

Magnetic draping and cosmic-ray driven winds in galaxies

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in collaboration with

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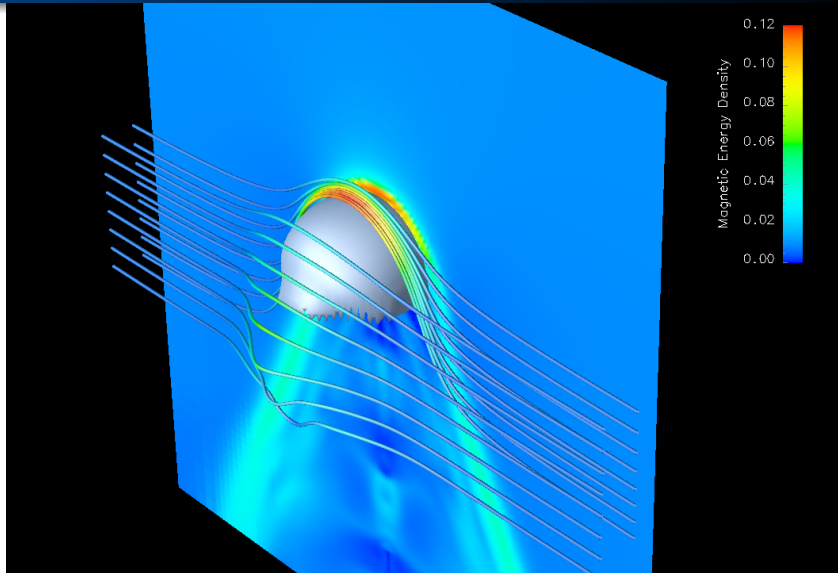


Outline

- 1 Magnetic draping
 - Mechanism
 - Observations
 - Physical insight
- 2 Polarized radio ridges
 - Observations
 - Draping simulations
 - Synthetic synchrotron emission
- 3 Cosmic ray-driven winds
 - Winds and cosmic rays
 - Galaxy simulations
 - The big picture

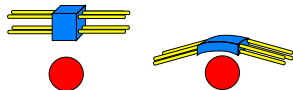
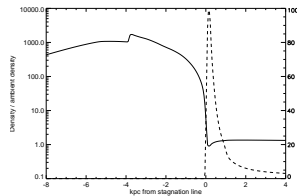


What is magnetic draping?



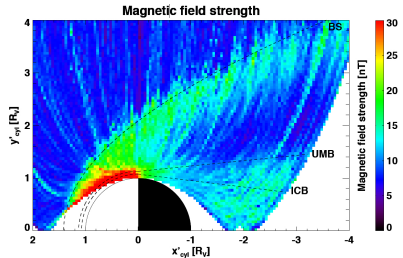
What is magnetic draping?

- Is magnetic draping (MD) similar to ram pressure compression?
 - no density enhancement for MD
 - analytical solution of MD for incompressible flow
 - ideal MHD simulations (*right*)
- Is magnetic flux still frozen into the plasma?
 - yes, but plasma can also move along field lines while field lines get stuck at obstacle



Draping of the interplanetary field over Venus

- Venus and Mars do not have a global magnetic field
- *Venus Express*: amplification of solar wind field by a factor ~ 6 at the side facing the Sun



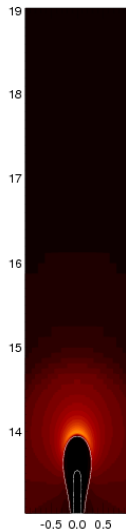
Guicking et al. (2010)

- draping of solar wind magnetic field around Venus/Mars leads to the **formation of magnetic pile-up region and the magneto tail**
→ enhanced magnetic field strength in the planets' wake



Magnetic draping in 2D

Sometimes,
2D just isn't
enough ...



Magnetic draping

Polarized radio ridges
Cosmic ray-driven winds

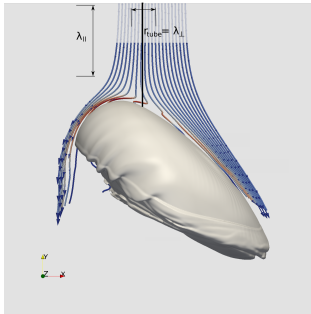
Mechanism

Observations

Physical insight



Streamlines in the rest frame of the galaxy



- analytic potential flow solution
→ critical impact parameter
 $p_{\text{cr}} = R/(2\mathcal{M}_A)$, $\mathcal{M}_A \simeq \mathcal{M}_s \sqrt{\beta} \sim 10$,
 R denotes the curvature radius
- **only streamlines initially in a narrow tube** of radius $p_{\text{cr}} \simeq R/20 \simeq 1$ kpc from the stagnation line **become part of the magnetic draping layer** (color coded) → constraints on λ_B

- the streamlines that do not intersect the tube get deflected away from the galaxy, become never part of the drape and eventually get accelerated (Bernoulli effect)
- note the kink feature in some draping-layer field lines due to back reaction as the solution changes from the hydrodynamic potential flow solution to that in the draped layer



Conditions for magnetic draping

- **ambient plasma sufficiently ionized** such that flux freezing condition applies
- **super-Alfvénic motion** of a cloud through a weakly magnetized plasma: $\mathcal{M}_A^2 = \beta\gamma\mathcal{M}^2/2 > 1$
- **magnetic coherence across the “cylinder of influence”:**

$$\frac{\lambda_B}{R} \gtrsim \frac{1}{\mathcal{M}_A} \sim 0.1 \times \left(\frac{\beta}{100}\right)^{-1/2} \quad \text{for sonic motions,}$$

R denotes the curvature radius of the working surface at the stagnation line



Polarized synchrotron emission in a field spiral: M51

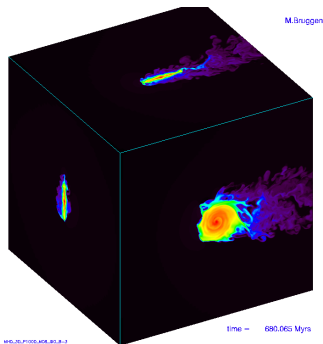


MPIfR Bonn and Hubble Heritage Team

- grand design 'whirlpool galaxy' (M51): optical star light superposed on radio contours
- polarized radio intensity follows the spiral pattern and is strongest in between the spiral arms
- the polarization 'B-vectors' are aligned with the spiral structure



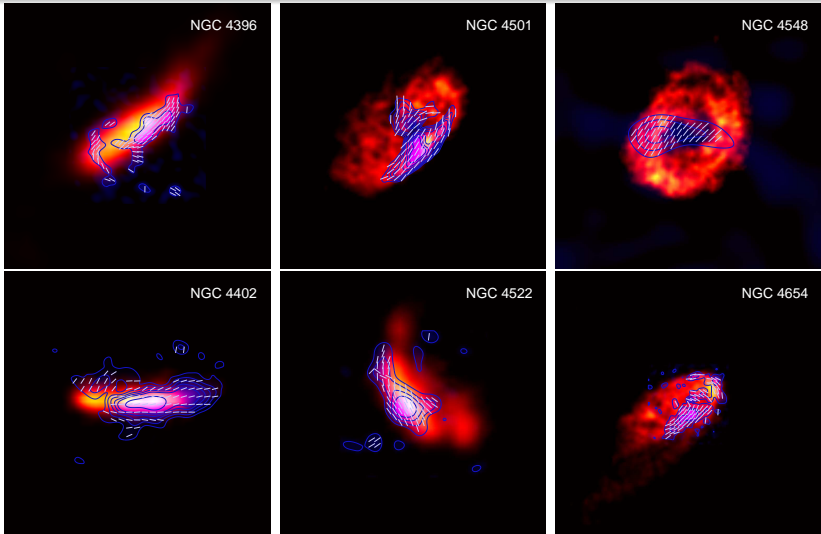
Ram-pressure stripping of cluster spirals



Brueggen (2008)

- 3D simulations show that the ram-pressure wind quickly strips the low-density gas in between spiral arms (Tonnesen & Bryan 2010)
 - being flux-frozen into this dilute plasma, the large scale magnetic field will also be stripped
- resulting radio emission should be unpolarized

Polarized synchrotron ridges in Virgo spirals



Vollmer et al. (2007): 6 cm PI (contours) + B-vectors; Chung et al. (2009): HI (red)

Observational evidence and model challenges

- asymmetric distributions of polarized intensity at the leading edge with extraplanar emission, sometimes also at the side
- coherent alignment of polarization vectors over ~ 30 kpc
- stars lead polarized emission, polarized emission leads gas
- HI gas only moderately enhanced (factor $\lesssim 2$), localized ‘HI hot spot’ smaller than the polarized emission region:
$$n_{\text{compr}} \simeq n_{\text{icm}} v_{\text{gal}}^2 / c_{\text{ism}}^2 \simeq 1 \text{ cm}^{-3} \simeq \langle n_{\text{ism}} \rangle$$
- flat radio spectral index (similar to the Milky Way) that steepens towards the edges of the polarized ridge
- no or weak Kelvin-Helmholtz instabilities at interface detectable

→ previous models that use ram-pressure compressed galactic magnetic fields fail to explain most of these points!



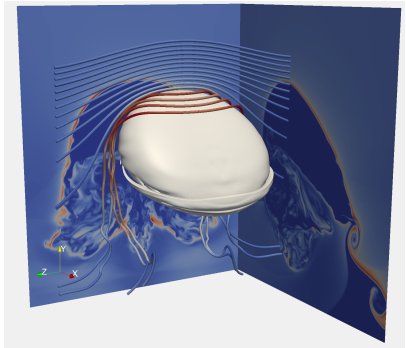
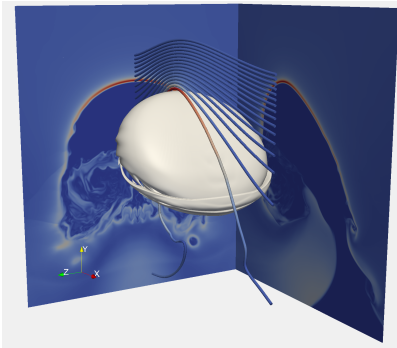
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→ need to consider the full MHD of the interaction spiral galaxy and magnetized ICM !



Magnetic draping around a spiral galaxy

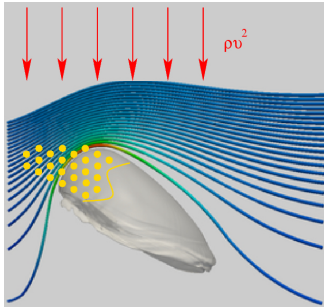


Athena simulations of spiral galaxies interacting with a uniform cluster magnetic field; **there is a sheath of strong field draped around the leading edge (shown in red)**

C.P. & Dursi (2010)



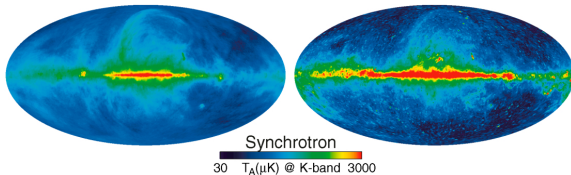
Magnetic draping around a spiral galaxy – physics



- the galactic ISM is pushed back by the ram pressure wind $\sim \rho v^2$
 - the stars are largely unaffected and lead the gas
 - the draping sheath is formed at the contact of galaxy/cluster wind
 - as stars become SN, their remnants accelerate CRes that populate the field lines in the draping layer
-
- CRes are transported diffusively (along field lines) and advectively as field lines slip over the galaxy
 - CRes emit radio synchrotron radiation in the draped region, tracing out the field lines there → **coherent polarized emission at the galaxies' leading edges**



Modeling the electron population



- typical SN rates imply a homogeneous CRe distribution (WMAP)
- FIR-radio correlation of Virgo spirals show comparable values to the solar circle → take CRe distribution of our Galaxy:

$$n_{\text{cre}} = C_0 e^{-(R-R_\odot)/h_R} e^{-|z|/h_z}$$

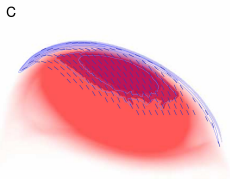
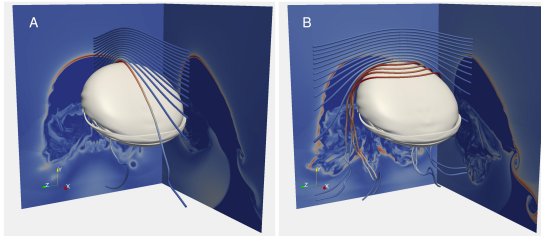
with normalization $C_0 \simeq 10^{-4} \text{ cm}^{-3}$,
 scale heights $h_R \simeq 8 \text{ kpc}$ and $h_z \simeq 1 \text{ kpc}$ at Solar position

- truncate at contact of ISM-ICM, attach exp. CRe distribution \perp to contact surface with $h_\perp \simeq 150 \text{ pc}$ (max. radius of Sedov phase)

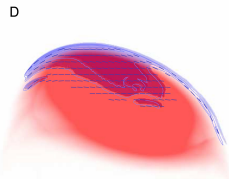


Magnetic draping and polarized synchrotron emission

Synchrotron B-vectors reflect the upstream orientation of cluster magnetic fields



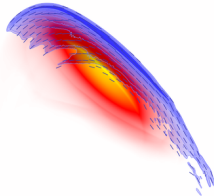
Total PI = 8.227 mJy
Max PI = 218.7 μ Jy/beam



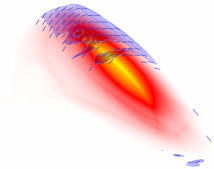
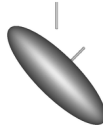
Total PI = 8.440 mJy
Max PI = 334.6 μ Jy/beam



Simulated polarized synchrotron emission



Total PI (mJ) = 23.47
Max PI (μ J/beam) = 3002.

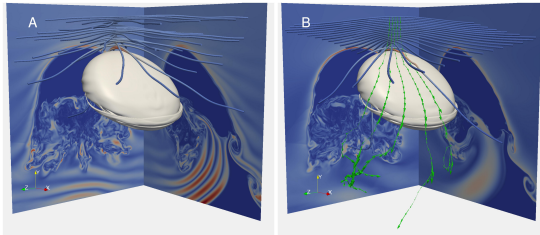


Total PI (mJ) = 4.114
Max PI (μ J/beam) = 133.9

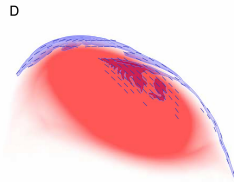
Movie of the simulated polarized synchrotron radiation viewed from various angles and with two field orientations.

Magnetic draping of a helical B-field

(Non-)observation of polarization twist constrains magnetic coherence length



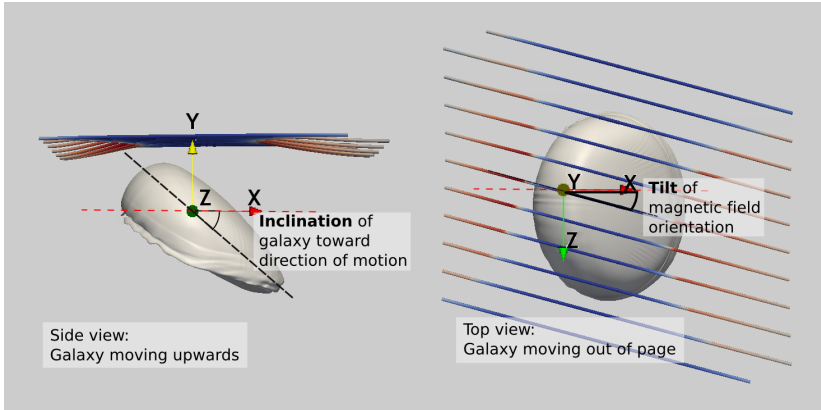
Total PI = 1.586 mJ
Max PI = 67.42 μ J/beam



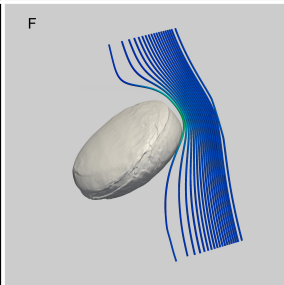
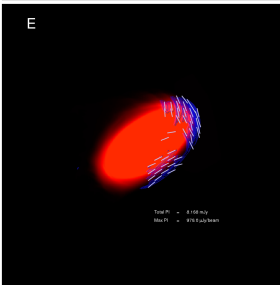
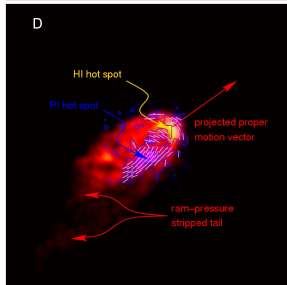
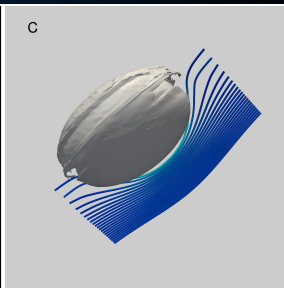
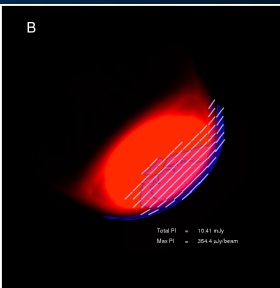
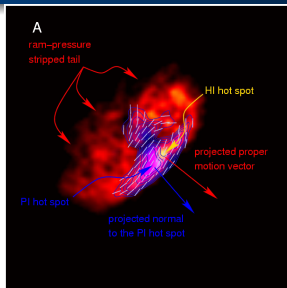
Total PI = 5.927 mJ
Max PI = 304.9 μ J/beam



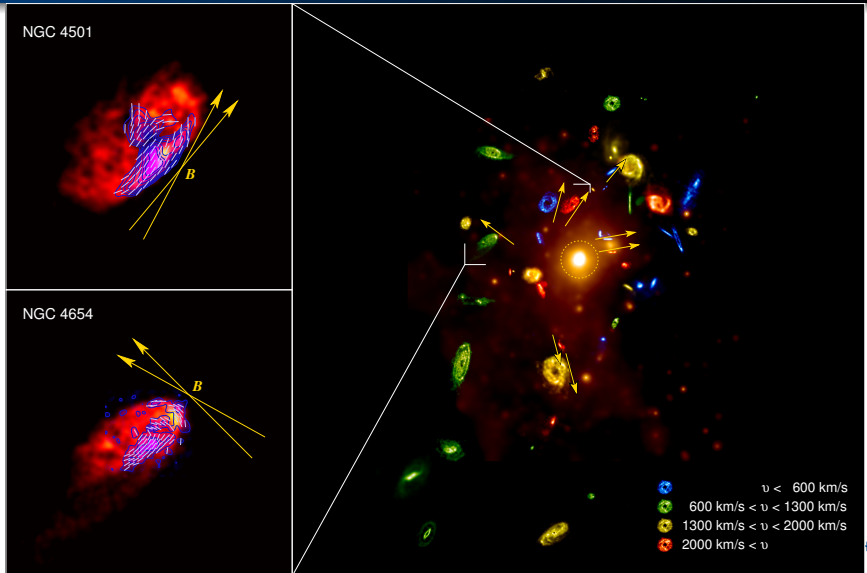
Varying galaxy inclination and magnetic tilt



Observations versus simulations



Mapping out the magnetic field in Virgo



Discussion of radial field geometry

- the alignment of the field in the plane of the sky is **significantly more radial than expected from random chance**; considering the sum of deviations from radial alignment gives a chance coincidence of less than 1.7% ($\sim 2.2 \sigma$)
- for the **three nearby galaxy pairs** in the data set, **all have very similar field orientations**

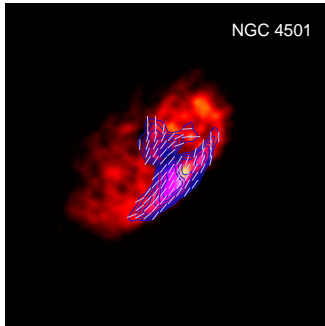
→ Which effect causes this field geometry?

Magneto-thermal instability? (Parrish+2007, C.P.+2010)

Radial infall? (Ruszkowski+2010)

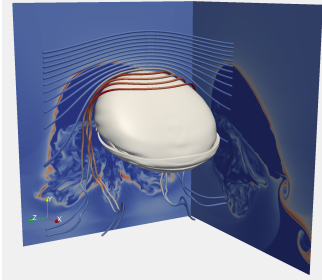


Conclusions on magnetic draping around galaxies



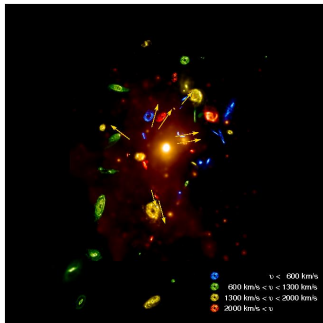
- draping of cluster magnetic fields naturally explains polarization ridges at Virgo spirals

Conclusions on magnetic draping around galaxies



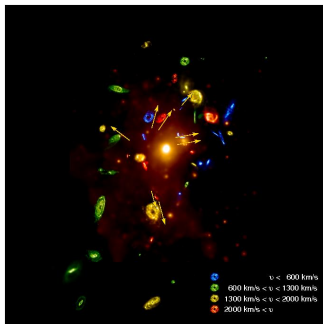
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- this represents a new tool for measuring the in situ 3D orientation and coherence scale of cluster magnetic fields

Conclusions on magnetic draping around galaxies



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- this represents a new tool for measuring the in situ 3D orientation and coherence scale of cluster magnetic fields
- application to the Virgo cluster shows that the magnetic field is preferentially aligned radially

Conclusions on magnetic draping around galaxies



- draping of cluster magnetic fields naturally explains polarization ridges at Virgo spirals
 - this represents a new tool for measuring the in situ 3D orientation and coherence scale of cluster magnetic fields
 - application to the Virgo cluster shows that the magnetic field is preferentially aligned radially
-
- this finding implies efficient thermal conduction across clusters
→ important for thermal cluster history/cluster cosmology
 - outlook: draping on cosmological galaxies, follow CR electron transport, . . .



Galactic super wind in M82

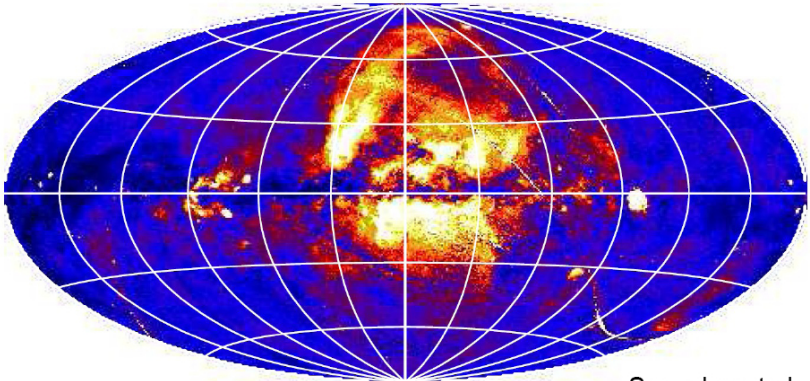


NASA/ESA



Galactic wind in the Milky Way?

Diffuse X-ray emission in our galaxy

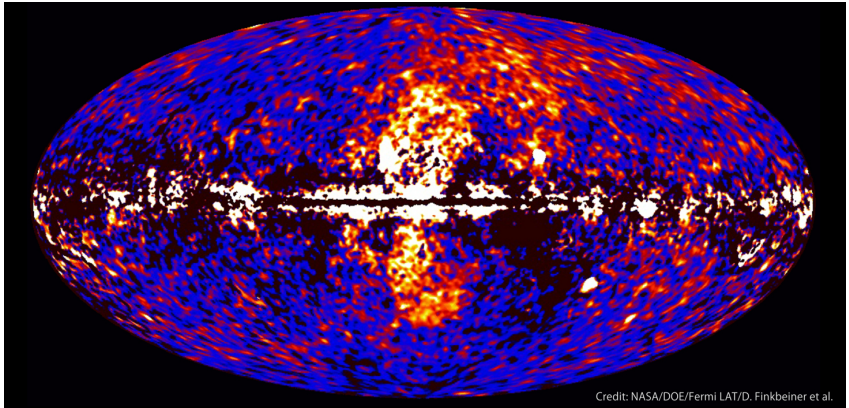


Snowden et al., 2007



Galactic wind in the Milky Way?

Fermi gamma-ray bubbles



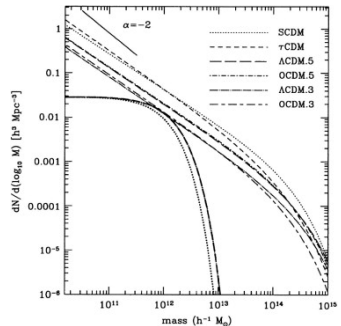
Credit: NASA/DOE/Fermi LAT/D. Finkbeiner et al.



Galactic wind trivia

Winds ...

- ... may explain mismatch between luminosity function and halo mass function on small scales
- ... may enrich the intergalactic medium (IGM) with metals and magnetic fields
- ... influence energy budget of IGM



Somerville+1999



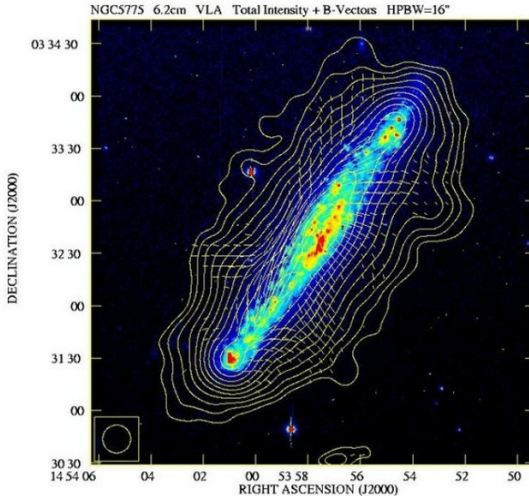
How to drive a wind?

- **standard picture:** wind driven by thermal pressure
- **energy sources for winds:** supernovae, AGN
- **problem with the standard picture:** fast radiative cooling
- **alternative channels:**
 - radiation pressure on dust grains
 - cosmic rays (CRs, relativistic protons with $\gamma_{\text{ad}} = 4/3$)



Radio halos in edge-on disk galaxies

CRs and magnetic fields exist at the disk-halo interface → wind launching site?



Tüllmann+2000



Cosmic ray-driven winds

- several reasons why CRs are important for wind formation:
 - CR pressure drops less quickly than thermal pressure ($P \propto \rho^\gamma$)
 - CRs cool less efficiently than thermal gas
 - most CR energy loss goes into thermal pressure
- analytical models: CR can aid in driving winds
(Ipavich 1975, Breitschwerdt+1991, Socrates+2008, Everett+2008/2010, Samui2010)
- up to now, no 3D hydrodynamical simulations that study CR driven winds!

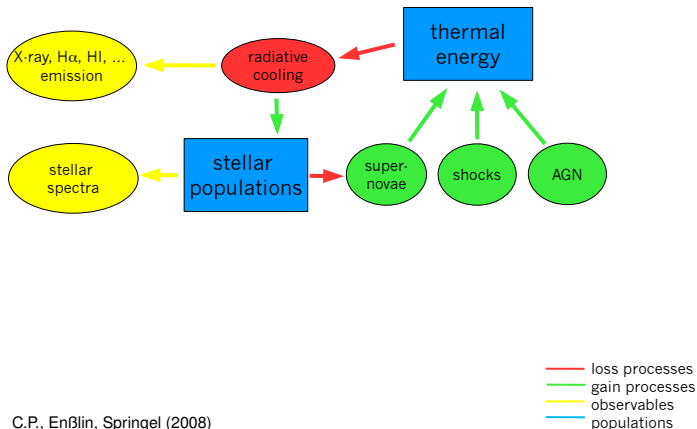
Uhlig, C.P., Sharma, Nath, EnBlin, Springel, *MNRAS* **423**, 2374 (2012)
Galactic winds driven by cosmic-ray streaming



Interstellar medium (ISM) simulations – flowchart

ISM observables:

Physical processes in the ISM:



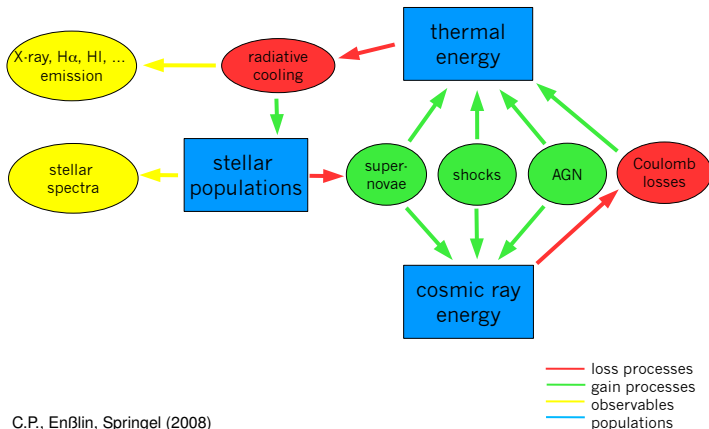
C.P., Enßlin, Springel (2008)



ISM simulations with cosmic ray physics

ISM observables:

Physical processes in the ISM:



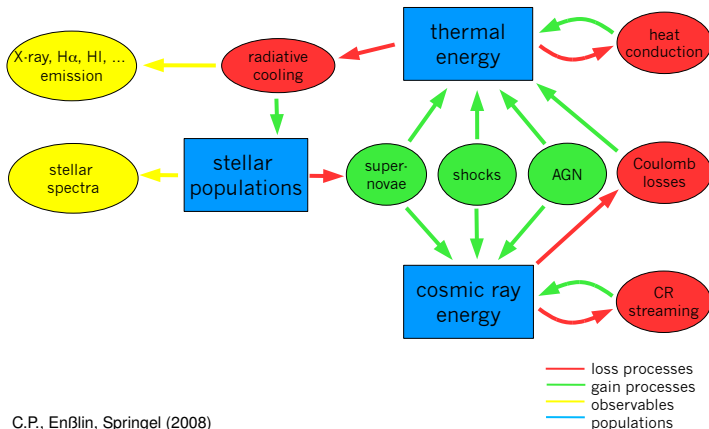
C.P., Enßlin, Springel (2008)



ISM simulations with extended cosmic ray physics

ISM observables:

Physical processes in the ISM:



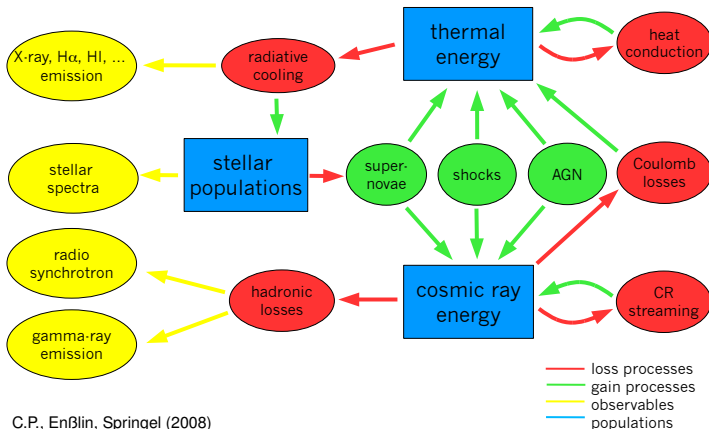
C.P., Enßlin, Springel (2008)



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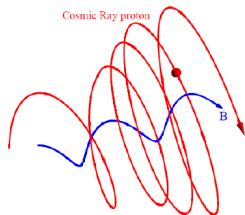


C.P., Enßlin, Springel (2008)



Interactions of CRs and magnetic fields

- CRs scatter on magnetic fields → isotropization of CR momenta
- **CR streaming instability:** Kulsrud & Pearce 1969
 - if $v_{\text{CR}} > v_{\text{waves}}$ with respect to the gas, CR excite Alfvén waves
 - scattering off this wave field limits the CRs' bulk speed $\ll c$
 - wave damping: **transfer of CR energy and momentum to the thermal gas**



→ **CRs exert a pressure on the thermal gas by means of scattering off Alfvén waves**



CR streaming (1)

- total CR velocity $\mathbf{v}_{\text{cr}} = \mathbf{v}_{\text{gas}} + \mathbf{v}_{\text{st}}$
- CRs stream down their own pressure gradient relative to the gas:

$$\mathbf{v}_{\text{st}} = -\lambda c_s \frac{\nabla P_{\text{cr}}}{|\nabla P_{\text{cr}}|},$$

- CR transport equation \rightarrow evolution equation for CR number and energy density:

$$\frac{\partial n_{\text{cr}}}{\partial t} = -\nabla \cdot [(\mathbf{v}_{\text{gas}} + \mathbf{v}_{\text{st}}) n_{\text{cr}}]$$

$$\frac{\partial \varepsilon_{\text{cr}}}{\partial t} = (\mathbf{v}_{\text{gas}} + \mathbf{v}_{\text{st}}) \cdot \nabla P_{\text{cr}} - \nabla \cdot [(\mathbf{v}_{\text{gas}} + \mathbf{v}_{\text{st}}) (\varepsilon_{\text{cr}} + P_{\text{cr}})]$$



CR streaming (2)

- Lagrangian time derivative

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \mathbf{v}_{\text{gas}} \cdot \nabla$$

- specific CR energy, $\tilde{\epsilon}_{\text{cr}}$, and CR particle number, \tilde{n}_{cr} ,

$$\epsilon_{\text{cr}} = \tilde{\epsilon}_{\text{cr}} \rho \quad \text{and} \quad n_{\text{cr}} = \tilde{n}_{\text{cr}} \rho$$

- CR evolution equations:

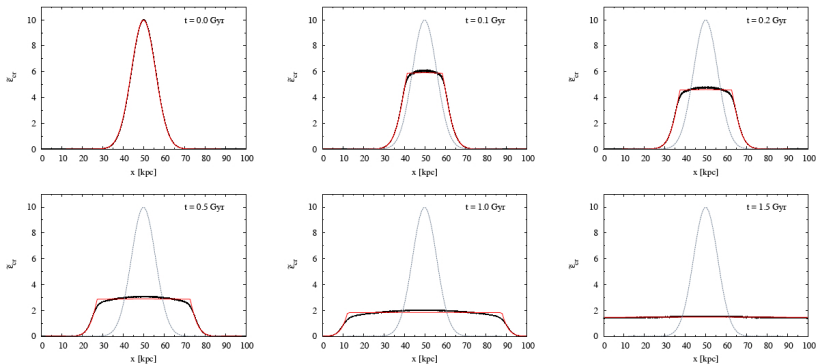
$$\rho \frac{d\tilde{n}_{\text{cr}}}{dt} = -\nabla \cdot [\mathbf{v}_{\text{st}} \rho \tilde{n}_{\text{cr}}]$$

$$\rho \frac{d\tilde{\epsilon}_{\text{cr}}}{dt} = \underbrace{\mathbf{v}_{\text{st}} \cdot \nabla P_{\text{cr}}}_{\text{energy loss term (wave damping)}} - \underbrace{P_{\text{cr}} \nabla \cdot \mathbf{v}_{\text{gas}}}_{\text{adiabatic changes due to converging/diverging gas flow}} - \underbrace{\nabla \cdot [\mathbf{v}_{\text{st}} (\rho \tilde{\epsilon}_{\text{cr}} + P_{\text{cr}})]}_{\text{energy change due to CR streaming in/out of a volume element}}$$



Test: Gadget-2 versus 1-d grid solver

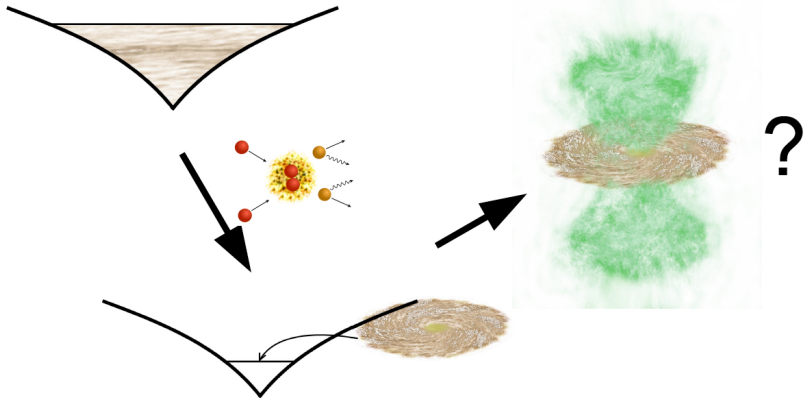
Evolution of the specific CR energy due to streaming in a medium at rest



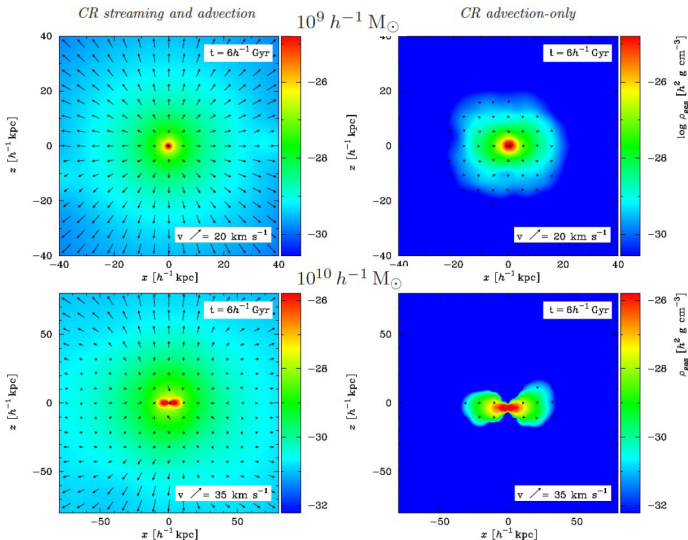
Uhlig+2012



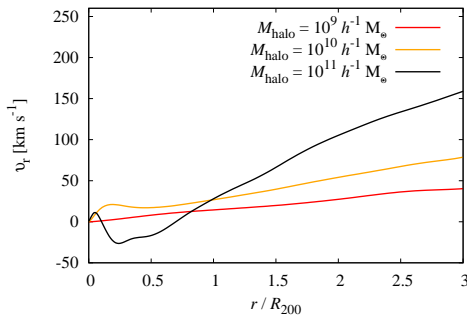
Simulation setup



CR streaming drives winds



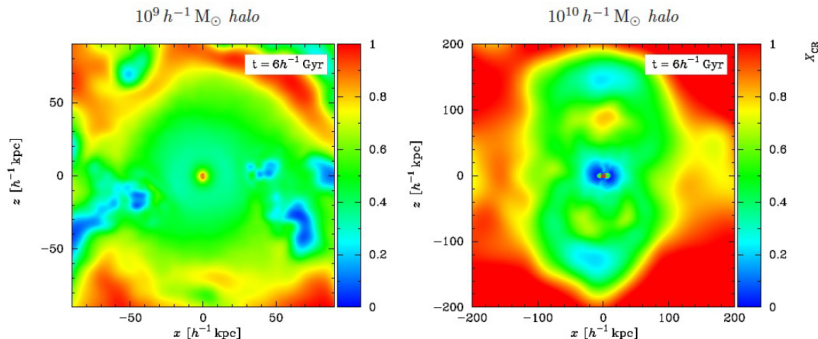
Wind velocity profile along the symmetry axis



- $10^9 - 10^{10} M_{\odot}$: accelerating wind due to a continuous CR momentum and energy deposition during the ascent of the wind in the gravitational potential
- $10^{11} M_{\odot}$: wind stalls in halo and falls back onto the disk → fountain flow



CR-to-thermal pressure in edge-on slice

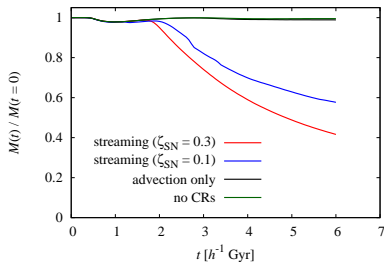


- $X_{\text{CR}} = P_{\text{CR}}/P < 50\%$ in vicinity of center because of loss processes that effectively transfer CR into thermal energy
- X_{CR} becomes dominant at larger heights due to the softer adiabatic index of CRs

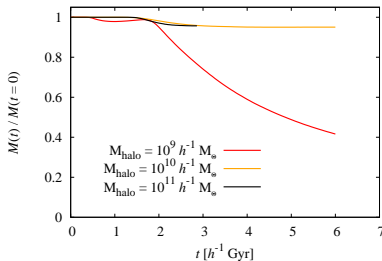


Gas mass loss within the virial radius

different scenarios:



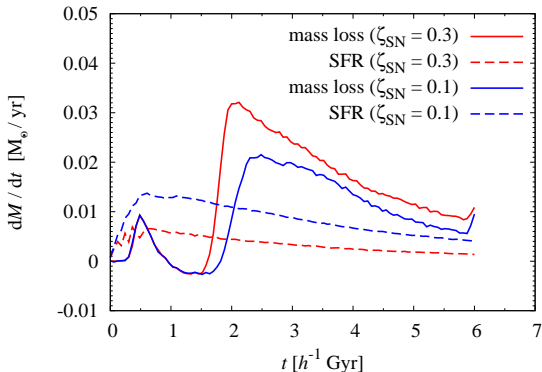
different galaxy masses:



- after initial phase (~ 2.5 Gyr), only winds driven by CR streaming overcome the ram pressure of infalling gas and expel gas from the halo
- mass loss rate increases with CR injection efficiency ζ_{SN} (*left*) and towards smaller galaxy masses (*right*)



Mass loss and star formation rates



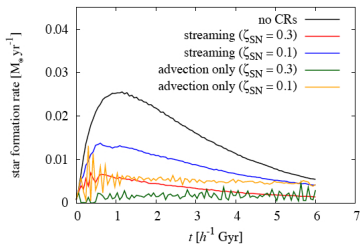
- time lag between onset of star formation and associated supernovae (that inject CRs) and mass loss rate (from R_{200})

$$10^9 h^{-1} M_{\odot} : \quad \tau_{\text{lag}} = \frac{R_{200}}{v_{\text{esc}}} \simeq \frac{20 \text{ kpc}}{20 \text{ km s}^{-1}} \simeq 1 \text{ Gyr}$$

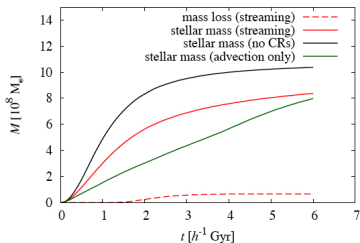
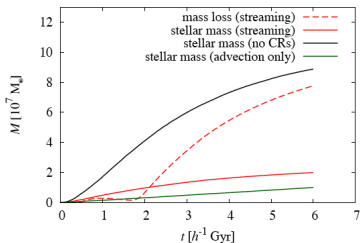
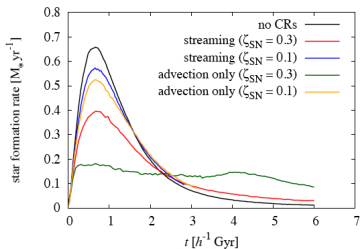


Mass loss and star formation histories

$10^9 h^{-1} M_{\odot}$ halo

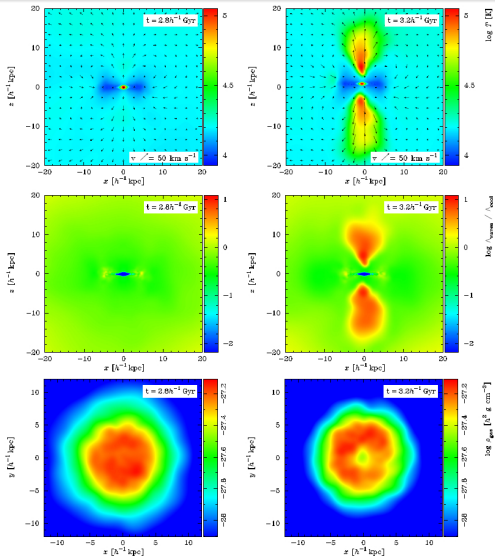


$10^{10} h^{-1} M_{\odot}$ halo

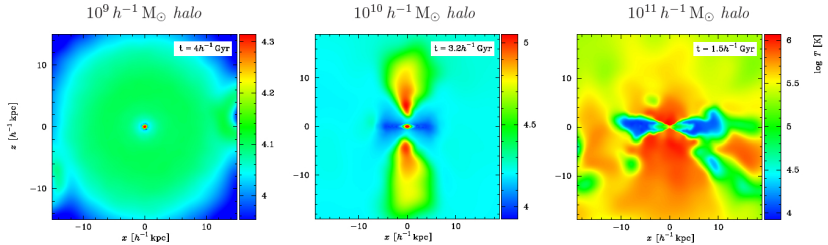


Heating of the halo gas by wave damping

$10^{10} h^{-1} M_{\odot}$:



Temperature structure

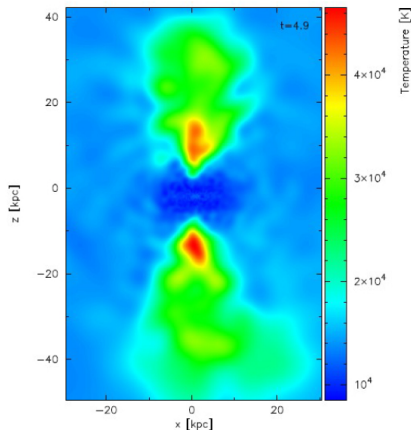


- halo temperatures scale as $kT \propto v_{\text{wind}}^2 \sim v_{\text{esc}}^2$
- $10^9 \rightarrow 10^{10} M_{\odot}$: **transition of isotropic to bi-conical wind**; in these cones, CR wave heating overcomes radiative cooling
- $10^{10} \rightarrow 10^{11} M_{\odot}$: **broadening of hot temperature structure** due to inability of CR streaming to drive a sustained wind; instead, fountain flows drive turbulence, thereby heating larger regions



Gas temperature: simulation ($10^{10} M_{\odot}$) vs. observation

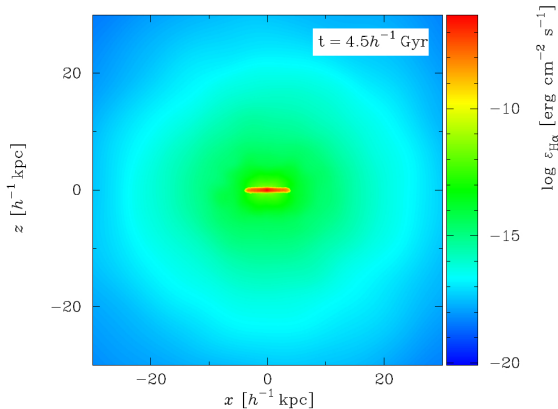
$t = 4.9$ Gyr, streaming



M82



H α emission ($10^{10} M_{\odot}$)

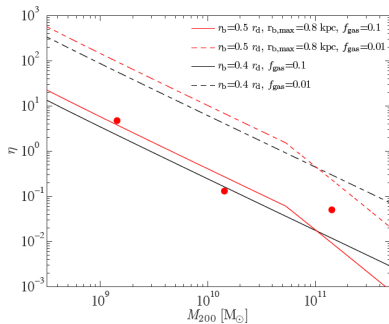
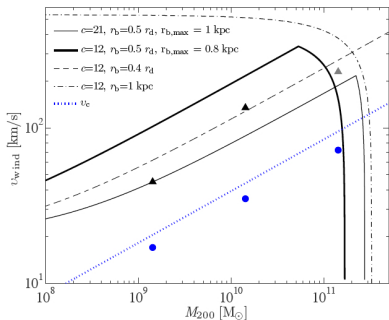


- diffuse H α emission by ionized gas, entrained in the wind
- no conical, filamentary structure as in M82:
numerics, missing physics, ... ?



CR-driven winds: analytics versus simulations

Wind speeds and mass loading factors

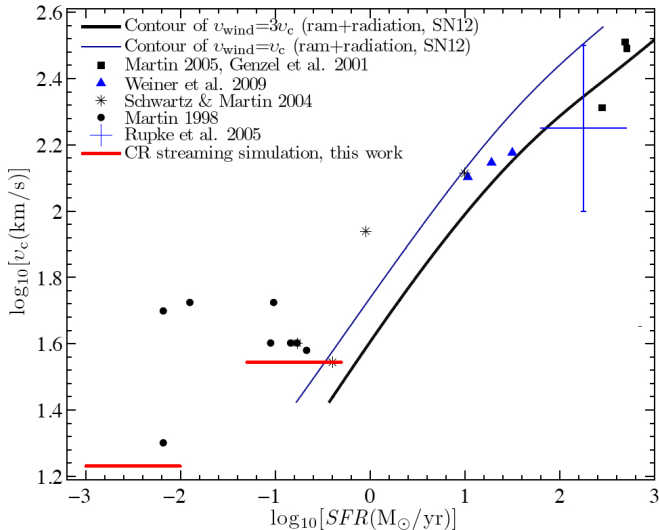


- **winds speeds increase with galaxy mass** as $v_{wind} \propto v_{circ} \propto M_{200}^{1/3}$ until they cutoff around $10^{11} M_{\odot}$ due to a fixed wind base height (set by radiative physics)
- **mass loading factor $\eta = \dot{M}/\text{SFR}$ decreases with galaxy mass**



Comparing different wind launching mechanisms

Galactic winds driven by CR streaming, ram and radiation pressure



Conclusions on cosmic-ray driven winds in galaxies

- galactic winds are naturally explained by CR streaming (energy source, known plasma physics, observed scaling relations)
- CR streaming heating can explain observed hot wind regions above disks
- substantial mass losses of low mass galaxies
→ opportunity for understanding the physics at the faint end of galaxy luminosity function

outlook: MHD simulations, better understanding of plasma physics, cosmological settings, . . .



Literature for the talk

Magnetic draping:

- Pfrommer & Dursi, *Detecting the orientation of magnetic fields in galaxy clusters*, Nature Phys., 6, 5206, 2010.
- Dursi & Pfrommer, *Draping of cluster magnetic fields over bullets and bubbles – morphology and dynamic effects*, ApJ, 677, 993, 2008.

CR-driven winds in galaxies:

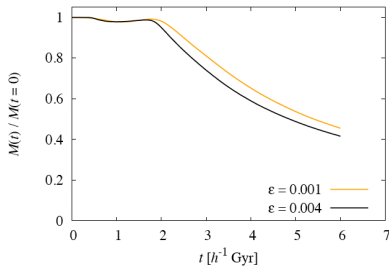
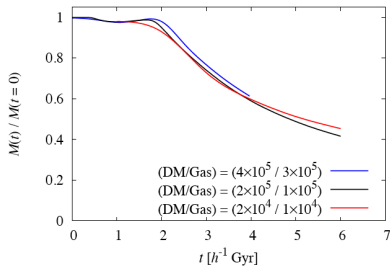
- Uhlig, Pfrommer, Sharma, Nath, EnBlin, Springel, *Galactic winds driven by cosmic-ray streaming*, MNRAS, 423, 2374, 2012.



Additional slides



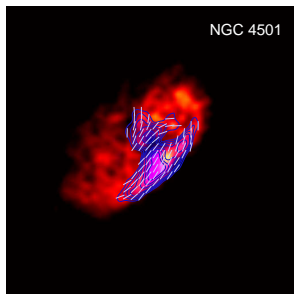
Resolution study



- our results winds driven by CR streaming are converged with respect to particle resolution (*left*) and time step of the explicit streaming solver (*right*)



Magnetic coherence scale estimate by radio ridges



- observed polarised draping emission
→ field coherence length λ_B is at least galaxy-sized
- if $\lambda_B \sim 2R_{\text{gal}}$, then the change of orientation of field vectors imprint as a change of the polarisation vectors along the vertical direction of the ridge showing a ‘polarisation-twist’
- the reduced speed of the boundary flow means that a small L_{drape} corresponds to a larger length scale of the unperturbed magnetic field ahead of the galaxy NGC 4501

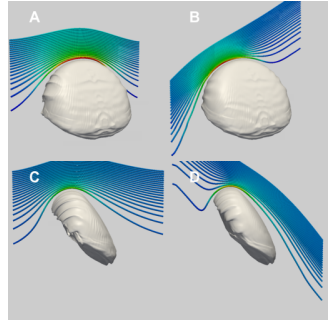
$$L_{\text{coh}} \simeq \eta L_{\text{drape}} v_{\text{gal}} / v_{\text{drape}} = \eta \tau_{\text{syn}} v_{\text{gal}} > 100 \text{ kpc},$$

with $\tau_{\text{syn}} \simeq 5 \times 10^7 \text{ yr}$, $v_{\text{gal}} \simeq 1000 \text{ km/s}$, and a geometric factor $\eta \simeq 2$



Biases in inferring the field orientation

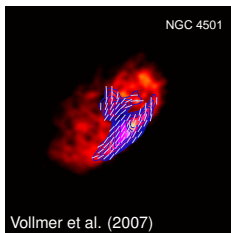
- uncertainties in estimating the 3D velocity: v_r , ram-pressure stripped gas visible in HI morphology $\rightarrow \hat{\mathbf{v}}_t$
- *direction-of-motion asymmetry*: magnetic field components in the direction of motion bias the location of $B_{\max, \text{drape}}$ (figure to the right): draping is absent if $\mathbf{B} \parallel \mathbf{v}_{\text{gal}}$



- *geometric bias*: polarized synchrotron emission only sensitive to traverse magnetic field B_t (\perp to LOS) \rightarrow maximum polarised intensity may bias the location of $B_{\max, \text{drape}}$ towards the location in the drape with large B_t



Magnetic draping with LOFAR



- NGC 4501: 5 GHz polarized intensity
- lower frequency
→ longer electron cooling time
→ **larger magnetic drape!**
- length scale of draping sheath:

$$\gamma = \left(\frac{2\pi\nu_{\text{syn}}m_e c}{3eB} \right)^{1/2} \simeq 10^4 \left(\frac{\nu_{\text{syn}}}{5 \text{ GHz}} \right)^{1/2} \left(\frac{B}{7 \mu\text{G}} \right)^{-1/2},$$

$$\tau_{\text{syn}} = \frac{6\pi m_e c}{\sigma_T B^2 \gamma} \simeq 50 \text{ Myr} \left(\frac{\nu_{\text{syn}}}{5 \text{ GHz}} \right)^{-1/2} \left(\frac{B}{7 \mu\text{G}} \right)^{-3/2},$$

$$L_{\text{drape}} = \eta v_{\text{drape}} \tau_{\text{syn}} \simeq 10 \text{ kpc} \left(\frac{\nu_{\text{syn}}}{5 \text{ GHz}} \right)^{-1/2} \simeq \mathbf{60 \text{ kpc}} \left(\frac{\nu_{\text{syn}}}{150 \text{ MHz}} \right)^{-1/2},$$

with velocity in draping layer $v_{\text{drape}} \simeq 100 \text{ km s}^{-1}$ and a geometric factor $\eta \simeq 2$.



Magneto-thermal instability: the idea

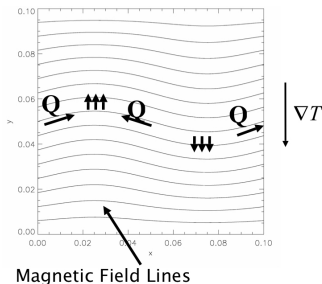


Figure from I. Parrish

Convective stability in a gravitational field:

- Classical Schwarzschild criterion:
 $\frac{dS}{dz} > 0$
- long MFP, Balbus criterion: $\frac{dT}{dz} > 0$
- **new instability causes field lines to reorient radially → efficient thermal conduction radially (close to Spitzer)**

The non-linear behavior of the MTI (Parrish & Stone 2007).

- **Adiabatic boundary conditions for $T(r)$** : the instability can exhaust the source of free energy → isothermal profile
- **Fixed boundary conditions for $T(r)$** : field lines stay preferentially radially aligned (35 deg mean deviation from radial)

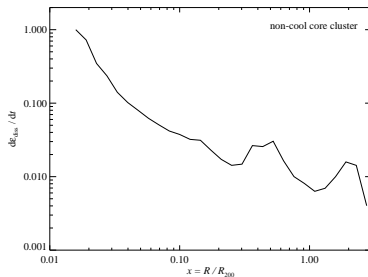
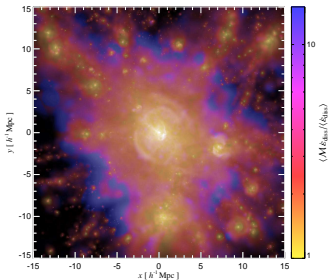


Gravitational shock wave heating

Observed temperature profile in clusters is decreasing outwards

→ heat also flows outwards along the radial magnetic field.

How is the temperature profile maintained? → gravitational heating



shock strengths weighted by dissipated energy

energy flux through shock surface

$$\dot{E}_{\text{diss}}/R^2 \sim \rho v^3$$

→ increase towards the center

