



the *theory* of the **Sunyaev-Zeldovich Probe of Gas in the Cosmic Web**

$\gamma + e \rightarrow \gamma + e$ Compton

$$\langle \Delta E_\gamma / E_\gamma \rangle = 4T_e / m_e c^2 - E_\gamma / m_e c^2$$

$$\langle (\Delta E_\gamma / E_\gamma)^2 \rangle = 2T_e / m_e c^2$$

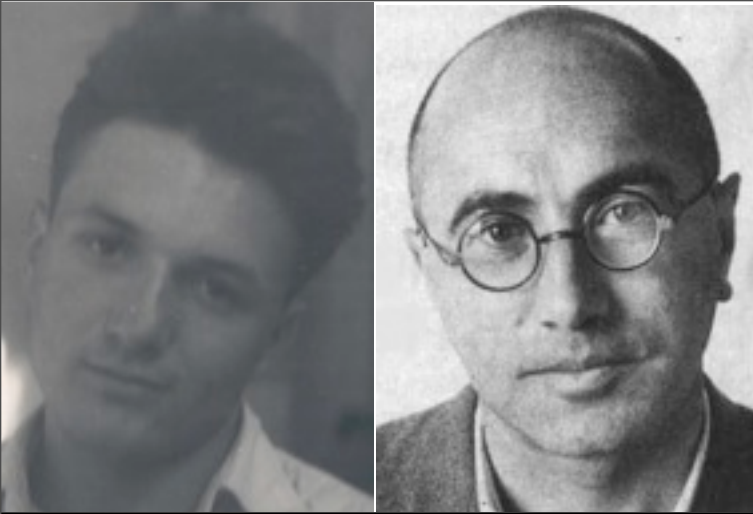
thermal SZ: $\Delta T / T = \mathbf{y} * (x(e^x + 1) / (e^x - 1) - 4)$, $x = h\nu / T_\gamma$

$$\mathbf{y} = \int n_e (T_e - T_\gamma) / m_e c^2 \sigma_T d\mathbf{l} \sim \int \mathbf{p}_e d\text{line-of-sight}$$

Compton \mathbf{y} -parameter

kinetic SZ: $\Delta T / T = \int n_e \mathbf{v}_{e\parallel} / c \sigma_T d\mathbf{l} \sim \int \mathbf{J}_e \cdot d\mathbf{r}$

$$\int \mathbf{k} \mathbf{SZ}(\theta, \varphi) d\Omega \sim \mathbf{M}_{\text{gas}} \mathbf{V}_{\text{bulk}} / D_A^2$$

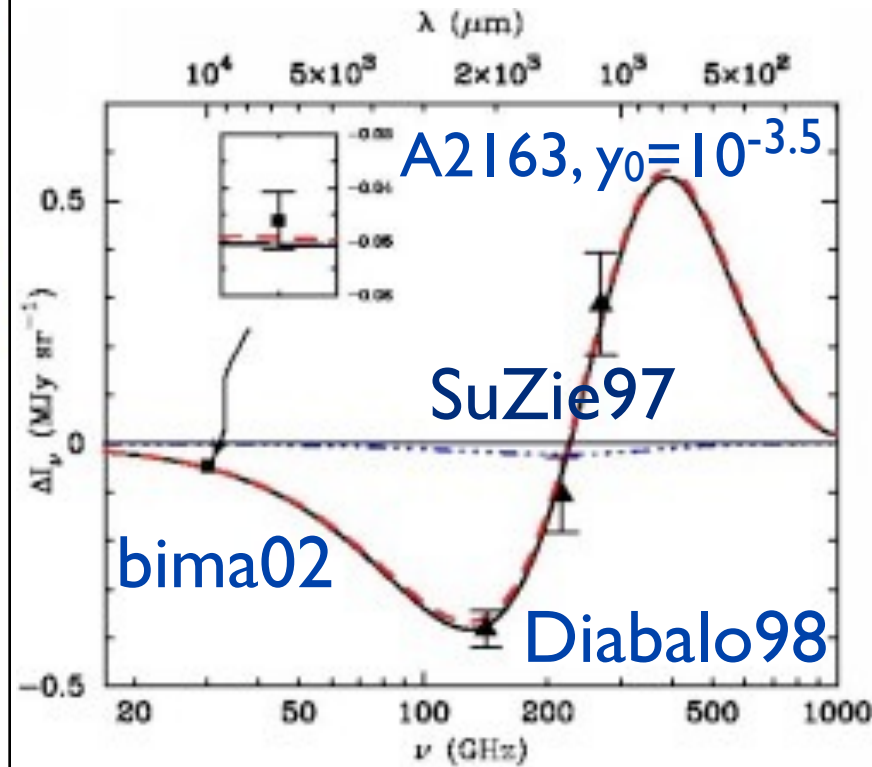
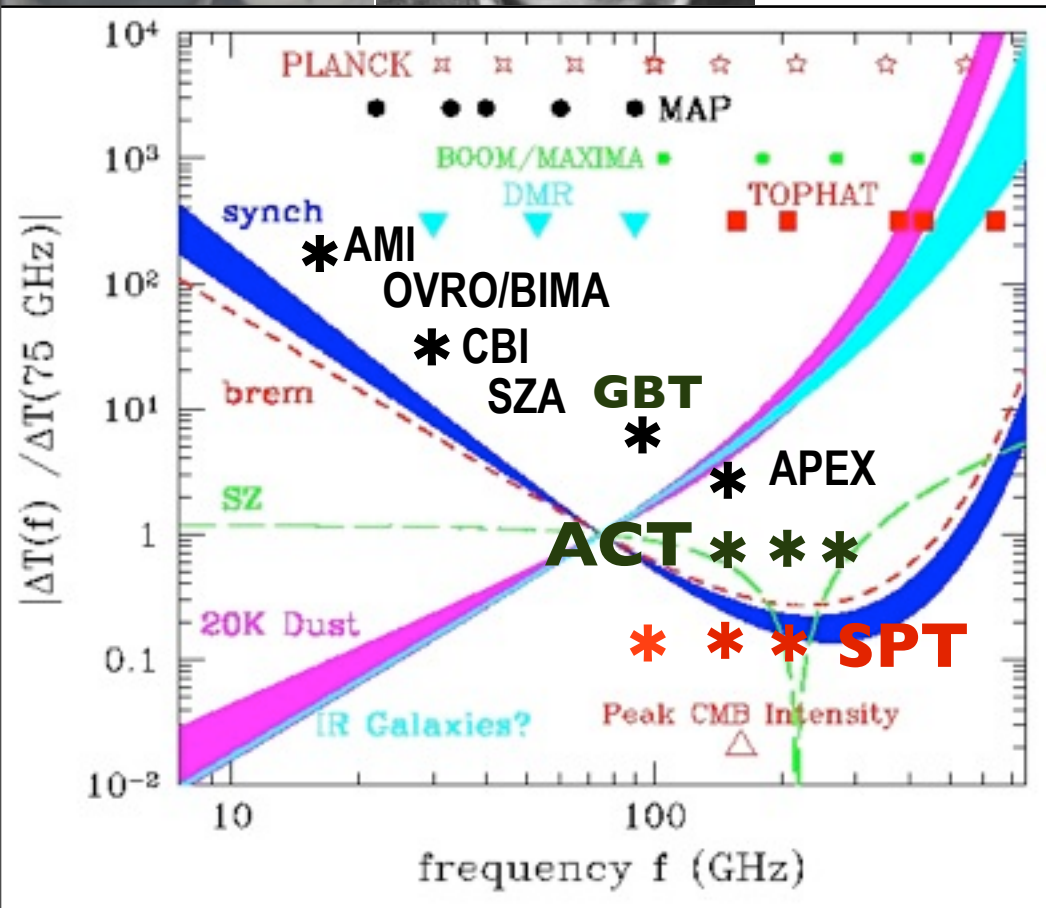


the theory of the **Sunyaev-Zeldovich Probe of Gas in the Cosmic Web: $\gamma \sim \int p_e$ dline-of-sight**

$$\Delta T/T = \gamma * (x(e^x + 1)/(e^x - 1) - 4), \quad x = hv/T_\gamma$$

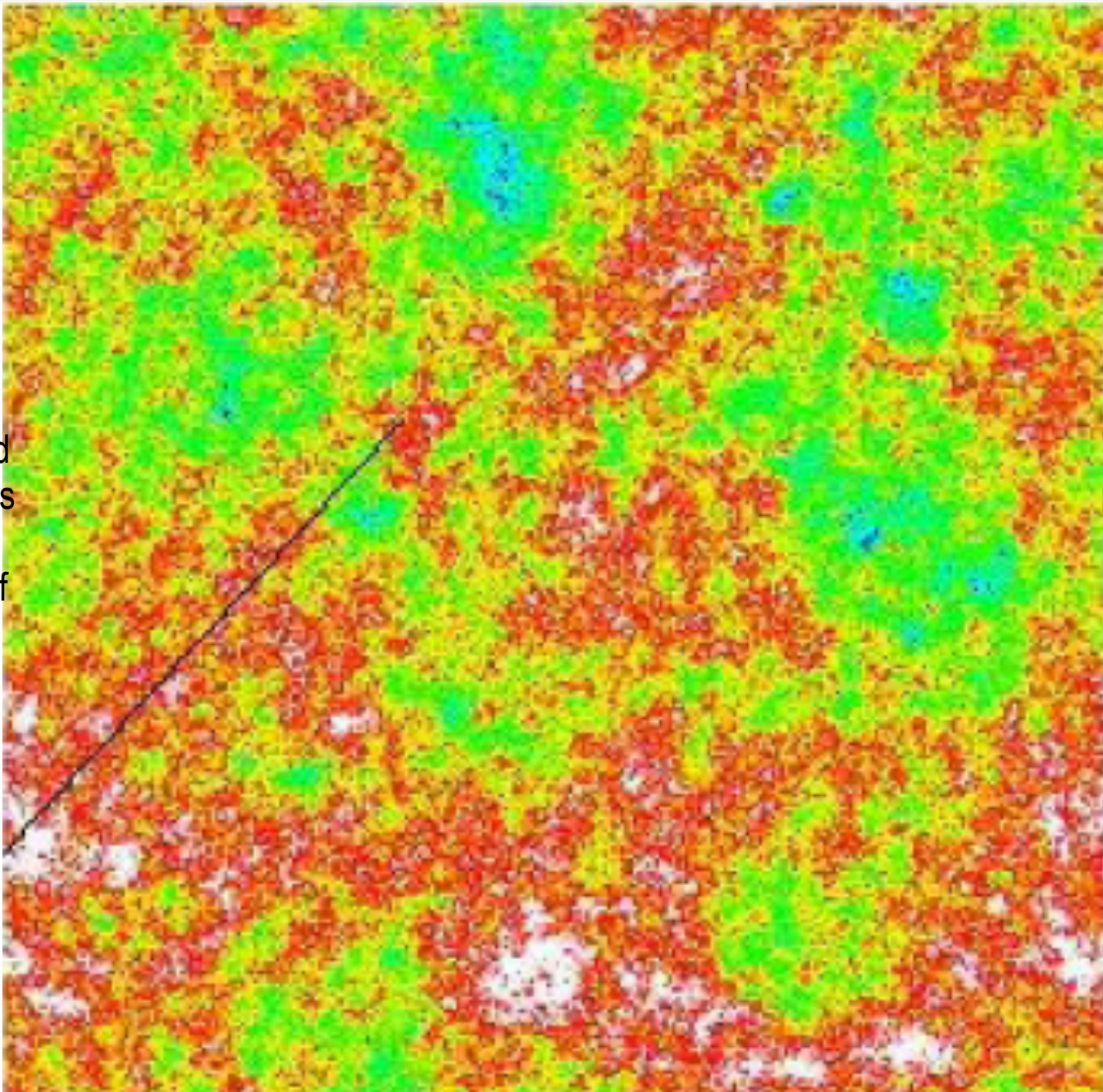
$$= -2\gamma \text{ to } x\gamma, \quad 0 \text{ @ } \nu = 217 \text{ GHz}$$

$$\Delta I_\nu = \Delta T/T * x^4 e^x / (e^x - 1)^2$$



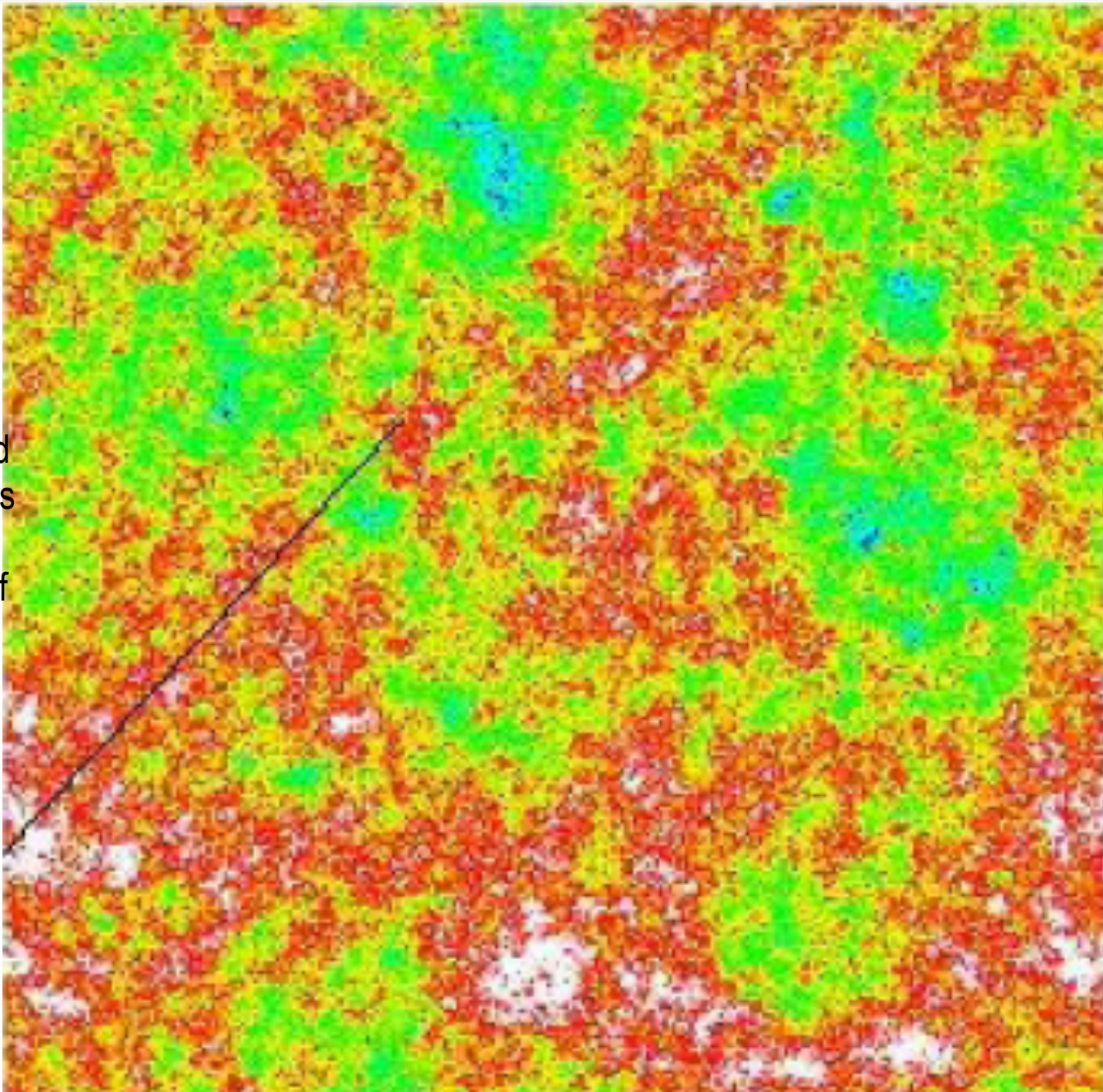
fluctuations in the early universe “vacuum” grow to *all* structure

scalar field
fluctuations
in the
vacuum of
the ultra-
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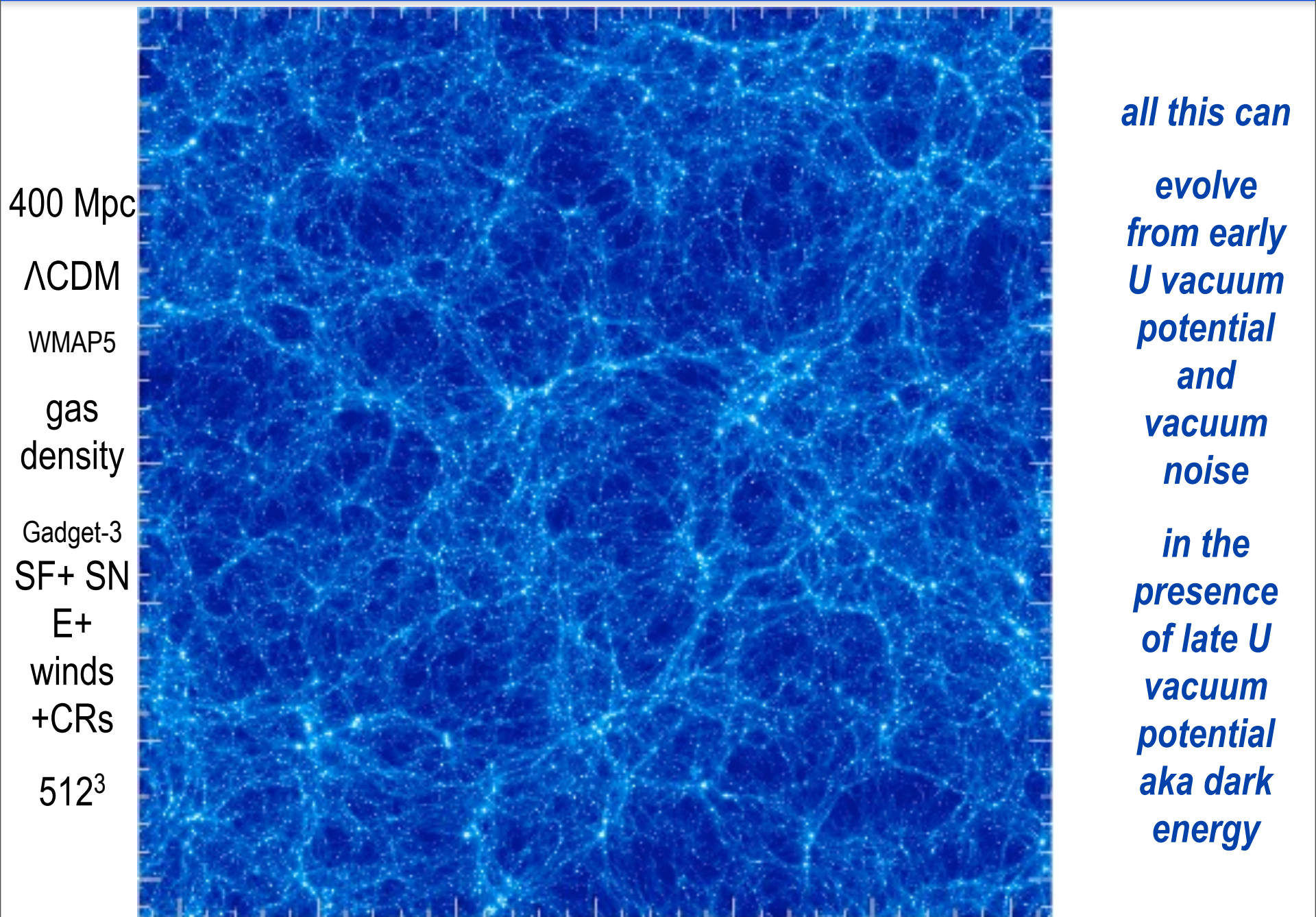
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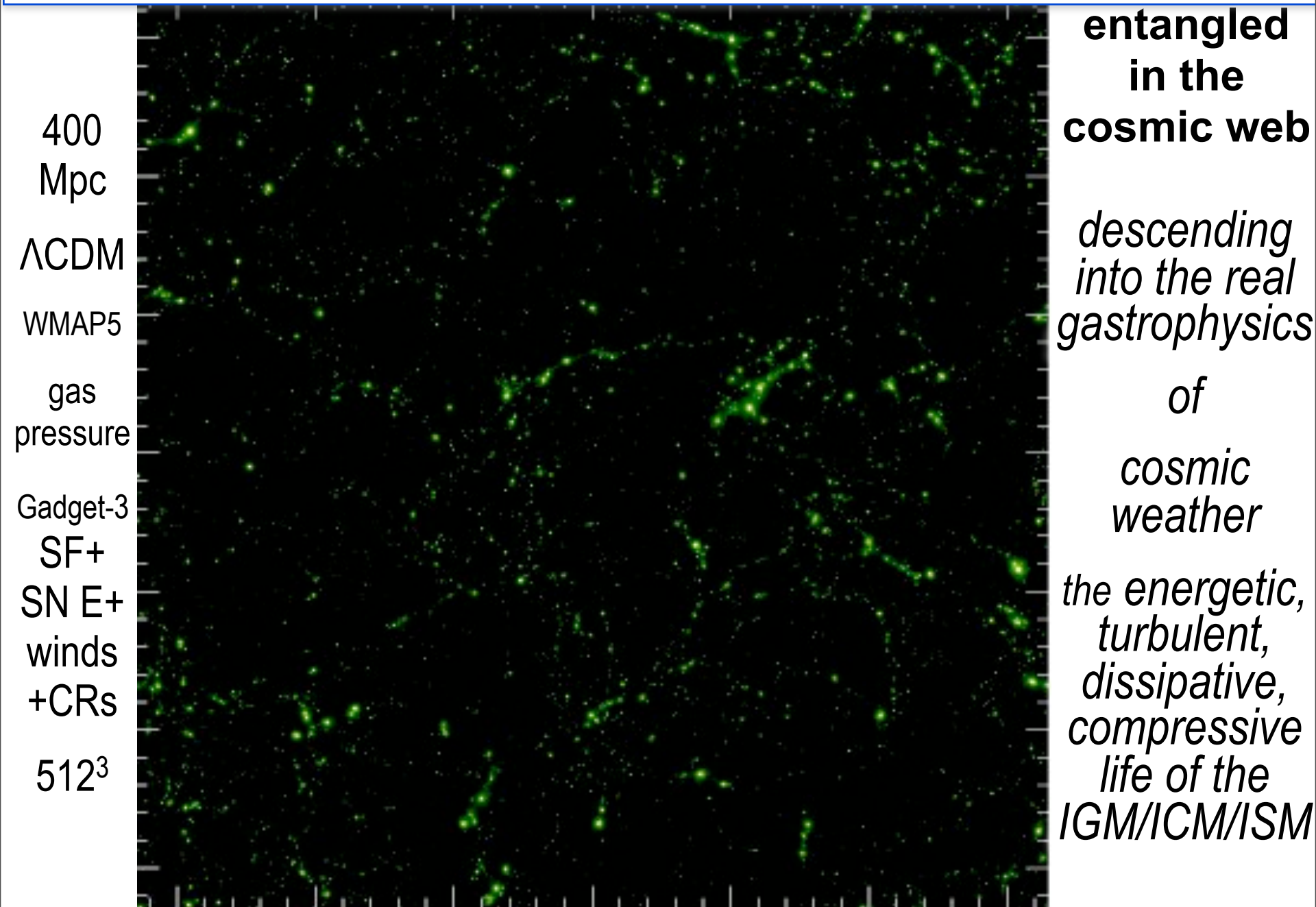
*evolve
from early
U vacuum
potential
and
vacuum
noise*

fluctuations in the early universe “vacuum” grow to *all* structure



*all this can
evolve
from early
U vacuum
potential
and
vacuum
noise
in the
presence
of late U
vacuum
potential
aka dark
energy*

pressure intermittency in the cosmic web, in cluster-group concentrations probed by tSZ





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$$\gamma = \int n_e (T_e - T_\gamma) / m_e c^2 \sigma_T d\text{los} \sim \int \mathbf{p}_e \text{ dline-of-sight}$$

Compton γ -parameter

$$\mathbf{Y}_\Delta = \int \mathbf{y}(\theta, \varphi) d\Omega \sim \mathbf{E}_{\text{th}} / D_A^2 \sim (\mathbf{E}_{\text{grav}} - 3\mathbf{P}_{\text{kinetic, etc}} V + 3\mathbf{P}_s V) / 2 D_A^2$$

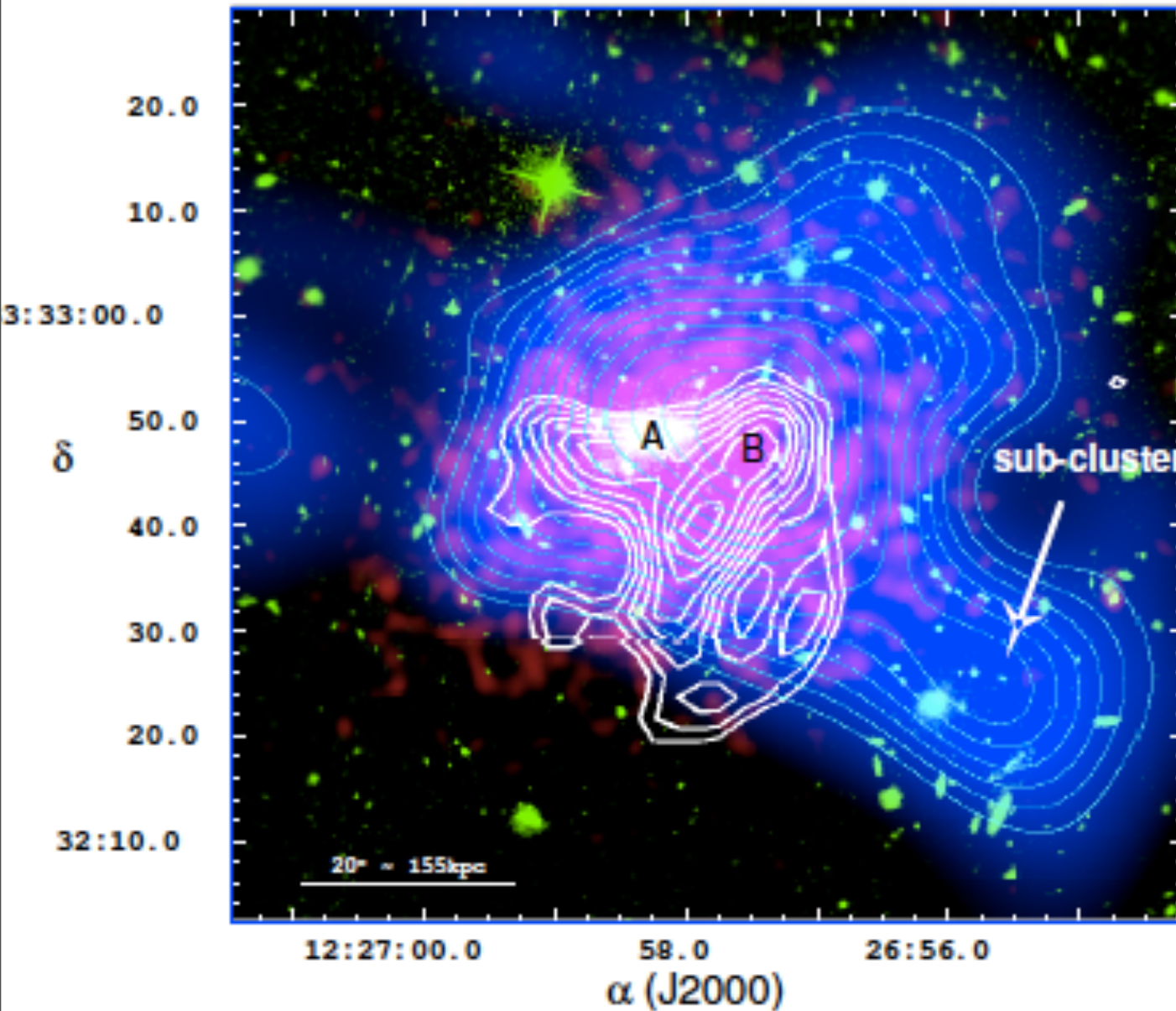
VIRIAL THEOREM: $\mathbf{E}_{\text{grav}} \sim GM_g M / R \sim M^{5/3}$ dark matter dominated

kinetic SZ: $\Delta T / T = \int n_e \mathbf{v}_{e\parallel} / c \sigma_T d\text{los} \sim \int \mathbf{J}_e \cdot d\mathbf{r}$

$$\int \mathbf{k} \mathbf{SZ}(\theta, \varphi) d\Omega \sim \mathbf{M}_{\text{gas}} \mathbf{V}_{\text{bulk}} / D_A^2$$

Mustang on GBT 90 GHz 64 bolometer array Imaging SZ

@~10'' res 4 cls 2010, ~25 Hubble CLASH cls to come Devlin, Mason, ...



CL1226 $z=0.89$

Red Chandra

Blue/cyan weak lens Σ

Green optical

White MUSTANG SZ $>3\sigma$

A BCG ~ X-ray peak

B Dark Matter peak

~ lobe of SZ ridge

Mustang on GBT 90 GHz 64 bolometer array Imaging SZ

@~10" res 4 cls 2010, ~25 Hubble CLASH cls to come Devlin, Mason, ...

future: High-Res SZ sim for MUSTANG2

now: CL1226 z=0.89

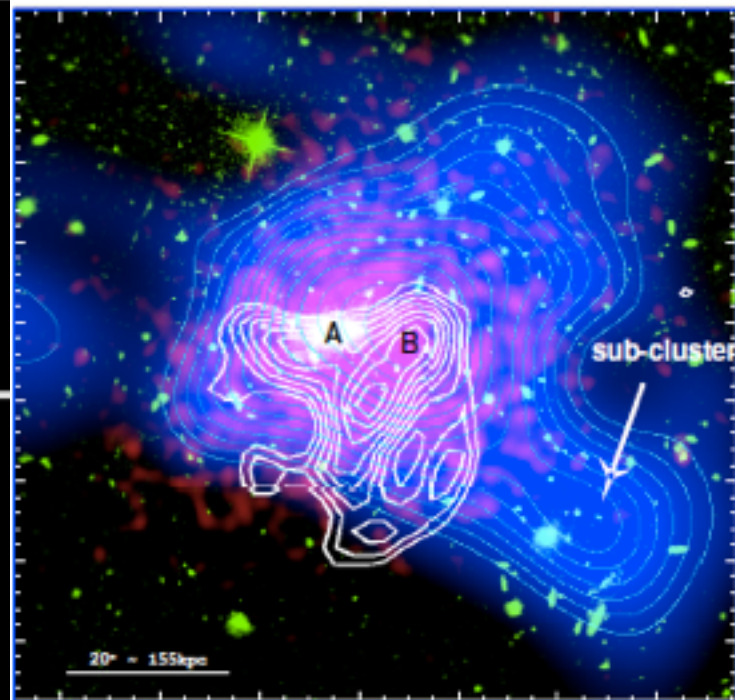
input cluster: $M_{500}=5.4e14$, $z=0.7$

GBT-beam 0.15'

SPT-beam 1'

SZA@30 GHz beam

<= Planck beam at 150 GHZ =>



12:27:00.0 58.0 26:56.0
 α (J2000)

Red Chandra

Blue/cyan weak lens Σ

Green optical

White MUSTANG SZ $>3\sigma$

A BCG ~ X-ray peak

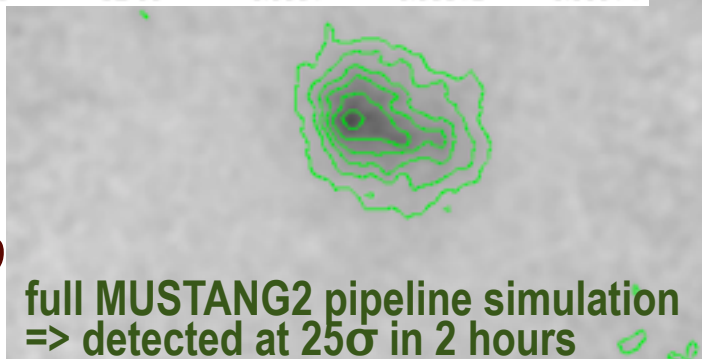
B Dark Matter peak

~ lobe of SZ ridge

100x mapping speed!
160 cf. 64 pixels, over larger area (5' vs. 40")

=> Planck followup to 35σ in 1hr

full MUSTANG2 pipeline simulation
=> detected at 25σ in 2 hours



Delta T over Tea Toronto May 1987: first dedicated CMB conference, exptalists +theorists, primary+secondary $\Delta T/T$

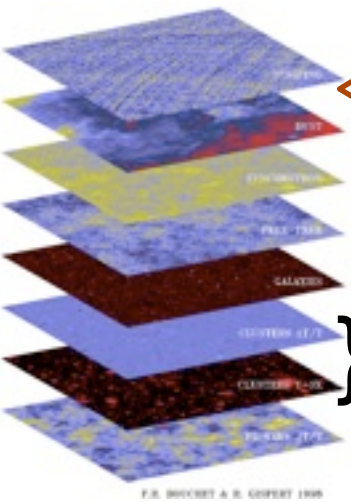
- very small angle anisotropies - VLA results, secondary fluctuations via the Sunyaev-Zeldovich effect, primeval dust emission, and radio sources
 - small angle anisotropies - current results, optimal measuring strategies, statistical methods for + effect of energy injection / explosions on LSS- a big pre-COBE forecast issue = feedback
- bond@ $\Delta T/Tea87$: "clustered shots" (aka halos aka bbks86-peaks) with spherical pressure profiles - via binding energy (not mass) but beta-profiles with core scaling and old X-ray beta's

BUT spherical collapse - too many cls & non-dynamical masses - high M 's too low \Rightarrow peak patches BM91-96 tidal fields - virial mass from homogeneous ellipsoid dynamics, accurate cluster positions, masses, binding energies, clustering

e.g, application to Planck sims 90s, CBI, AMIBA, ..

constrained supercluster tree PM-SPH sim of Λ CDM +cooling: largest k-range of its time (\gg Virgo sim) SZ in supercls may give us the outskirts of cls & gps, not filaments (unless \exists large gas E-outflows) B+Kofman+Pogosyan+Wadsley 97/99

painting halos with analytic Y_{SZ} & pressure form factors 2002-11 cf. SPH-hydro (Gadget/Gasoline, MMH, ENZO, ART 2001-11; ITP cluster test 96-00): discrepancy from 2002: big issue was/is: Δ 200 to 20, non-thermal KE/Eth



What sort of objects in the cosmic web dominate the SZ effect?

$\Delta_{cut} = 200, 120, 60, 20$ then convergence, pick up far-field of clusters and groups, + a little into filaments (unless \exists large gas E-outflows into filaments)

What is the redshift range that contributes to the SZ effect?

all from 0 to ~ 2 half $\langle C_L^{SZ} \rangle 3000$ from $z > 0.5$ & $M < 3 \times 10^{14} M_{\odot} h^{-1}$

CITA-SZ with feedback: Battaglia, Bond, Pfrommer, Sievers & Sijacki 2010, BBPS 2011a,b,c
for ACT+SPT+Planck et al, urgent to show the cluster-theory-variance as effects are added
07 goal large treePM-sph sims ($\sim 1000^3$ gas+DM)-NOT 08-11 goal 512^3 & 256^3 & single-hi-res-cl

shock heat only “adiabatic”; cool+SN E; cool + SN E + winds; **cool + SN E-feedback
+ winds + CRs from cluster shocks;**

but because of core overcooling and overproduction of stars, needed a subgrid
model of **AGN/starburst feedback in halo cores**, calibrated with the (small mass) cluster-BH
calculations of Sijacki (with Springel, Pfrommer, ...). **Feedback is the essence of Gastrophysical
Cosmology. Energy/Momentum driven winds, Relativistic injection.**

full Sijacki-resolution was/is \sim infeasible for single massive clusters, and certainly strongly
infeasible for big-box statistically useful samples, & also itself is just a subgrid model hence our
exploratory subgrid BH/Starburst feedback model

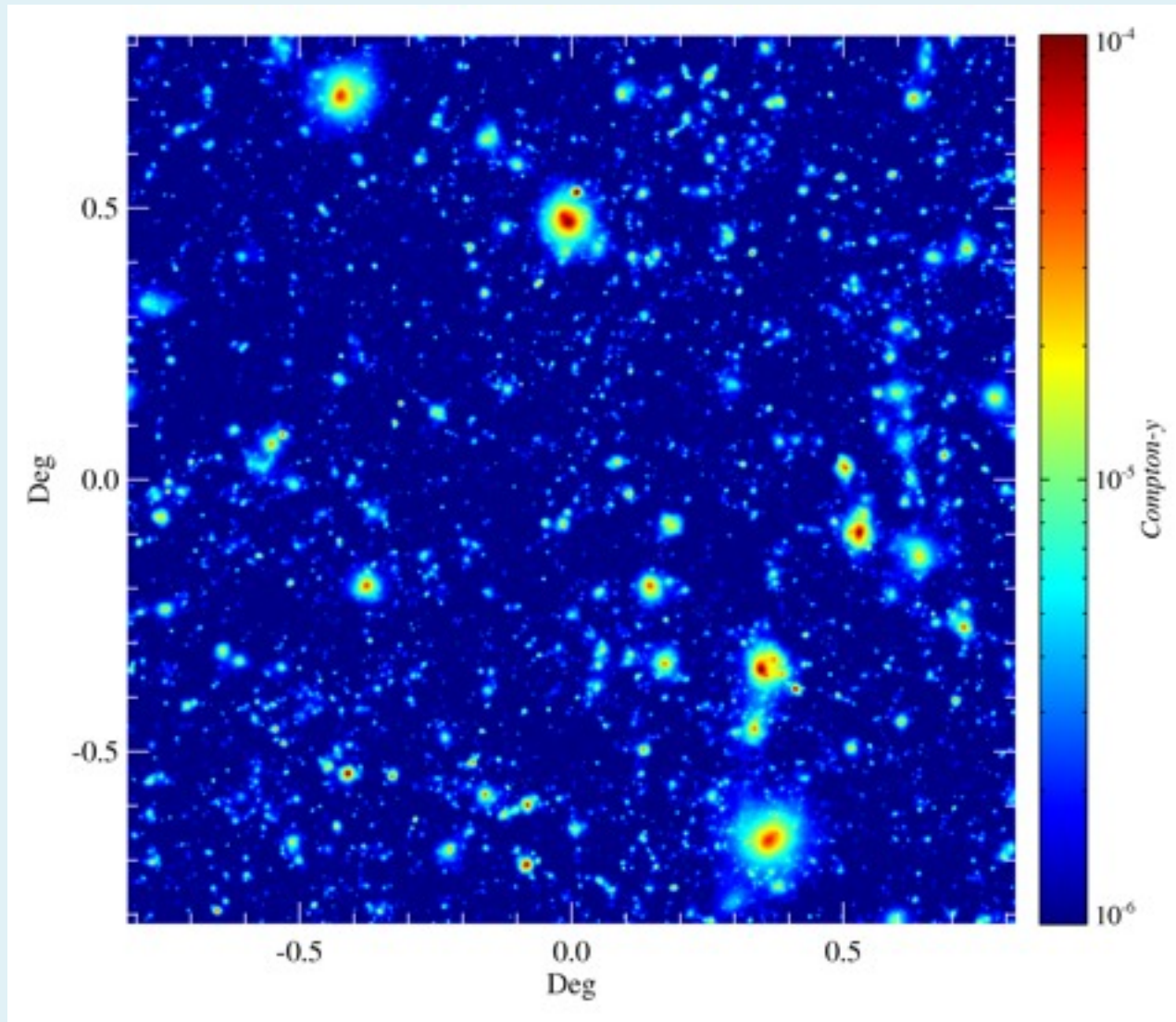
**AGN feedback + cool + SN E + winds: $\Delta E_{inj} \sim \epsilon \Delta t$ SFR over R_{AGN} in halo
centre, episodic above a SFR threshold, $\epsilon_{eff} < \epsilon$: most E_{inj} above $z=2$, so
much freedom to minimize ϵ_{eff} e.g., E_{inj} 58% at $z > 2$, 23% in $1 < z < 2$ 19% $z < 1$**

conclusion circa 2011: ~~A~~ universal panacea to cure cluster cores: highly inhomogeneous,
episodic and cluster-history-dependent. if observables are overly sensitive to this, then we become
gastrophysical weather reporters and not cosmological gold-sample miners delivering pure cosmic
parameters. **BUT most relevant SZ-region $\sim 0.5R_{500}$ to $\sim 3R_{200} \Rightarrow$ different non-thermal problems:**

**kinetic pressure aka “turbulence”, pressure/density clumping, asphericity, ... but we need
hydrodynamically-reasonable inner cores hence subgrid feedback (beware of cutouts of overcooled cores)
“every cluster is a bullet cluster” - or was a bullet**

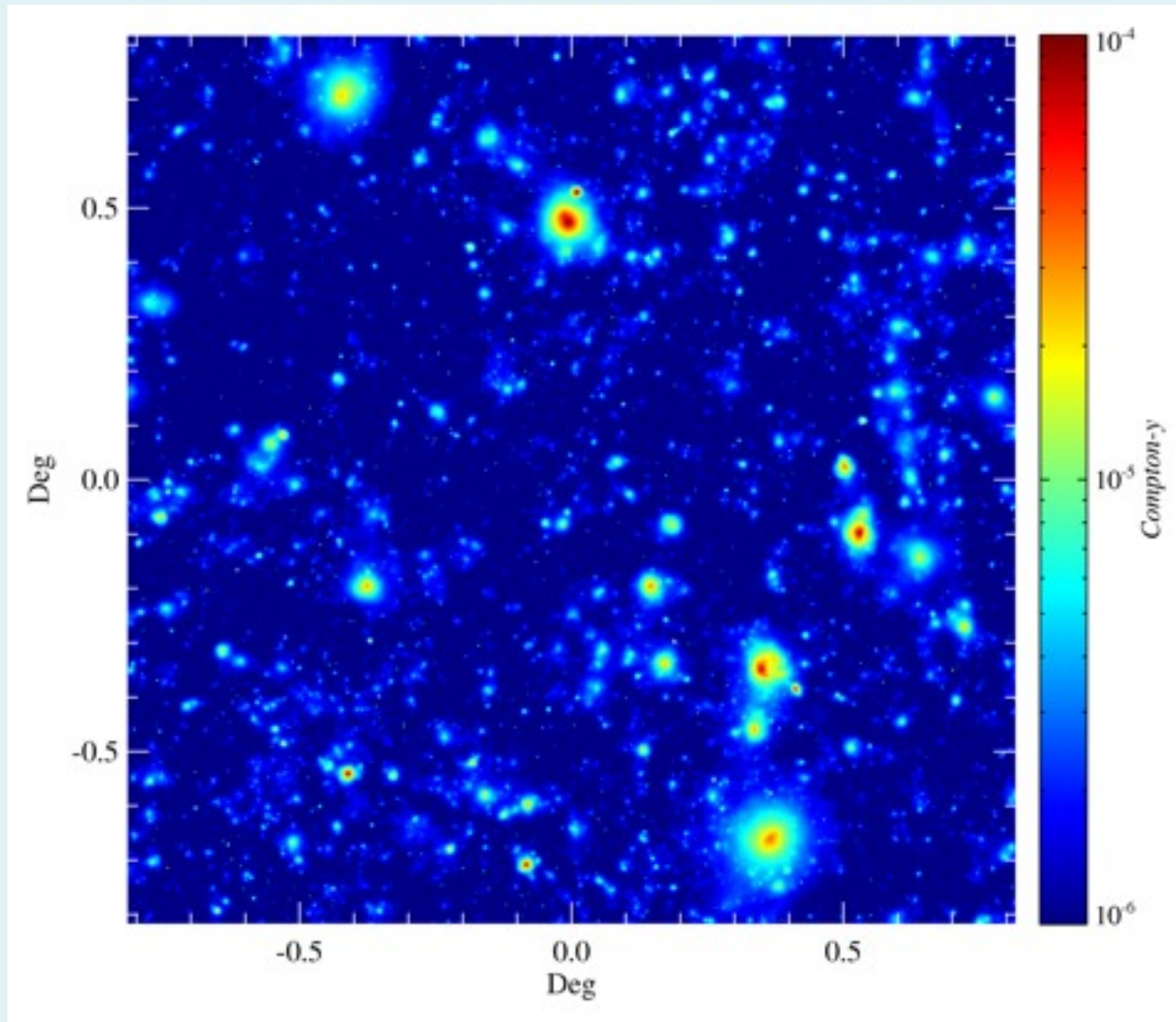
Compton-y map: “adiabatic”

= formation shock entropy from gravitational accretion only

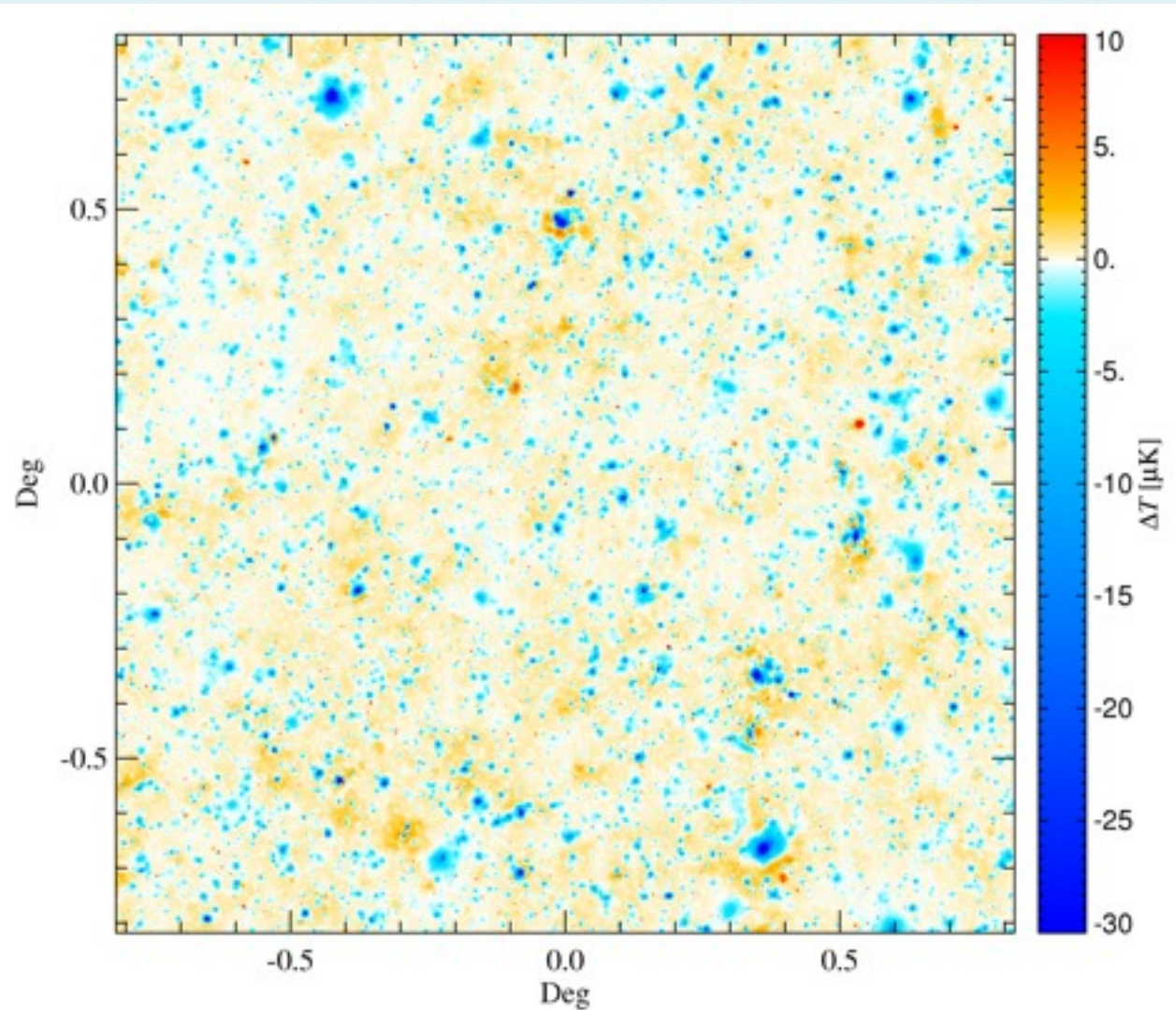


Compton- γ map: Feedback

= AGN or Starburst E-feedback + radiative cool + SN energy + wind + (CR)



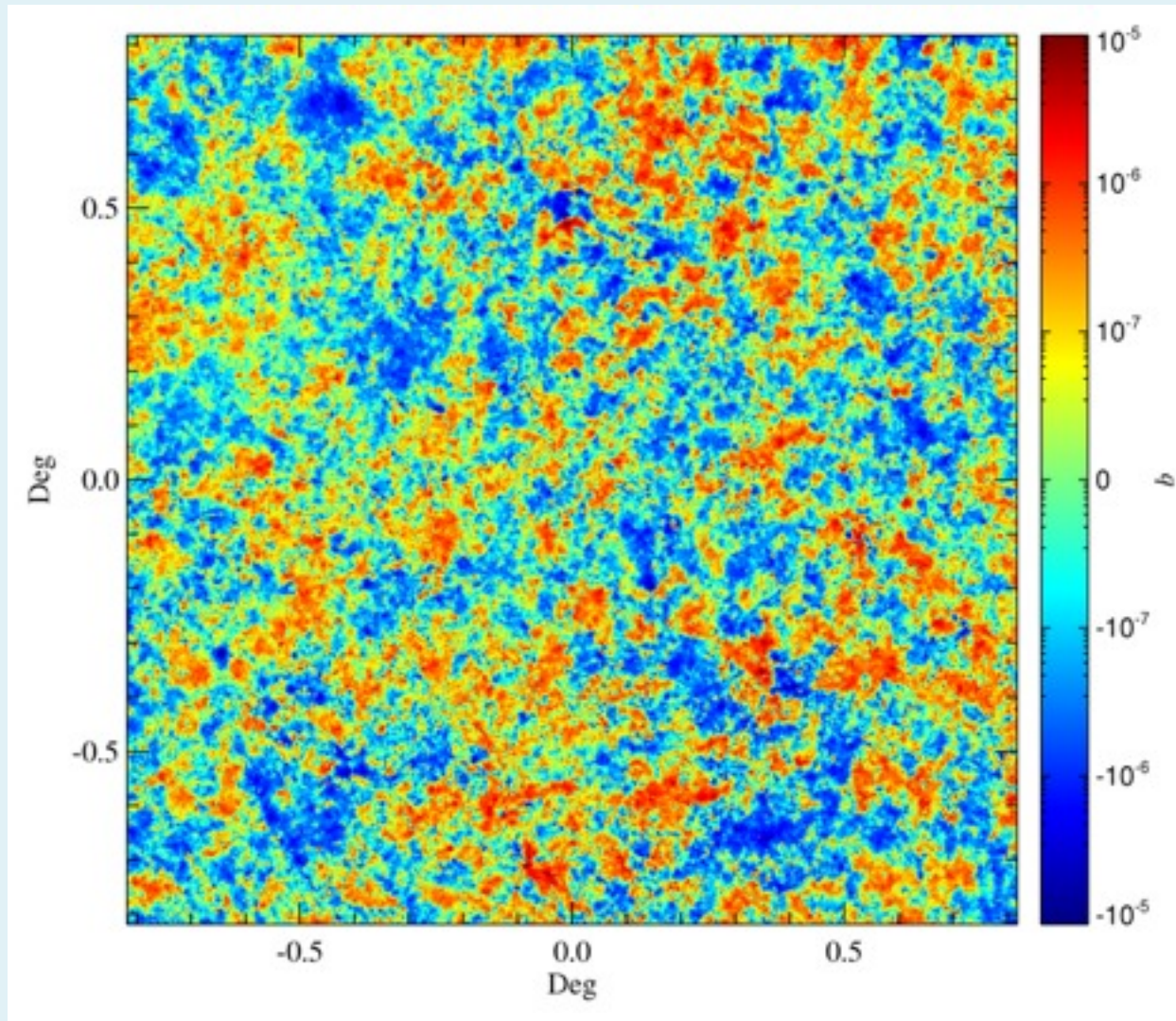
Adiabatic - Feedback



feedback
gives
“puffier”
clusters,
with lower
core
pressures

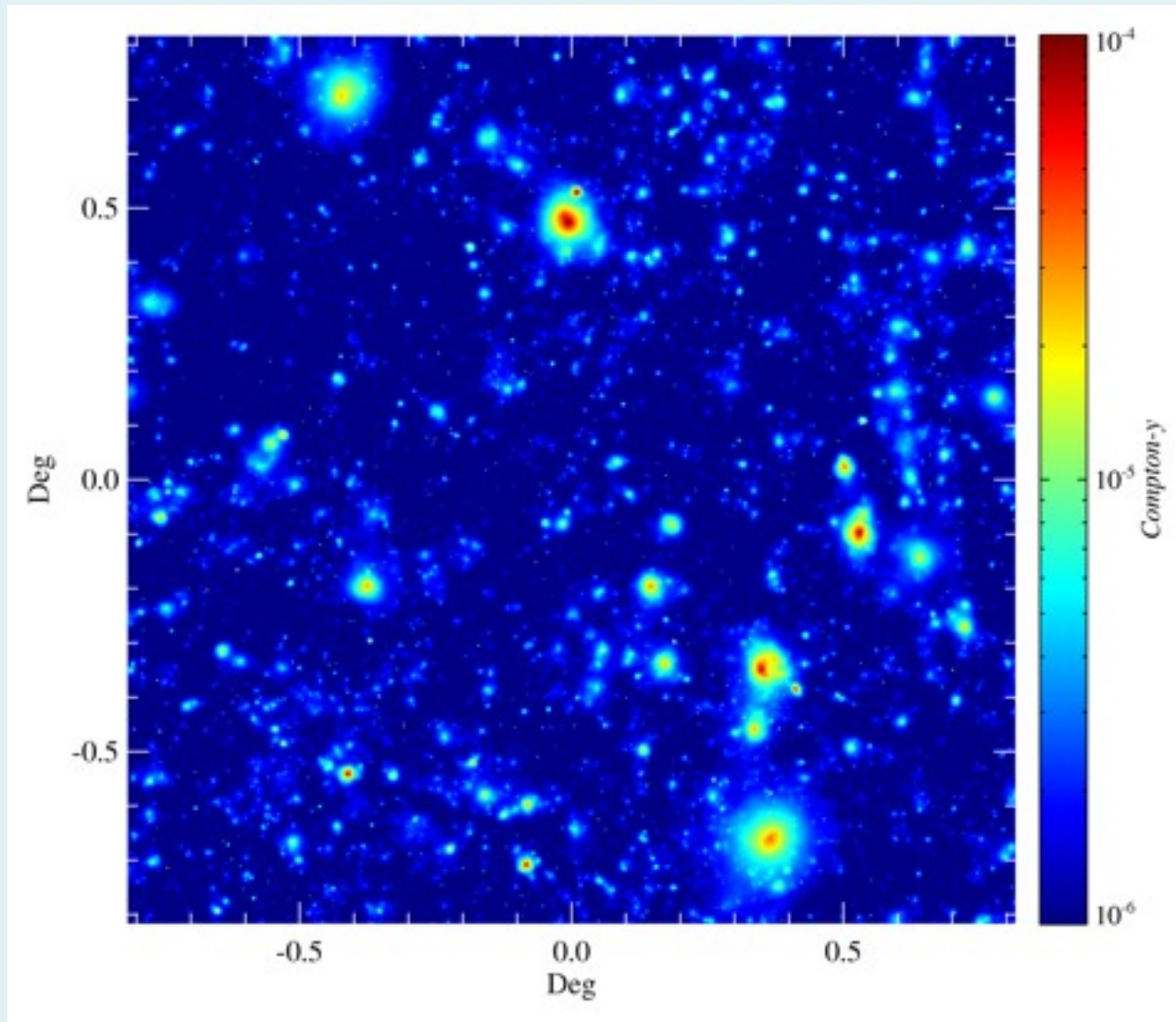
kinetic SZ map (*log*): Feedback

= AGN or Starburst E-feedback + radiative cool + SN energy + wind + (CR)



Compton- γ map: Feedback

= AGN or Starburst E-feedback + radiative cool + SN energy + wind + (CR)



CBI pol to Apr'05 @Chile **CBI2** **QUaD** @SP



Planck09.4

52+ bolometers
+ HEMTs @L2
9 frequencies



WMAP @L2 to 2010



>96
OVRO
/BIMA
array

2005
Acbar@SP

SZA@Cal

2007
AMIBA

AMI



APEX
~400 bolos@Chile

SPT
1000 bolos
@SPole



ACT
3000 bolos
3 freqs @Chile



SCUBA2
12000 bolos
JCMT @Hawaii



SPTpol
ACTpol
ALMA

CCAT@Chile
LMT@Mexico

80s-90s
Ryle
OVRO



GBT

CBI pol to Apr'05 @Chile

CBI2

QUaD @SP

53+35 cls (≥ 40)

189 +10 cls (≥ 1000)

Planck09.4

52+ bolometers
+ HEMTs @L2
9 frequencies



WMAP @L2 to 2010

2004

2006

2008

2011

LHC

Bpol
@L2

2005

Acbar@SP

~1 blind

SZA@Cal

3 cls ($z > 1$), x?

2007

AMIBA

6 cls

21+26~50 (≥ 750)

2009

SPT

1000 bolos
@SPole



ACT

3000 bolos
3 freqs @Chile

23+27~50 cls



SCUBA2

12000 bolos

JCMT @Hawaii

SPTpol

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ALMA

CCAT@Chile

LMT@Mexico

>96

OVRO
/BIMA

array

38 cls

80s-90s

Ryle

OVRO

AMI

7+1 cls $\geq 50+25$



GBT

4 cls (~25 CLASH)



APEX

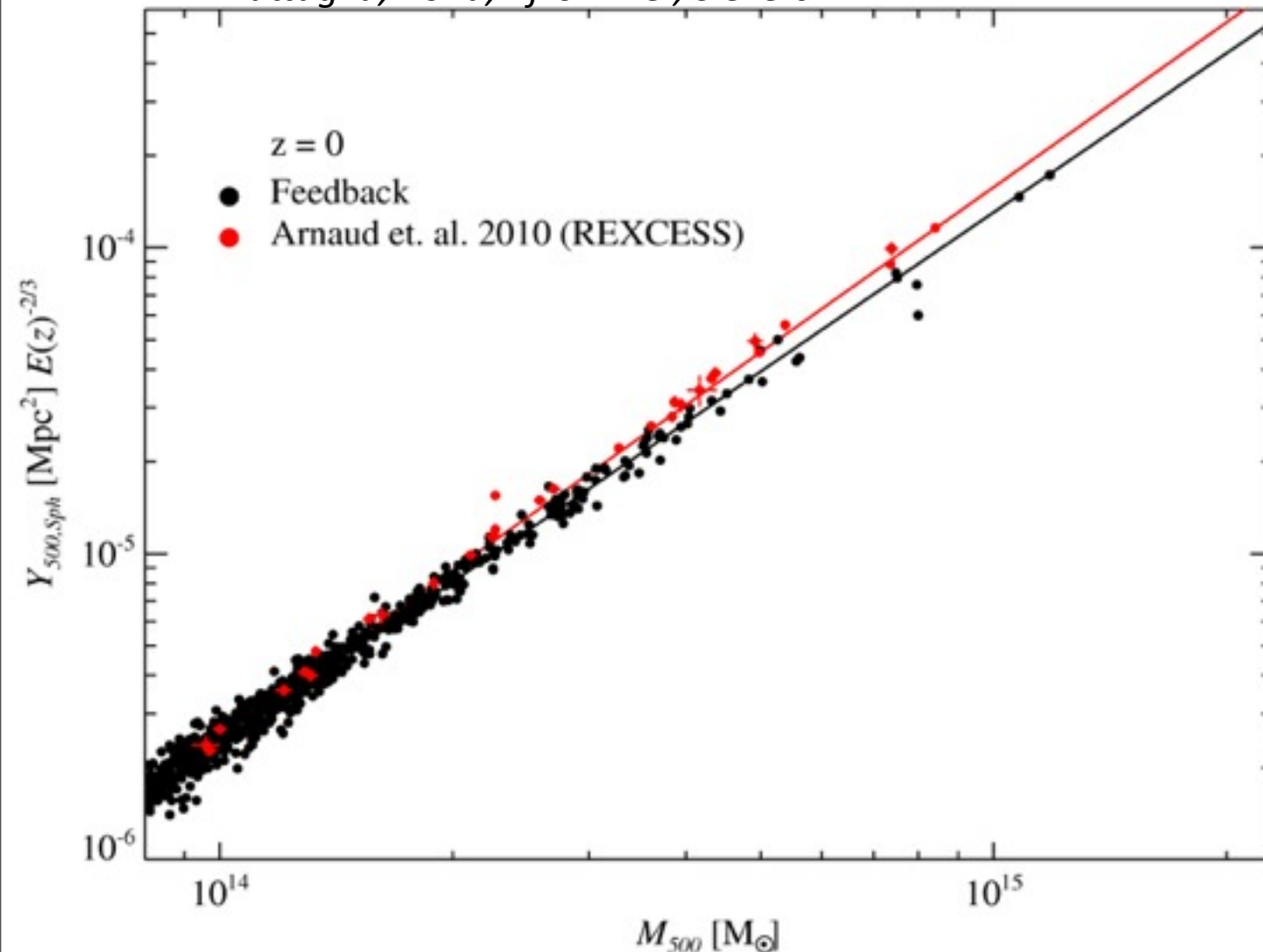
~400 bolos @Chile

~25 cls

$Y(<r_\Delta)$ - $M(<r_\Delta)$ relation, where

$$M(<R_\Delta)/V(<R_\Delta)=\Delta \rho_{\text{crit}}, \Delta=2500, 500, 200$$

Battaglia, Bond, Pfrommer, Sievers 11



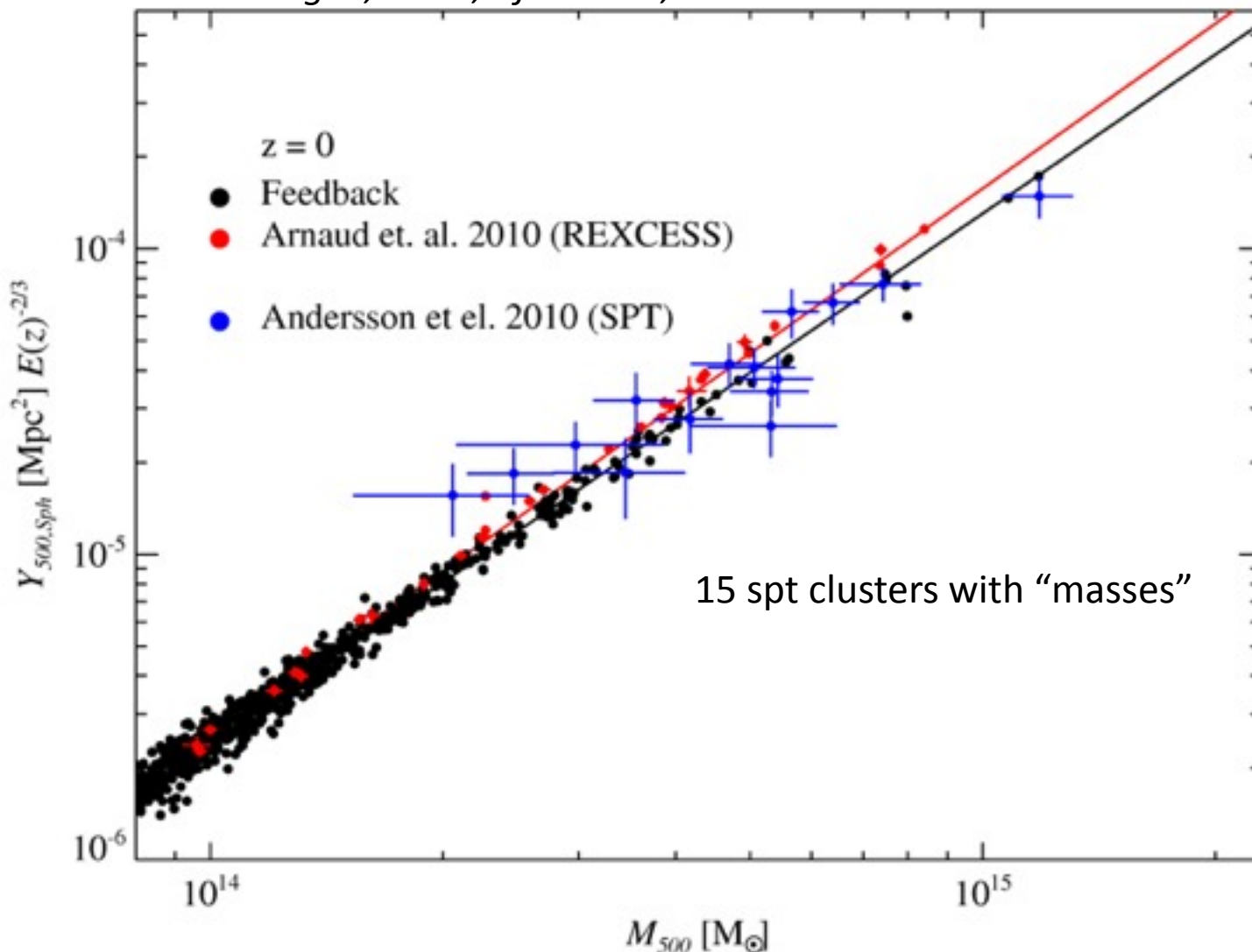
Planck-ESZ
gives Y_{5R500}

is Y_{sz} a good
mass proxy in
 $n_{cl}(M, z)$?
even though
virial theorem
 $Y(e, K/U, \dots | M)$
 $\Rightarrow n_{cl}(Y, z)$

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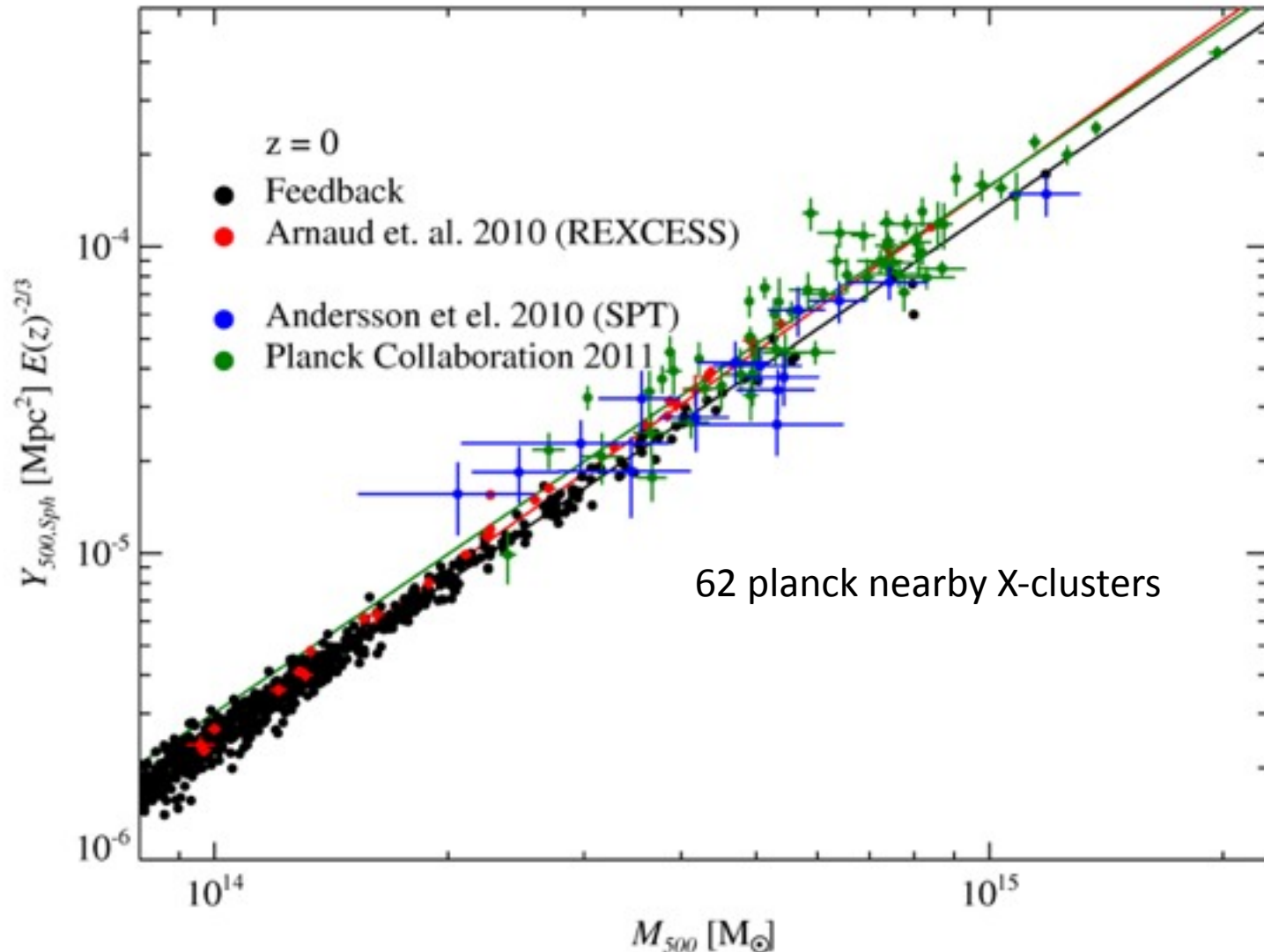
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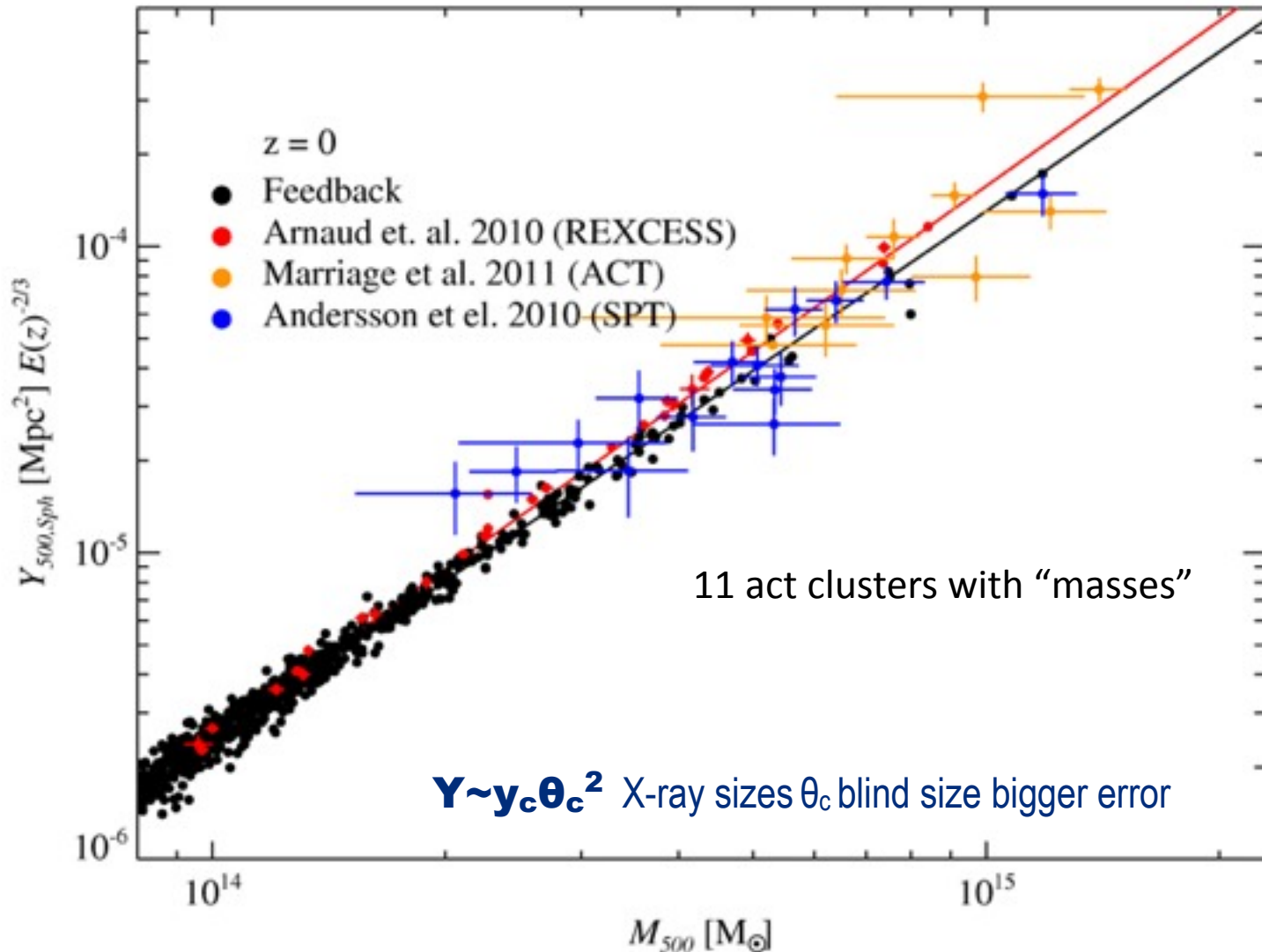
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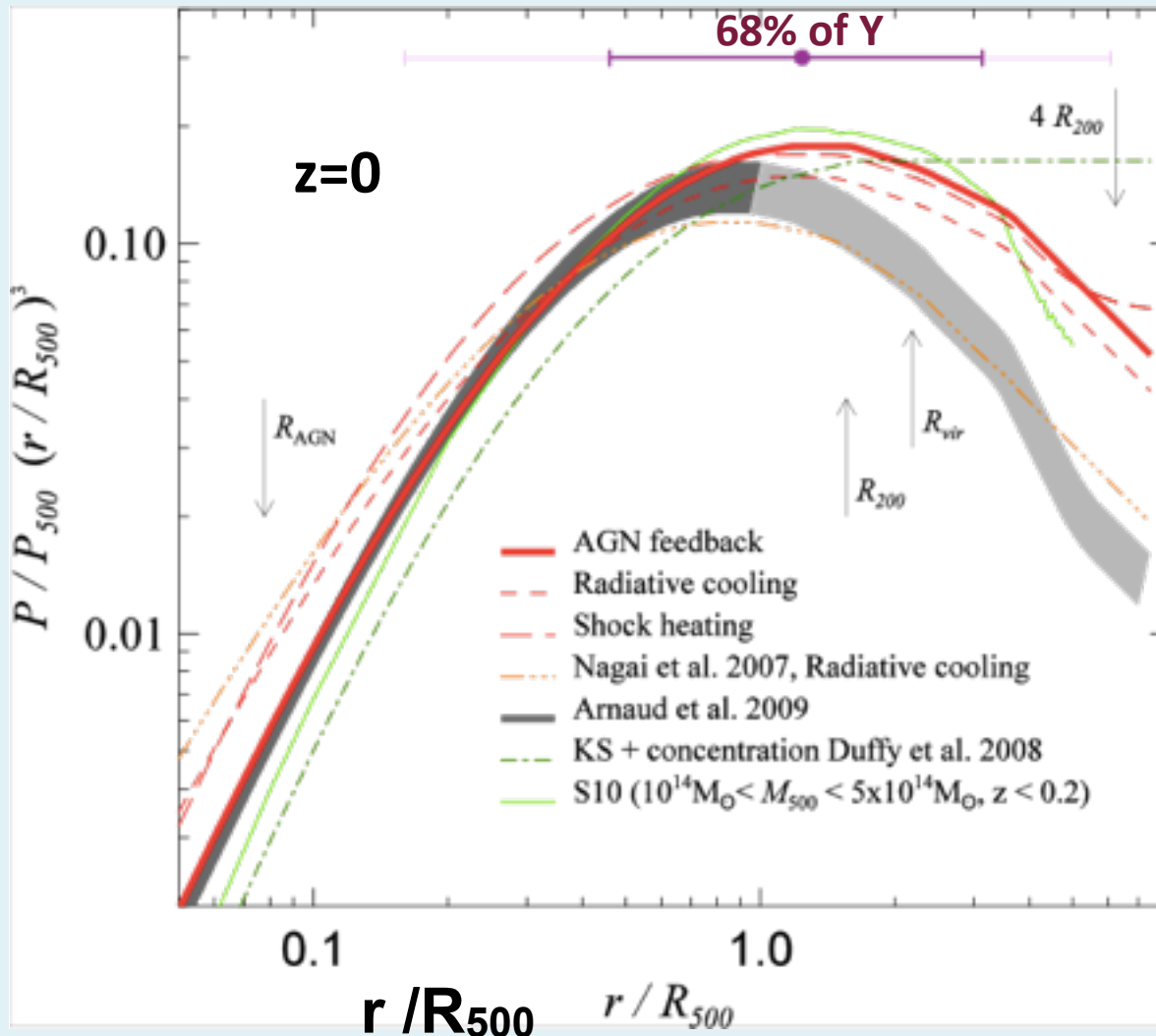


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scaled Pressure profiles: $d \ln E_{\text{th}}(<r) / d \ln r$

Battaglia, Bond, Pfrommer, Sievers, Sijacki 10



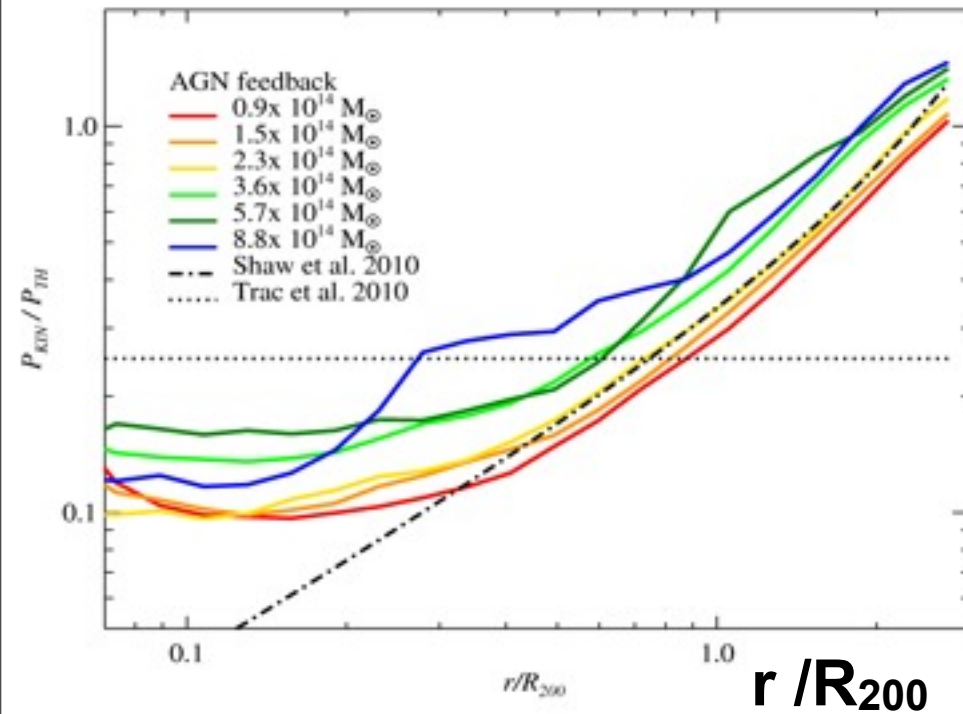
AGN Feedback
sims match
Arnaud *etal*
<X-ray profiles>
to data-end $\sim r_{500}$
universal?
redshift, mass, ...
dependent

$$\frac{P}{P_{\Delta}} = \frac{A}{\left[1 + \left(\frac{x}{x_c} \right)^{\frac{\alpha}{\gamma}} \right]^{\gamma/\alpha}}$$

$P_{\text{kin}} / P_{\text{th}} \sim 0.1 - 0.6!$

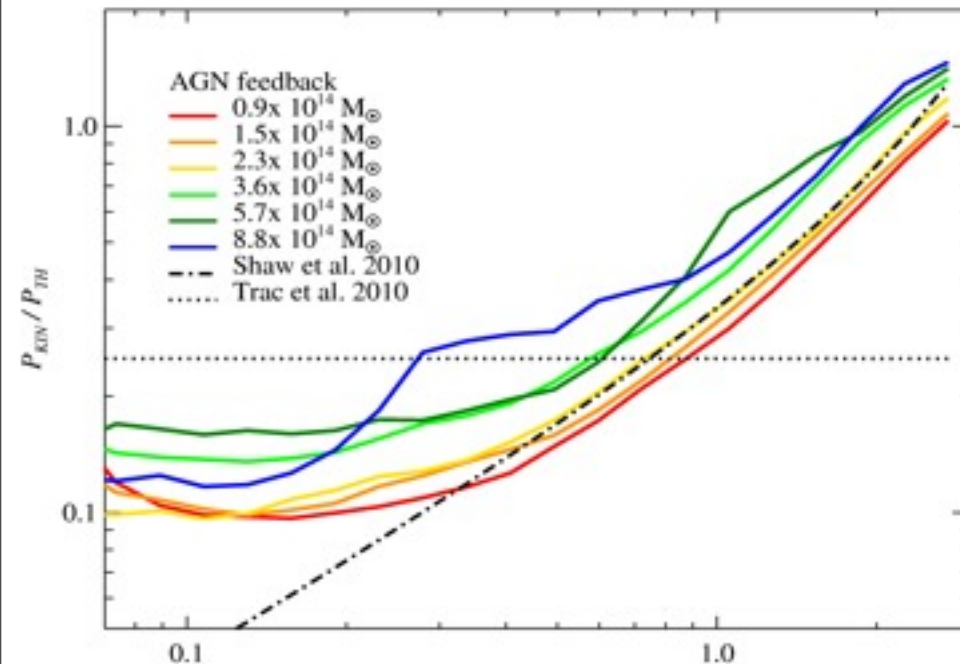
$\langle (\Delta v)^2 \rangle / c_s^2$
cannot be
ignored in HSE

$$\nabla p_{\text{g,tot}} = \rho_{\text{g}} g$$

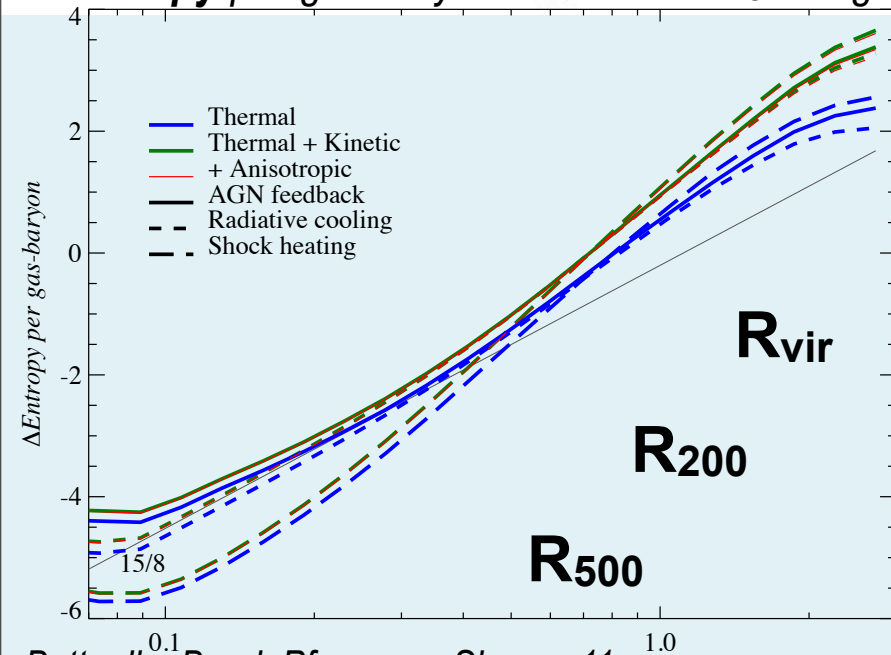


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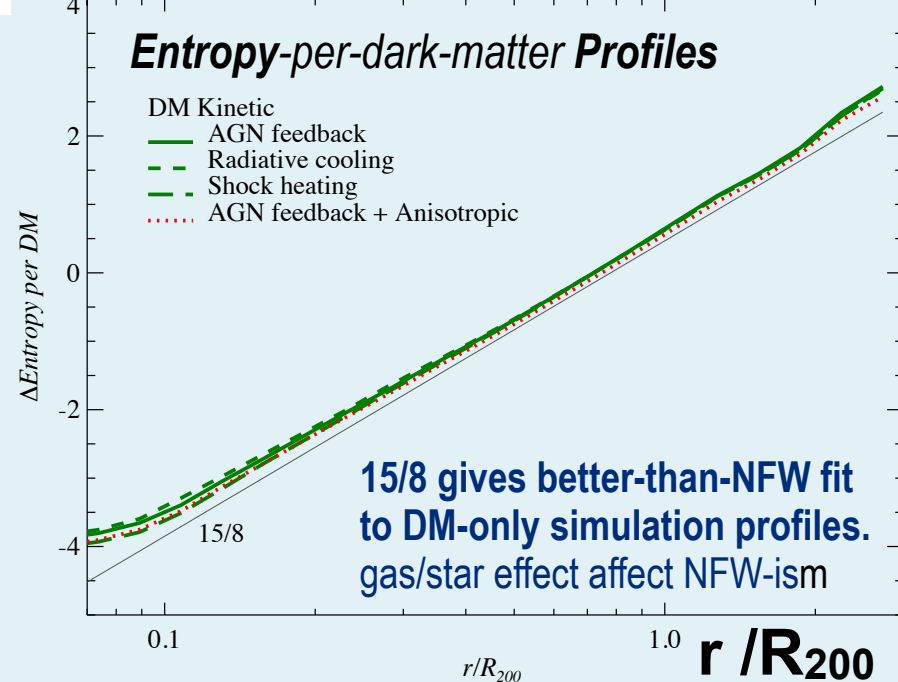
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Entropy-per-gas-baryon Profiles for Y_{sz} -weighted Scaled-stacked Clusters



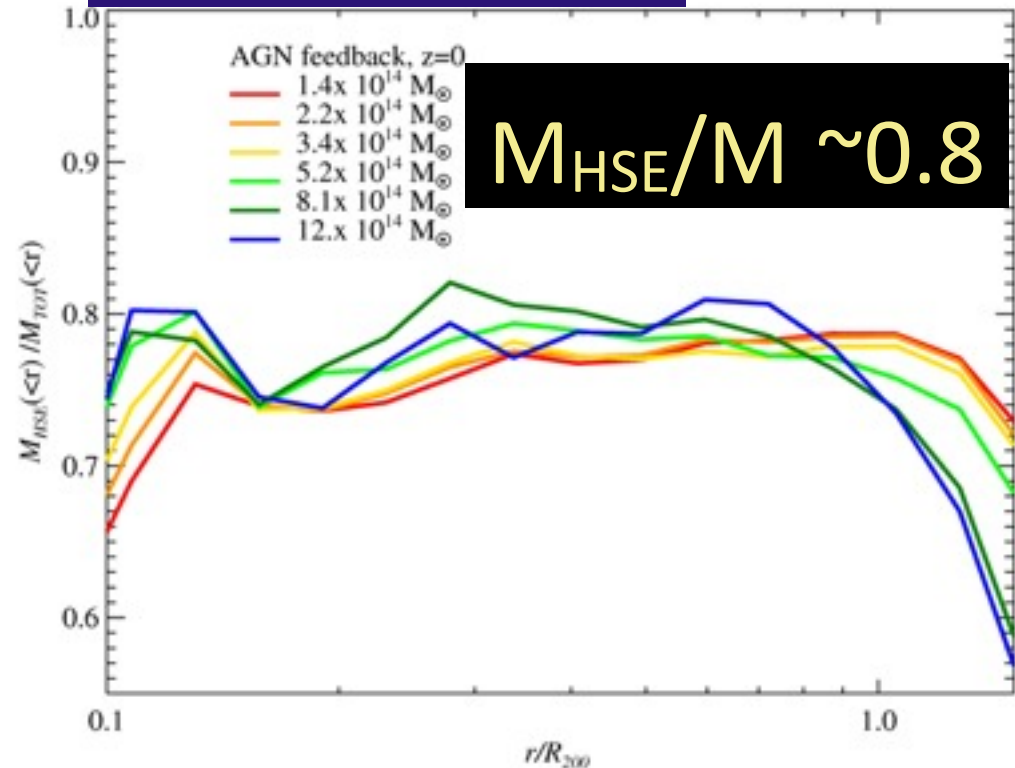
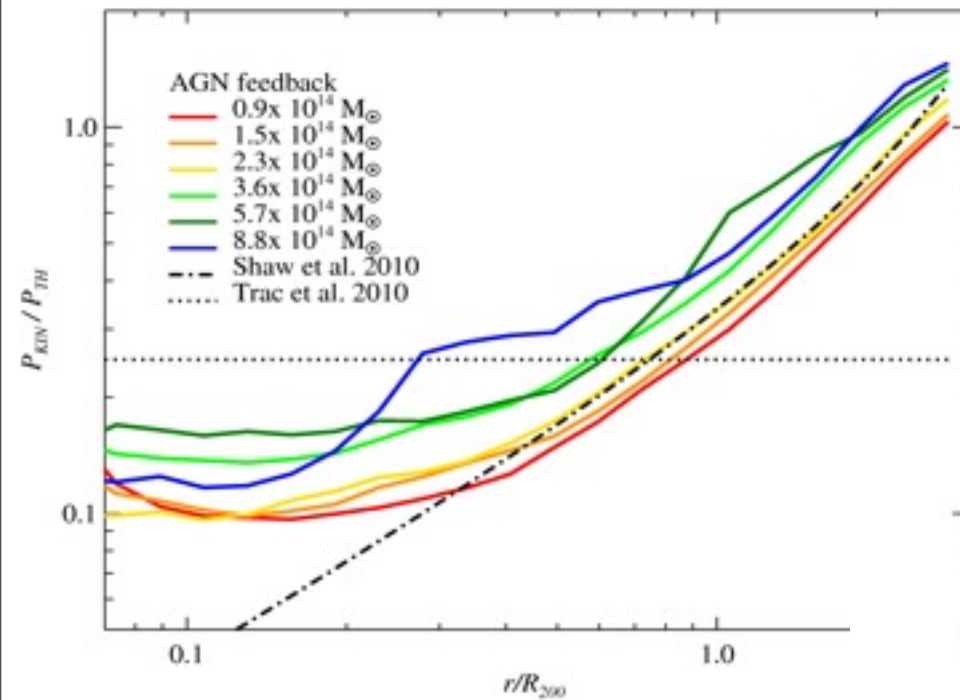
Entropy-per-dark-matter Profiles



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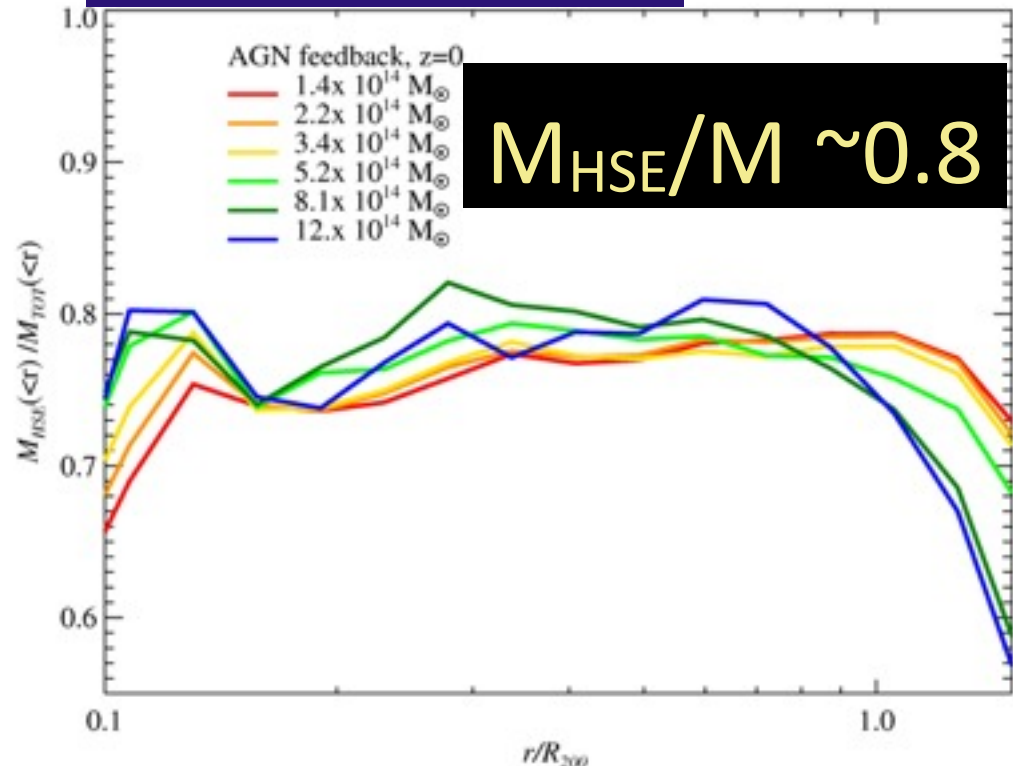
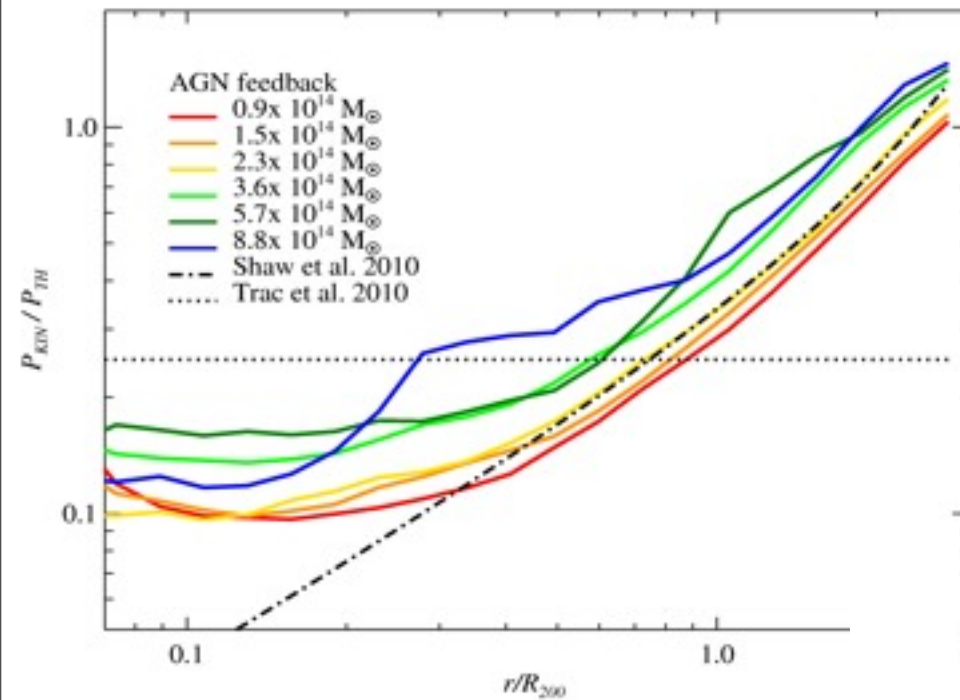
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$M_{\text{HSE}} / M \sim 0.8$

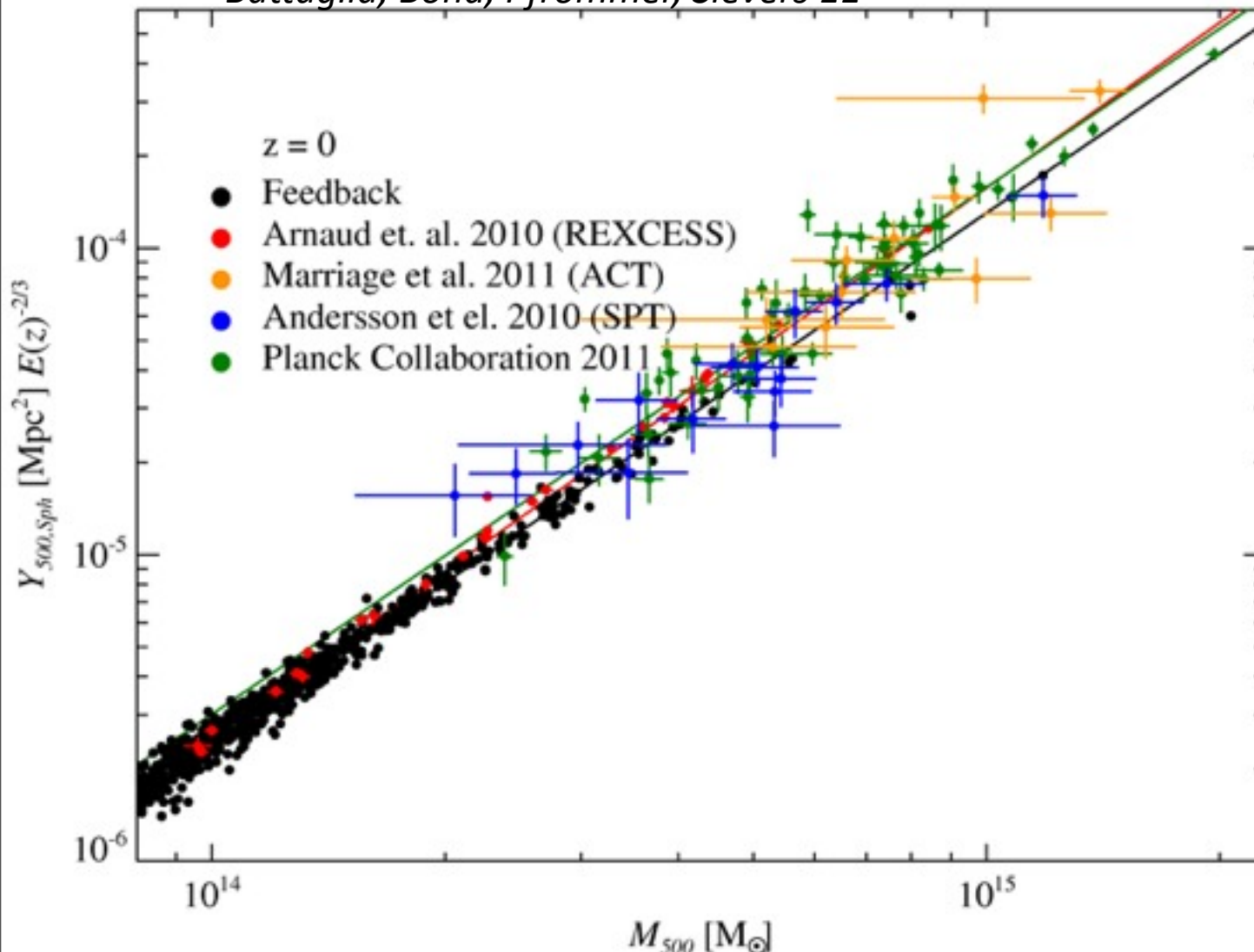
Hydro Sims include all effects
(except of course for those not included).

Analytic and semi-analytic
treatments must be fully
calibrated with sims to give a
useful phenomenology.

$Y(<r_\Delta)$ - $M(<r_\Delta)$ relation, where

$$M(<R_\Delta)/V(<R_\Delta)=\Delta \rho_{\text{crit}}, \Delta=2500, 500, 200$$

Battaglia, Bond, Pfrommer, Sievers 11



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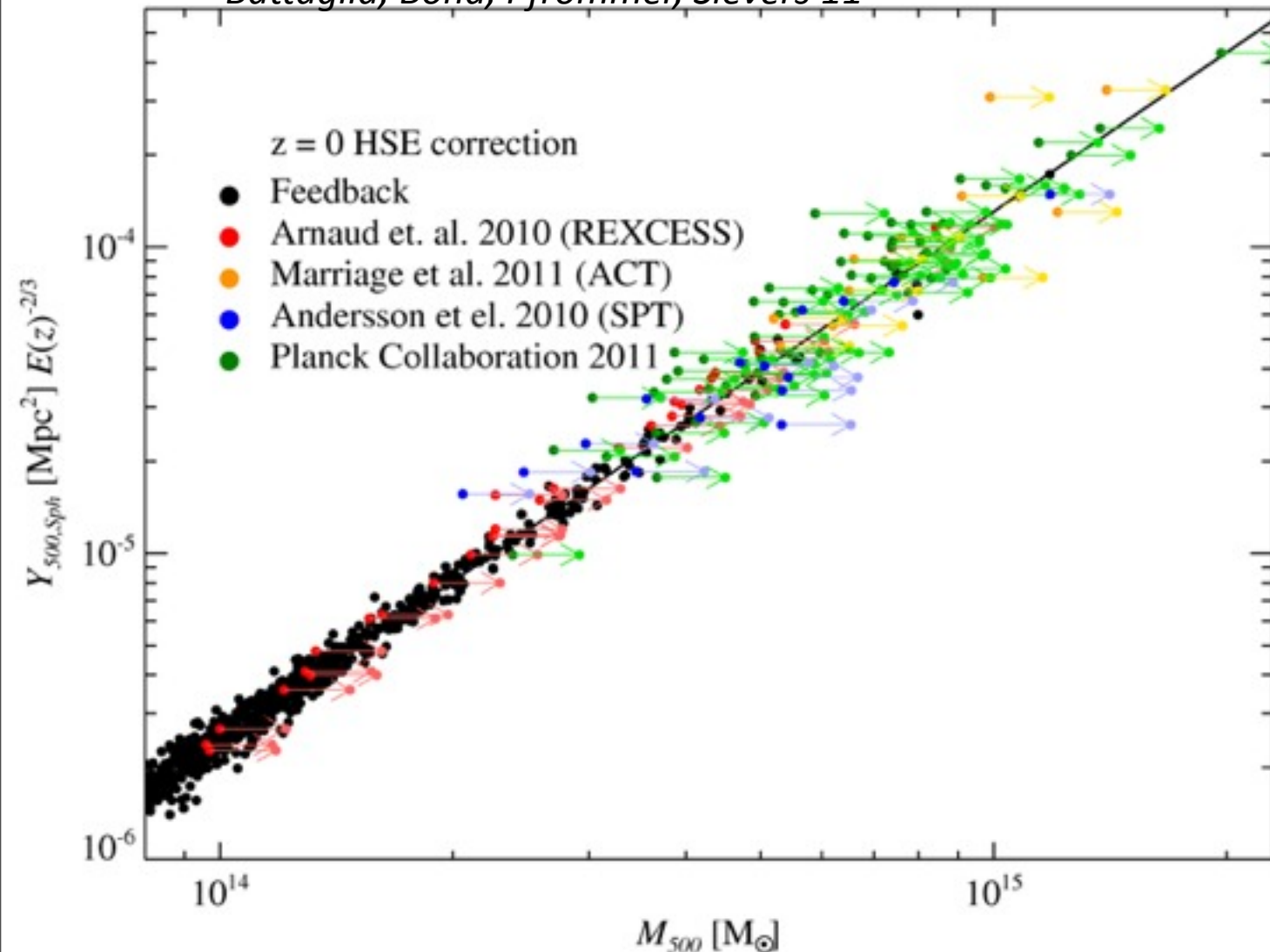
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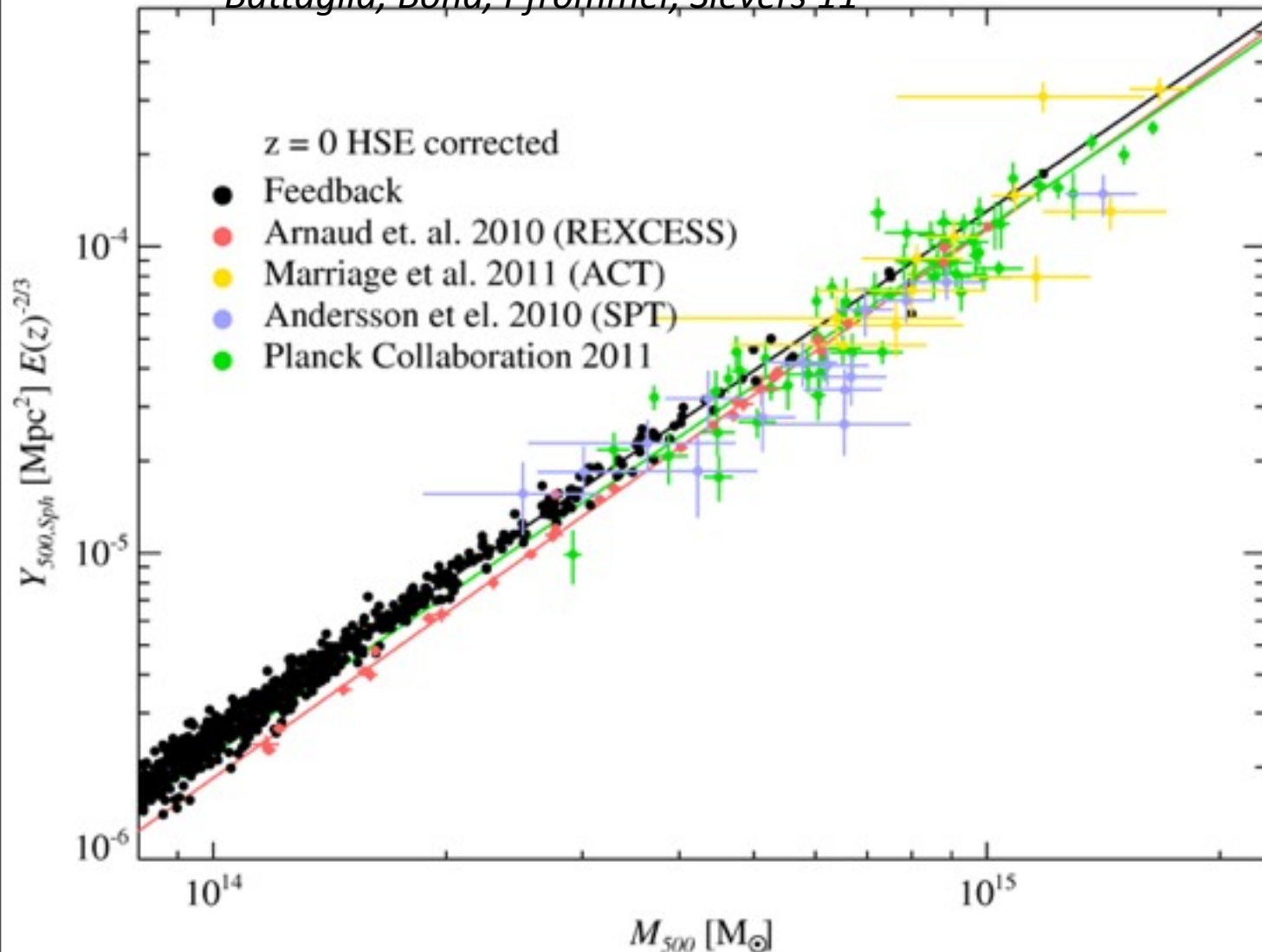
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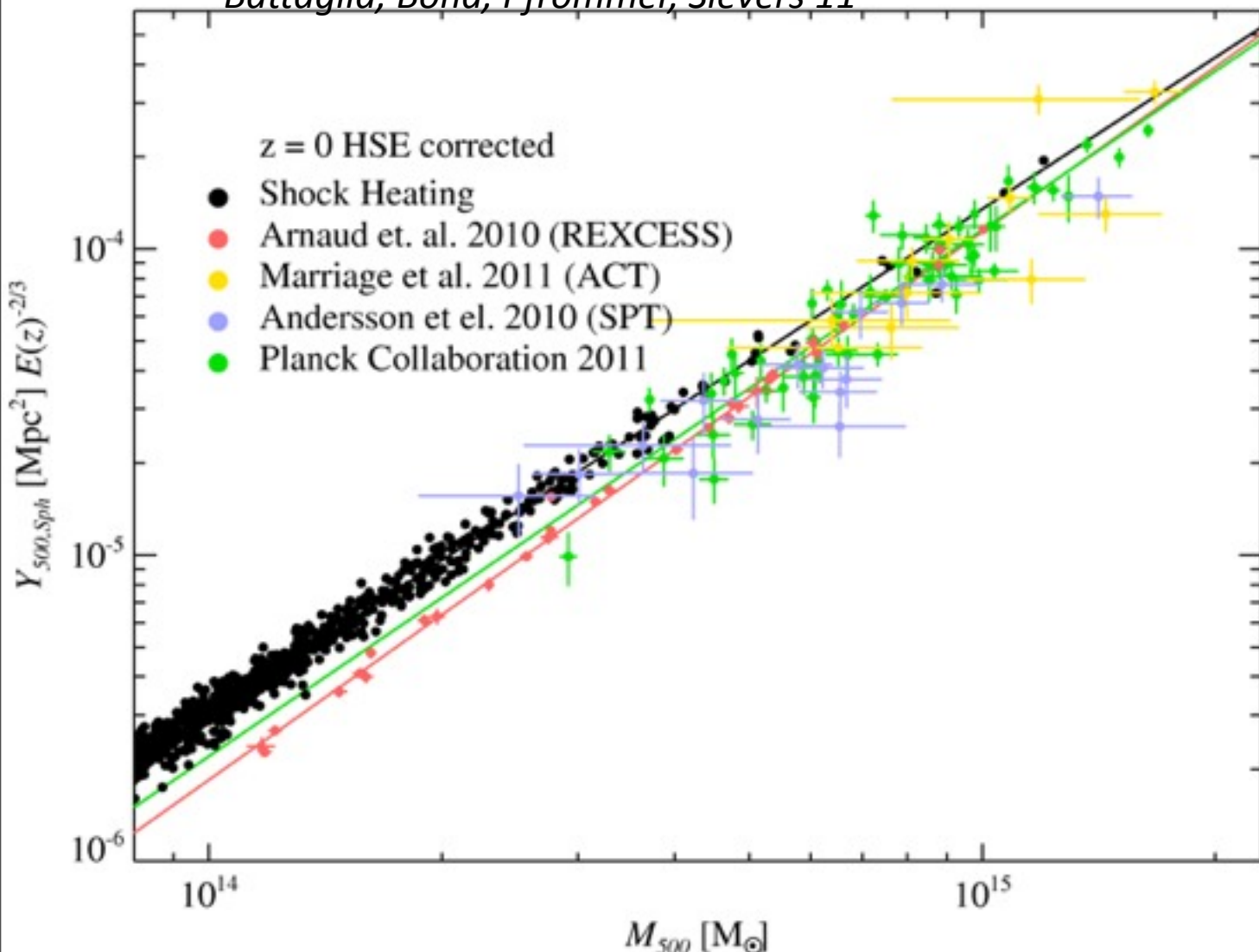
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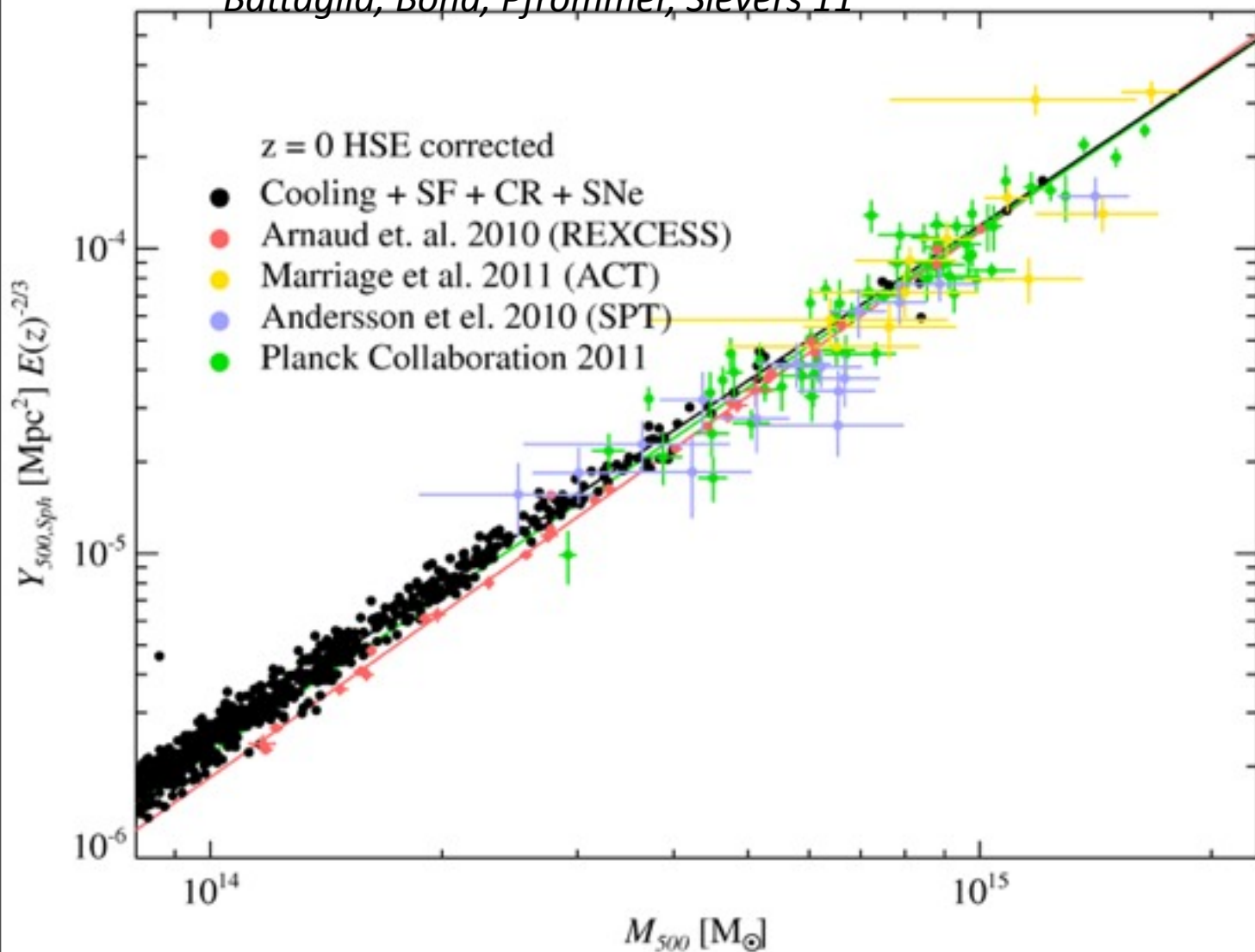
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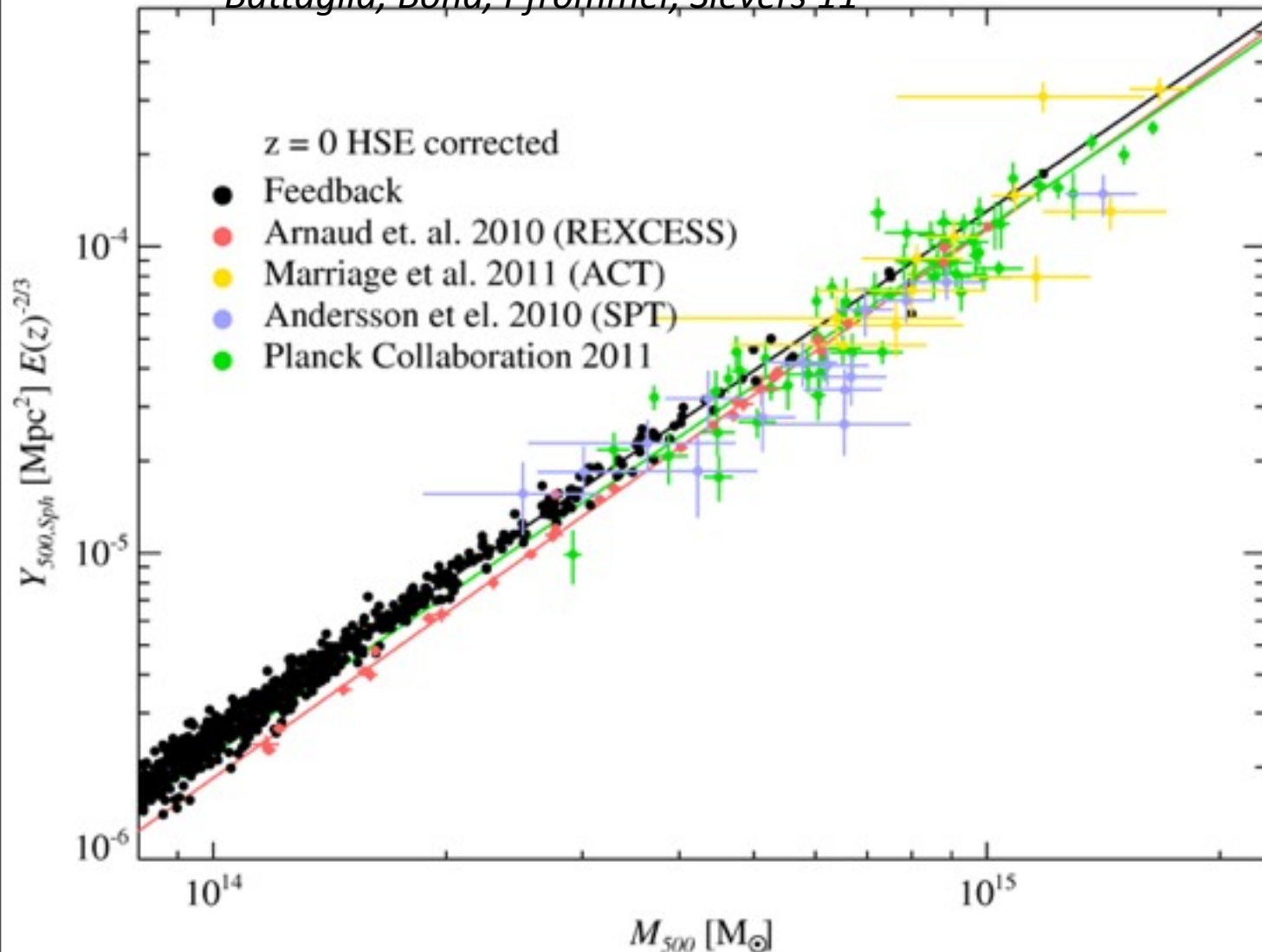
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 $n_{\text{cl}}(M, z)$?
even though
virial theorem
 $Y(e, K/U, \dots | M)$
 $\Rightarrow n_{\text{cl}}(Y, z)$

$Y(<r_\Delta)$ - $M(<r_\Delta)$ relation, where

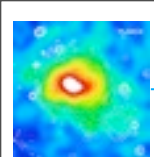
$$M(<R_\Delta)/V(<R_\Delta)=\Delta \rho_{\text{crit}}, \Delta=2500, 500, 200$$

Battaglia, Bond, Pfrommer, Sievers 11

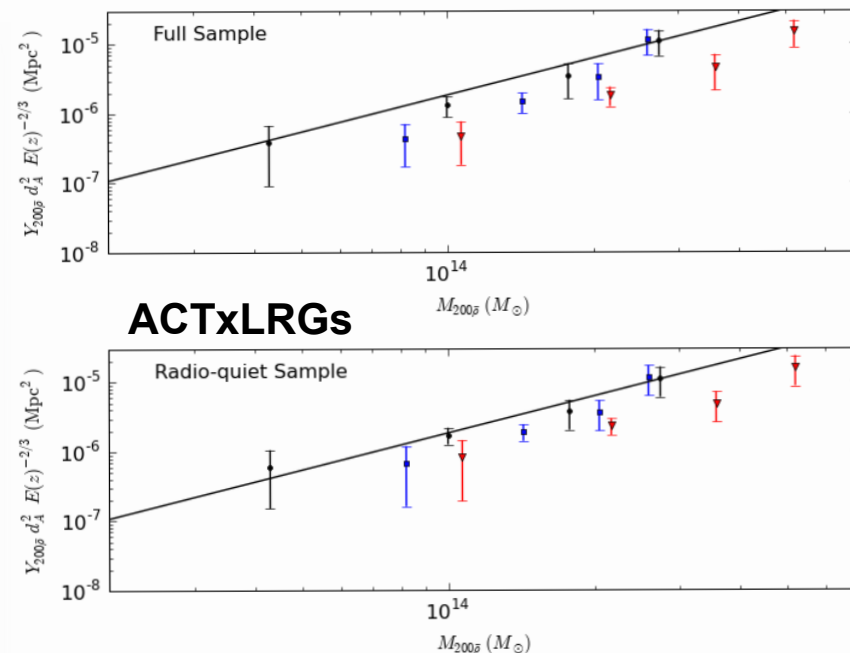
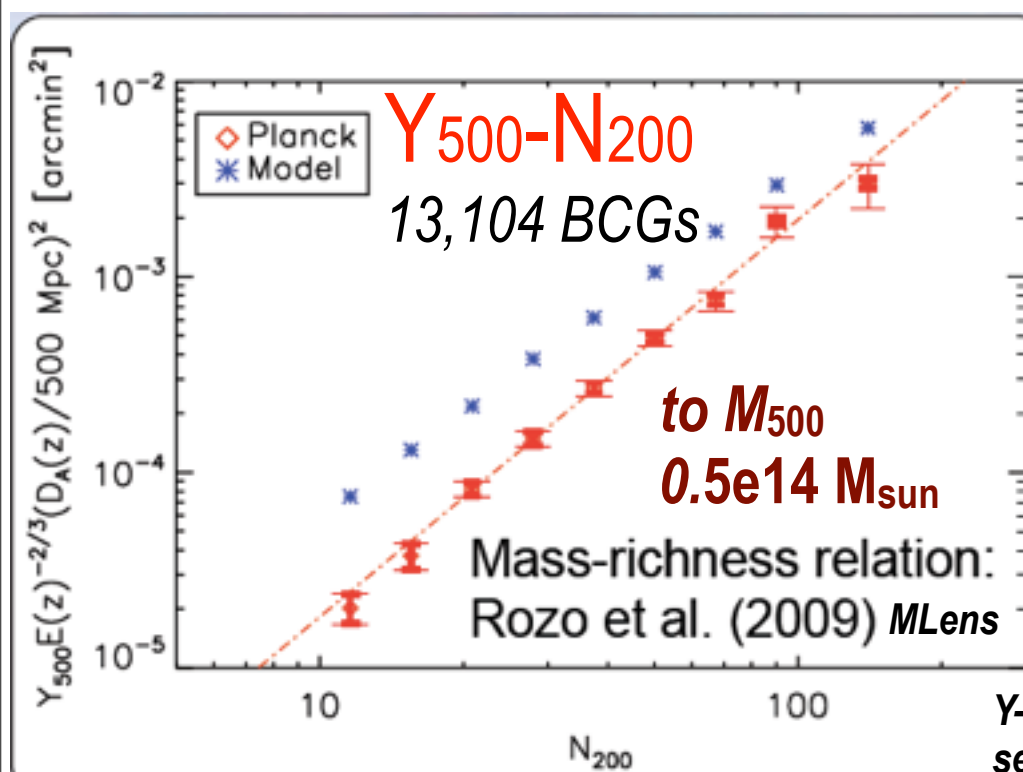


Planck-ESZ
gives Y_{5R500}

is Y_{sz} a good
mass proxy in
 $n_{\text{cl}}(M, z)$?
even though
virial theorem
 $Y(e, K/U, \dots | M)$
 $\Rightarrow n_{\text{cl}}(Y, z)$



Planck sees the rarest and most massive clusters over the whole sky: 86% with $z < 0.3$; masses to $1.5 \times 10^{15} M_{\text{sol}}$. 90% of the RASS above $M > 9 \times 10^{14} M_{\text{sol}}$ detected by blind ESZ, 5/21 of new Planck $> 9 \times 10^{14} M_{\text{sun}}$. But “stacking” with the multifrequency filter extends the mass range to $\sim 0.5e14 M_{\text{sun}}$

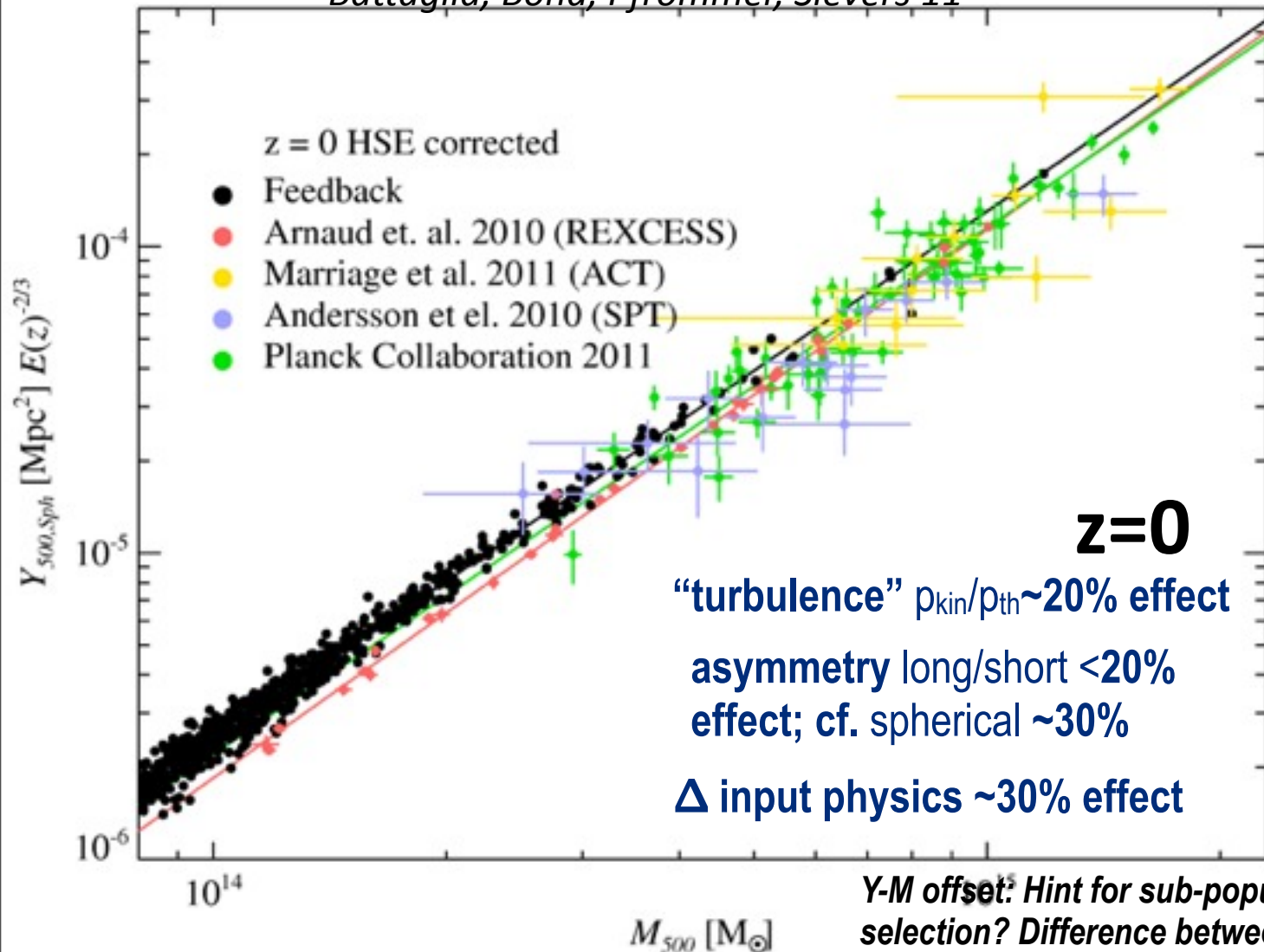


Y-M offset: Hint for sub-populations? Optical selection? Difference between M_x & $MLens$ & M_{bias} ?

$Y(<r_\Delta)$ - $M(<r_\Delta)$ relation, where

$$M(<R_\Delta)/V(<R_\Delta)=\Delta \rho_{\text{crit}}, \Delta=2500, 500, 200$$

Battaglia, Bond, Pfrommer, Sievers 11



Planck-ESZ
gives Y_{5R500}

is Y_{sz} a good mass proxy in $n_{\text{cl}}(M, z)$?
even though virial theorem $Y(e, K/U, \dots | M)$
 $\Rightarrow n_{\text{cl}}(Y, z)$

Y-M offset: Hint for sub-populations? Optical selection? Difference between M_x & M_{Lens} & M_{bias} ?

CBI pol to Apr'05 @Chile **CBI2**

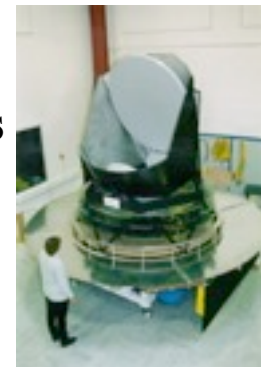
CLSZ

QUaD @SP

CLSZ

Planck09.4

52+ bolometers
+ HEMTs @L2
9 frequencies



WMAP @L2 to 2010

2004

2006

2008

2011



2005

2007

2009

Bpol
@L2

>96

OVRO
/BIMA
array

CLSZ

Acbar @SP
~1 blind

CLSZ

SZA @Cal

CLSZ

AMI

AMIBA



APEX
~400 bolos @Chile

CLSZ

SPT
1000 bolos
@SPole



ACT
3000 bolos
3 freqs @Chile

CLSZ



SCUBA2
12000 bolos
JCMT @Hawaii



SPTpol
ACTpol
ALMA

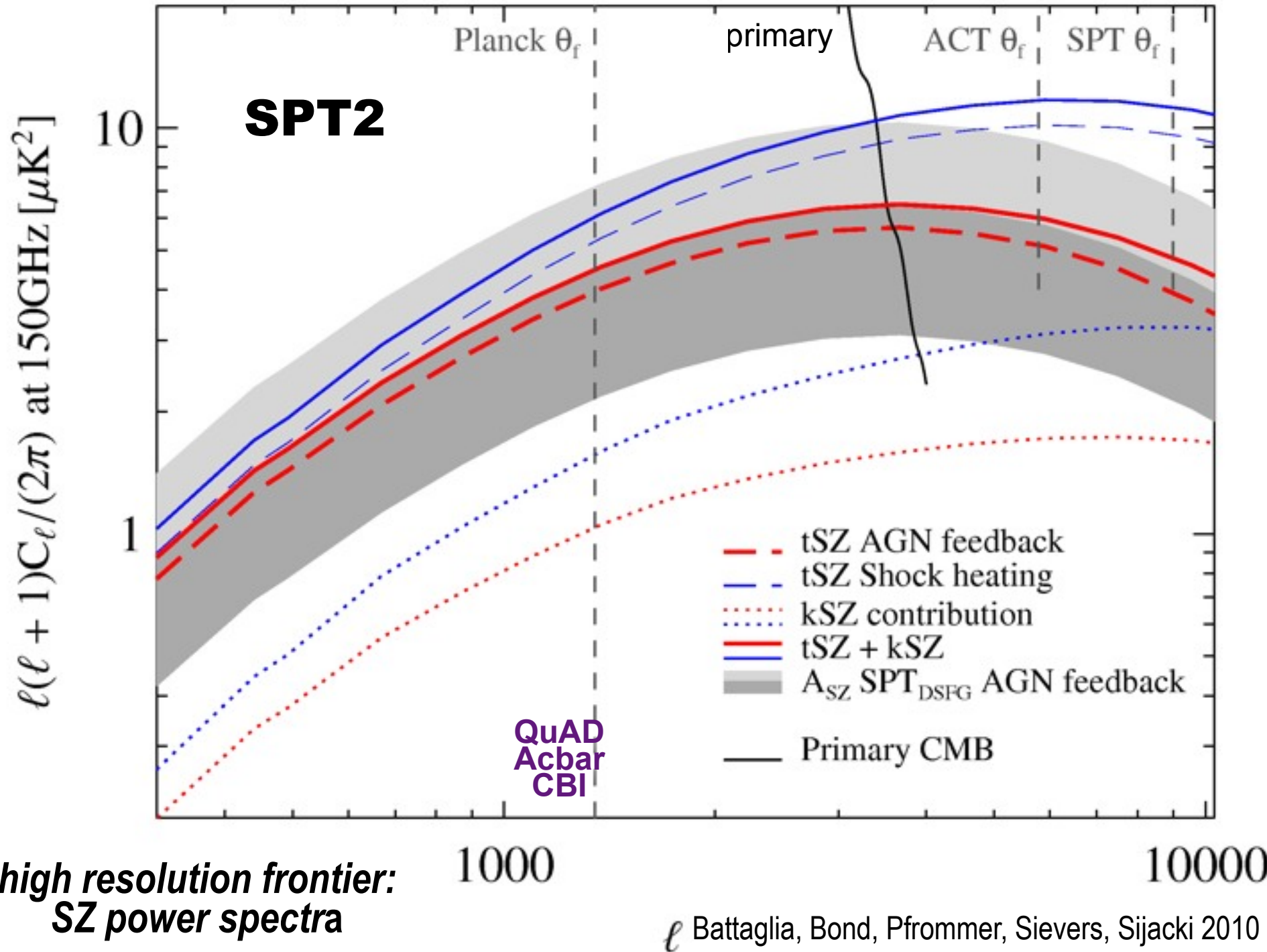
CCAT @Chile

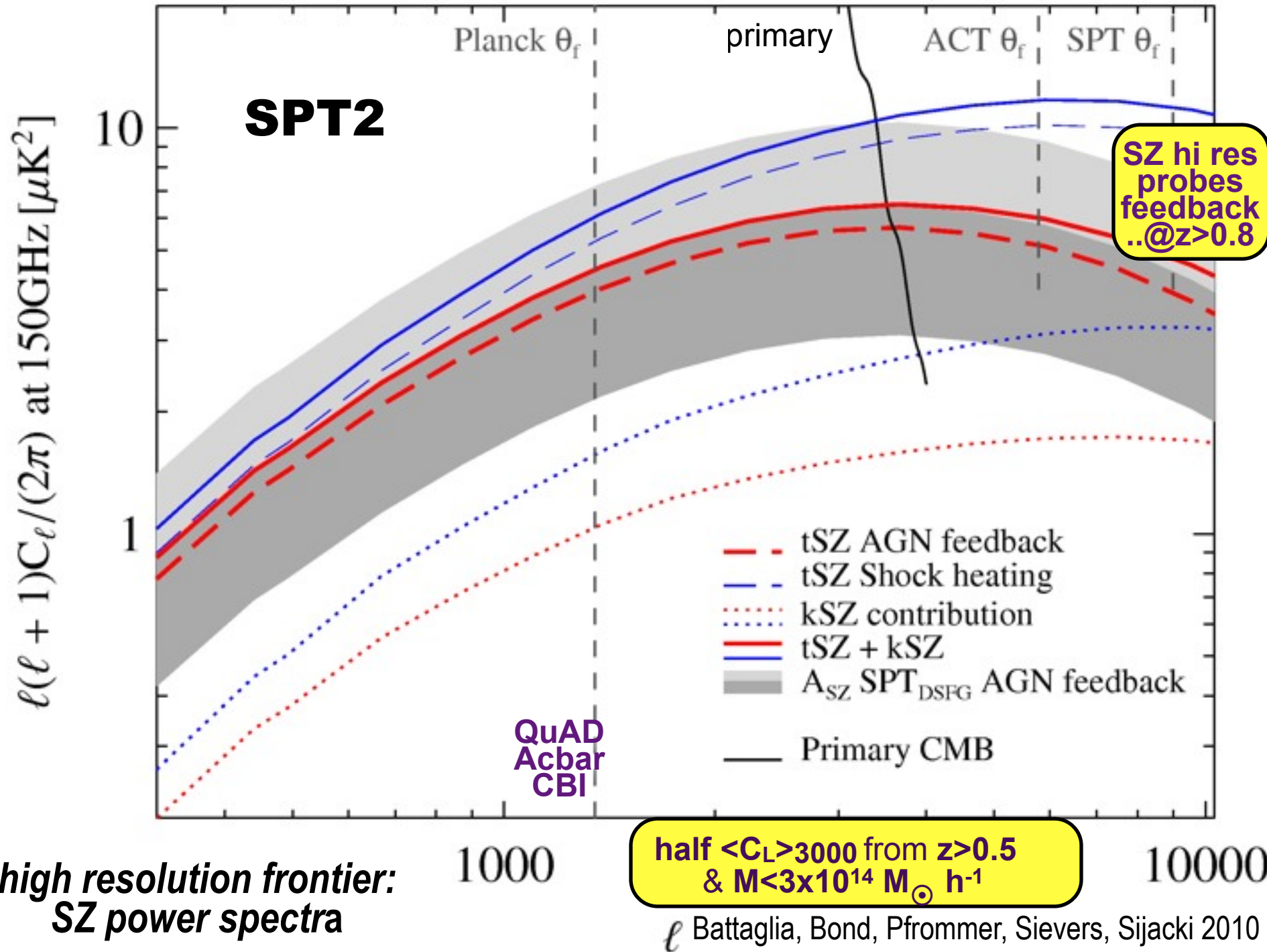
LMT @Mexico

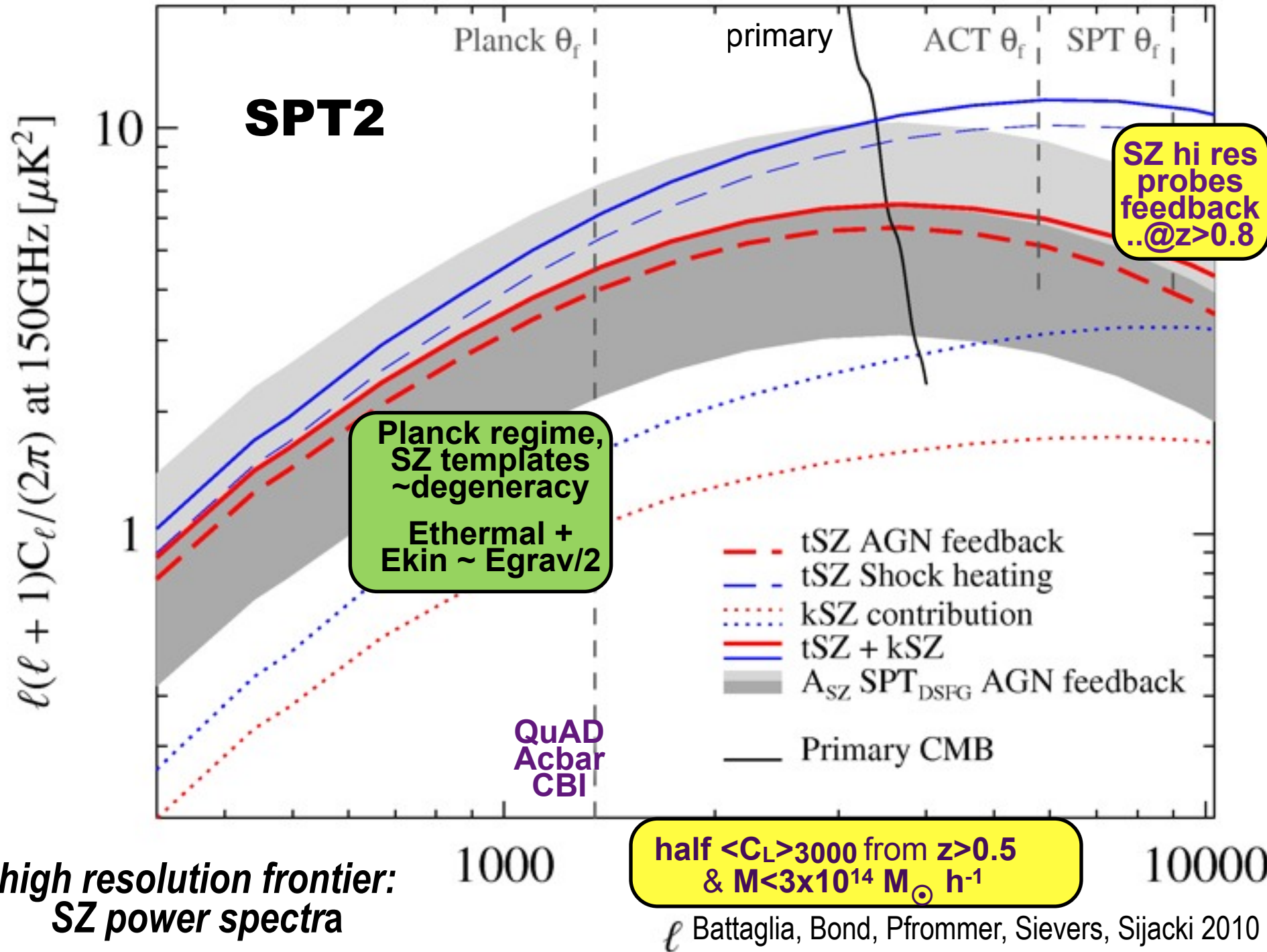
80s-90s
Ryle
OVRO

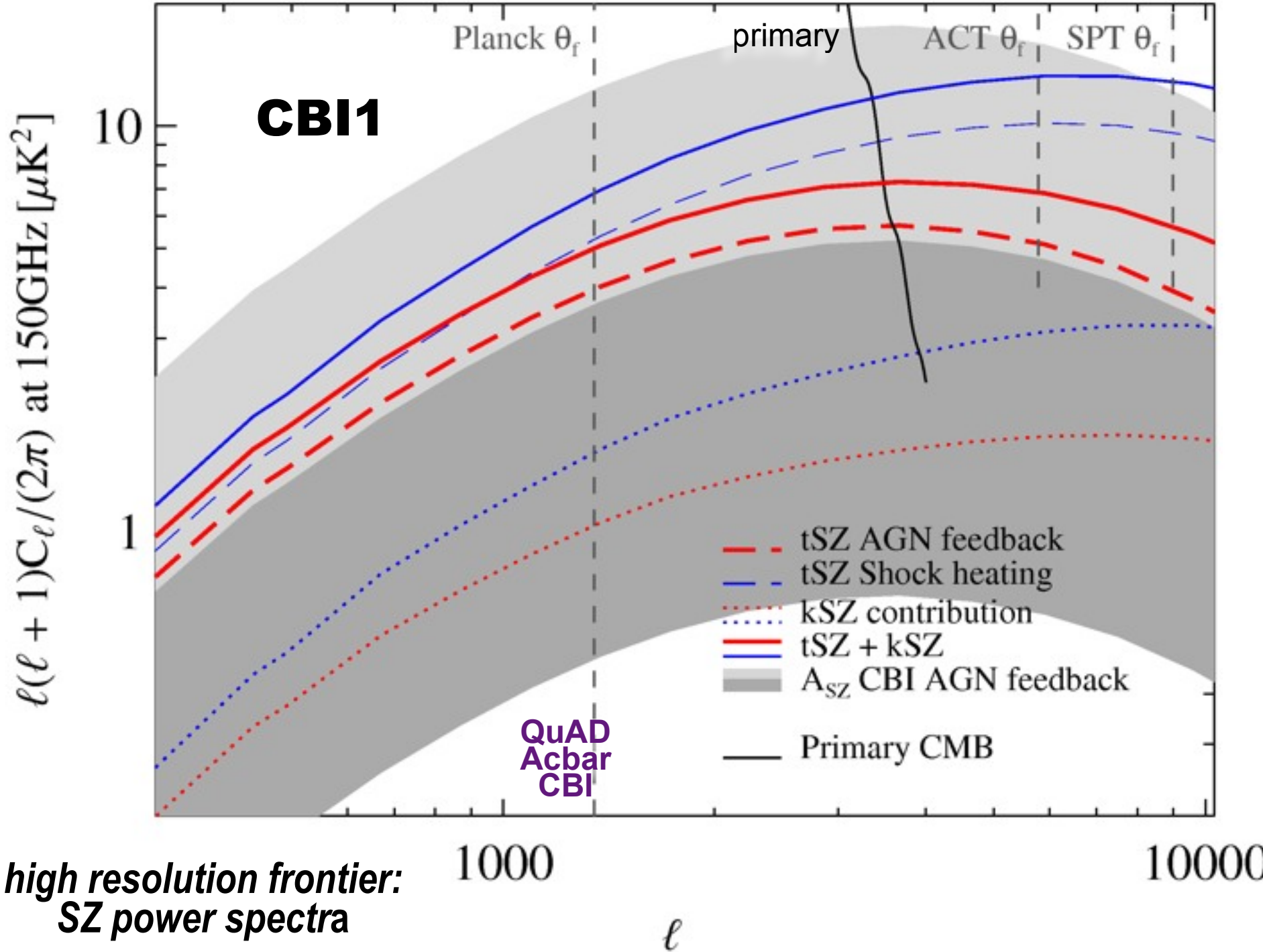


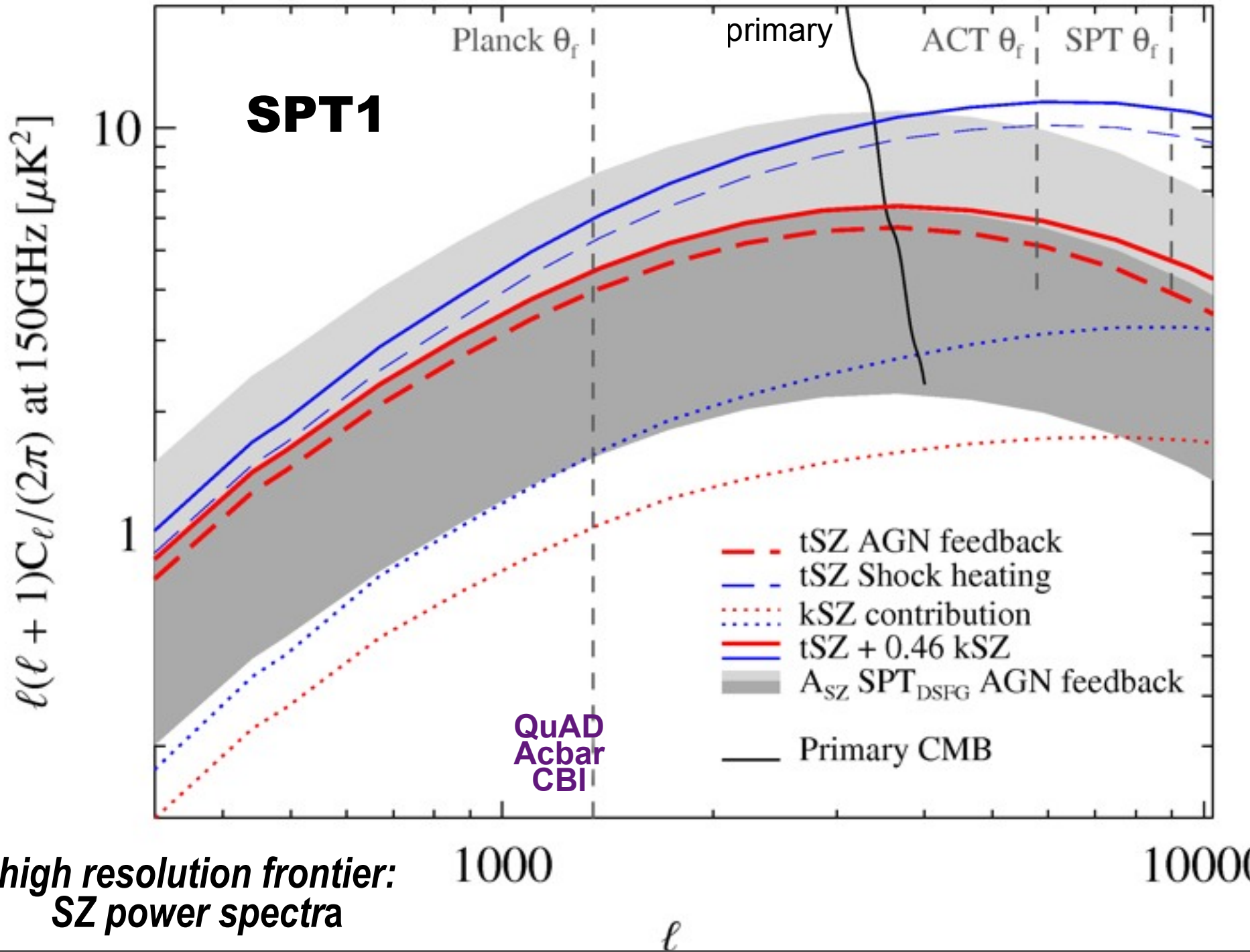
GBT

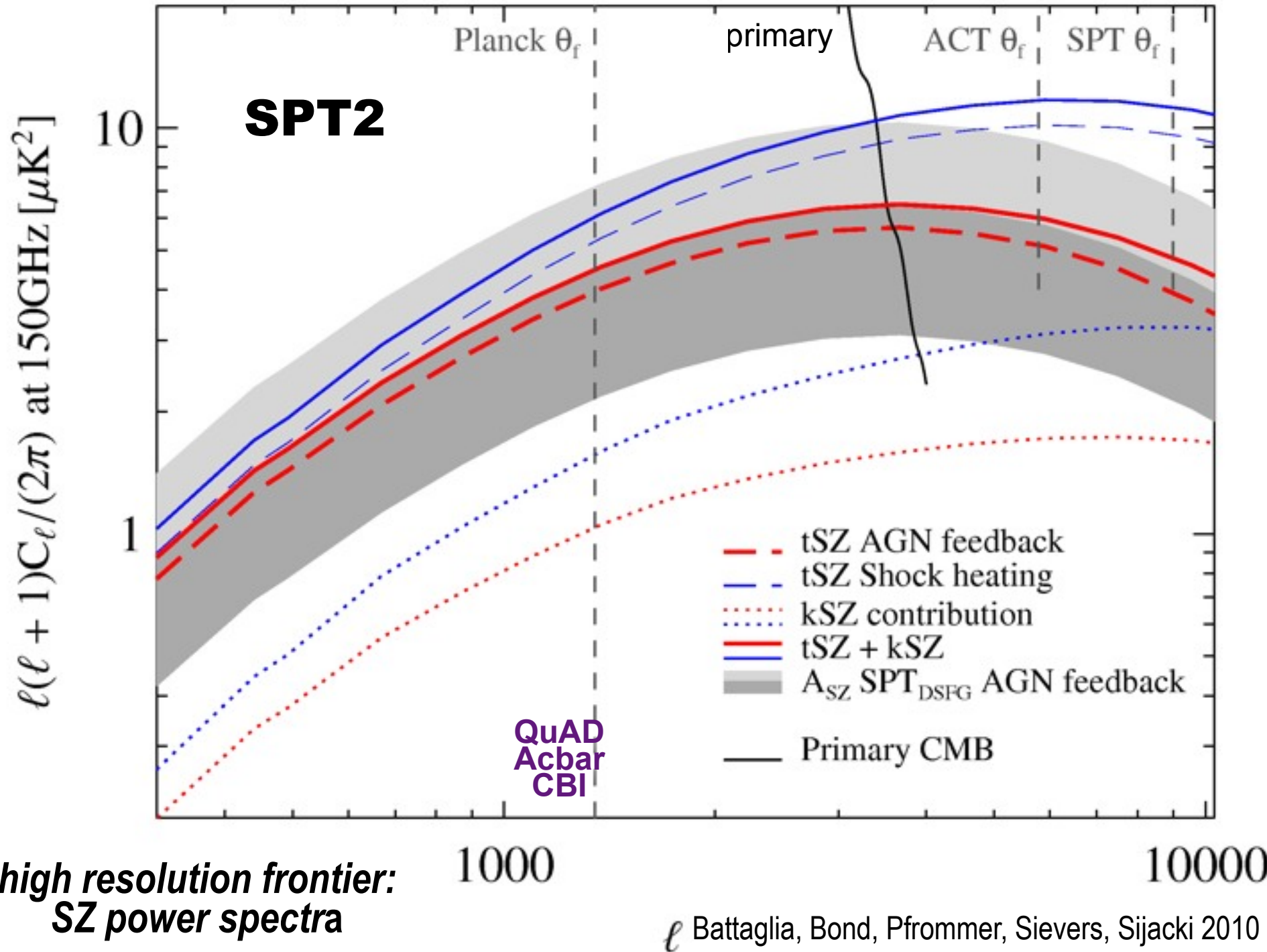


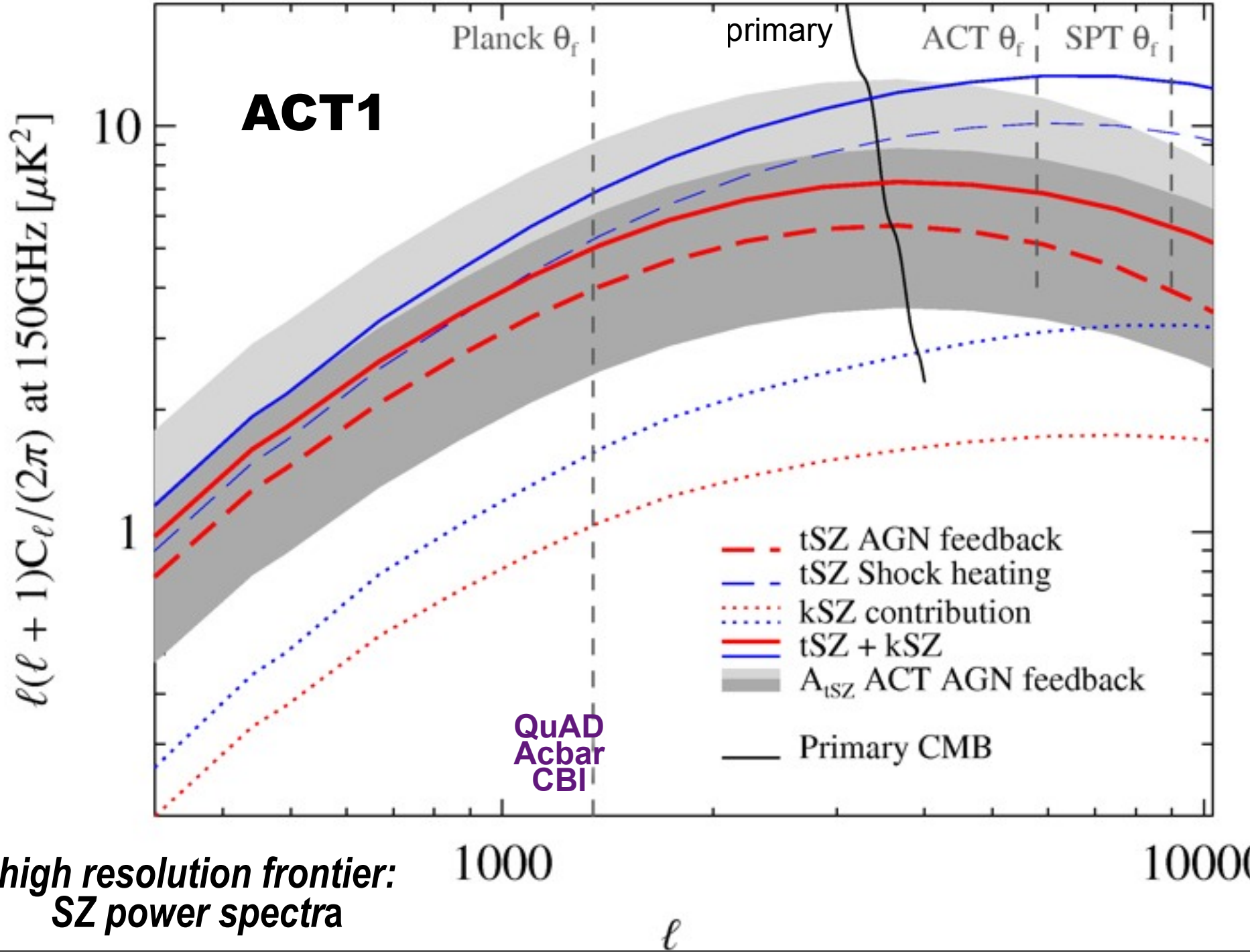


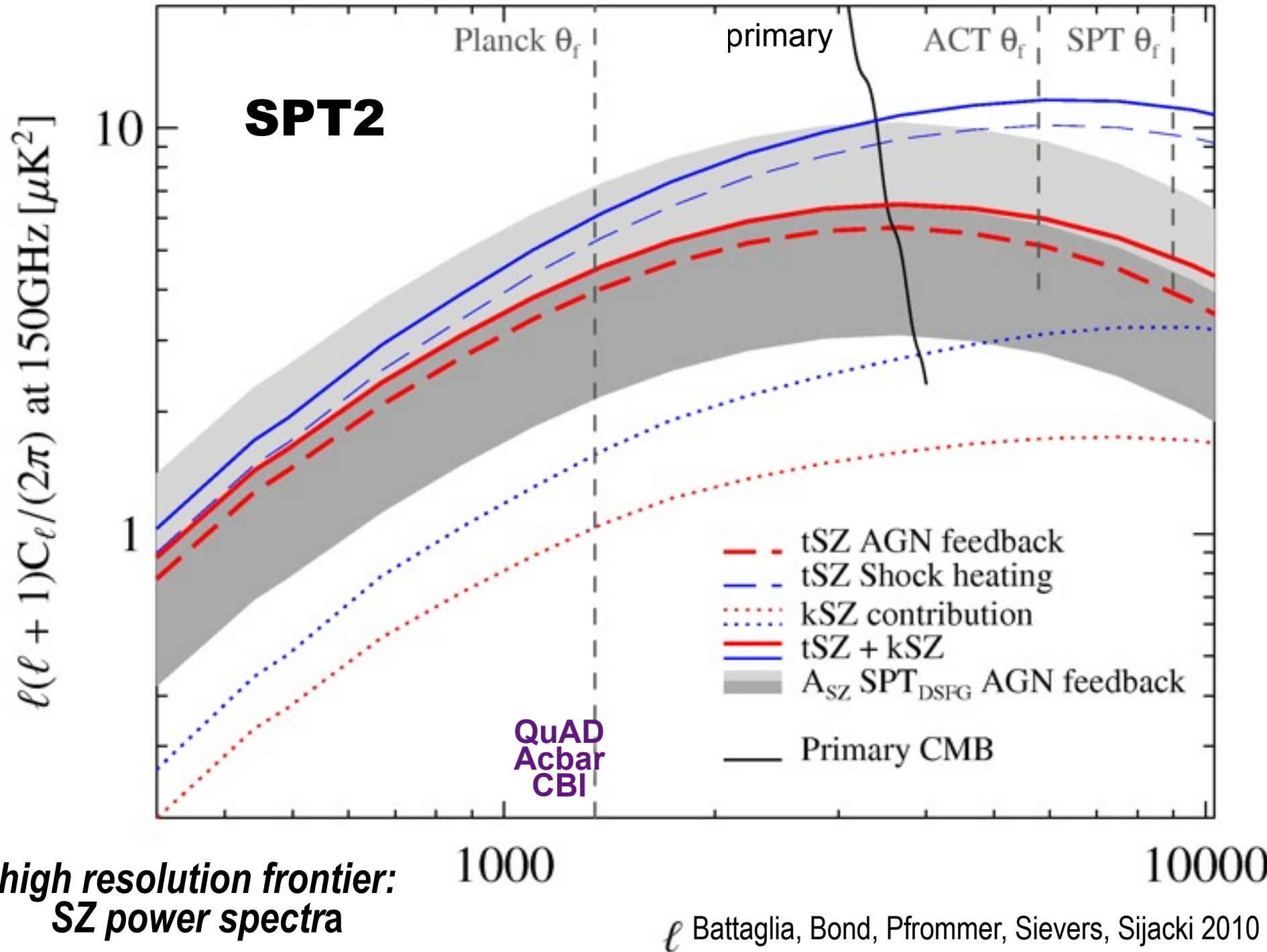


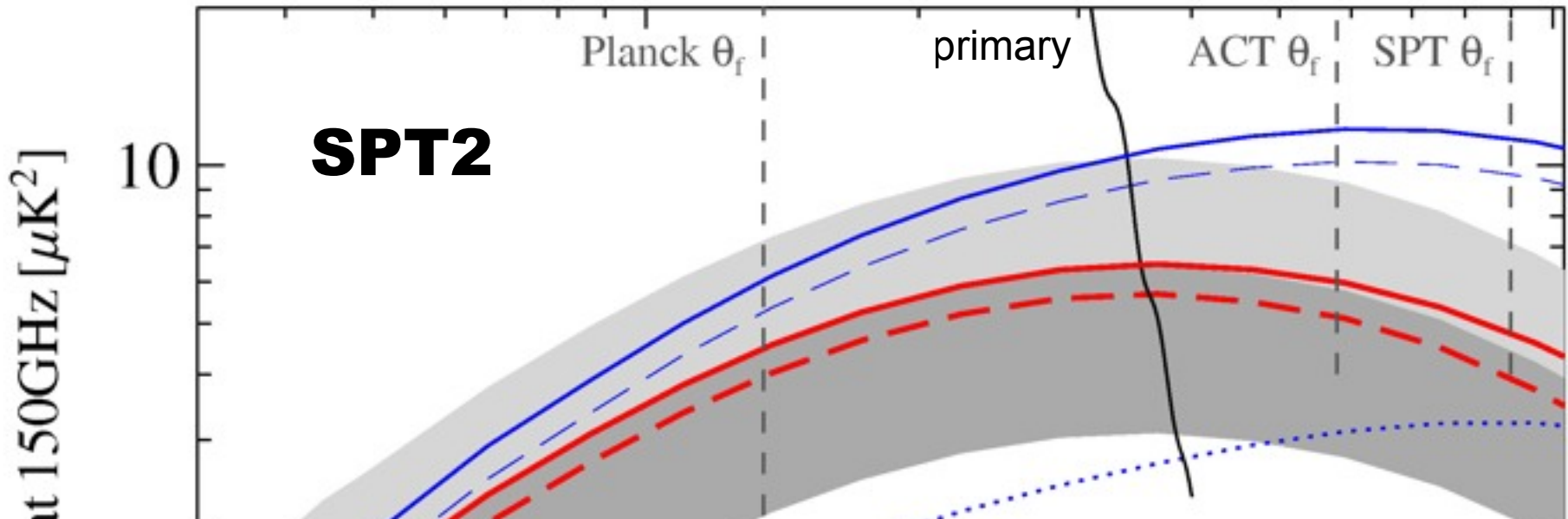






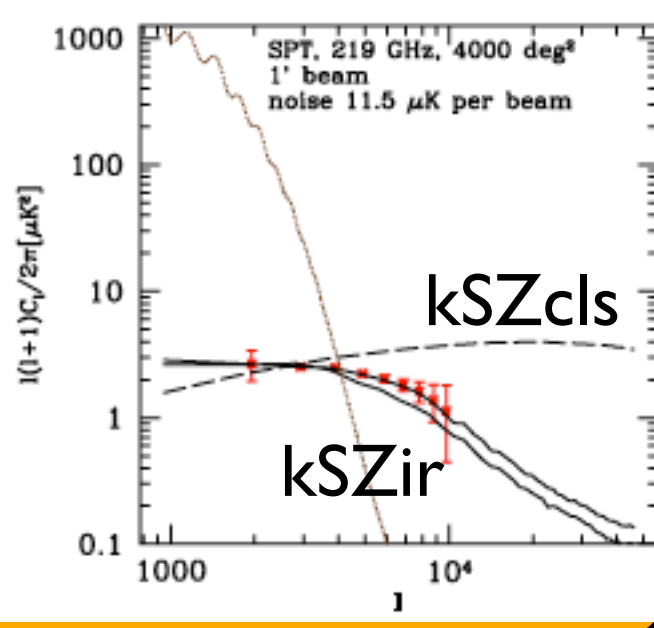
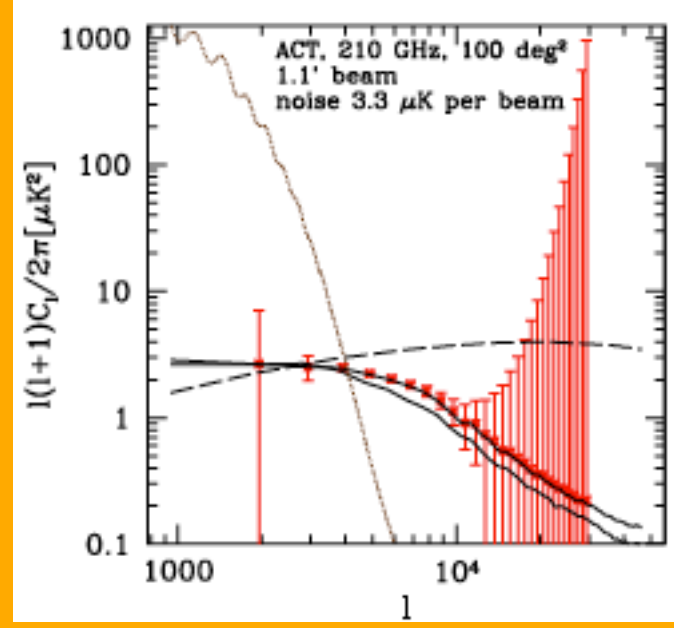






SPT2

no inhomog reionization-kSZ but Iliev etal 07,08



*high resolution frontier,
SZ power spectra*

l Battaglia, Bond, Pfrommer, Sievers, Sijacki 2010

n_{cluster}

($Y_{\text{SZ}}, M_{\text{lens}}, Y_X, L_X, T_X, L_{\text{cl,opt}}, R_{\text{ich}}, \dots$

| gold-sample, thresholds)

+ C_L^{SZ} (cuts) will deliver valuable

cosmic gastrophysics for sure.

**Will it deliver fundamental physics
e.g., the dark energy EOS, primordial
non-Gaussianity???** σ_8 even?

**so much for context
& theory &
forecasts.**

on to the results:

Planck, ACT, SPT,

Mustang on GBT,

AMI, SZA, APEX, Bolocam,...