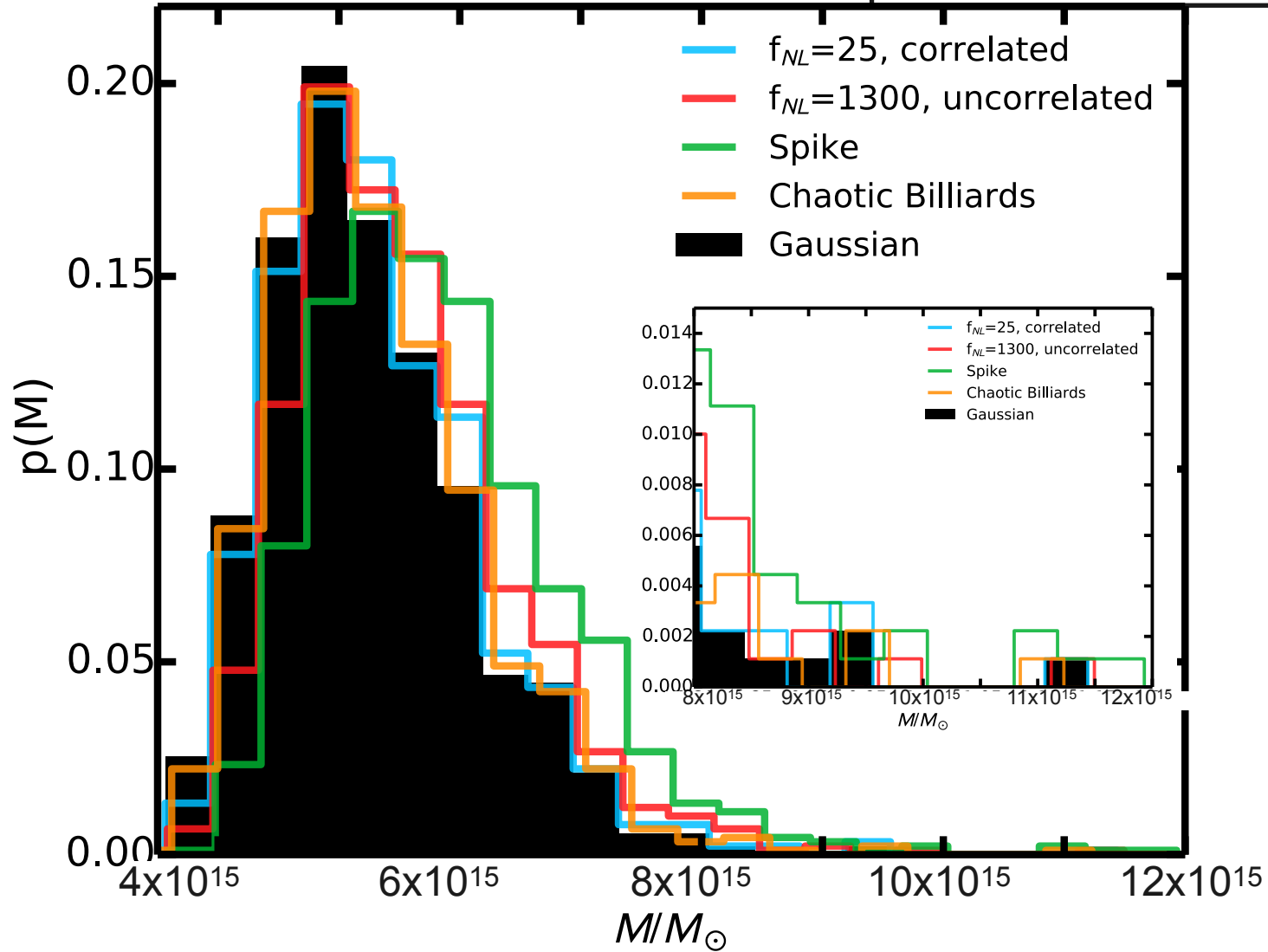
$$\zeta(x) = F_{NL}(\chi(x))$$

Peak Patch Sims: 2048 Mpc box,  $1024^3$  cells  
900 realizations, ~3 mins each on 64 cores



# Single Largest Halo Statistics Indeterminate

# Intermittent non-Gaussianity

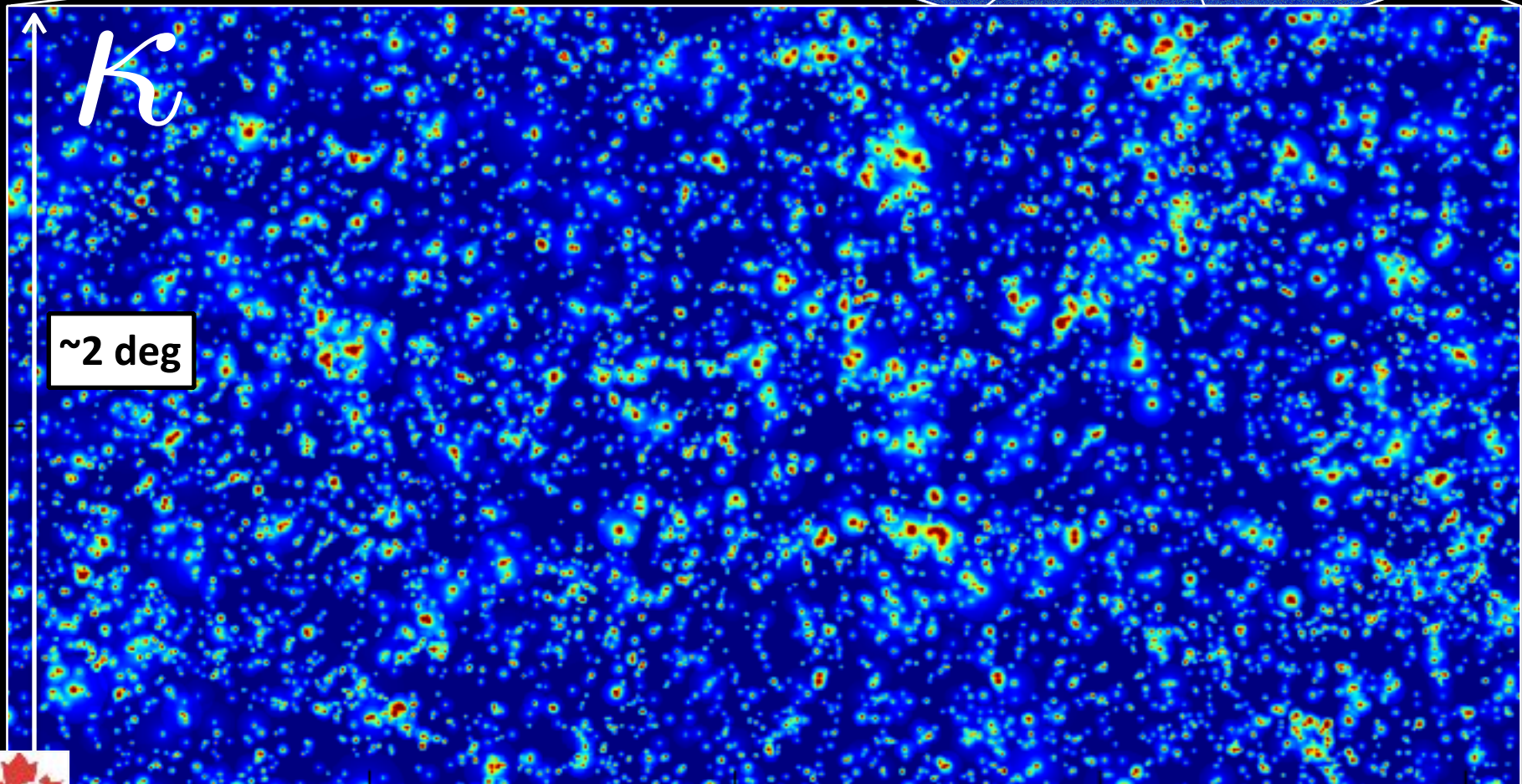


Combining LPT and Peak Patches  
"good enough" for lensing?

**CMB**

"Paint on" NFW + 2LPT Field  
= Lensing Convergence Map

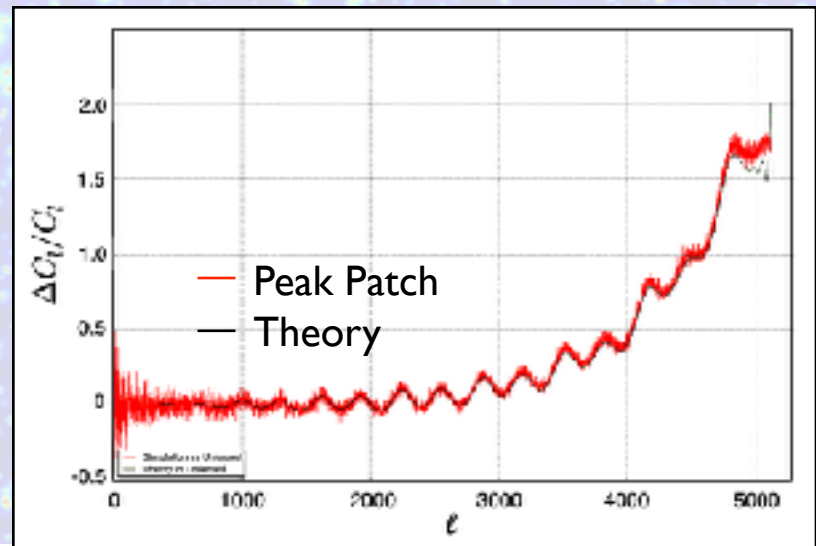
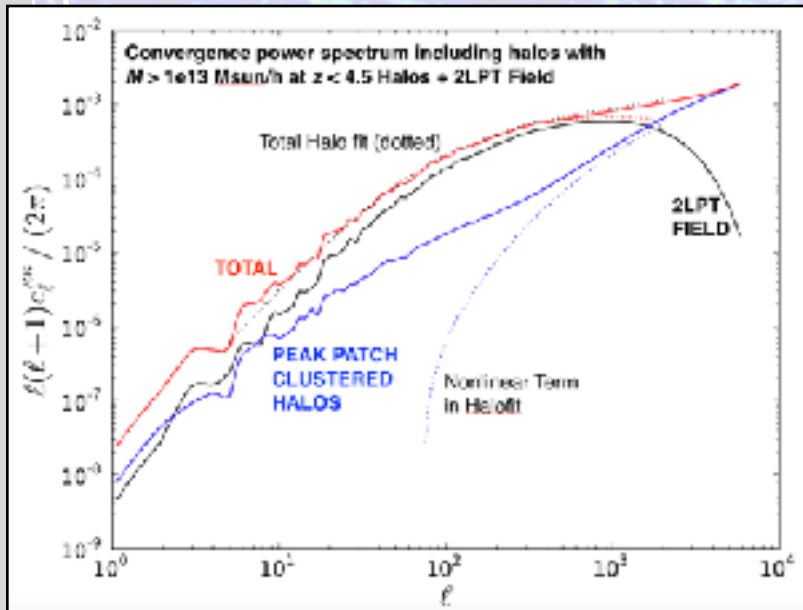
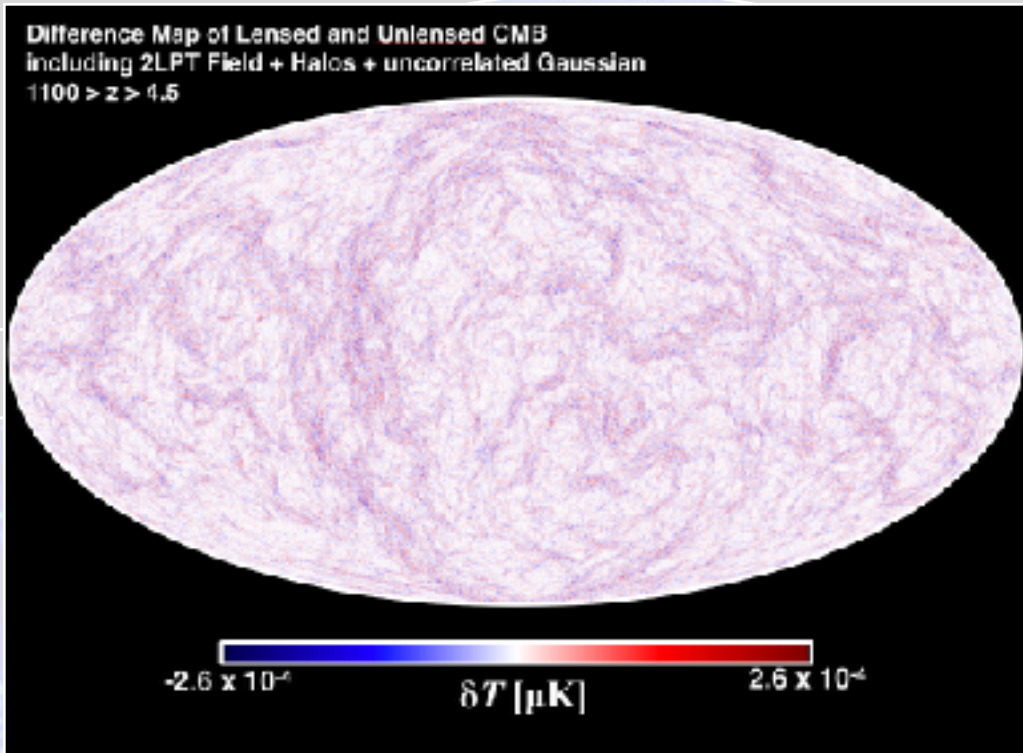
$z < 4.6$  light cone,  $8 \times 4096^3$  resolution  
= 8000 core hours  
300 available



Combining LPT and Peak Patches  
 “good enough” for lensing?

**CMB**

Modified Lenspix to read in our non-Gaussian Kappa maps



**end**

**end**



**end**

**end**

**end**

**end**

**end**