

Dick Bond @ CIFAR17

all cosmic structure from **entropy!** $\sim \zeta$ 
adiabatic trajectories $+ d_{bar} S$

stochastic “coarse grain” S

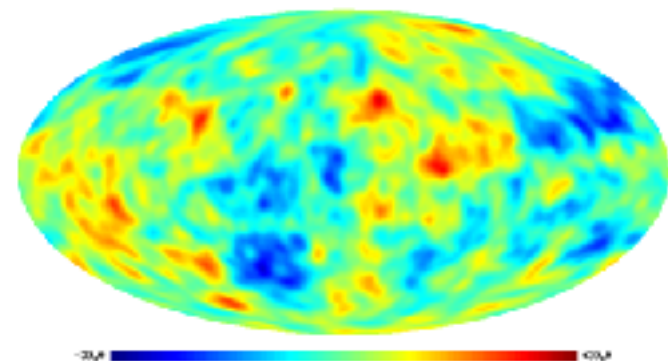
ballistics \Rightarrow caustics

\Rightarrow corrugated shock-in-time

\Rightarrow  **S intermittent nonG**

uncorrelated nonG cf. usual correlated nonG

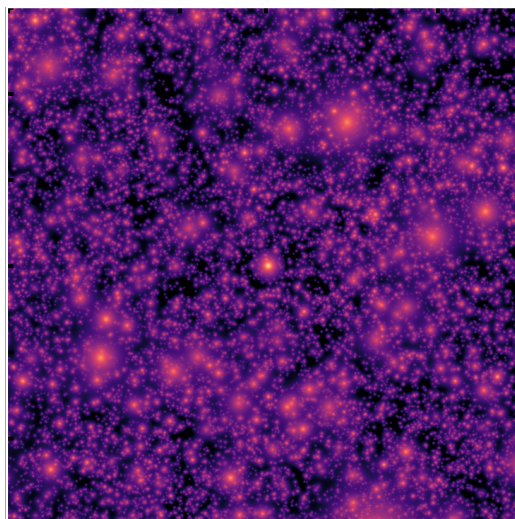
**CMB+LSS: std Gaussian inflaton ζ +
subdominant uncorrelated ζ from
modulated preheating by isocons**



-2σ  2σ

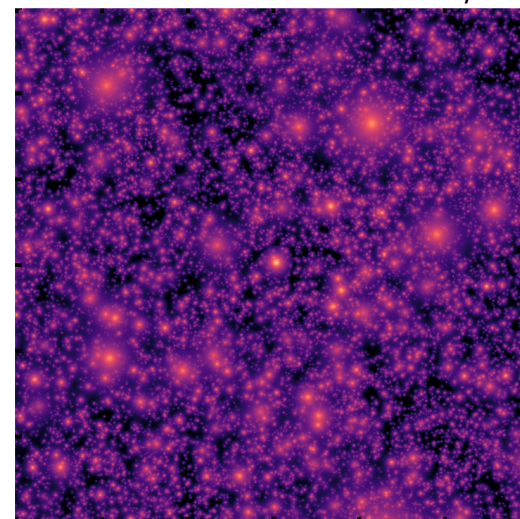
B2FH, b+braden+frolov+huang

LSS tSZ: Gaussian std



ABSB+FH, alvarez+b+stein+frolov+huang

LSS tSZ: Gaussian std +
subdominant uncorrelated ζ



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adiabatic trajectories + dS

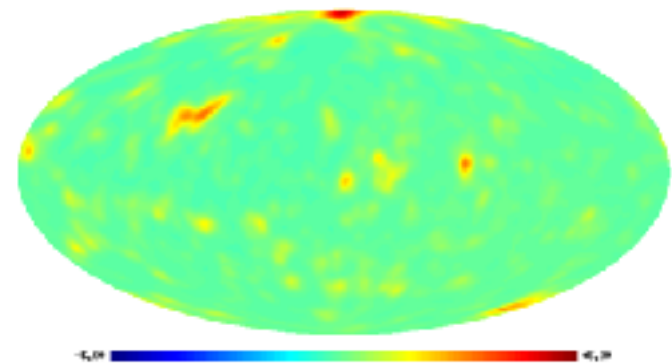
stochastic “coarse grain” S

ballistics \Rightarrow caustics

\Rightarrow corrugated shock-in-time

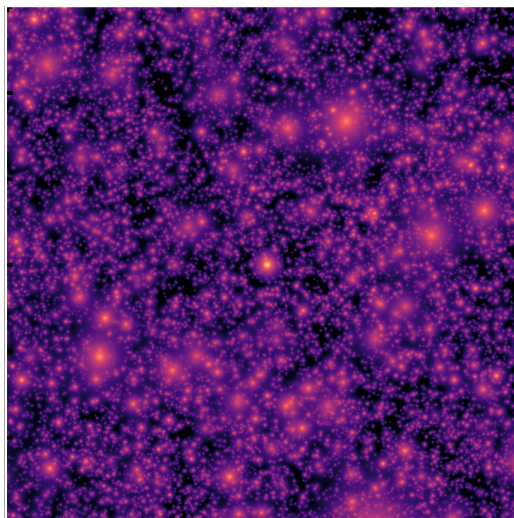
\Rightarrow  **S intermittent nonG**

*CMB+LSS: std Gaussian inflaton ζ +
subdominant uncorrelated ζ
from modulated preheating*



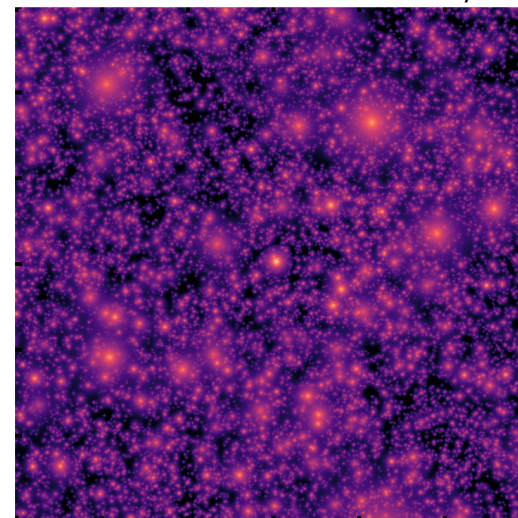
B2FH, b+braden+frolov+huang

LSS tSZ: Gaussian std



ABSB+FH, alvarez+b+stein+frolov+huang

LSS tSZ: Gaussian std +
subdominant uncorrelated ζ



the **Super-WEB** aka the
primordial 3-curvature web aka the
phonon/isotropic strain = volume deformation **web**

$$\ln \rho(\mathbf{x}, t) / \langle \rho \rangle |v \quad \ln V / \langle V \rangle |_{\rho} = 3 \ln \mathbf{a}(\mathbf{x}, t) / \langle a \rangle |_{\rho}$$

$$d\zeta \sim dS \ T/3(E+PV)$$

$$\zeta(\mathbf{x}, t) = \int (dE+pdV) / E \ / \langle 3(1+p/\rho) \rangle (t) \quad \text{BST83, SBB89, SB90,91, B95, Bond+Braden2017 } \zeta \text{ for preheating}$$

$$\zeta(\mathbf{x}, t) = \ln \rho(\mathbf{x}, t) / \langle 3(1+p/\rho) \rangle (t) + \int (1+p/\rho)(\mathbf{x}, t) \ d \ln \mathbf{a}(\mathbf{x}, t) / \langle 1+p/\rho \rangle (t)$$

$$\text{or: } \zeta(\mathbf{x}, t) = \ln \rho(\mathbf{x}, t) / \rho_b / 3(1+p_b/\rho_b) + \ln \mathbf{a}(\mathbf{x}, t) / a_b$$

gradient / Morse flow + *stochastic jitter*, simple Hamilton principle function $S \sim H(\phi_b)$
along coarse-grain trajectories $d\zeta = d \ln \rho / \rho_b / 3(1+p/\rho) + d \ln \mathbf{a} / a_b = [d \bar{\text{bar}} \zeta](fg \rightarrow cg)$
 early preheating: **gradient / Morse flow**, complicated Hamilton principle function **S**
ballistic / caustic phase $\Rightarrow \Delta S$ **nonlinear** ζ lattice sims

cf. late-time density web \sim strain web - $\ln \rho / \langle \rho \rangle = \text{Trace} \ln \mathbf{e}_J^J = \ln V / \langle V \rangle |_{\rho}$
cold $\langle p/\rho \rangle \sim 0 \Rightarrow \zeta(\mathbf{x}, t | cdm)$ conserved before shell crossing (³preheating)

quadratic map of the ζ -scape

(radical) **compression** in quadratic space, using Planck likelihood rather than linear Wiener compression ($\langle \zeta | \text{Temp}, E \text{ pol} \rangle + \delta\zeta$) maps, e.g., onto 12 bands in k -space (LM projection) Planck15 inflation B+Huang 13-15-17.. => fully includes lensing & BB from BKP & cosmic param marginalization

the exploration of the $L=20-30$ anomaly will improve in Planck2017
 + BICEP/KECK2017 + Spider 201x, $x=7$
 lower tau helps a bit
 + highL AdvACTPol

uniform $n_s=0.968$
 P15+LSS best fit

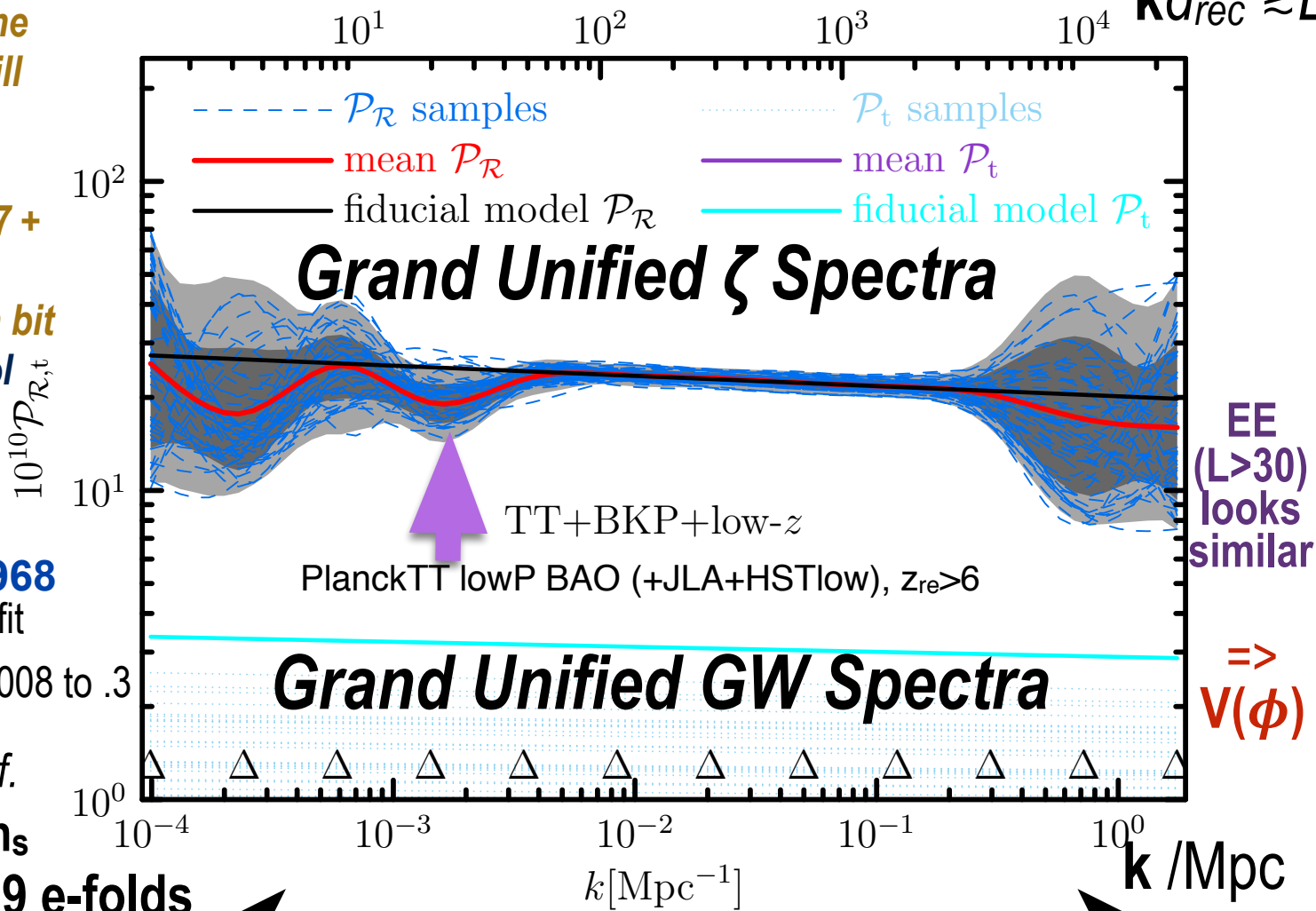
superb 12-knot fit $k \sim .008$ to $.3$

$r < .11$ 95%CL cf.
 $r < 0.09$ uniform n_s

9 e-folds

$$\ell_k \equiv k D_{\text{rec}}$$

$$k d_{\text{rec}} \gtrsim L$$



Grand Unified ζ Spectra

Grand Unified GW Spectra

EE
 ($L > 30$)
 looks
 similar

=>
 $V(\phi)$

$k [\text{Mpc}^{-1}]$

k / Mpc

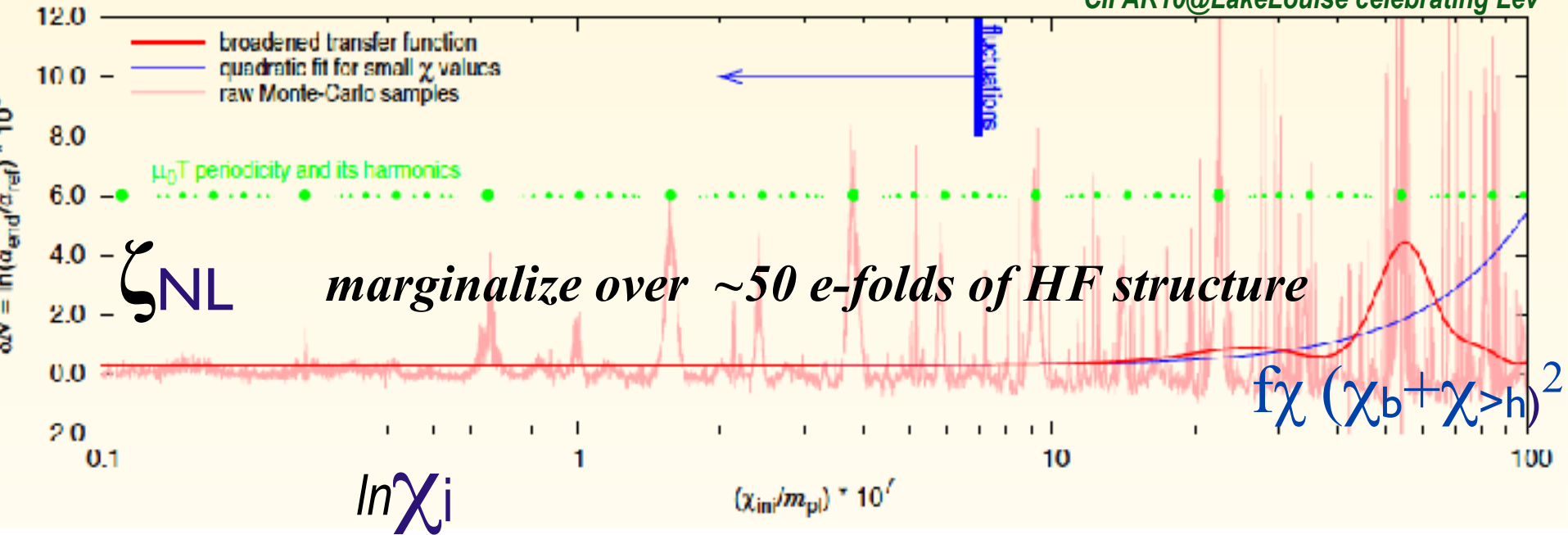
Local nonG: correlated quadratic $\zeta(\mathbf{x}) = \zeta_G(\mathbf{x}) + \mathbf{f}_{NL} \zeta_G^2(\mathbf{x})$

Chaotic Billiards: NonG from Parametric Resonance in Preheating

B+Frolov, Huang, Kofman 09
B+Braden, Frolov, Huang 17

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

CIFAR10@LakeLouise celebrating Lev

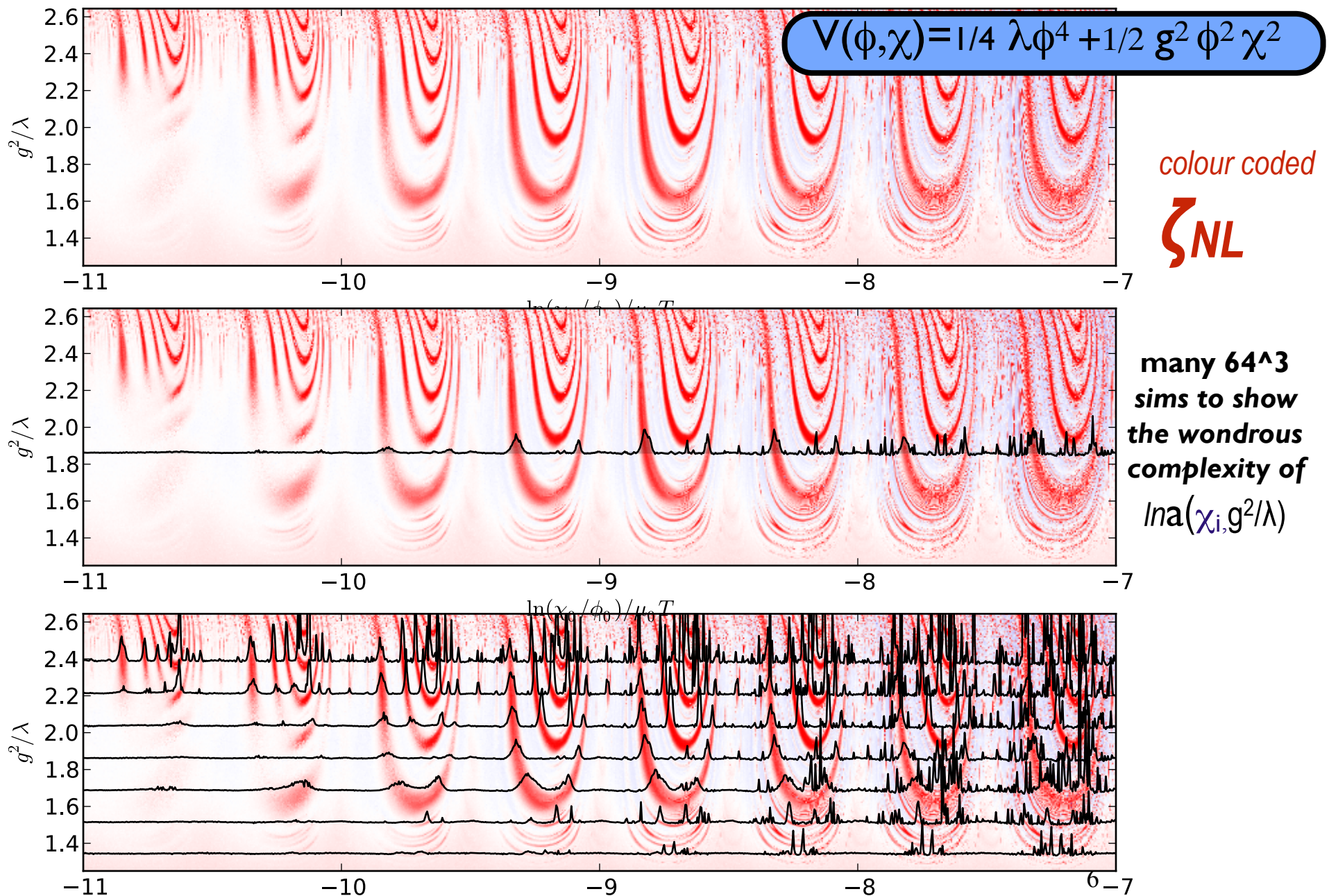


$$\langle \zeta_{NL} | \chi_b + \chi_{>h} \rangle \sim \beta(\chi_{>h}) \chi_b + \mathbf{f}(\chi_{>h}) \chi_b^2 + \dots$$

$$\mathbf{f}_{NL}^{\text{equiv}} = \beta^2 \mathbf{f}_{\chi} [P_{\chi}/P_{\phi}]^2(k_{\text{pivot}})$$

\Rightarrow constrain $\mathbf{f}_{\chi}^3 \chi_{>h}^2$ ($P_{\chi}/P_{\phi} \sim 2\epsilon \Rightarrow$ very relaxed limit)

nonG 3-pt f_{nl} : 0.8 ± 5.0 local for Φ_N
 $\Rightarrow f_{NL}^* = -0.52 \pm 3.0$ for ζ phonons



nonlinearly-arrested caustic structure of ballistic $k=0$ trajectories

$k \sim 0$ “ballistic” trajectories

become **entangled** *with*

non-zero **k-modes** *in a coarse-grained*

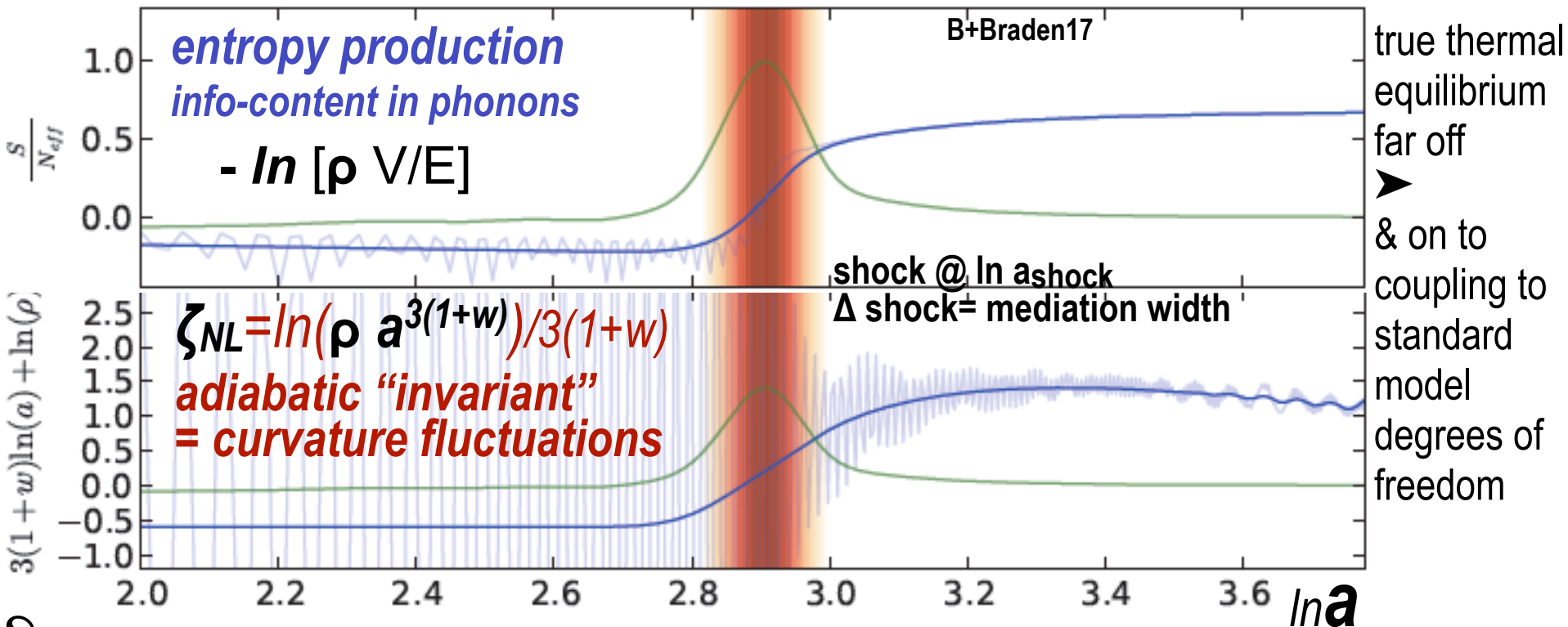
non-equilibrium **entropy** *generating*

shock-in-time

whence to the **StdModel-pp**

- $\ln [\rho V/E]$ & $\zeta_{NL} = \ln(\rho a^{3(1+w)})/3(1+w)$ are nearly Gaussian within a preheating horizon (\sim cm) shown by BB lattice sims for pdf in k-bands, smallness of the 3 pt, etc. (!!!)

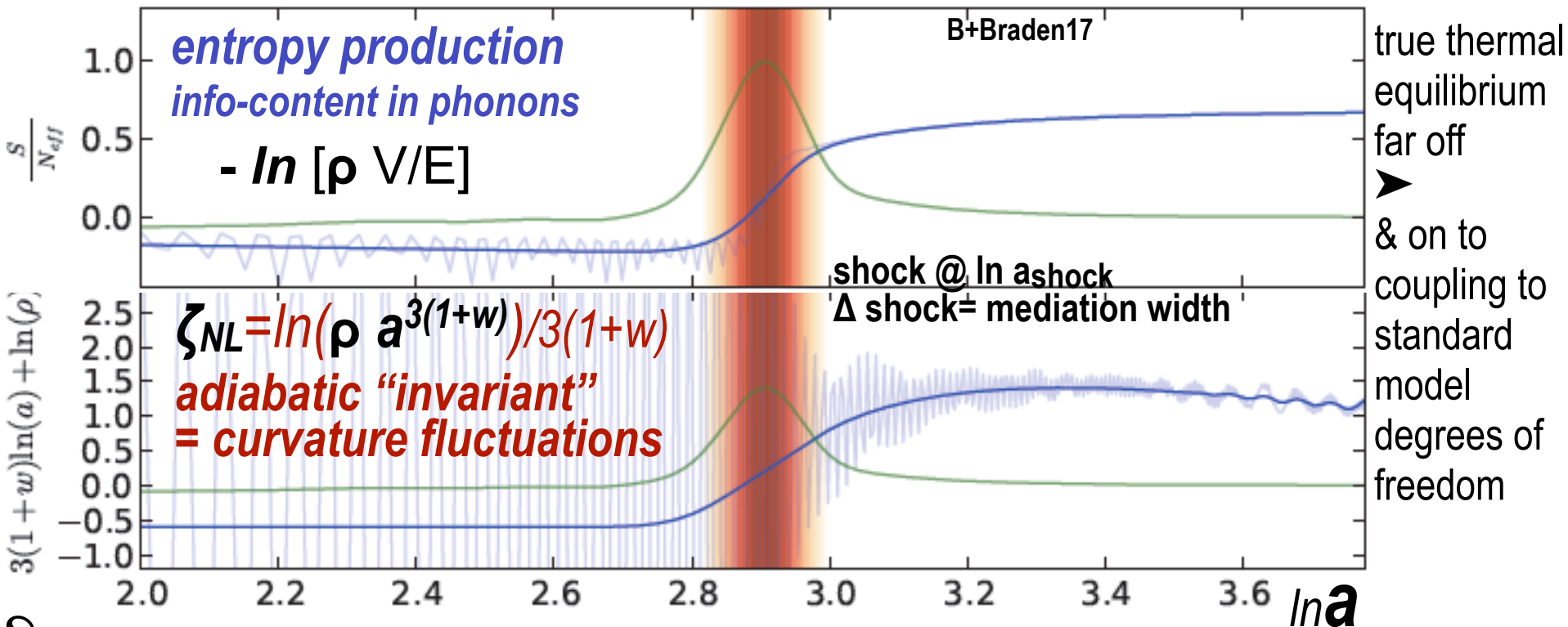
nonG from large-scale modulations of the shock-in-times of preheating



$$\delta \zeta_{NL\text{shock}}(\text{tf} | \chi_i(\mathbf{x}), g^2/\lambda)$$

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

nonG from large-scale modulations of the shock-in-times of preheating



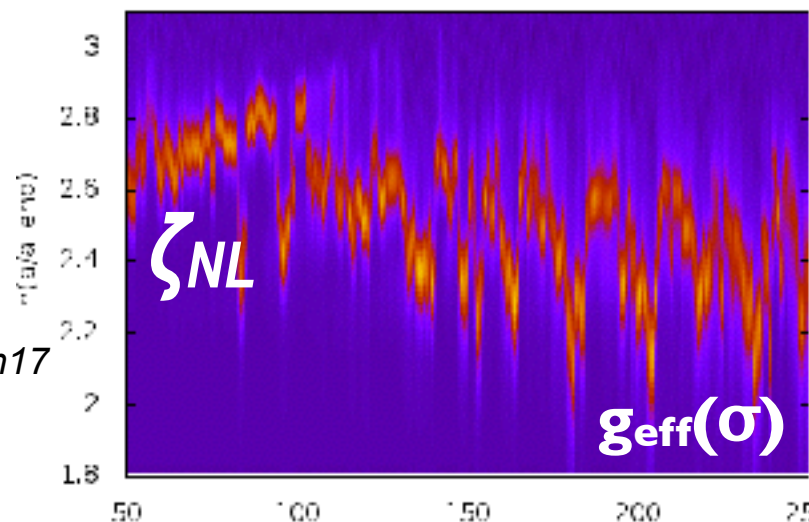
$$\delta \zeta_{NLshock}(tf | \chi_i(\mathbf{x}), g^2/\lambda)$$

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

$$\delta \zeta_{NLshock}(tf | \mathbf{g}(\sigma(\mathbf{x})) \Rightarrow \text{modulated}$$

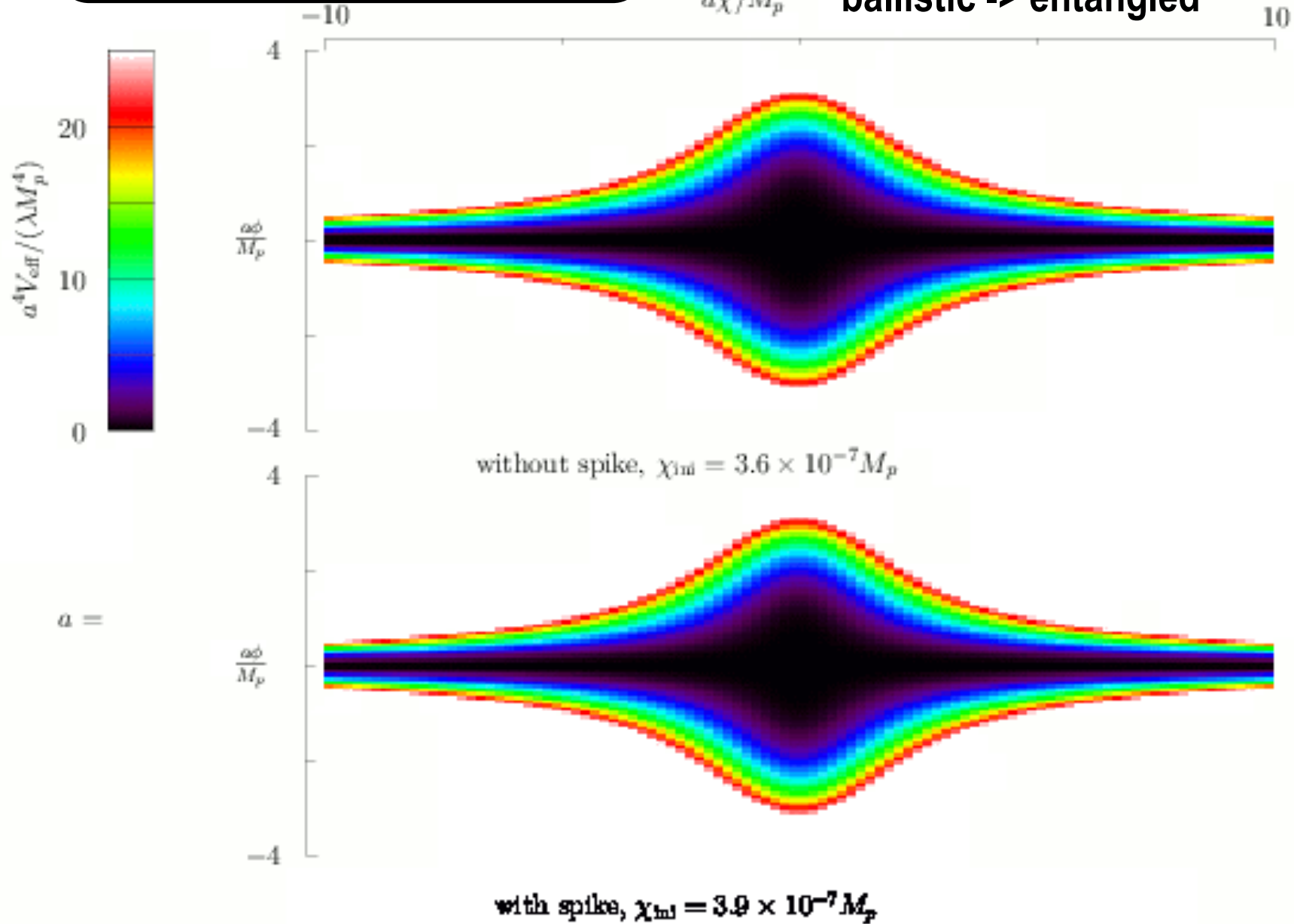
$$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g_{eff}(\sigma)^2 \phi^2 \chi^2 \quad \text{Bond, Braden17}$$

$$g_0 + g_1 \sigma/M_P, g_0 \exp[\gamma_1 \sigma/M_P], ..$$



$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

full lattice simulations of $k \sim 0$ trajectories (χ_i)
 ballistic \rightarrow entangled



(nonlinear) V_{eff} is trajectory-bundle dependent

caustics in ballistic orbits

$$\langle \delta q^A t_2 \mid \delta q^B t_1 \rangle \sim \exp(\mathcal{E}(t_2 \mid t_1)) \langle \delta q^A t_1 \mid \delta q^B t_1 \rangle$$

early U parameters: final $\ln a$, $\ln \rho$, ϕ , χ , Π_ϕ , Π_χ , initial χ_i , couplings g , λ , ..

parameter strain tensor $\mathcal{E}(t_2 \mid t_1)$

$d\mathcal{E}/dt$ strain rate \sim local Lyapunov coefficients *Floquet instability charts*

instability to have nearby parameters diverge \Rightarrow chaotic billiards

small \mathcal{E} eigenvalues \Rightarrow coherent trajectory bundles (for a time) =

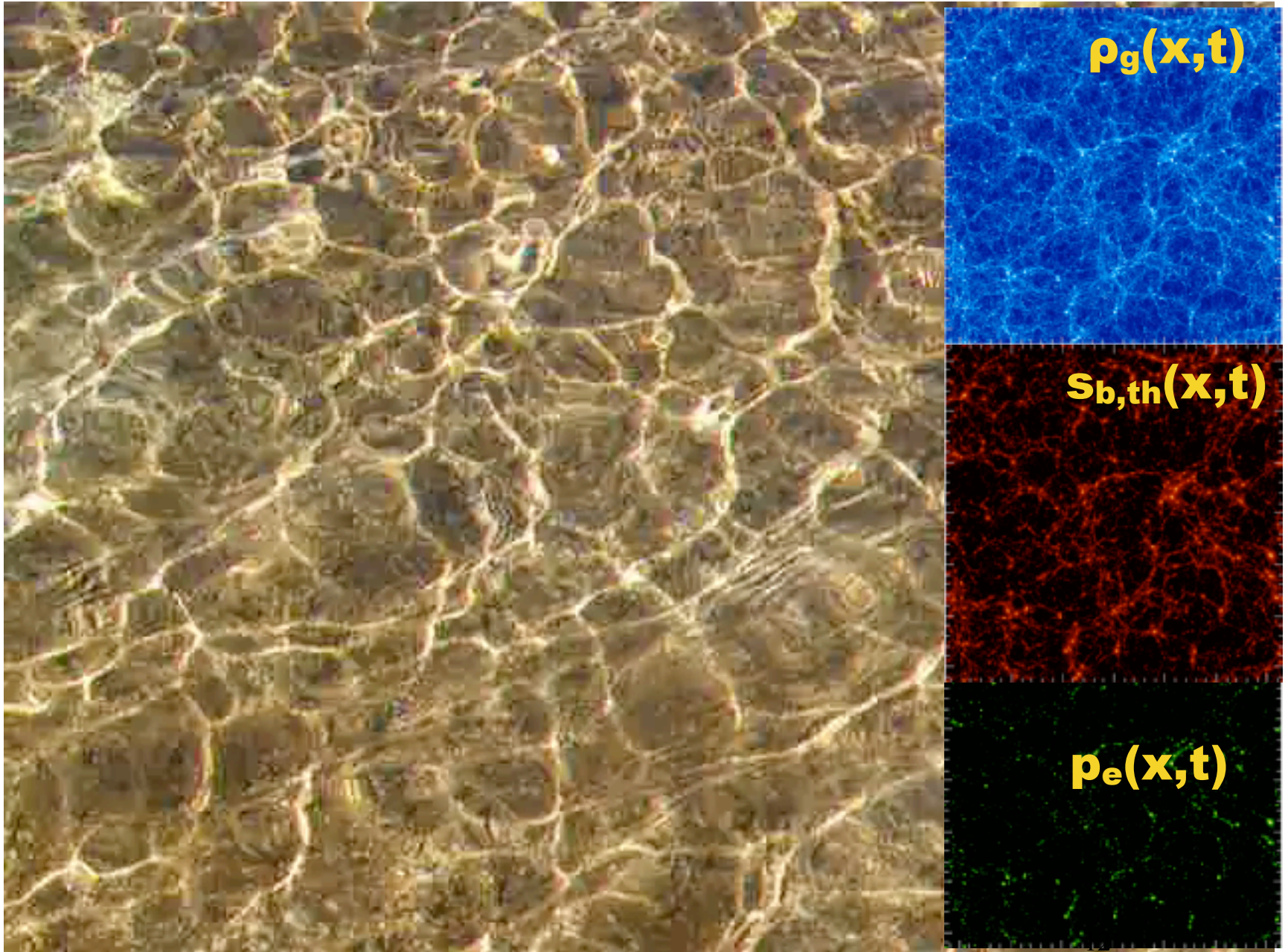
caustics (inverse $\rightarrow \infty$) $1/[\partial \ln a / \partial \chi_i(\mathbf{x})]$; caustics \Rightarrow peaks in $\ln a(\chi_i)$

stopping time $t_{\text{stop}}(\chi_i)$ when \mathcal{E} values get large \Leftrightarrow local gradients \uparrow

cf. LSS parameters: final Eulerian position \Leftarrow initial Lagrangian position

1LPT aka Zeldovich: $\partial x / \partial r = \exp(\mathcal{E}) \rightarrow 0$ density $\rho \sim \exp(-\text{Tr}(\mathcal{E})) \rightarrow \infty$

caustics are ubiquitous: **LSS/cosmic web & preheating**



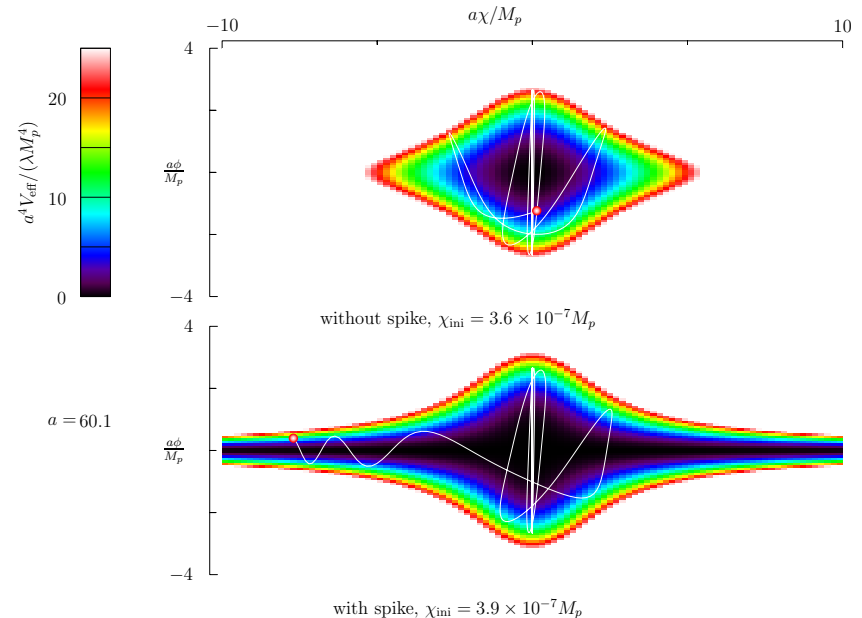
understanding the ζ -spike structure, B^2FH 17

qualitatively YES and quantitatively MAYBE

arresting the orbits via a shock-in-time, incoherent cf. coherent (caustic) trajectory bundles

incoherent

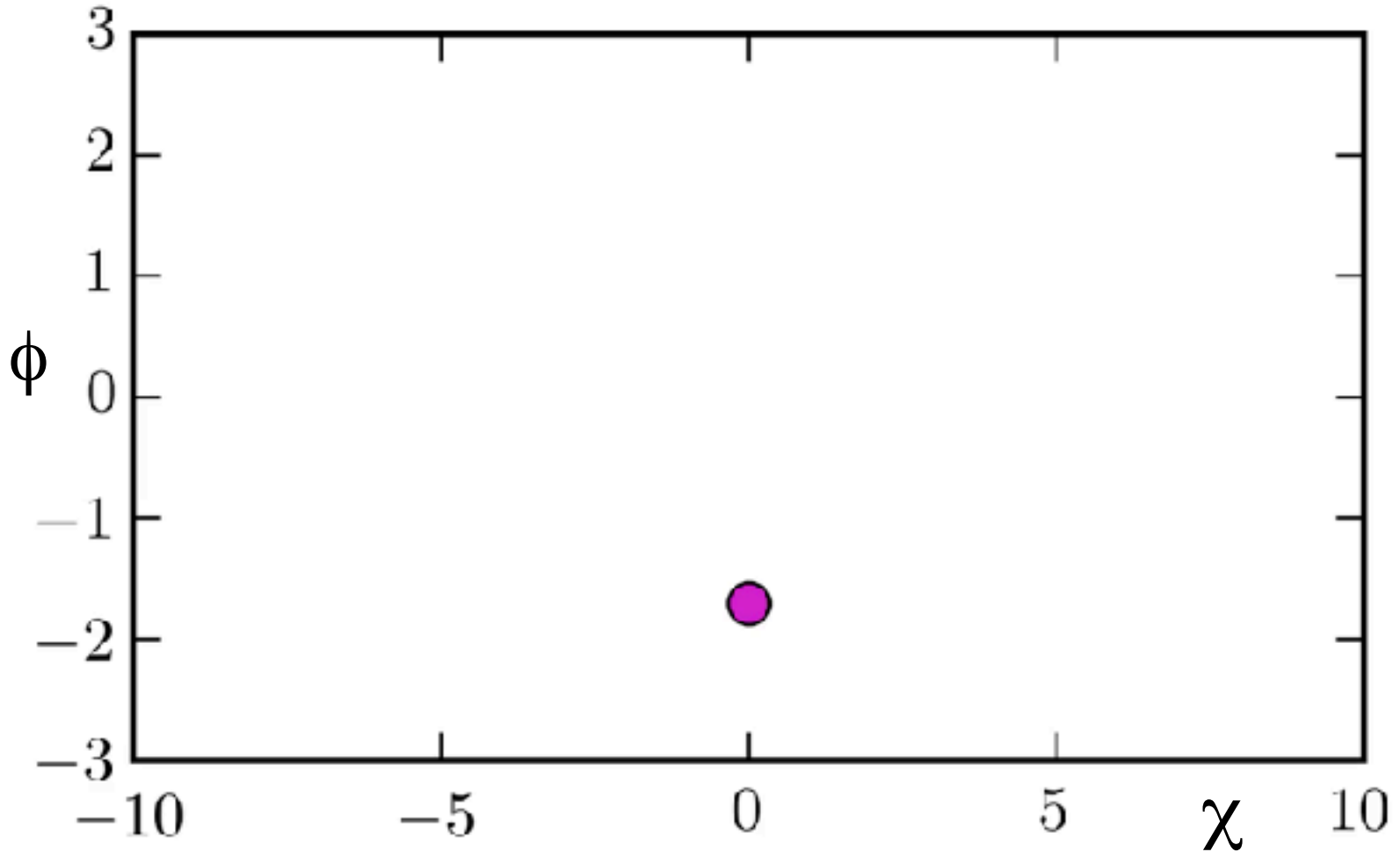
coherent



ballistic billiards $k=0$ mode **phase space string** evolution

2D constrained distribution functions

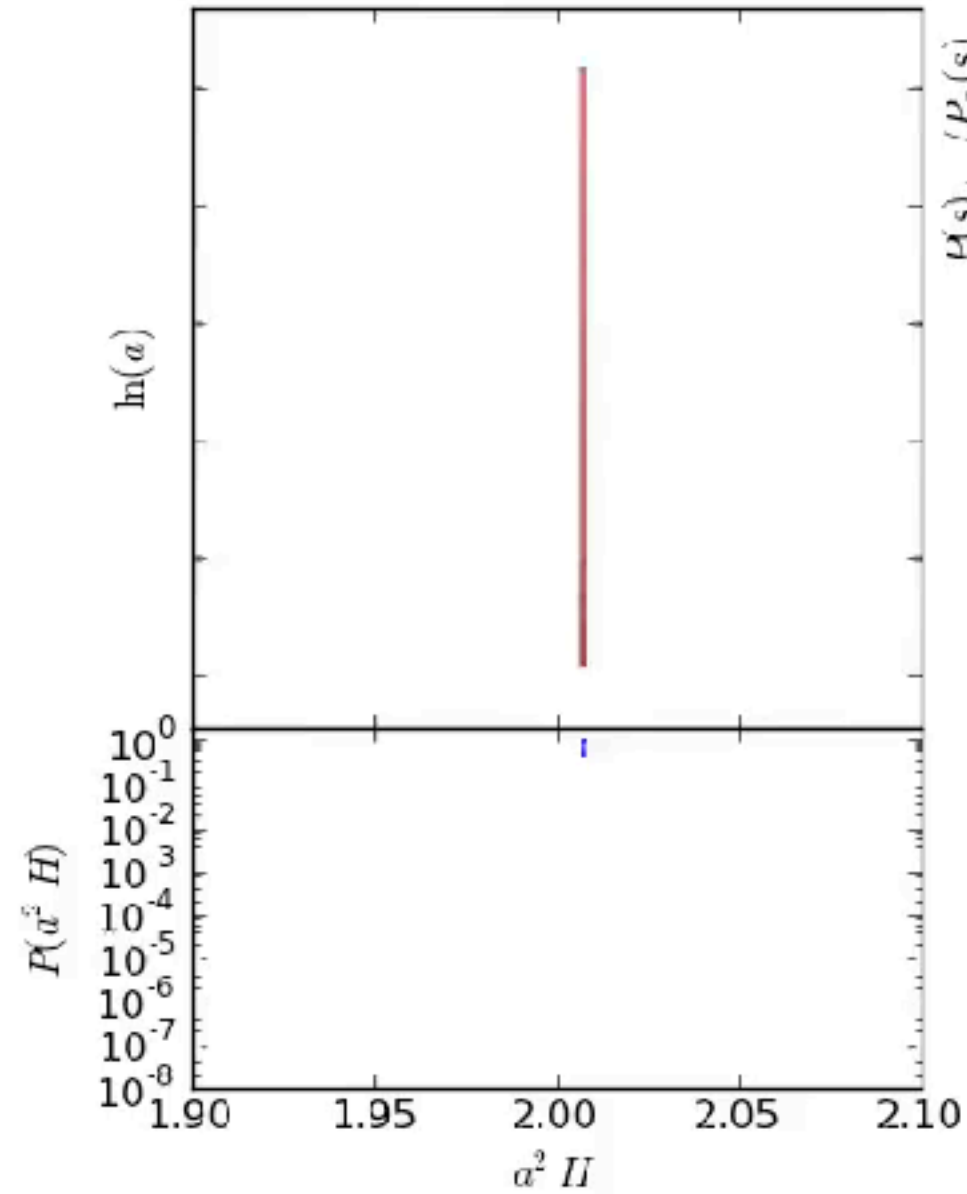
stopping criterion when coarse-grained entropy of field variables rises \Leftrightarrow strain high



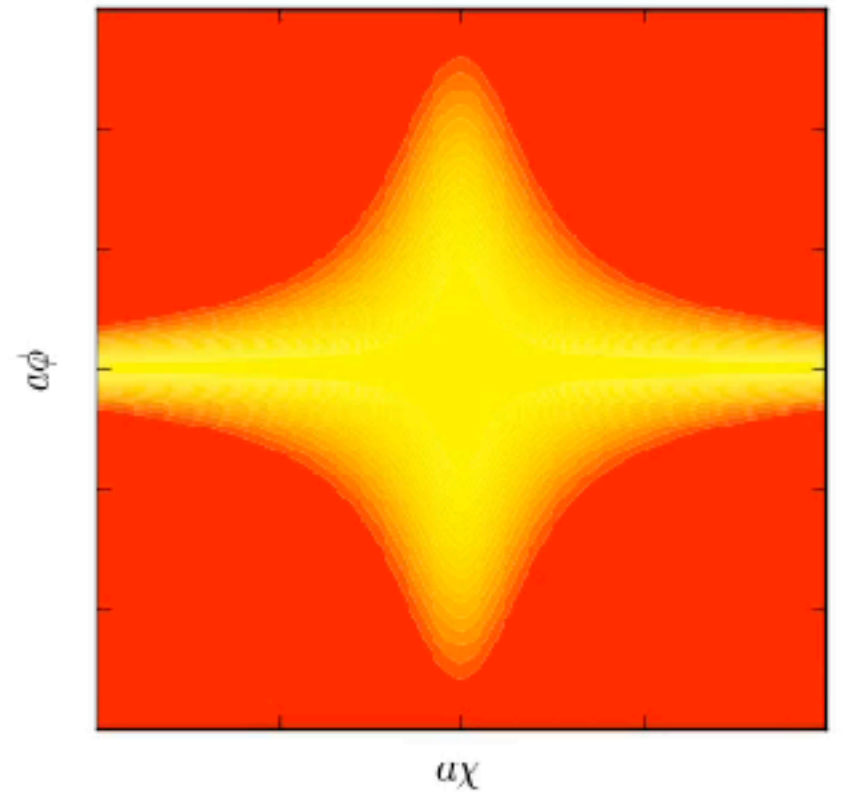
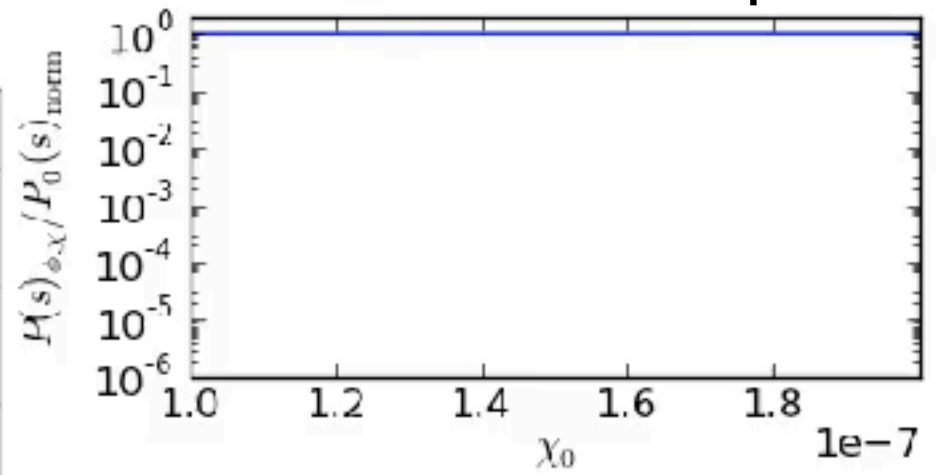
$$V = \frac{1}{4} \lambda \phi^4 + \frac{1}{2} g^2 \phi^2 \chi^2$$



phase space strings

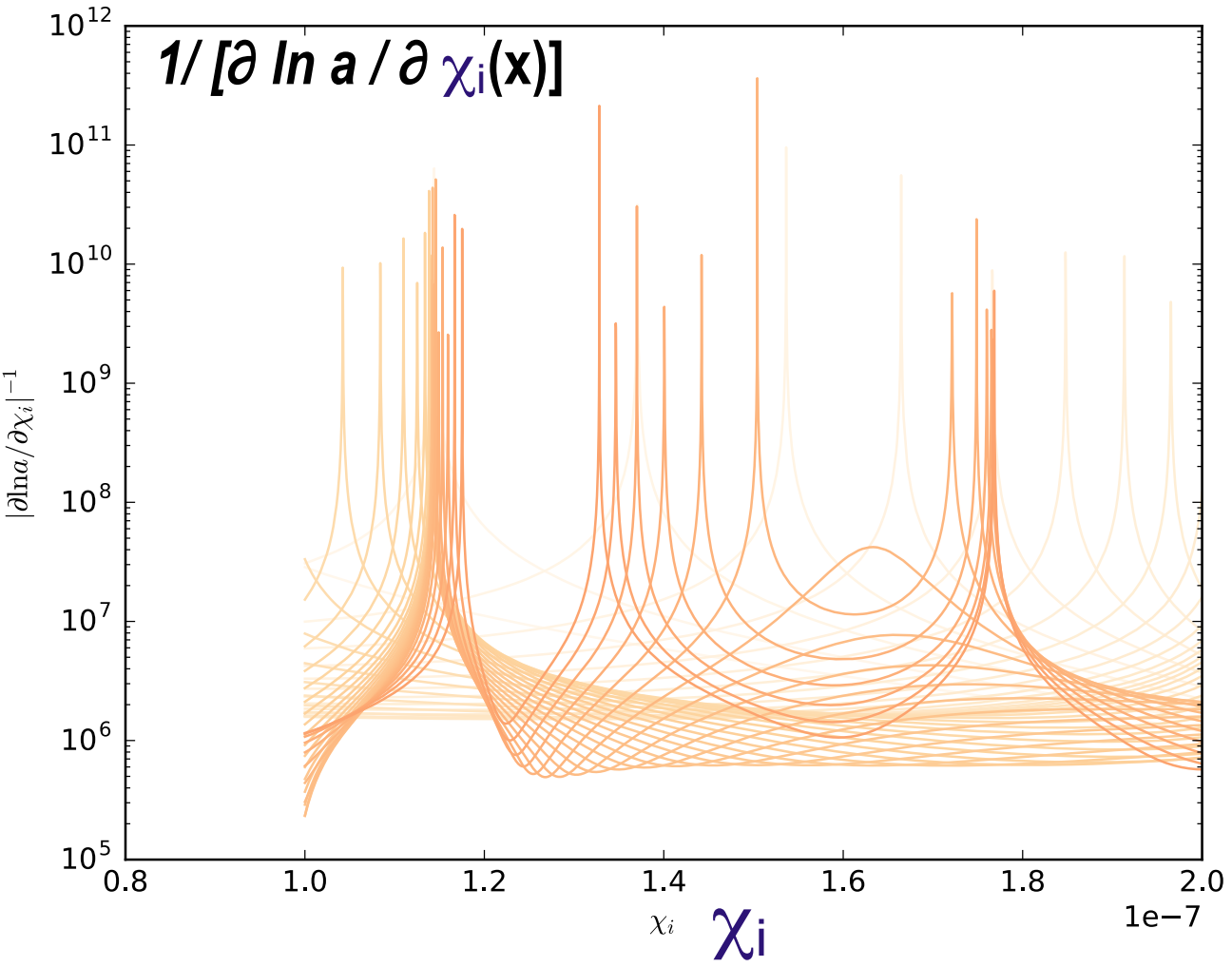


caustics are ubiquitous



**calculating ballistic evolution to caustics
gives the spikes in good agreement with
full nonlinear lattice simulations**

ϵ^{-1}



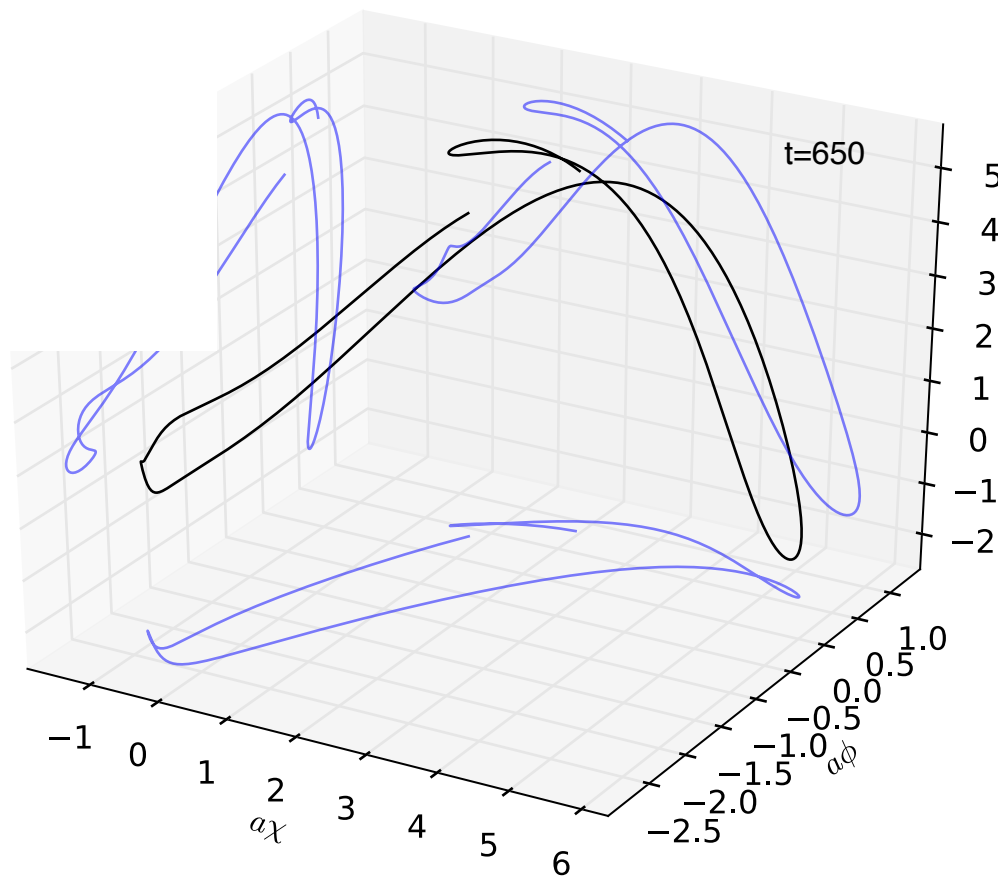
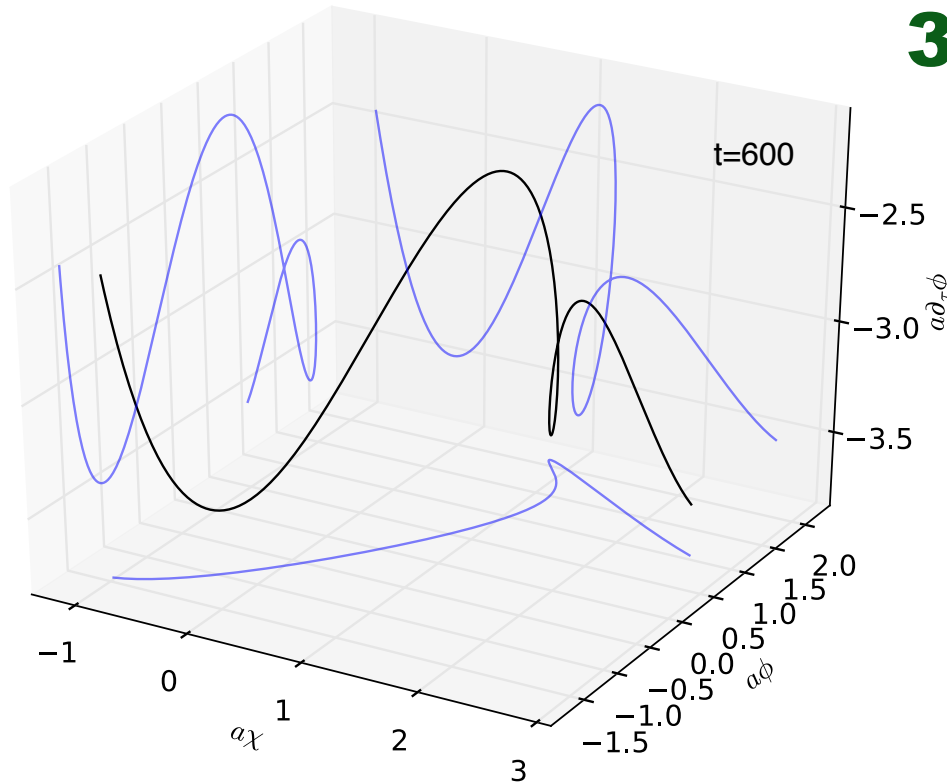
B2FH, b+braden+frolov+huang

nonG from post-inflation but pre-entropy generation ballistic trajectories can lead to pre-shock-in-time caustics and other phase space convergences in the deformations (!) Zeldovich map-ish

eg $\partial \ln a / \partial \chi_i(x)$, $\partial \ln a / \partial g(x) \Rightarrow P[\ln a(x), t_{shock} \mid \chi_i(x), g(x), t_{end-of-inflation}]$

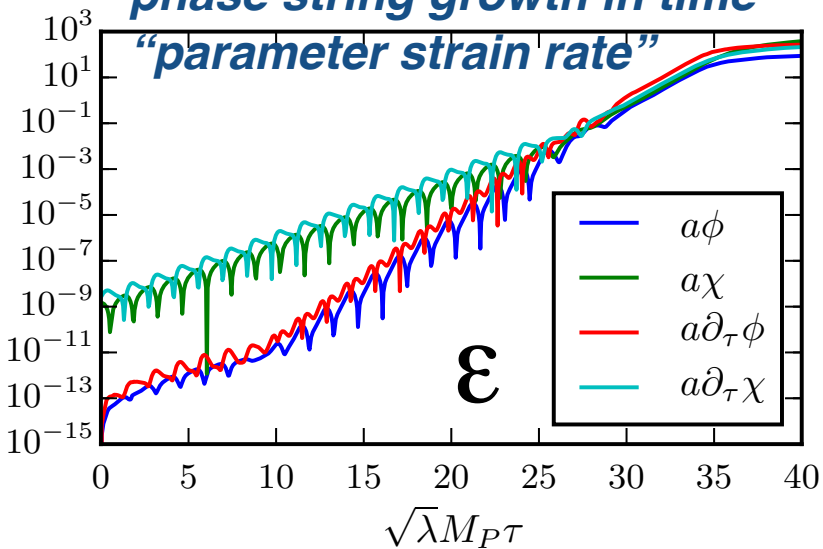
3D phase space strings

3D constrained distribution functions



phase string growth in time

“parameter strain rate”



**how generic will caustic
preheating be? structure
around potential minima:**

=> filamentary potentials

=> ballistic flow channels

multi-filaments may lead to caustics

2 std inflaton, slow heating? roulette V is fast. 3-star

4 case workhorse. the 5-star... 'axionic' angles

works with conformal flattening of $V +$

cf. filaments that join at clusters in the LSS web

isocon

$\chi(\mathbf{x})$

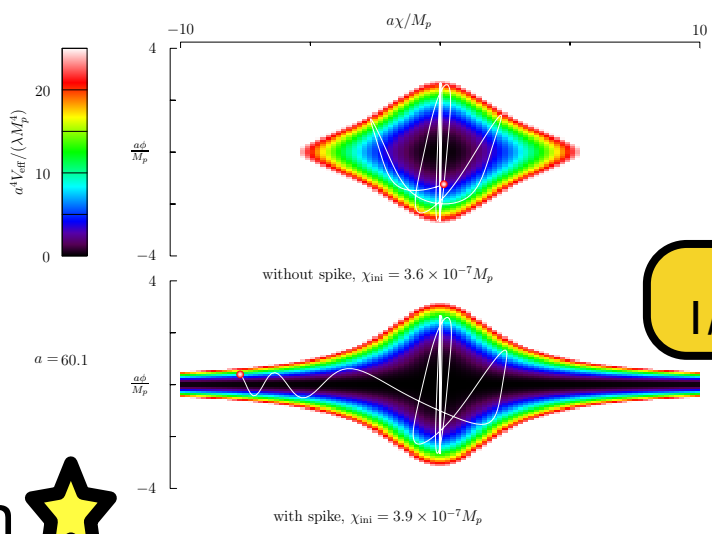
or
 $g(\sigma(\mathbf{x}))$
or..

ϕ

inflaton

pre-heating
patch
(~1cm)

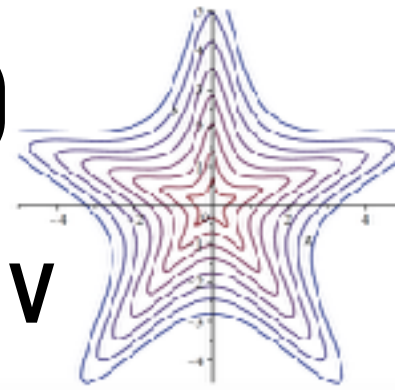
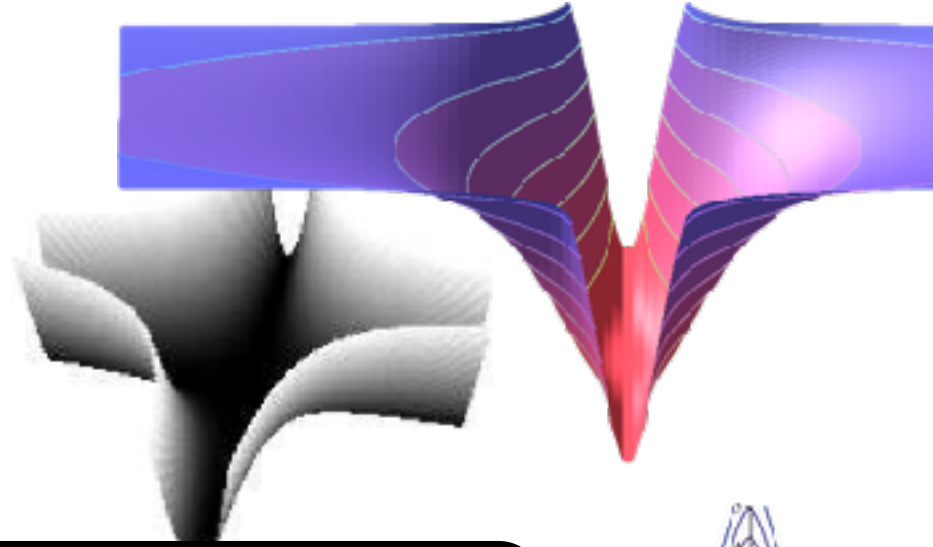
How generic is the intermittent caustic phenomenon? Holds for many basin potentials at the end of inflation. but not if rapid heating



$$1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2,$$

$$1/2 m^2 \phi^2 + 1/2 g^2(\sigma) \phi^2 \chi^2$$

3-star => **5-star V**

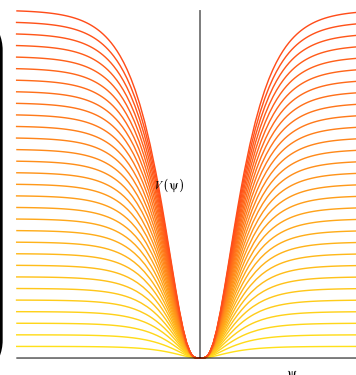


$$1/4 \lambda (r^2 - v^2)^2 U$$

$$V(\mathbf{r})U(\cos\theta), r^2 = \phi^2 + \chi^2$$

filaments!

conformal transforms
potential flatten



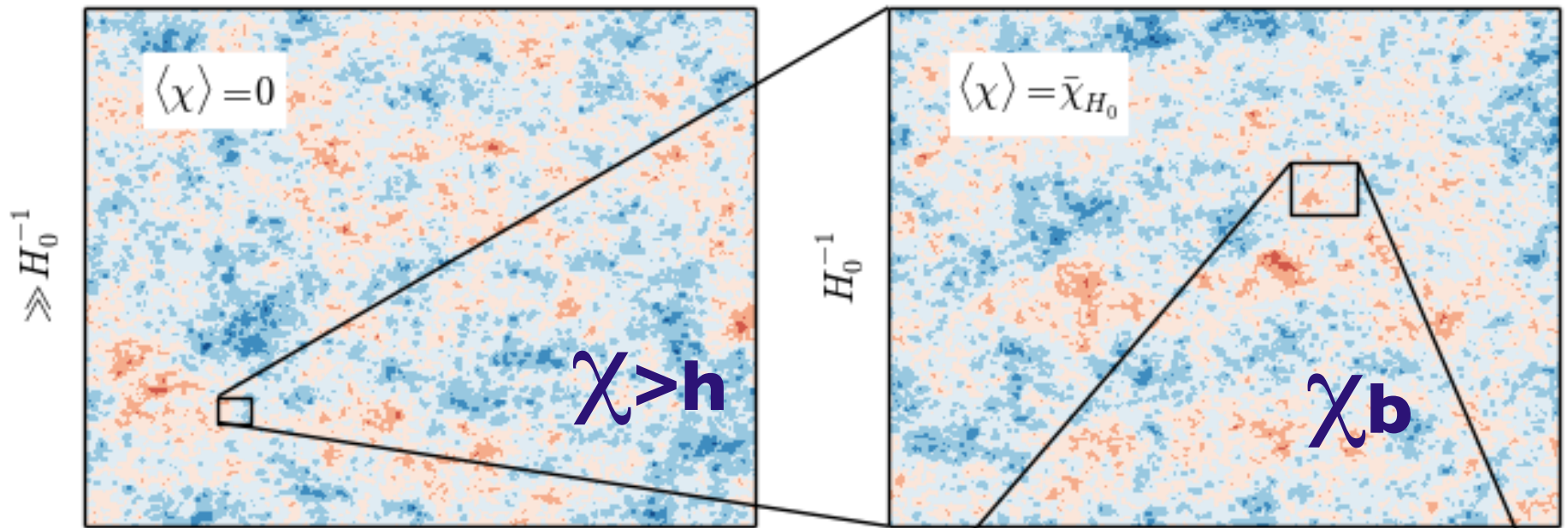
angular variables pNGB natural inflation, racetrack, monodromy, ..
 $V(\mathbf{r}, \theta) = \sum_M V_M(\mathbf{r}) \cos(m\theta)$ pNGB, Roulette r~hole size
 3D $\phi \chi \sigma$ fields $V(\mathbf{r}, \mathbf{n}) = \sum_{LM} V_{LM}(\mathbf{r}) Y_{LM}(\mathbf{n})$
 $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$
 conformally transformed potentials a la Higgs/ R^2 , modified kinetic terms, flattened potentials of all sorts B2FH, b+braden+frolov+huang



**how modulated caustics in
preheating could give
observable intermittency**

**modulating the caustics
on large scales & super-
horizon scales via isocons
(coupling constant g modulation via isocon)**

these isocons are NOT spectators

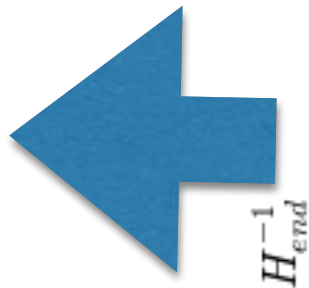


ULSS modulation beyond our Hubble patch

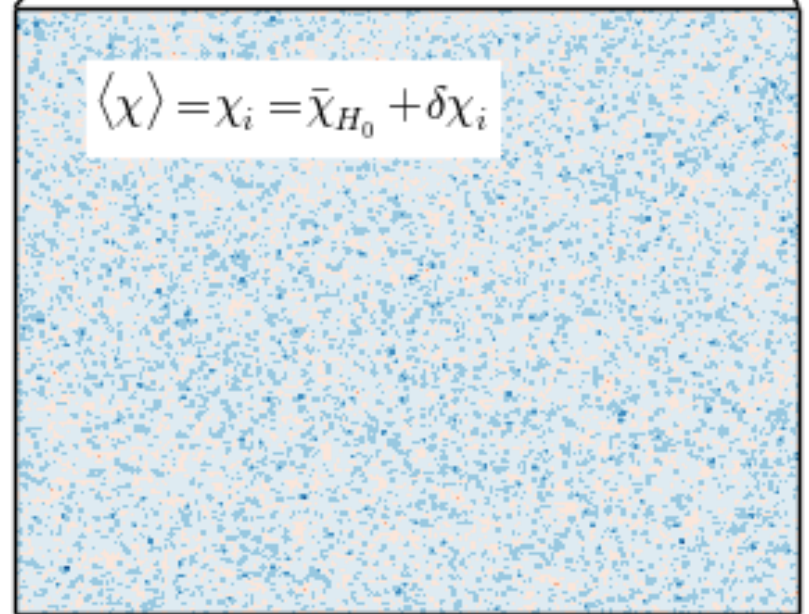
LSS modulation within our Hubble patch

$$\delta \zeta_{NL\text{shock}}(\chi_i(\mathbf{x}) | g^2/\lambda)$$

=> NonG cold spots ++



H_{end}^{-1}



preheating horizon scale < comoving cm

the complex preheating cm is modulated by a large scale Gaussian field

highly nonlinear field evolutions happened

(Eol caustics, bubble collisions)!

subdominant patterns do arise! => will any be observable as rare-event CMB/LSS 'GRF-biasing' anomalies?

or weak constraints on multifield potentials, >horizon fields, nucleation rates, etc.

b2fh17 progress in semi-analytic understanding of complex lattice sims with prob strings, caustics, trajectory stopping, shocks-in-time in the V-web

light isocons cf. heavy isocons, the heavy can lighten up = original SBB nG isocon modulators, coupling(isocon) modulators, isocon tunneling, isocon oscillons, isocon short-lived fuzzy-strings, + very long-lived strings

alas a 2-number A_s - n_s early universe so far

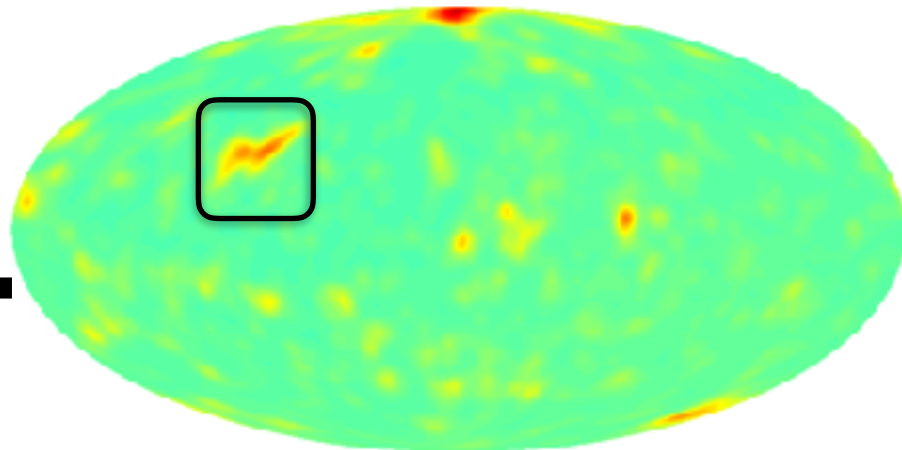
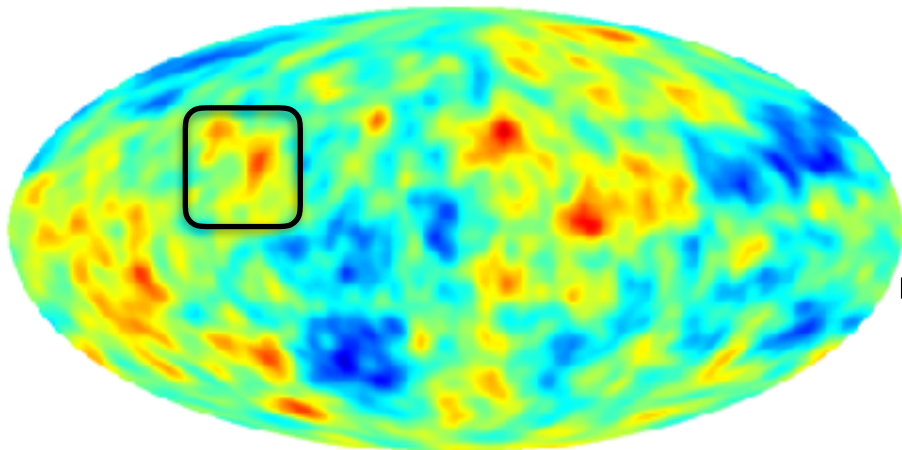
intermittency frustration: statistical variance is large cf. 2-3 parameter search

CMB restricts us to a projected 2D ζ -scape to reconstruct phonon/isotropic-strain power, the future may look much the same as now for $\zeta \Rightarrow$ potential $V(\phi) \Rightarrow$ acceleration $\epsilon(a)$; **r** helps

we mock the LSS future *end-to-end* to probe the mode-rich 3D ζ -scape

Gaussian; 10°S axis

single spike 40; 10°S axis



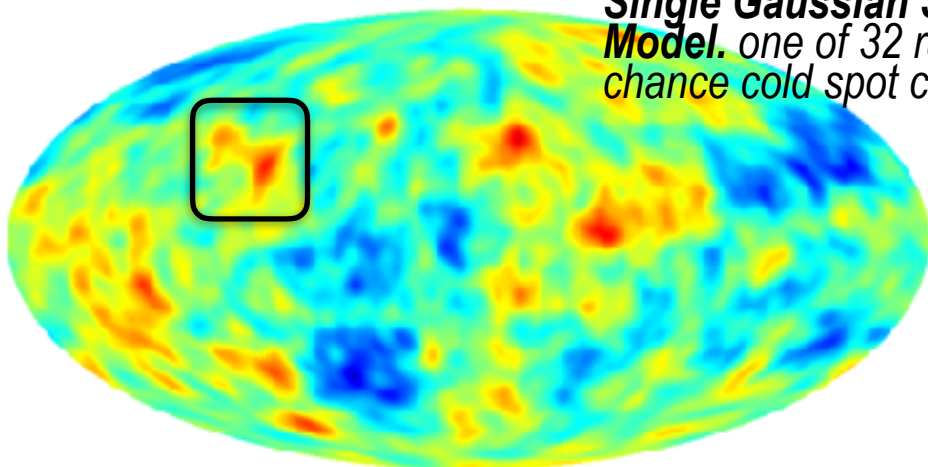
+

-20.0 -10.0 0 10.0 20.0

-4.00 -2.00 0 2.00 4.00

Gaussian + single spike 40; 10°S axis

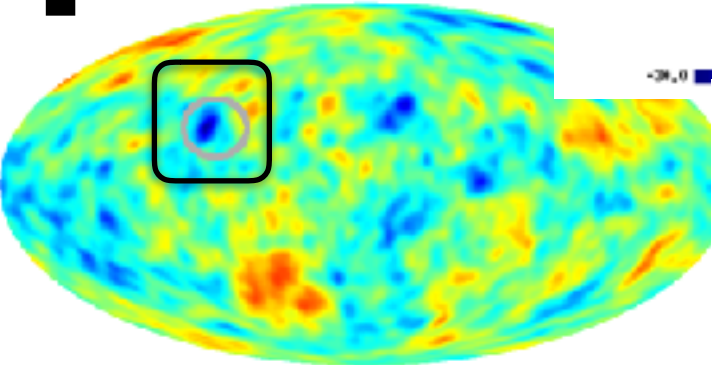
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Single Gaussian Spike intermittent non-Gaussian Model. one of 32 random choices to yield chance cold spot constructive interference.

T

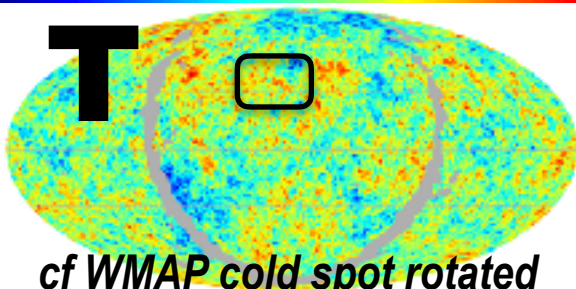
Gaussian + single spike 40; T 0.00



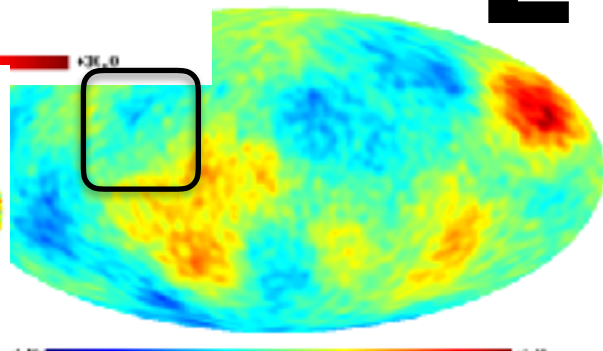
-20.0 -10.0 0 10.0 20.0

E

20 + 0.0000 0.000 0.01 0.1000



cf WMAP cold spot rotated



-4.00 -2.00 0 2.00 4.00

end