

# High-Energy Phenomena and Dark Matter Searches in Galaxy Clusters

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in collaboration with

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# Outline

- 1 **Introduction to dark matter**
  - Properties of dark matter
  - Theory and observations
  - Recent exciting developments
- 2 **Indirect dark matter searches**
  - Our approach
  - Gamma-ray signatures
  - Implications for cosmological structure formation
- 3 **High-energy phenomena**
  - Cosmological simulations with cosmic rays
  - Shocks and particle acceleration
  - Non-thermal emission from clusters



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# Properties of dark matter

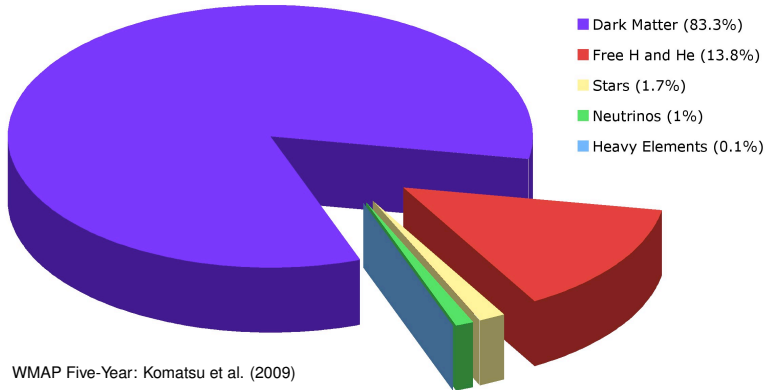
## What have galaxy clusters taught us about dark matter?

Dark matter exists and is ...

- ... **gravitationally interacting**: most of the matter in the Universe is dark (galaxy clusters, galactic rotation curves, gravitational lensing, CMB, ...)



# The matter content of the Universe – 2009



# Zwicky: first evidence for dark matter



- Zwicky (1933) applied the virial theorem to the Coma cluster of galaxies:

$$E_{\text{grav}} + 2E_{\text{kin}} = 0$$

- $E_{\text{kin}}$ : energy based on galaxies motions,  
 $E_{\text{grav}}$ : estimated gravitational energy
  - Zwicky found about 400 times more estimated mass than visually observable
- “missing mass problem”: the gravity of the visible galaxies in the cluster would be far too small for such fast orbits:
- there must be some non-visible form of matter that provides enough of the mass and gravity to hold the cluster together

# Properties of dark matter

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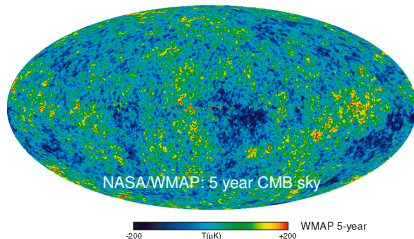
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- ... **non-baryonic**: it does not interact electro-magnetically with ordinary matter (CMB + structure formation)





# Evidence for non-baryonic dark matter

- temperature fluctuations the epoch of recombination ( $z \simeq 1100$ ) have an amplitude  $\delta T/T \simeq 10^{-5}$
- linear regime of structure formation:  $\delta(z) \propto 1/(1+z)$
- if dark matter were baryonic, we would only have time to grow fluctuations of size  $\delta \simeq 10^{-2}$
- since we observe galaxies with  $\delta \gtrsim 10^2$ , dark matter fluctuations must have started to grow before recombination which is only possible **if dark matter does not interact electro-magnetically with matter**



# Properties of dark matter

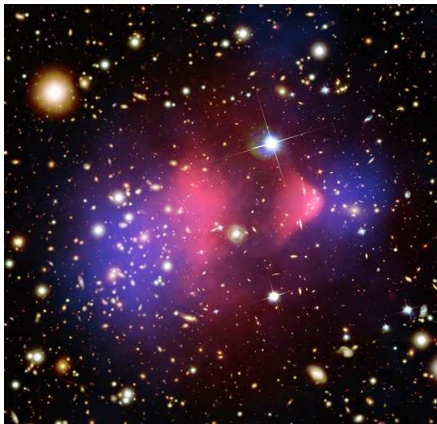
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- ... **collisionless**: it has a very weak self-interaction cross section (galaxy clusters, relic density)



# Evidence for collisionless dark matter



1E 0657-56 (“Bullet cluster”)

(X-ray: NASA/CXC/CfA/M.Markevitch et al.; Optical:  
NASA/STScI; Magellan/U.Arizona/D.Clowe et al.; Lensing:  
NASA/STScI; ESO WFI; Magellan/U.Arizona/D.Clowe et al.)

- **red:** X-ray emitting cluster plasma
- **blue:** weak lensing (dark matter) map
- **yellow:** galaxies

the (collisionless) galaxies follow the dark matter distribution, the bulk of the plasma lags behind

→ **dark matter is collisionless**



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# Properties of dark matter

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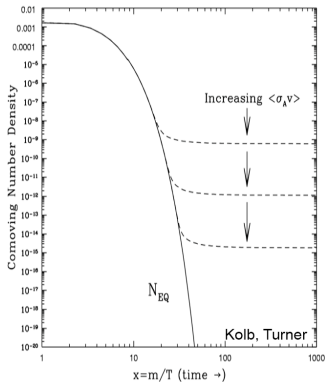
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→ dark matter is a weakly interacting massive particle (WIMP), but what is it really (SUSY, extra dimensions, ...)?



# The WIMP miracle



- Fermi introduced a new mass scale of  $m_{\text{weak}} \sim 100 \text{ GeV}$  to describe the beta decay:  $n \rightarrow p e^- \bar{\nu}$
- assuming a new (heavy) particle  $X$ , initially in thermal equilibrium, with a relic density

$$\Omega_X \sim \frac{1}{m_{\text{Pl}} T_0 \langle\sigma v\rangle} \sim \frac{m_X^2}{m_{\text{Pl}} T_0 g_X^4}$$

- 

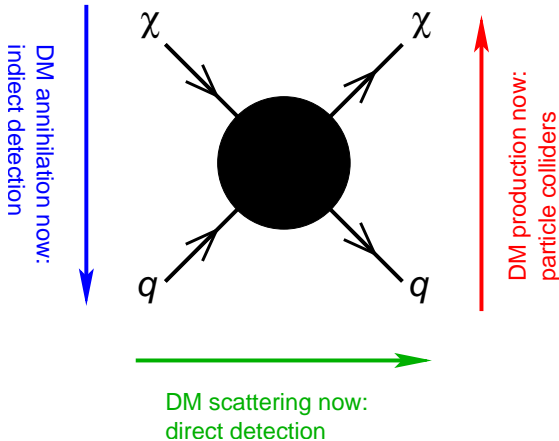
$$\left. \begin{array}{l} m_X \sim m_{\text{weak}} \sim 100 \text{ GeV} \\ g_X \sim g_{\text{weak}} \sim 0.6 \end{array} \right\} \Omega_X \sim 0.1$$

- Remarkable coincidence: particle physics independently predicts particles with the right density to be dark matter

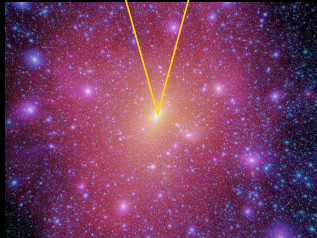
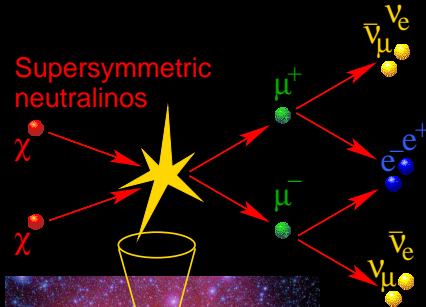


# WIMP detection

Correct relic density  $\rightarrow$  DM annihilation in the Early Universe

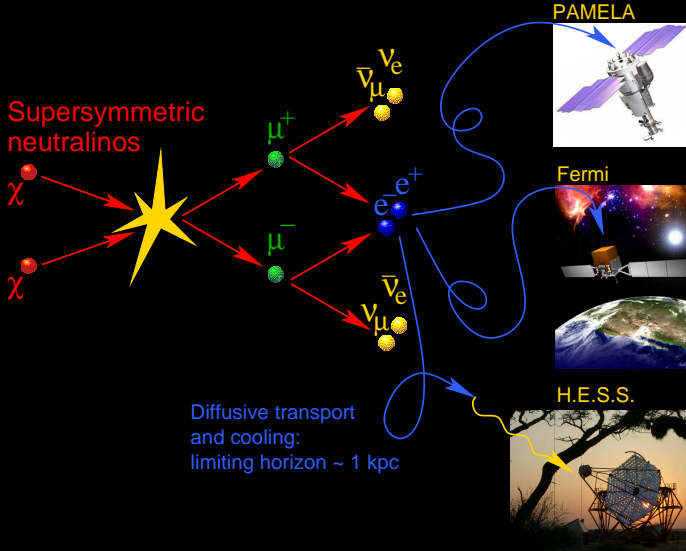


# Indirect detection of dark matter



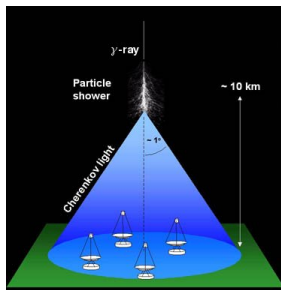
Springel et al. 2008

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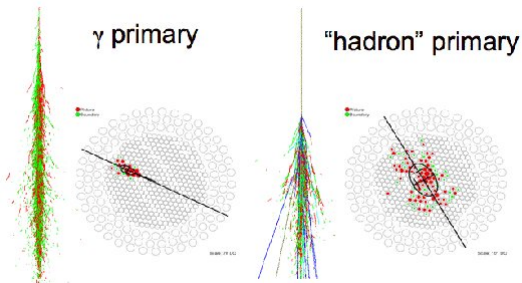
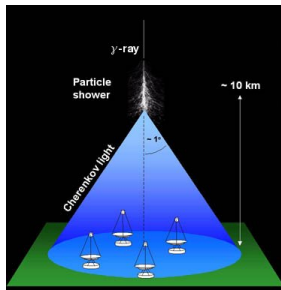


# Imaging air Čerenkov telescopes – the technique (1)



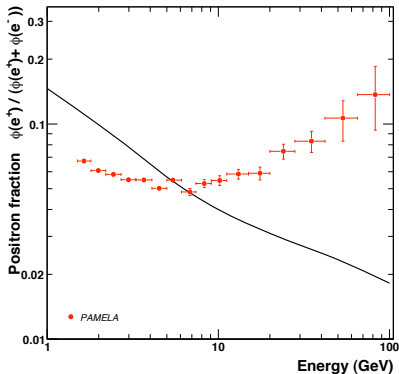
- high-energy  $\gamma$ -ray impacts the Earth's atmosphere and sets off an electro-magnetic cascade in the vicinity of a nucleus
- $e^+ / e^-$  travel faster than the speed of light in the atmosphere  $\rightarrow$  emission of a cone of blue Čerenkov light

# Imaging air Čerenkov telescopes – the technique (2)



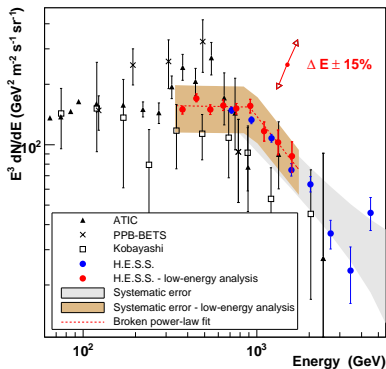
- primary  $\gamma$ -rays and hadrons cause different shower characteristics  $\rightarrow$  separation of  $\gamma$ -rays from 'background' events
- opening angle and shower location in the shower image allows reconstructing the initial energy and direction of the  $\gamma$ -ray

# PAMELA and HESS data on electrons and positrons



**PAMELA:** (Adriani et al. 2009)

rising positron fraction with energy  
 $\rightarrow e^-/e^+$  pair acceleration source



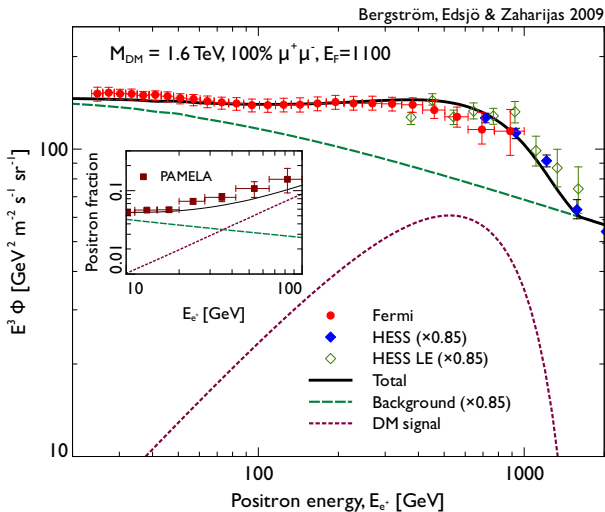
**HESS:** (Aharonian et al. 2009)

break in the  $e^-/e^+$  spectrum  
 $\rightarrow$  maximum voltage of accelerator  
 or DM particle mass



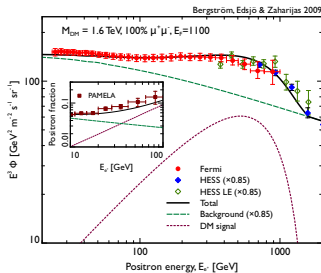
# Combining recent electron and positron data

Fermi: excess number of leptons compared to background model (Abdo et al. 2009)



# Interpretations of recent electron and positron data

- **excess number of leptons** compared to background (Fermi/HESS)
- **break in the  $e^-/e^+$  spectrum** indicates special energy scale (HESS)
- **rising positron fraction** with energy (PAMELA)



## 1.) nearby pulsars:

energetics convincing but smoothness of Fermi data was claimed to be difficult to model (Harding & Ramaty 1987, Aharonian et al 1995, Malyshev et al. 2009)

## 2.) DM annihilations:

excellent fit to data but enhancement of cross-section over standard value and muon decay channel necessary (Bergström et al. 2009)

→ Sommerfeld enhancement:  $\langle \sigma v \rangle \sim C/v$  (Arkani-Hamed et al. 2009)



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# The key questions

- How can we test this scenario?
- Which are the most promising objects to target?
- What are the cosmological implications of such an effective dark matter annihilation?

I will argue in favor of **gamma-ray observations of galaxy clusters** being able to scrutinize the DM interpretation of Fermi/HESS/PAMELA data and will end with a **surprising cosmological result**.

Pinzke, CP, Bergström, Phys. Rev. Lett., 2009, 103, 181302



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# Dissecting the dark matter flux

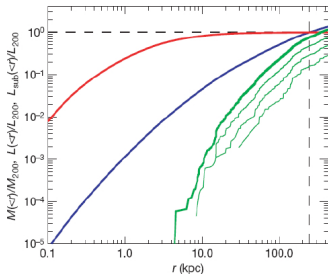
$$N_\gamma = \left[ \int_{\text{LOS}} \rho_\chi^2 d l_\chi \right] \frac{\langle \sigma v \rangle}{2M_\chi^2} \left[ \int_{E_{\text{th}}}^{M_\chi} \left( \frac{dN_\gamma}{dE} \right)_{\text{SUSY}} A_{\text{eff}}(E) dE \right] \frac{\Delta\Omega}{4\pi} \tau_{\text{exp}}$$

- **astrophysics**: contains the uncertainty about the DM profile with its central behavior and the substructure distribution
- **particle physics**: assuming DM is supersymmetric, there is the uncertainty about the cross section, neutralino mass, and decay channels
- **detector properties**: energy dependent effective area, detector response, scanning strategy, ...



# Boost factors

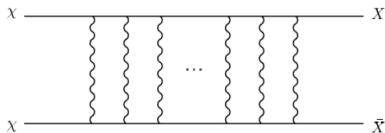
## Substructures:



$$N = (M_{\text{min}}/M_{\text{lim}})^{0.226}$$

Springel *et al.*, Nature **456N7218** 73 (2008)

## Sommerfeld:



$$\langle \sigma v \rangle \approx \langle \sigma v \rangle_0 \times (c/v)$$

$$v = 960 \text{ km/s} \times (M_{200}/10^{15} M_{\odot})^{1/3}$$

# Galaxy clusters vs. dwarf galaxies

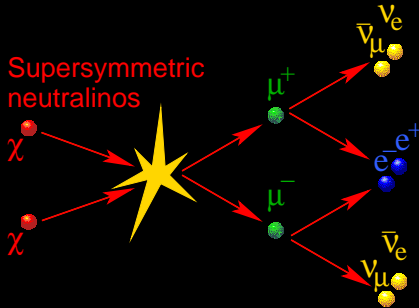
Why look for clusters in the  $\gamma$ -ray band?

- 1 The DM annihilation flux of the smooth halo component scales as  $F \sim \int dV \rho^2 / D^2 \sim M / D^2$  assuming a universal density scaling<sup>1</sup>: **the smooth component of dwarfs and galaxy clusters are equally bright!**
- 2 Substructure in dark matter halos is less concentrated compared to the smooth halo component (dynamical friction, tidal heating and disruption): **the DM luminosity is dominated by substructure at the virial radius, IF present!**
  - these regions are **tidally stripped in dwarf galaxies**
  - galaxy clusters are dynamically 'young' and their **subhalo population can boost the DM luminosity by up to 200**  
(Springel et al. 2008).

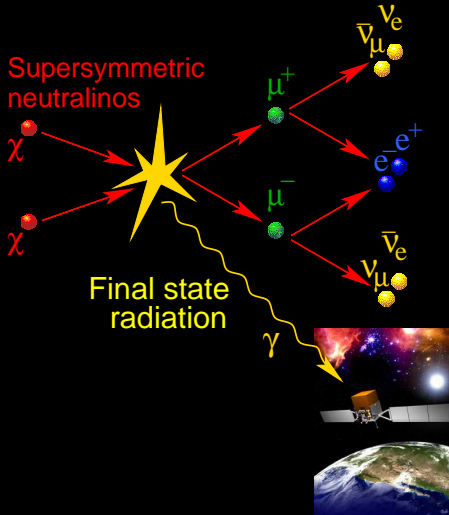
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<sup>1</sup>A more refined argument that takes into account the different halo formation epochs breaking scale invariance yields the same result.

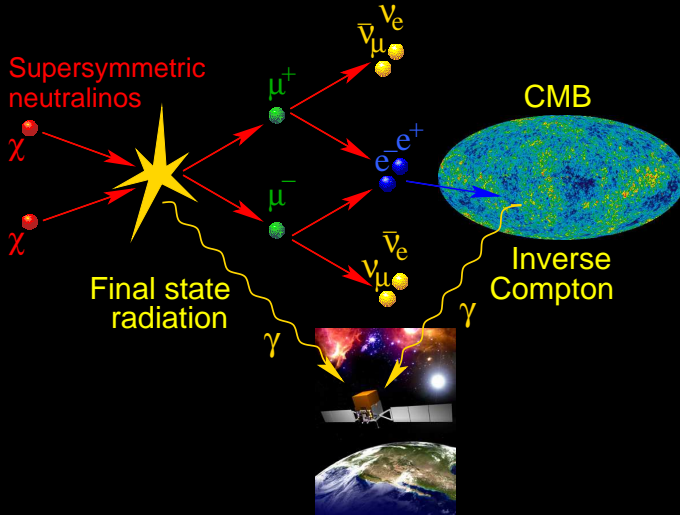
# Indirect detection of DM through gamma-rays



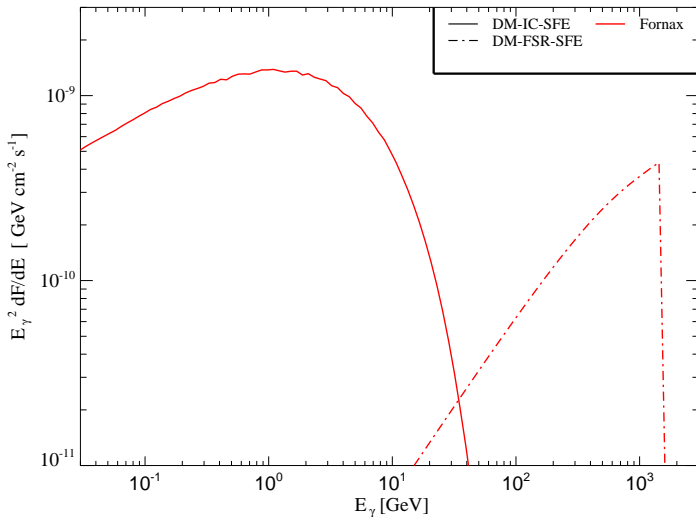
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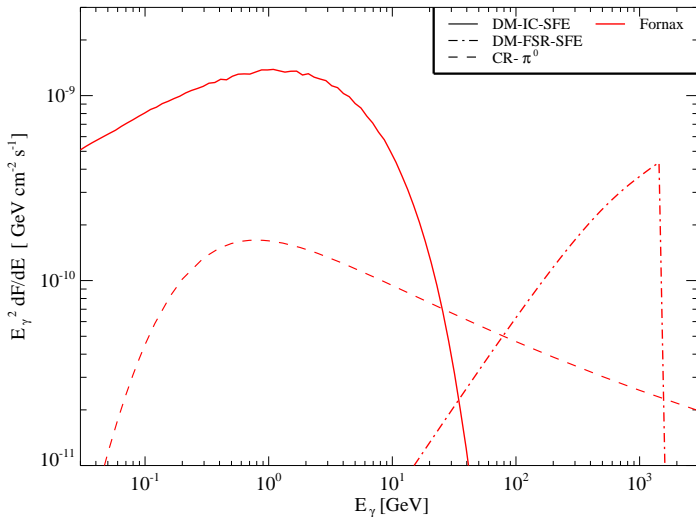
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# Gamma-ray spectrum from DM annihilations

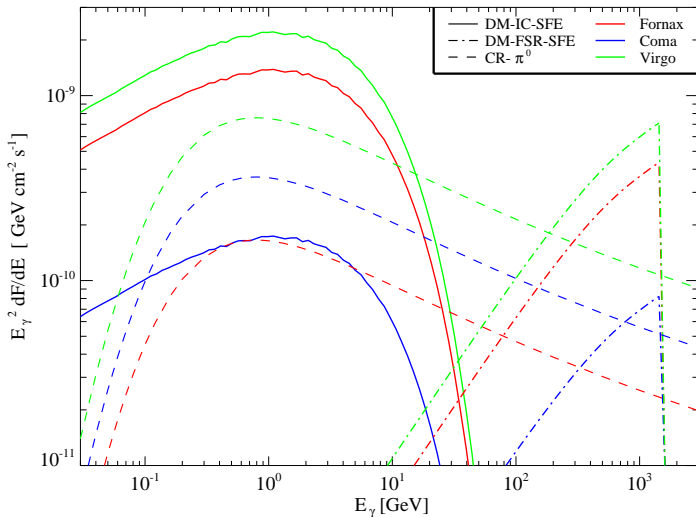


# Gamma-ray spectrum from DM vs. CR interactions

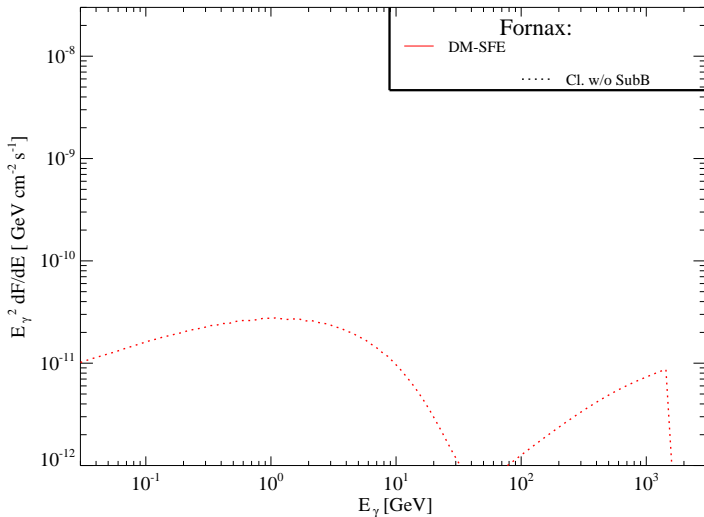




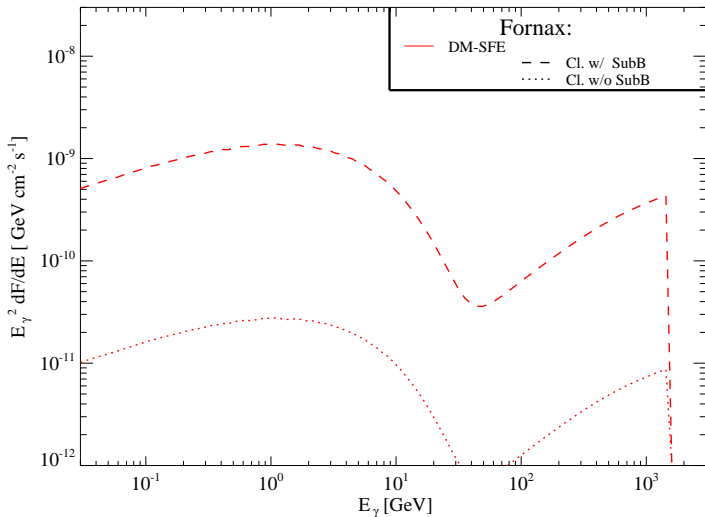
# Gamma-ray spectrum for various galaxy clusters



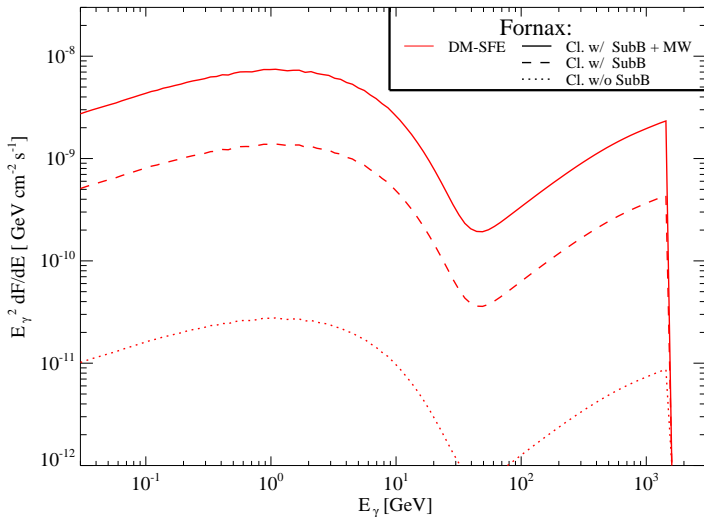
# DM gamma-rays: without substructure



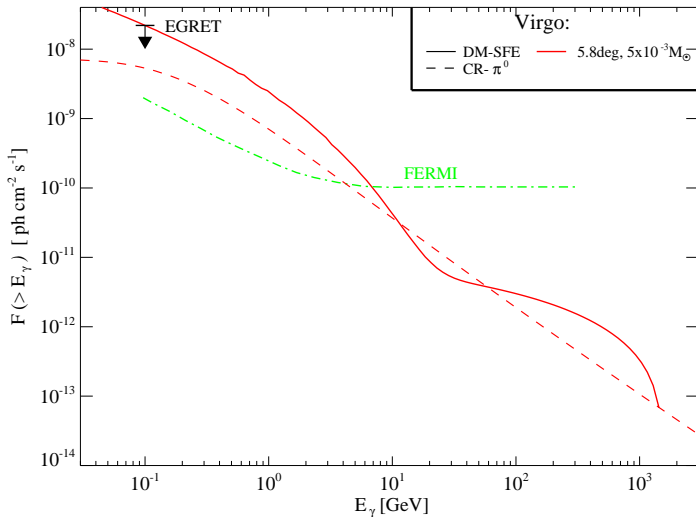
# DM gamma-rays: with substructure



# DM gamma-rays: with substructure and Milky Way

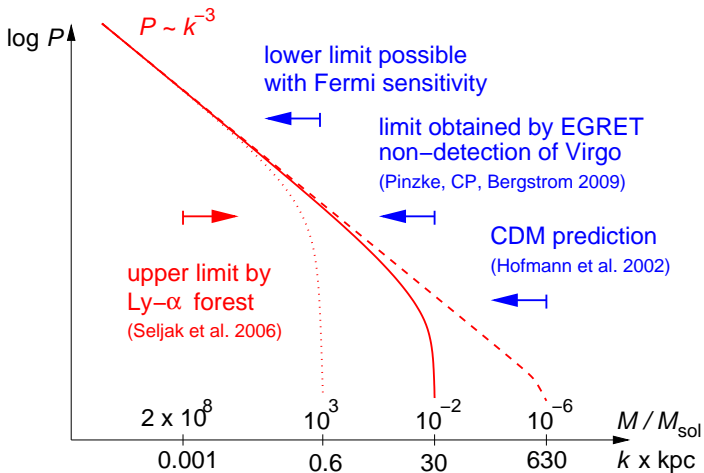


# Probing small scales with gamma-rays



# Implications for cosmological structure formation

Probing the linear power spectrum on the smallest scales



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# Conclusions on dark matter searches

- Gamma-ray observations of galaxy clusters by Fermi will test the DM interpretation of the Fermi/HESS/PAMELA data in the next years.
- If the DM interpretation is correct, then we either live in a warm dark matter Universe or there is a new dynamical effect during non-linear structure formation that wipes out the smallest structures.
- Gamma-ray observations might be the most sensitive probes of the smallest cosmological structures.



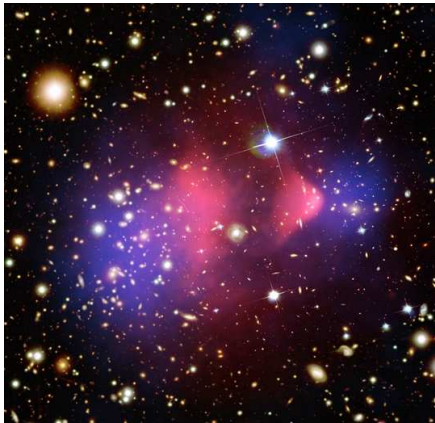
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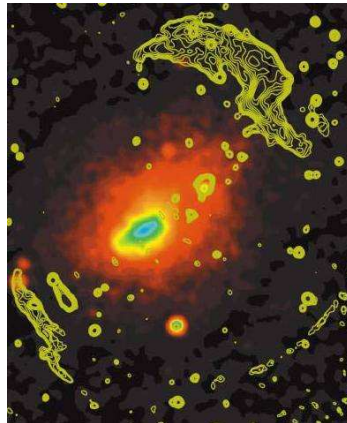


# Shocks in galaxy clusters



1E 0657-56 (“Bullet cluster”)

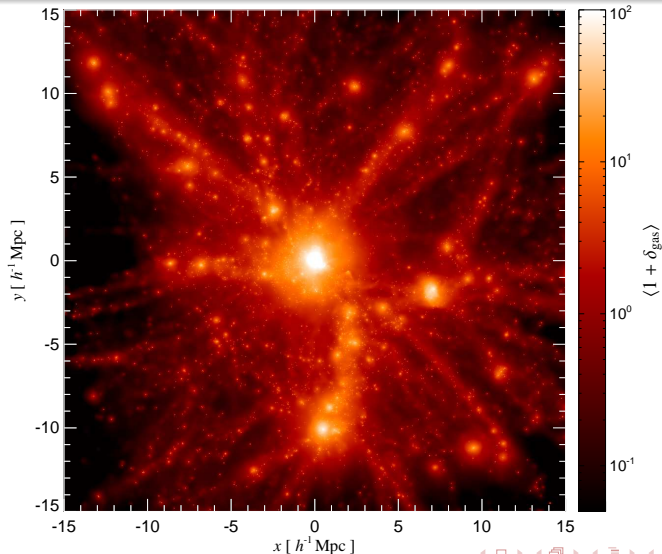
(X-ray: NASA/CXC/CfA/M.Markevitch et al.; Optical: NASA/STScI; Magellan/U.Arizona/D.Clowe et al.; Lensing: NASA/STScI; ESO WFI; Magellan/U.Arizona/D.Clowe et al.)



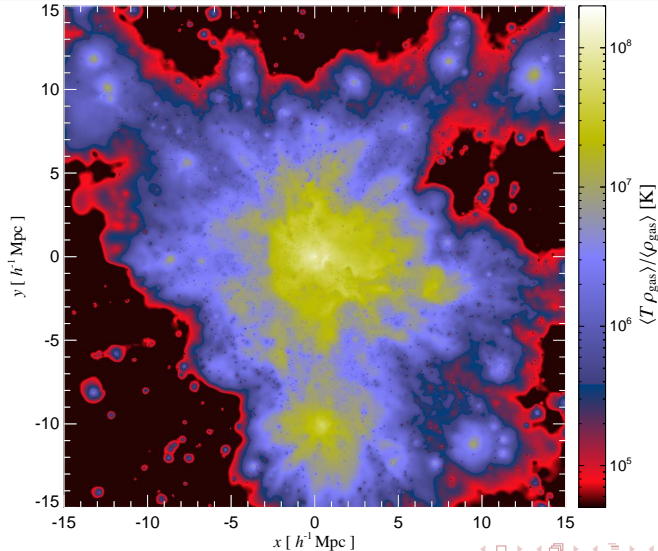
Abell 3667

(radio: Johnston-Hollitt. X-ray: ROSAT/PSPC.)

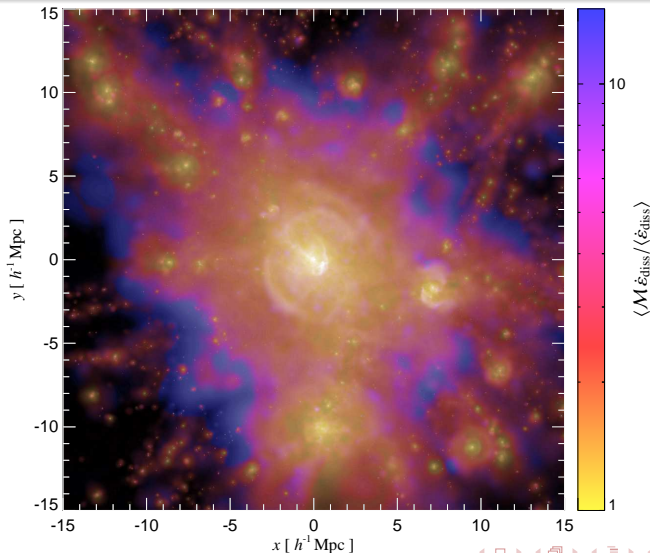
# Radiative cool core cluster simulation: gas density



# Mass weighted temperature



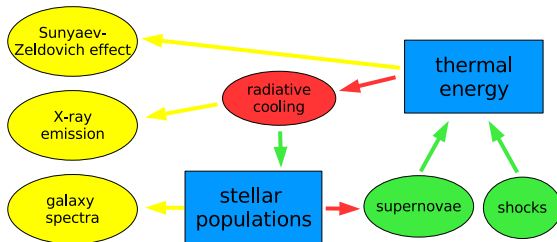
# Mach number distribution weighted by $\epsilon_{\text{diss}}$



# Radiative simulations – flowchart

Cluster observables:

Physical processes in clusters:



CP, EnBlin, Springel (2008)

— loss processes  
— gain processes  
— observables  
— populations



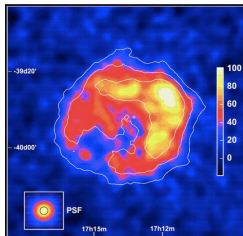
# Collisionless shocks at supernova remnants

Astrophysical collisionless shocks can:

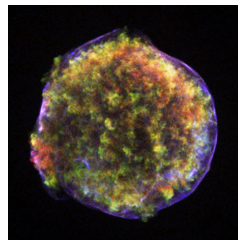
- accelerate particles (electrons and ions)
- amplify magnetic fields (or generate them from scratch)
- exchange energy between electrons and ions



SN 1006 X-rays (CXC/Hughes)



G347.3 HESS TeV  
(Aharonian et al. 2006)

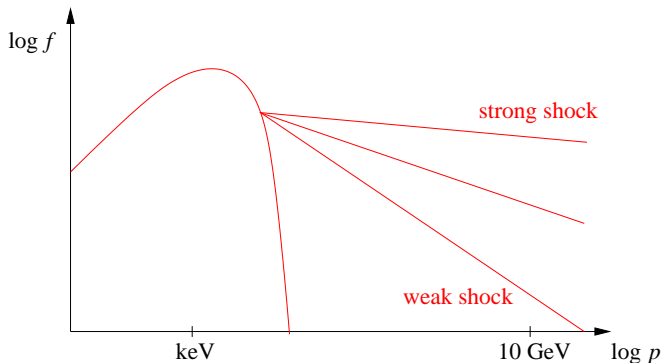


Tycho X-rays (CXC)

# Diffusive shock acceleration – Fermi 1 mechanism

Spectral index depends on the Mach number of the shock,

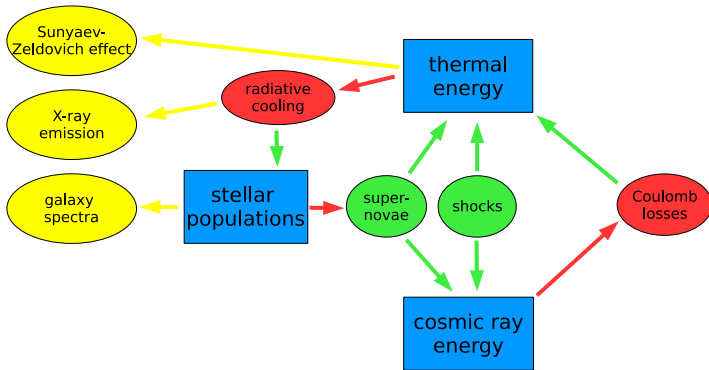
$$\mathcal{M} = v_{\text{shock}}/c_s:$$



# Radiative simulations with cosmic ray (CR) physics

Cluster observables:

Physical processes in clusters:



CP, EnBlin, Springel (2008)

— loss processes  
— gain processes  
— observables  
— populations

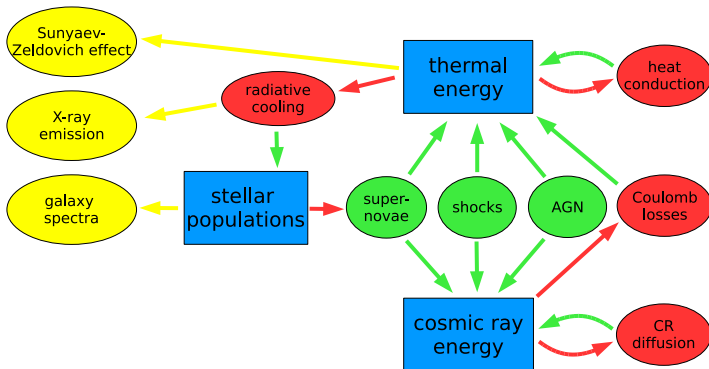




# Radiative simulations with extended CR physics

Cluster observables:

Physical processes in clusters:

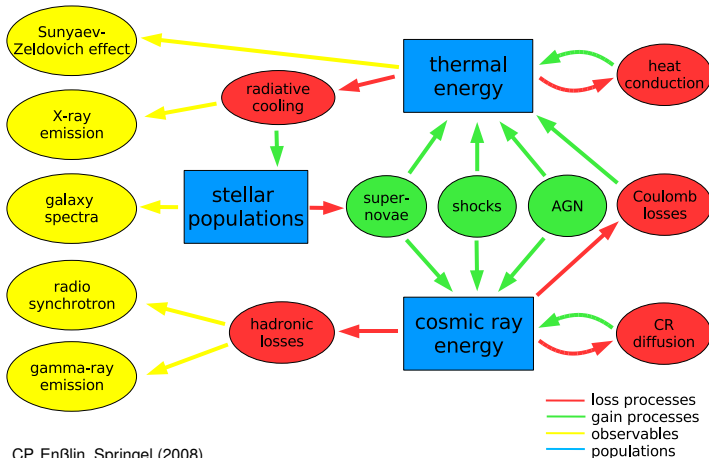


CP, EnBlin, Springel (2008)

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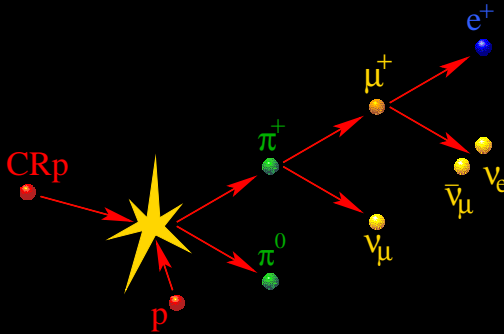
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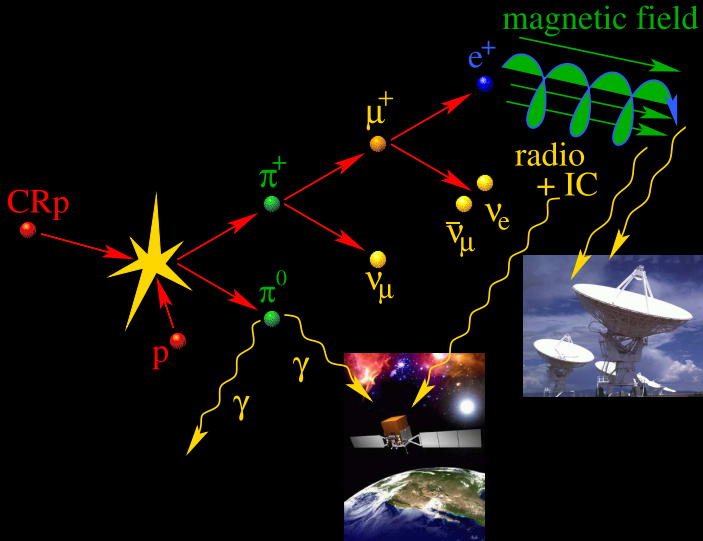


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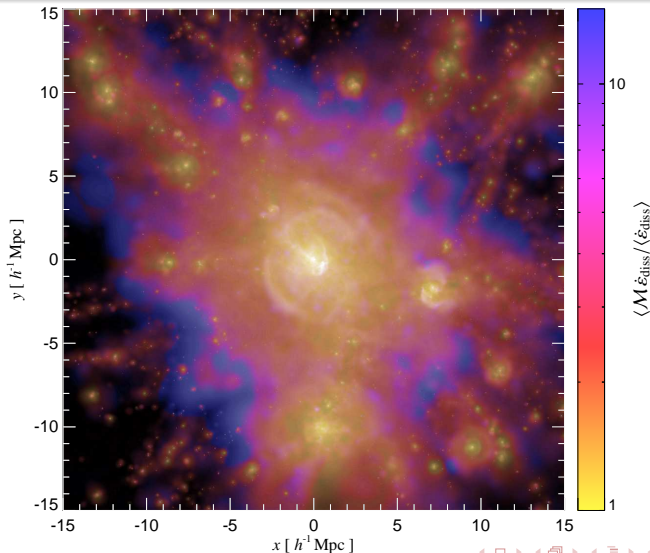
# Hadronic cosmic ray proton interaction



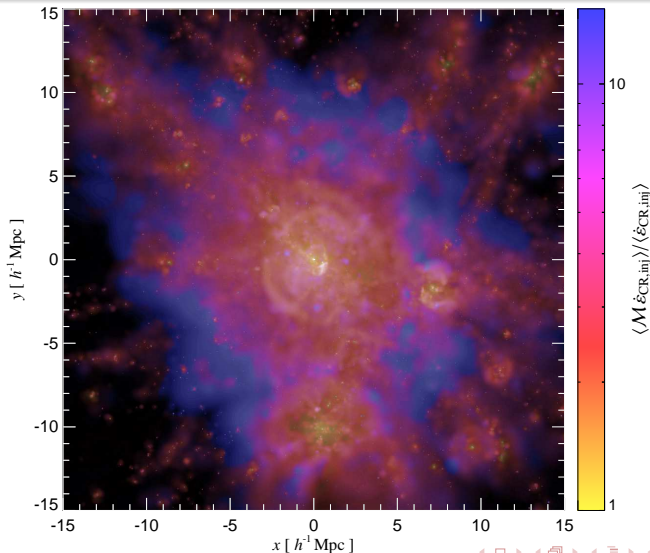
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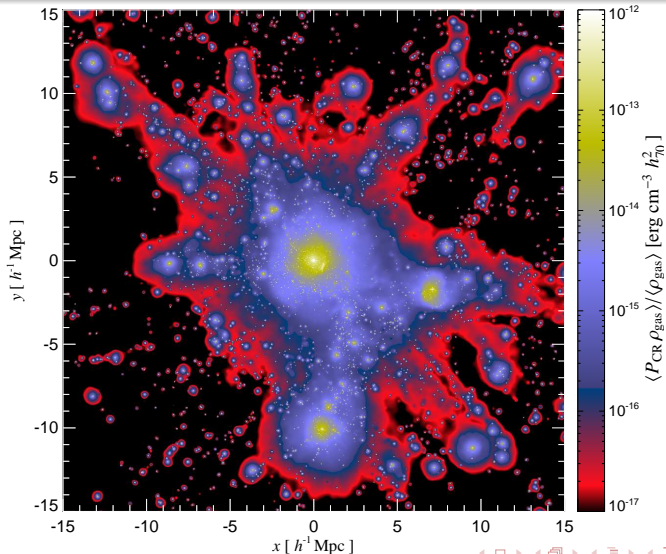
# Mach number distribution weighted by $\epsilon_{\text{diss}}$



# Mach number distribution weighted by $\varepsilon_{\text{CR},\text{inj}}$

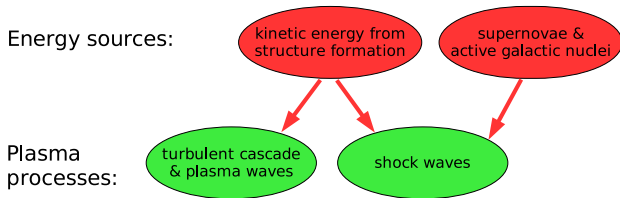


# CR pressure $P_{\text{CR}}$



# Multi messenger approach for non-thermal processes

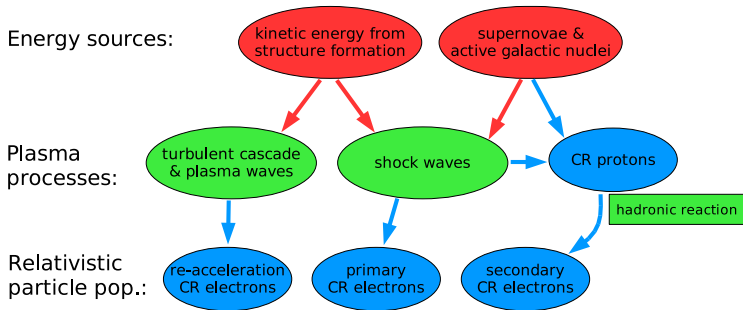
Relativistic populations and radiative processes in clusters:





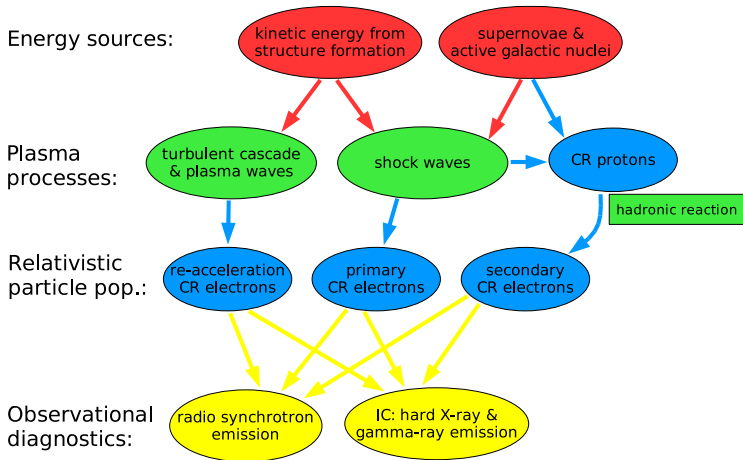
# Multi messenger approach for non-thermal processes

Relativistic populations and radiative processes in clusters:



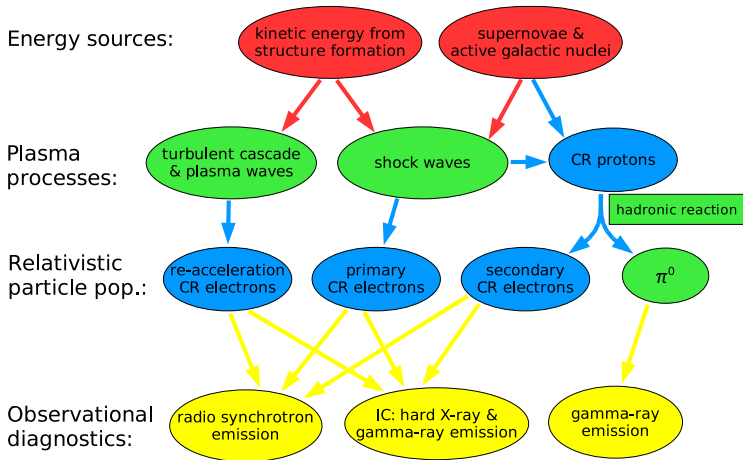
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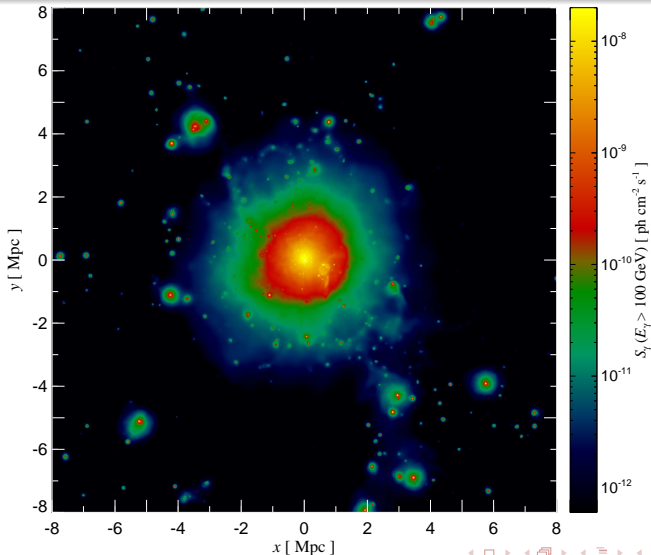


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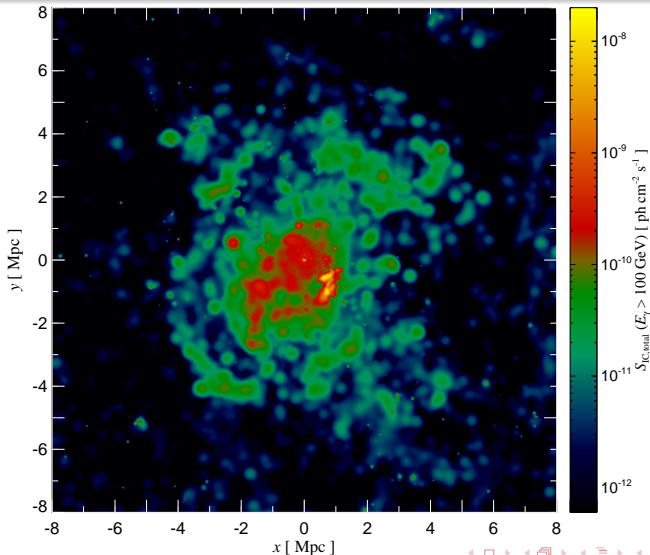
Relativistic populations and radiative processes in clusters:



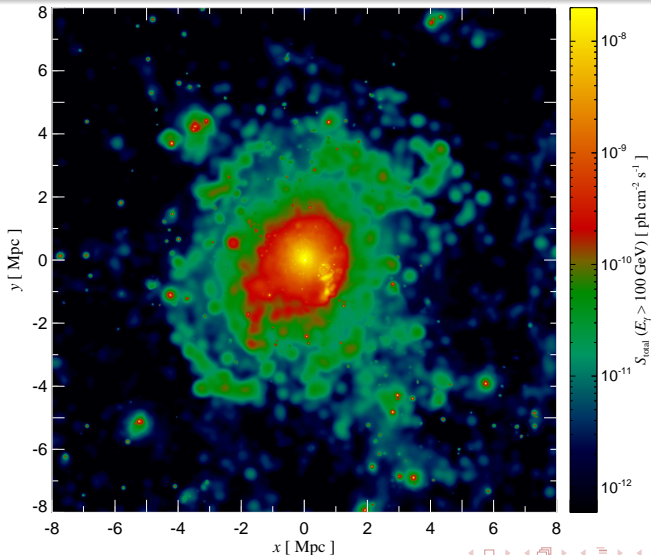
# Hadronic $\gamma$ -ray emission, $E_\gamma > 100$ GeV



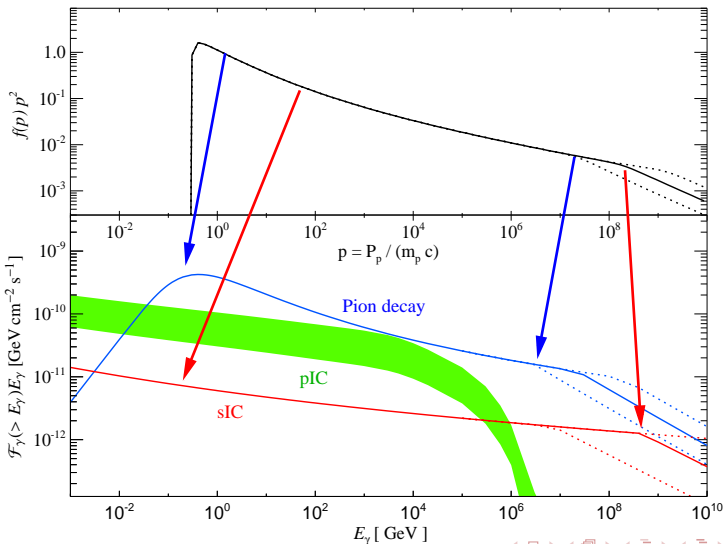
# Inverse Compton emission, $E_{IC} > 100 \text{ GeV}$



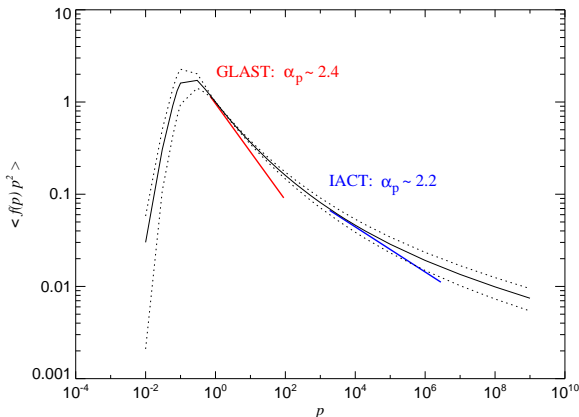
# Total $\gamma$ -ray emission, $E_\gamma > 100$ GeV



# CR proton and $\gamma$ -ray spectrum (Pinzke & CP 2009)



# Universal CR spectrum in clusters

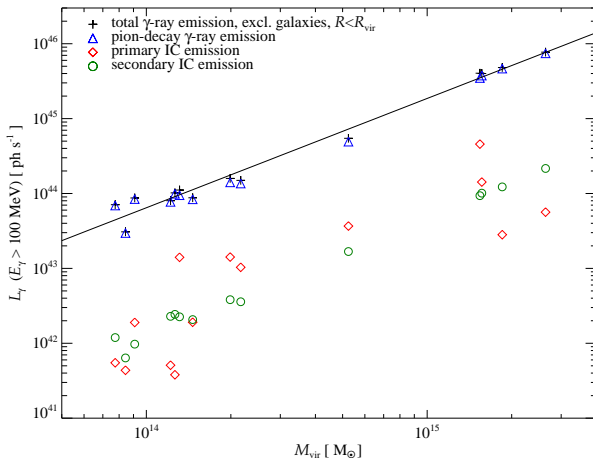


Normalized CR spectrum shows **universal concave shape**  $\rightarrow$  governed by hierarchical structure formation and the implied distribution of Mach numbers that a fluid element had to pass through in cosmic history (Pinzke & CP 2009).



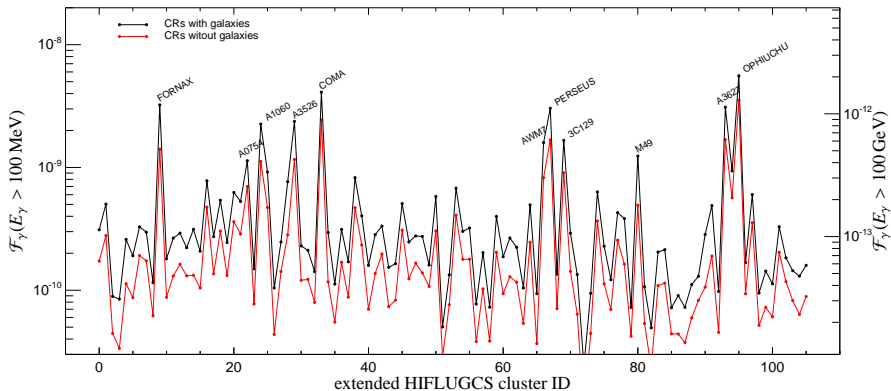


# Gamma-ray scaling relations



Scaling relation + complete sample of the brightest X-ray clusters (HIFLUGCS)  $\rightarrow$  predictions for *Fermi* and *IACT*'s

# Predicted cluster sample for *Fermi* and *IACT*'s

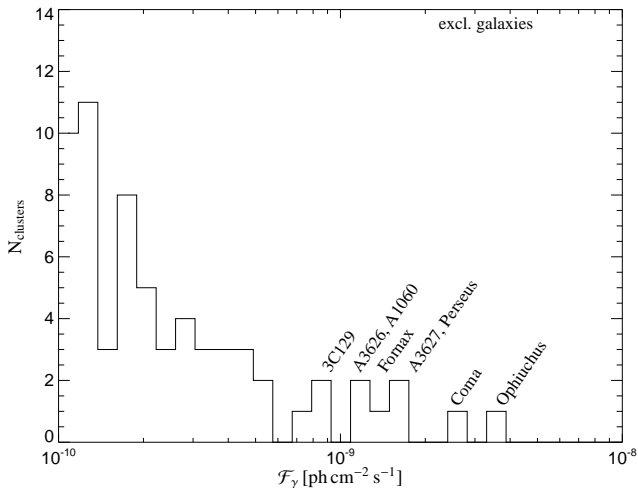


black: optimistic model, including galactic 'point sources' that bias  $\gamma$ -ray flux high; red: realistic model, excluding galactic 'point sources'



CITA-ICAT

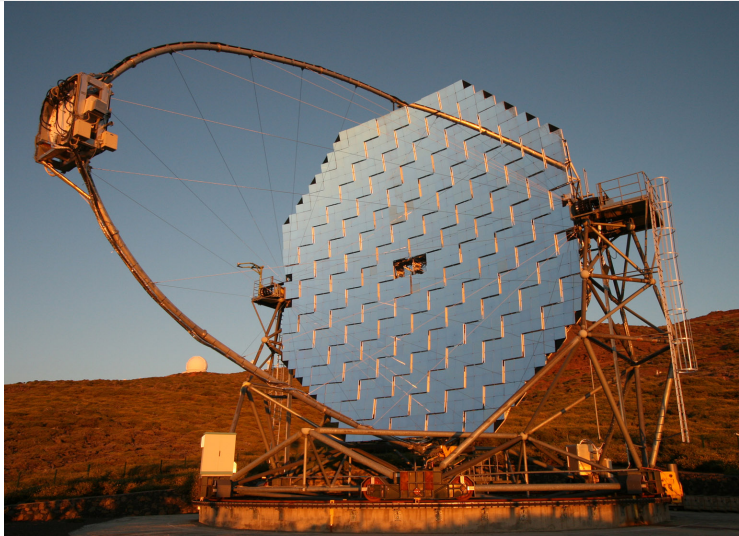
# Predicted cluster sample for *Fermi* – brightest objects



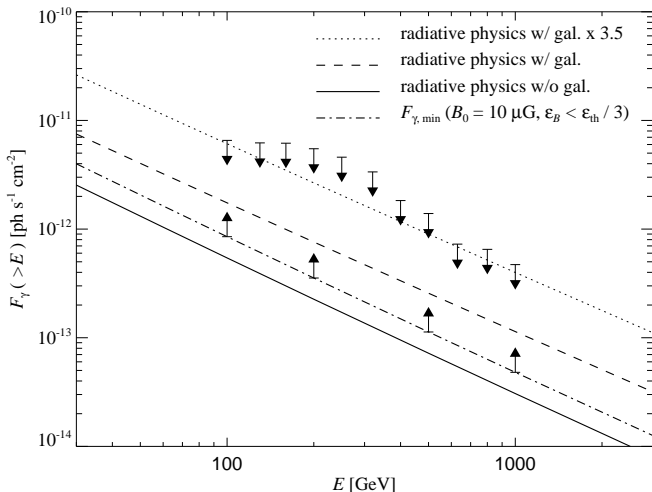
Introduction to dark matter  
Indirect dark matter searches  
High-energy phenomena

Cosmological simulations with cosmic rays  
Shocks and particle acceleration  
Non-thermal emission from clusters

# MAGIC observations of Perseus



# Upper limit on the TeV $\gamma$ -ray emission from Perseus



The MAGIC Collaboration: Aleksic et al. & CP et al. 2009



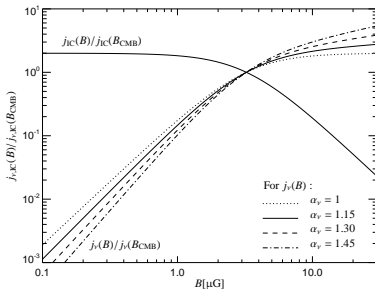
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# Results from the Perseus observation by *MAGIC*

- assuming  $f \propto p^{-\alpha}$  with  $\alpha = 2.1$ ,  $P_{\text{CR}} \propto P_{\text{th}}$ :  
 $E_{\text{CR}} < 0.017 E_{\text{th}} \rightarrow$  most stringent constraint on CR pressure!
- upper limits consistent with cosmological simulations:  
 $F_{\text{upper limits}}(100\text{GeV}) = 3.5 F_{\text{sim}}$  (optimistic model)
- simulation modeling of pressure constraint yields  
 $\langle P_{\text{CR}} \rangle / \langle P_{\text{th}} \rangle < 0.07$  (0.14) for the core (entire cluster)
- 3 physical effects that resolve the apparent discrepancy:
  - concave curvature ‘hides’ CR pressure at GeV energies
  - galactic ‘point sources’ bias  $\gamma$ -ray flux high and pressure limits low (partly physical)
  - relative CR pressure increases towards the outer parts (adiabatic compression and softer equation of state of CRs)



# Minimum $\gamma$ -ray flux in the hadronic model



Synchrotron emissivity of high-energy, steady state electron distribution is independent of the magnetic field for  $B \gg B_{\text{CMB}}$ !

Synchrotron luminosity:

$$L_\nu = A_\nu \int dV n_{\text{CR}} n_{\text{gas}} \frac{\epsilon_B^{(\alpha_\nu+1)/2}}{\epsilon_{\text{CMB}} + \epsilon_B}$$

$$\rightarrow A_\nu \int dV n_{\text{CR}} n_{\text{gas}} \quad (\epsilon_B \gg \epsilon_{\text{CMB}})$$

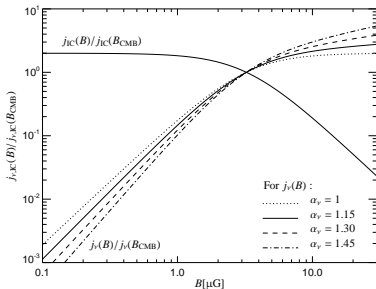
$\gamma$ -ray luminosity:

$$L_\gamma = A_\gamma \int dV n_{\text{CR}} n_{\text{gas}}$$

$\rightarrow$  minimum  $\gamma$ -ray flux:

$$\mathcal{F}_{\gamma, \text{min}} = \frac{A_\gamma}{A_\nu} \frac{L_\nu}{4\pi D^2}$$

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# Minimum $\gamma$ -ray flux in the hadronic model: *Fermi*

Minimum  $\gamma$ -ray flux ( $E_\gamma > 100$  MeV) for the Coma cluster:

CR spectral index	2.0	2.3	2.6	2.9
$\mathcal{F}_\gamma$ [ $10^{-10}$ ph cm $^{-2}$ s $^{-1}$ ]	0.8	1.6	3.4	7.1

- These limits can be made even tighter when considering energy constraints,  $P_B < P_{\text{gas}}/30$  and  $B$ -fields derived from Faraday rotation studies,  $B_0 = 3 \mu\text{G}$ :  
 $\mathcal{F}_{\gamma, \text{COMA}} \gtrsim (1.1 \dots 1.5) \times 10^{-9} \gamma \text{ cm}^{-2} \text{ s}^{-1} \lesssim \mathcal{F}_{\text{Fermi}, 2\text{yr}}$
- Non-detection by Fermi seriously challenges the hadronic model.
- Potential of measuring the CR acceleration efficiency for diffusive shock acceleration.

# Conclusions on high-energy phenomena

In contrast to the thermal plasma, the non-equilibrium distributions of CRs preserve the information about their injection and transport processes and provide thus a unique window of current and past structure formation processes!

- 1 **Cosmological hydrodynamical simulations** are indispensable for understanding non-thermal processes in galaxy clusters  
→ illuminating the **process of structure formation**
- 2 **Multi-messenger approach** including radio synchrotron, hard X-ray IC, and HE  $\gamma$ -ray emission:
  - **fundamental plasma physics**: diffusive shock acceleration, large scale magnetic fields, and turbulence
  - **nature of dark matter**
  - **gold sample** of clusters for precision cosmology



# Literature for the talk

- Pinzke, Pfrommer, Bergström, Phys. Rev. Lett., 2009, 103, 181302, *Gamma-rays from dark matter annihilations strongly constrain the substructure in halos*
- Pfrommer, 2008, MNRAS, 385, 1242 *Simulating cosmic rays in clusters of galaxies – III. Non-thermal scaling relations and comparison to observations*
- Pfrommer, Enßlin, Springel, 2008, MNRAS, 385, 1211, *Simulating cosmic rays in clusters of galaxies – II. A unified scheme for radio halos and relics with predictions of the  $\gamma$ -ray emission*
- Pfrommer, Enßlin, Springel, Jubelgas, Dolag, 2007, MNRAS, 378, 385, *Simulating cosmic rays in clusters of galaxies – I. Effects on the Sunyaev-Zel'dovich effect and the X-ray emission*
- Pfrommer, Springel, Enßlin, Jubelgas, 2006, MNRAS, 367, 113, *Detecting shock waves in cosmological smoothed particle hydrodynamics simulations*
- Enßlin, Pfrommer, Springel, Jubelgas, 2007, A&A, 473, 41, *Cosmic ray physics in calculations of cosmological structure formation*
- Jubelgas, Springel, Enßlin, Pfrommer, A&A, , 481, 33, *Cosmic ray feedback in hydrodynamical simulations of galaxy formation*