

the Shock-in-Times of Entropy/Information Generation in Post-inflation Preheating

Dick Bond CIFAR@CITA with CITA aka Cosmic Information Theory & Analysis

dS_G/dt
I
N
F
L
A
T
I
O
N
dS/dt

primary anisotropies

- linear perturbations: scalar/density, tensor/gravity wave
- tightly-coupled photon-baryon fluid: oscillations $\delta\gamma$ $v\gamma$ $\pi\gamma$
- viscously damped
- polarization $\pi\gamma$
- gravitational redshift




Φ SW $d\Phi/dt$

Decoupling LSS

17 kpc
(19 Mpc)

secondary anisotropies

- nonlinear evolution 
- weak lensing
- thermal SZ + kinetic SZ
- $d\Phi/dt$
- dusty/radio galaxies, dGs

the nonlinear COSMIC WEB

dS/dt

MILKYWAY



z=0

DarkE

reionization

z ~ 1100 redshift z

z ~ 10

time t

13.7-10⁻⁵⁰ Gyrs

13.7 Gyrs

10 Gyrs

today

how (most of) the **entropy** in matter

=> *GUT plasma/quark soup* => $S(\gamma, \nu)$ was

generated (through a *shock-in-time*)

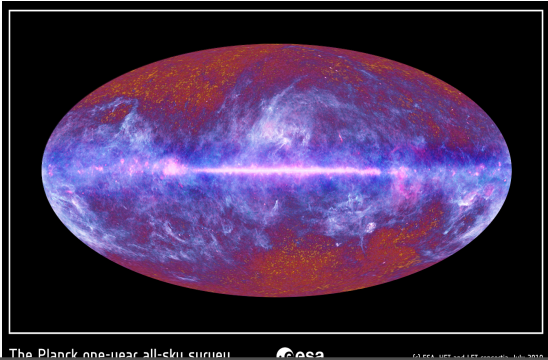
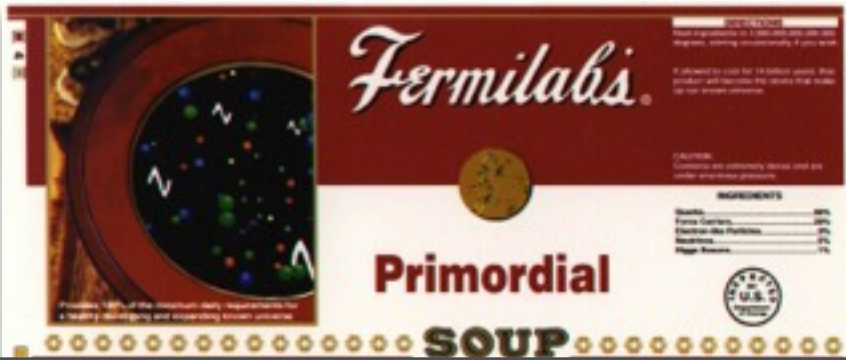
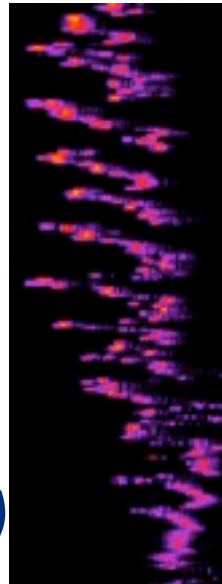
via *nonlinear coupling* of the *inflaton* to

new interaction channels g, χ_a ultimately to
standard model degrees of freedom

∃ a role for *decaying particles, 1st order phase transitions?*

exactly who, what, where, when, why?

we search for fossil "non-Gaussian" structures from this period with Planck +WMAP9



$a_{shock}(g)$

non-Gaussianity
(WMAP, Planck, LSS)
spiky nG preheating

modulating post-inflation entropy generation shocks *via* longrange fields

isocon

$\chi(\mathbf{x})$

or

$\mathbf{g}(\sigma(\mathbf{x}))$

or..

scalar field

fluctuations

in the

vacuum of

the ultra-

early

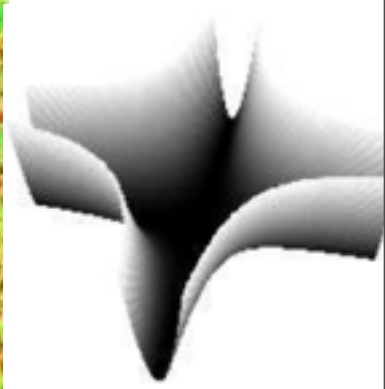
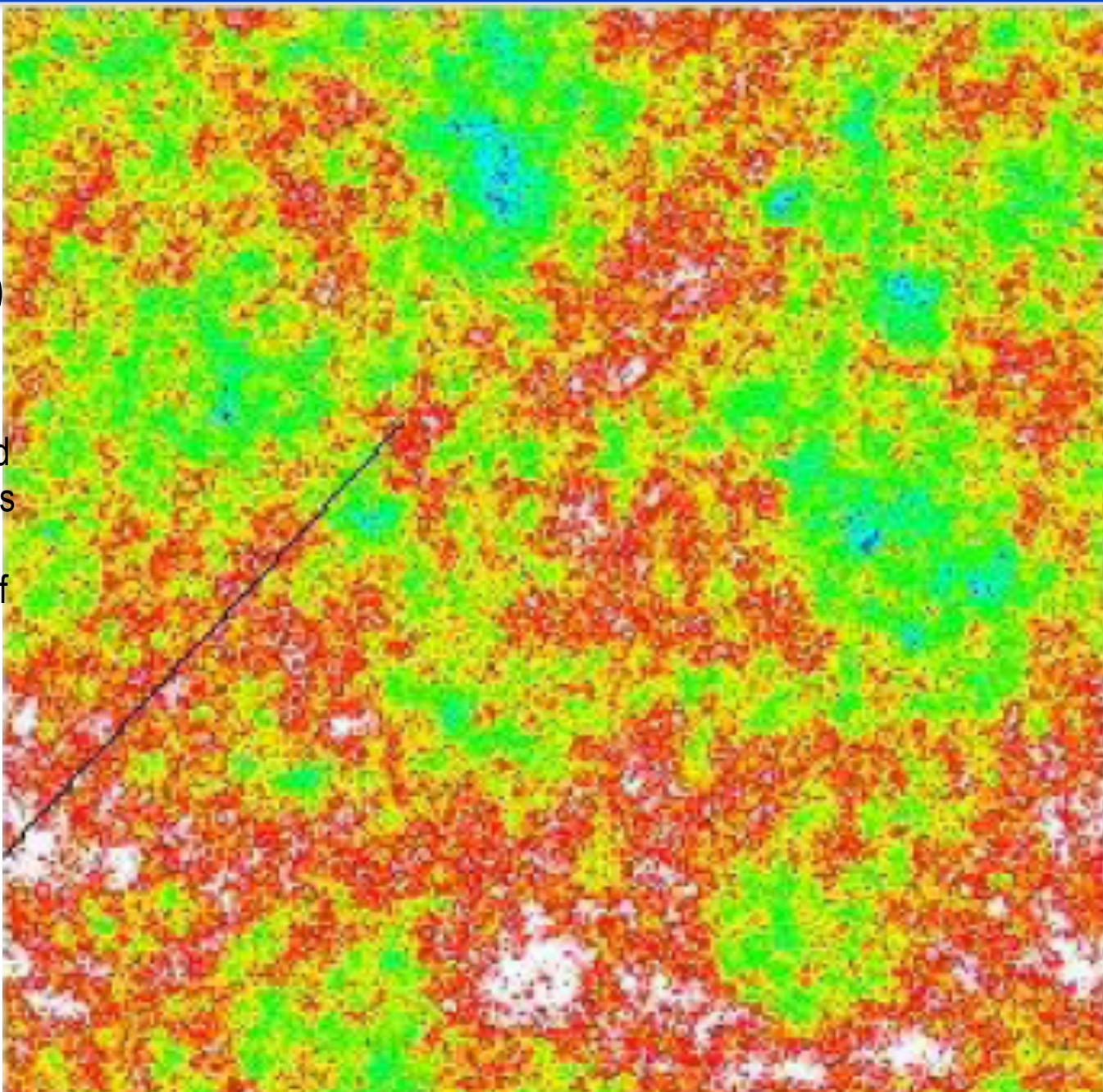
Universe

pre-

heating

patch

(~1cm)

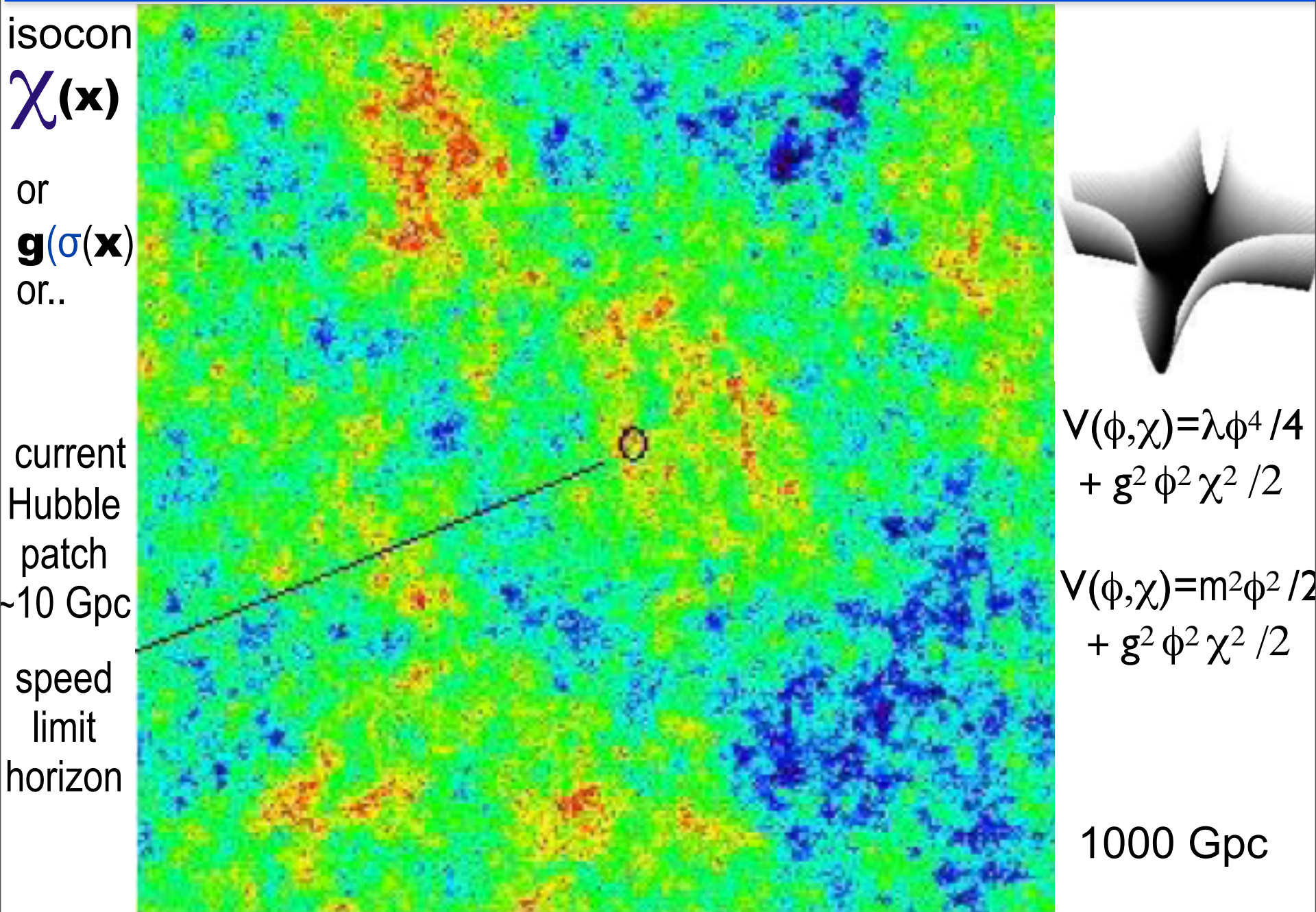


$$V(\phi, \chi) = \lambda \phi^4 / 4 + g^2 \phi^2 \chi^2 / 2$$

$$V(\phi, \chi) = m^2 \phi^2 / 2 + g^2 \phi^2 \chi^2 / 2$$

10 Gpc

modulating post-inflation entropy generation shocks *via* longrange fields



modulating post-inflation entropy generation shocks *via* long range fields

isocon

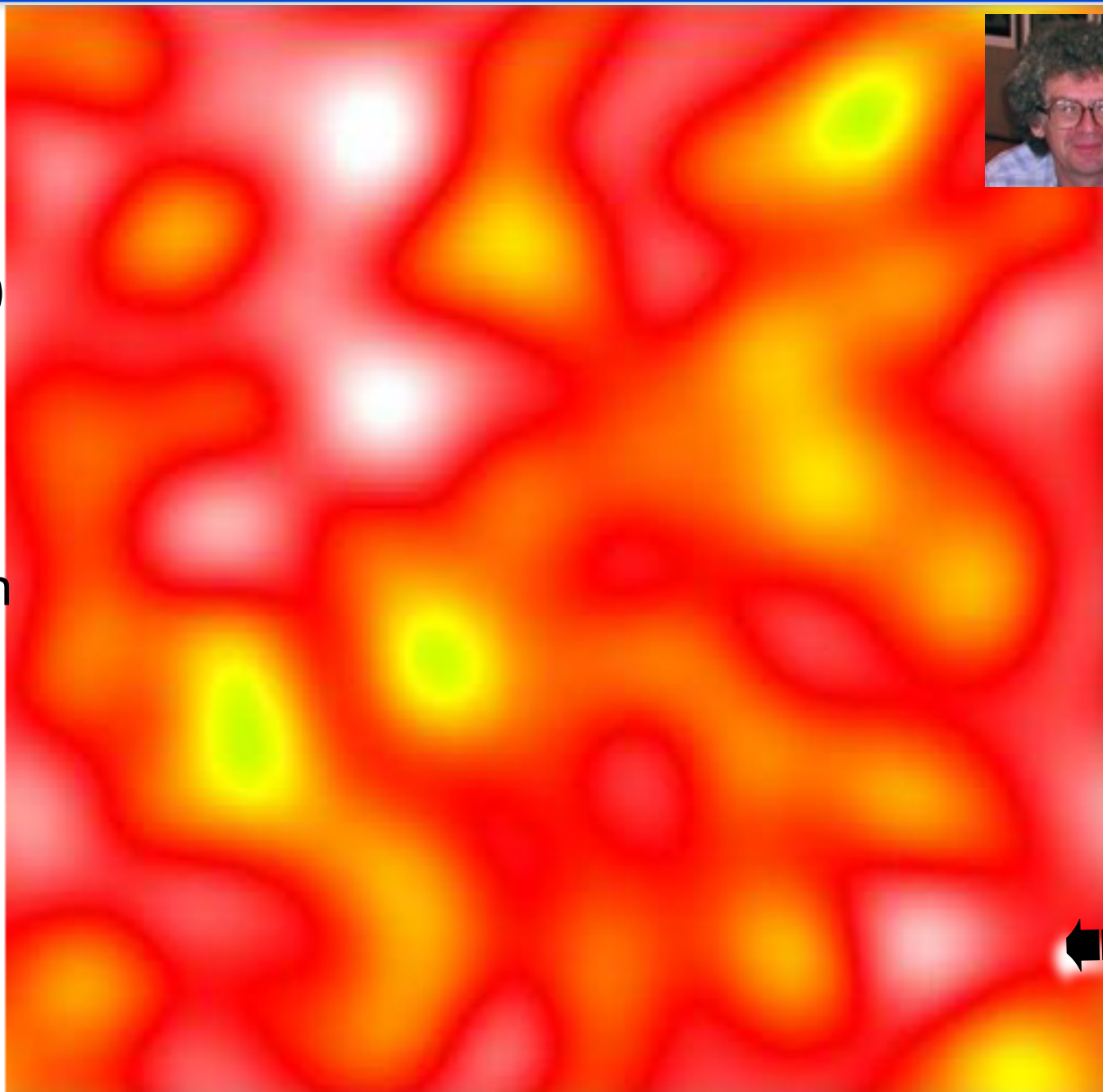
$$\chi(\mathbf{x})$$

or
 $\mathbf{g}(\sigma(\mathbf{x}))$
or..

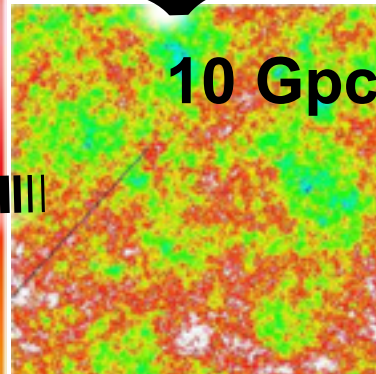
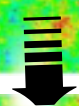
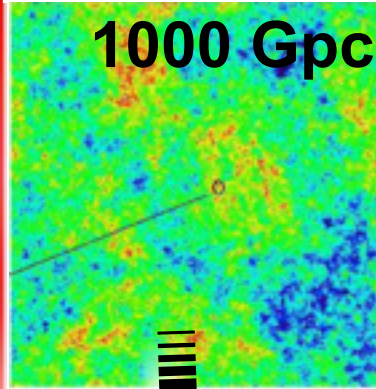
$$\phi$$

inflaton

pre-heating
patch
($\sim 1\text{cm}$)



Parametric
Resonance
 $g^2/\lambda \sim 1$



modulating post-inflation entropy generation shocks via long range fields

isocon
 $\chi(\mathbf{x})$

or
 $g(\sigma(\mathbf{x}))$
or..

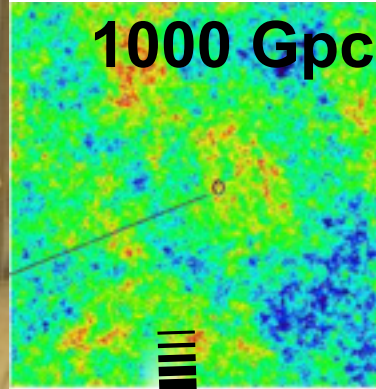
pre-heating
patch
(~1cm)



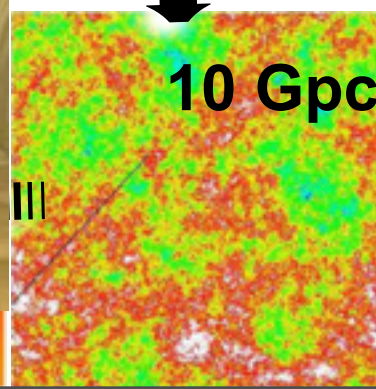
Parametric
Resonance
 $g^2 / \lambda \sim 1$



BB12



1000 Gpc



10 Gpc

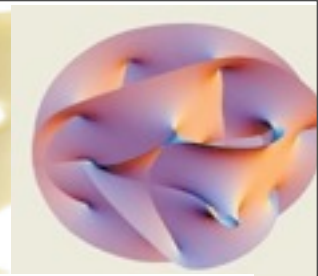


B²FH12 @ifaUH aka Waikiki Feb12

Roulette Inflation: *a statistical mini-landscape (one of very many) of the early U origins of observed cosmic structure:*

holey U: *sizes/shapes of geometrical structures such as holes in a dynamical extra-dimensional (6-7D) space settling into a stable bit of extra-dim at each point in our 3D space;*

braney U: *motions of lower-dimension subspaces:*



Preheating After
Roulette Inflation

$$\langle \tau \rangle =$$

quantum
diffusion
spatial jitter

drift

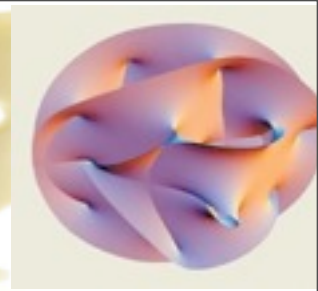
$$\ln a(\mathbf{x}, \ln H)$$

let there be
heat

entropy generation in
preheating from the coherent
inflaton (origin of all matter)

S E M I - I N T E R N A L I N F L A T I O N

Roulette Inflation: *a statistical mini-landscape (one of very many) of the early U origins of observed cosmic structure:*

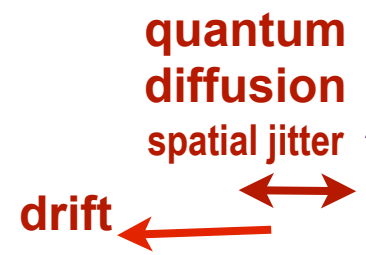


holey U: sizes/shapes of geometrical structures such as holes in a dynamical extra-dimensional (6-7D) space settling into a stable bit of extra-dim at each point in our 3D space;

braney U: motions of lower-dimension subspaces

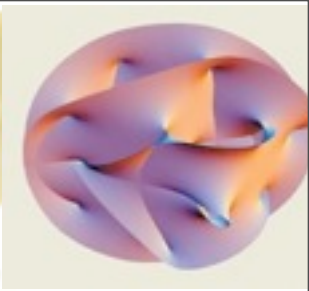
Barnaby, Bond, Huang, Kofman 2009

pre-heating patch (<1cm-now, <10⁻³⁰ cm-then)



let there be heat

Roulette Inflation: *a statistical mini-landscape (one of very many) of the early U origins of observed cosmic structure:*



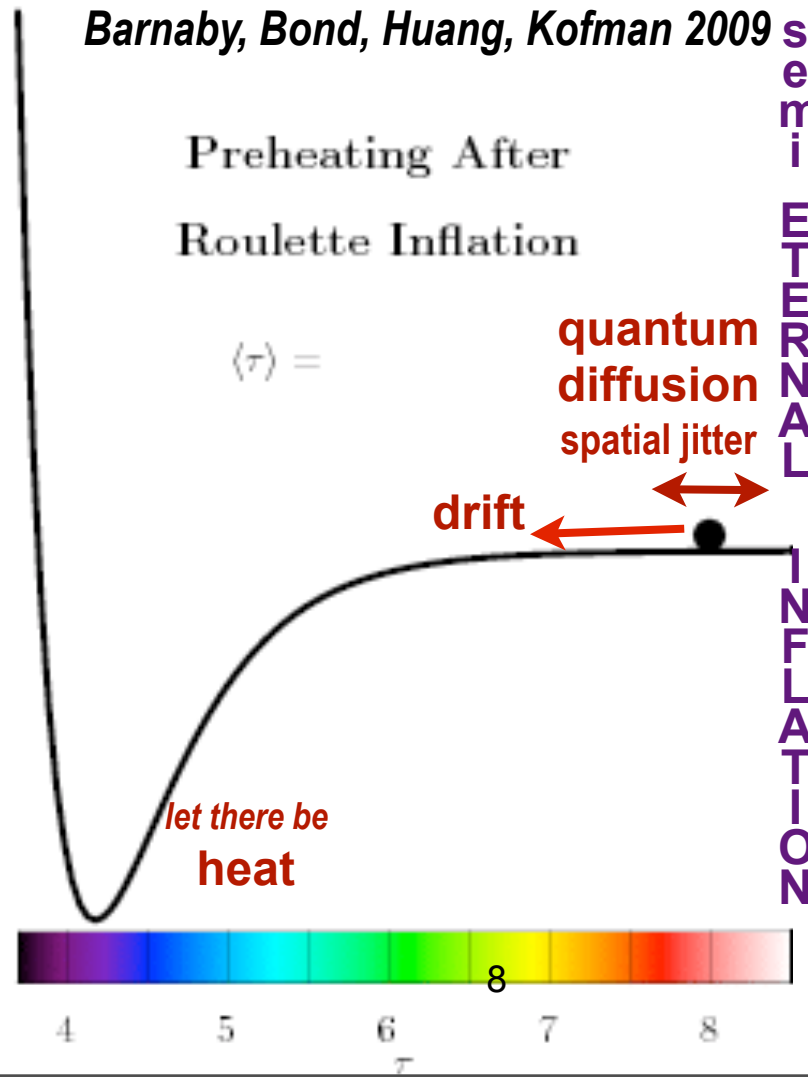
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A visualized 2D slice in lattice simulation

Barnaby, Bond, Huang, Kofman 2009



www.youtube.com/watch?v=FW__su-W-ck&NR=1

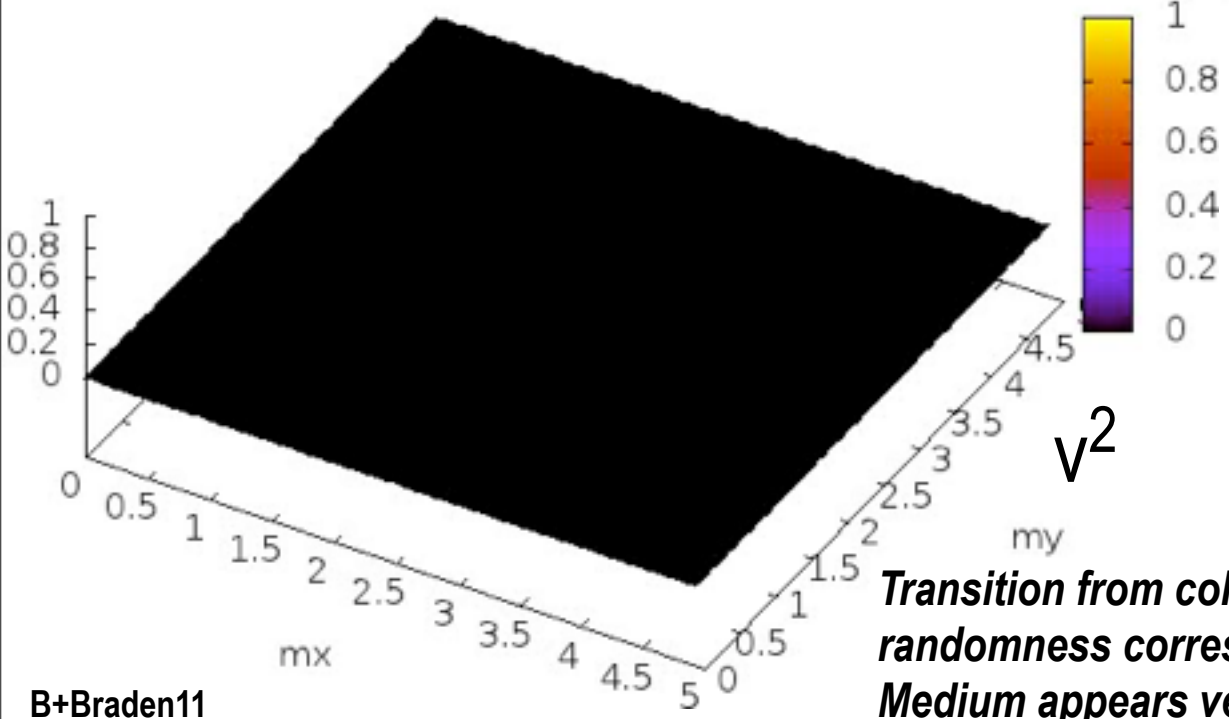
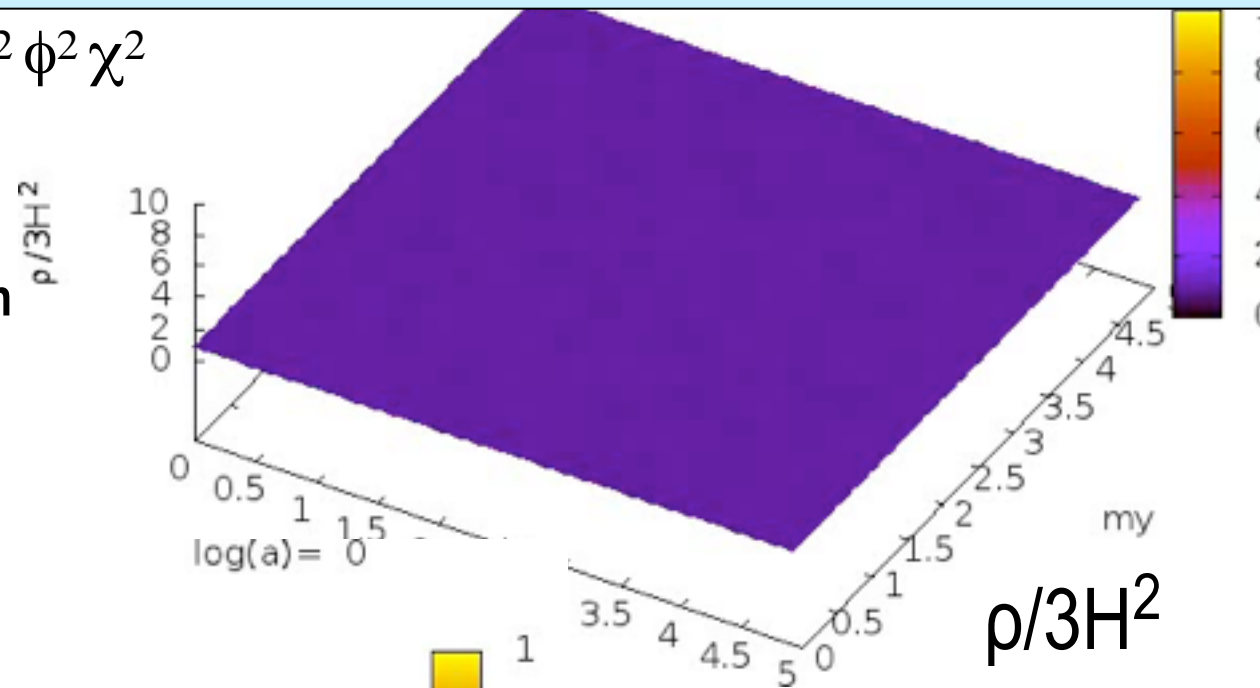
coherent inflaton => incoherent mode cascade of fields thru a shock-in-time to thermal equilibrium

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

Slow Dynamics of IR Modes
 => Hydrodynamic Description

$$\rho = -T^0_0 \quad P = -T^i_i$$

$$v^i = a T^i_0 / (\rho + P)$$



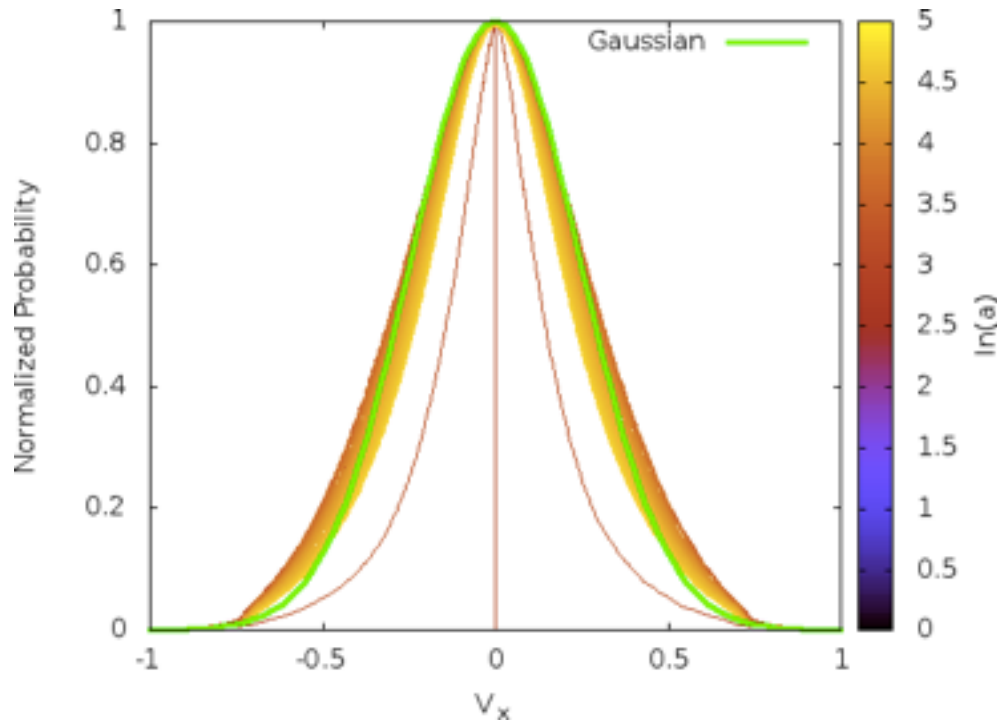
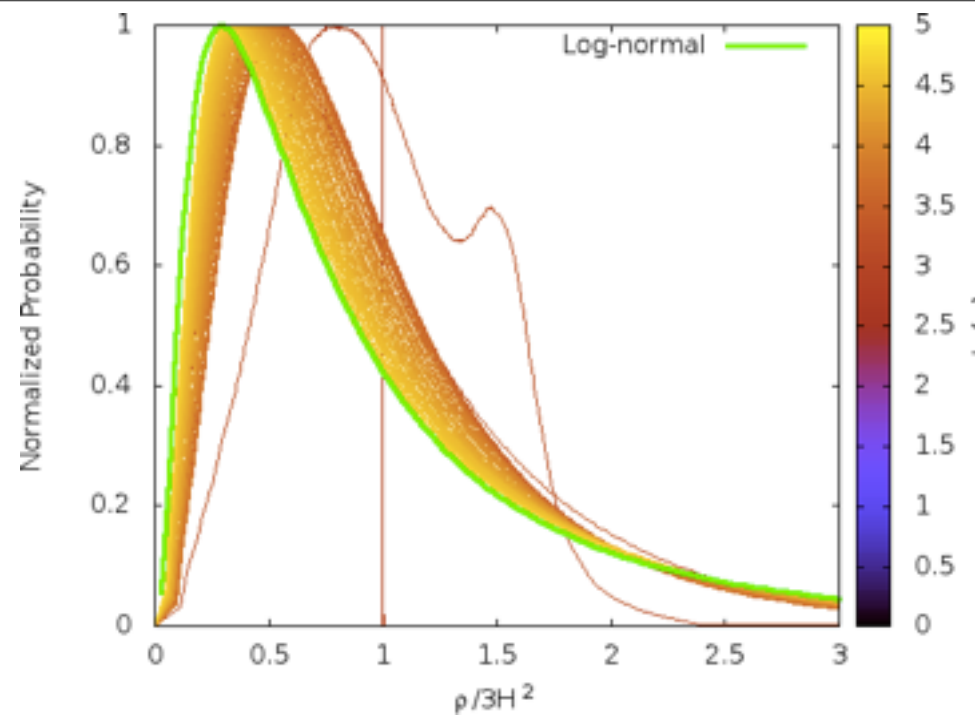
non-Gaussianity
 (WMAP, Planck, LSS)
 spiky nG preheating

Transition from coherent wall-like structures to randomness corresponds to the shock-in-time. Medium appears very complex in space and time, but ...

but Statistical Simplicity

Density PDF ~ log-normal after initial transient Frolov10

Velocity components ~ Gaussian PDF



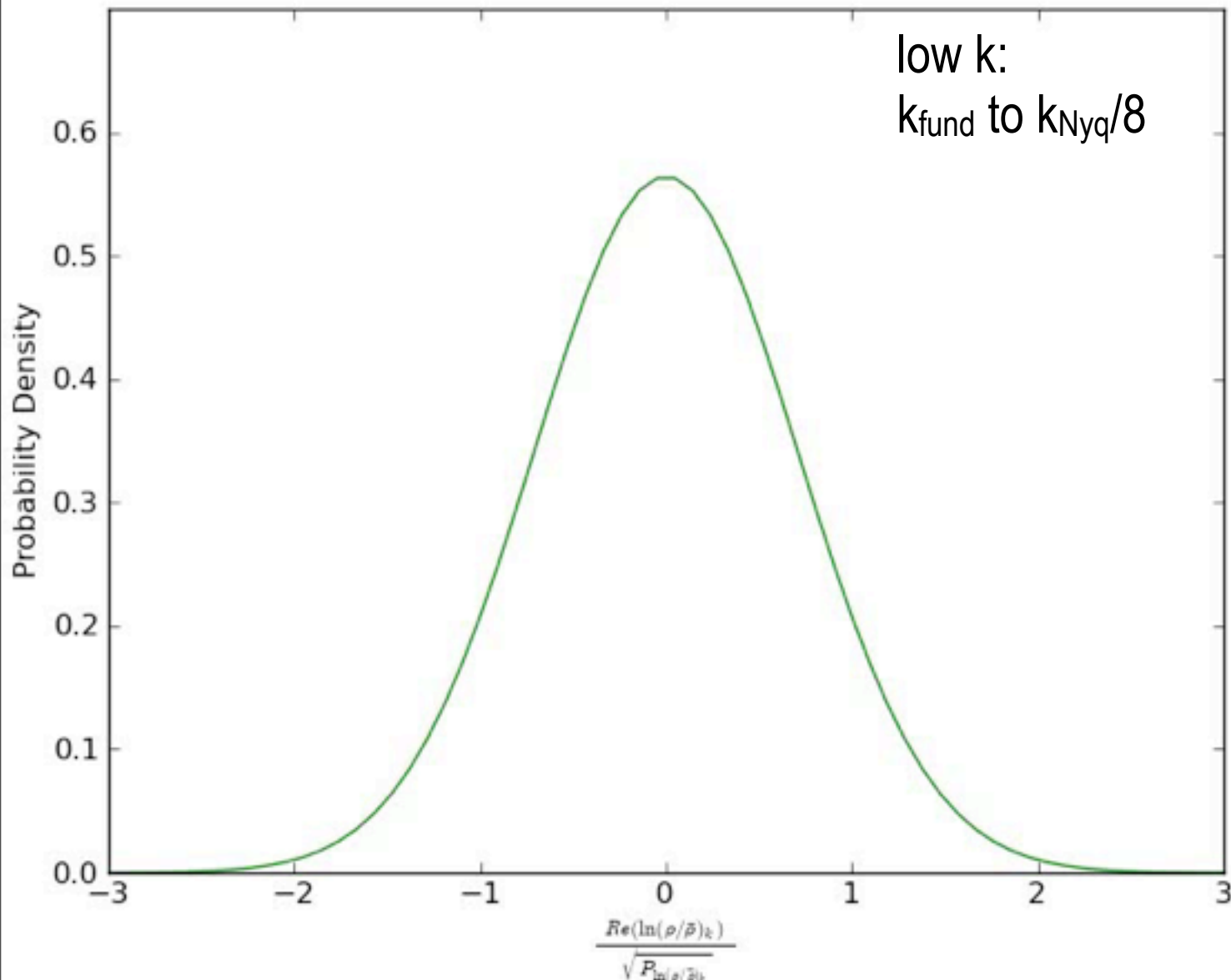
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B+Braden11

but Statistical Simplicity

box $L=10m$ and $N=1024^3$

FT(\ln density) PDF \sim log-normal after initial transient

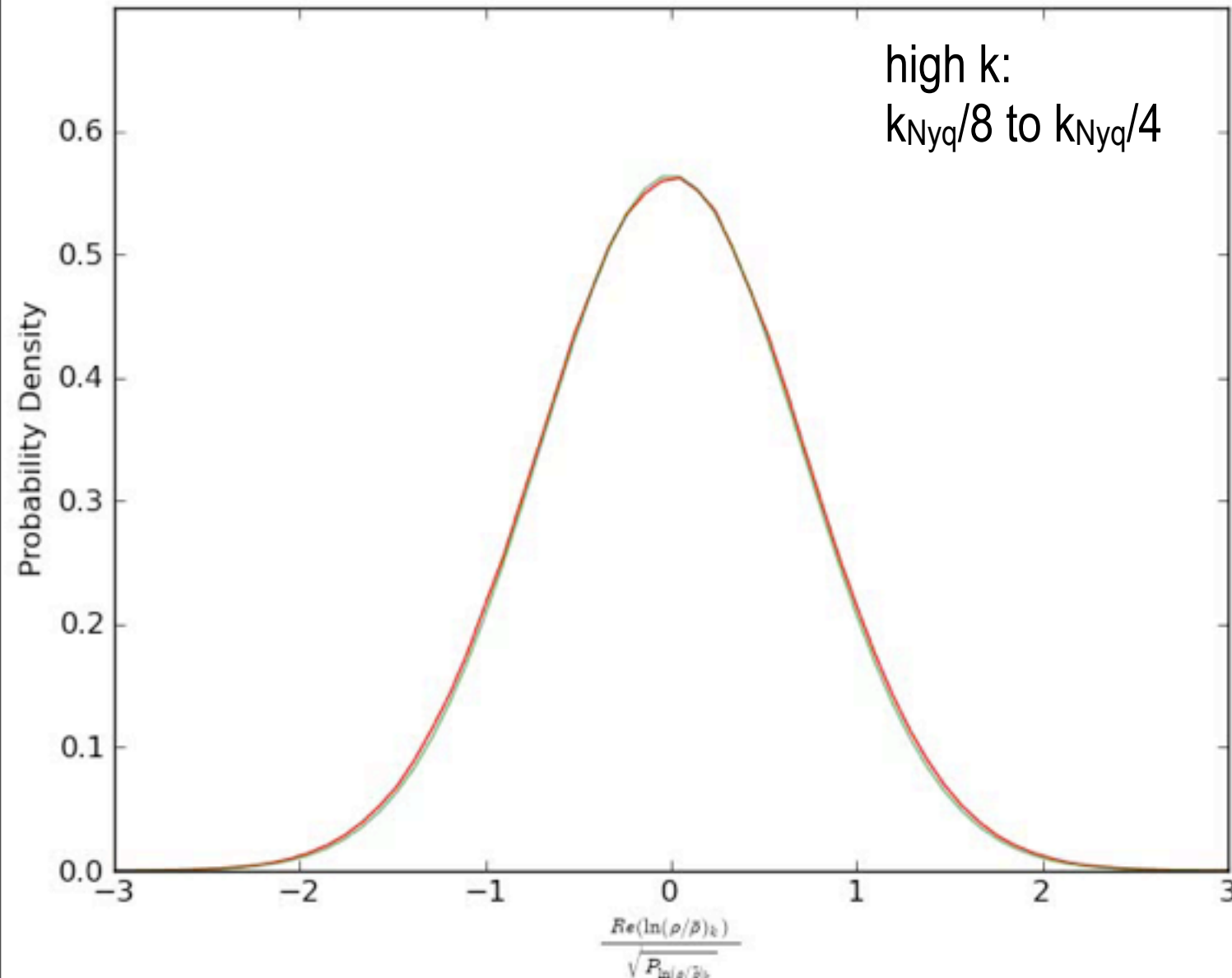


B+Braden11

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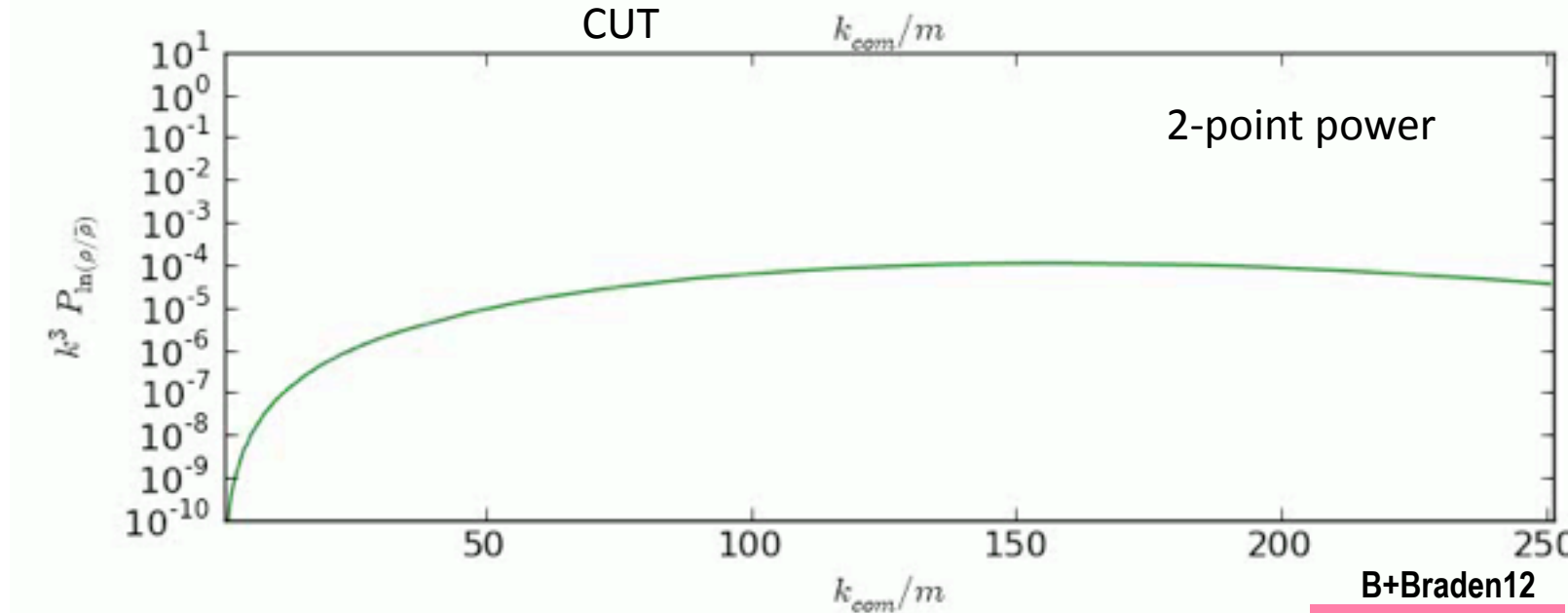
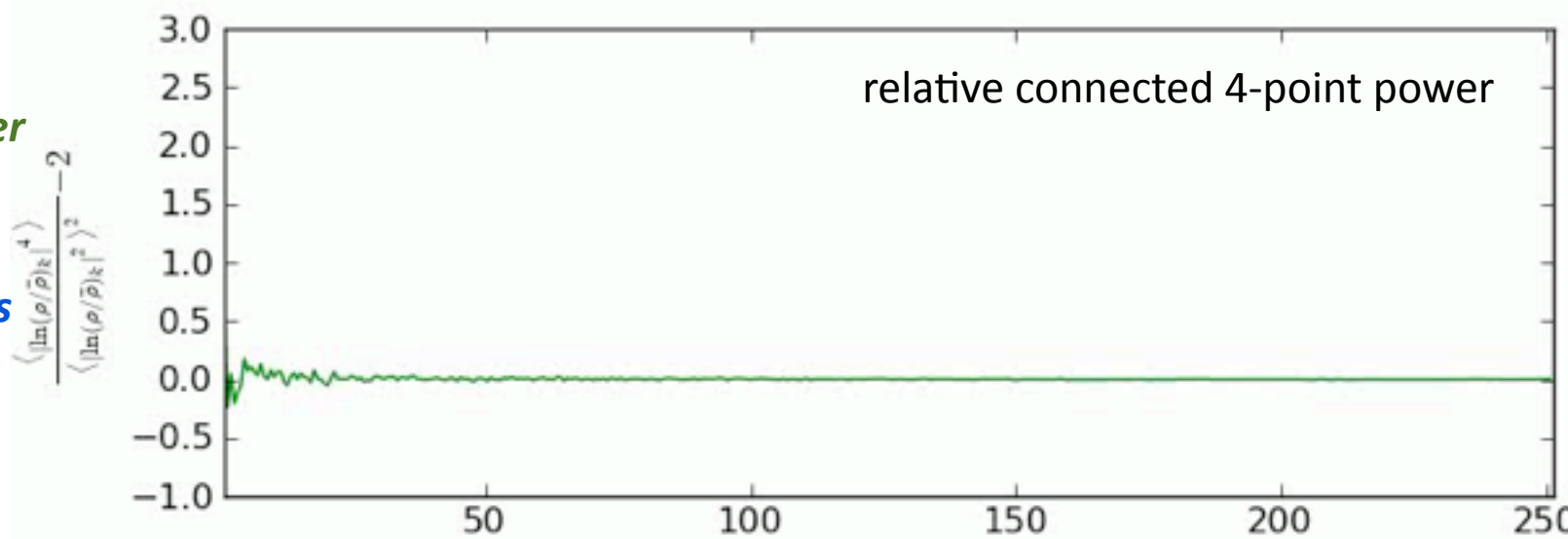
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B+Braden11

coherent inflaton => incoherent mode cascade of fields thru a shock-in-time to thermal equilibrium

$S_{U_i} \sim 0$; $S_{U_{tot,m+r}} / n_b \sim 1.66 \times 10^{10}$ bits/b; $s_Y / n_Y = 5.2$ bits/Y = 2130/411; $s_v = 21/22 s_Y$

In $\rho / \langle \rho \rangle$ power spectrum
cf. instantaneous full thermal spectrum
cf. conventional energy spectrum using a pseudo particle occupation number



$$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2 \chi^2$$

momentum

B+Braden12
 non-Gaussianity (WMAP, Planck, LSS)
 spiky nG preheating



$$S/k_B = \ln N_{\text{states}}$$

$$dS / dt > 0$$

Studying the Cosmic en-TANGO-ment the dance of $U=R+U+S$

of phase & probability: $q(U) = q(S,R) = q(R|S) q(S)$ Universe
 =System(s)+Reservoir =Signal(s)+Residual noise =Effective (F)
 Theory+Hidden variables=Data+Theory, observer(s)+observed

classical nonequilibrium Shannon (relative) entropy

$$S_{fi} = - \int dq [P_f(q) \ln P_f(q) / P_i(q)] + [P_f(q) - P_i(q)]$$
 -KL divergence

$P_f(q)$ probability density functional distribution function

\Leftarrow quantum (von Neumann) $S = -Tr \rho \ln \rho$ density matrix

coarse graining & entropy "production" ($S=0$ pure state)

max S constrained by "measurements" of theorists on the medium
 parameters $q =$ Field variables \Rightarrow Correlation Functions

Measurements: e.g., constraints (information) on Correlators
 marginalize higher order correlators (i.e., unknown) $\Rightarrow S \uparrow$

Bayes $dS < 0$ as System knowledge $\uparrow P(q|D,T) = P(D|q,T)P(q|T)P(T)/P(D|T)$

Gaussian distribution=max-entropy distⁿ fn given 2-pt correlation fn

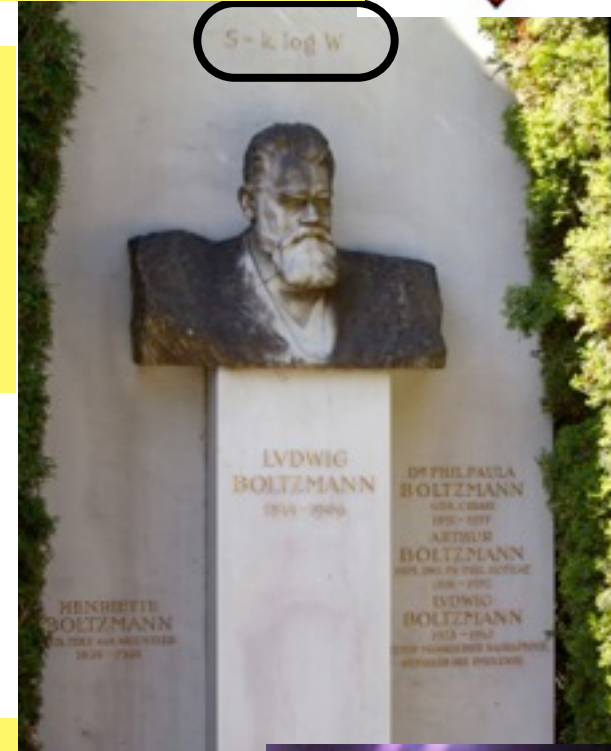
$$S = (\text{Trace } \ln C + N_{dof} \ln 2\pi + N_{dof}) / 2 = \langle \ln V_{p\text{-space}} \rangle + N_{dof} / 2$$

=Shannon entropy subject to the constraint $\int dq P_f \delta q^i \delta q^j = C^{ij}$

$\ln = \log_e$ measure info in nats, $\text{lb} = \log_2$ measure info in bits

$C(k) = \langle | \ln p |^2(k) \rangle$ but want discrete state counting or relative entropy

$$S_{fi} = (\text{Trace } \ln C_f C_i^{-1}) / 2 = \langle \ln V_{p\text{-space},f} / V_{p\text{-space},fi} \rangle_f$$



A Shocking End to Post Inflation Mean Field Dynamics

Shock-in-space $t = \text{const}$

$$V_{\text{bulk}}^2 > c_s^2 \Rightarrow V_{\text{bulk}}^2 < c_s^2$$

supersonic \Rightarrow subsonic

Characteristic spatial scale

Jump Conditions: $\Delta T^{\mu\nu}$

Randomizing Shock Front: ΔS

Mediation: width via viscosity
or collisionless dynamics

post-shock evolution, slow, of
temperature, etc.

Shock-in-time $x = \text{const}$ (deviations for nonG)

$$\langle \rho \rangle \gg \delta \rho \Rightarrow \langle \rho \rangle \ll \delta \rho$$

Homogeneous \Rightarrow Fluctuations

Characteristic temporal scale

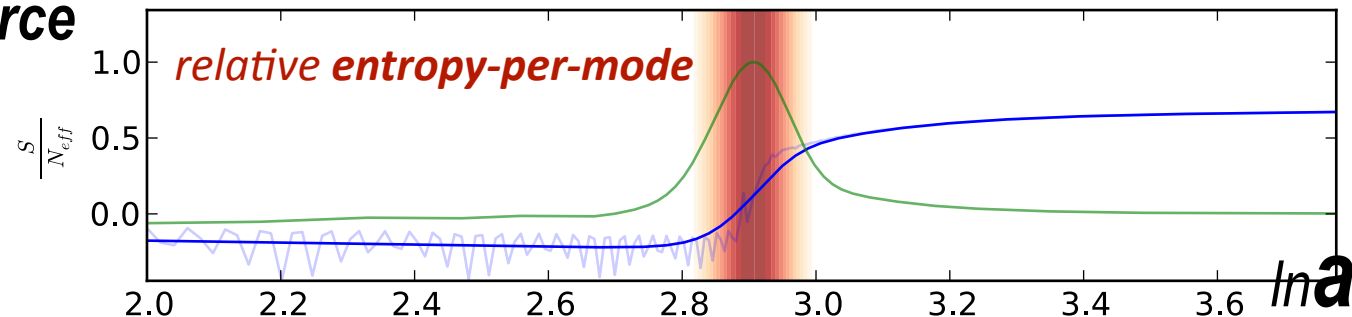
Jump Conditions: $\Delta T^{\mu 0}$

Randomizing mode cascade & Particle Production: ΔS

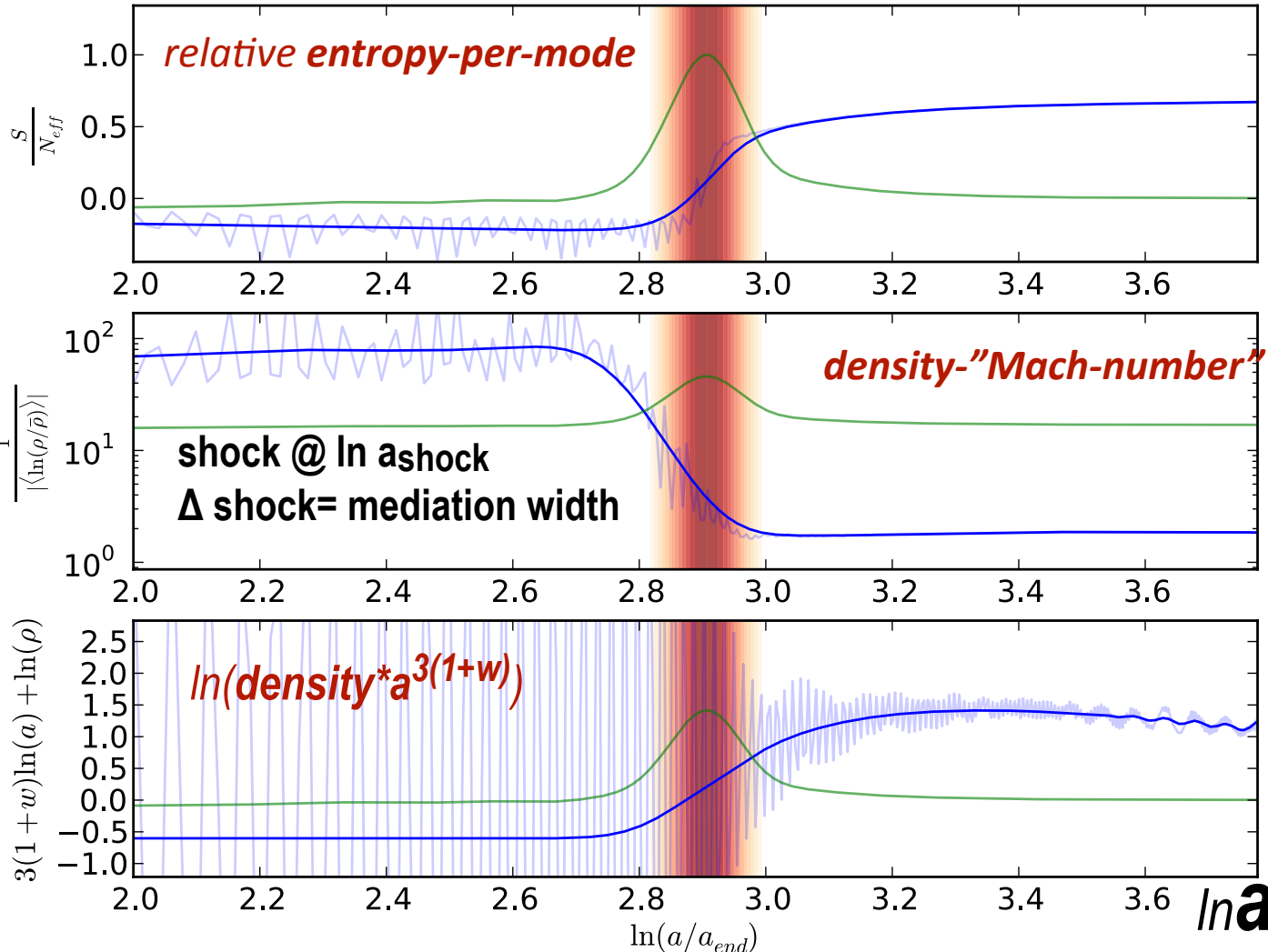
Mediation: width via gradients
and nonlinearities

post-shock evolution, slow, of fluctuations

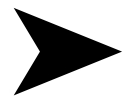
**Preheating is a shockingly
efficient entropy source**



*the Shock-in-time: entropy production, $\langle \ln(\text{density-contrast}) \rangle^{-1}, \ln(\text{density} * a^{3(1+w)})$*



true thermal equilibrium far off



& on to coupling to standard model degrees of freedom

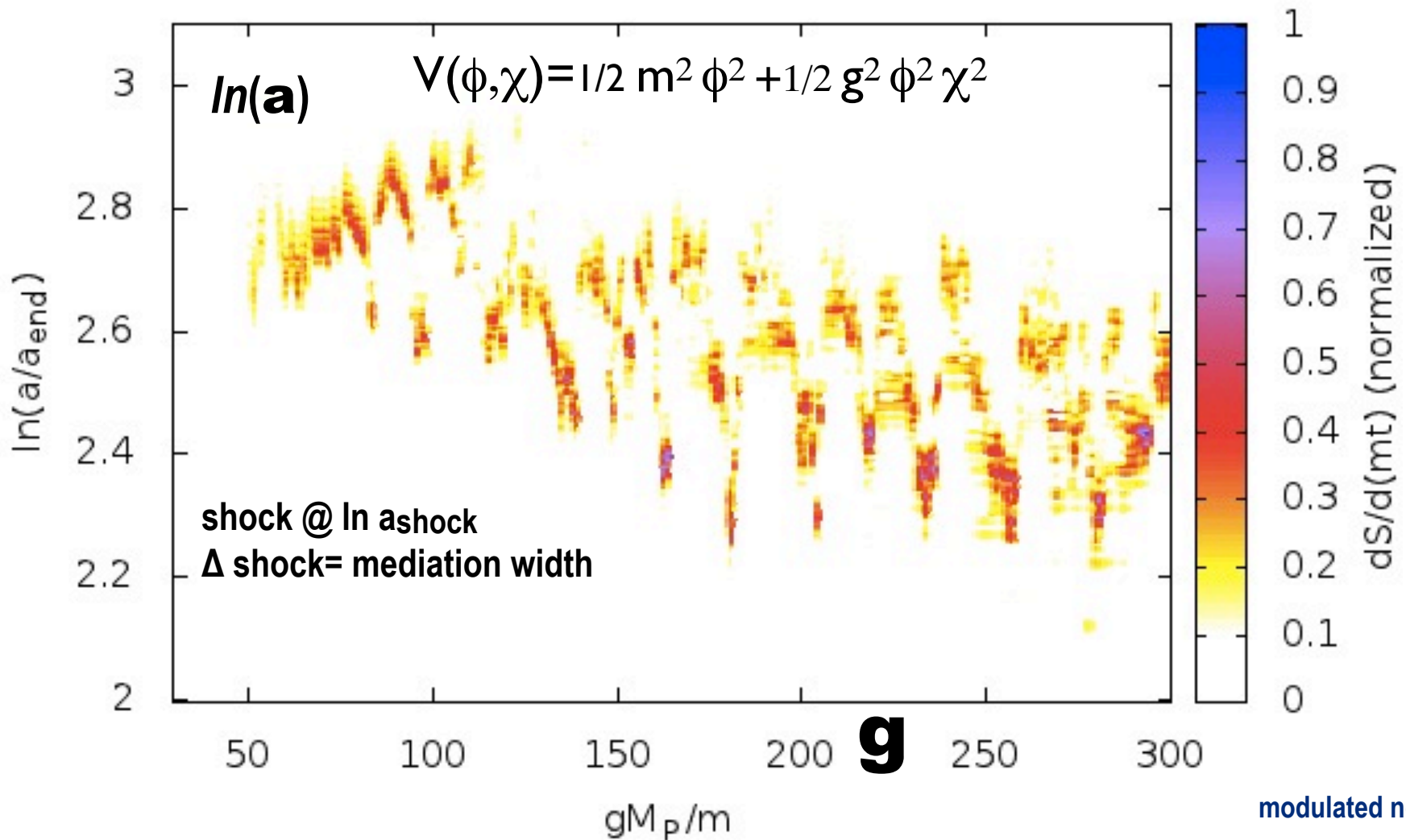
constrained coarse-grained **Shannon-entropy**($\ln a$) minus the initial Gaussian random field entropy (from band-limited quantum fluctuations)
there is indeed a spike of entropy production at the shock front.

$$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2 \chi^2$$

non-Gaussianity (WMAP, Planck, LSS) spiky nG preheating
 B+Braden11

$dS/dt(t, \mathbf{g}) \Rightarrow$ the Shock-in-time: entropy production rate

$\delta \ln a_{\text{shock}}(\mathbf{g}(\sigma(\mathbf{x}))) \Rightarrow$ modulated non-Gaussianity from preheating!



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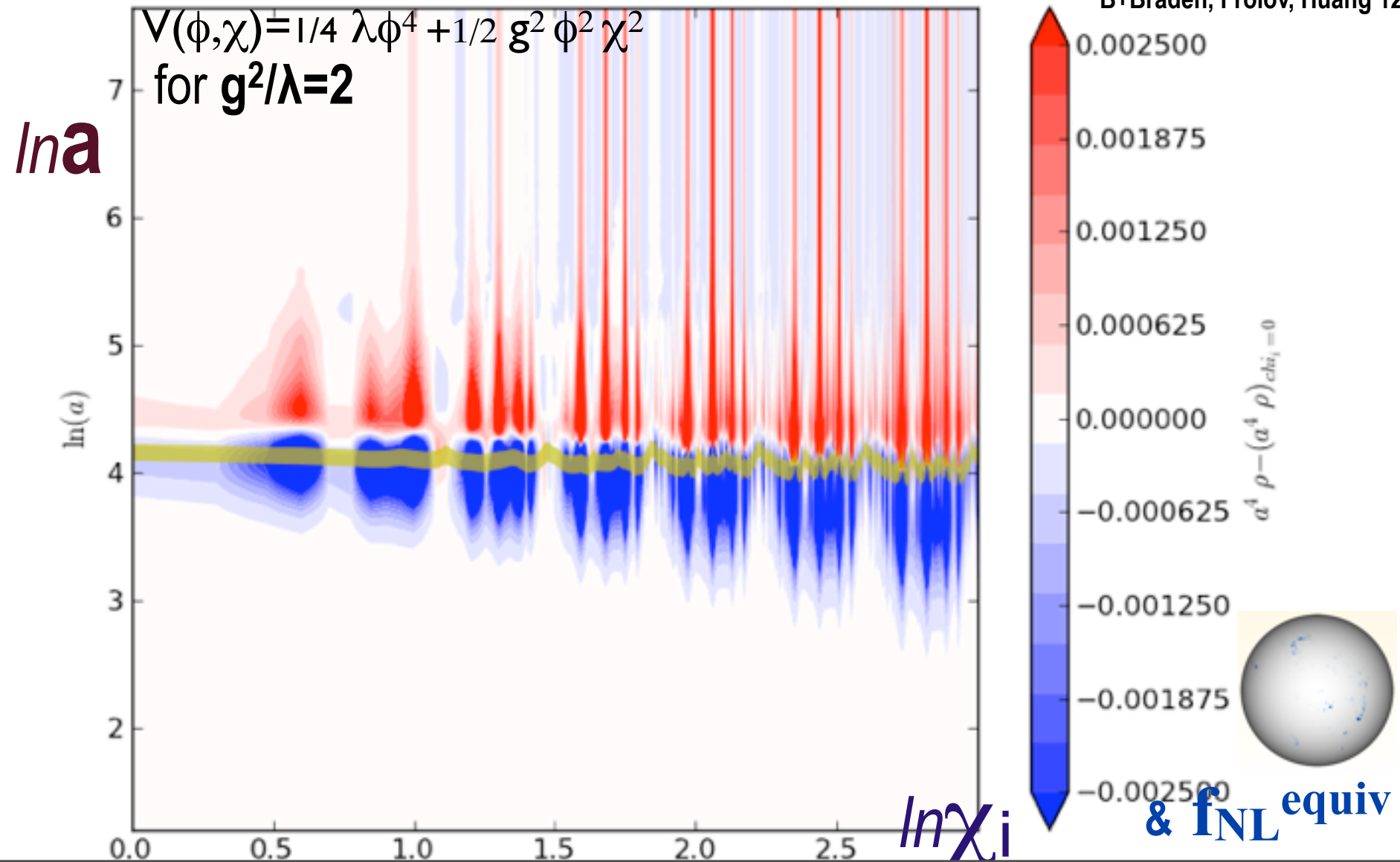
Kofman03

Dvali, Gruzinov+Zaldarriaga03

B+Braden12

$dS/dt(t, g) \Rightarrow$ the Shock-in-time: entropy production rate

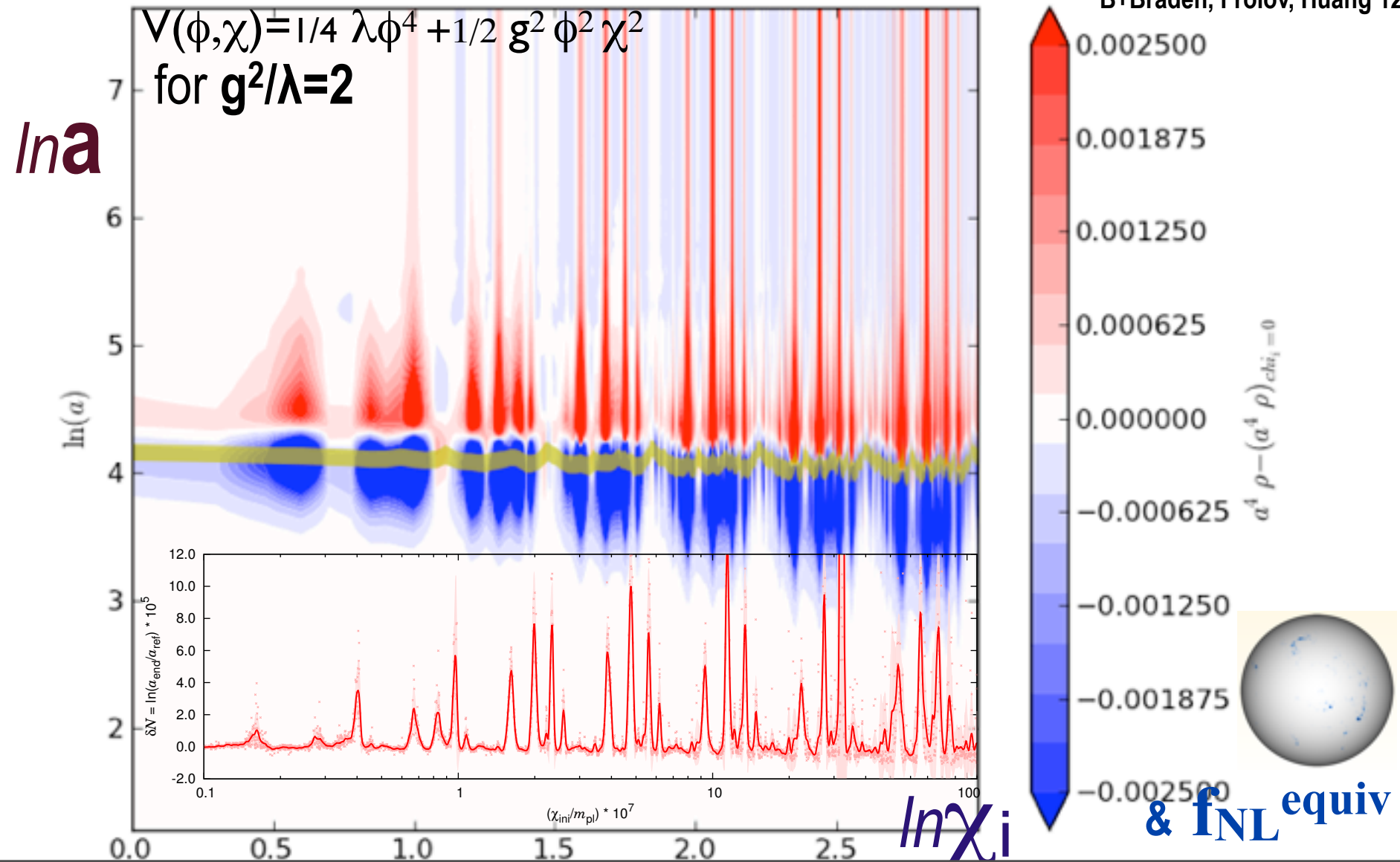
$\delta \ln a_{\text{shock}}(\chi_i(\mathbf{x}) | g^2/\lambda) \Rightarrow$ Chaotic Billiards: NonG from Parametric Resonance in Preheating
 B+Frolov, Huang, Kofman 09
 B+Braden, Frolov, Huang 12



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B+Frolov, Huang, Kofman 09
B+Braden, Frolov, Huang 12



the Shock-in-Times of Post-inflation Preheating B+Braden12

Initial State = Nearly Homogeneous Inflaton

low entropy (coherent ϕ + vac fluctuations), *information encoded in a few parameters*

Preheating

Instabilities result in nonlinear transition to an incoherent state, resonances?

KLS 94, 97, e.g. Tkachev, Felder, Garcia-Bellido, ...

***the shock-in-time is the sharp mediator between the linear & the highly nonlinear transition
a fascinating non-Gaussianity can arise if there is a spatial modulator field varying the shock time***

(Near Adiabatic) Transition Regime

Complex slowly evolving nonlinear, nonequilibrium state e.g. Micha and Tkachev 2004,
turbulence analogy?? ***the evolution is NOT a Kolmogorov-like turbulent cascade to higher modes***

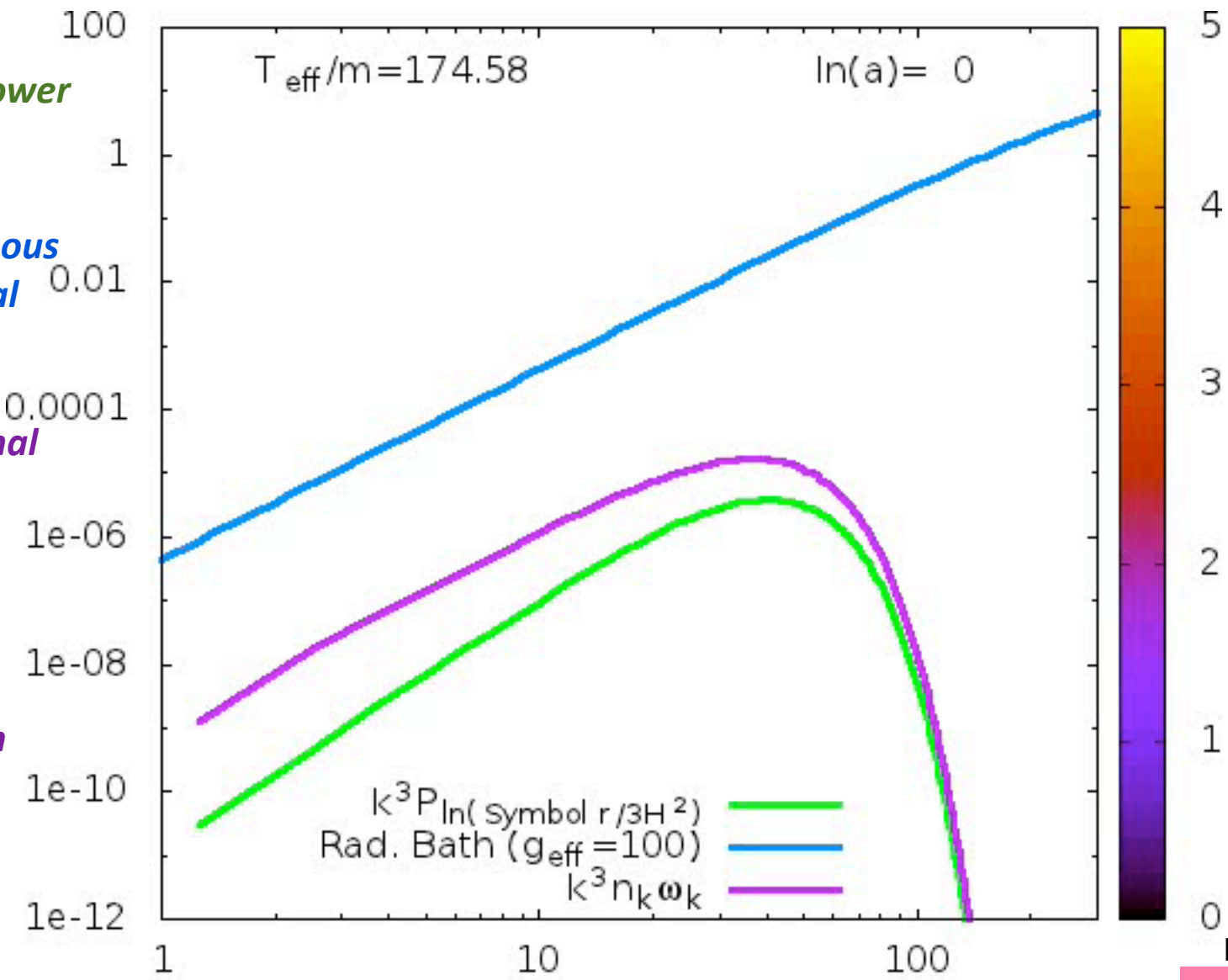
Final State = Thermal Equilibrium

= maximum spreading of information in modes subject to energy & particle number
constraints. *How to couple to standard model dofs to accelerate the power
spectrum evolution to a thermal bose-einstein distribution function?*

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B+Braden12

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Conclusions

BB12 new language for preheating using complex information measures:
the shock-in-time = randomization front, an efficient entropy source

Spatial block RenormGp smoothing indicates that PDF's of fluctuations around local values evolve slowly post-shock

nearly Gaussian PDF for $\ln \rho_k$ & \mathbf{V}_k hydro/phonon regime

Observable preheating nonGaussianities can be encoded in the spatial

structure of the shock-in-time, characterized by $\ln \mathbf{a}_{\text{shock}}(\mathbf{x}) / \mathbf{a}_{\text{end}}$

narrow mediation width. reasonable case made that $\approx \ln \mathbf{a}_{\text{final}}(\mathbf{x}) / \mathbf{a}_{\text{end}}$

generalized nonG from **shock-in-time**(\mathbf{x} | couplings, isocon, ...) TBD fully
explore the potential surface dependence => the **variety of preH nonG B^2FH12**

*phenomenology CMB cold spot /quadratic constraints for preheating nG's; **constrain/detect with PlanckEXT; explore more short-astro-distance exotica of high-k spiky potential pits***

whence opens up the large number of particle dofs & standard model? can this kick in earlier, aka warm inflation. anyway, we are having fun with the high k drain

end