

Origin of the observed entropy in the Universe and SMpp/BSMpp particles

- *coarse-grained coherent condensate breaks up into fine-grained fluctuations*
- *particle creation = instability \Rightarrow stretch and break via mode-mode coupling*

Lev Kofman

Dick Bond?

Misao Sasaki

Bond+Braden+Frolov+Huang+Morrison





The Kinematics of Inflation, Preheating and Heating: a Playground for Kolmogorov-Sinai and Shannon Entropies

Dick Bond @ ipmu18 11 29

what are the degrees of freedom / parameters of the ultra early Universe? TBD

begin-inflate => inflate => end-inflate => preheat => non-equilibrium heat+entropy
=> *Standard Model particle physics* QG plasma radiation dominated
=> dark matter dominated *structure via gravitational instability* => dark energy now

$$d\zeta(x,t) = (dE+pdV)/3(E+pV) = d \ln \rho_c / 3(1+w) + \text{Trace } d\alpha^i_j$$

fit into a **UV-complete theory** (ultra-high energy to the Planck scale) strings, landscape, ..
& **IR-complete theory** (post-inflation heating -> quark/gluon plasma)???

role of (1) **instabilities after inflation**

entropy generation via the breakup of the coherent low-k inflaton condensate into incoherent high-k fluctuations at a “shock-in-time” => **nonGaussianity**

role of (2) **instabilities during inflation**

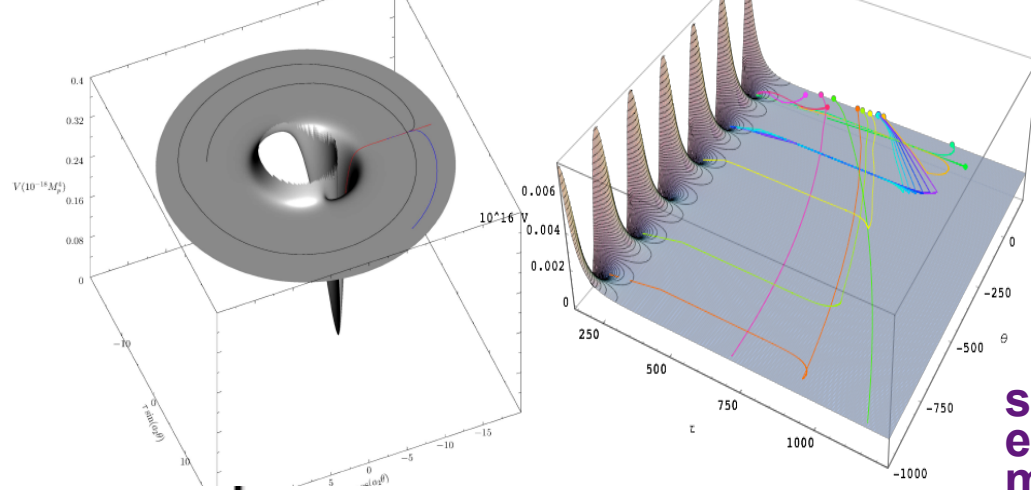
phenomenology of in-states propagating through localized unstable potential structures to out-states, like scattering theory => **nonGaussianity**

(3) **|cg <=> fg>** condensate/fluctuation framework, for both using coherent states classical-like approach with \hbar . includes **Bogoliubov** transformations for fluctuations as condensate evolves
=> **particle creation** interpretation in both heating and inflating regimes.

single field V heating slow, oscillating
 but shaped V can give rapid heating (roulette)
coarse-grain cm-horizon \Rightarrow
fine-grain fluctuations = S
generation

longitudinal instability
 KS yes *but* no LSS modulation

$$a = 1$$



A visualized 2D slice
 in lattice simulation

Preheating After
 Roulette Inflation

$$\langle \tau \rangle =$$

quantum
 diffusion
 spatial jitter

drift \longleftrightarrow

E_{ol}

let there be
 heat

roulette oscillations
 highly damped
 \Rightarrow no-non-G
 if redirect by $\chi_{cg, eoi}$, \mathbf{g}
 \Rightarrow non-G??

\longleftrightarrow *Eol horizon ~ 1cm comoving* \longleftrightarrow



SEMIFLATION

the true quadratic ζ -Websky of the ζ -scape

Planck 2018 X inflation: TTTEEE lowL Epol + CMB lens + BK15 BB + BAO

CMB TT power L~ 20-30 dip => ζ -Spectrum k-dip; includes CMB lensing, parameter marginalization

uniform $n_s = 0.9669 \pm 0.00367$

P18+BK15 LSS best fit

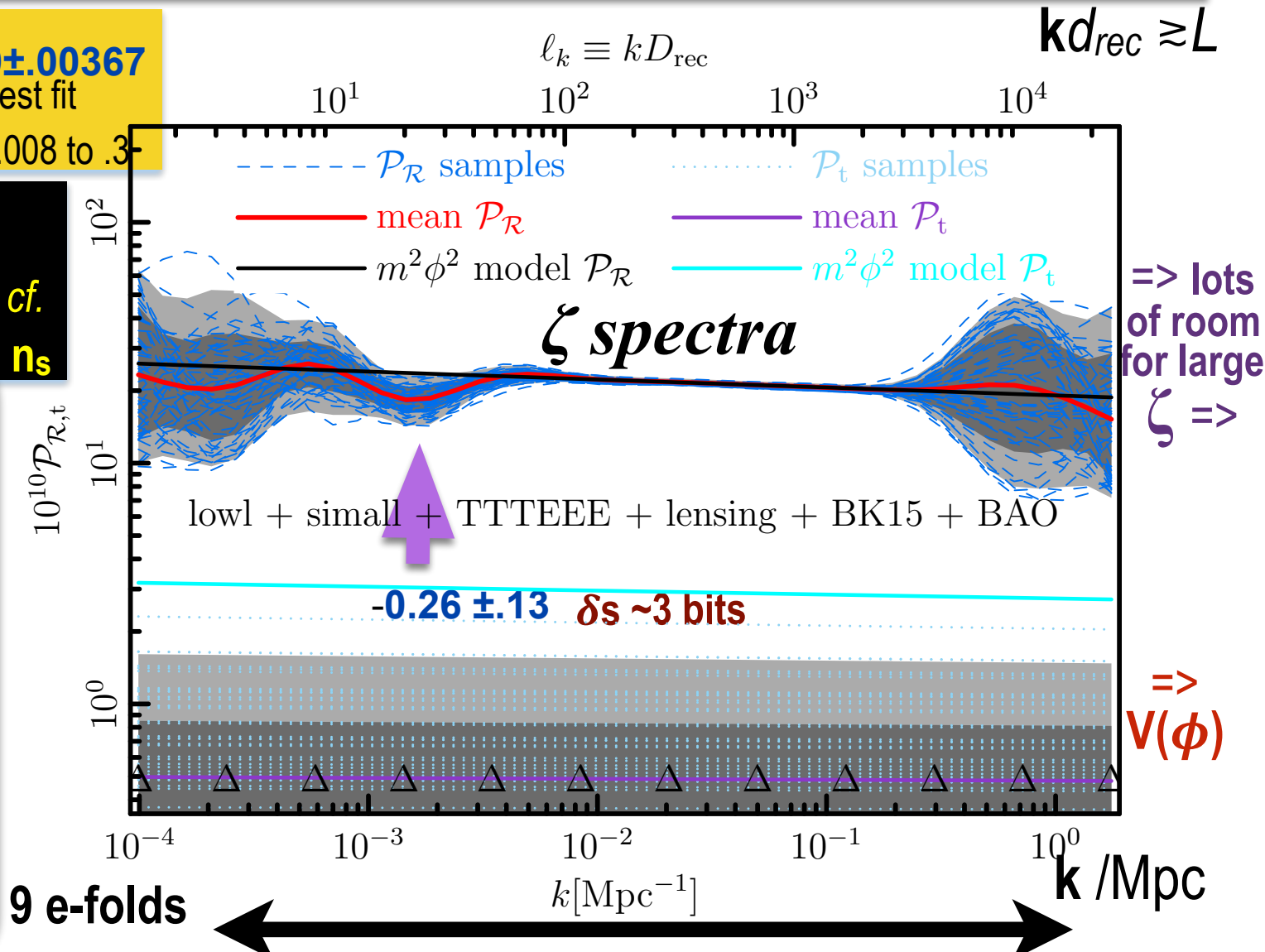
superb 12-knot fit $k \sim .008$ to $.3$

P18+BK15

$r < .069$ 95%CL cf.

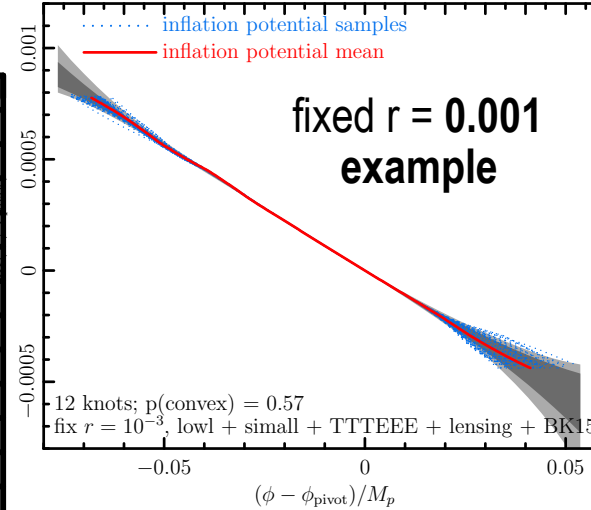
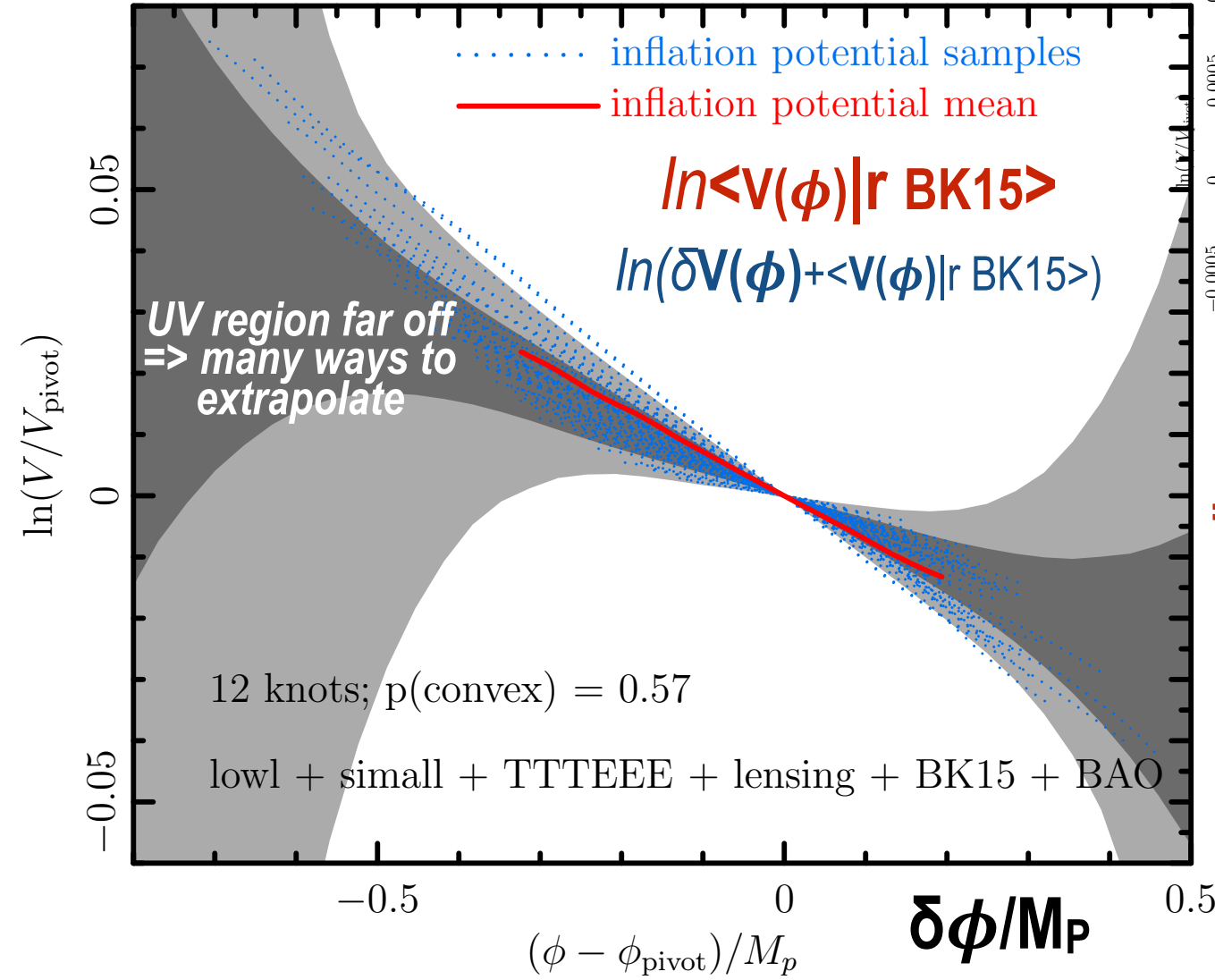
$r < 0.061$ uniform n_s

stochastic inflation
 $|\phi_{cg}; \phi_{fg}\rangle$
 coherent state picture of coarse-grain condensate + fine-grain bugoliubov fluctuations
 QM-correct



inflaton $V(\phi)$ -maps $= 3M_{\text{P}}^2 H^2 (1-\epsilon/3)$ HJ eqn, $d\phi/M_{\text{P}}/d\ln a = \pm \text{sqrt}(2\epsilon)$
 along the gradient / Morse flow

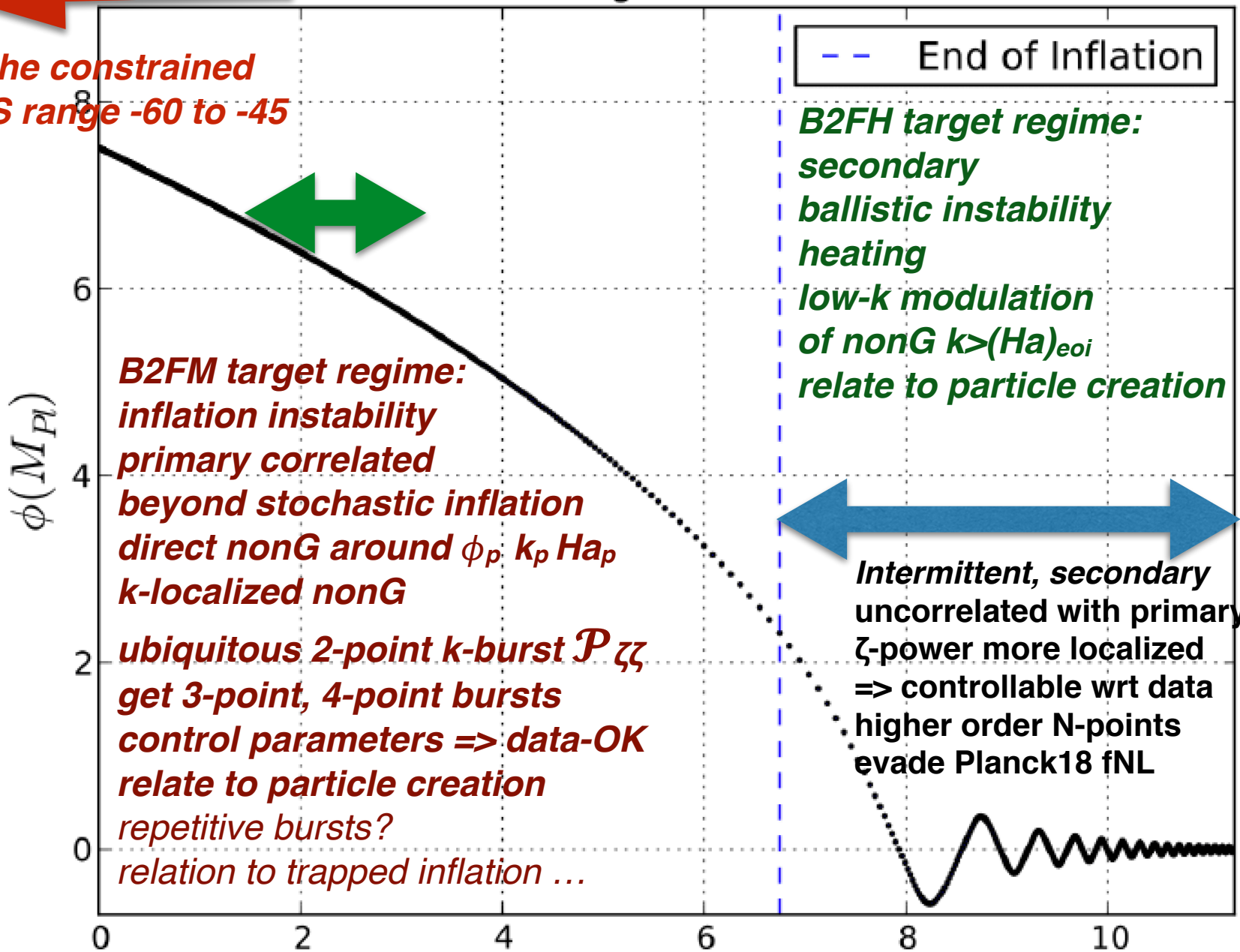
Planck 2018 X



IR heating region is far off \Rightarrow many ways to extrapolate



to the constrained LSS range -60 to -45



--- End of Inflation

*B2FH target regime:
secondary
ballistic instability
heating
low-k modulation
of nonG $k > (Ha)_{eoi}$
relate to particle creation*

*B2FM target regime:
inflation instability
primary correlated
beyond stochastic inflation
direct nonG around ϕ_p, k_p, Ha_p
k-localized nonG*

*ubiquitous 2-point k-burst $\mathcal{P}_{\zeta\zeta}$
get 3-point, 4-point bursts
control parameters => data-OK
relate to particle creation
repetitive bursts?
relation to trapped inflation ...*

*Intermittent, secondary
uncorrelated with primary
 ζ -power more localized
=> controllable wrt data
higher order N-points
evade Planck18 fNL*

apply to PBHs etc!!

$\ln(a)$

The Kinematics of Inflation, Preheating and Heating: a Playground for Kolmogorov-Sinai and Shannon Entropies

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what are the degrees of freedom / parameters of the ultra early Universe? TBD

Quantum Inflation - if quantum energy then quantum gravity (entangled) then gravitons
Phonons *density fluctuations = Trace strain = spatial 3-volume fluctuations*

=> combined **entropy-like measure** ζ =inflaton



Gravitons *tensor perturbations transverse traceless strain* $P_{GW} = r P_{\zeta}$ *grail* $r < .06$ now, to $< .001$
Isocons *when multiple particle-species - orthogonal scalar degrees of freedom to inflaton/phonon*
Dilaton *4-volume fluctuations - Higgs inflation* $L_G(R)$ *gravity - conformally-flatten potentials*
moduli, axions *connection to particle physics models "fundamental scalars" .. string theory*
fermions, vector gauge fields, Higgs **Standard model of particle physics** . vector perturbations

$$\frac{d\zeta}{dt} = \sum_i \frac{\nabla \dot{\phi}_i \cdot \nabla \phi_i + \dot{\phi}_i \nabla^2 \phi_i}{3a^2(\rho + P)}$$

nonlinear multi-field classical coupled system. evolve using lattice simulations. via symplectic defrost++ code + spectral code => high accuracy to unveil small effects after and during inflation

CMB/LSS observations give access to limited partial operator-paths in field-space aka **kinematics** => *limited glimpse of a UV/IR complete theory aka dynamics*. so far just through the ζ -fluctuation spectrum encoding the quantum diffusion of (**longitudinal/inflaton**) paths.

Transverse field-motion aka isocons may influence $\mathcal{P}_{\zeta\zeta}(k)$ and ζ -nonG stochastic dynamical systems theory for kinematics of cg variables

coarse-grained stochastic inflation $k \sim Ha$ resolution/dynamics relation

$d\zeta(x, Ha) = [\mathcal{P}_{\zeta\zeta}(k)]^{1/2} [d \ln Ha]^{1/2} \eta_{\text{GRD}}(x, Ha)$ quantum fluctuations & no drift

order parameters from the ultra early U? so far $\zeta \approx \text{GRF}$, $\mathcal{P}_{\zeta\zeta}(k)$ 2 ζ -params

ζ = **an adiabatic invariant**, conserved even with large field-strains to get nonG need to break adiabaticity => nonlinear fluctuations

role of (1) *instabilities after inflation*

*entropy generation via the breakup of the coherent low- k inflaton condensate into incoherent high- k fluctuations at a “shock-in-time” => **nonGaussianity***

stochastic dynamical systems theory for kinematics of cg variables

ζ = **an adiabatic invariant**, conserved even with large field-strains
to get nonG need to break adiabaticity => nonlinear fluctuations

Kinematics of Preheating:

BBFH are developing a **trajectory bundle evolution framework** for nonG in **post-inflation preheating -> heating**. field-space path deviations aka strains and their shear can characterize smoothed-bundle “ballistic” chaotic evolutions. arrested by nonlinear fluctuation-mode generation. **metric entropy (KS) in the ballistic phase -> Shannon entropy in the fluctuation-mode phase.**

*condensate evolves chaotically? => phase-transition-like melting into phonon+ modes,
fast scramble of fundamental fields, evolution of statistically-simple energy-density phonons
can one use coherent states to address this quantum mechanically? TBD*

$$d\zeta_{fi}(x,t) = d\ln \rho_c / 3(1+w) + \text{Trace}(d\alpha)$$

cf. $ds_{fi} = ds_{Ksfi} - d\text{Tr}\mathcal{E}_{fi} = \delta S_{fi} (fg \rightarrow cg)$ FokkerPlanck eqn for $\text{Prob}(\delta S_{fi} | \text{control})$

$\zeta_{NL}(x)$ from "isocon" degrees of freedom cf. $\zeta_{NL}(x)$ from inflaton

modulated heating, ballistic chaos, caustics, shock-in-time,

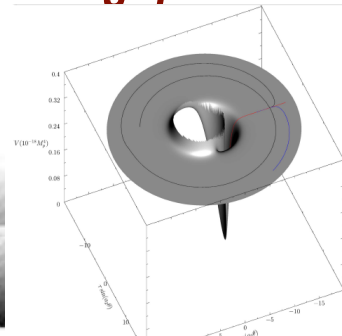
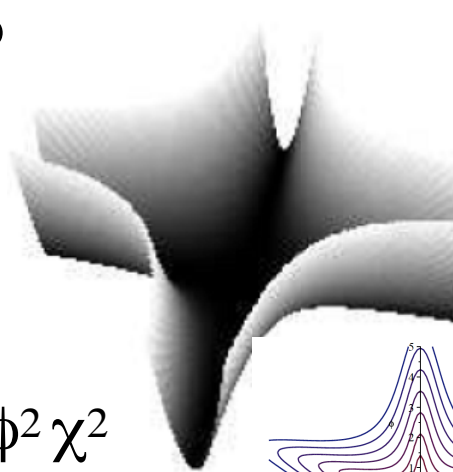
modulators isocon $\chi(x)$, axionic-isocon(x) couplings $g(x)$ super-horizon accessible

complex field configs *Oscillons, Stringy configurations, curvatons, .. Bubble Collisions*

what is the inflaton+isocons potential?

around a minimum is the HOT /heating question

2 filament?

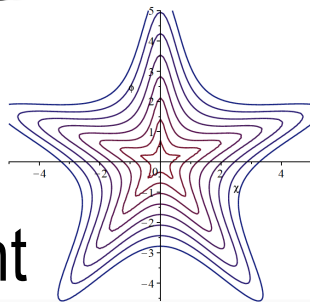


how was *matter & entropy* generated at the end of *acceleration = inflation*?

Relate to Higgs & standard model?

4 filament

$$1/4\lambda\phi^4 + 1/2g^2\phi^2\chi^2$$



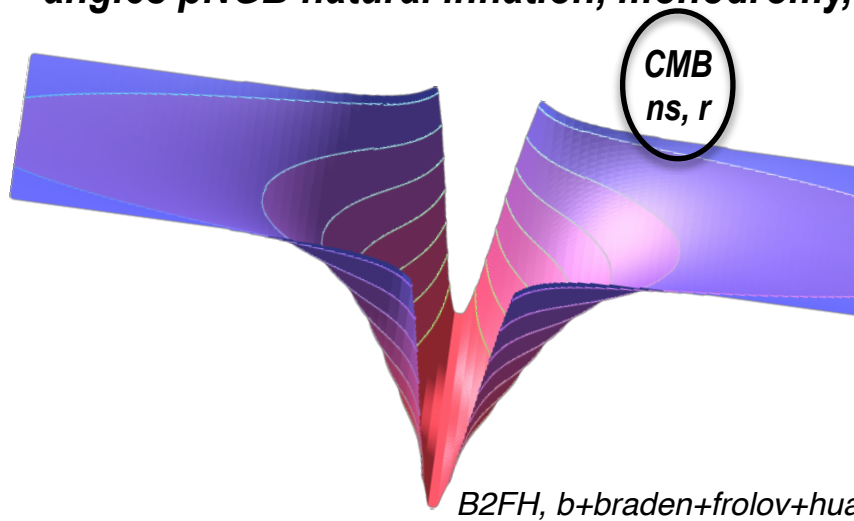
Preheating After
Roulette Inflation

3-filament 5-filament

angles pNGB natural inflation, monodromy, ..

$$\langle \tau \rangle =$$

**quantum
diffusion
spatial jitter**



**CMB
ns, r**

B2FH, b+braden+frolov+huang

*entropy
generation in
preheating
from the
coherent
inflaton
(origin of all
matter)*

drift

$$\ln \mathbf{a}(\mathbf{x}, \ln \mathbf{H})$$

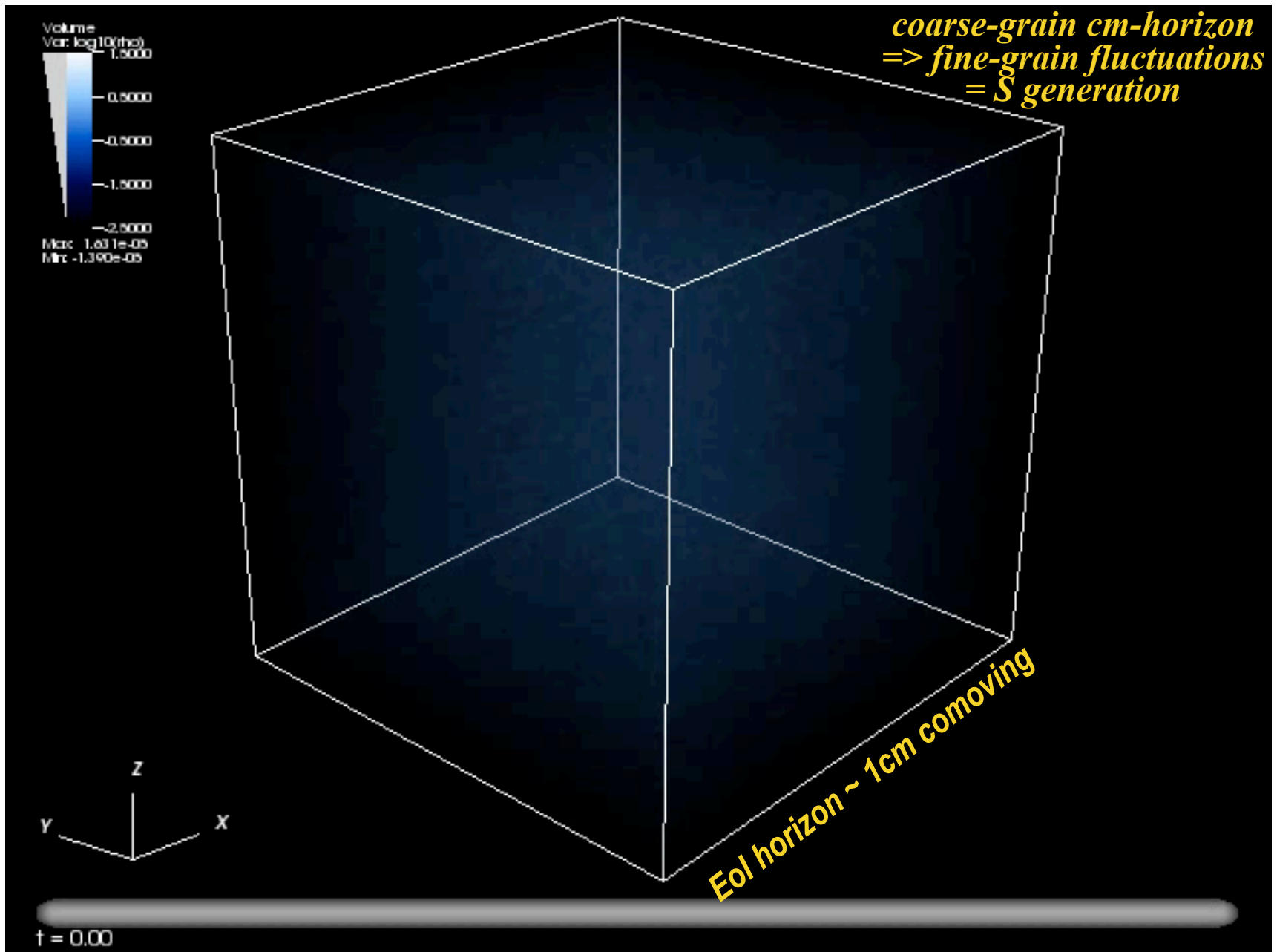
*isocon directions,
e.g., axion*

**let there be
heat**

conformal potential-flattening eg Higgs inflation SBB89 etc

S E M I - T E R M I N A L I N F L A T I O N

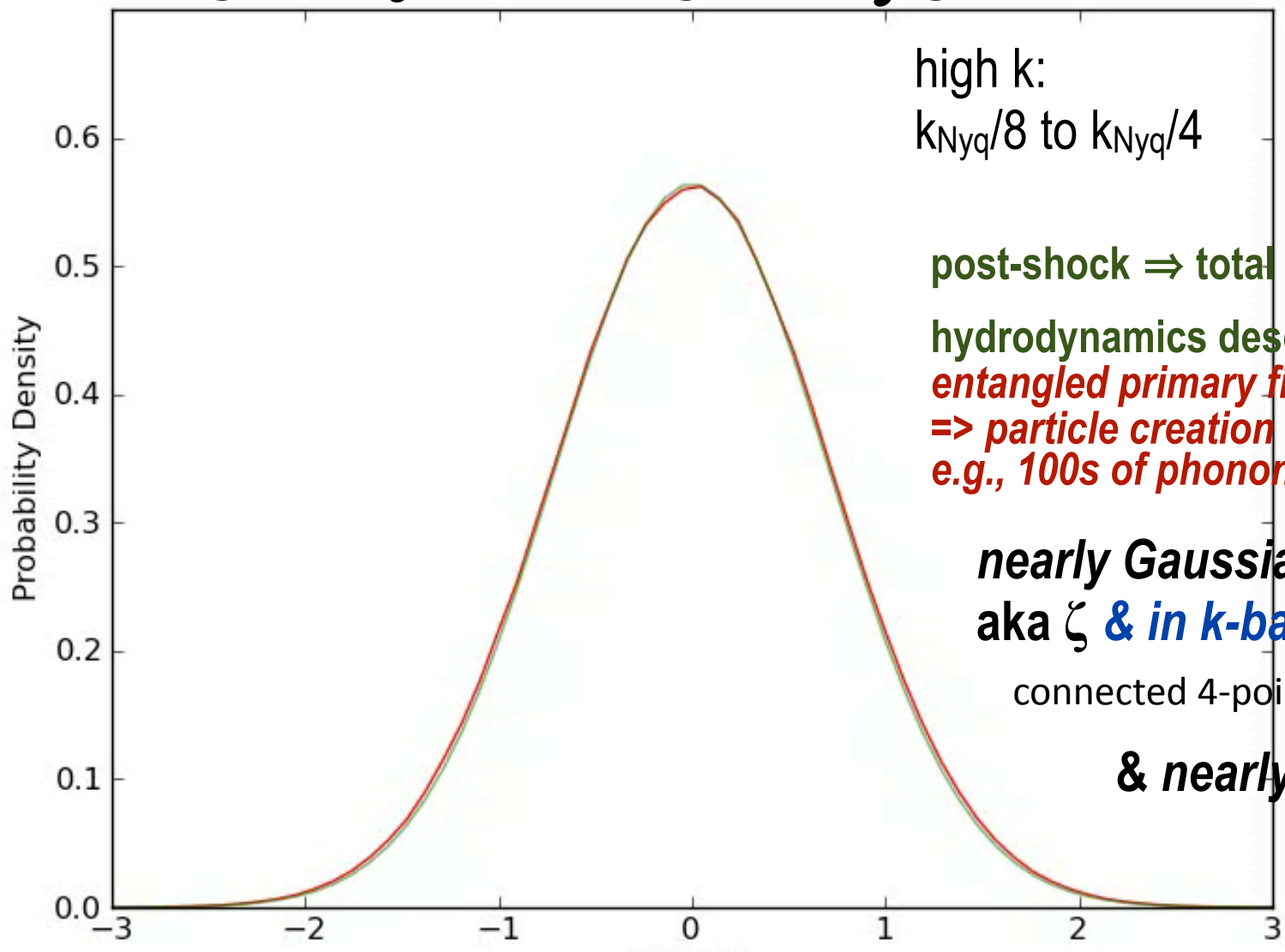
$$\text{quartic inflaton } V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



log-normal pdf (density aka ζ), in k-bands too; normal pdf (velocity)

but **Statistical Simplicity** $Prob(\zeta)$: FourierTransform(ln density) PDF
 $\sim \log\text{-normal after initial transient}$

coarse-grain $\langle \zeta \rangle \Leftrightarrow$ fine-grain $\delta \zeta_k$ gradients, δV



high k:
 $k_{Nyq}/8$ to $k_{Nyq}/4$

$Prob(\zeta)$

post-shock \Rightarrow total stress-energy T^{ab}
 hydrodynamics description phonons
entangled primary fields ($\varphi, \Pi_\varphi, \chi, \Pi_\chi$)
 \Rightarrow *particle creation description*
e.g., 100s of phonons at a time

nearly Gaussian in $\ln \rho / \langle \rho \rangle$
 aka ζ & *in k-bands!*

connected 4-point power is small

& nearly Gaussian in v

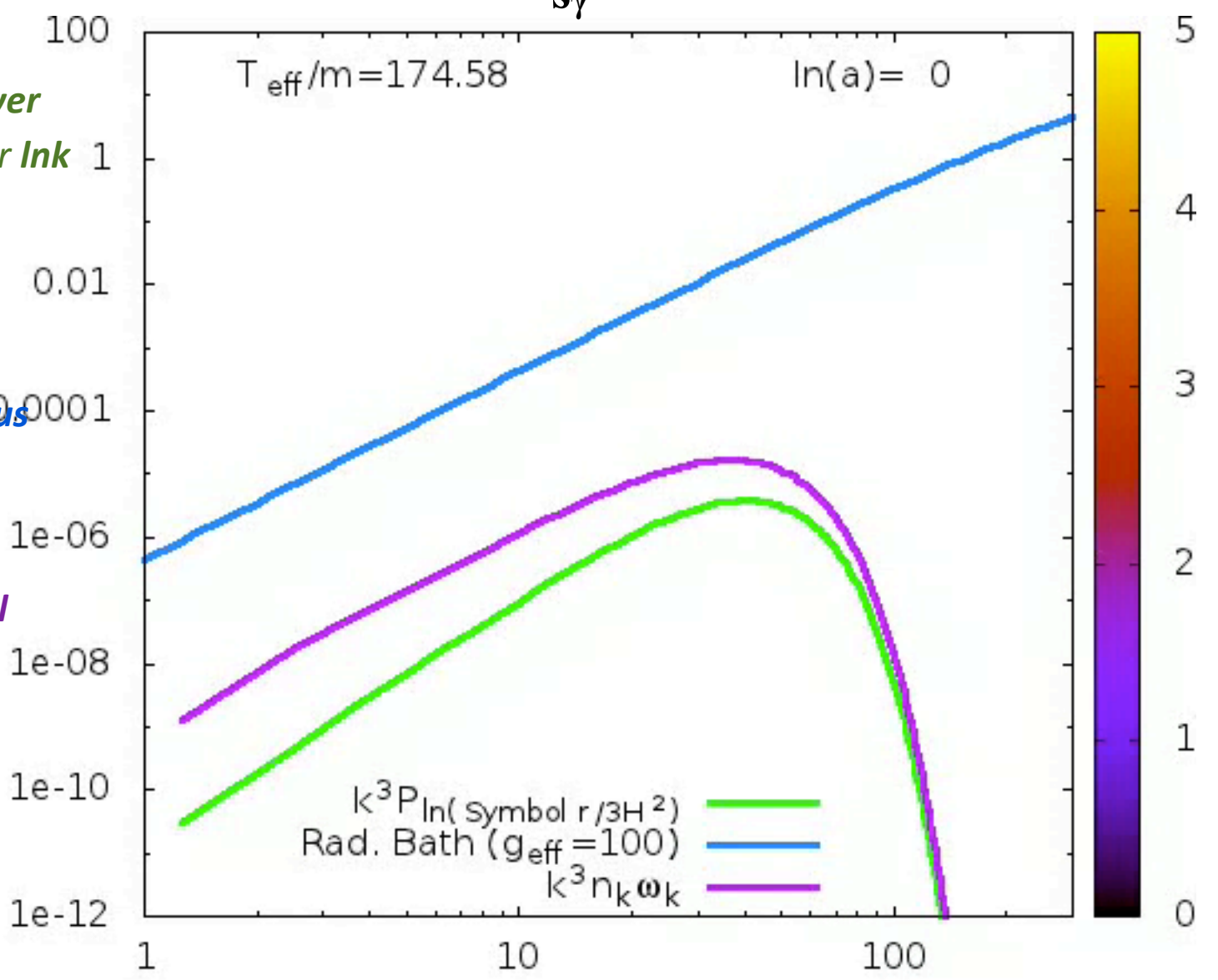
box $L=10m$ and $N=1024^3$

$$\frac{Re(\ln(\rho/\bar{\rho})_k)}{\sqrt{P_{\ln(\rho/\bar{\rho})_k}}}$$

coherent inflaton => incoherent mode cascade of fields thru a shock-in-time to thermal equilibrium

$S_{U_i} \sim 0$; $S_{U_{tot,m+r}}/n_b \sim 1.66 \times 10^{10} \text{ bits/b}$; $s_\gamma/n_\gamma = 5.2 \text{ bits}/\Upsilon = 2130/411$; $s_v = 21/22$

In $p/\langle \rho \rangle$ power spectrum per $\ln k$ aka entropy aka phonon aka ζ cf. instantaneous full thermal spectrum cf. conventional energy spectrum using a pseudo particle occupation number



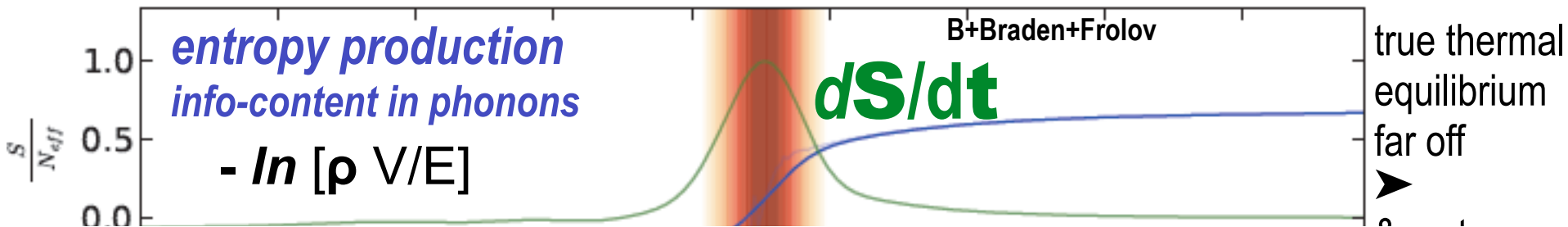
$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2$

k/m

momentum

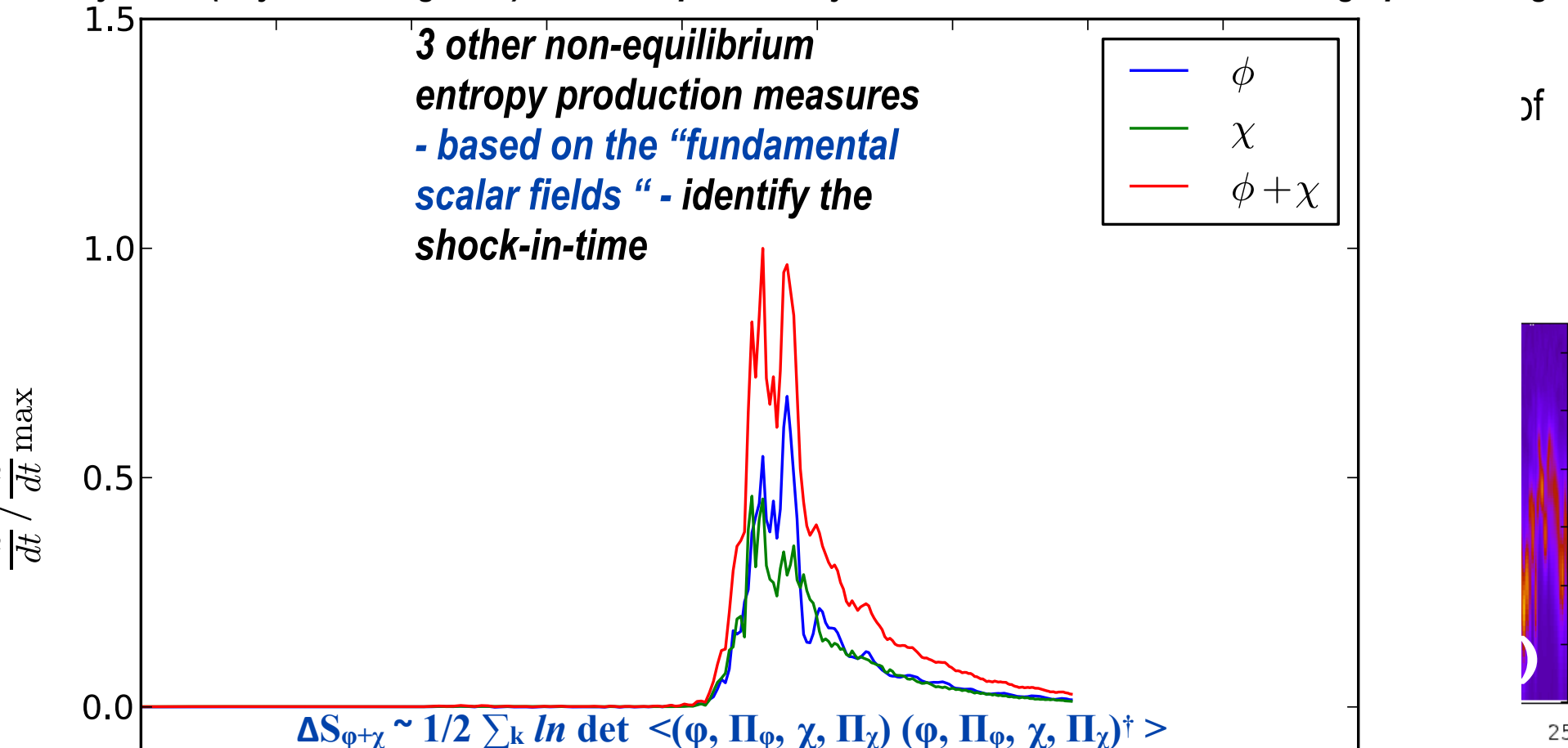
B+Braden+Frolov

nonG from large-scale modulations of the shock-in-times of preheating

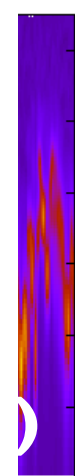


entangled primary fields $(\phi, \Pi_\phi, \chi, \Pi_\chi)$

decay rates (Feynman diagrams) and transport theory difficult to make accurate through preheating



of



A Shocking End to Post Inflation Mean Field Dynamics

Shock-in-space $t = \text{const}$

$v_{\text{bulk}}^2 > c_s^2 \Rightarrow v_{\text{bulk}}^2 < c_s^2$

supersonic \Rightarrow subsonic

Characteristic spatial scale

Jump Conditions: $\Delta T^{\mu\nu}$

Randomizing Shock Front: ΔS

Mediation: width via viscosity or collisionless dynamics

post-shock evolution, slow, of temperature, etc.

coherent condensate breakup?

Shock-in-time $x = \text{const}$ (deviations for nonG)

$\langle \rho \rangle \gg \delta \rho \Rightarrow \langle \rho \rangle \ll \delta \rho$

Homogeneous \Rightarrow Fluctuations

Characteristic temporal scale

Jump Conditions: $\Delta T^{\mu 0}$

Randomizing mode cascade & Particle Production: ΔS

Mediation: width via gradients and nonlinearities

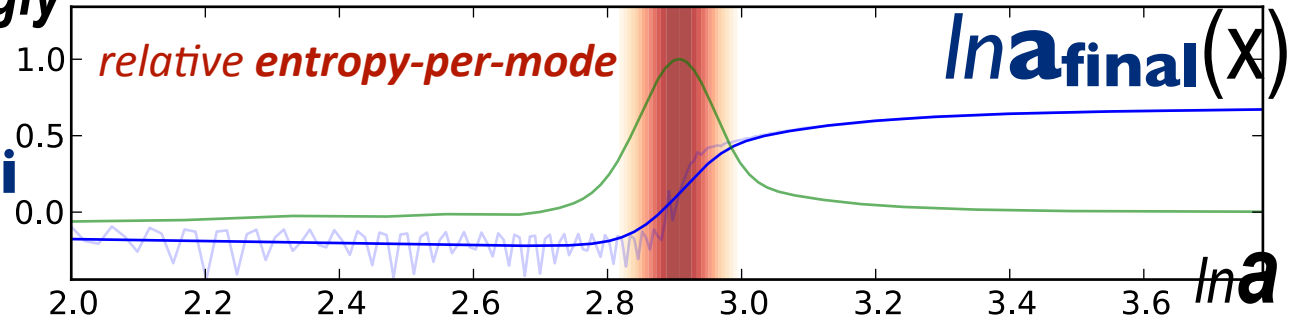
post-shock evolution, slow, of fluctuations
coherent condensate breakup E-phonon soup

- a difference: chaotic lead in to shock

Preheating is a shockingly efficient entropy source

$\ln \mathbf{a}_{\text{shock}}(x) / \mathbf{a}_{\text{eoi}}^{S/V_{\text{eff}}}$

& the mediation width

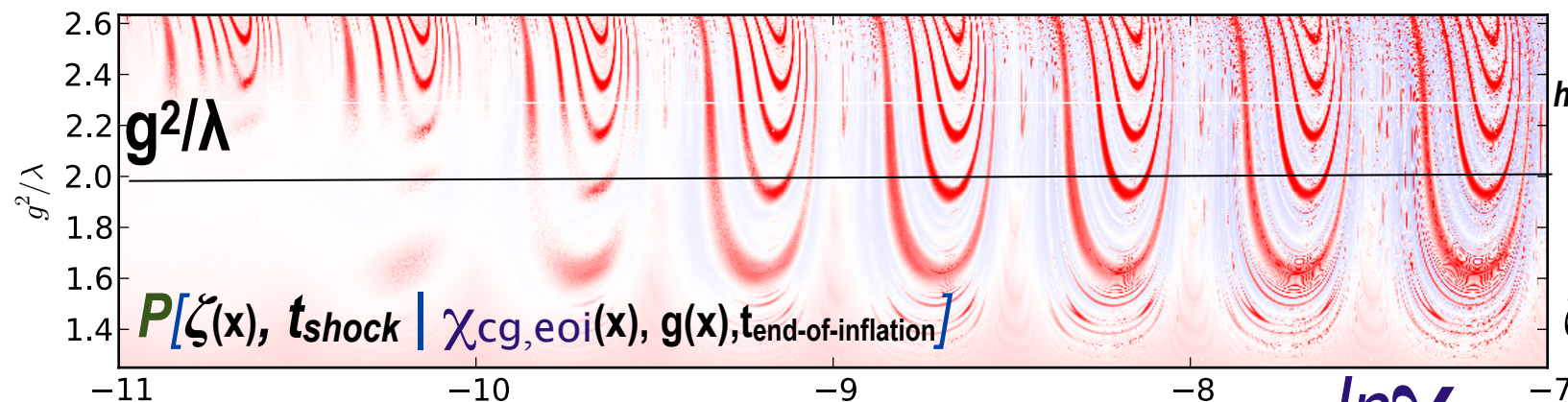
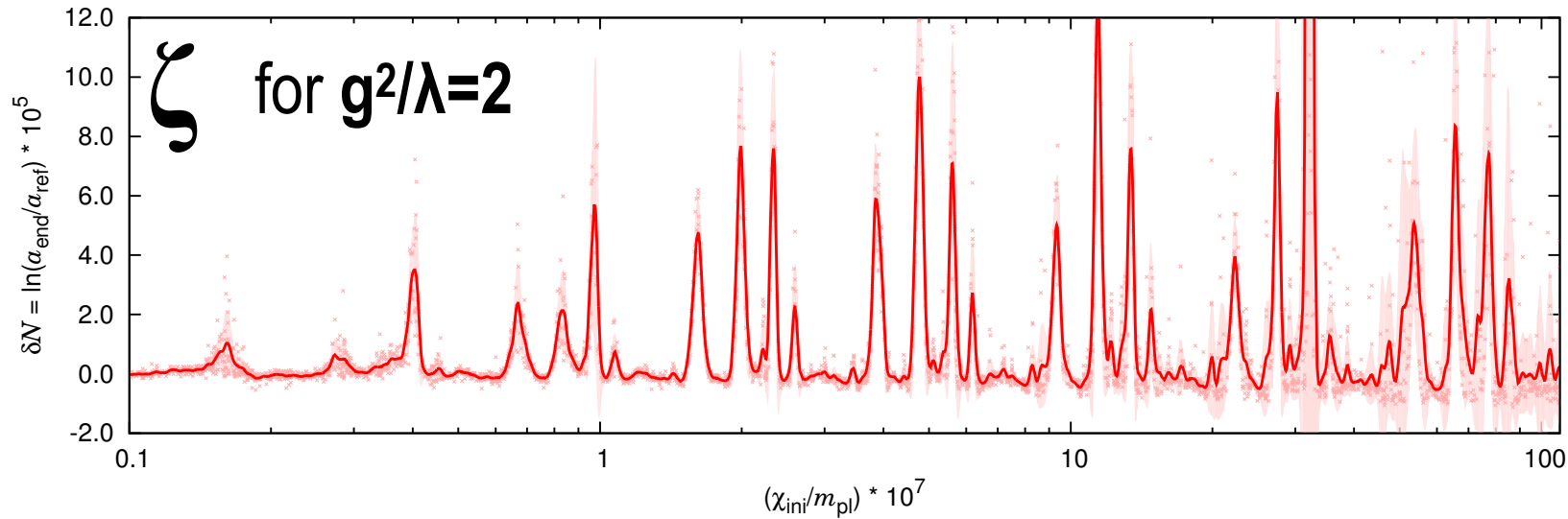


$dS/dt(t, g) \Rightarrow$ the Shock-in-time: entropy production rate

$\zeta_{\text{shock}}(\chi_{\text{cg, eoi}}(x) | g^2/\lambda) \Rightarrow$ Chaotic Billiards: NonG from Parametric Resonance in Preheating

B+Frolov, Huang, Kofman 09
 B+Braden, Frolov, Huang 19

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



computational tour de force

huge number of 64^3 sims to show the wondrous complexity of

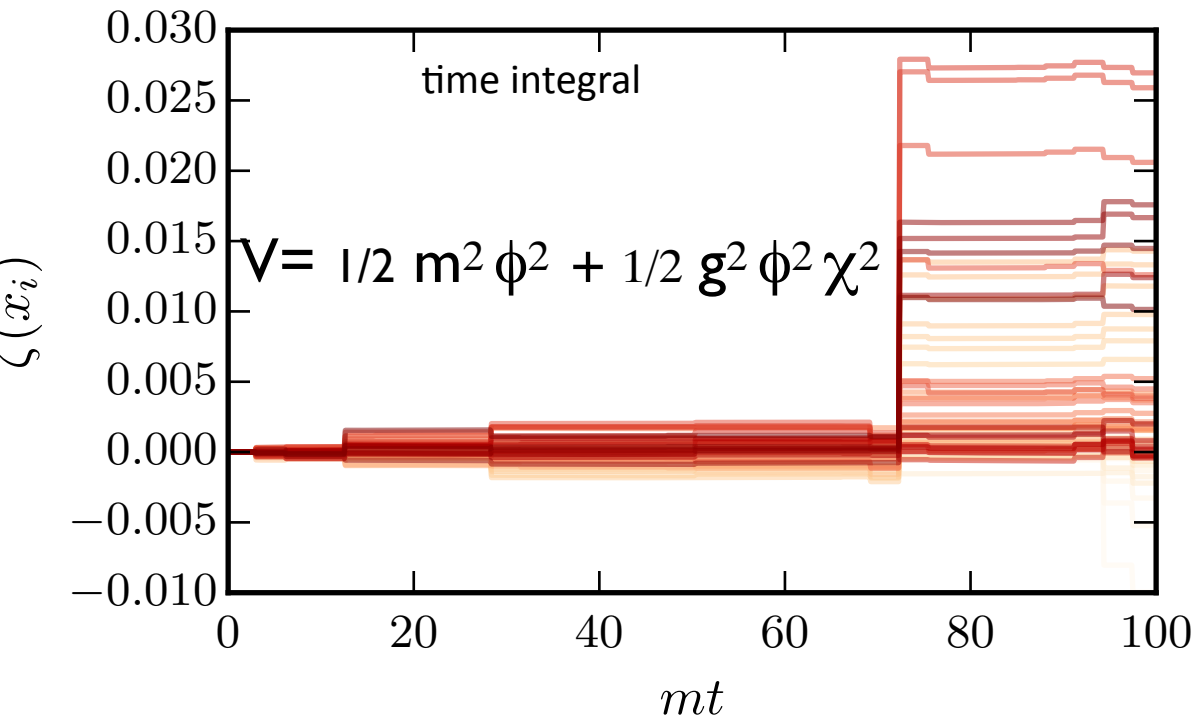
gigafigure of lattice simulations $\ln(\chi_0/\phi_0)/\mu_0 T$

$\ln \chi_{\text{cg, eoi}}$

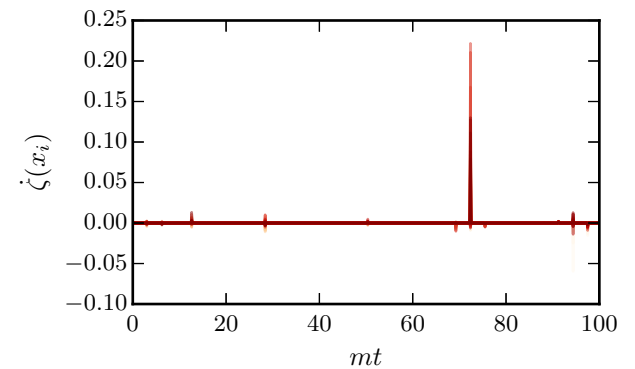
ζ conserved along trajectories until the “shock-in-time” when high \mathbf{k} fluctuations (fine-grain) develop from coarse-grain, measure is $S_{\text{Shannon}} = -\ln \mathcal{P}v_g$

but $-\text{Dln } \mathcal{P} / \text{dt} = \text{Trace } d\mathcal{E} / \text{dt}$ does change \sim KS entropy (rate)

stretching of phase strings. begin with anisotropic Gaussian at EoI and watch it stretch, \mathcal{E} grows, rotates, locally OK as distorted ellipsoid, but strain depends upon the central value \Rightarrow phase tubes



evolution of the ζ source term



$$\zeta_{\text{final}}(\mathbf{x}, t_f | \chi_{\text{cg, eoi}}(\mathbf{x}), g^2/\lambda) \sim \zeta_{\text{shock}}$$

caustics in $\langle q^A \rangle$ ballistic orbits

$$\langle \delta q^A X_{t2} \mid \delta q^B X_{ti} \rangle \sim \exp(\mathcal{E}(X_{t2} \mid X_{t1}))^{A_C} \langle \delta q^C X_{t1} \mid \delta q^B X_{ti} \rangle$$

early U parameters: **final** $\varphi, \Pi_\varphi, \chi, \Pi_\chi, \ln a, \ln \rho$, **initial** $\chi_{cg, eoi}$, *couplings* g, λ, \dots

parameter strain tensor in field space $\mathcal{E}^{A_C}(X_{t2} \mid X_{t1})$ deformation $e^\mathcal{E}$

$d\mathcal{E}^{A_C}/dt$ strain rate \sim local Lyapunov coefficients *Floquet instability charts*

instability to have nearby parameters diverge \Rightarrow chaotic billiards

Kolmogorov-Sinai entropy: \sim Sum of positive values of $d\mathcal{E}/dt$

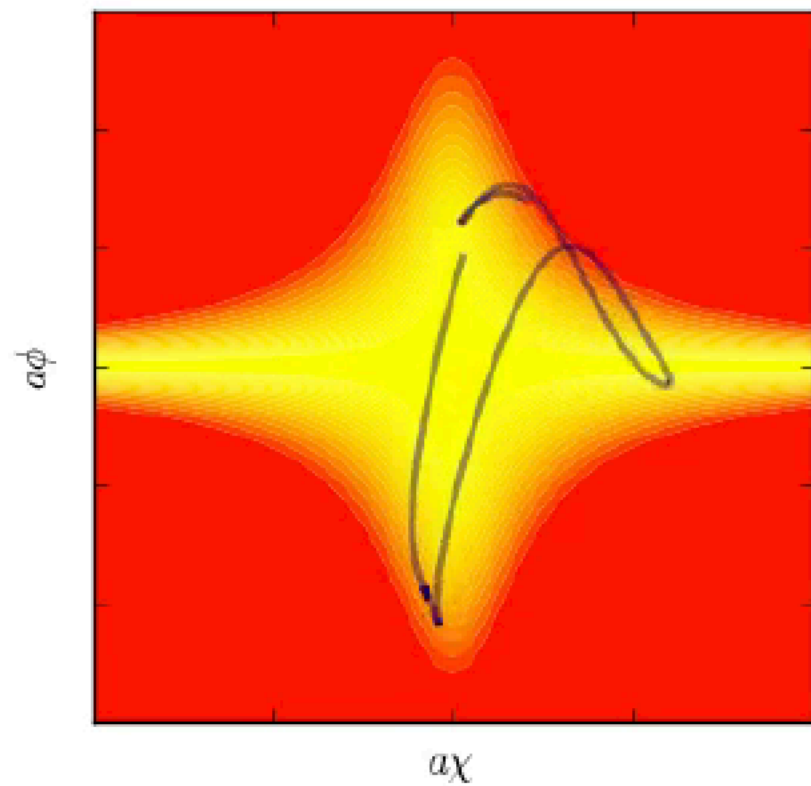
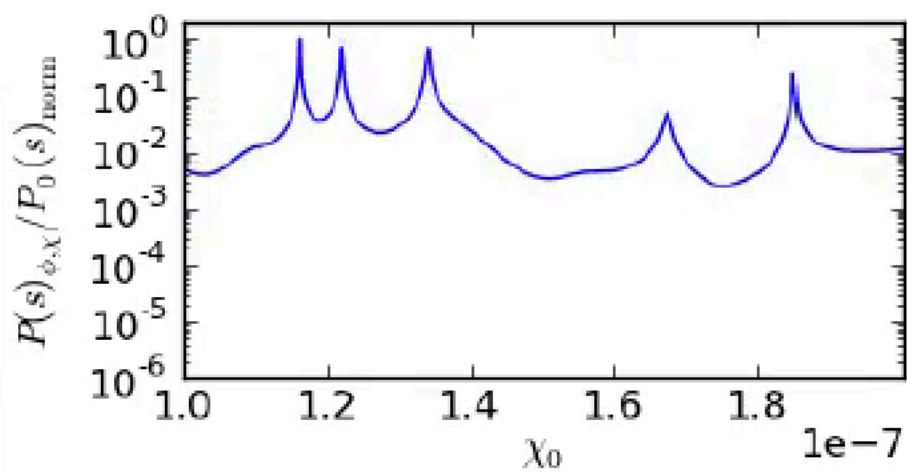
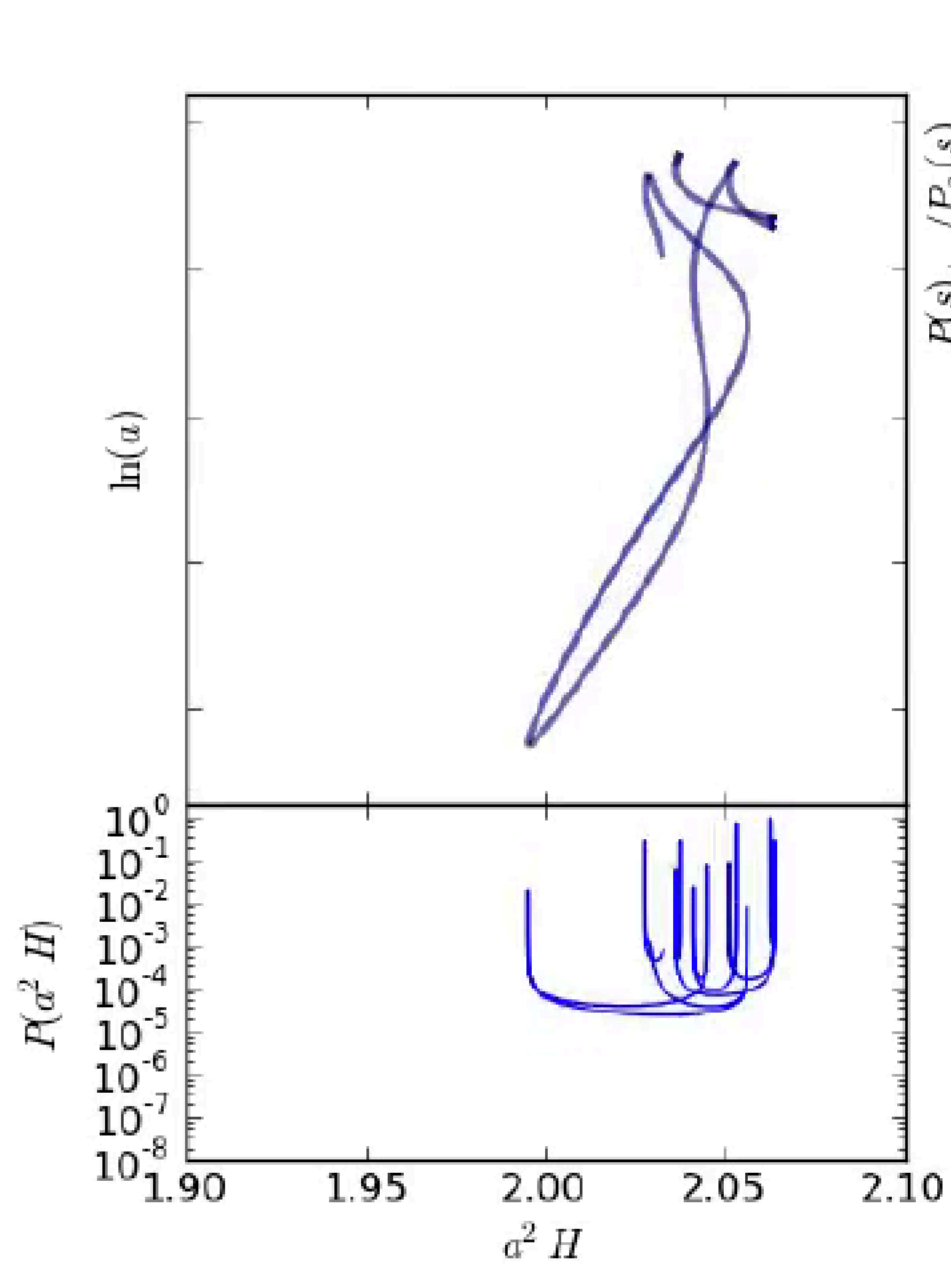
small \mathcal{E}^{A_A} eigenvalues \Rightarrow coherent trajectory bundles (for a time)

= caustics (inverse $\rightarrow \infty$) $1/[\partial \alpha / \partial \chi_{cg, eoi}]$; \Rightarrow peaks in $\zeta(\chi_{cg, eoi})$

stopping time **tstop** ($\chi_{cg, eoi}$) when \mathcal{E}^{A_A} values get large \Leftrightarrow local gradients \uparrow

cf. LargeScaleStructure: final Eulerian position \Leftarrow initial Lagrangian position

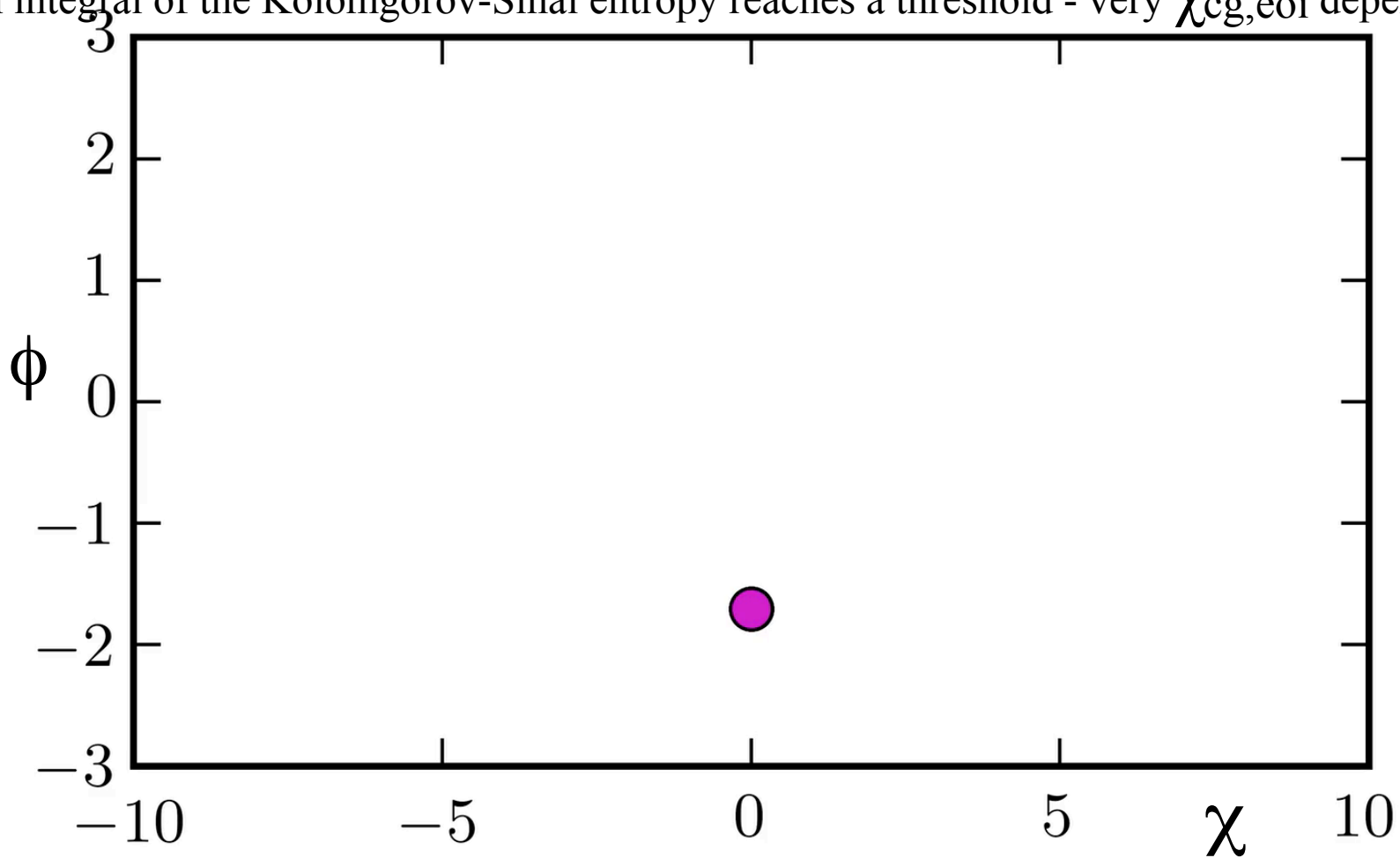
1LPT aka Zeldovich: $\partial x / \partial r = \exp(\mathcal{E}) \rightarrow 0$ density $\rho \sim \exp(-\text{Tr}(\mathcal{E})) \rightarrow \infty$



ballistic billiards $k=0$ mode **phase space string** evolution

2D constrained distribution functions

stopping criterion when coarse-grained entropy of field variables rises \Leftrightarrow strain \mathcal{E} high,
ie when integral of the Kolomgorov-Sinai entropy reaches a threshold - very $\chi_{cg, eoi}$ dependent



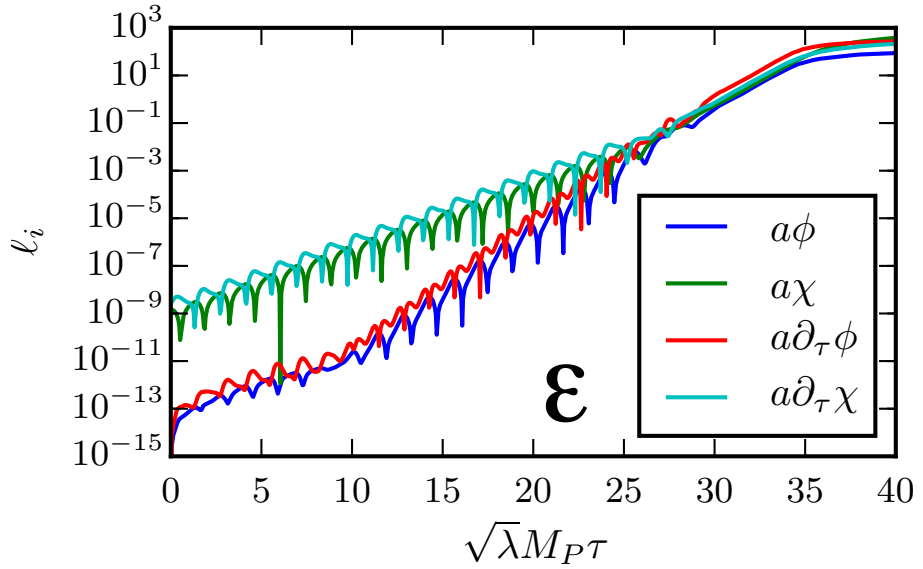
$$V = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



phase space strings

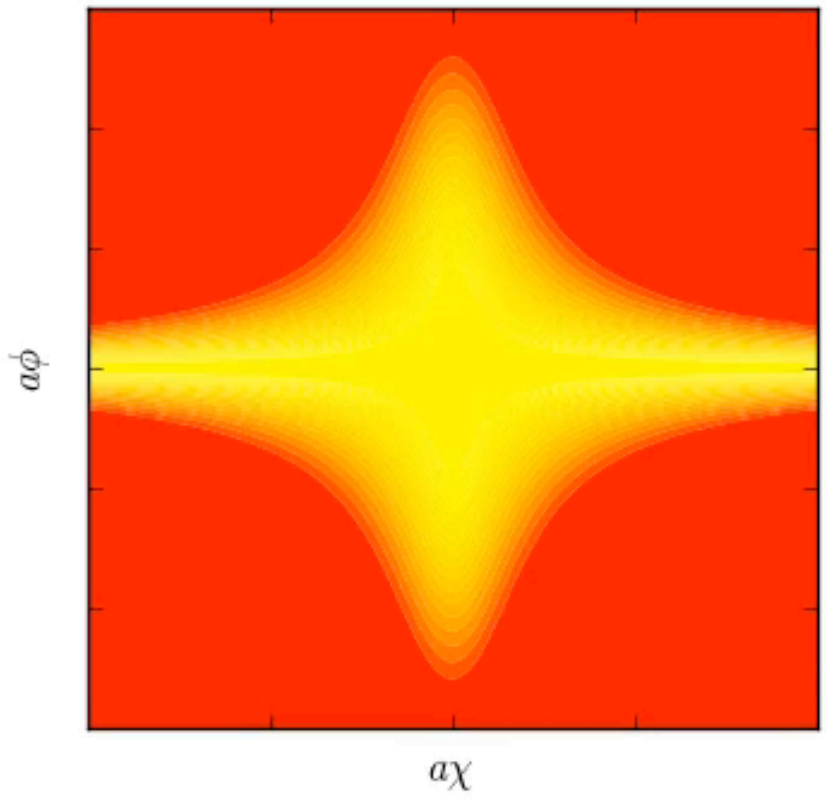
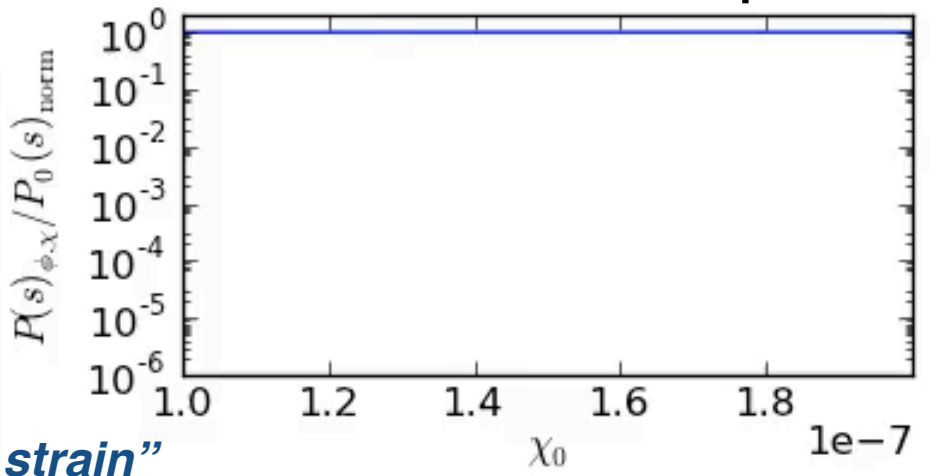
2D constrained distribution functions

*phase string growth in time “parameter strain”
integral of Kolmogorov-Sinai entropy rate*



=> 3D constrained distribution functions

caustics are ubiquitous



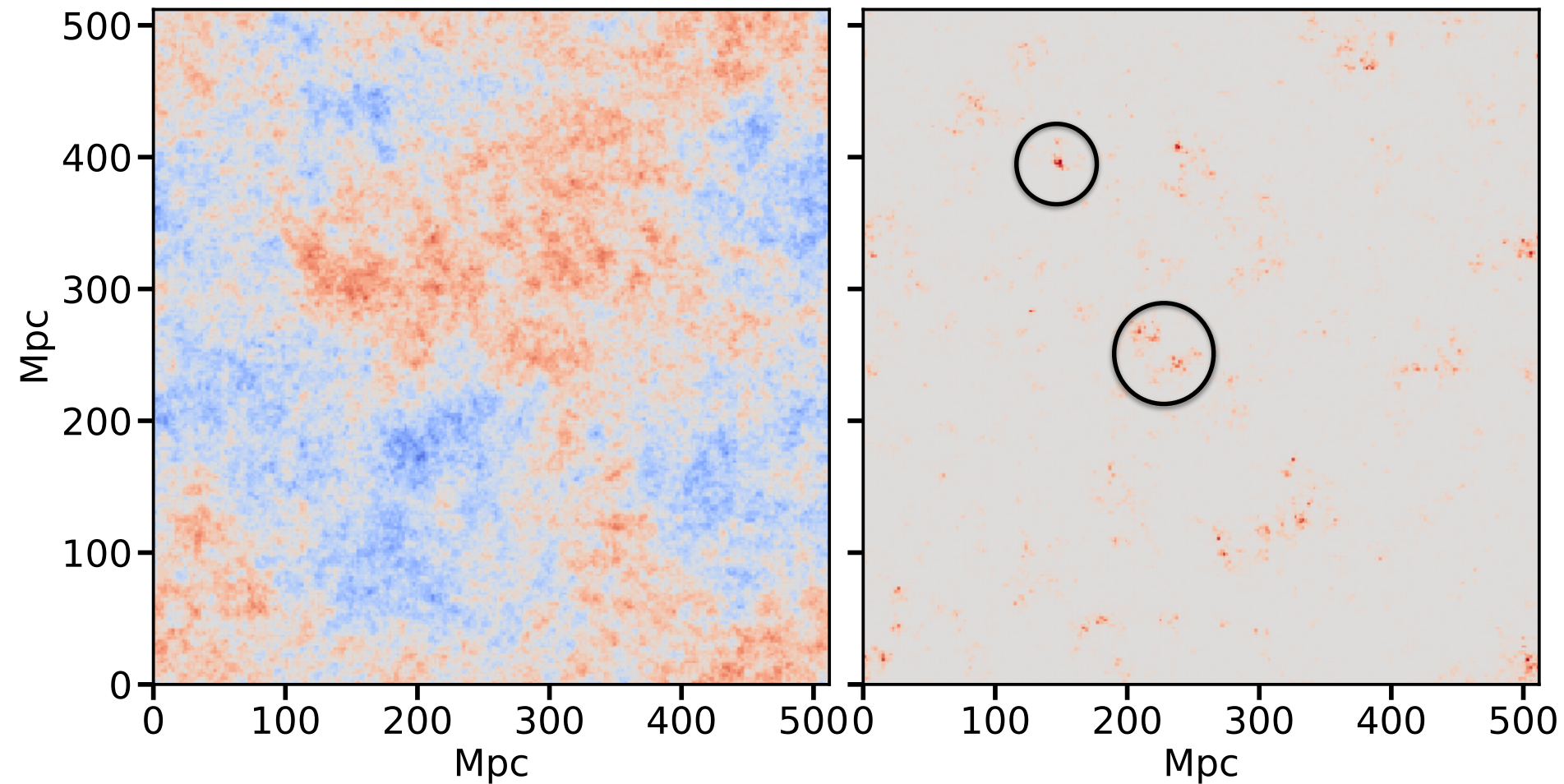
B2FH, b+braden+frolov+huang

Primordial Non-Gaussianity in observable Webskys constructed with the mass-Peak Patch method
+ gas-halo response functions/susceptibilities

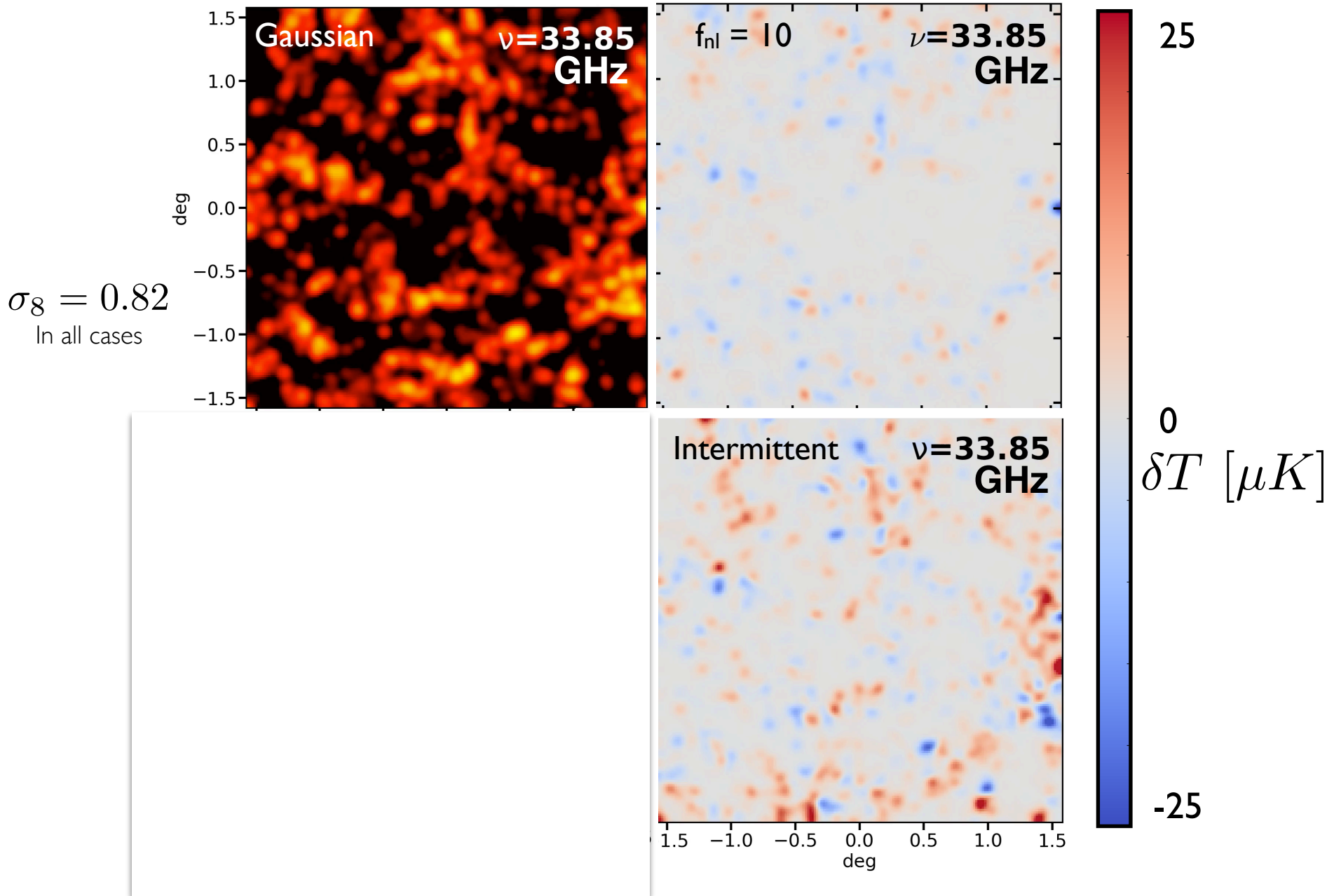
Intermittent Non-Gaussian case
uncorrelated ζ [GRF]

ζ_G

$\zeta_{F(\chi)}$



Primordial Non-Gaussianity in CO; large scale => CHIME much larger volume is better



*role of (2) **instabilities during inflation***

*phenomenology of in-states propagating through localized unstable potential structures to out-states, like scattering theory => **nonGaussianity***

role of “classical evolution/instabilities” in “particle creation” (1) in heating ✓ (2) during inflation

Bond+Braden+Frolov+Morrison - work very much in experimental/exploratory phase

map ballistic extreme-parameter-strain view of (pre-) heating into inflating regime i.e., role of classical instabilities during inflation, need to start with quantum fluctuations but then classical “particle creation” what about particles? tie to entropy old & new way:

$$n_{Ak} \sim \rho_{Ak} / \hbar \omega_{Ak}(t) \sim \exp(\Delta s_{Ak})$$

quantum fluctuations are there, but **only as seeds for instabilities** in which trajectories diverge: *little probability Gaussian blobs stretch into highly deformed elongated surfaces. “phase strings” in 2D, 3D*

history (for me). sbb87-89 $\langle \delta \mathcal{P}_{\phi^A \phi^A}(k) | \delta V, \delta m_{eff}^2 \rangle$, $\langle \delta \mathcal{P}_{\zeta \zeta}(k) | \delta V(\phi, \chi) \text{ controls} \rangle$
multifield hybrid, mountains/valleys of extra power. role in non-Gaussianity. role of Higgs et al.

tool: full linearized k evolution, from inside to outside

build on vilenkin/starobinsky stochastic inflation: sb90, 91

used the attractor, aka reduced Hamilton principal function, $\mathbf{S}_{reduced} \sim -2M_{Pl}^2 H$ gives $\boldsymbol{\pi}_A$

B91 more general Langevin network leads to $P(\phi_A, \boldsymbol{\pi}_A, H | \alpha)$ or better $P(\phi_A, \boldsymbol{\pi}_A, H | H_a)$

=> nice expression in terms of quantum diffusion velocity/current

today:

dilemma 1: missing terms in crossing horizon (coarse grain / fine grain flow)

dilemma 2: outside horizon is a condensate. how to express this

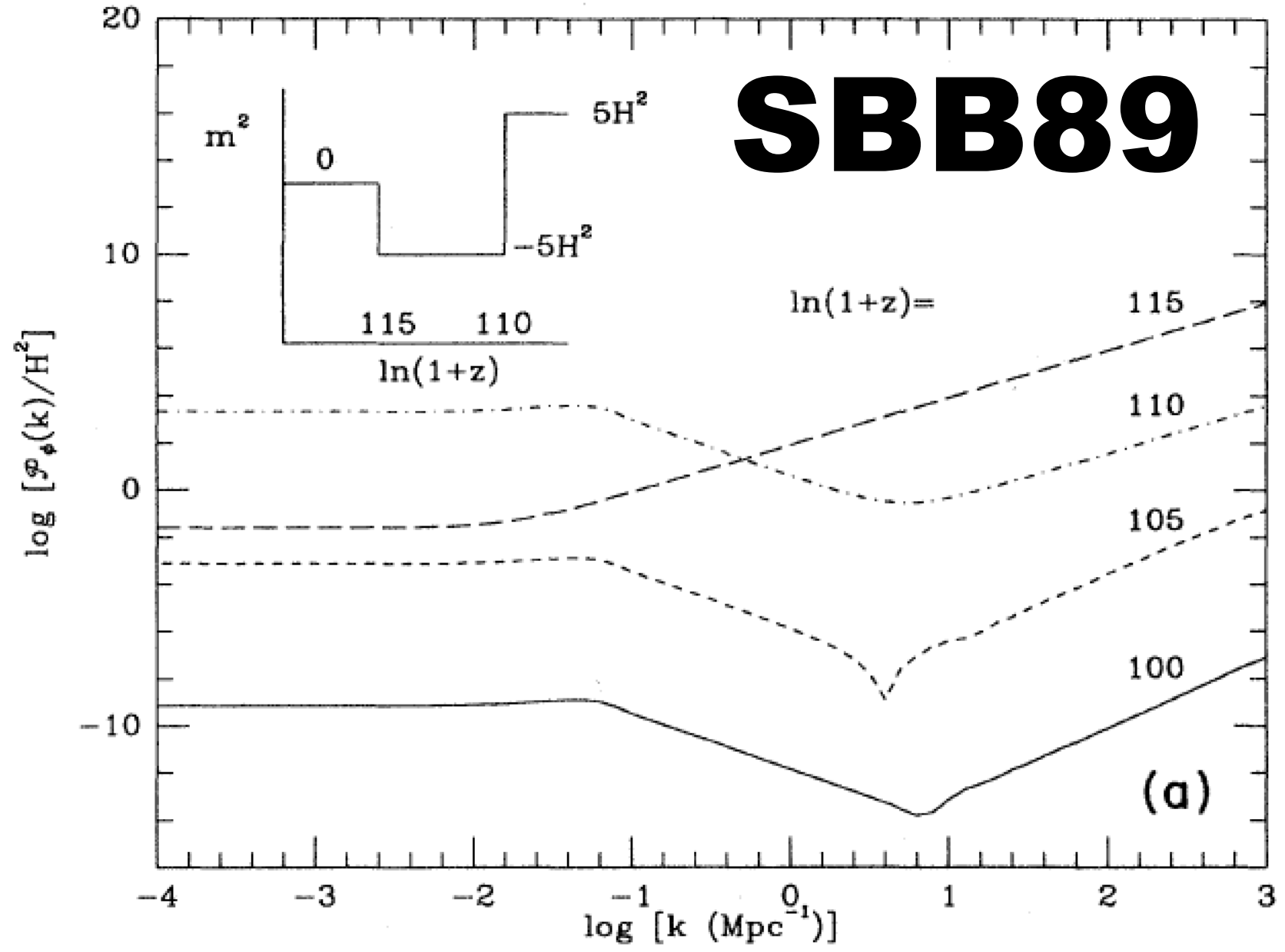
dilemma 3: phase coherence as in classical realizations are useful

- incorporate via coherent state condensates and fluctuations upon them??

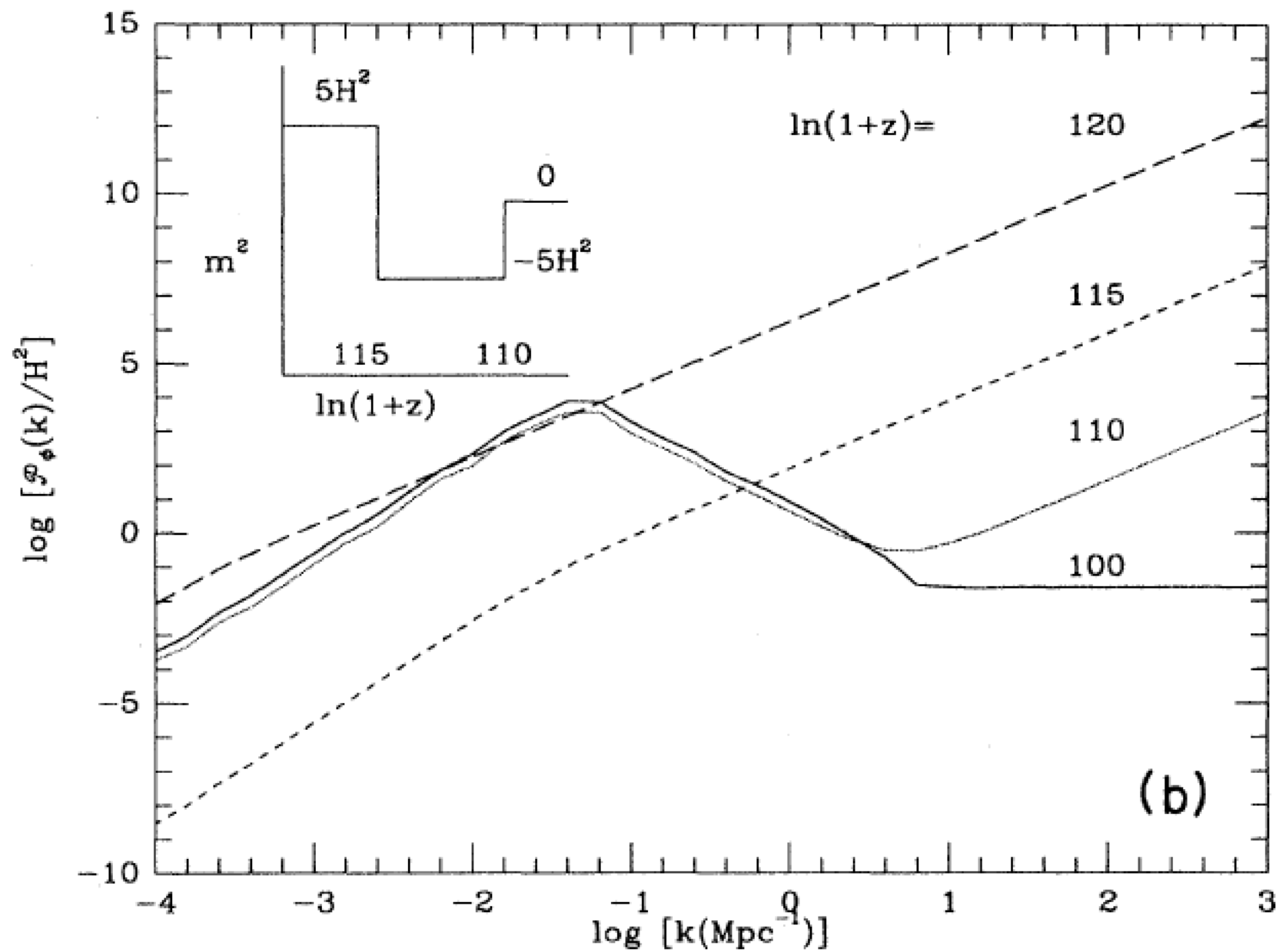
instabilities with quantum fluctuations the tiny seeds

Quantum Response of Driven Field to Potential Changes

SBB89

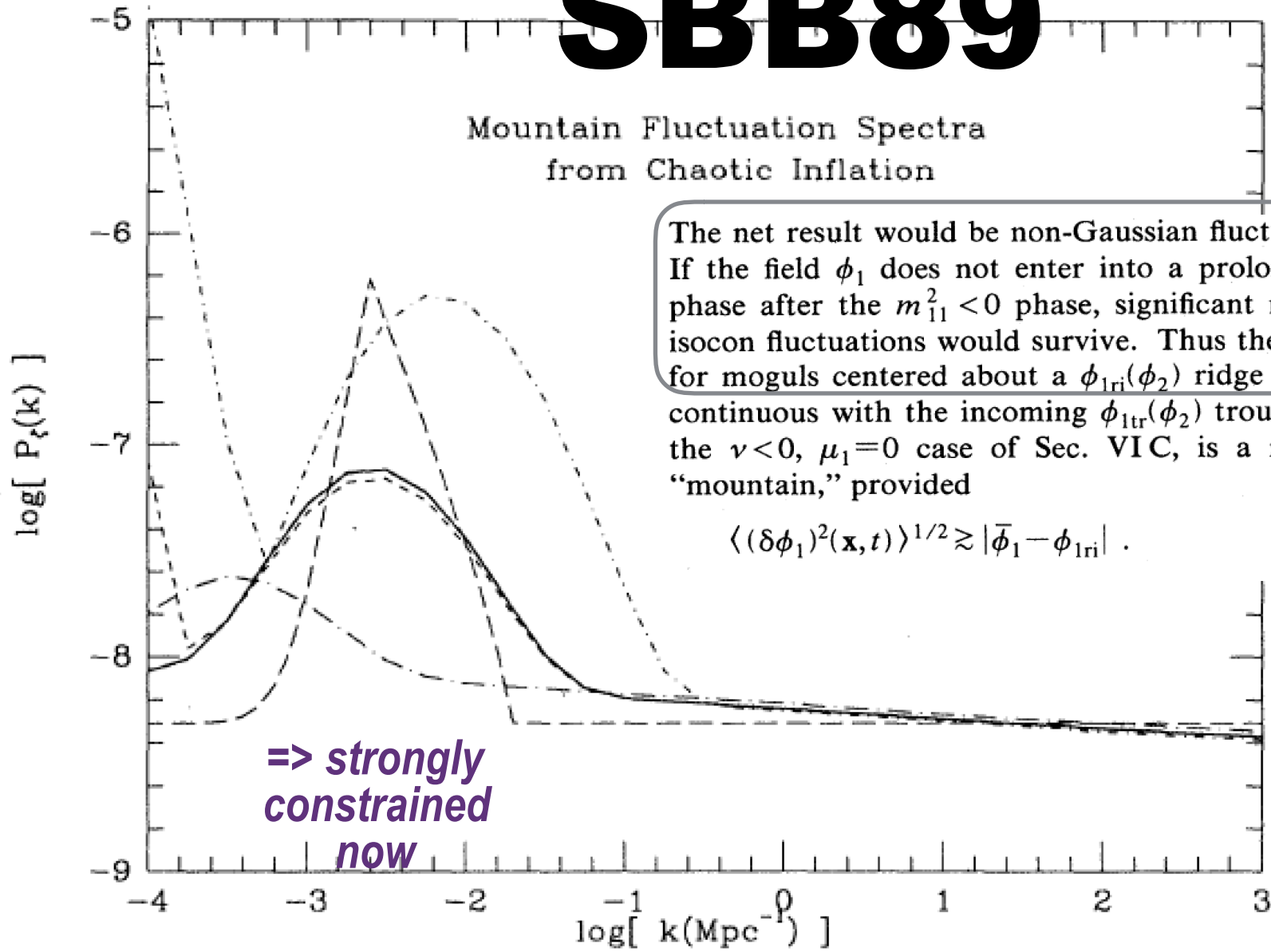


(a)



SBB89

Mountain Fluctuation Spectra from Chaotic Inflation



experiment χ -light

in states

$1e-11 V + \Delta V$

7
6
5
4
3

0.04

0.00
 t

-0.04

5.5

6.0

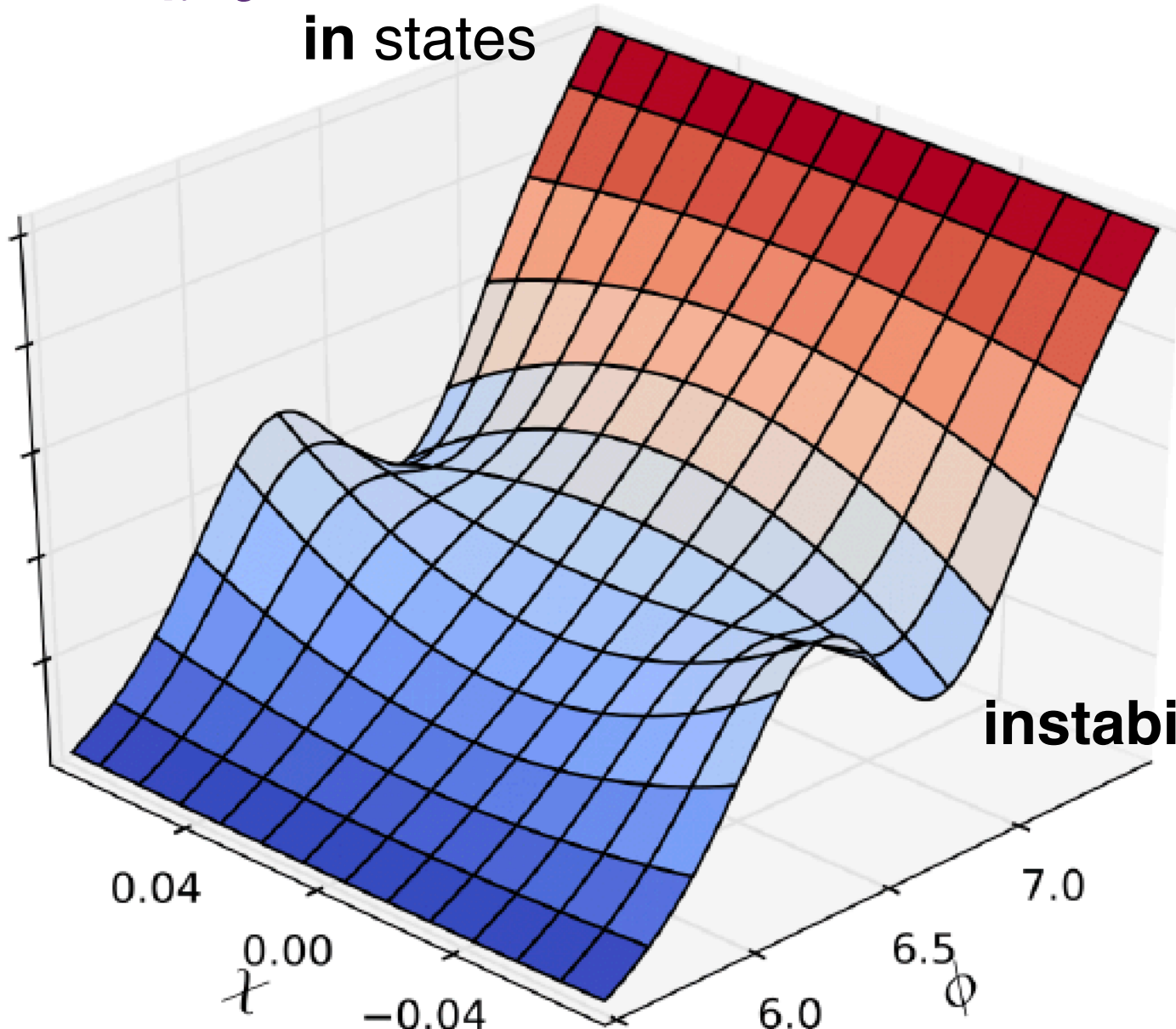
6.5
 ϕ

7.0

instability

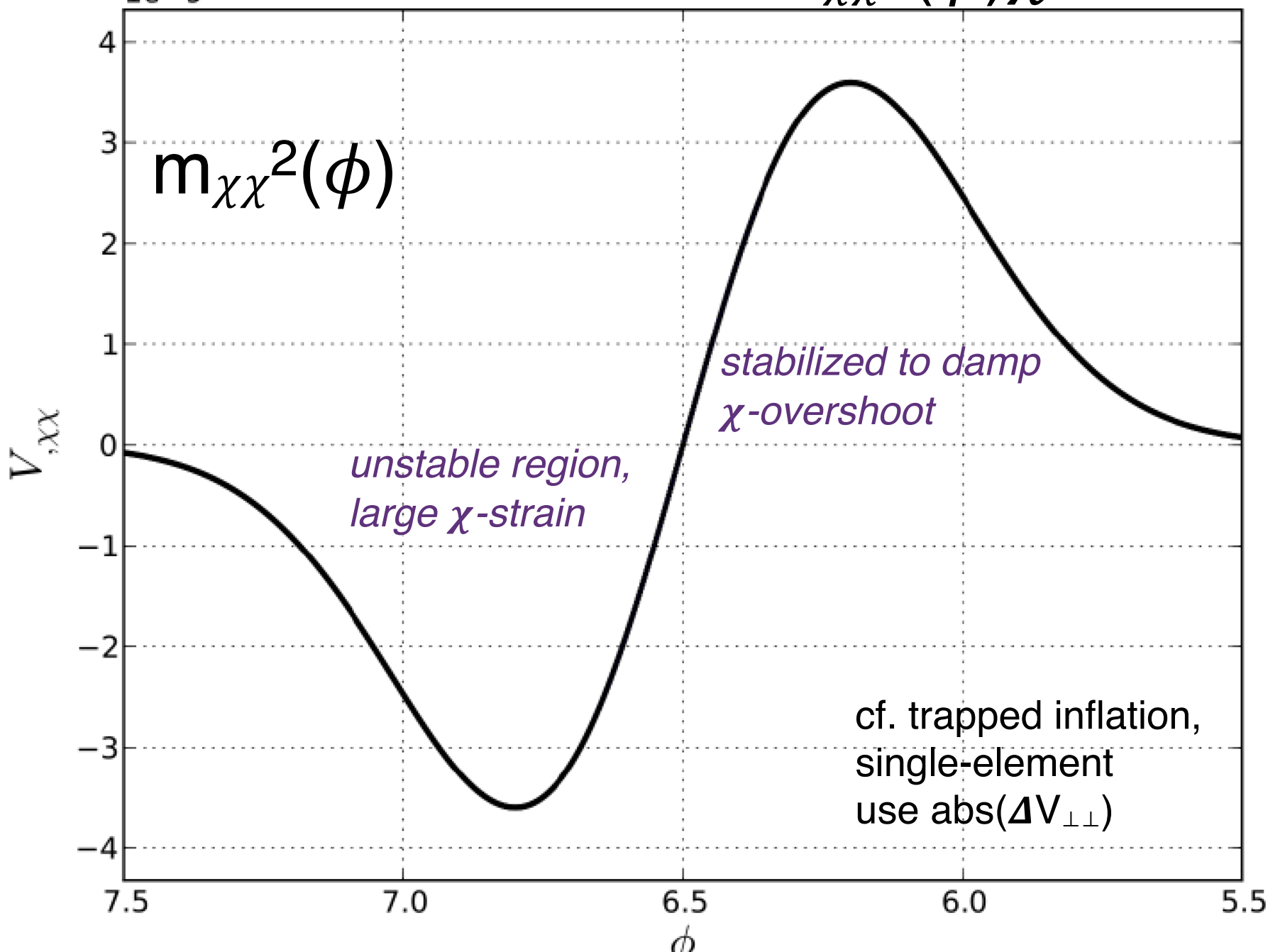
out states

Bond+Braden+Frolov+Morrison



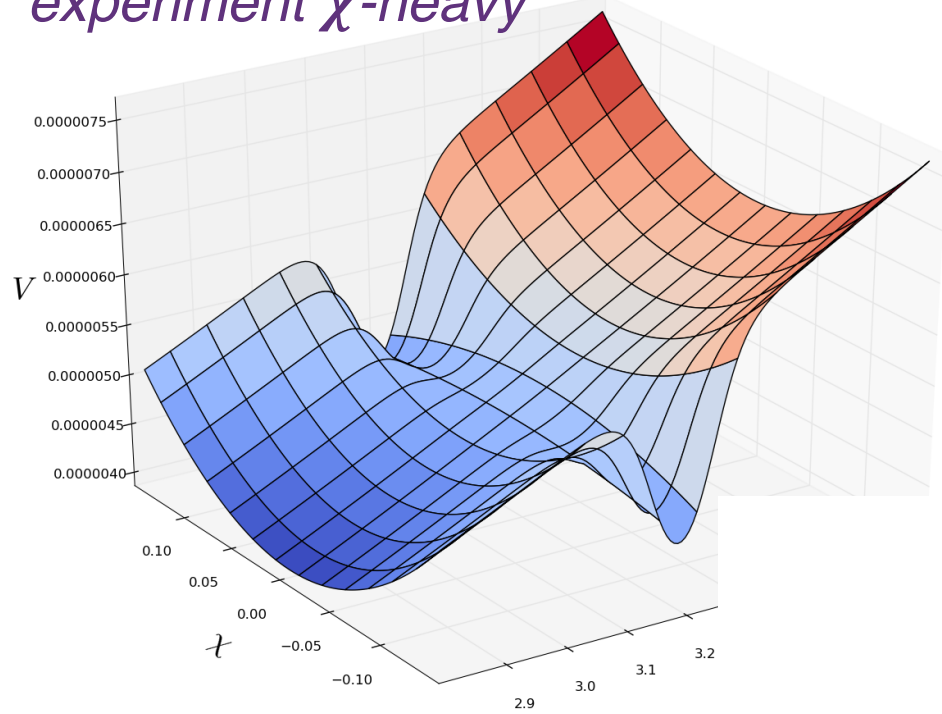
experiment χ -light
1e-9

$$\Delta V_{\perp\perp} = m_{\chi\chi}^2(\phi) \chi^2 / 2$$



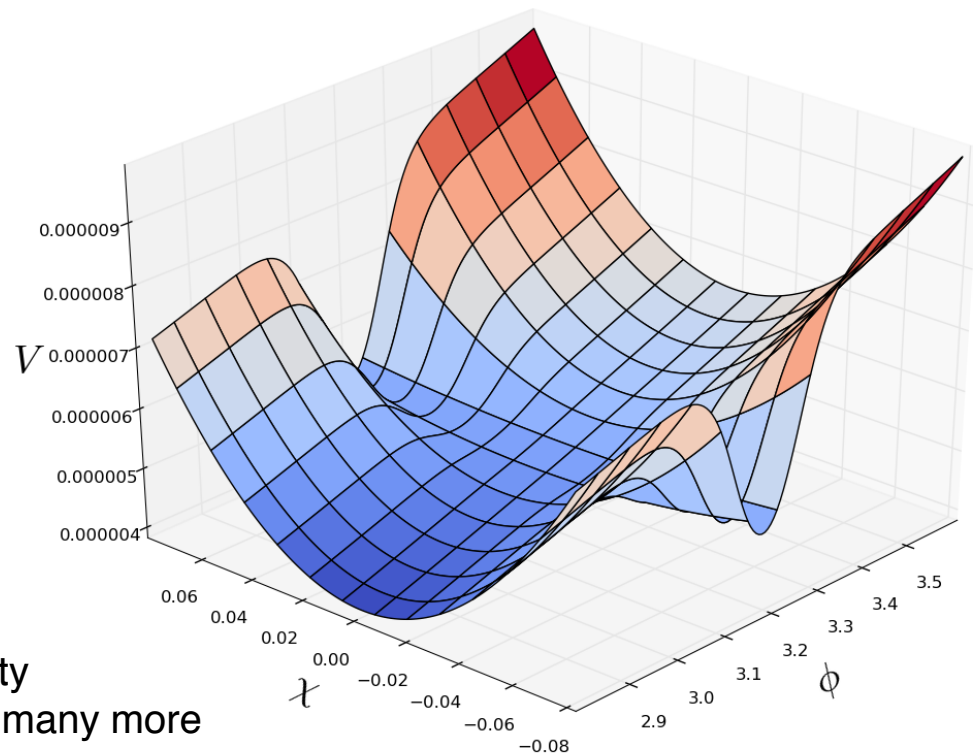
experiment χ -heavy

Bond+Braden+Frolov+Morrison



potential surface instability

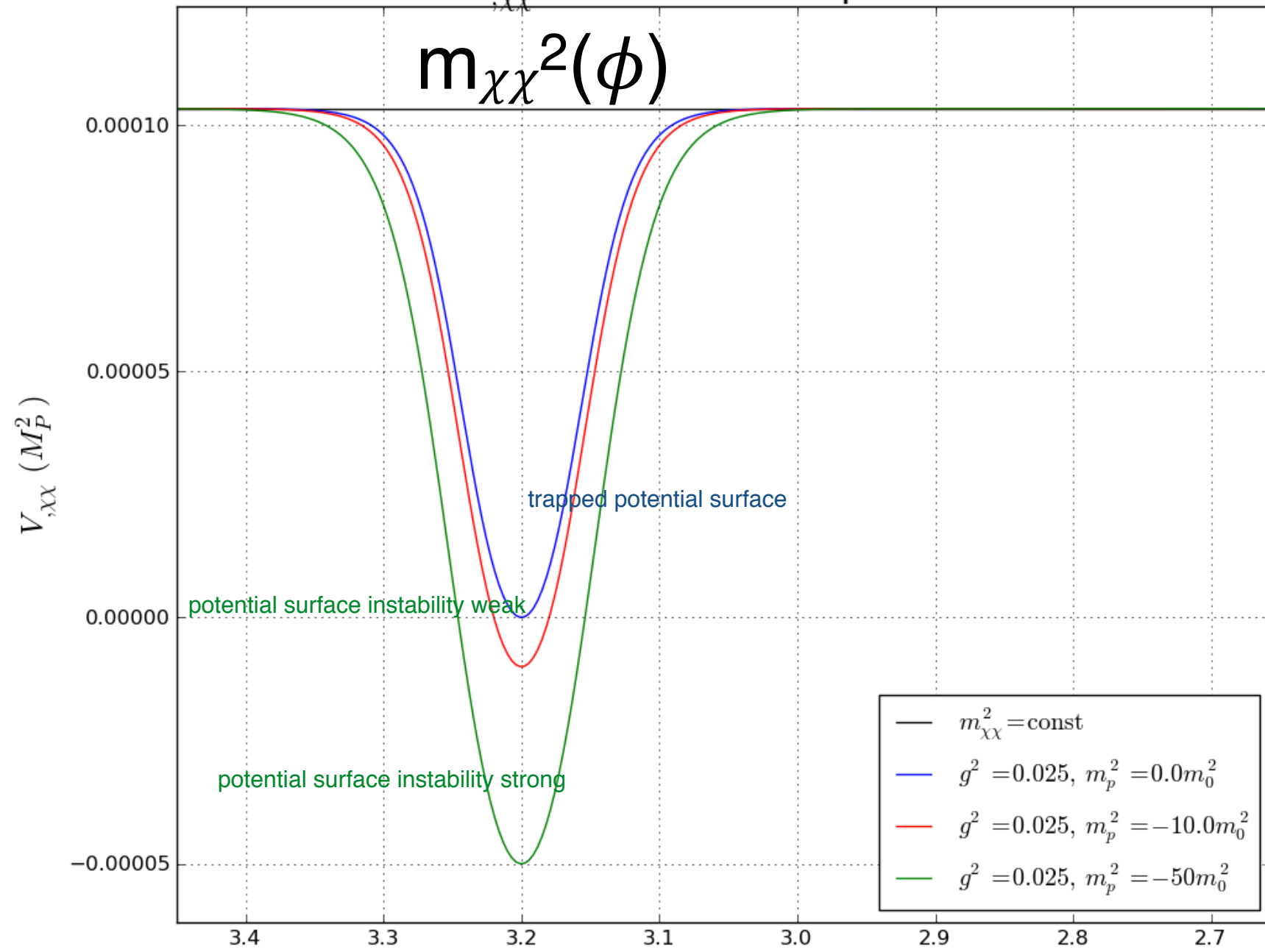
trapped potential surface



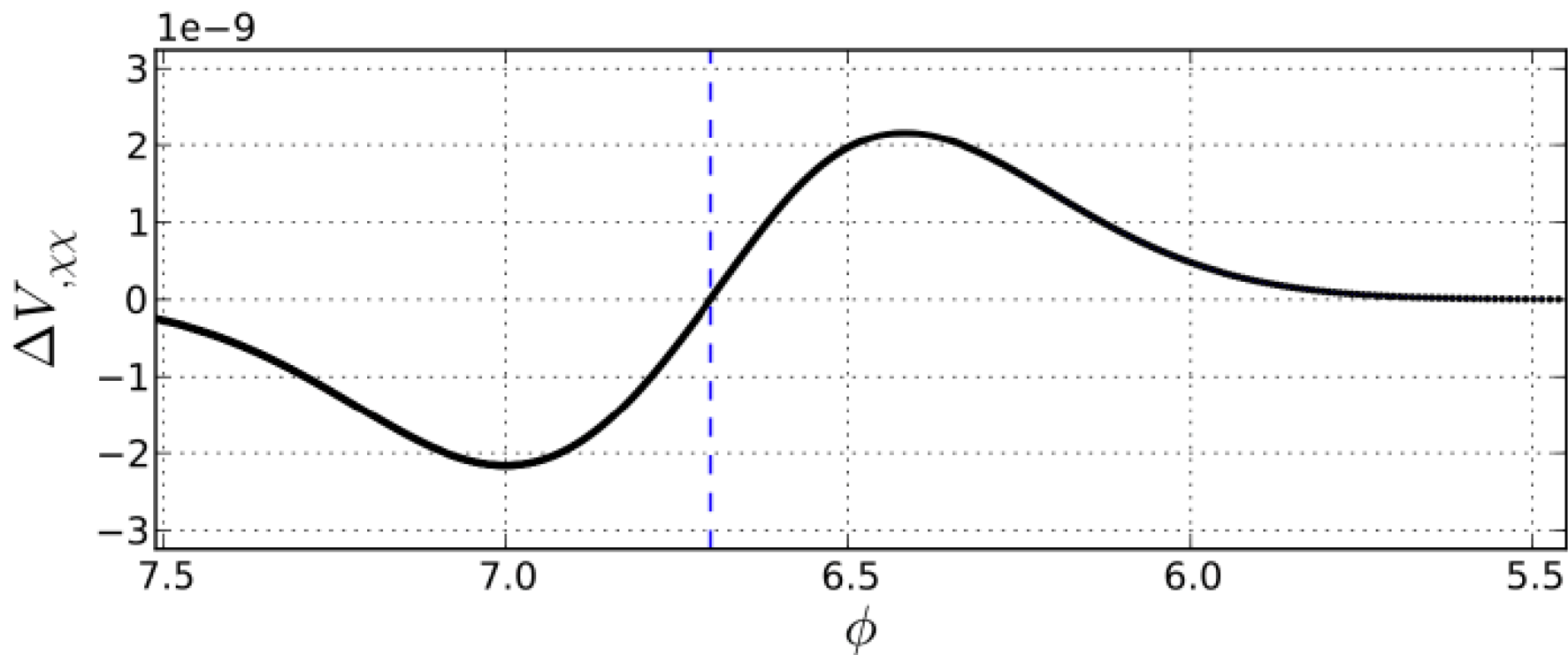
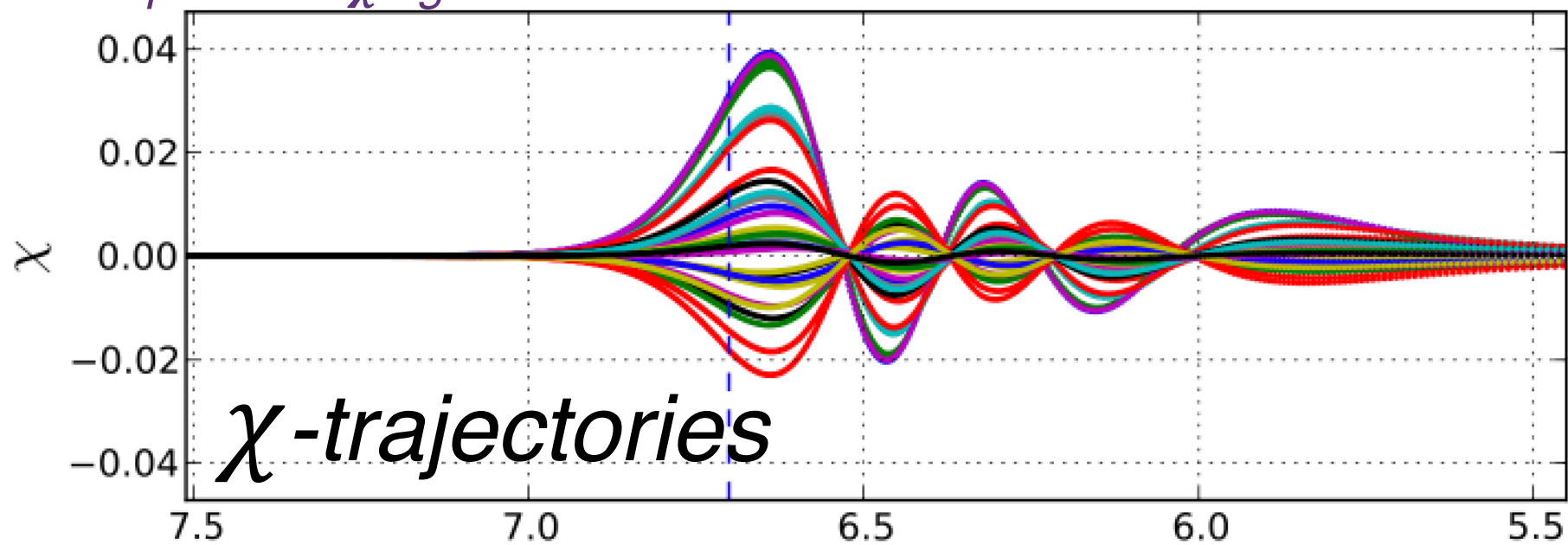
trapped inflation: same parameters, no instability
.. Kofman, Silverstein, Green, Barnaby, Huang, many more

$V_{,\chi\chi}$ Parameter Comparison

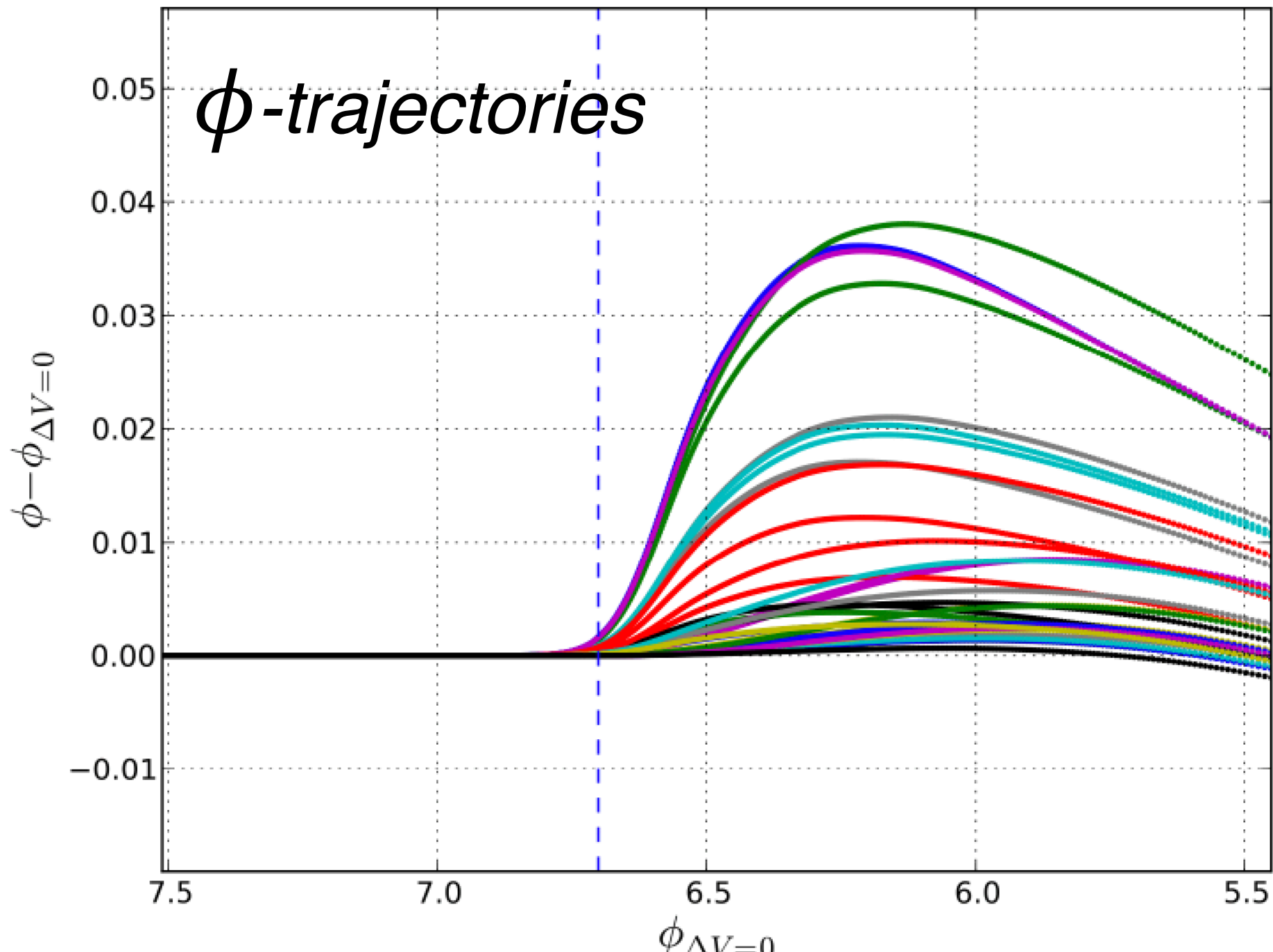
$$m_{\chi\chi}^2(\phi)$$



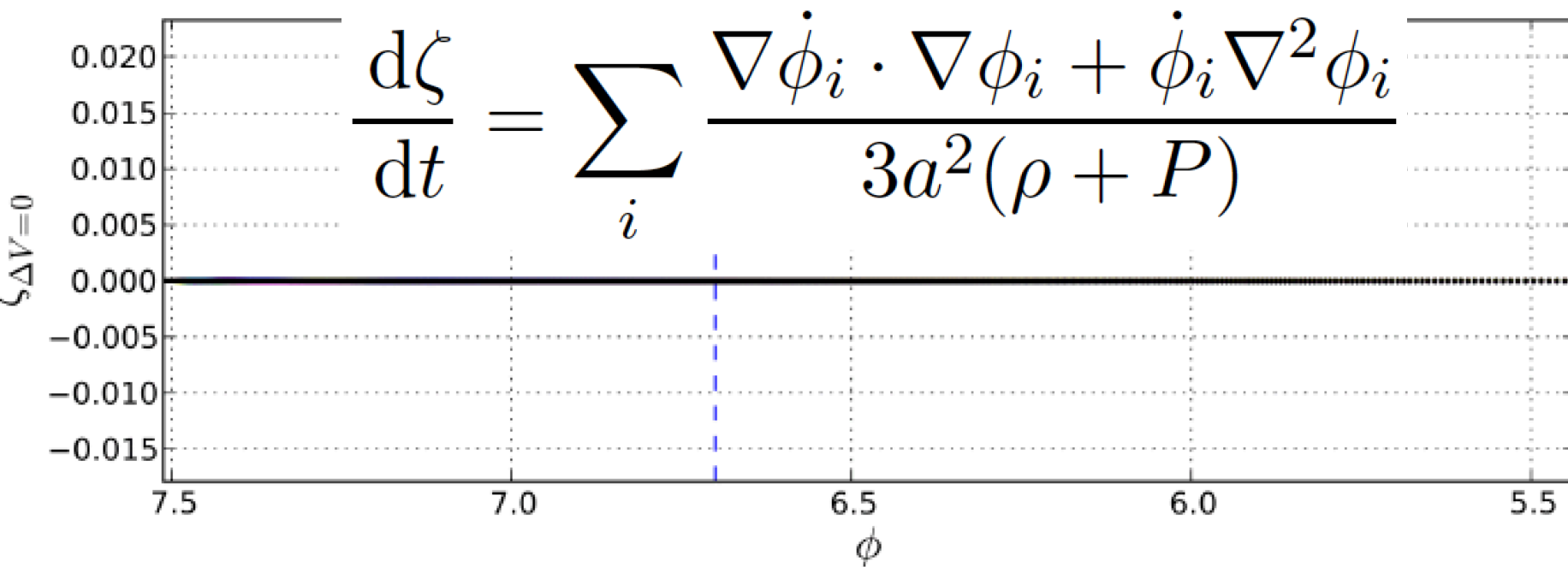
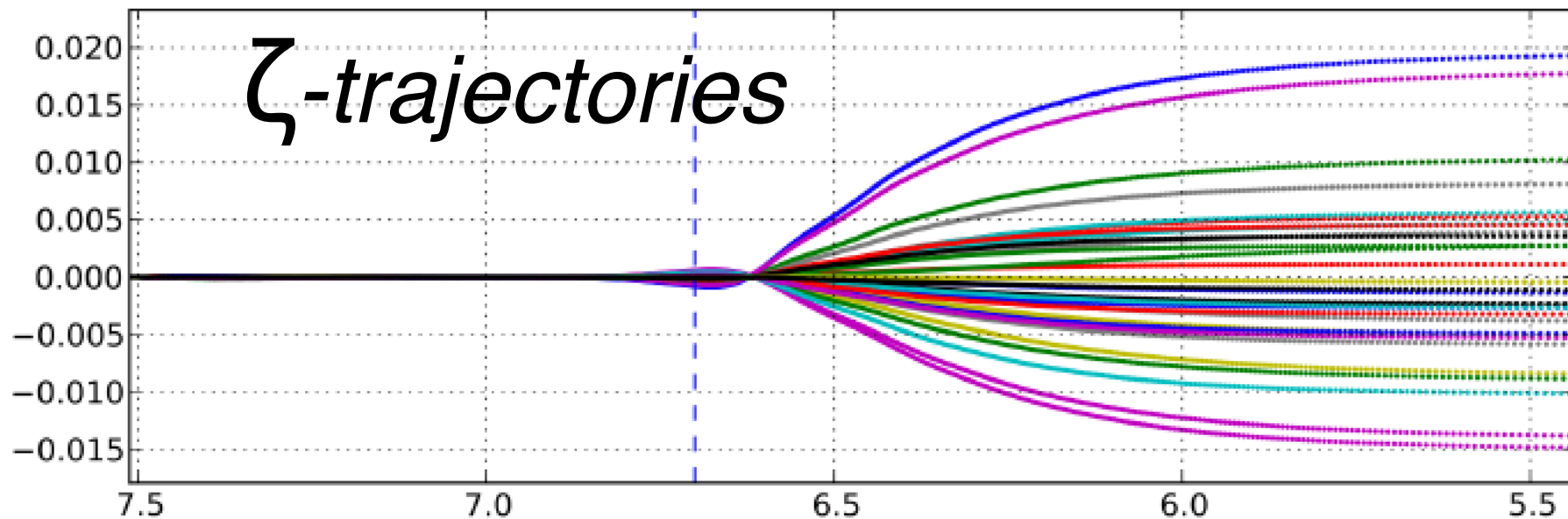
experiment χ -light

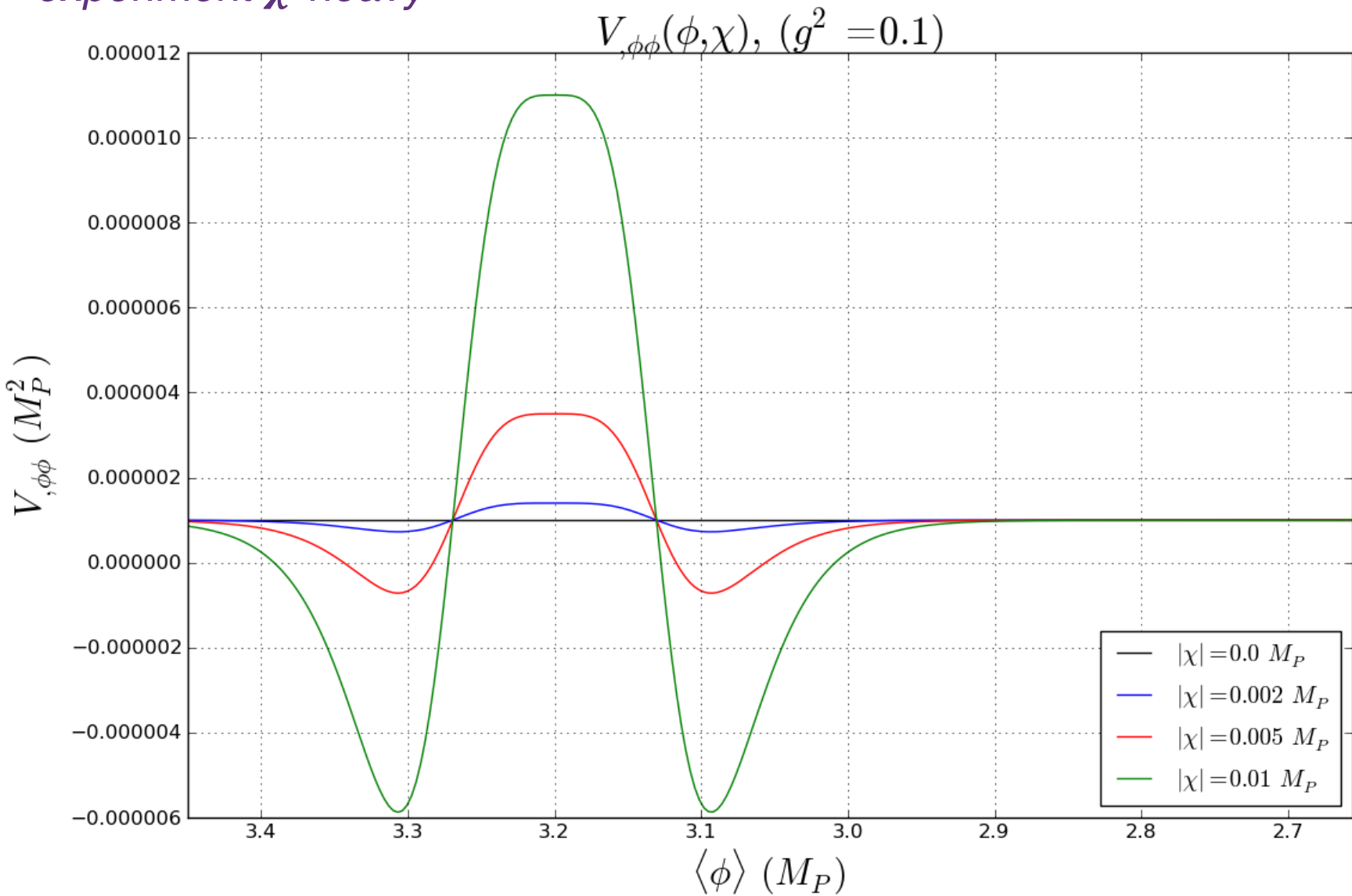


experiment χ -light

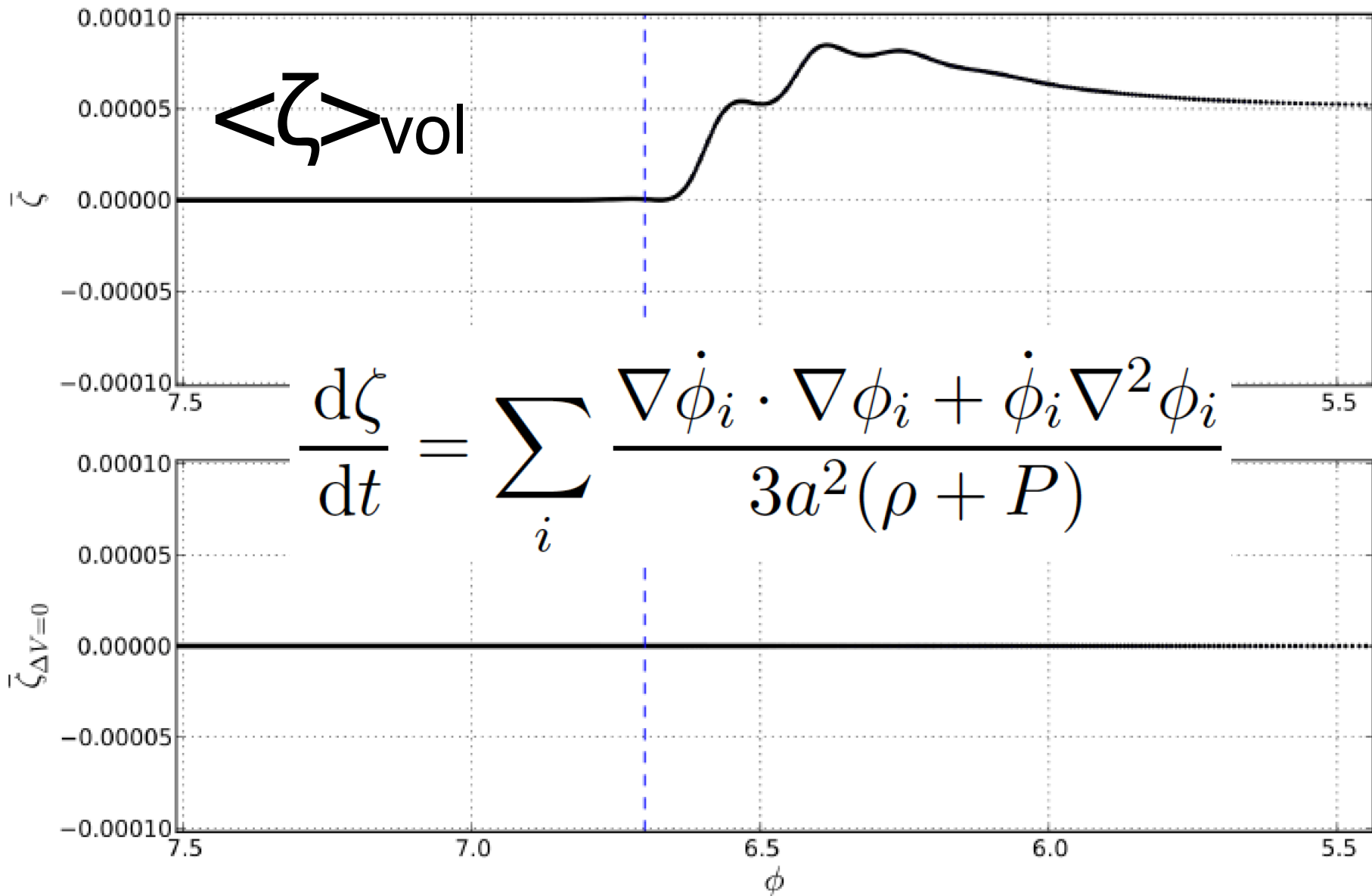


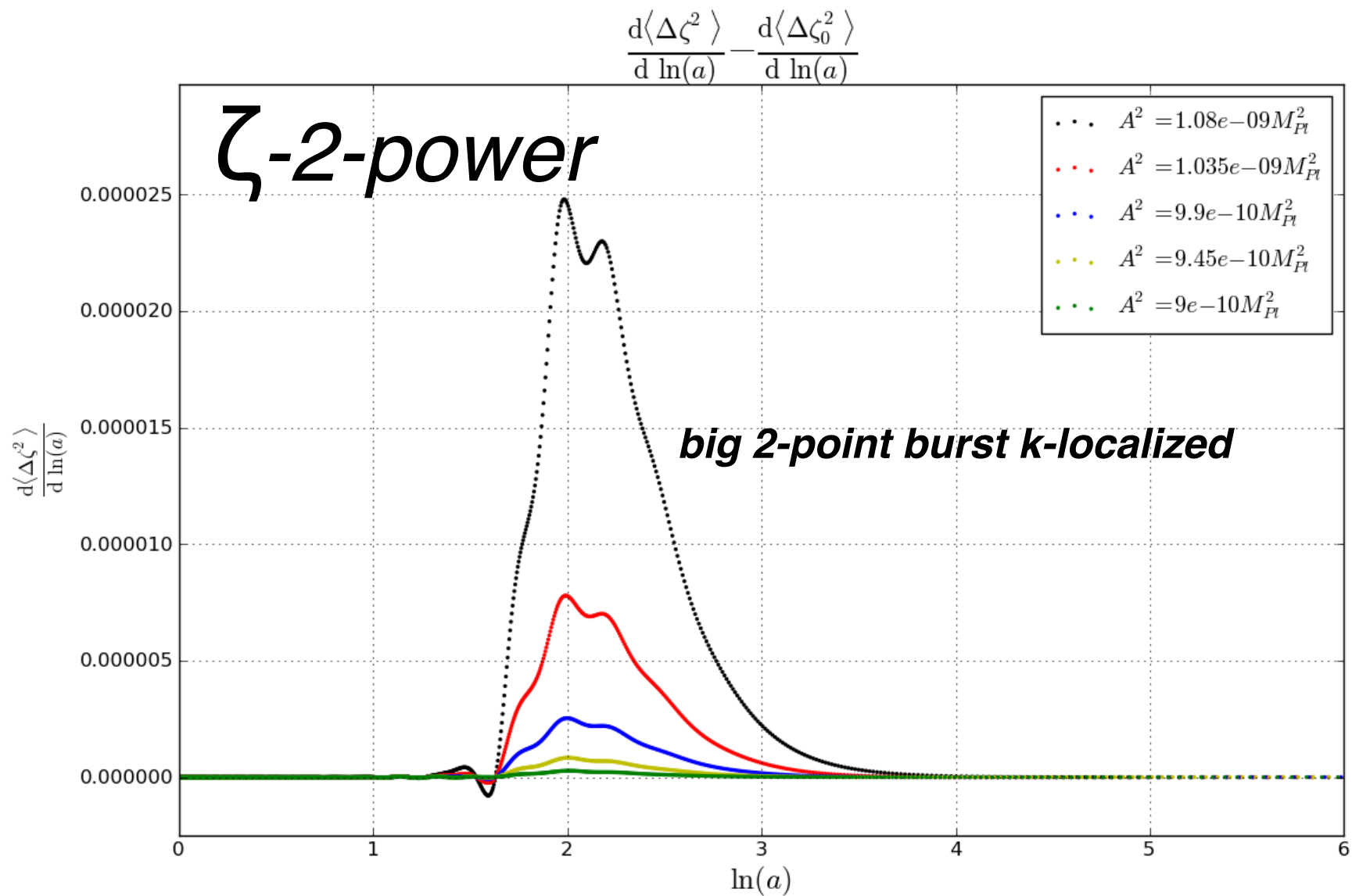
experiment χ -light

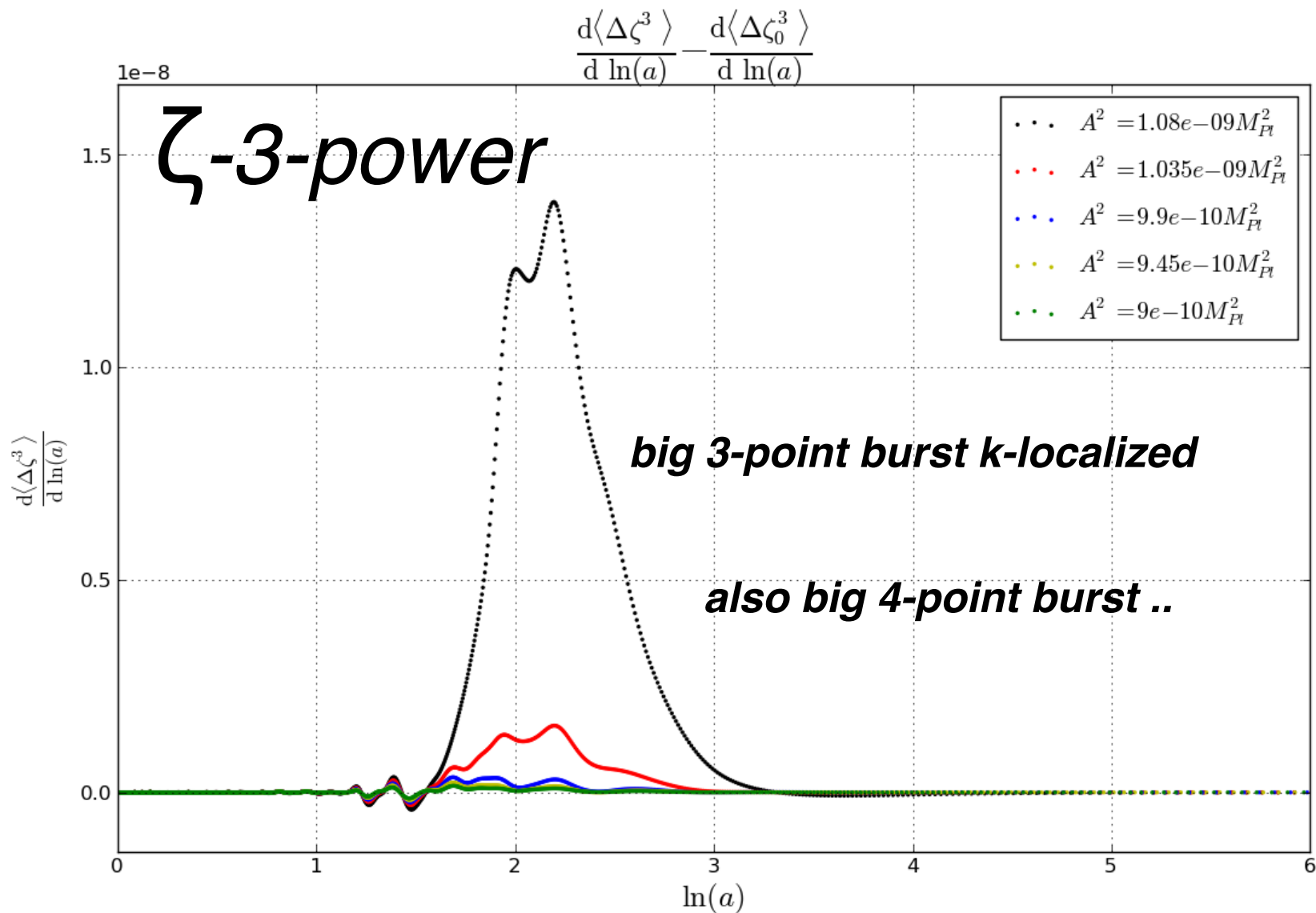




experiment χ -light







occupation numbers & particle creation ~ “Gaussian entropy” in the single A-field

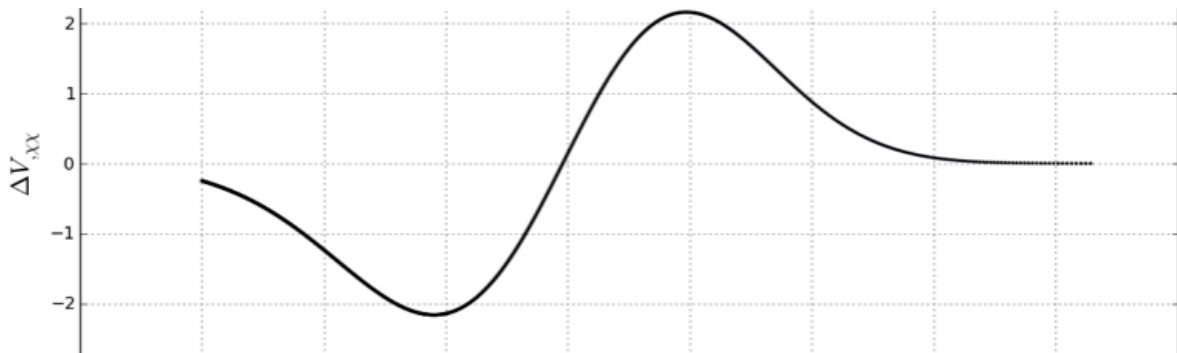
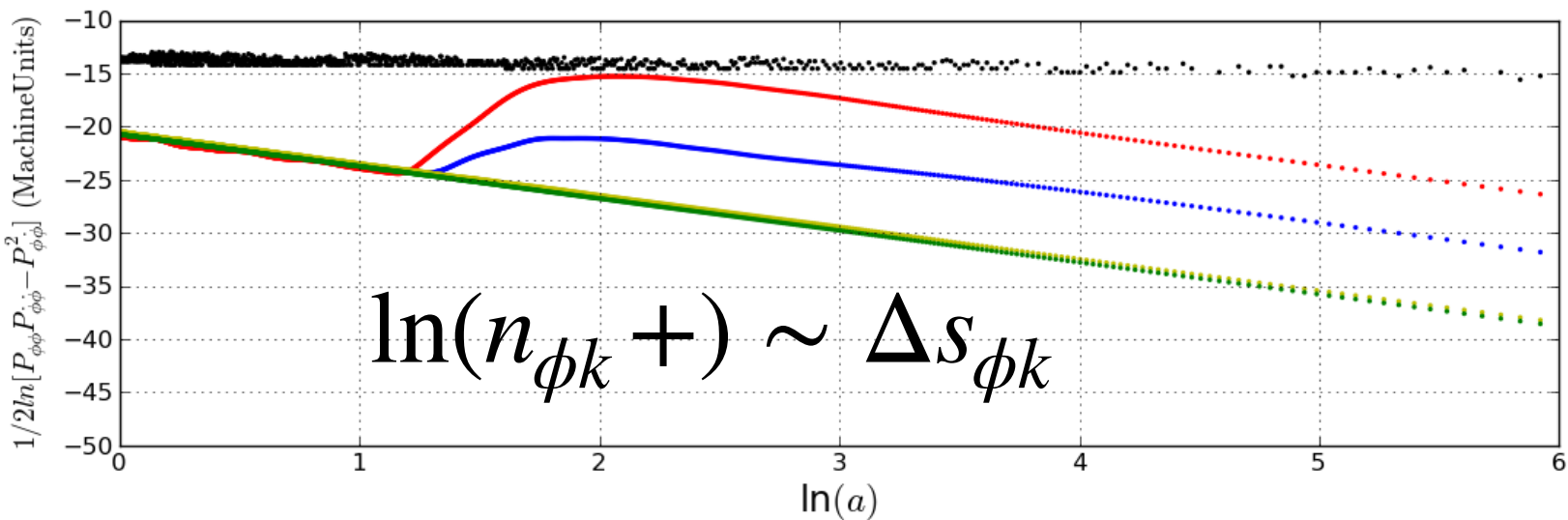
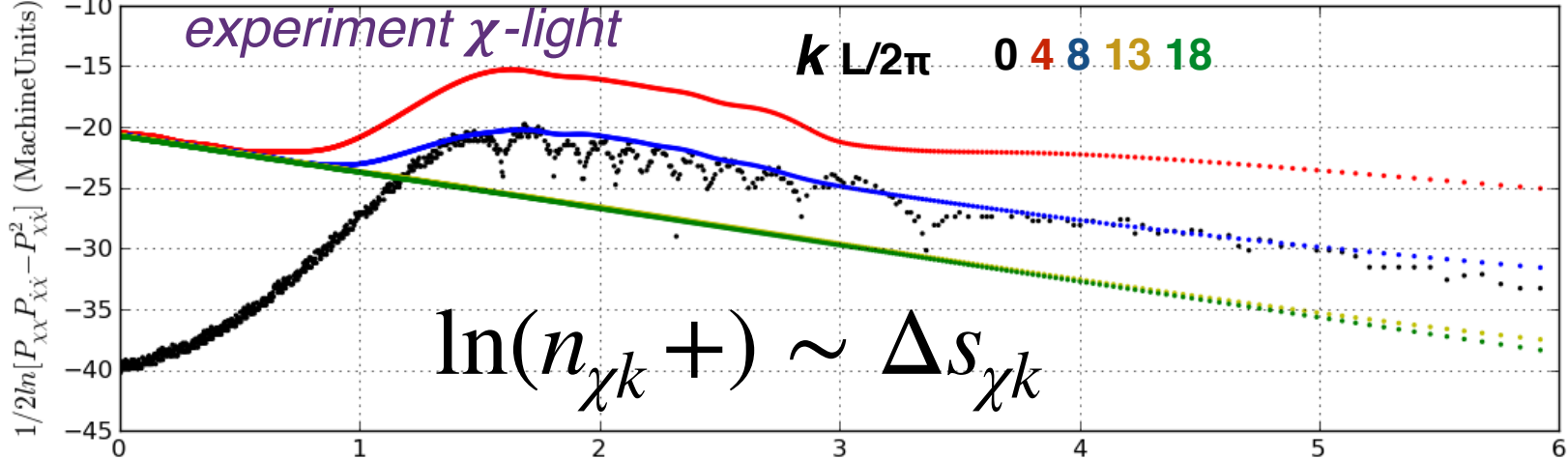
$$\ln(n_{\phi^{Ak}} +) \sim \Delta S_{\phi^{Ak}} \sim \frac{1}{2} \text{Trace} \ln [C_{\phi^A \phi^A} C_{\Pi_A \Pi_A} - C_{\phi^A \Pi_A}^2]$$

occupation $\sim n_{Ak} \sim e^{\Delta S_{Ak}}$

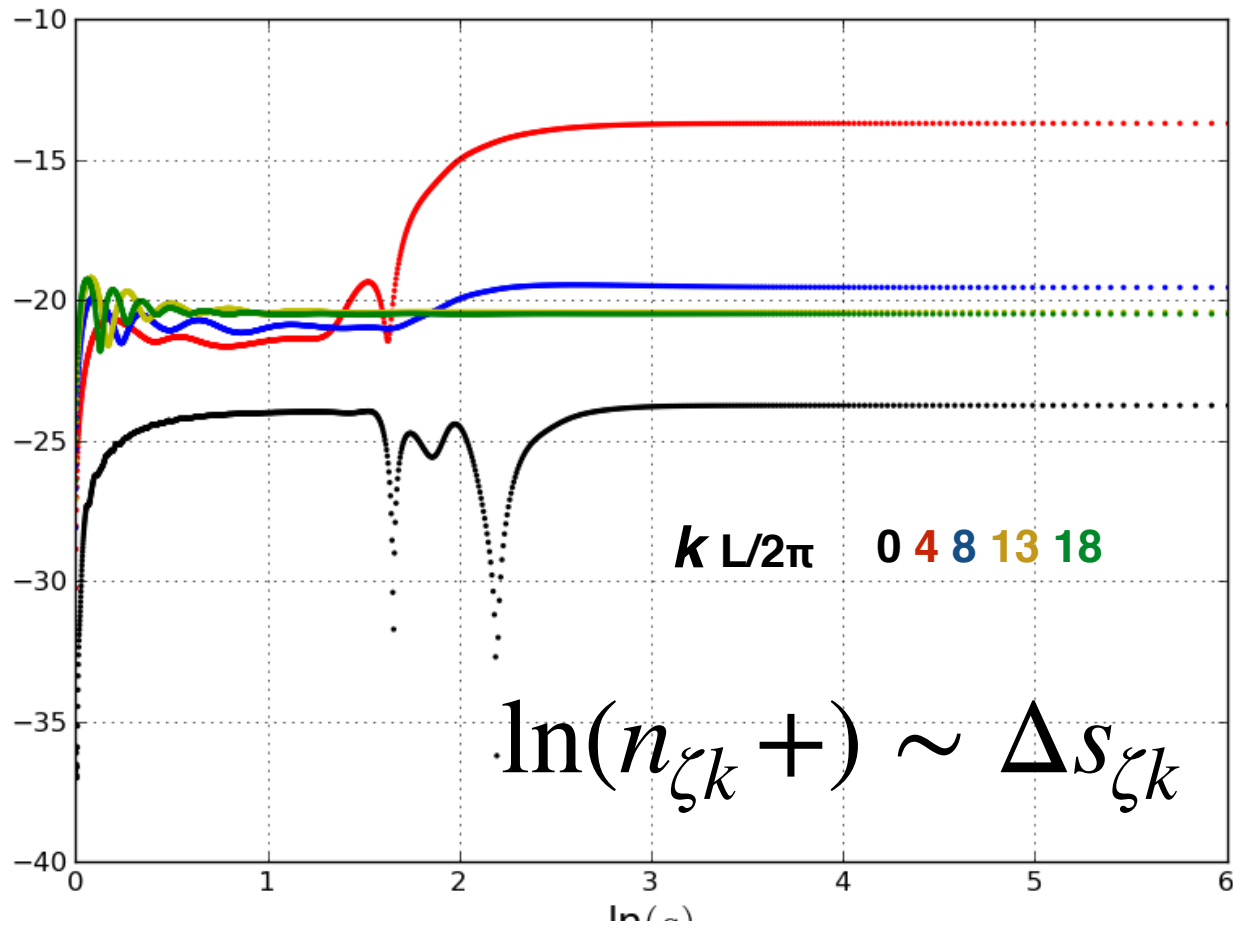
old way if well defined mode energies $\omega_{Ak}(t)$ $\ln(n_{Ak} + 1/2) \sim \ln[\rho_A / \hbar \omega_{Ak}]$

full “Gaussian entropy” in the 2 fields, C are k-mode correlations = power spectra - generalized Sackur-Tetrode

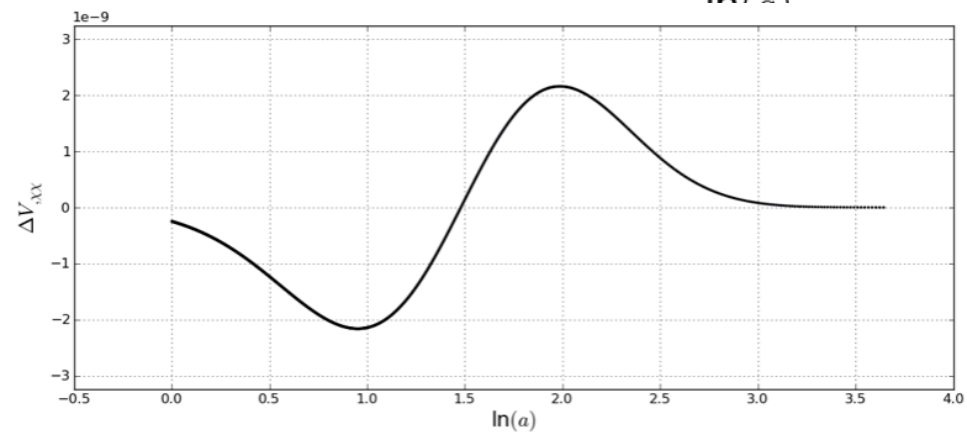
$$\Delta S_{A+B,k} = \frac{1}{2} \text{Trace} \ln [C_{\phi^A \phi^B} C_{\Pi^A \Pi^B} - C_{\phi^A \Pi^B} C_{\Pi^A \phi^B}]$$

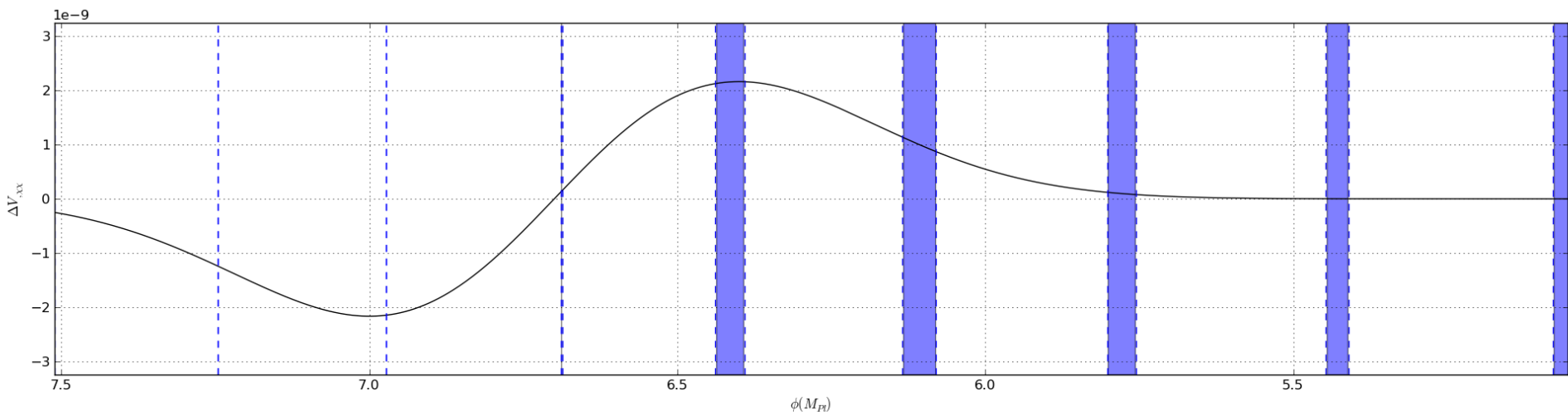
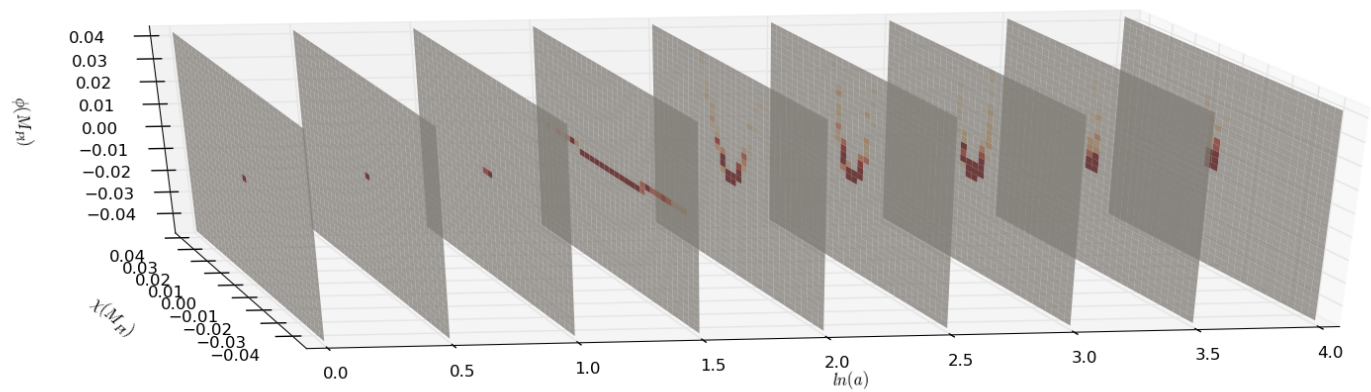


experiment χ -light $\ln(P_{\zeta\zeta})$

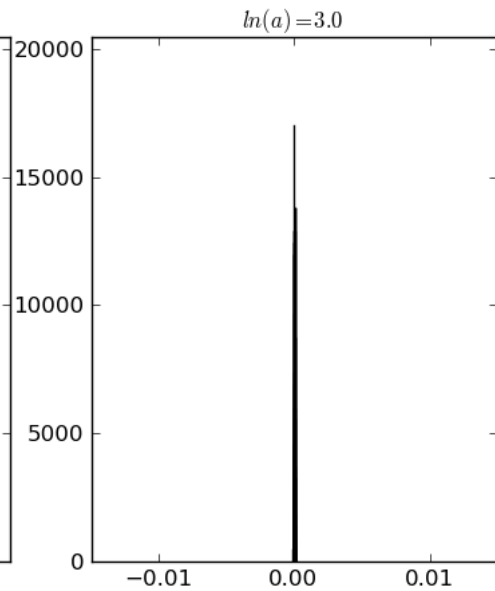
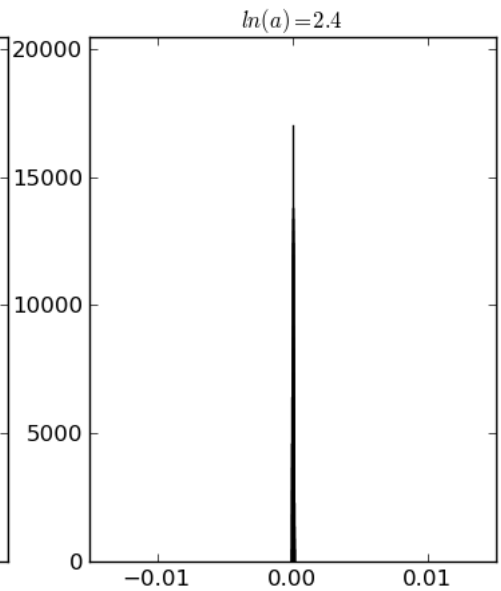
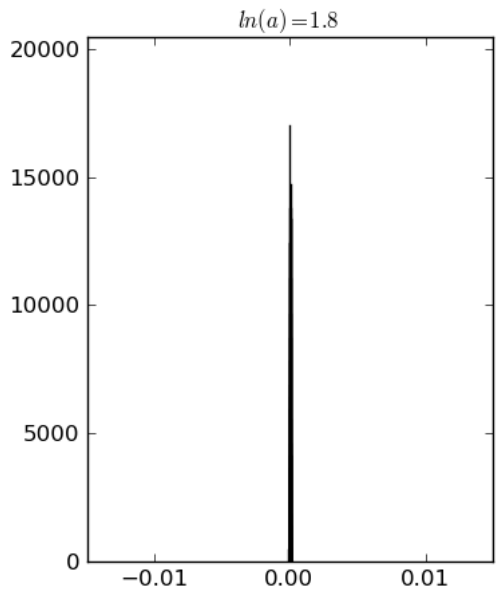
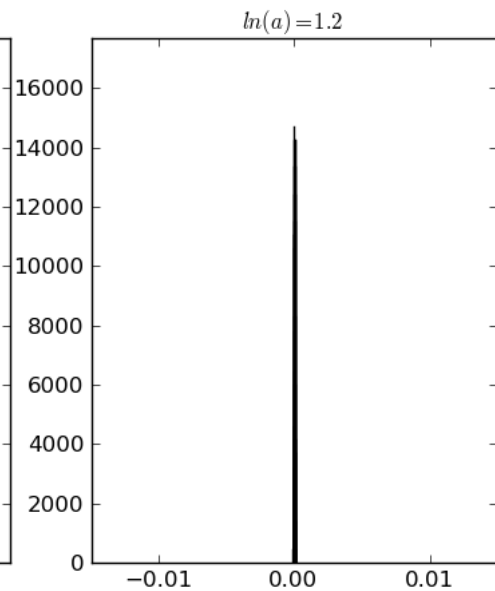
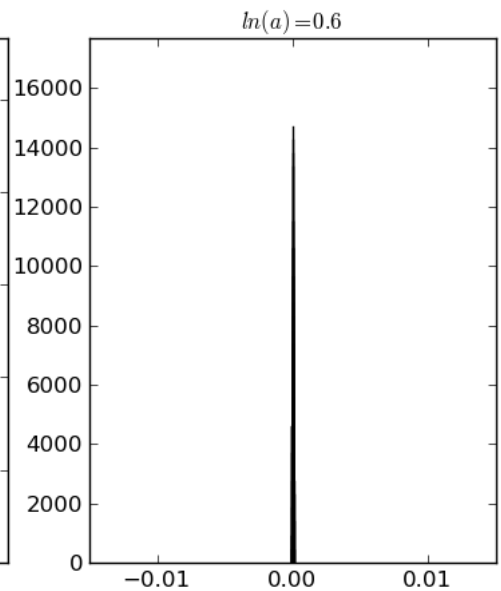
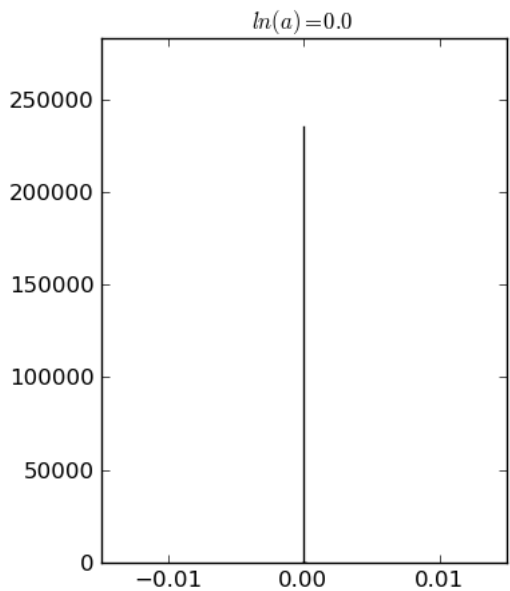


phonon occupation

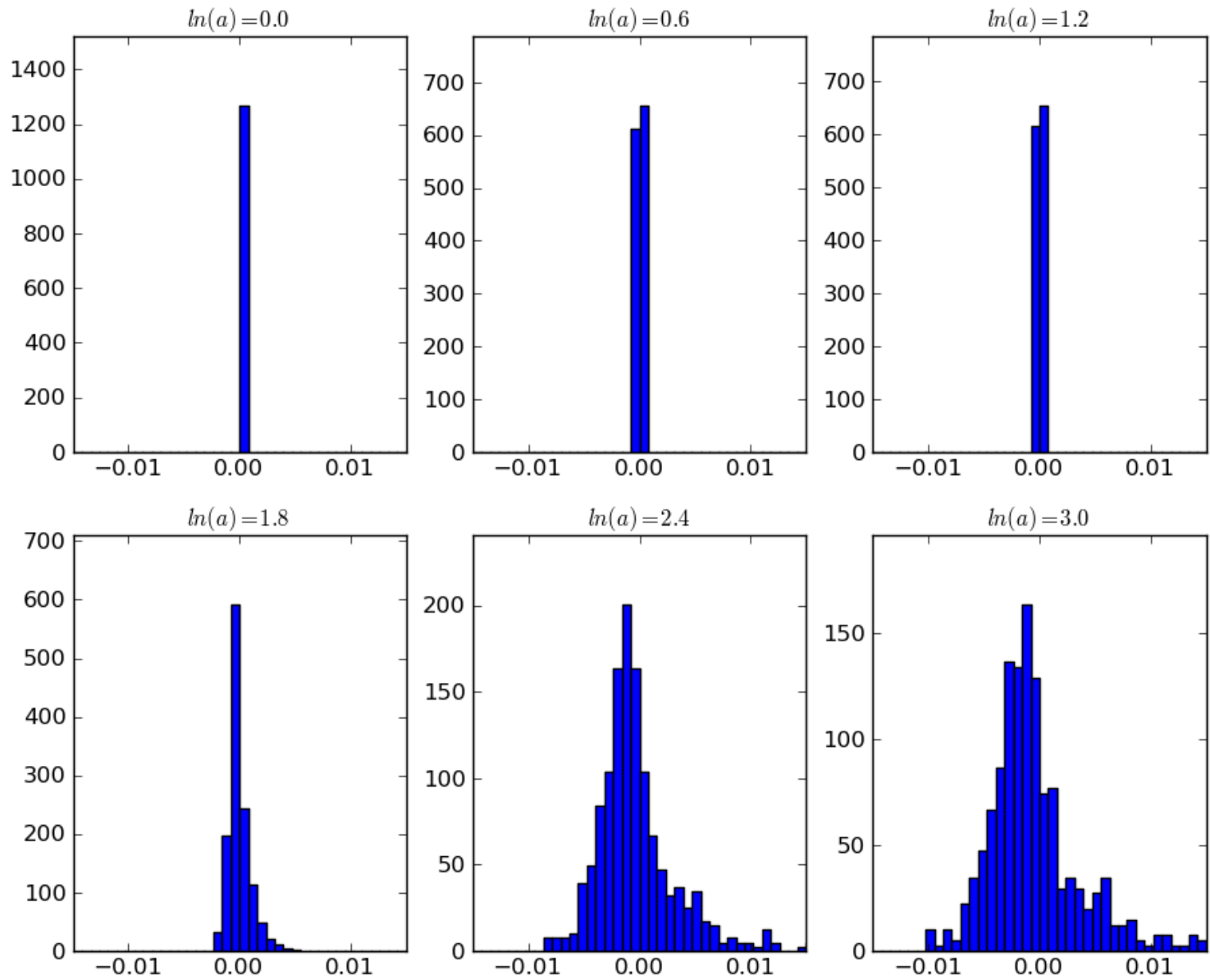




ζ PDF ($\Delta V=0$)

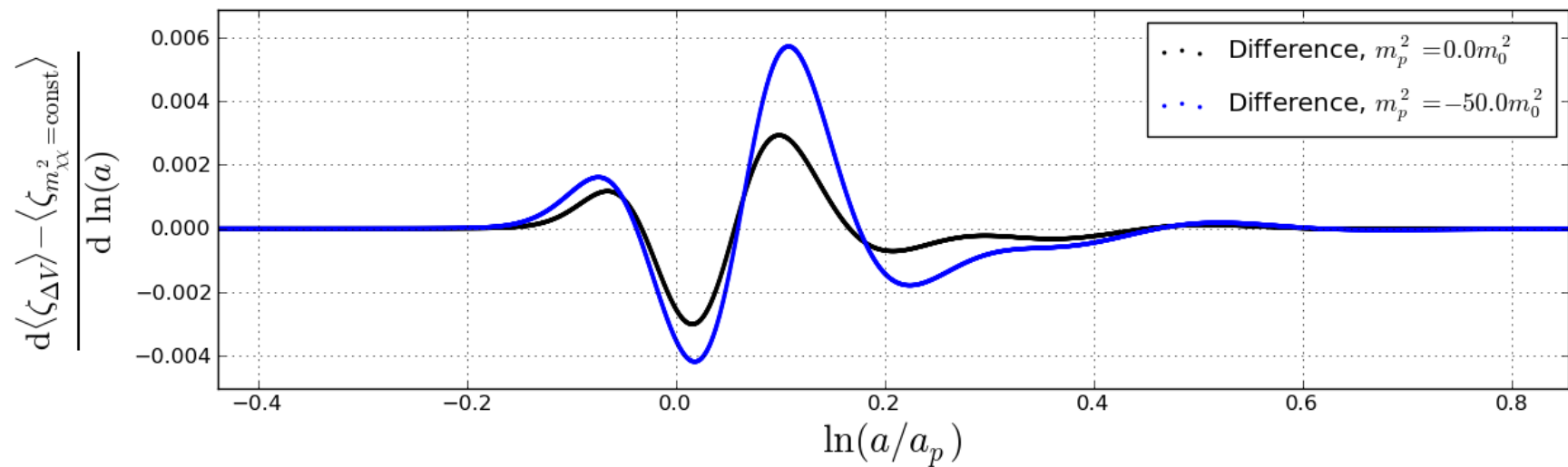
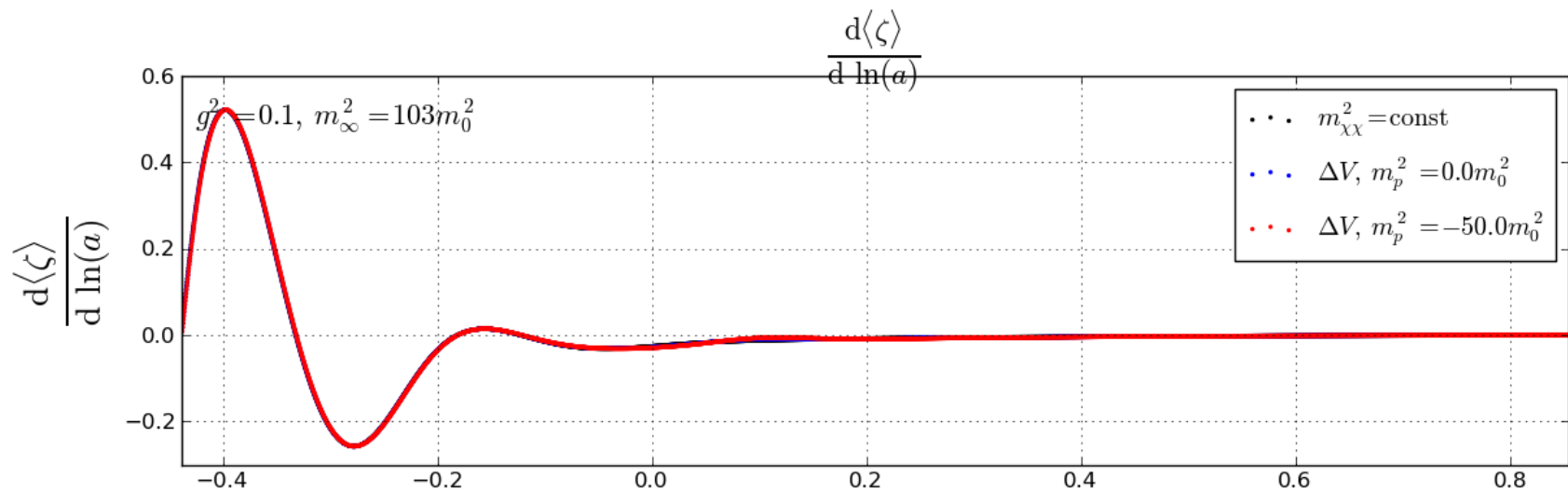


ζ PDF



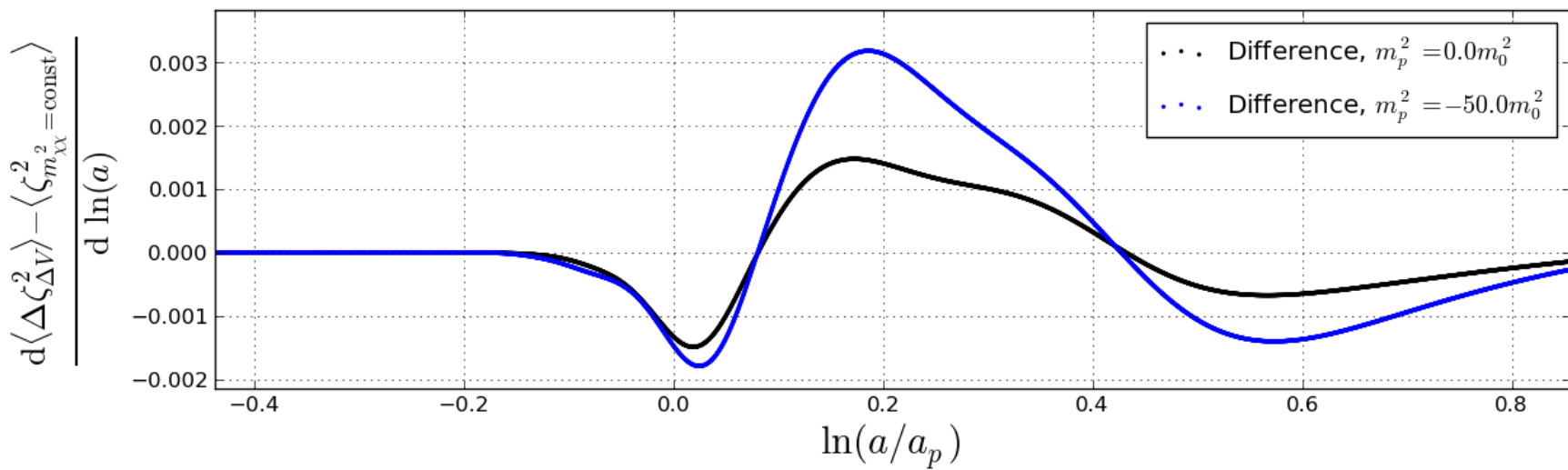
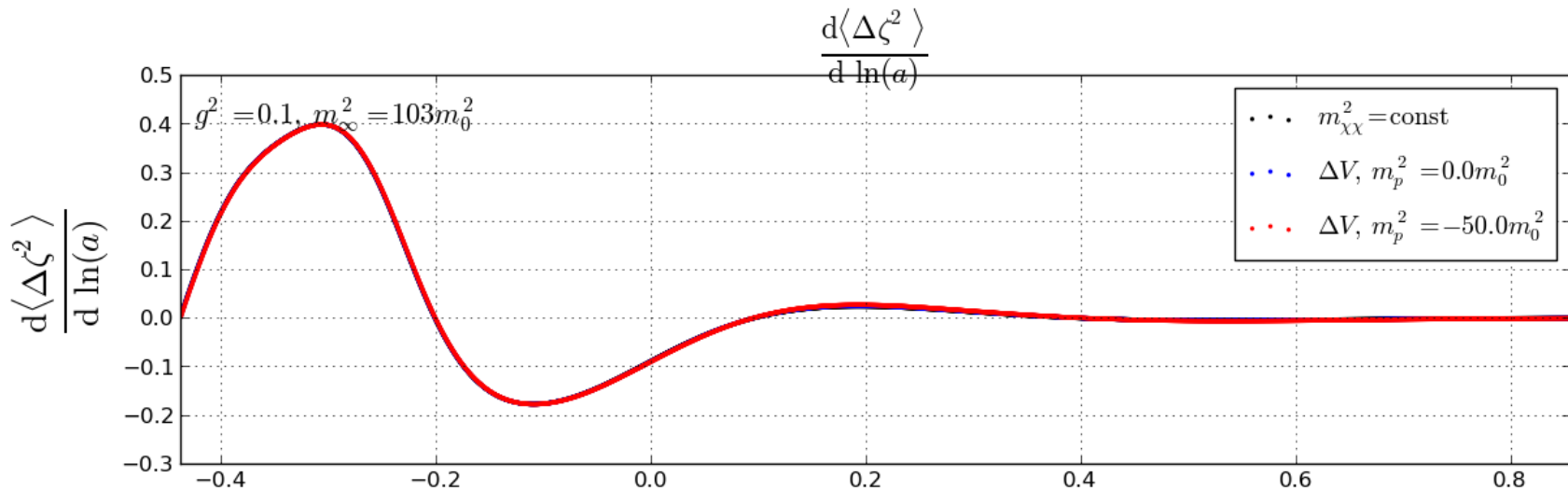
experiment χ -heavy

unstable χ cf. trapped



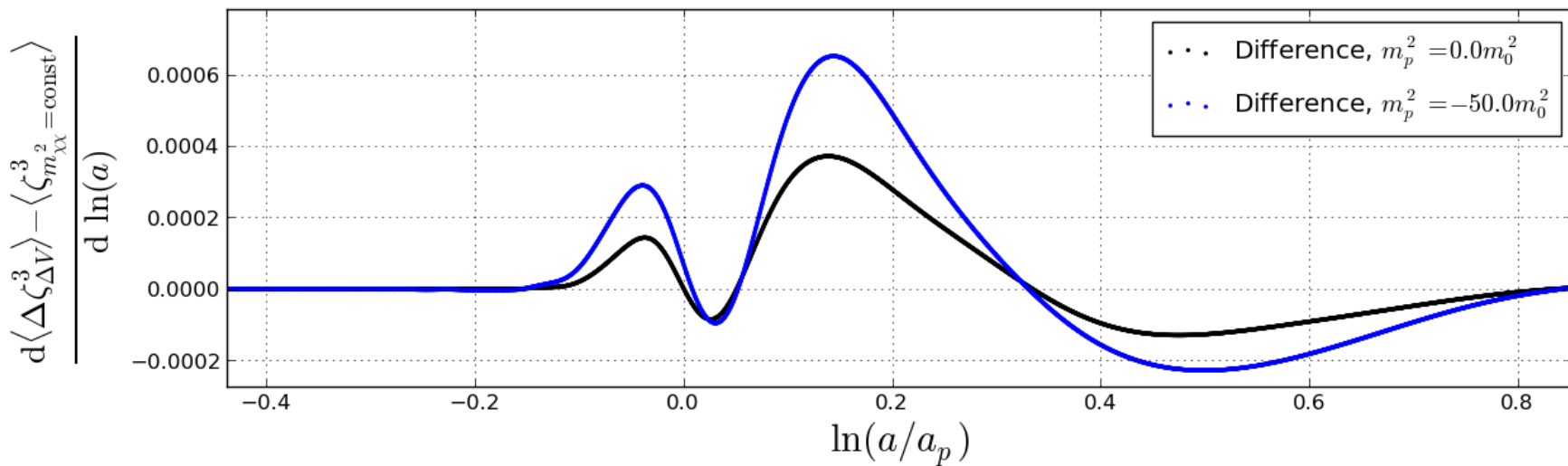
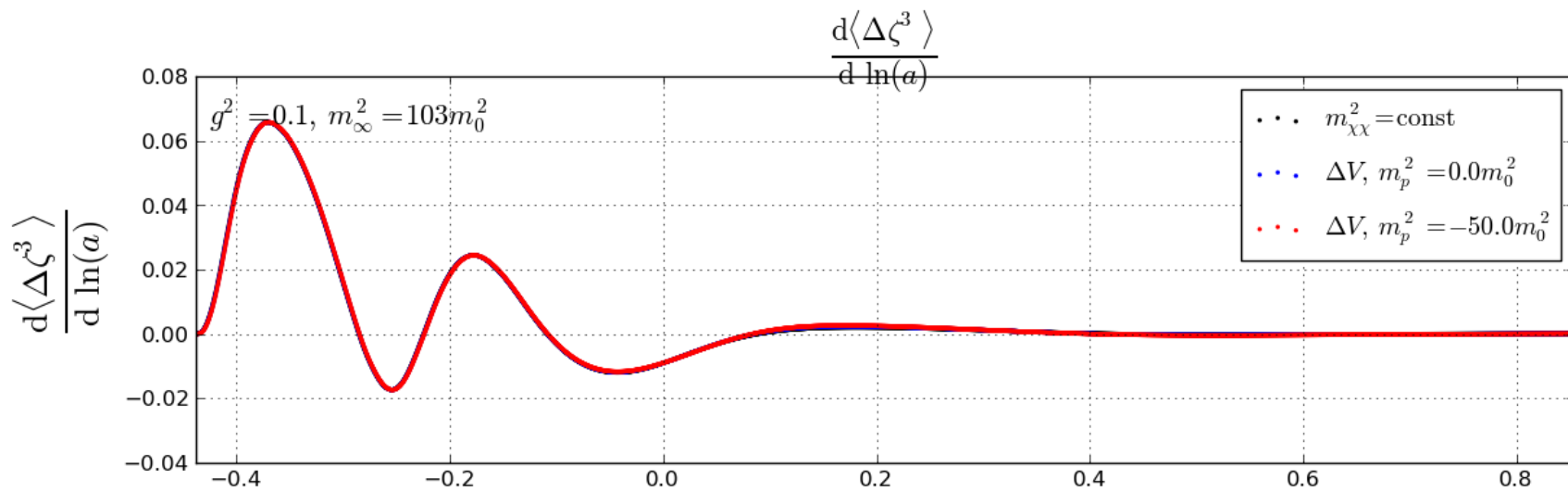
experiment χ -heavy

unstable χ cf. trapped



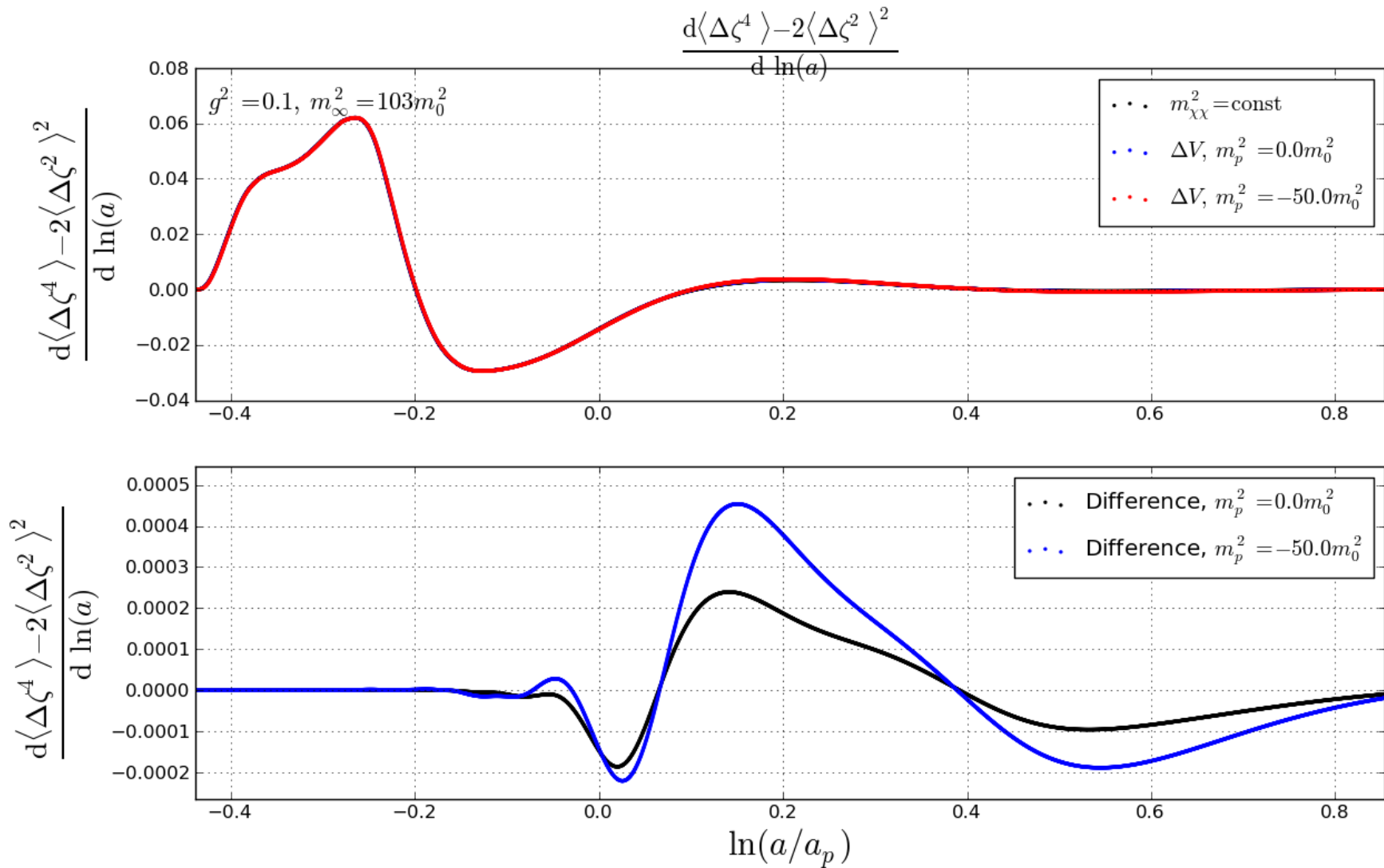
experiment χ -heavy

unstable χ cf. trapped



experiment χ -heavy

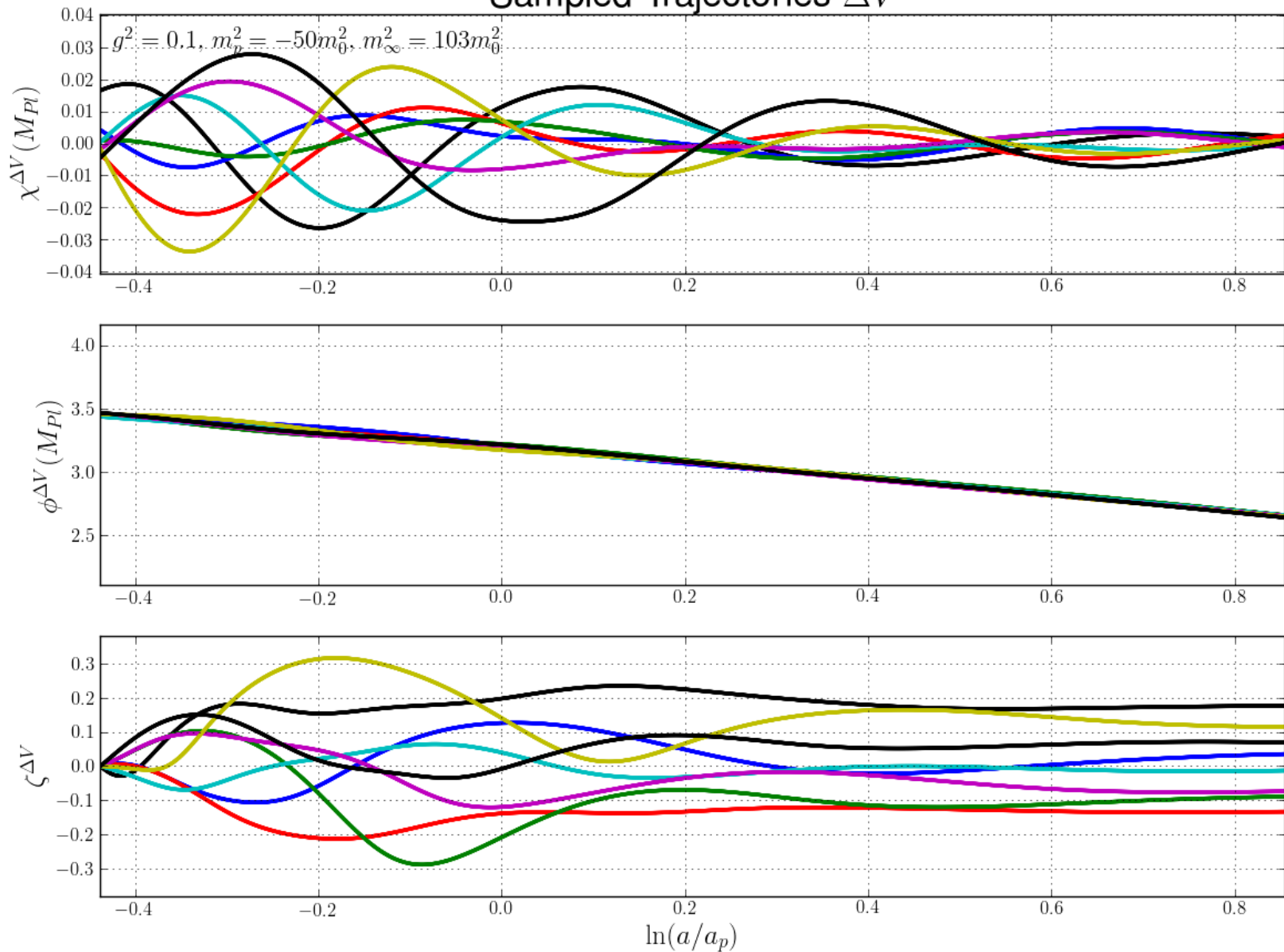
unstable χ cf. trapped



experiment χ -heavy

unstable χ

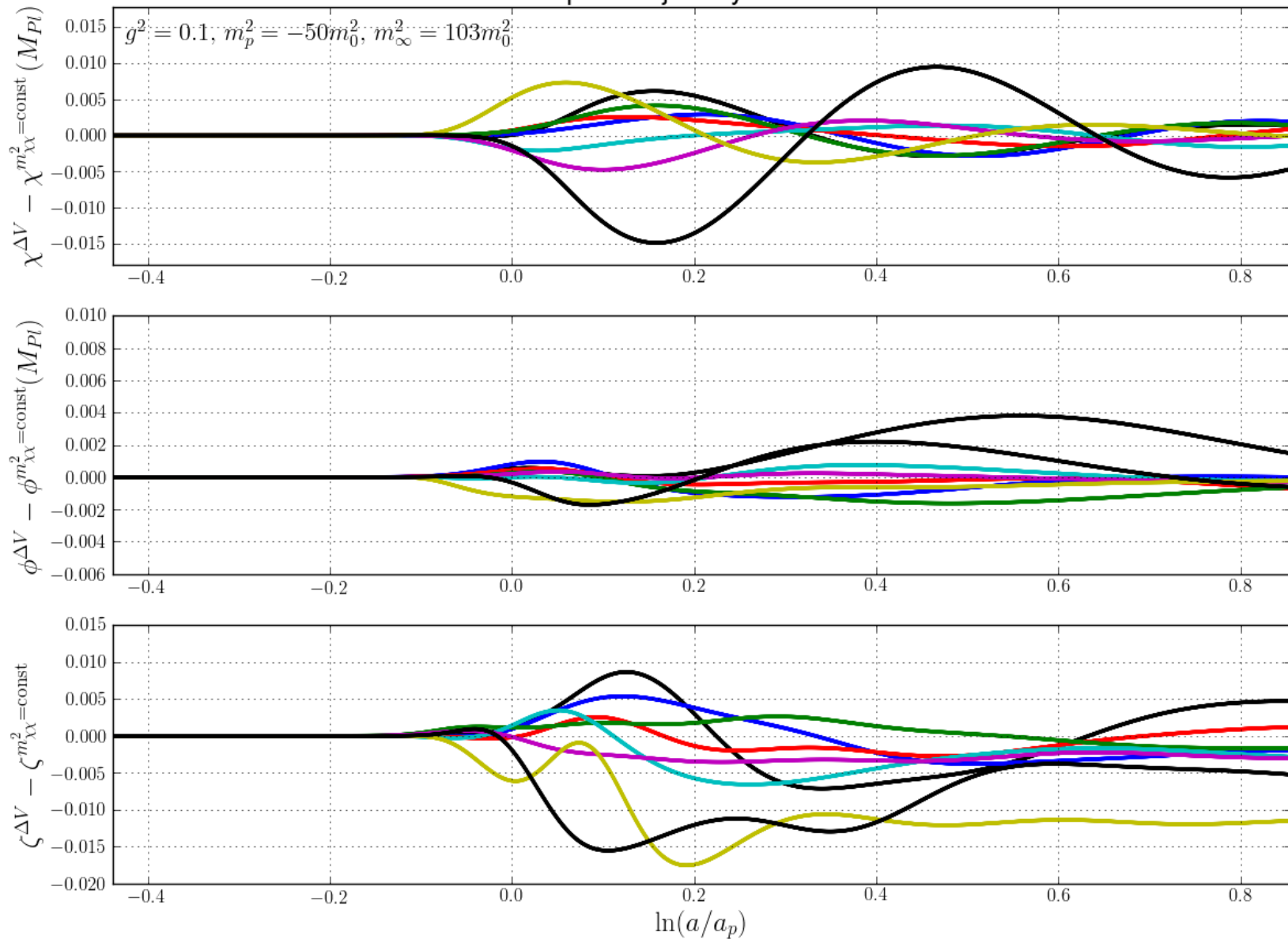
Sampled Trajectories ΔV



experiment χ -heavy

unstable χ

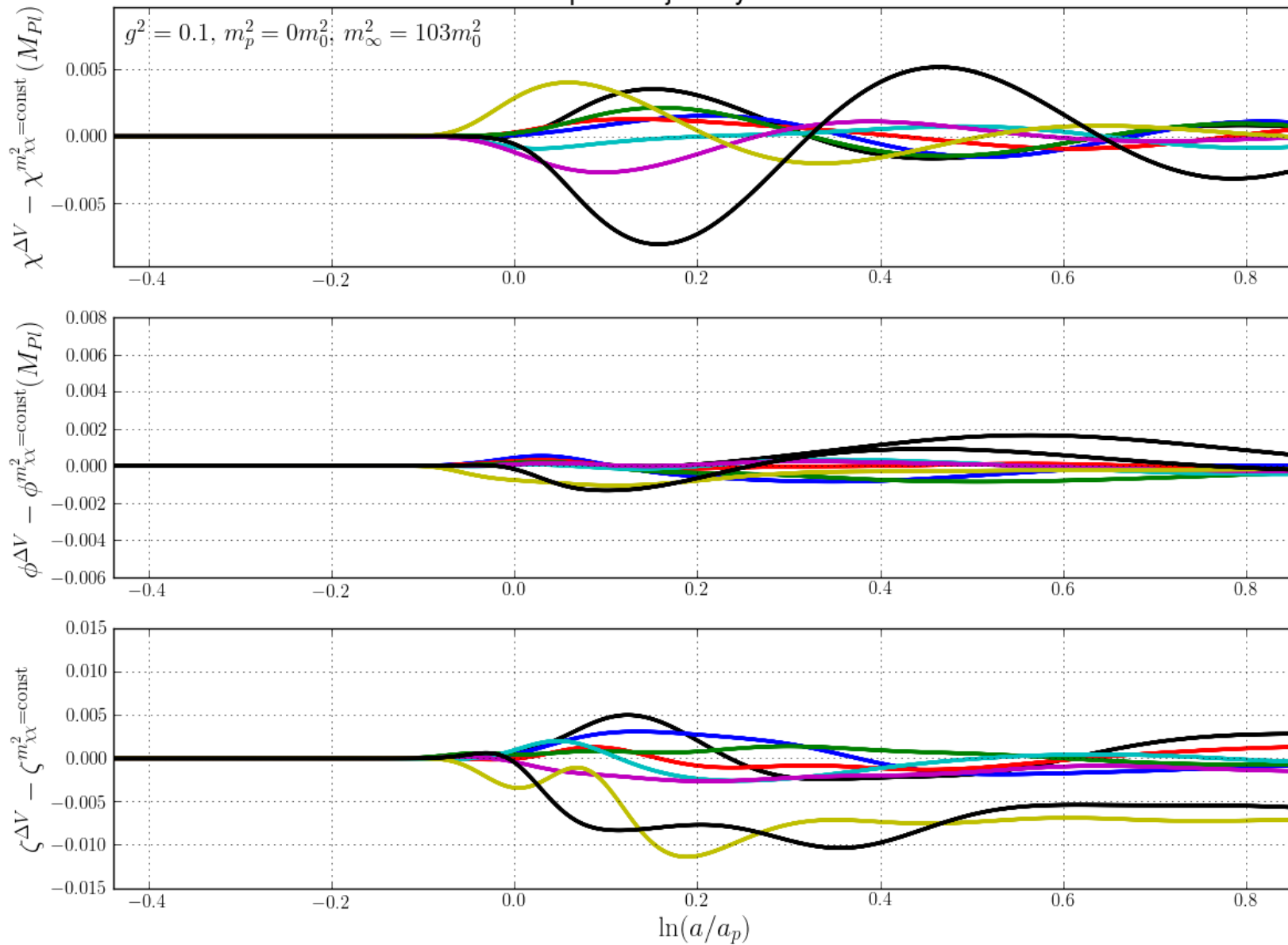
Sampled Trajectory Differences



experiment χ -heavy

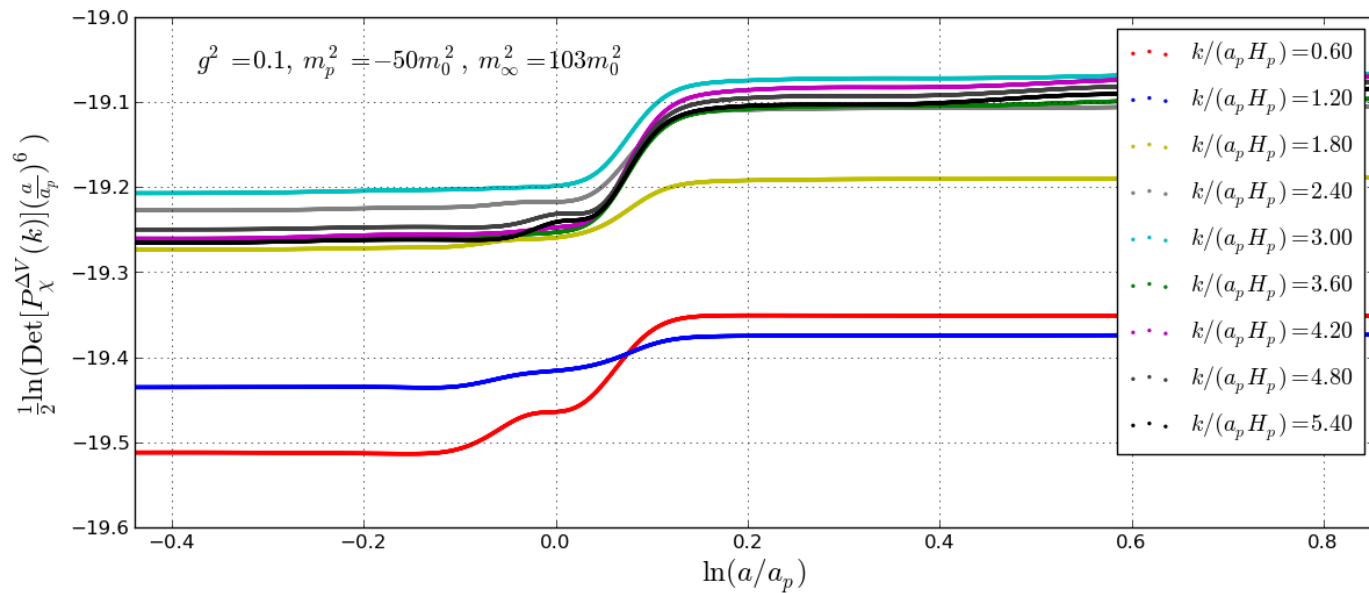
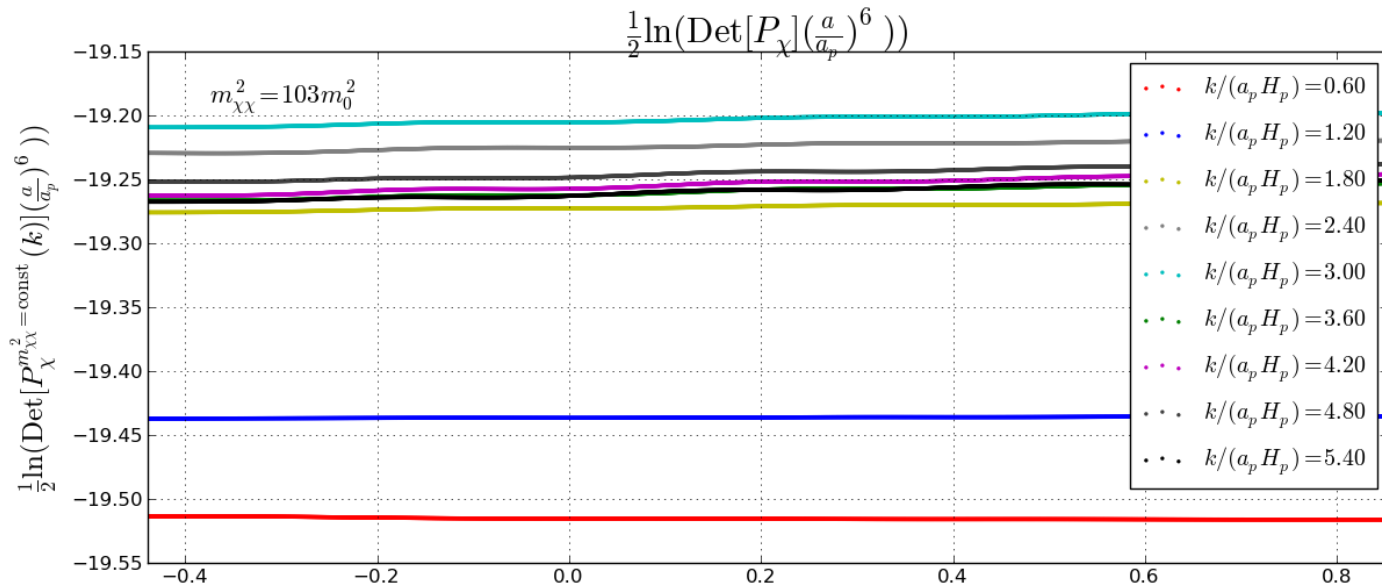
trapped χ

Sampled Trajectory Differences



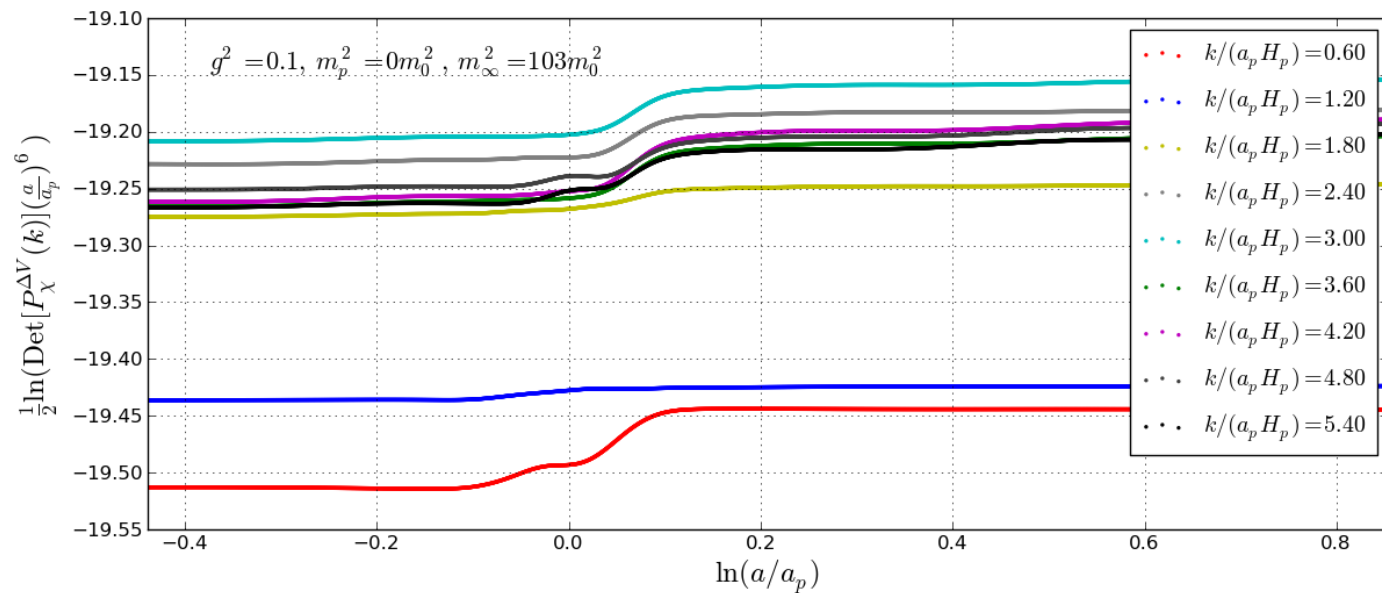
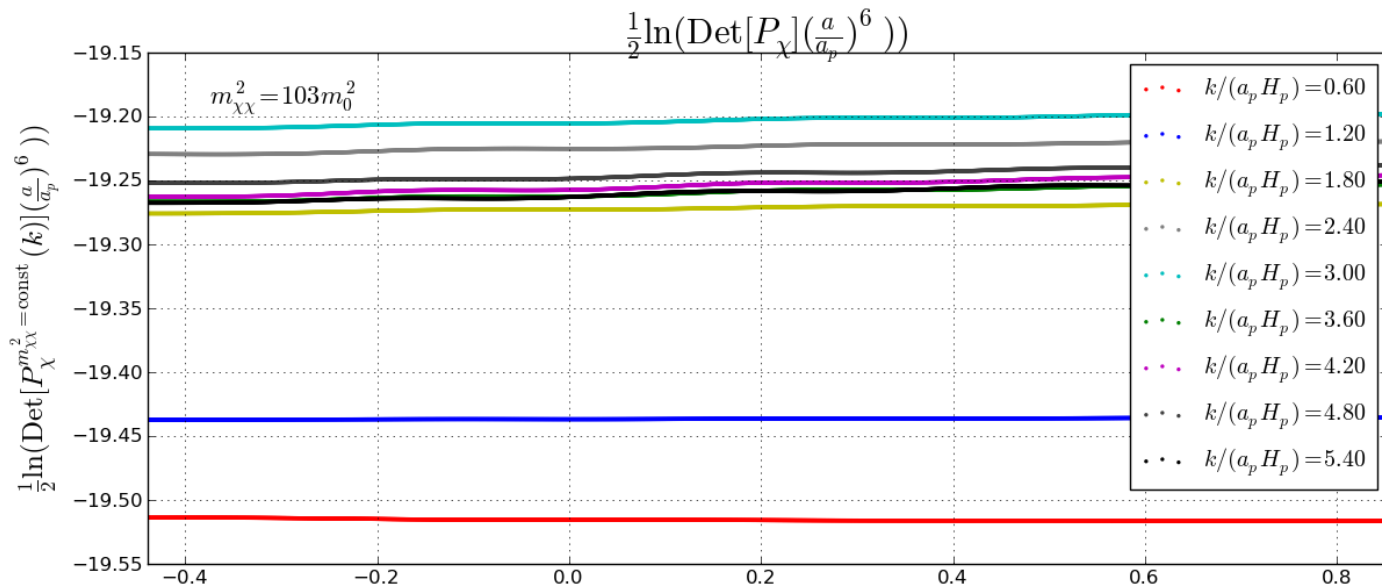
experiment χ -heavy

unstable χ



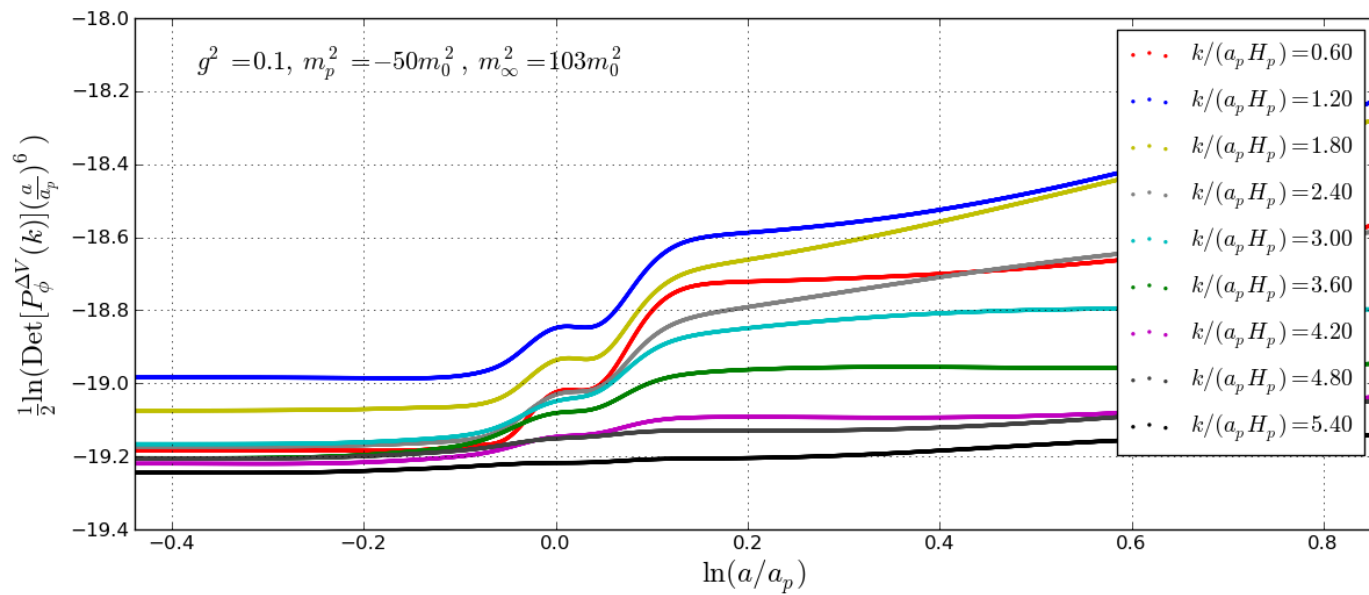
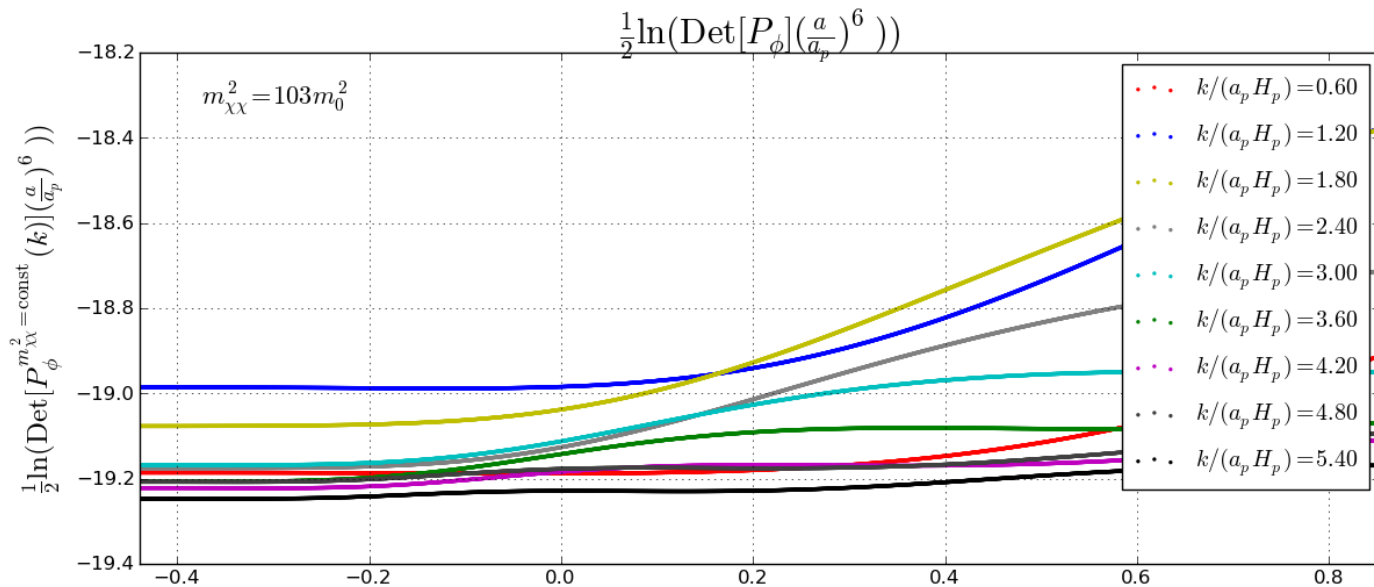
experiment χ -heavy

trapped χ



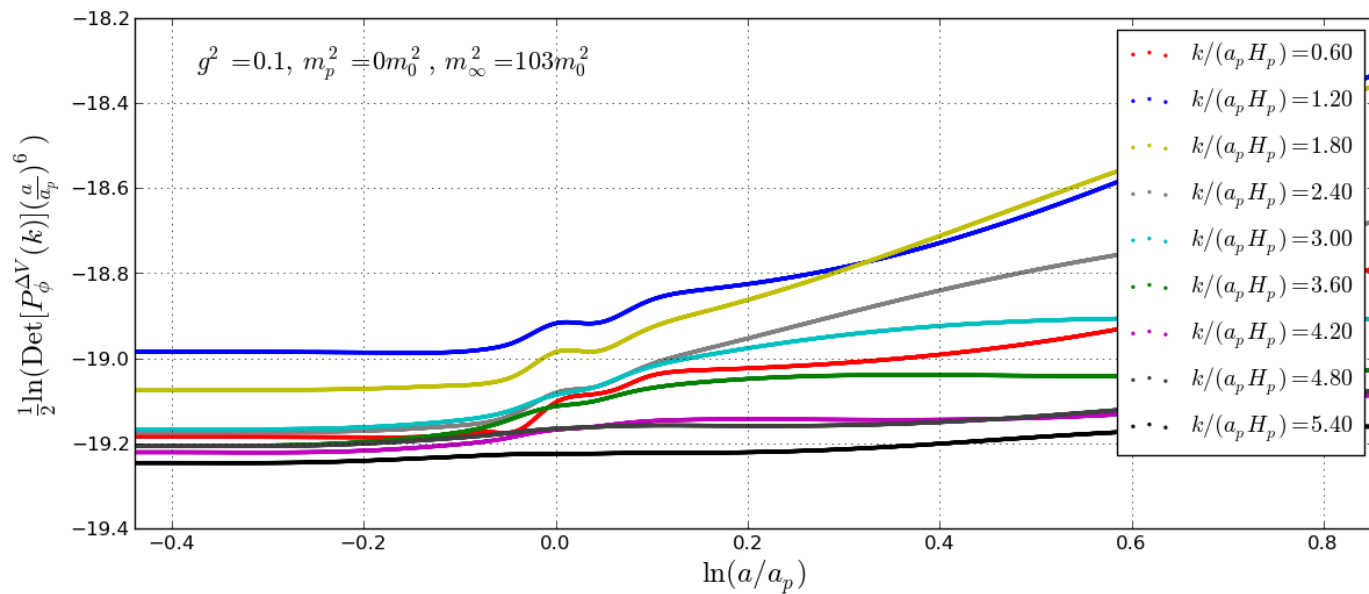
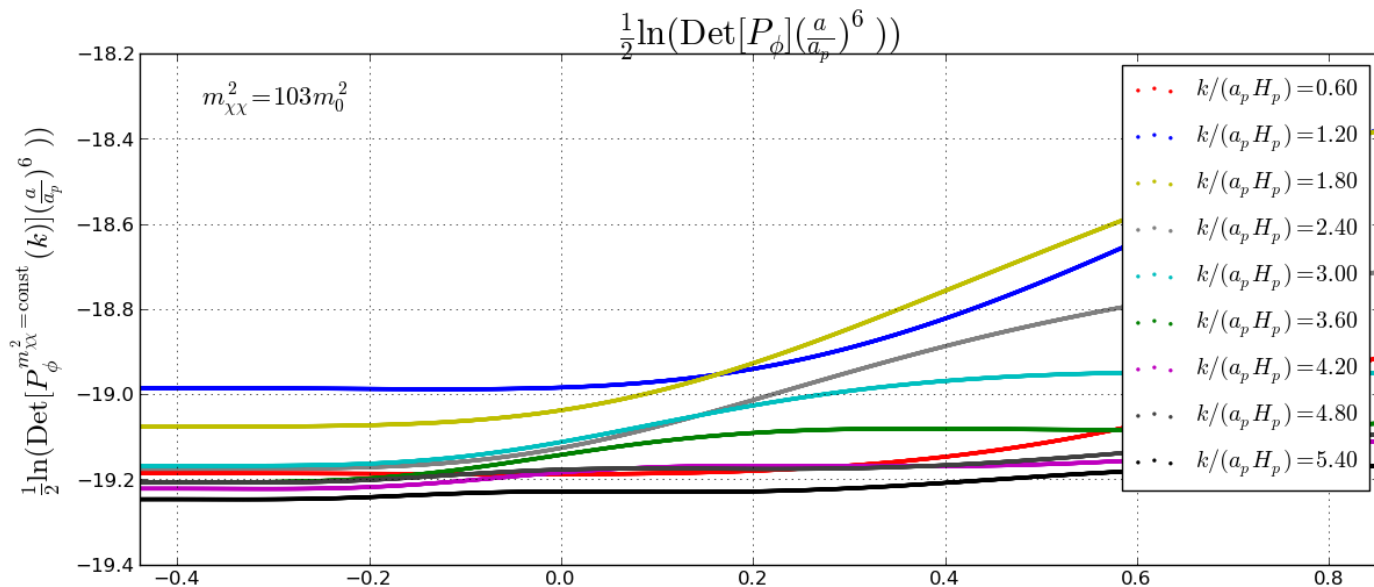
experiment χ -heavy

unstable χ



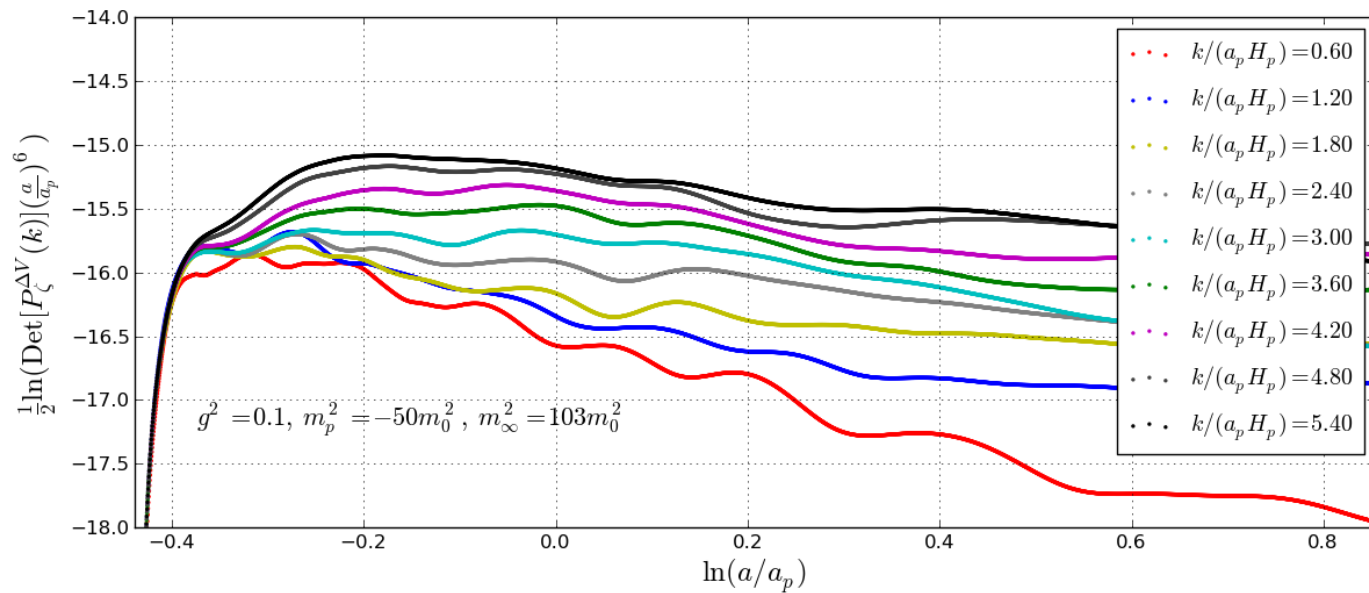
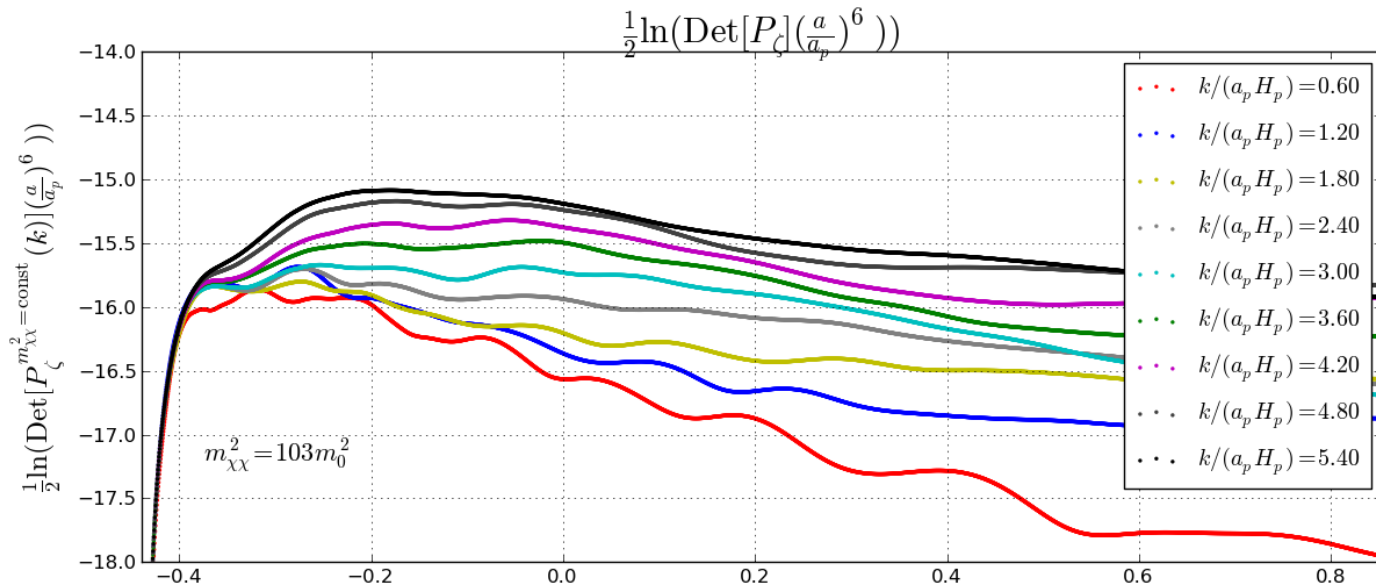
experiment χ -heavy

trapped χ



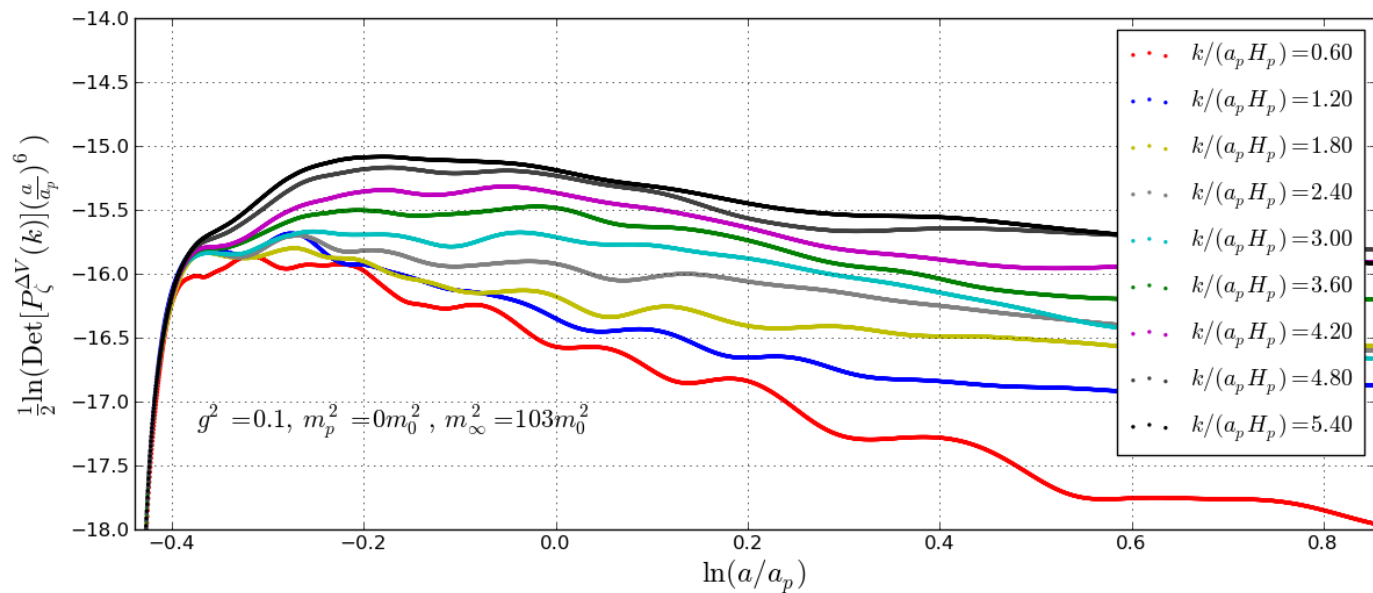
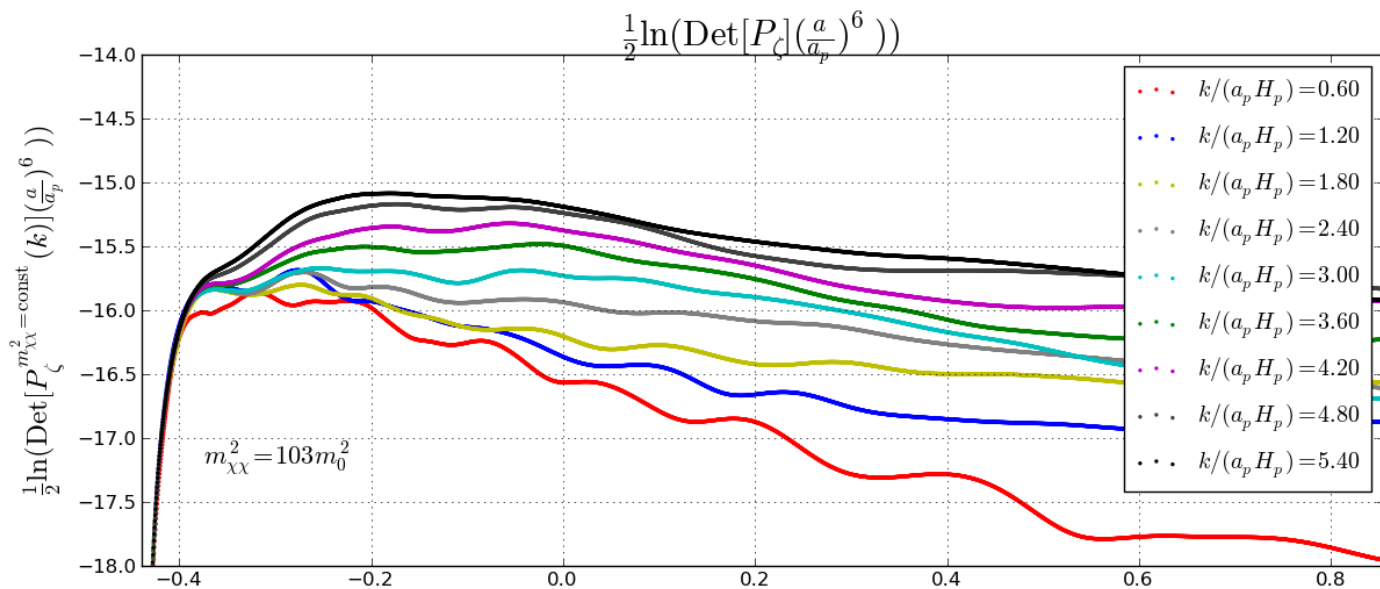
experiment χ -heavy

unstable χ



experiment χ -heavy

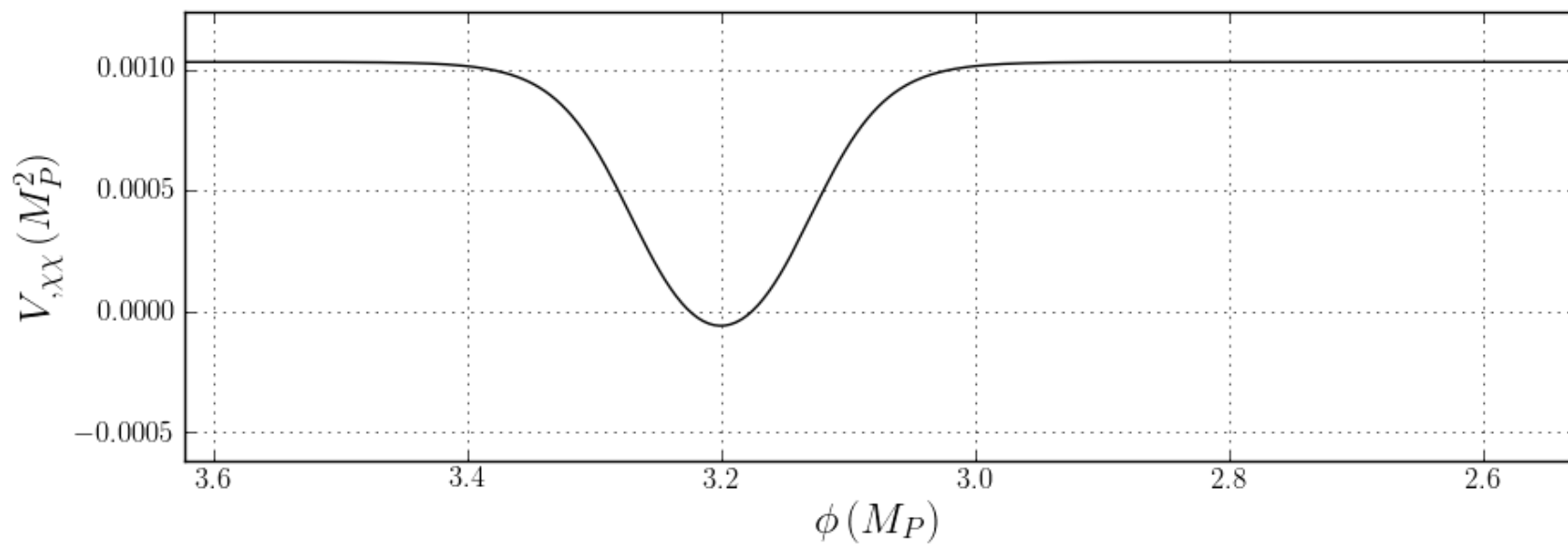
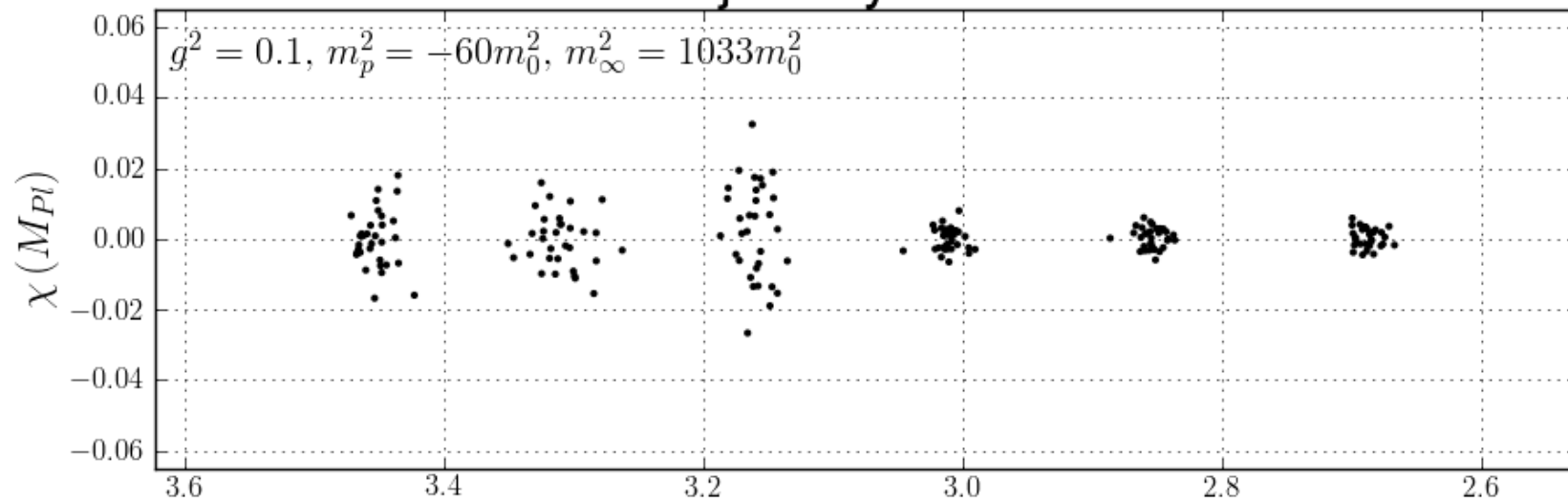
trapped χ



experiment χ -heavy

unstable χ

Trajectory Bundle



(3) $|cg \Leftrightarrow fg\rangle$ condensate/fluctuation framework, for both using coherent states classical-like approach with \hbar . includes **Bogoliubov** transformations for fluctuations as condensate evolves
 \Rightarrow **particle creation** interpretation in both heating and inflating regimes.

condensate/fluctuation framework, classical-like approach with \hbar + Bogoliubov transformations for fluctuations as condensate evolves \Rightarrow particle creation & fluctuation freeze-out into new condensate

stochastic inflation $|\mathbf{q}_c; \mathbf{q}_f\rangle$ instead of $d\mathbf{q}_c^A = \mathbf{V}_c^A dT + \mathbf{K}_v^A \sqrt{dT} \boldsymbol{\eta}^{v(\text{GRD})}$

Langevin network evolution step: $\mathbf{q}_c(\mathbf{X}, T+dT) = \mathbf{q}_c(\mathbf{X}, T) + \mathbf{V}_c dT + \delta\mathbf{q}_f$

cf. **condensate evolution** step $|\mathbf{q}_c(T+dT)\rangle = \exp(\mathbf{V}_c dT) \exp(\delta\mathbf{q}_f) |\mathbf{q}_c(T)\rangle$
schematic $\delta\mathbf{q}_f(\mathbf{x}, T) = \sum_{\mathbf{k}\text{-band}} (\mathbf{Q}_k^*(\mathbf{x}, T) \mathbf{a}_k^\dagger - \mathbf{Q}_k(\mathbf{x}, T) \mathbf{a}_k)$

$$\mathbf{V}_c dT = \mathbf{V}_c(\mathbf{x}, T) dT (\mathbf{a}_x^\dagger - \mathbf{a}_x)$$

annihilation/creation operators in position and momentum $\mathbf{a}_x, \mathbf{a}_x^\dagger, \mathbf{a}_k, \mathbf{a}_k^\dagger$

fluctuating part $|\mathbf{q}_f\rangle \sim \exp(\sum \delta\mathbf{q}_f) |0\rangle$ *a coherent state description?*

what is the relation to the usual $\mathbf{q}_{f,op} = \sum_{\mathbf{k}} (\mathbf{Q}_k^*(\mathbf{x}, T) \mathbf{a}_k^\dagger + \mathbf{Q}_k(\mathbf{x}, T) \mathbf{a}_k)$
operator linear in Bunch Davies vacuum operators $\mathbf{a}_k, \mathbf{a}_k^\dagger$ (sign difference)

it is an **overcomplete basis representation**, **but it conforms to a classical lattice simulation of inflation (no bipartite split).**

still use the gradient expansion for $|\mathbf{q}_c(T)\rangle$

& mixed operators $\mathbf{V}_c dT$ and $\delta\mathbf{q}_f(\mathbf{x}, T)$ - promising approach?



The Kinematics of Inflation, Preheating and Heating: a Playground for Kolmogorov-Sinai and Shannon Entropies

Dick Bond @ ipmu18 11 29

what are the degrees of freedom / parameters of the ultra early Universe? TBD

begin-inflate => inflate => end-inflate => preheat => non-equilibrium heat+entropy
=> *Standard Model particle physics* QG plasma radiation dominated
=> dark matter dominated *structure via gravitational instability* => dark energy now

$$d\zeta(x,t) = (dE+pdV)/3(E+pV) = d \ln \rho_c / 3(1+w) + \text{Trace } d\alpha^i_j$$

fit into a **UV-complete theory** (ultra-high energy to the Planck scale) strings, landscape, ..
& **IR-complete theory** (post-inflation heating -> quark/gluon plasma)???

role of (1) **instabilities after inflation**

entropy generation via the breakup of the coherent low-k inflaton condensate into incoherent high-k fluctuations at a “shock-in-time” => **nonGaussianity**

role of (2) **instabilities during inflation**

phenomenology of in-states propagating through localized unstable potential structures to out-states, like scattering theory => **nonGaussianity**

(3) **|cg <=> fg> condensate/fluctuation framework**, for both

using coherent states classical-like approach with \hbar . includes **Bogoliubov** transformations for fluctuations as condensate evolves

=> **particle creation** interpretation in both heating and inflating regimes.