

# Cosmic Rays and Cluster Cosmology: A Critical Review

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in collaboration with

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# Outline

- 1 **Introduction to galaxy clusters**
  - Properties of galaxy clusters
  - Physical processes in simulations
  - Cosmic ray physics
- 2 **Cosmic rays in cosmological simulations**
  - Cosmic ray acceleration
  - Radiative high-resolution cluster simulations
  - Modified X-ray emission and Sunyaev-Zel'dovich effect
- 3 **Cosmological implications of cosmic rays**
  - Modified X-ray scaling relations
  - Fisher matrix analysis
  - Degeneracies of cosmological parameters



# Observational properties of galaxy clusters

Exploring complementary methods for studying cluster formation

Each frequency window is sensitive to different processes and cluster properties:

- **optical**: gravitational lensing of background galaxies, galaxy velocity dispersion measure **gravitational mass**
- **X-ray**: thermal plasma emission,  $F_X \propto n_{\text{th}}^2 \sqrt{T_{\text{th}}} \rightarrow$  **thermal gas with abundances, cluster potential, substructure**
- **Sunyaev-Zel'dovich effect**: IC up-scattering of CMB photons by thermal electrons,  $F_{\text{SZ}} \propto \rho_{\text{th}} \rightarrow$  **cluster velocity, turbulence, high- $z$  clusters**
- **radio synchrotron halos**:  $F_{\text{sy}} \propto \epsilon_B \epsilon_{\text{CRe}} \rightarrow$  **magnetic fields, CR electrons, shock waves**
- **diffuse  $\gamma$ -ray emission**:  $F_{\gamma} \propto n_{\text{th}} n_{\text{CRp}} \rightarrow$  **CR protons**



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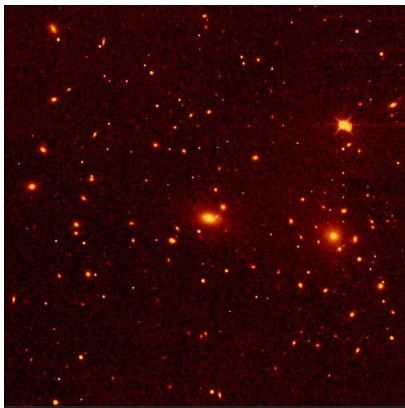


# Coma cluster: member galaxies



optical emission,

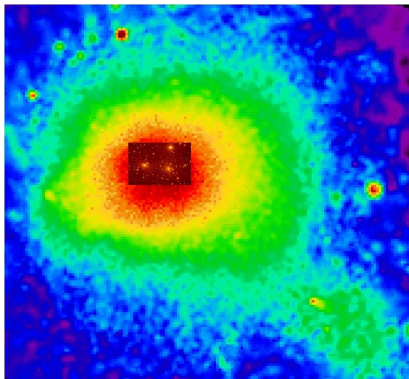
(credit: Kitt Peak)



infra-red emission,

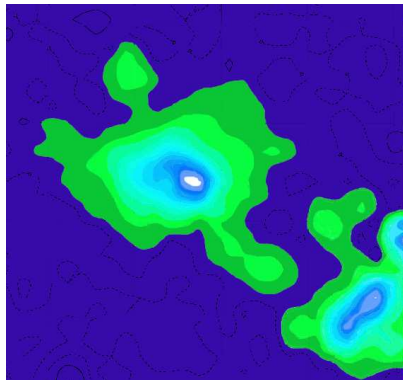
(credit: ISO)

# Coma cluster: (non-)thermal plasma



thermal X-ray emission,

(credit: S.L. Snowden/MPE/ROSAT)



radio synchrotron emission,

(credit: B.Deiss/Effelsberg)



# Dynamical picture of cluster formation

- structure formation in the  $\Lambda$ CDM universe predicts the hierarchical build-up of dark matter halos from small scales to successively larger scales
- clusters of galaxies currently sit atop this hierarchy as the largest objects that have had time to collapse under the influence of their own gravity
- cluster are dynamically evolving systems that have not finished forming and equilibrating,  $\tau_{\text{dyn}} \sim 1 \text{ Gyr}$

→ two extreme dynamical states of galaxy clusters:

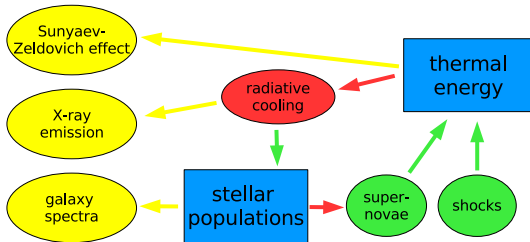
**merging clusters** and **cool core clusters**, which are relaxed systems where the central gas develops a dense cooling core due to the short thermal cooling times



# Radiative simulations – flowchart

Cluster observables:

Physical processes in clusters:

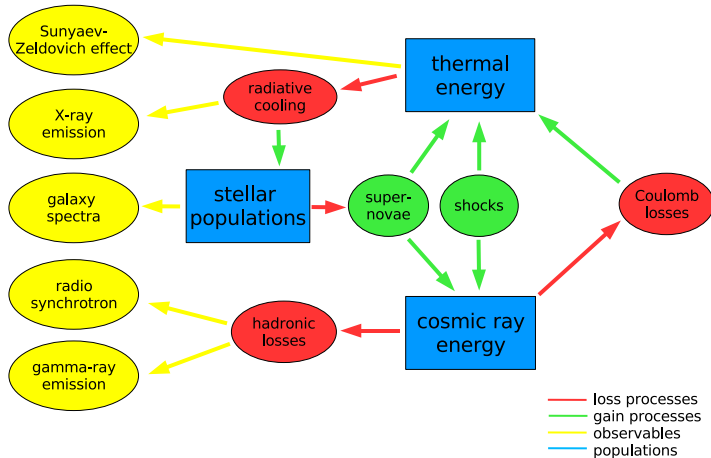


— loss processes  
 — gain processes  
 — observables  
 — populations

# Radiative simulations with cosmic ray (CR) physics

Cluster observables:

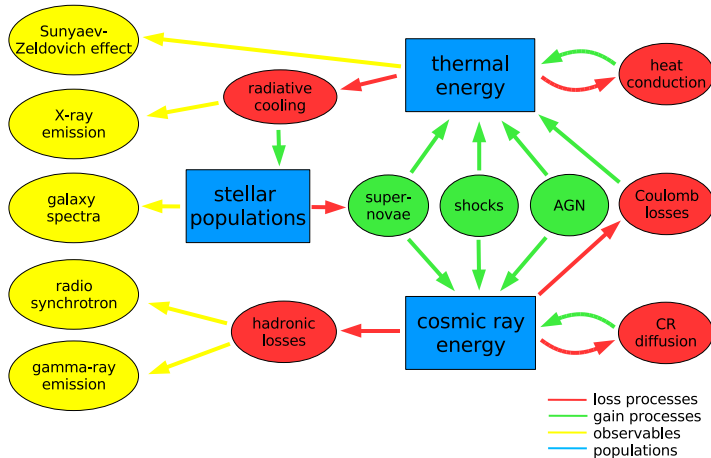
Physical processes in clusters:



# Radiative simulations with extended CR physics

Cluster observables:

Physical processes in clusters:



# Philosophy and description

An accurate description of CRs should follow the evolution of the spectral energy distribution of CRs as a function of time and space, and keep track of their dynamical, non-linear coupling with the hydrodynamics.

## We seek a compromise between

- capturing as many physical properties as possible
- requiring as little computational resources as necessary

## Assumptions:

- protons dominate the CR population
- a momentum power-law is a typical spectrum
- CR energy & particle number conservation



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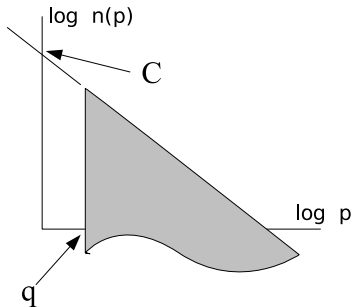
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# CR spectral description



$$p = P_p / m_p c$$

$$f(p) = \frac{dN}{dp dV} = C p^{-\alpha} \theta(p - q)$$

$$q(\rho) = \left( \frac{\rho}{\rho_0} \right)^{\frac{1}{3}} q_0$$

$$C(\rho) = \left( \frac{\rho}{\rho_0} \right)^{\frac{\alpha+2}{3}} C_0$$

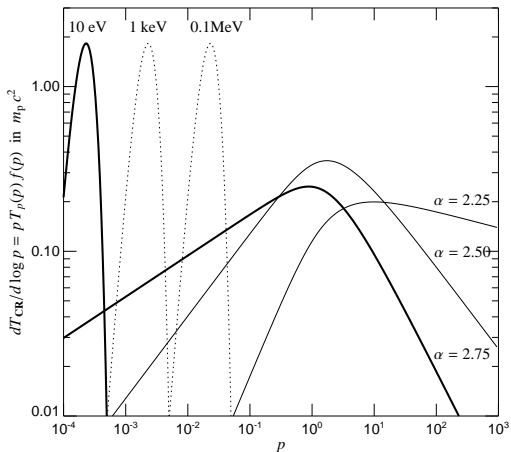
$$n_{\text{CR}} = \frac{C q^{1-\alpha}}{\alpha-1}$$

$$P_{\text{CR}} = \frac{C m_p c^2}{6} \mathcal{B}_{\frac{1}{1+q^2}} \left( \frac{\alpha-2}{2}, \frac{3-\alpha}{2} \right)$$



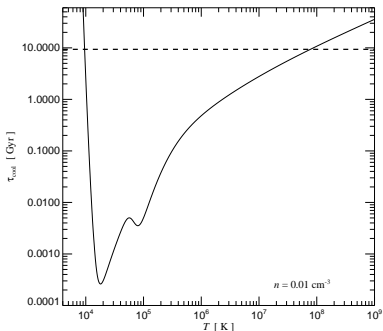
# Thermal & CR energy spectra

Kinetic energy per logarithmic momentum interval:

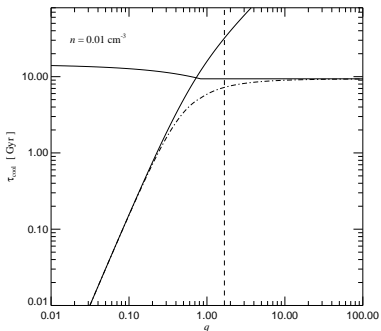


# Radiative cooling

Cooling of primordial gas:



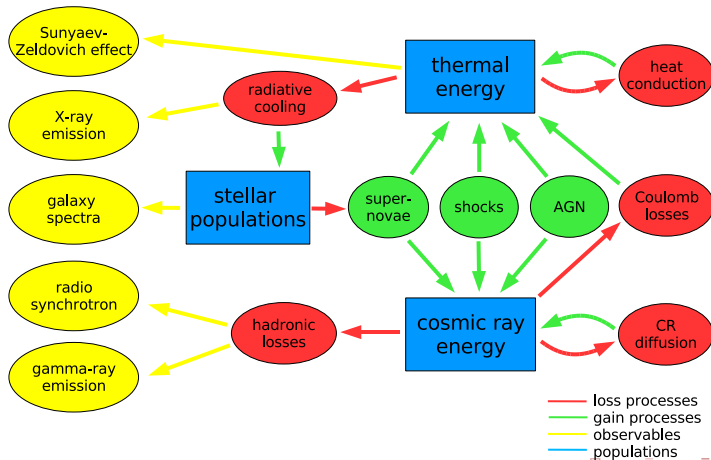
Cooling of cosmic rays:



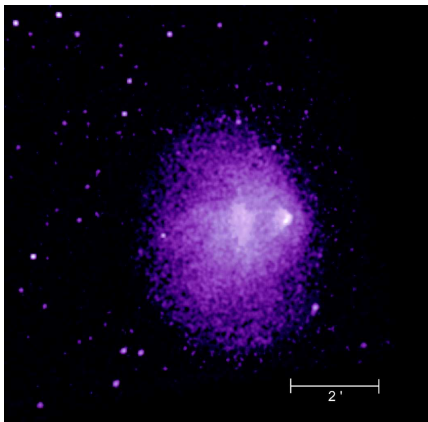
# Cosmic rays in clusters – flowchart

Cluster observables:

Physical processes in clusters:

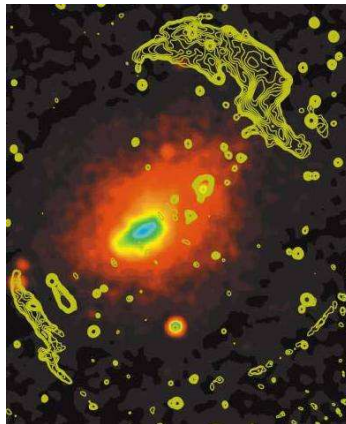


# Observations of cluster shock waves



1E 0657-56 (“Bullet cluster”)

(NASA/SAO/CXC/M.Markevitch et al.)



Abell 3667

(radio: Austr.TC Array. X-ray: ROSAT/PSPC.)

# Diffusive shock acceleration – Fermi 1 mechanism (1)

## conditions:

- a collisionless shock wave
- magnetic fields to confine energetic particles
- plasma waves to scatter energetic particles → particle diffusion
- supra-thermal particles

## mechanism:

- supra-thermal particles diffuse upstream across shock wave
- each shock crossing energizes particles through momentum transfer from recoil-free scattering off the macroscopic scattering agents
- momentum increases exponential with number of shock crossings
- number of particles decreases exponential with number of crossings

→ power-law CR distribution



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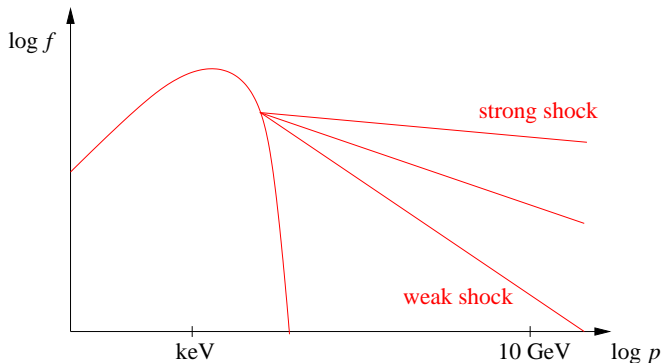
→ power-law CR distribution



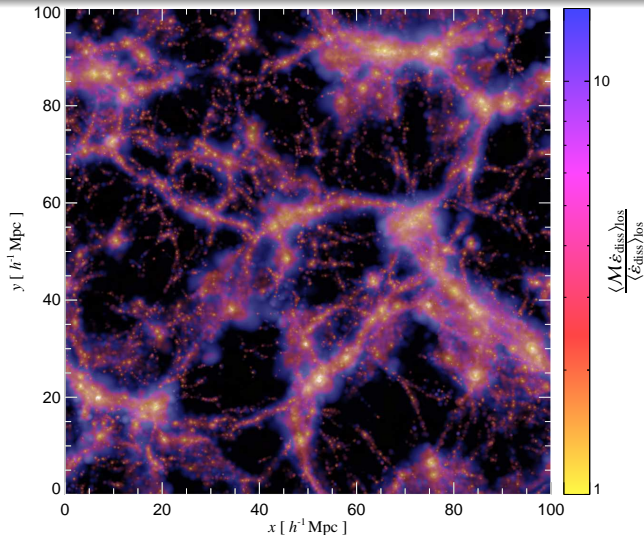
# Diffusive shock acceleration – Fermi 1 mechanism (2)

Spectral index depends on the Mach number of the shock,

$$\mathcal{M} = v_{\text{shock}}/c_s:$$

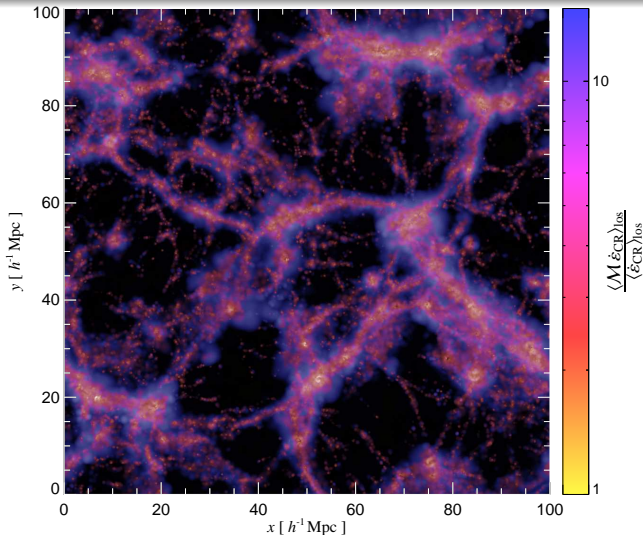


# Cosmological Mach numbers: weighted by $\varepsilon_{\text{diss}}$

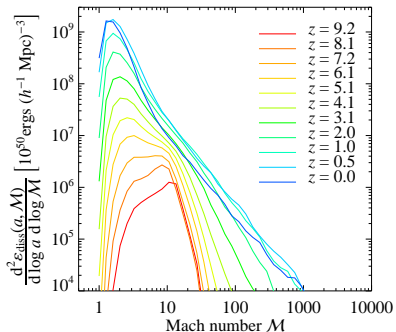




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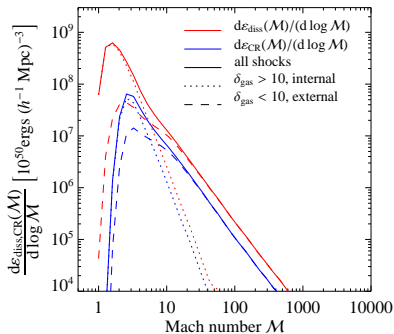
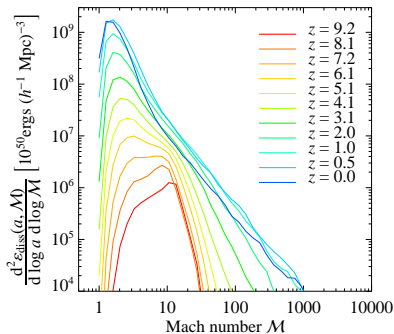


# Cosmological Mach number statistics



- more energy is dissipated at later times
- mean Mach number decreases with time

# Cosmological statistics: CR acceleration



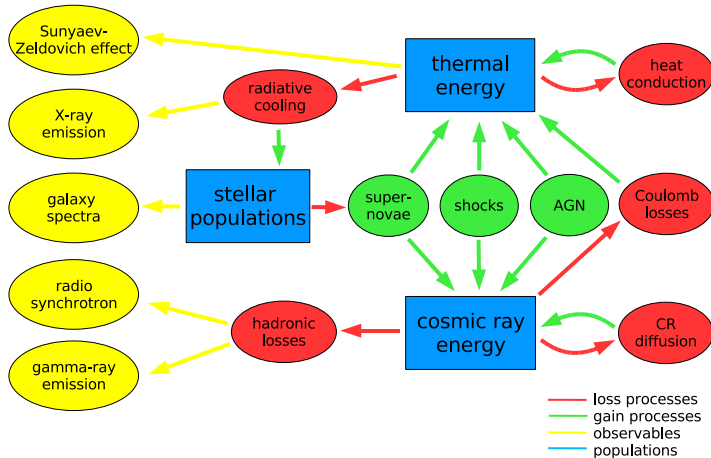
- more energy is dissipated in weak shocks internal to collapsed structures than in external strong shocks
- non-radiative simulations: injected CR energy inside cluster makes up only a small fraction of the total dissipated energy



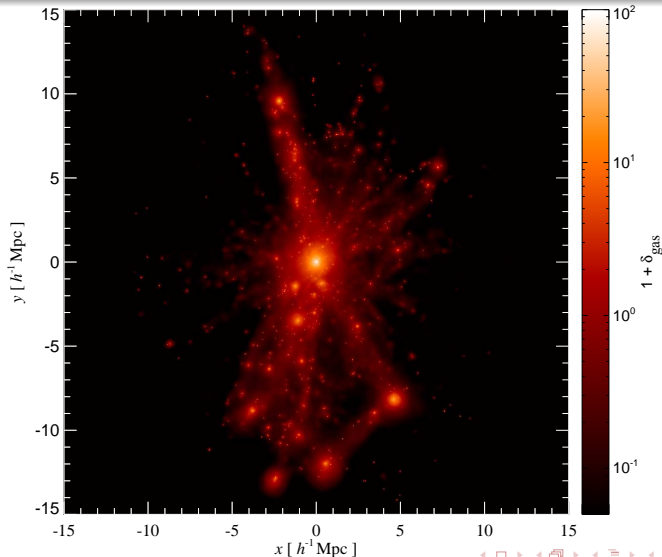
# Radiative simulations with extended CR physics

Cluster observables:

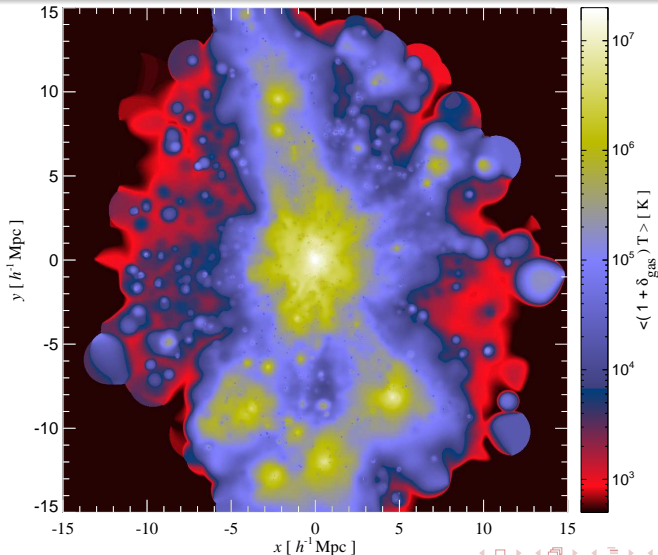
Physical processes in clusters:



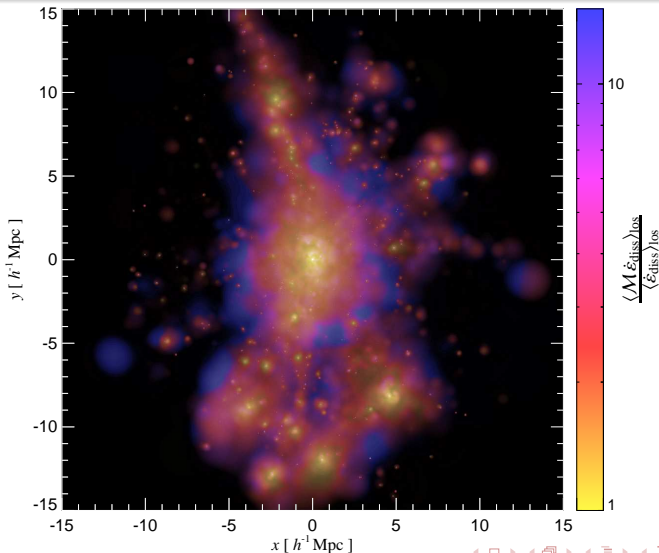
# Radiative cool core cluster simulation: gas density



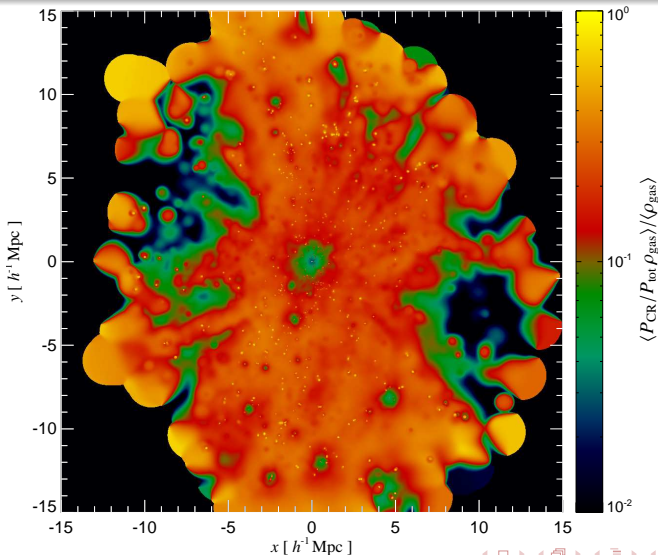
# Mass weighted temperature



# Mach number distribution weighted by $\varepsilon_{\text{diss}}$

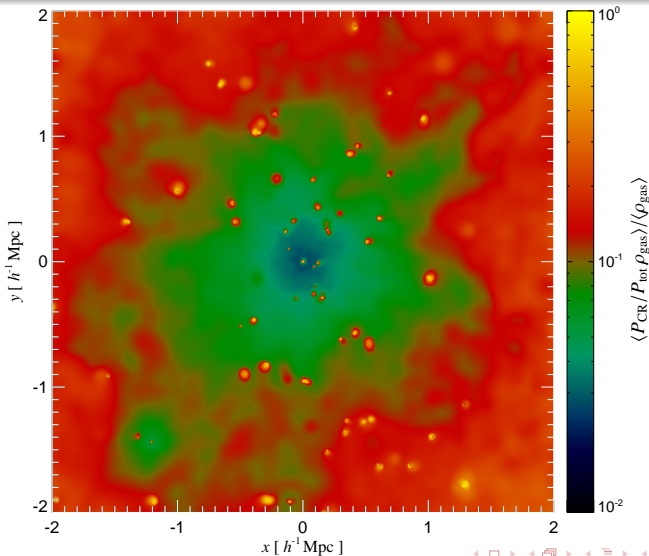


# Relative CR pressure $P_{\text{CR}}/P_{\text{total}}$

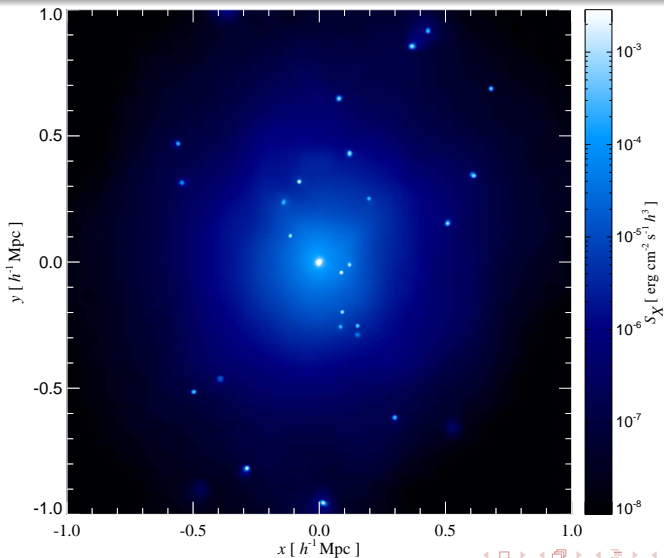




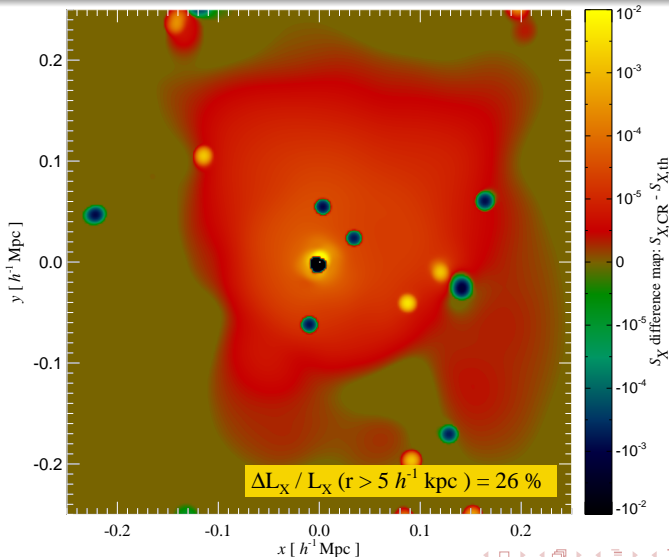
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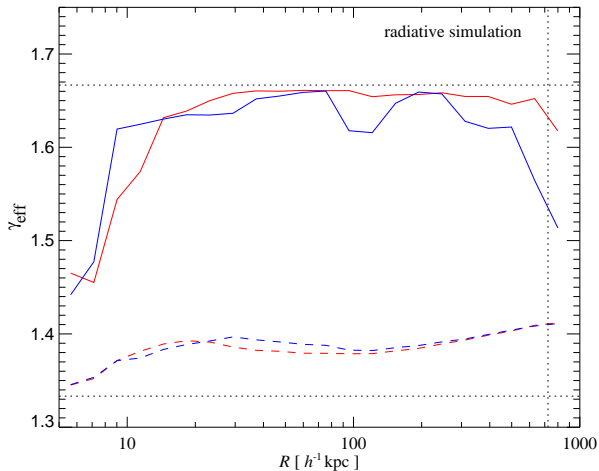
# Thermal X-ray emission



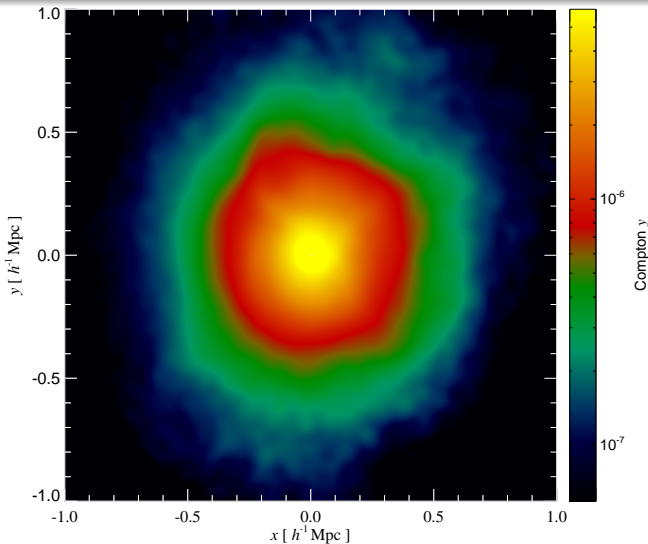
# Difference map of $S_X$ : $S_{X,CR} - S_{X,th}$



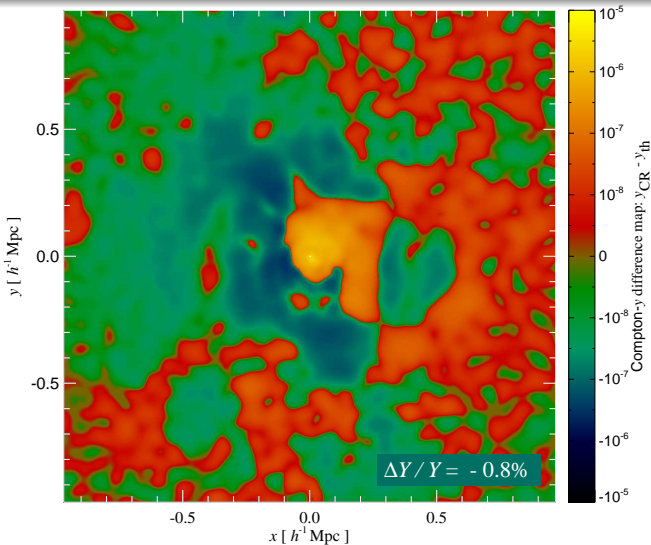
# Softer effective adiabatic index of composite gas



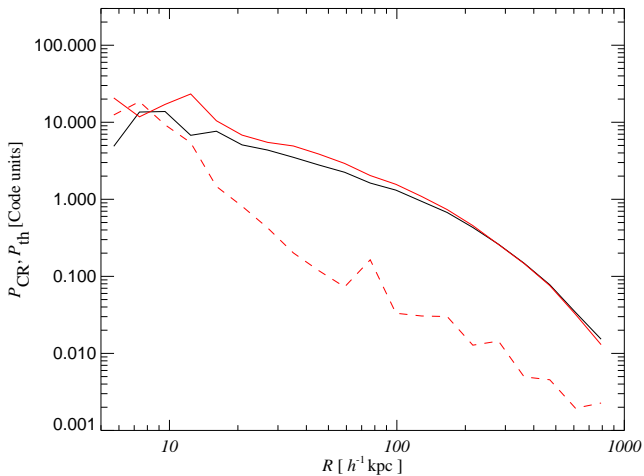
# Compton $y$ parameter in radiative cluster simulation



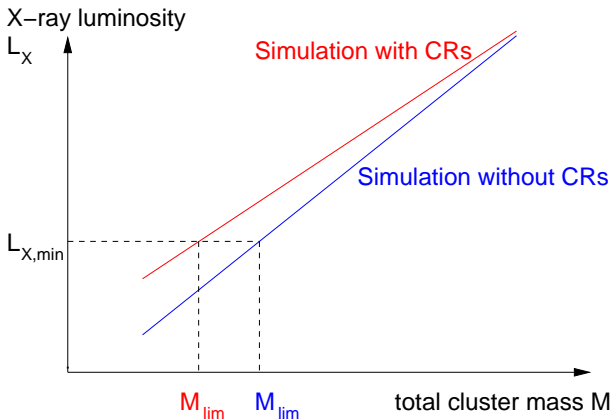
# Compton $y$ difference map: $y_{\text{CR}} - y_{\text{th}}$



# Pressure profiles with and without CRs



# Modified X-ray scaling relations



→ CR feedback lowers the effective mass threshold for X-ray flux-limited cluster sample

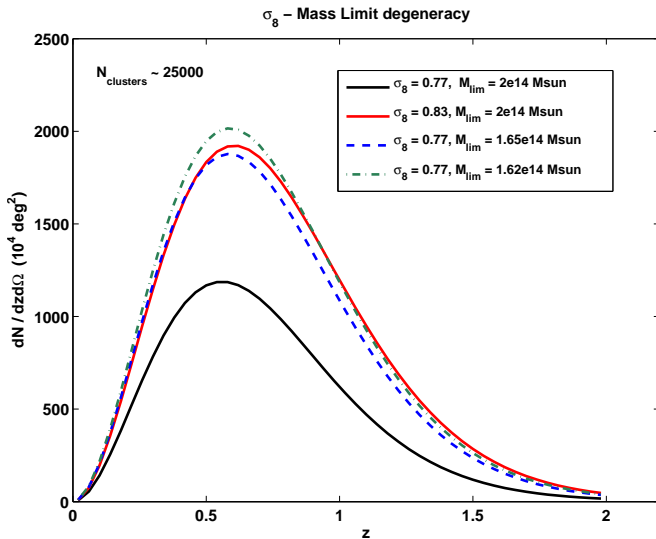


# Degeneracies of the cluster redshift distribution (1)

- The number density of massive clusters is exponentially sensitive to the amplitude of the initial Gaussian fluctuations, whose normalization we usually describe using  $\sigma_8$ , the *rms* fluctuations of overdensity within spheres of  $8 h^{-1}$  Mpc.
- The cluster redshift distribution  $dn/dz$  is increased by a lower effective mass threshold  $M_{\text{lim}}$  in a survey or by increasing  $\sigma_8$  respectively  $\Omega_m \rightarrow$  degeneracies of cosmological parameters with respect to cluster physics.



# Degeneracies of the cluster redshift distribution (2)



# Fisher matrix analysis (1)

Survey Fisher matrix information for a data set:

$$F_{ij} \equiv - \left\langle \frac{\partial^2 \ln \mathcal{L}}{\partial p_i \partial p_j} \right\rangle = \sum_n \frac{\partial N_n}{\partial p_i} \frac{\partial N_n}{\partial p_j} \frac{1}{N_n},$$

where  $\mathcal{L}$  is the likelihood for an observable (proportional to  $dN/dz$  for the redshift distribution),  $p_i$  describes our parameter set, the sum extends over the redshift bins, and  $N_n$  represents the number of surveyed clusters in each redshift bin  $n$  (statistically independent, Poisson distributed).

The inverse  $F_{ij}^{-1}$  describes the best attainable covariance matrix  $[C_{ij}]$  (assuming Gaussianity) for measurement of the parameters considered. The diagonal terms of  $[C_{ij}]$  then give the uncertainties of each of our parameters.



## Fisher matrix analysis (2)

### Assumed survey details:

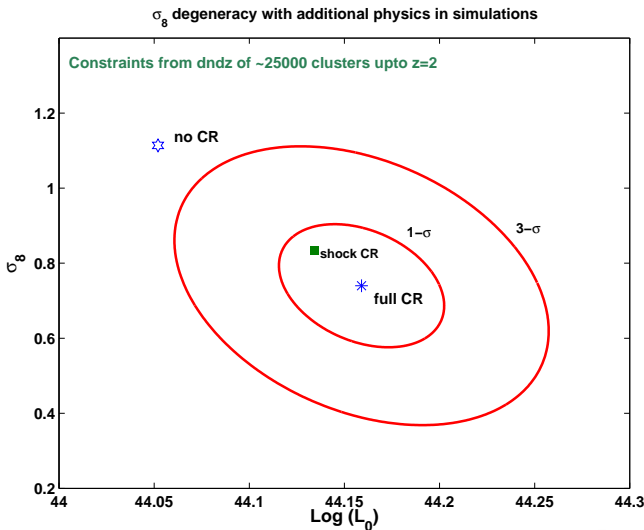
- survey area  $A = 10^4$  square degrees (1/4 of the sky)
- redshift range:  $0 < z < 2$
- bolometric X-ray flux limit  $F_X = 2.5 \times 10^{-13}$  erg s $^{-1}$  cm $^{-2}$
- sample size: 25000 clusters

### Fisher matrix preliminaries:

- free parameters: 2 parameters of the scaling relations:  
slope and normalization,  $\Omega_m$ ,  $\Omega_b$ ,  $n_s$ ,  $h$ ,  $\sigma_8$
- priors: flat Universe, WMAP prior on  $h = 72 \pm 5$



# Degeneracy of $\sigma_8$ with cosmic ray physics (preliminary)



# Summary

CR physics modifies the intracluster medium in merging clusters and cooling core regions:

- Galaxy cluster **X-ray emission is enhanced** up to 35%, systematic effect in low-mass cooling core clusters.
- Integrated **Sunyaev-Zel'dovich effect** remains largely unchanged while the Compton- $y$  profile is more peaked.
- Cosmological parameters such as  $\sigma_8$  and  $\Omega_m$  as derived from clusters **are degenerate with cluster parameters**.
- Understanding **non-thermal processes** is crucial for using clusters as cosmological probes (high- $z$  scaling relations).

