

Novel LSS/CMB non-Gaussianities from Instabilities & Entropy Generation During and After Inflation



Generate fully-correlated nonGaussian Websky-Ensembles for CMB/LSS probes

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Bond+Braden+Frolov+Huang+Morrison+Stein
varieties of primordial nonG and how to search for them

Simons Modern Inflation group - b2fhms & Eva Silverstein+ & Dan Green+

Origin of the observed entropy in the Universe and SMpp/BSMpp particles

- coarse-grained coherent condensate breaks up into fine-grained fluctuations
- particle creation = (instability => stretch and break via mode-mode coupling aka fluctuation generation)
- episodic stretching (adiabatic) and breaking (non-adiabatic => nonG) during inflation & after

nonlinear multi-field classical coupled system. evolve using lattice simulations. via *pseudo-spectral code & symplectic defrost++ code* => very high accuracy to unveil small nonlinear effects leading to nonG

$$3\zeta(\mathbf{x}, t) = \int_{\text{field-path}} (dE + pdV)/(E + pV) = \text{Trace } \alpha^i_j + \int_{\text{field-path}} d \ln \rho_{Ec}/(1 + w_c)$$

during inflation (beyond stochastic inflation. nonlinear k-space burst structure)

$$\langle \Delta \mathcal{P}_{\phi^A \phi^A}(k) | \Delta V, \Delta m_{eff}^2 \rangle, \quad \langle \Delta \mathcal{P}_{\zeta \zeta}(k) | \Delta V(\phi, \chi) \text{ controls} \rangle \quad \langle \Delta \langle \prod \zeta^N \rangle_{cc} | \Delta V \text{ controls} \rangle \quad \text{SBB89, SB90,91 B95..}$$

& after inflation ends (modulated heating. marginalize ~50 e-folds of sub-LSS)

$$\langle \zeta_{NL} | \chi_{cg} + \chi \rangle_h$$

dynamical system Kolmogorov-Sinai entropy cf. true Shannon entropy
nonG ~ "particle" production ~ Shannon entropy generation

$$\Delta S_{\text{flucs}, k} = \text{Trace} \ln [C_{\phi^A \phi^B} C_{\Pi_A \Pi_B} - C_{\phi^A \Pi_B} C_{\Pi_A \phi^B}] / 2 \approx \ln(n_{\text{flucs}, k} + 1/2) \text{ cf. old way } \sim \ln[\rho_{Ak}(t) / \hbar \omega_{Ak}(t)]$$

adiabatic flucs encoded in the collective Phonons, fluctuations + condensate = ζ_k

$$\langle \delta_J(\mathbf{x}, t) | \zeta \rangle = \chi_{J\zeta}(\mathbf{x}t | \mathbf{x}_i) * \zeta(\mathbf{x}_i), \quad \chi_{J\zeta} = \text{linear transfer fn } \forall \text{ fields } J$$

varieties of primordial nonG and how to search for them

perturbative, nonG part correlated with dominant Gaussian part

*see Planck 2015/2018 nonG for exhaustive study and current constraints - 2018 including T+Epol
local f_{NL}* - current limit cf. f_{NL} target < 1. & equilateral orthogonal*

if uncorrelated quadratic nonG suppressed by at least $\sim \epsilon^2$

$$\langle \zeta_{\text{NL}} | \chi_{\text{cg}} + \chi_{>h} \rangle \sim \beta(\chi_{>h}) \chi_{\text{cg}} + f(\chi_{>h}) \chi_{\text{cg}}^2 +$$

$$f_{\text{NL}}^{\text{equiv}} = f [\beta P_\chi / P_{\zeta, \text{inf}}]^2 \quad \& \quad P_\chi / P_\zeta \lesssim \epsilon$$

**Planck2015 ... Planck2018 not yet
nonG 3-point-correlation-pattern measure**
f_{nl}: 2.7 ± 5.8 local for Newton potential
=> f_{NL}* = 0.44 ± 3.5 for phonons/3-curvature
-f_{nl}: 42.3 ± 75.2 equilateral
-25.3 ± 39.2 orthogonal

beyond Planck2015/2018 nonG: some nonG probes in Planck 2015/2018 Isotropy & Statistics. main result is no strong evidence, anomalies

outside horizon (very): via stochastic inflation - huge nonG from feedback via diffusion *sb90/91 semi-eternal*

k-localized nonG: wide open. role of instabilities during inflation to make k-localized zeta-bursts. could even make PBHs. chain together instabilities - oscillations in power and 3-point. silverstein and Planck

new silverstein et al approach. explore higher N-points => anomalous tails.

BBM numerical pseudo-spectral codes to correct stochastic inflation, all weakly nonlinear terms included. B2FHMS can ensemble-measure everything, N-pt, coherences!

nonG from heating: 1 cm comoving scale => to be in observable LSS/CMB bands need modulation, but that is natural if there are light fields (heavy fields damp power)

nonG in long-lived field-condensates: strings, oscillons, curvaton structures, ... short-scale short-lived

nonG bubbles from tunneling during inflation *bbm*

nonG from later phase transition structures - need first order (discontinuity in entropy - latent heat) cf. second order (discontinuity in second derivative aka in fluctuations) or smoother higher order, eg adiabatic evolution of particle content - entropy conserving

nonG from out-of-equilibrium decays

Bond+Braden+Frolov+Huang+Morrison & Stein



ζ TOPOGRAPHY & CARTOGRAPHY

of our Hubble-patch bit of the early universe: RECONSTRUCT

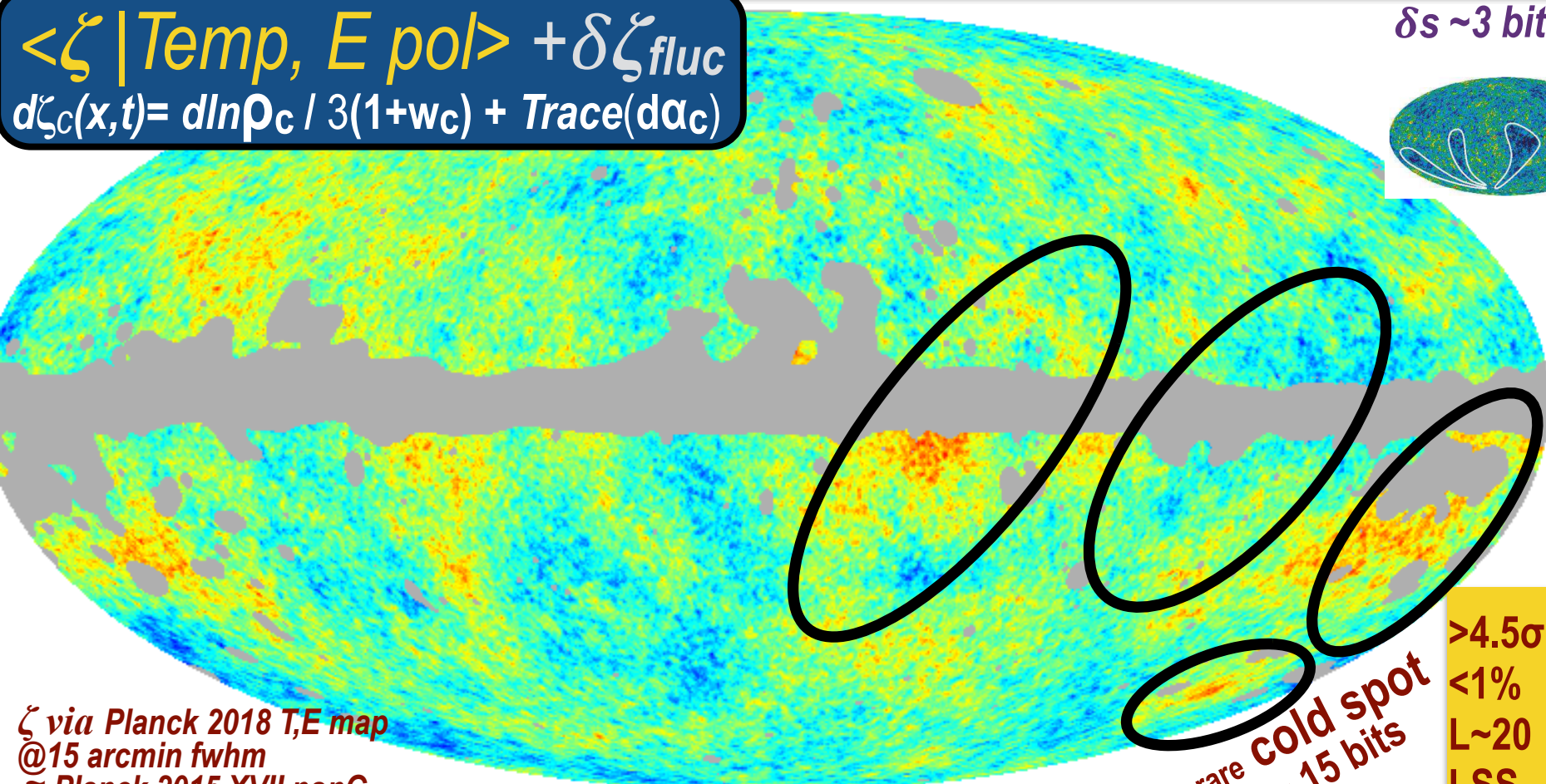
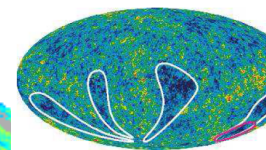
Beyond the Standard Model of cosmology? $SM_c = \text{tilted } \Lambda\text{CDM} + r \text{ via } (\zeta, h_{+x})$

BSM_c = SM_c + primordial anomalies (nonG) in the true ζ -WebSky anomalies @ low L => sample variance limited ~2σ's *CMB TT power L~ 20-30 dip => ζ-Spectrum k-dip*

$$\langle \zeta | \text{Temp}, E \text{ pol} \rangle + \delta \zeta_{\text{fluc}}$$

$$d\zeta_c(x,t) = d \ln \rho_c / 3(1+w_c) + \text{Trace}(d\alpha_c)$$

$\delta s \sim 3 \text{ bits}$

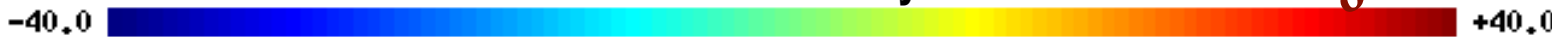


ζ via Planck 2018 T,E map
@15 arcmin fwhm
 \approx Planck 2015 XVII nonG

GUTA = Grand Unified Theory of Anomalies?

the rare cold spot
 $\delta s \sim 15 \text{ bits}$

>4.5σ
<1%
L~20
LSS
void?

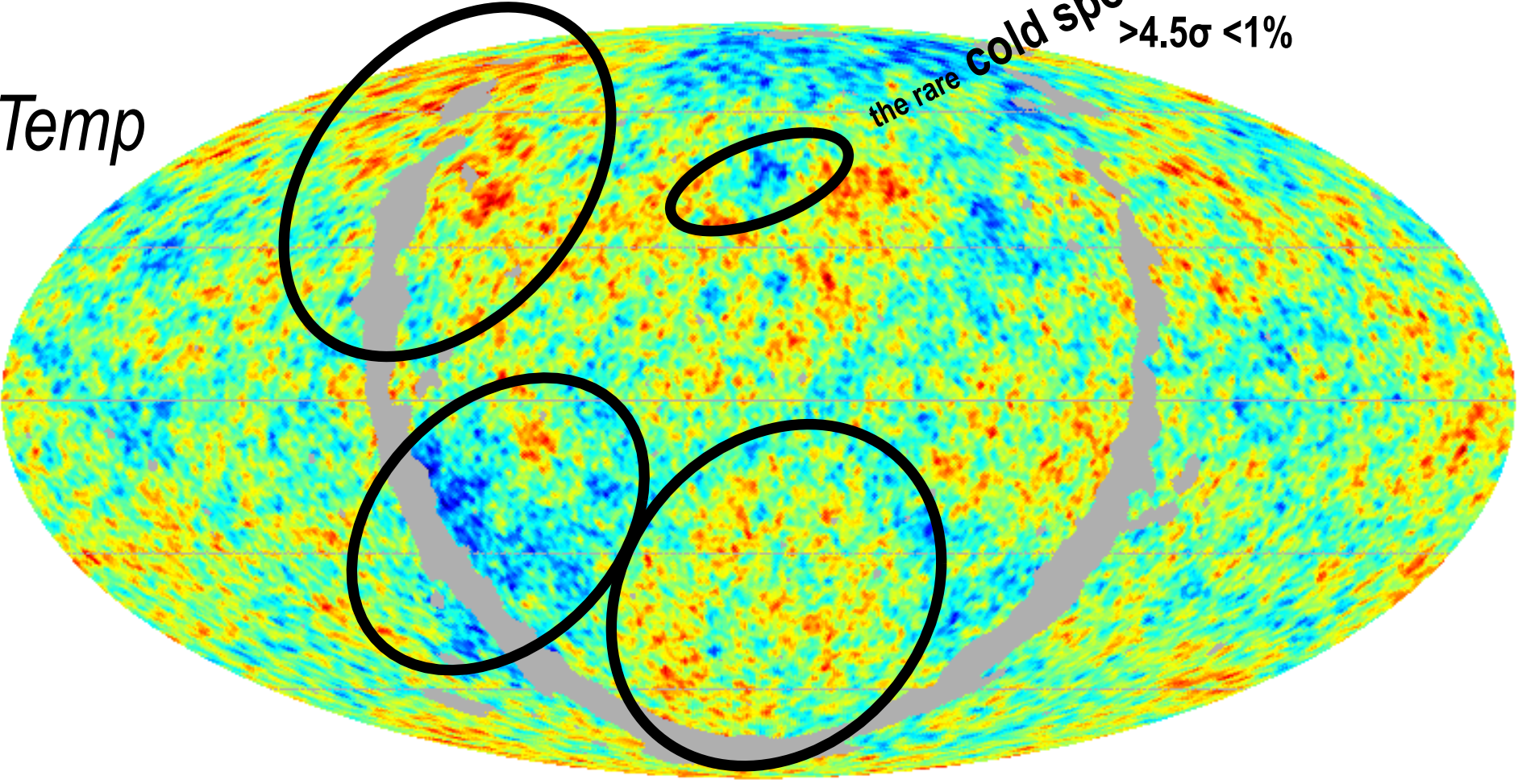


CMB ~10,000,000 T/E modes of Λ CDM
 \approx 500 modes of anomaly
 \approx 100 modes reionization history

CMB modes $LSS \Rightarrow$
 $\sim f_{\text{sky}} L_{\text{max}}^2$ tomography
 $\times k_{\text{max}} d_{\text{max}}$

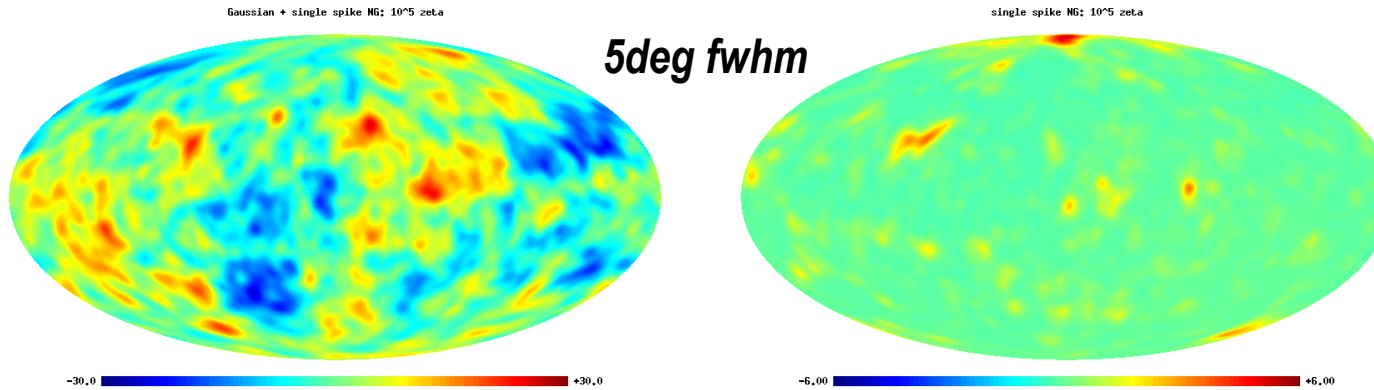
the rare cold spot
 $>4.5\sigma <1\%$

Temp



2D intermittency WMAP cold spot

CMB+LSS mocks to test: standard Gaussian inflaton ζ_{inf} + subdominant uncorrelated ζ_{isoc}
e.g., from modulated preheating



uncorrelated nonG 'wide open' cf. usual correlated highly constrained nonG

**scan sims to get
chance intermittent
alignment to get a
WMAP "cold spot"**

**intermittent nonG from
early U preheating
lattice sims**
- here tunable peak model

**also cf. quadratic nG:
correlated f_{NL}
uncorrelated large f_{NL}^{eff}**

the true quadratic ζ -Websky of the ζ -scape

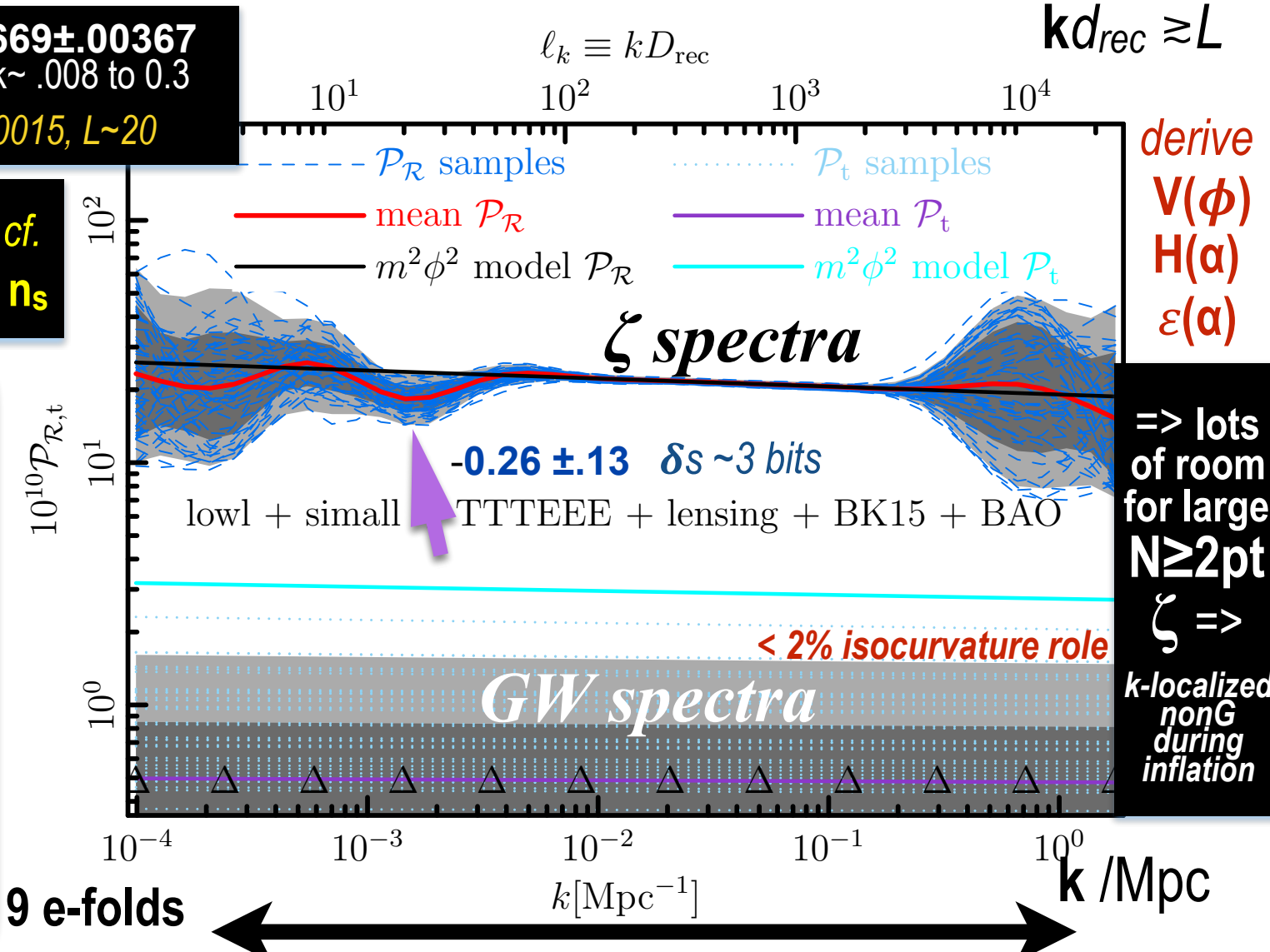
Planck 2018 X inflation: TTTEE lowL Epol + CMB lens + BK15 BB + BAO

Anomalies in CMB TT power: $L \sim 20-30$ dip $\Rightarrow \zeta$ -Spectrum k -dip $\sim 2\sigma$
 includes CMB lensing, parameter marginalization

uniform $n_s = 0.9669 \pm 0.00367$
 superb 12-knot fit $k \sim .008$ to 0.3
 $\delta s \sim 3$ bits @ $k \sim .0015, L \sim 20$

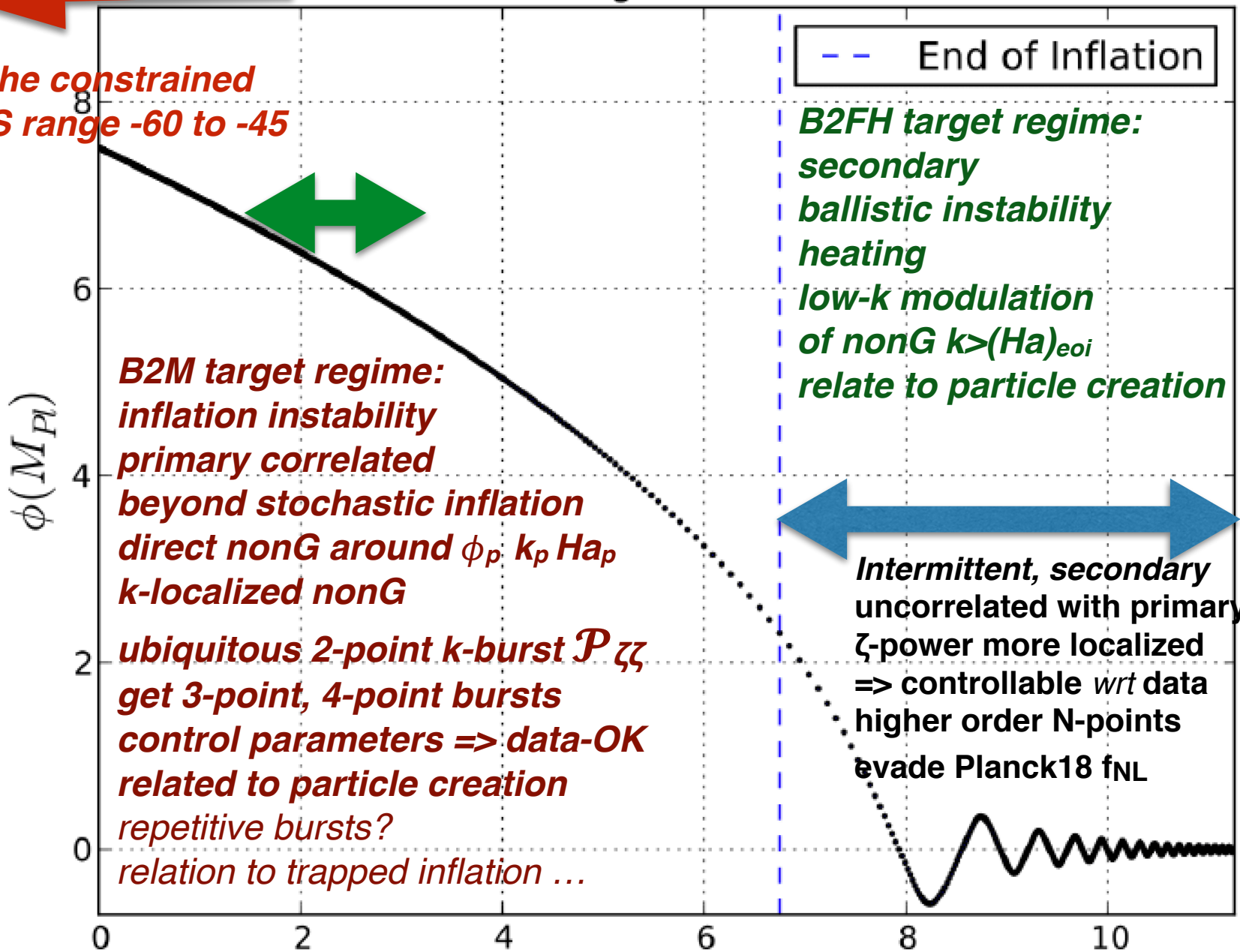
$r < 0.069$ 95%CL cf.
 $r < 0.061$ uniform n_s

stochastic inflation
 $|\phi_{cg}; \phi_{fg}\rangle$
 coherent state picture of coarse-grain condensate + fine-grain bugoliubov fluctuations QM-correct





to the constrained LSS range -60 to -45

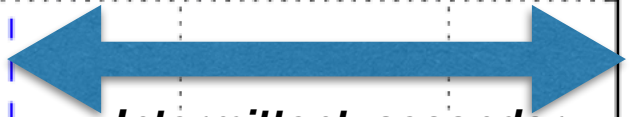


-- End of Inflation

*B2FH target regime:
secondary
ballistic instability
heating
low-k modulation
of nonG $k > (Ha)_{eoi}$
relate to particle creation*

*B2M target regime:
inflation instability
primary correlated
beyond stochastic inflation
direct nonG around $\phi_p, k_p, H a_p$
k-localized nonG*

*ubiquitous 2-point k-burst $\mathcal{P}_{\zeta\zeta}$
get 3-point, 4-point bursts
control parameters => data-OK
related to particle creation
repetitive bursts?
relation to trapped inflation ...*



*Intermittent, secondary
uncorrelated with primary
 ζ -power more localized
=> controllable wrt data
higher order N-points
evade Planck18 fNL*

apply to PBHs etc!!

$\ln(a)$

WebSkys: Mocking with *PeakPatches*+*Hydro*+



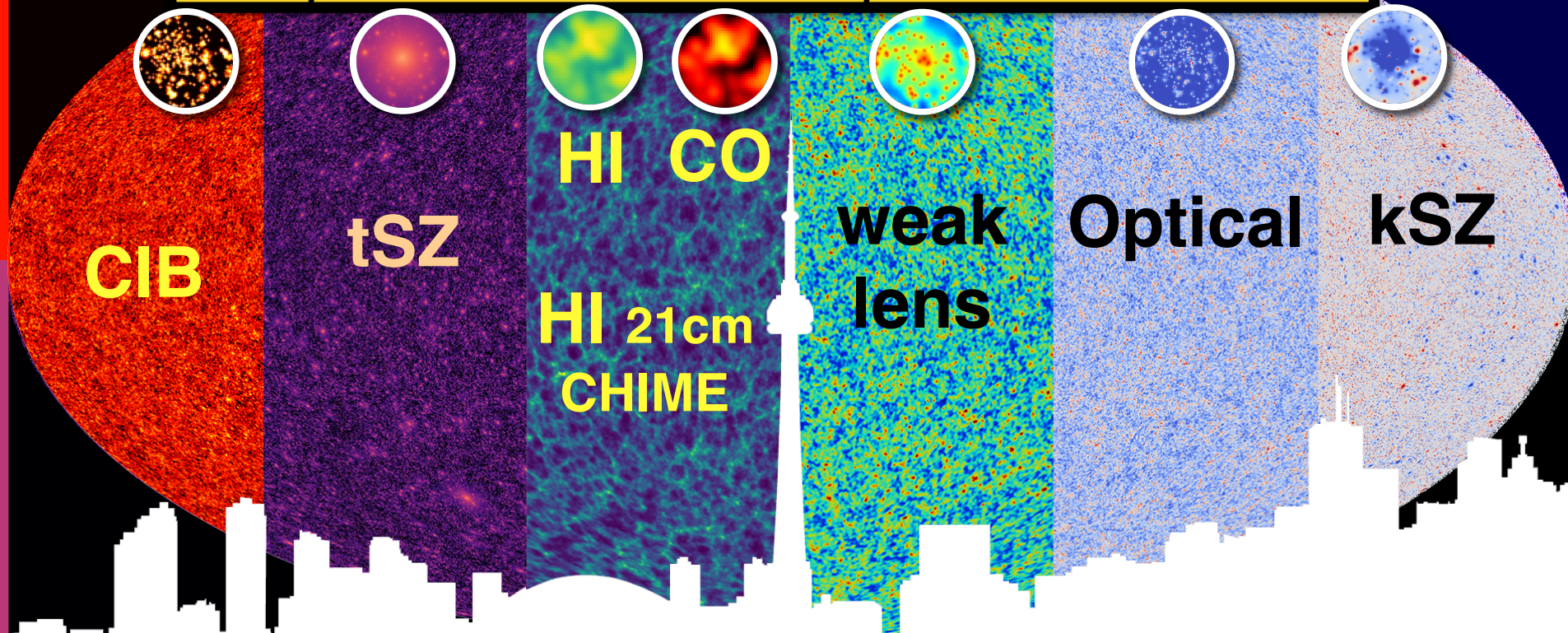
THEN BBKS, BCEK, B+Myers91,93,96, BKP96 web, BW96 importance

NOW: CITA mini-industry *Alvarez, Bond, George Stein* 2018, .. Validation SAB18 + Euclid 2018 validation a,b,c

Berger, Battaglia, Codis, van Engelen, Motloch, Huang, Frolov,

now 19.2 *Lague, Lokken, Murray, Keating, Lahklani, Breyse, bruno, connor, ronan, furen, remi, jason lee* ++

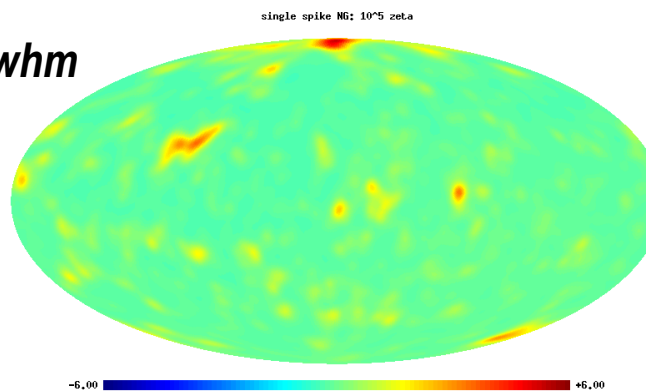
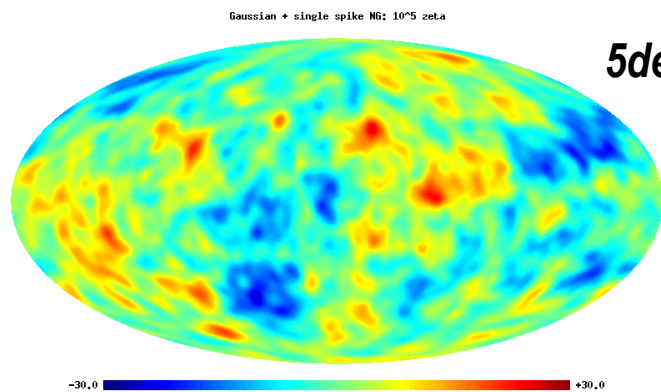
need **End to End** mocks: **BSMc, nonG, DE/modG, Mnu, ...**
need all signals to be correlated, 1, 2, 3, .. Npt
need speed to build ensembles & explore BSMc



Planck, AdvACT, SO, CMB-S4, CCATp, EUCLID, LSST, *DES*, CHIME, HIRAX, COMAP, ...SKA

2D intermittency WMAP cold spot

CMB+LSS mocks to test: standard Gaussian inflaton ζ_{inf} + subdominant uncorrelated ζ_{isoc}
e.g., from modulated preheating



scan sims to get chance intermittent alignment to get a WMAP "cold spot"

intermittent nG from early U preheating lattice sims

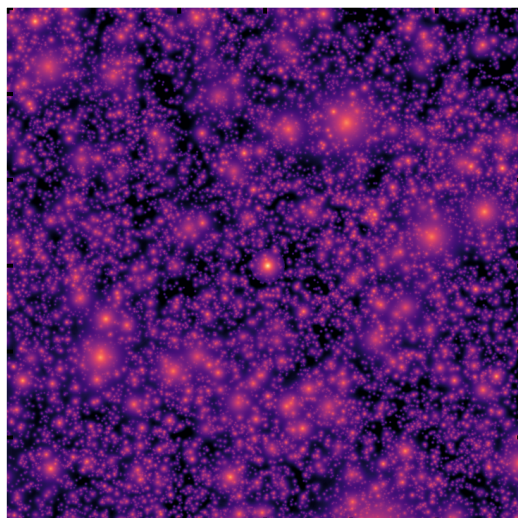
tunable peak model

also cf. quadratic nG: correlated fNL

uncorrelated large fNL_{eff}

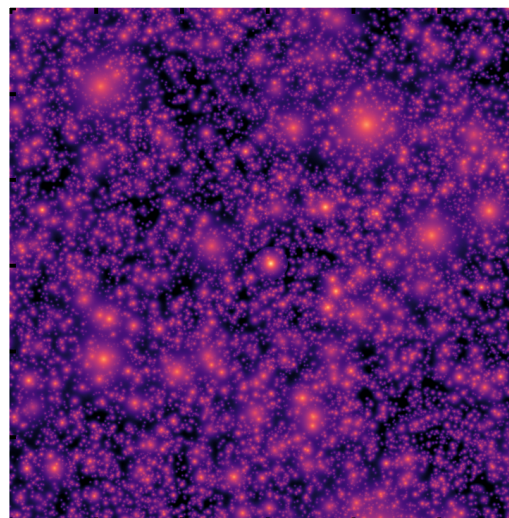
3D intermittency *uncorrelated nonG 'wide open' cf. usual correlated highly constrained nonG*

LSS tSZ: Gaussian std



B2FH, b+braden+frolov+huang

LSS tSZ: Gaussian std + subdominant uncorrelated ζ



ABSB+FH, alvarez+b+stein+frolov+huang

COMap sims using Li+ Mhalo \Rightarrow L_{CO} cf. CIB *a la* Planck13,15

Danger: correlated stochasticity of bursty star formation etc.



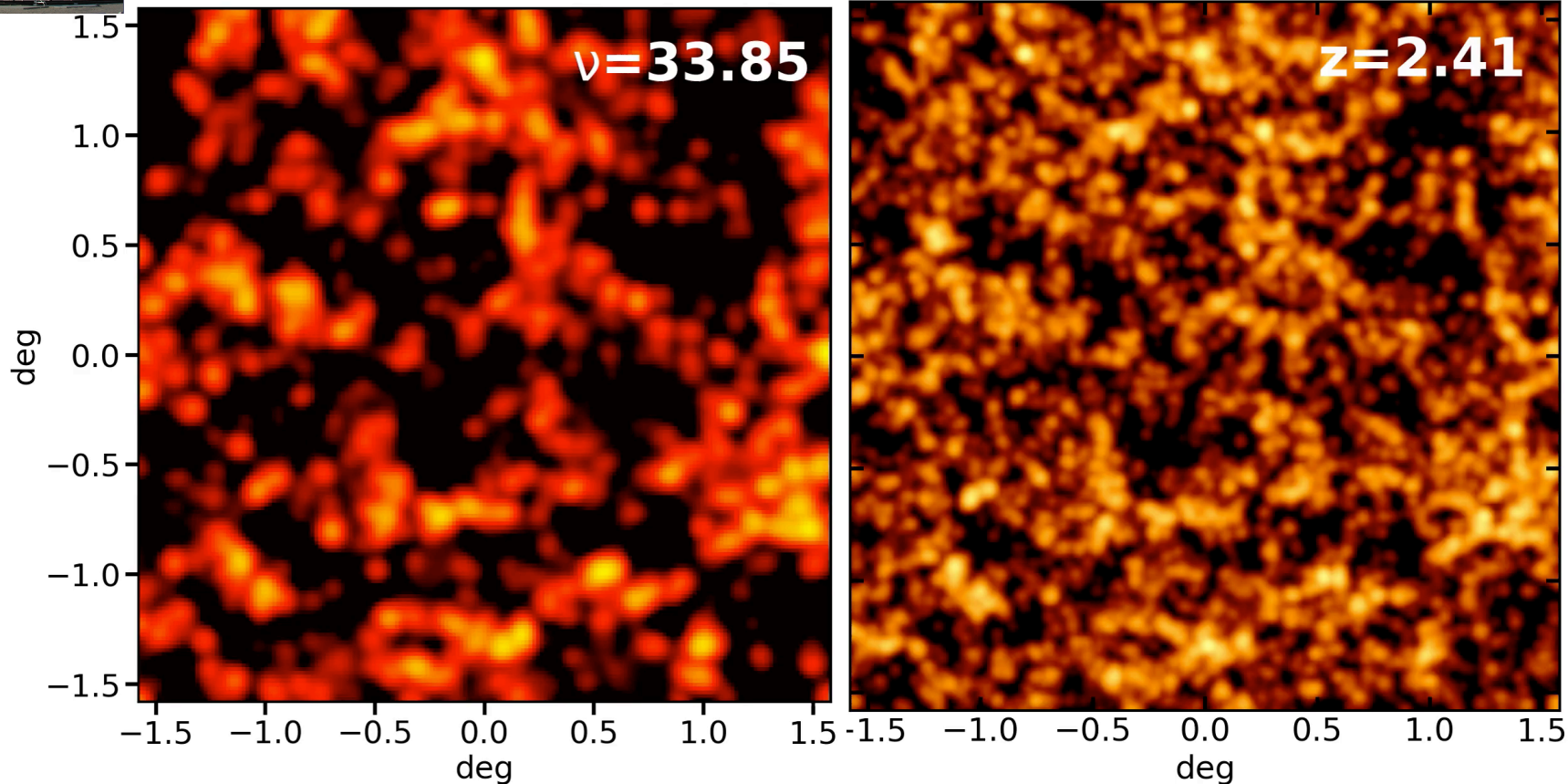
$z=2.4-3.4$ eventually $z=6-8$ cf. CHIME HI $z=.8-2.5$

CO

using Li et al. 2016 Model

CIB

using 217 GHz Planck 2015 Model, no tomography



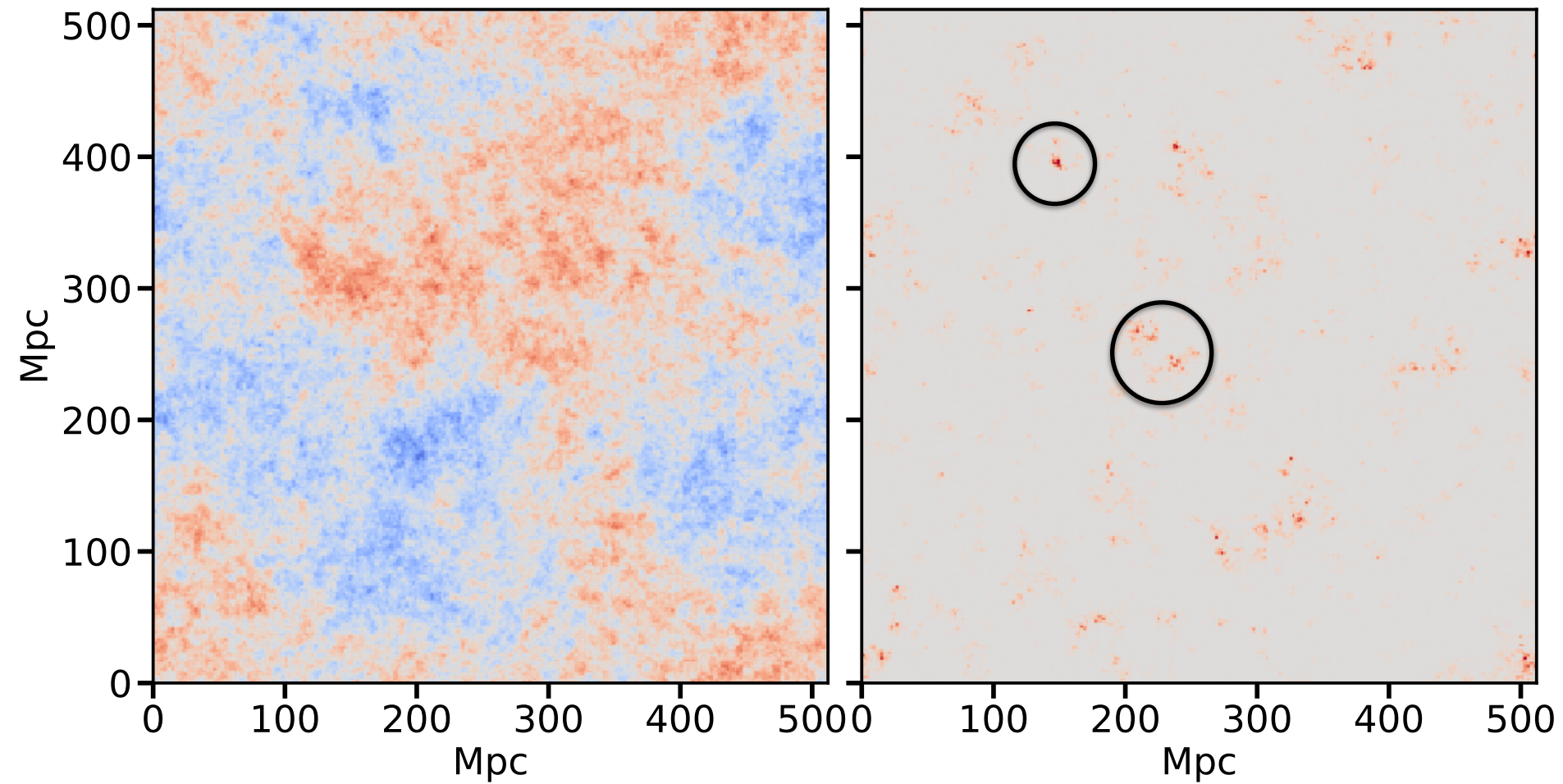
underway: **Lensing of CIB COMap HImaps kSZ tSZ**
nonG sources seen through a nonG lens

Primordial Non-Gaussianity in observable Webskys constructed with the mass-Peak Patch method
+ gas-halo response functions/susceptibilities

Intermittent Non-Gaussian case
uncorrelated ζ [GRF]

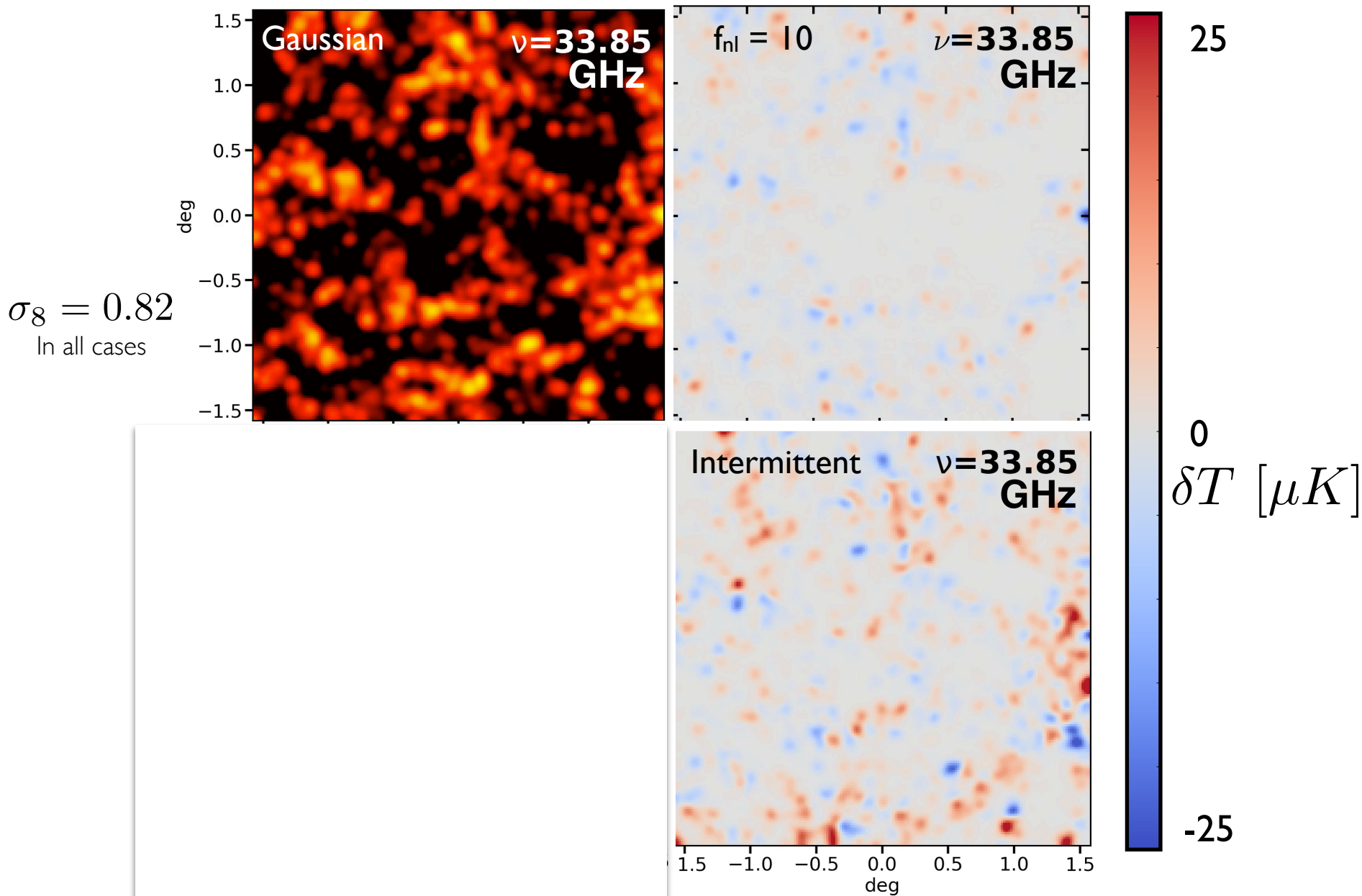
ζ_G

$\zeta_{F(\chi)}$



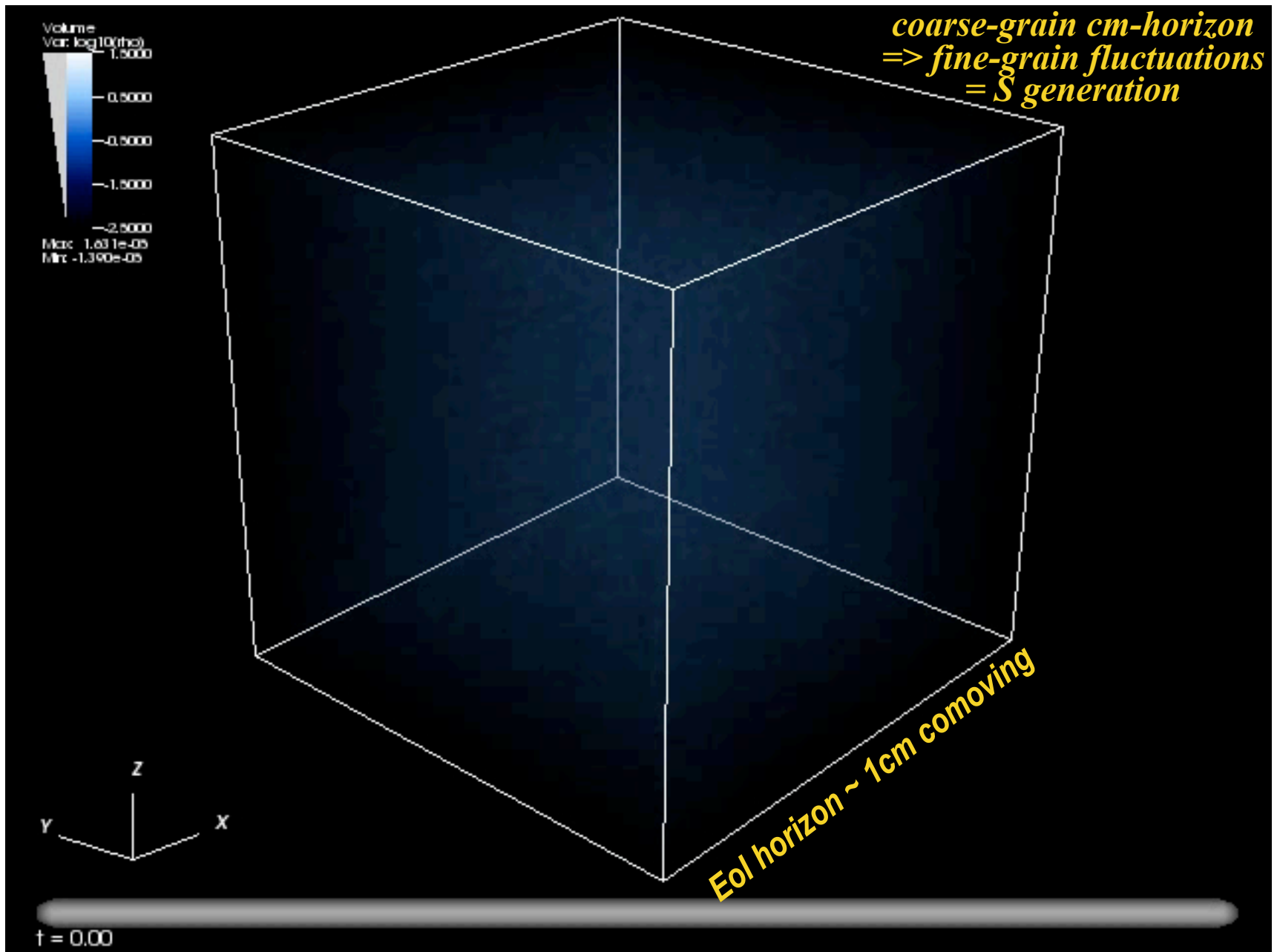
Bond , Huang, Stein; Braden, Morrison, ...

Primordial Non-Gaussianity in CO example: the LCDM signal and 2 nonG difference maps - a movie



large scale => CHIME much larger volume is better

$$\text{quartic inflaton } V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



log-normal pdf (density aka ζ), in k-bands too; normal pdf (velocity)

after inflation - instabilities => entropy => nonG

$$dS/dt(t, g) =>$$

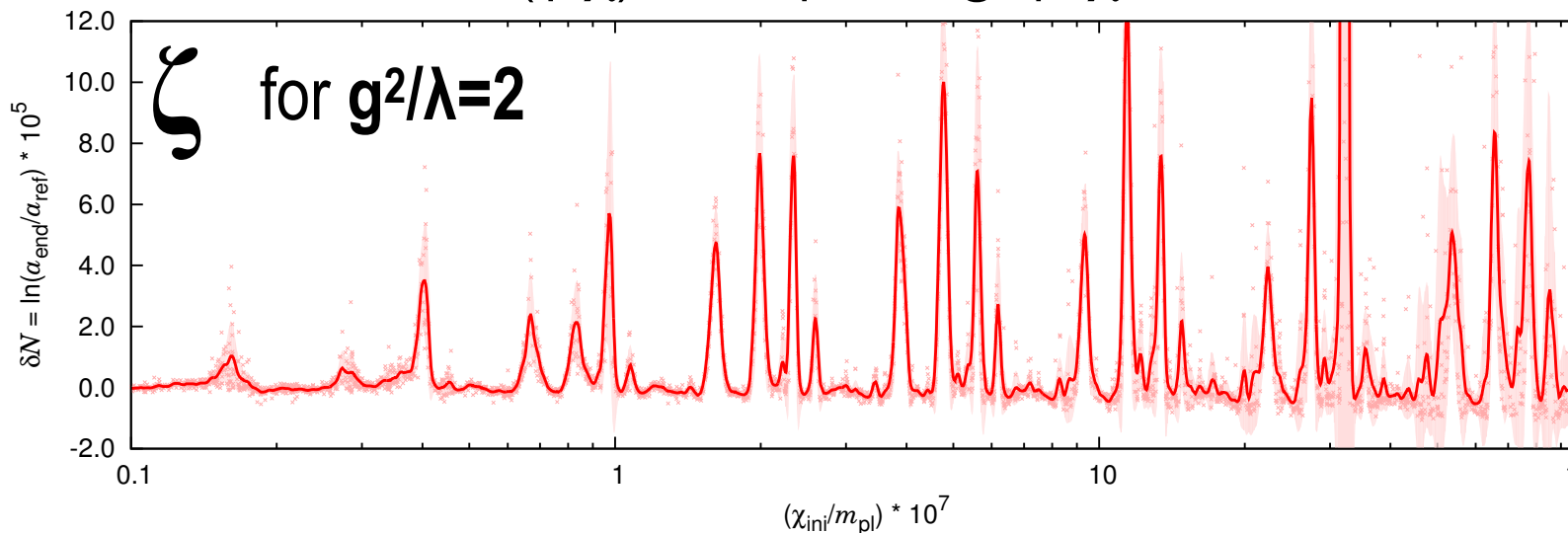
the Shock-in-time: entropy production rate

$$\zeta_{\text{shock}}(\chi_{c, \text{eoi}}(x) | g^2/\lambda) => \text{Chaotic Billiards: NonG from Parametric Resonance in Preheating}$$

B+Frolov, Huang, Kofman 09

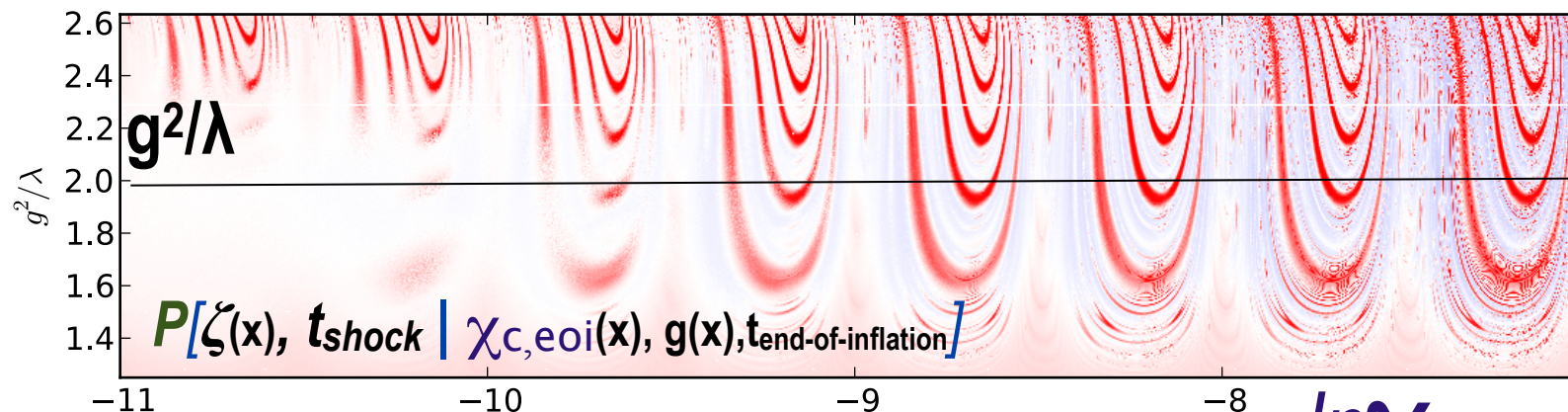
B+Braden, Frolov, Huang 19

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



smooth over
~50 e-folds of
HF structure
 $\chi_c \Rightarrow \zeta_c$
 ζ -bias cf.
late-time
density-bias
 $\chi_{>h}$ control
parameter

computational
tour de force



huge number of
 64^3 sims to
show the
wondrous
complexity of
 $\zeta(\chi_c, g^2/\lambda)$

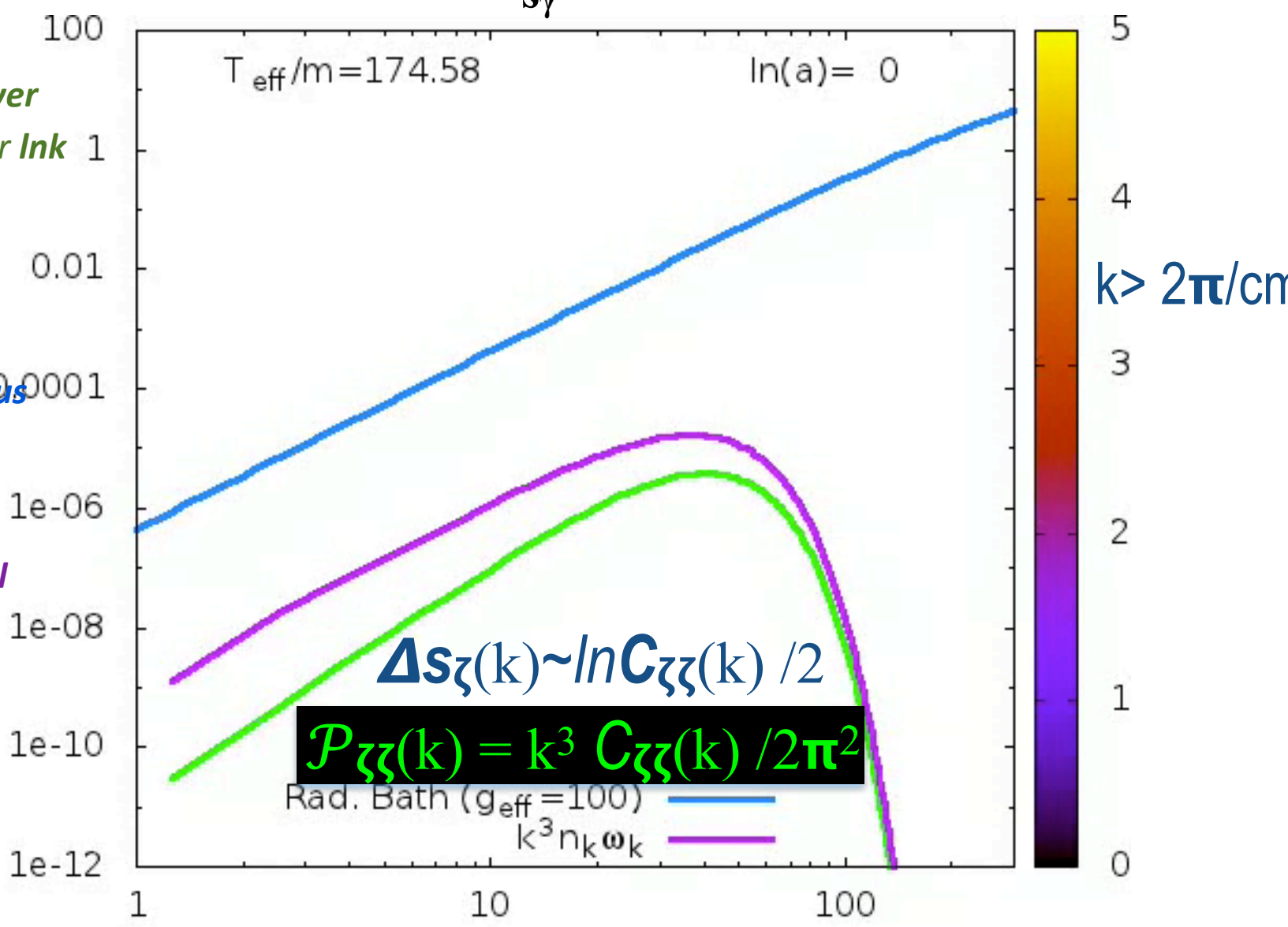
gigafigure of lattice simulations $\ln(\chi_0/\phi_0)/\mu_0 T$

$\ln \chi_{c, \text{eoi}} / \text{MPL}$

coherent inflaton => incoherent mode cascade of fields thru a shock-in-time to thermal equilibrium

$S_{U_i} \sim 0$; $S_{U_{tot,m+r}} / n_b \sim 1.66 \times 10^{10} \text{ bits/b}$; $s_\gamma / n_\gamma = 5.2 \text{ bits}/\Upsilon = 2130/411$; $s_v = 21/22$

In $p/\langle \rho \rangle$ power spectrum per $\ln k$ aka entropy aka phonon aka ζ cf. instantaneous full thermal spectrum cf. conventional energy spectrum using a pseudo particle occupation number

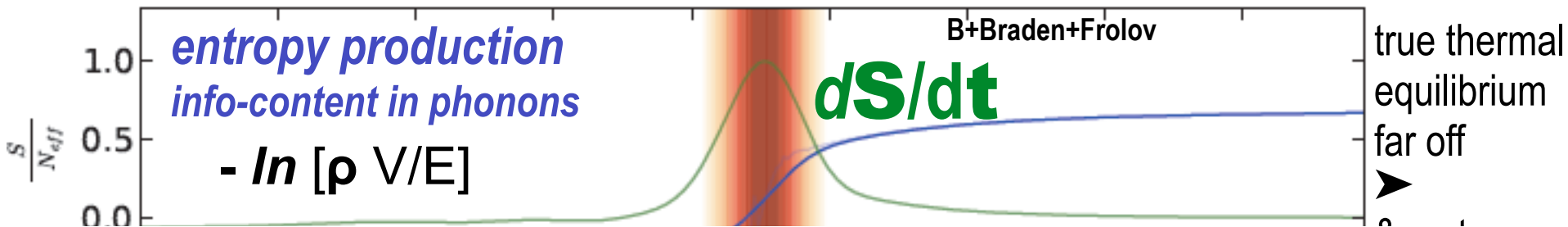


$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2$

k/m momentum

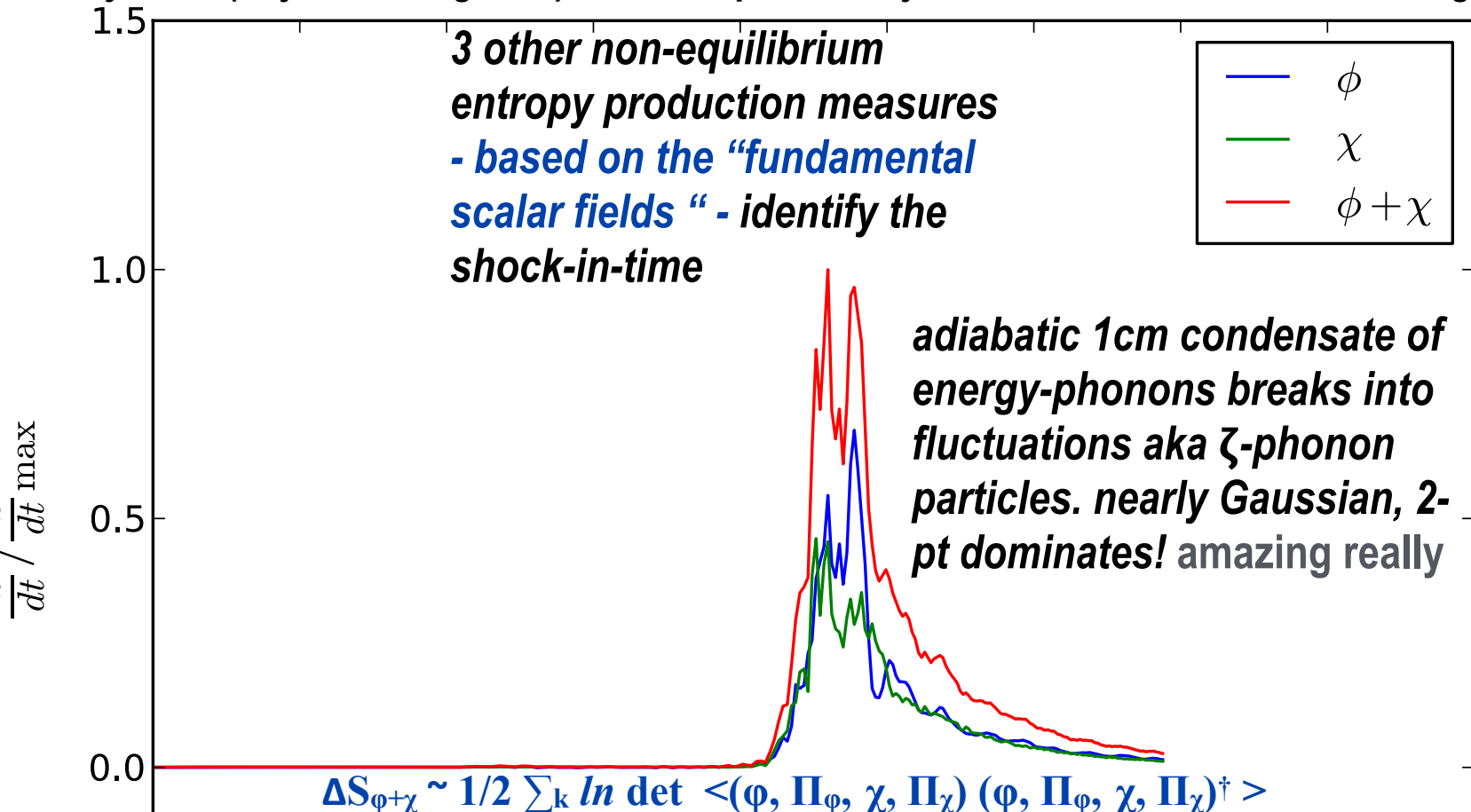
B+Braden+Frolov

nonG from large-scale modulations of the shock-in-times of preheating

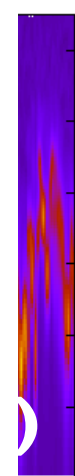


entangled primary fields $(\phi, \Pi_\phi, \chi, \Pi_\chi)$

decay rates (Feynman diagrams) and transport theory difficult to make accurate through preheating



of



generic nature of ζ -spikes post inflation - lessons learned

< ζ | V-control χ -control g^2 -control, ...>

multi-arm/filament potentials: here 4, but 3, 5-star, .. angular $V = \sum V_M(r) \cos(M\theta)$

modulate coupling “constants” in potential, g^2/λ g^2 controlled by 3rd field

spikes are ubiquitous though details change

understood via caustics of trajectory bundles: Lyapunov = strain-rate > 0

Kolmogorov-Sinai entropy (rate) = \sum positive strain-rate eigenvalues

field-strains of the deforming condensate in the ballistic regime - instability

probability density bundles stretch s.t. - $\ln \rho = \text{Trace strain}$ (Shannon conserved)

$\zeta(x,t)$ is conserved at each x in the ballistic regime

stopped by the shock in time: a burst of phonon production to alleviate the strain

$\zeta(x,t)$ is not conserved Shannon entropy $S = -\ln \rho \sqrt{G} = -\ln \rho - \text{Trace strain}$

spectrum of phonons is very non-thermal

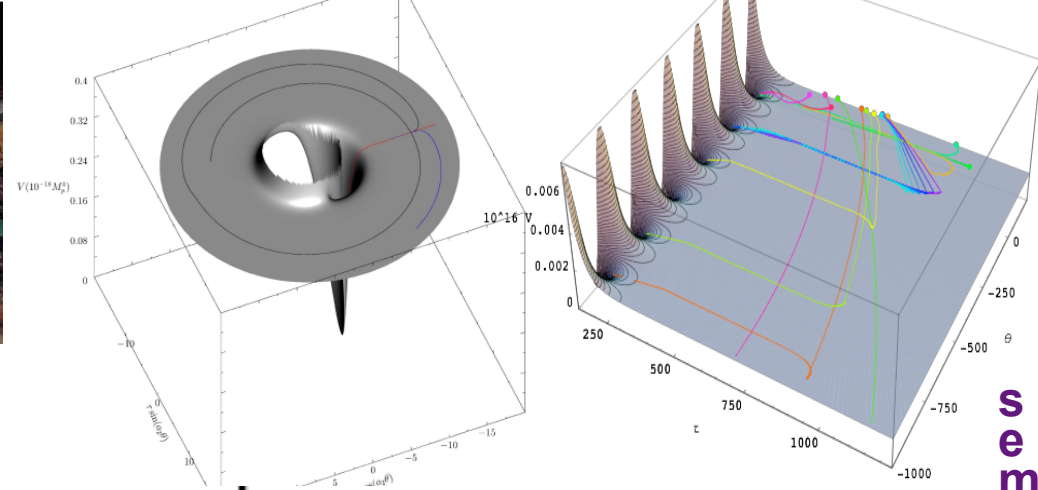
slow adiabatic evolution toward thermal

phonons are the control variables for the other field degrees of freedom

\Rightarrow subdominant nonG ubiquitous, need χ -light

single field V heating slow, oscillating
 but shaped V can give rapid heating (roulette)
 still driven by a radial instability $m^2_{\text{eff}} < 0$
 field-strain story the same but no modulation
 \Rightarrow transverse fields to get observable nonG

$$a = 1$$



A visualized 2D slice
 in lattice simulation

Preheating After
 Roulette Inflation

$$\langle \tau \rangle =$$

quantum
 diffusion
 spatial jitter

drift

E_{ol}



$$m^2_{\text{eff}} = 0$$

roulette oscillations
 highly damped
 \Rightarrow no-non-G



let there be
 heat

if redirect by χ_{eoi} , g
 \Rightarrow non-G??



E_{ol} horizon $\sim 1\text{cm}$ comoving

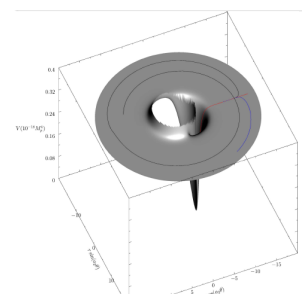


SEMIFINAL EMERGENT NON

stochastic inflation:
 the battle of classical drift V_C &
 diffusion of quantum fluctuations V_D
 $V_C \sim \nabla S_R$ $V_D = D_H \nabla S_I$
 eternal inflation $\Rightarrow V_D$ dominates
 emergence $\Rightarrow V_C$ dominates

inflaton+isocons potential $V(\varphi, \chi, \dots) = ?$

$\varphi_C, \chi_C, \dots, \alpha_C, H_C$



$V(\varphi, \chi, \dots)$

Preheating After
 Roulette Inflation

$\langle \tau \rangle =$

$\hbar H_C$
 quantum
 diffusion
 spatial jitter

entropy
 generation in
 preheating
 from the
 coherent
 inflaton
 (origin of all
 matter)

$-M_{Pl} \nabla \ln H_C$
 drift

isocon directions χ
 e.g., axion

let there be
 heat

SEMI-ETERNAL
 INFLATION-
 NO
 ENERGE

conformal potential-flattening eg Higgs inflation SBB89 etc

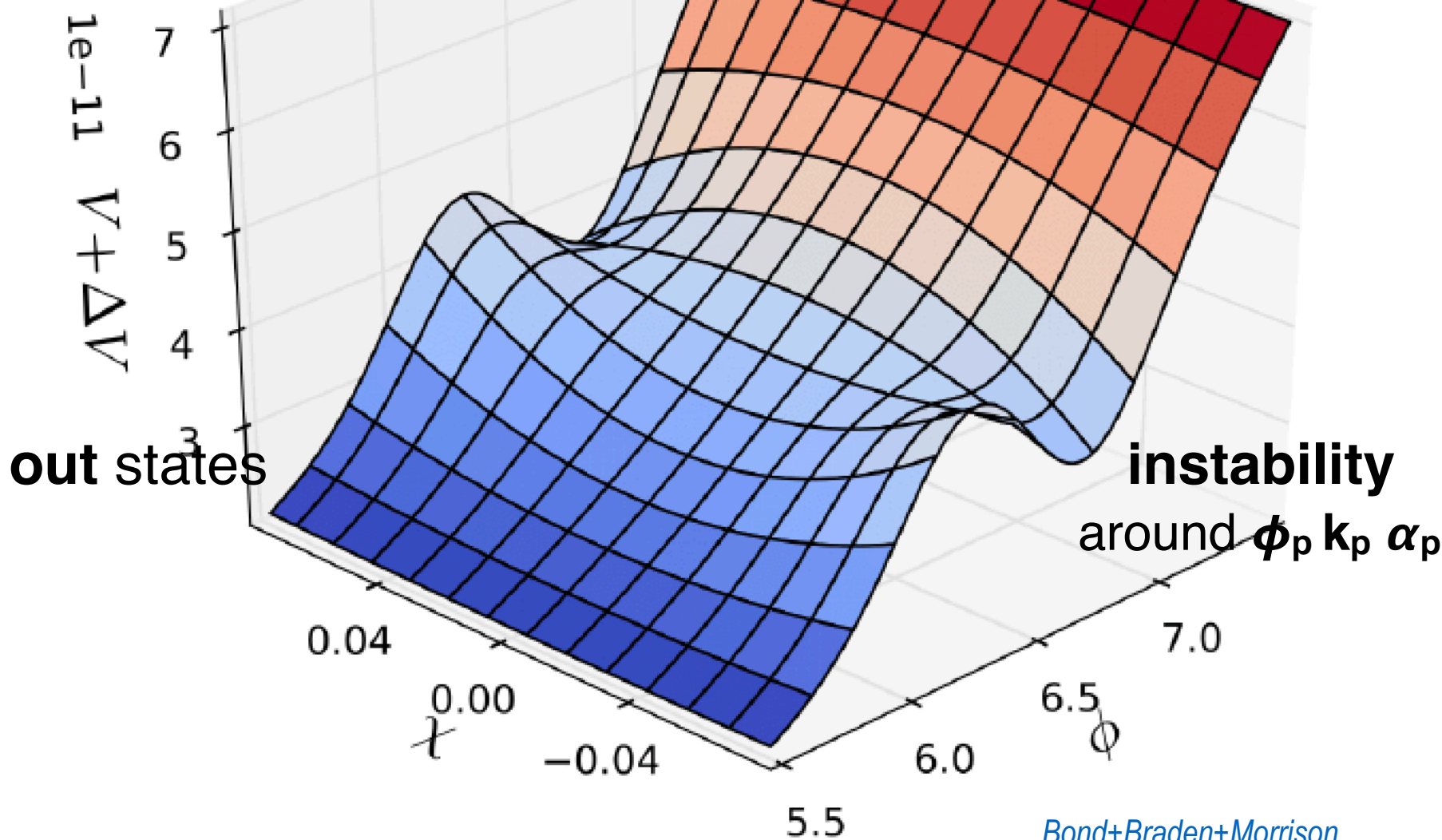
B2FH, b+braden+frolov+huang

during inflation - instabilities => entropy => nonG

*numerical experiments
of in-out states through
localized ΔV .
chain together .. oscillating*

experiment χ -light

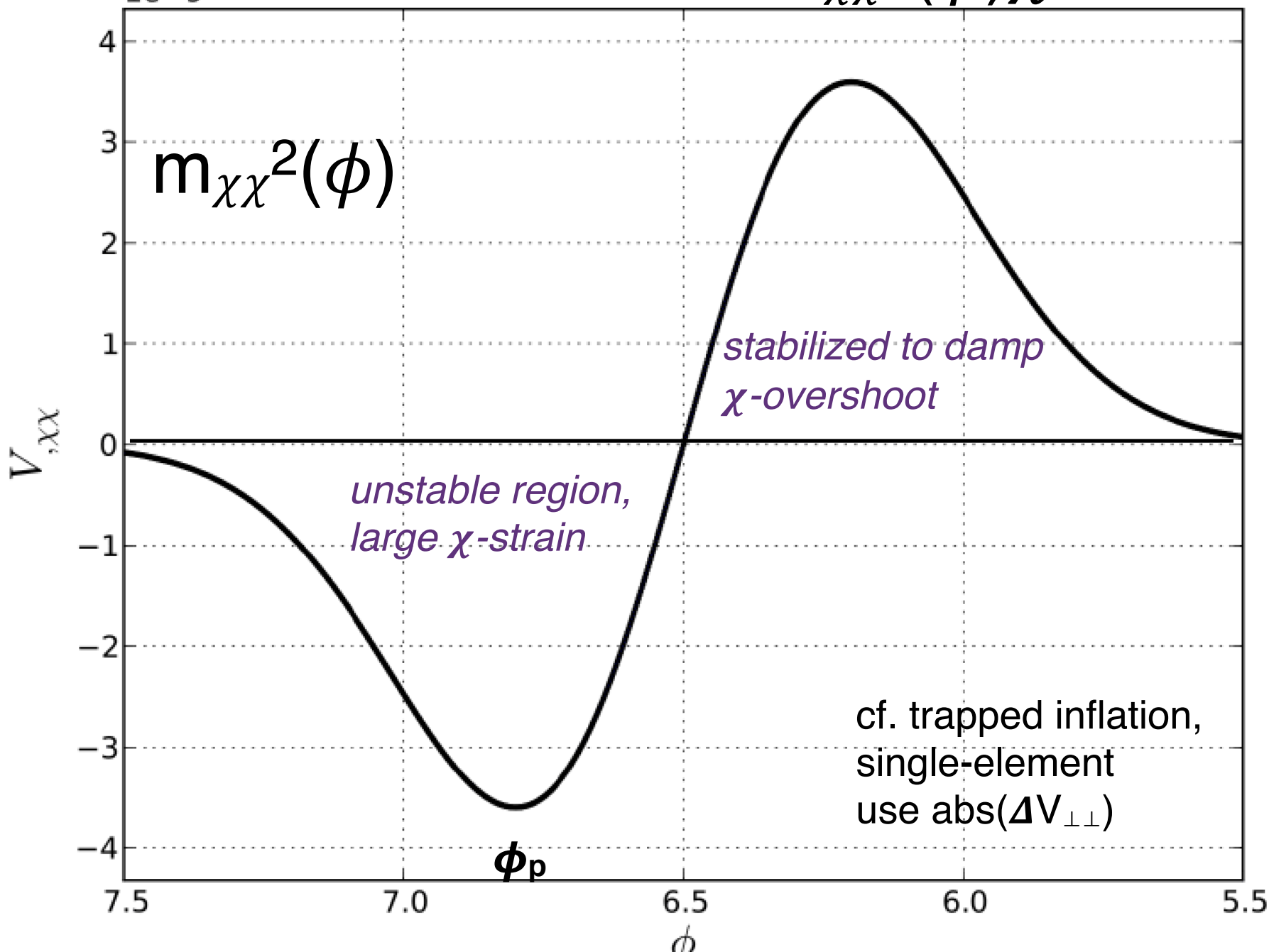
in states

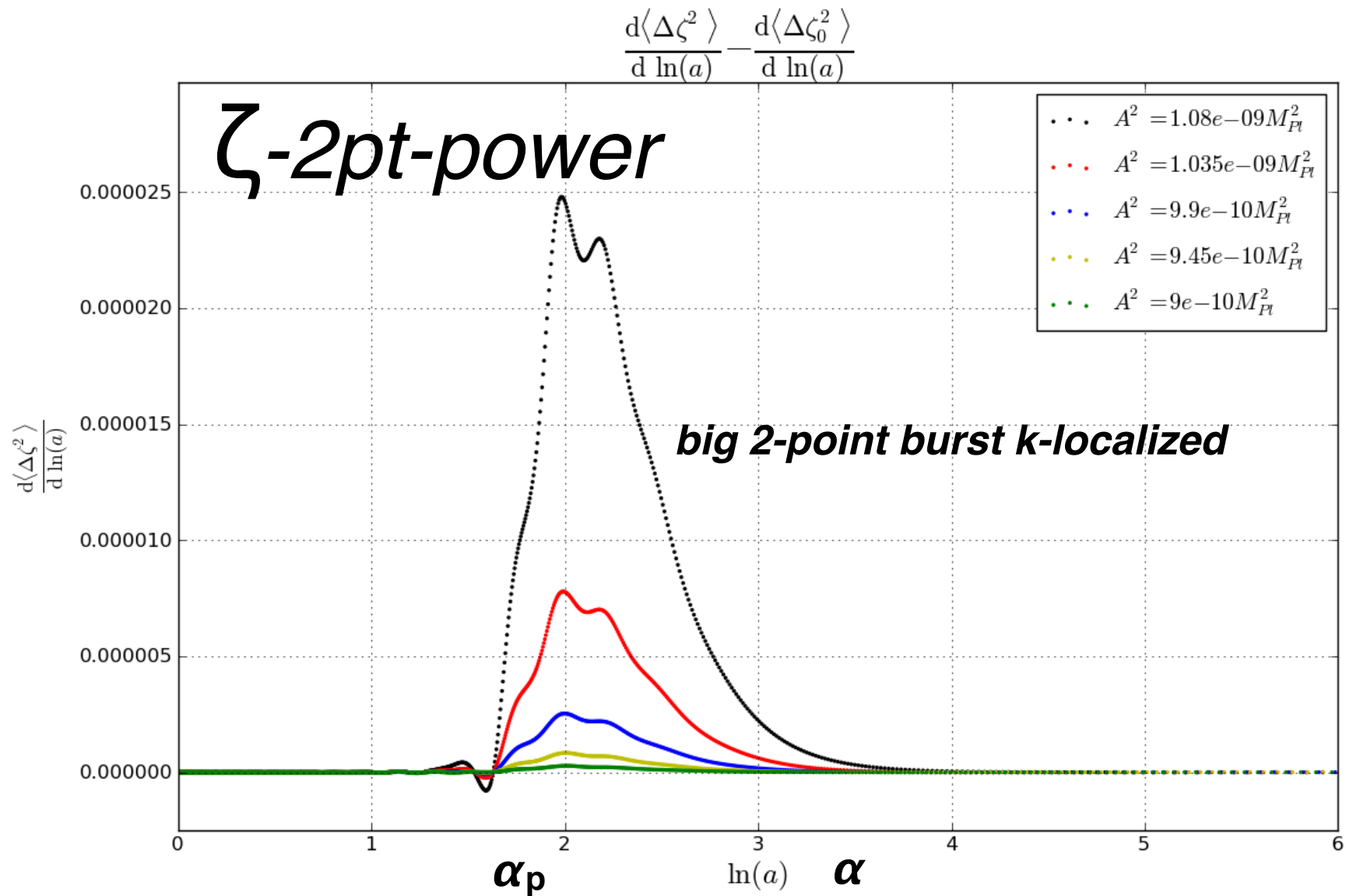


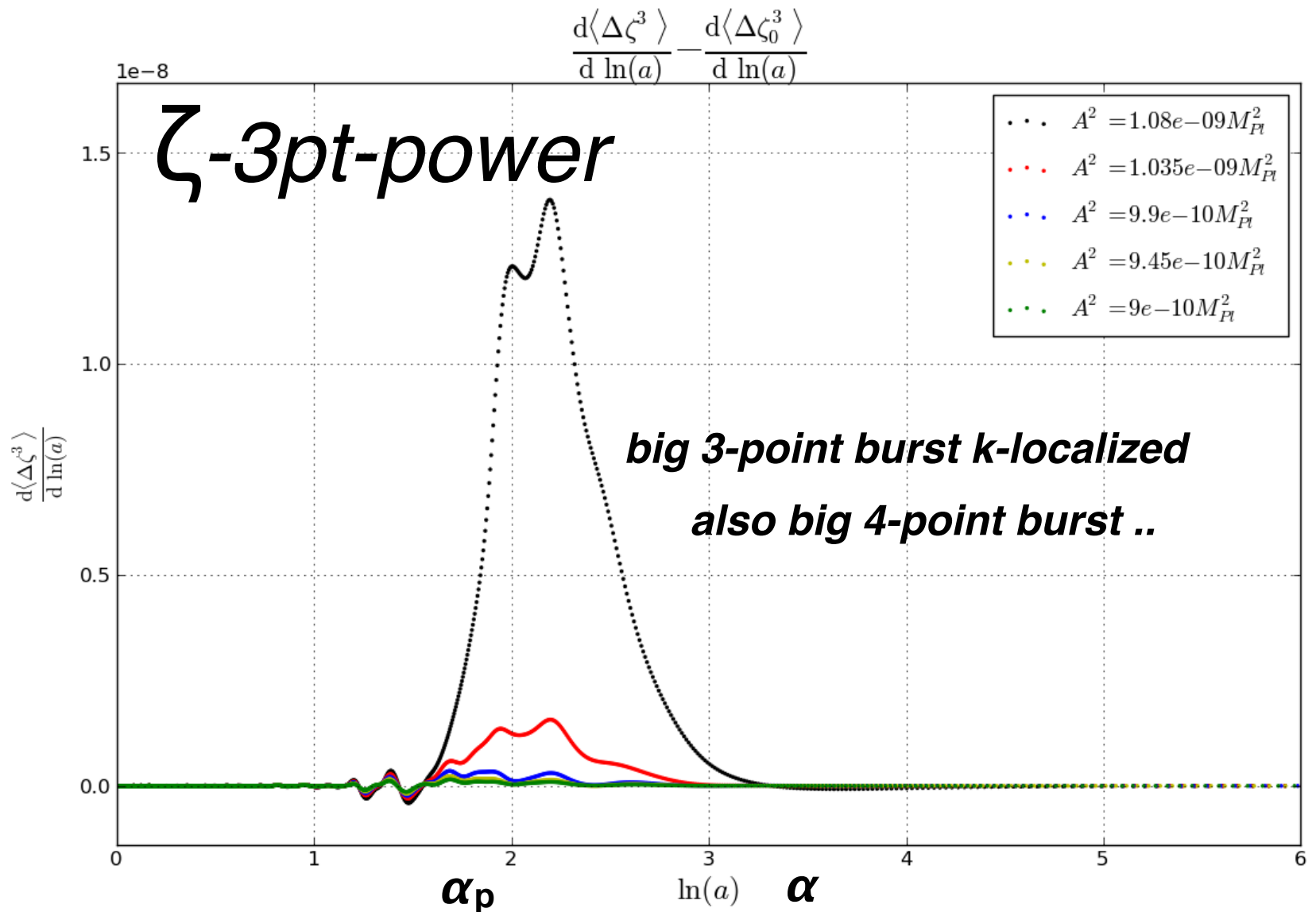
Bond+Braden+Morrison

experiment χ -light
1e-9

$$\Delta V_{\perp\perp} = m_{\chi\chi}^2(\phi) \chi^2 / 2$$





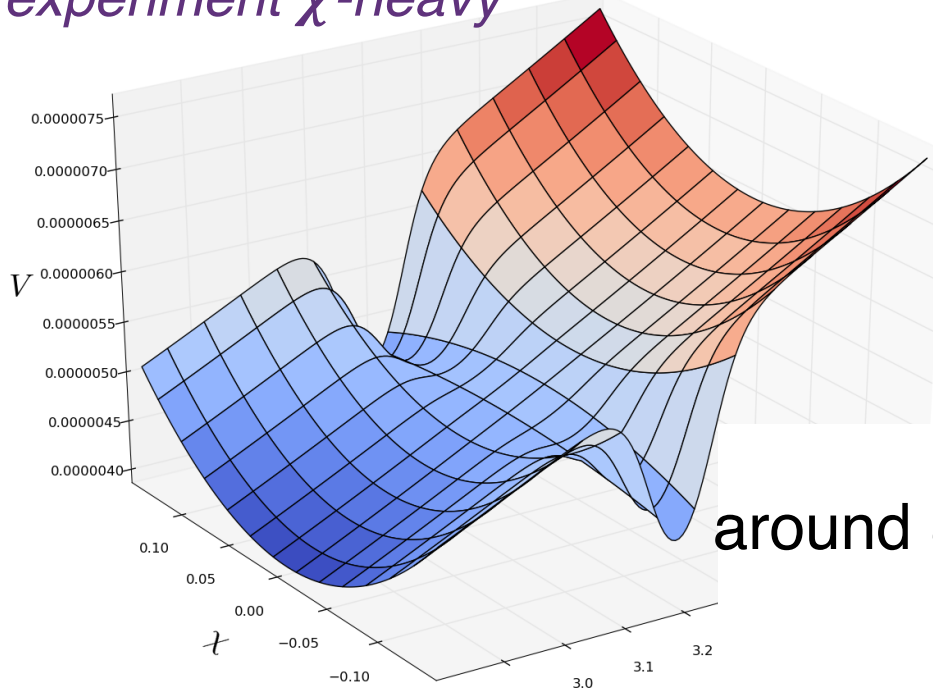


TBD coherence of N-point bursts in N-space ..

during inflation - instabilities => entropy => nonG

numerical experiments
of in-out states through
localized ΔV .
chain together .. oscillating

experiment χ -heavy



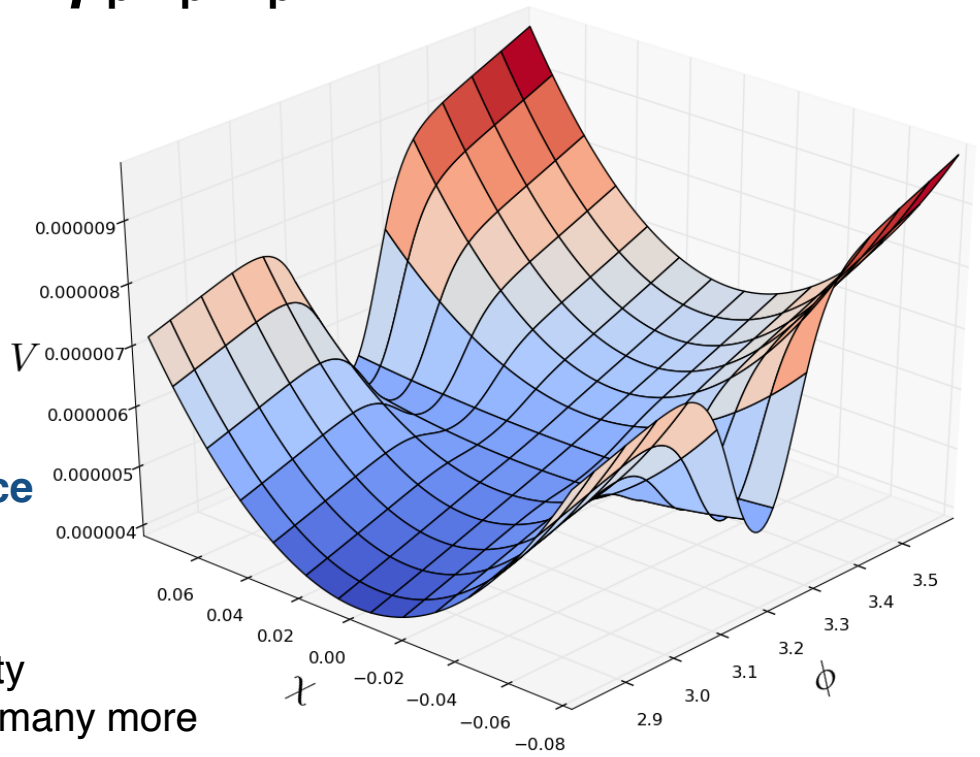
around ϕ_p k_p α_p

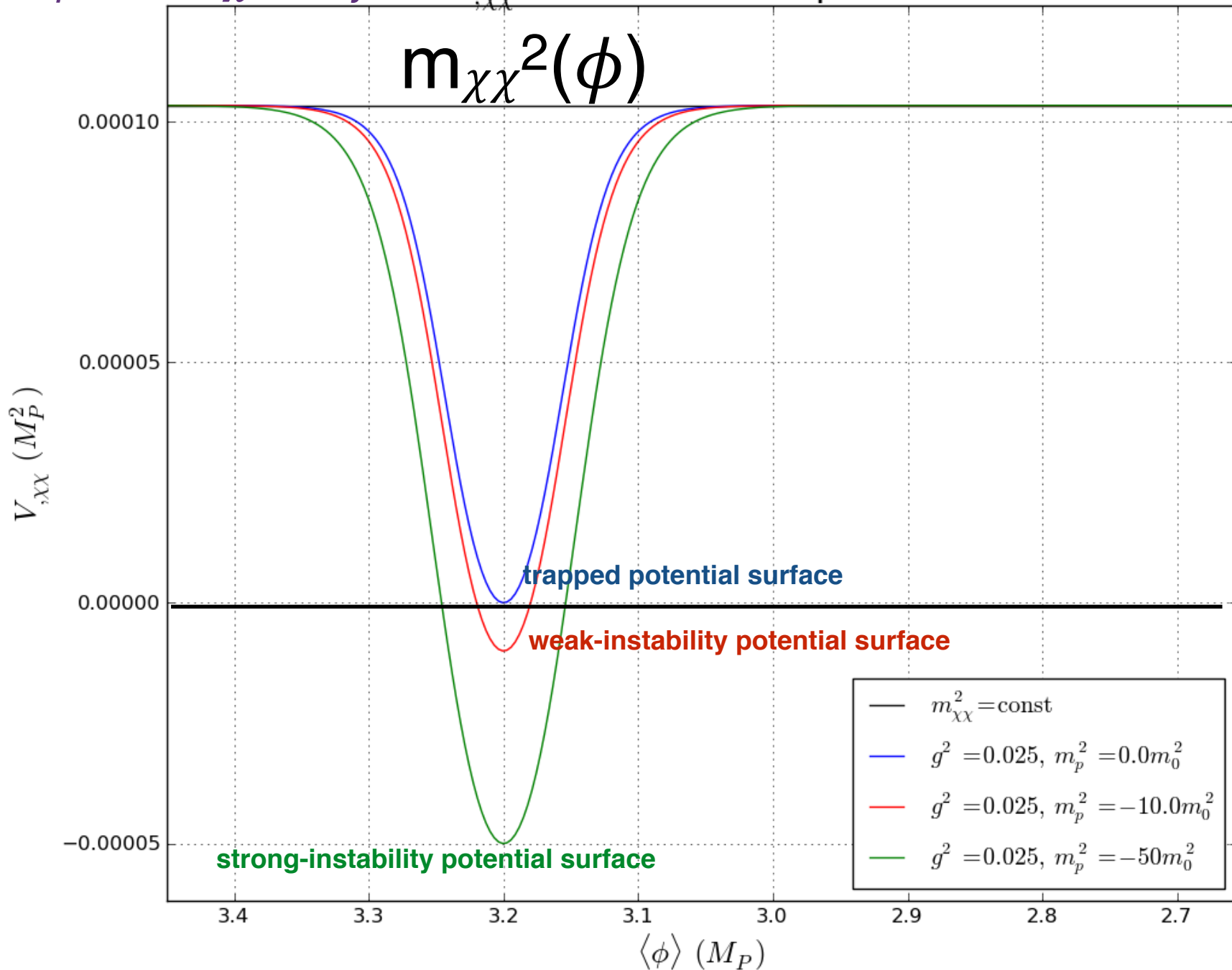
instability potential surface

Bond+Braden+Frolov+Morrison

trapped potential surface

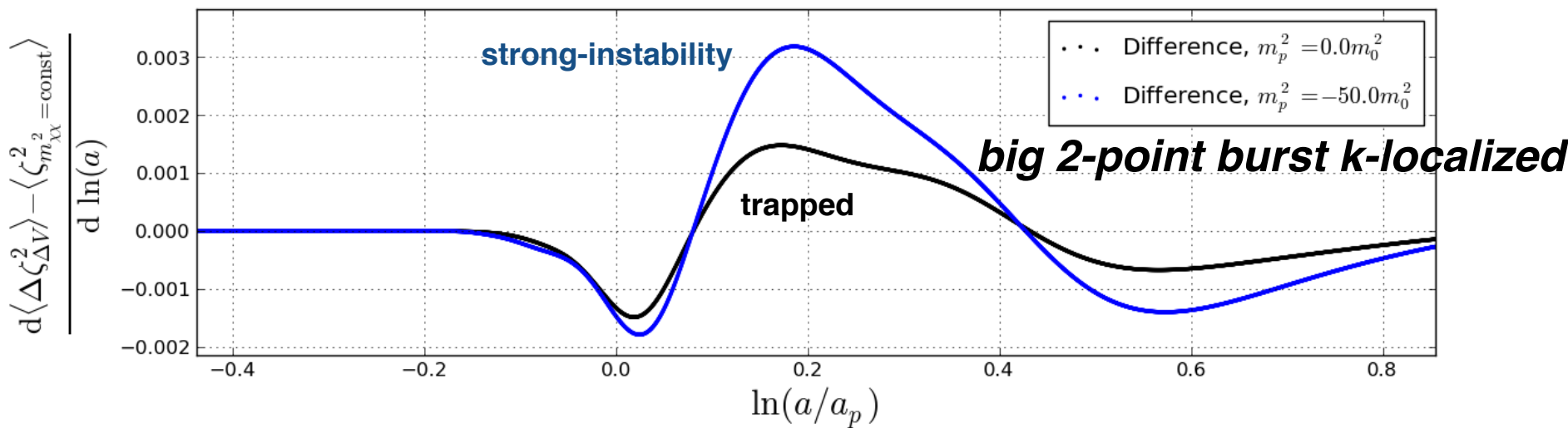
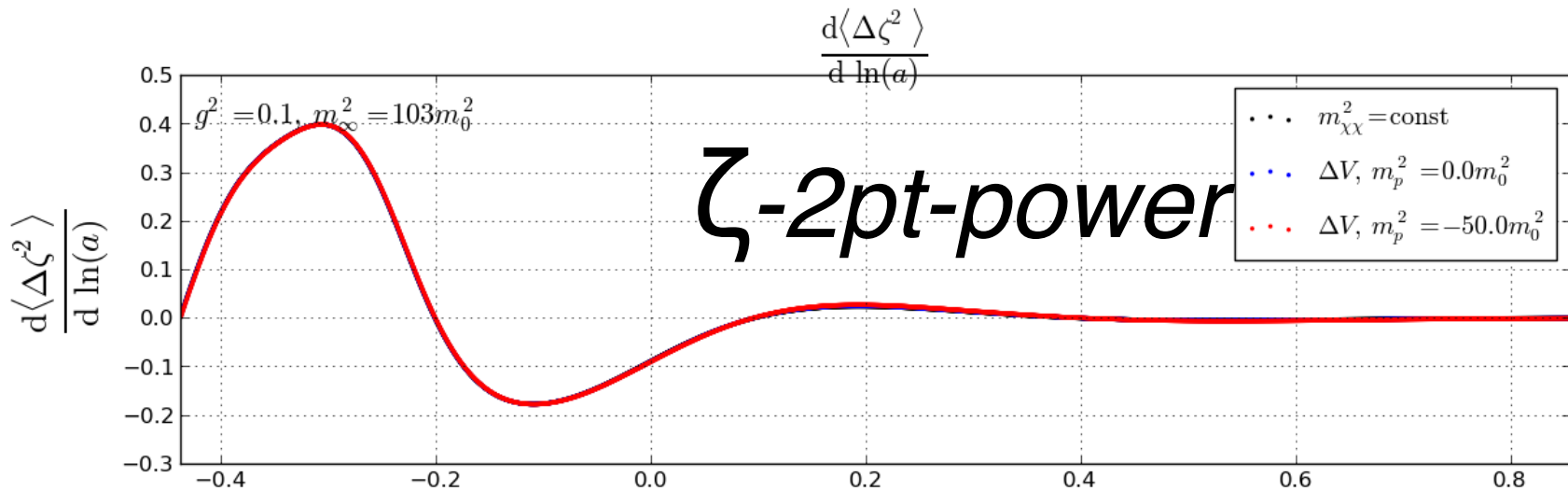
trapped inflation: same parameters, no instability
.. Kofman, Silverstein, Green, Barnaby, Huang, many more





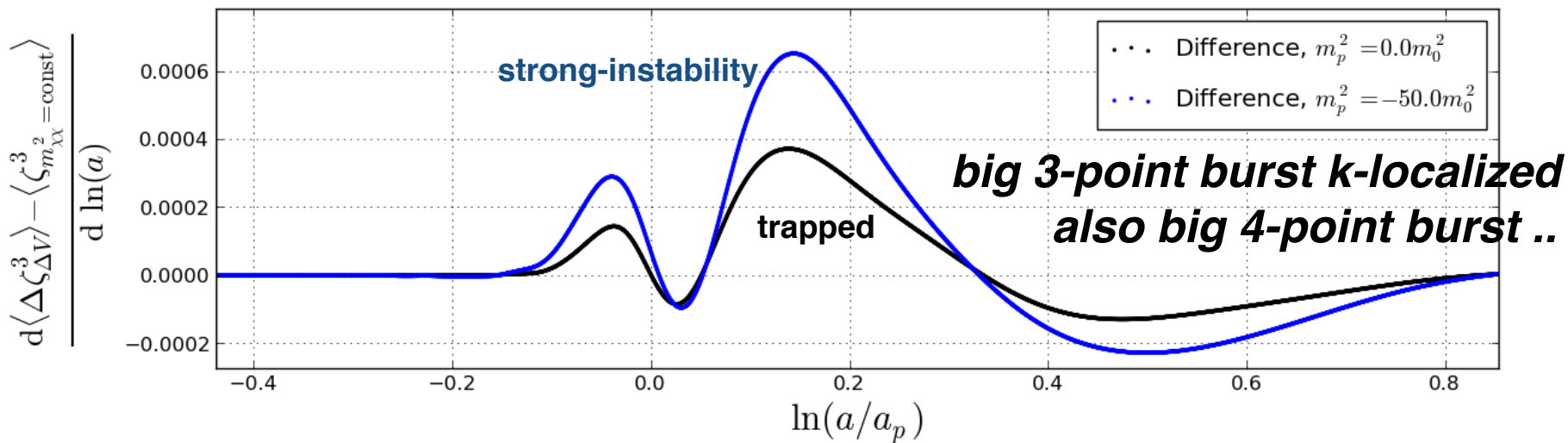
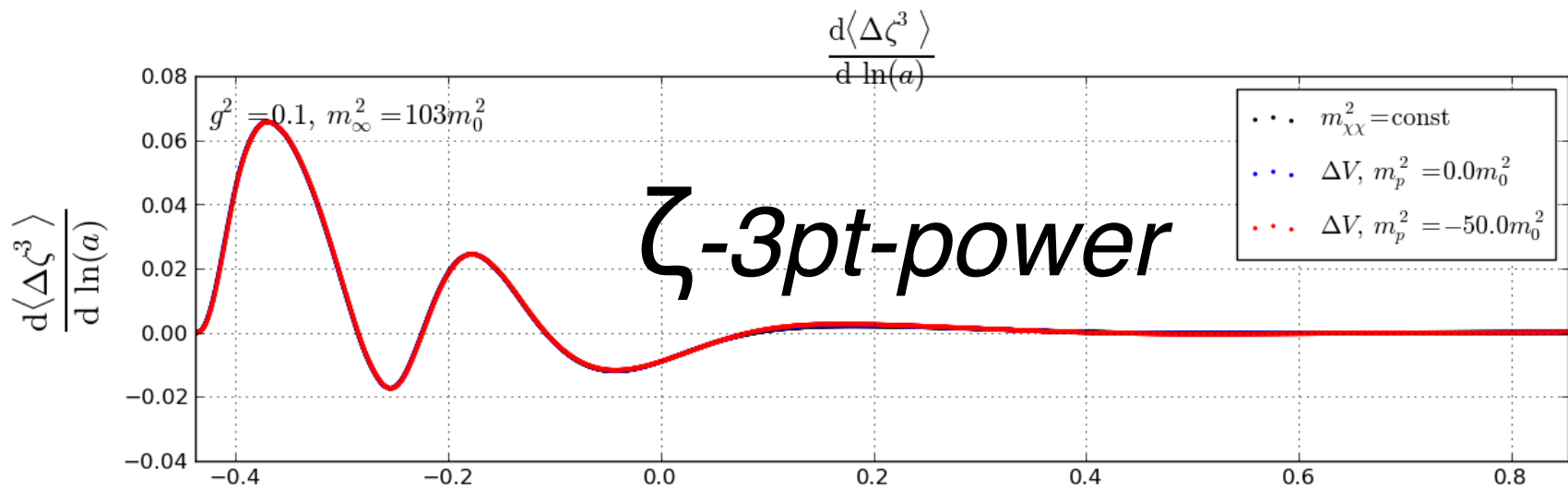
experiment χ -heavy

unstable χ cf. trapped



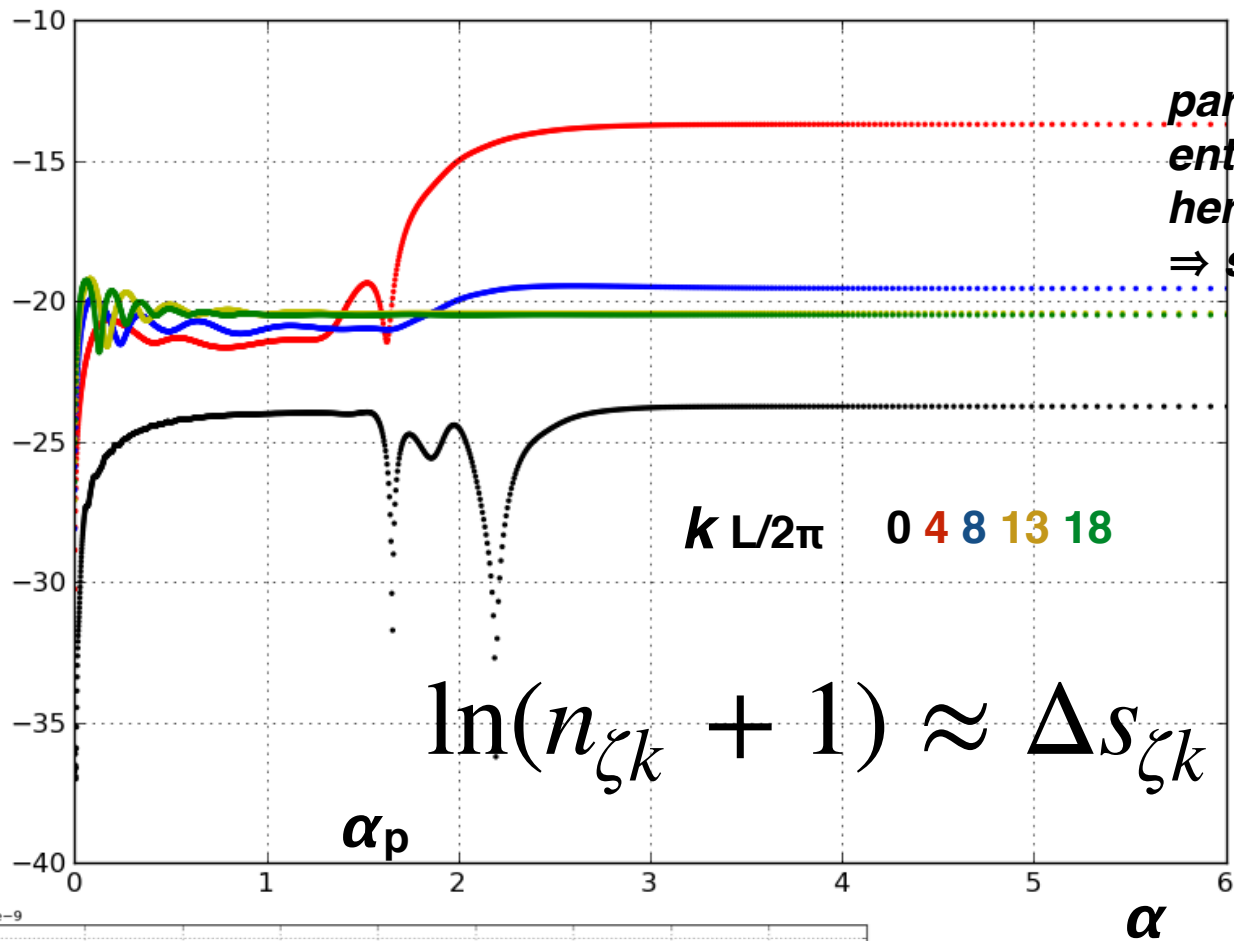
experiment χ -heavy

unstable χ cf. trapped

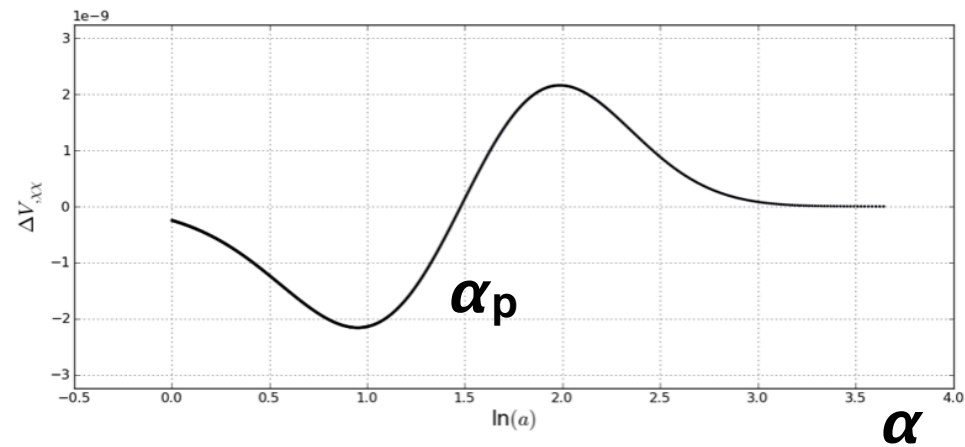


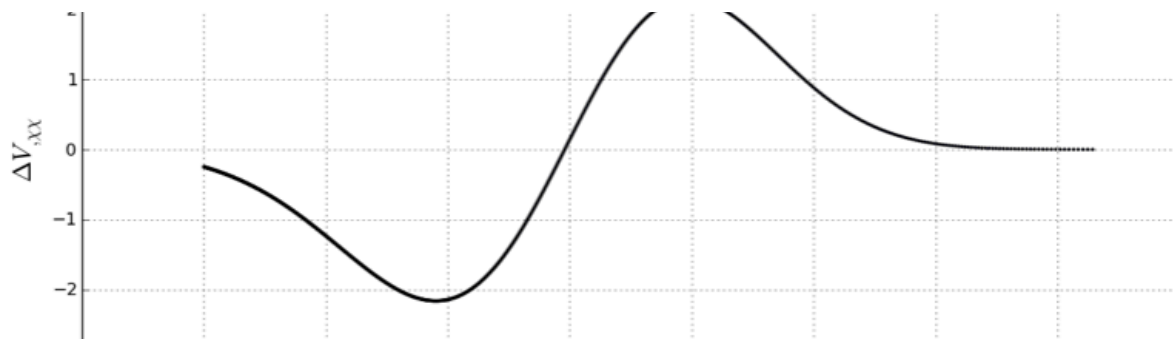
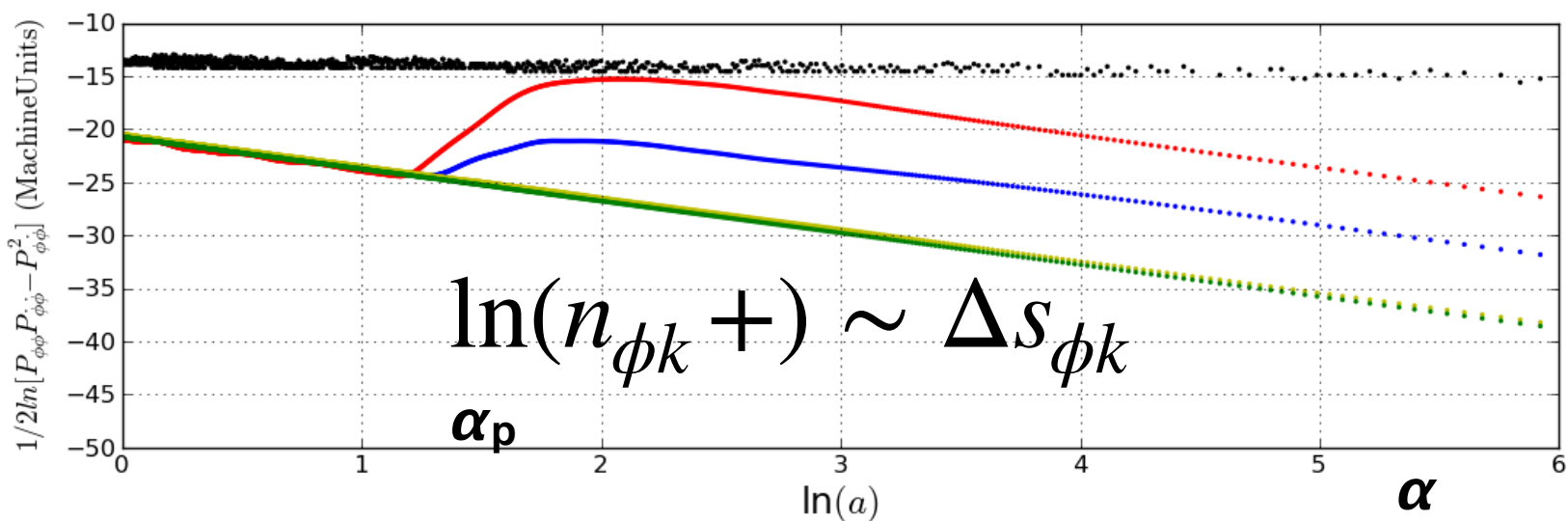
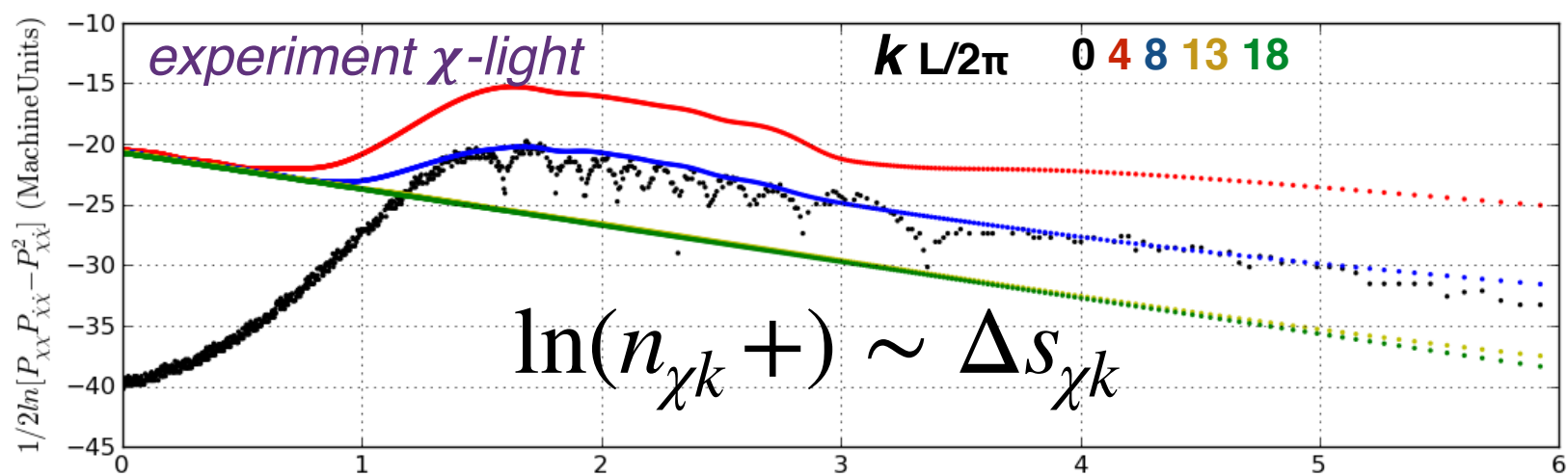
TBD coherence of N -point bursts in N -space ..

experiment χ -light $\ln(P_{\zeta\zeta})$



phonon occupation





***particle production picture aka
entropy production picture
here in isocons χ & inflatons ϕ
soft particle production***

Novel LSS/CMB non-Gaussianities from Instabilities & Entropy Generation During and After Inflation



Generate fully-correlated nonGaussian Websky-Ensembles for CMB/LSS probes

Dick Bond @ PSU 19 02 01

what are the degrees of freedom / parameters of the ultra early Universe? TBD

begin-inflate => inflate => end-inflate => preheat => non-equilibrium heat+entropy
=> *Standard Model particle physics* QG plasma radiation dominated
=> dark matter dominated *structure via gravitational instability* => dark energy now

$$d\zeta(x,t) = (dE+pdV)/3(E+pV) = d \ln \rho_c / 3(1+w_c) + \text{Trace } d\alpha^i_j$$

fit into a *UV-complete theory (ultra-high energy to the Planck scale)* strings, landscape, ..
& *IR-complete theory (post-inflation heating -> quark/gluon plasma)???* TBD

role of (1) *instabilities after inflation*

entropy generation via the breakup of the deforming coherent low-k inflaton condensate into incoherent high-k fluctuations aka phonons at a “shock-in-time” => **nonGaussianity**

role of (2) *instabilities during inflation*

phenomenology of in-states propagating through localized unstable potential structures to out-states, like scattering theory => *k-localized nonGaussianity*

(3) $|cg\rangle \Leftrightarrow |fg\rangle$ *condensate/fluctuation framework*, for both using coherent states classical-like approach with \hbar .

includes *Bogoliubov* transformations for fluctuations as condensate evolves
=> **particle creation** interpretation in both heating and inflating regimes.

END