

Lensing autospectrum

Autospectrum current state-of-the-art

Also: SPTpol (Story+ 2015)
PolarBear (2015)

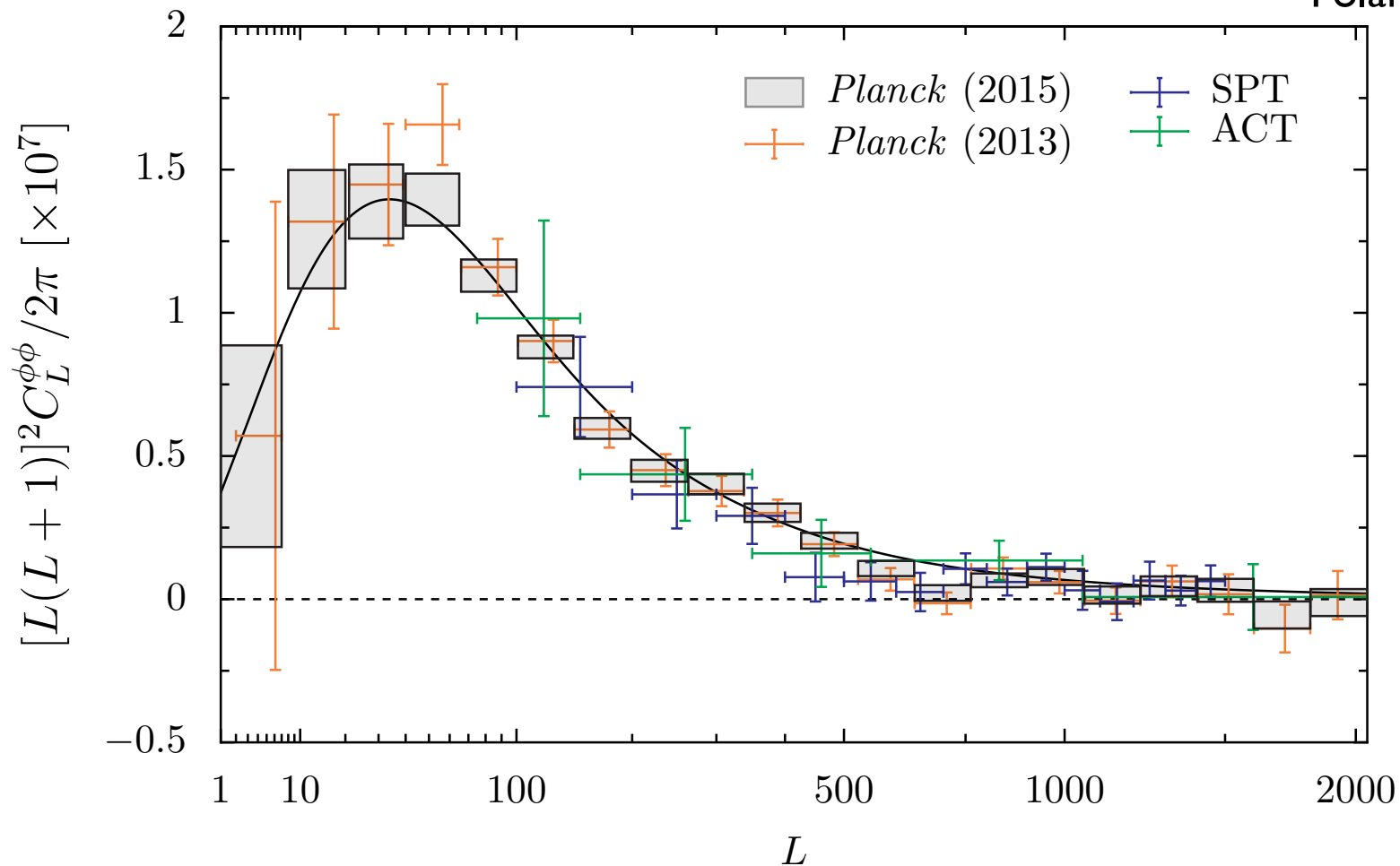
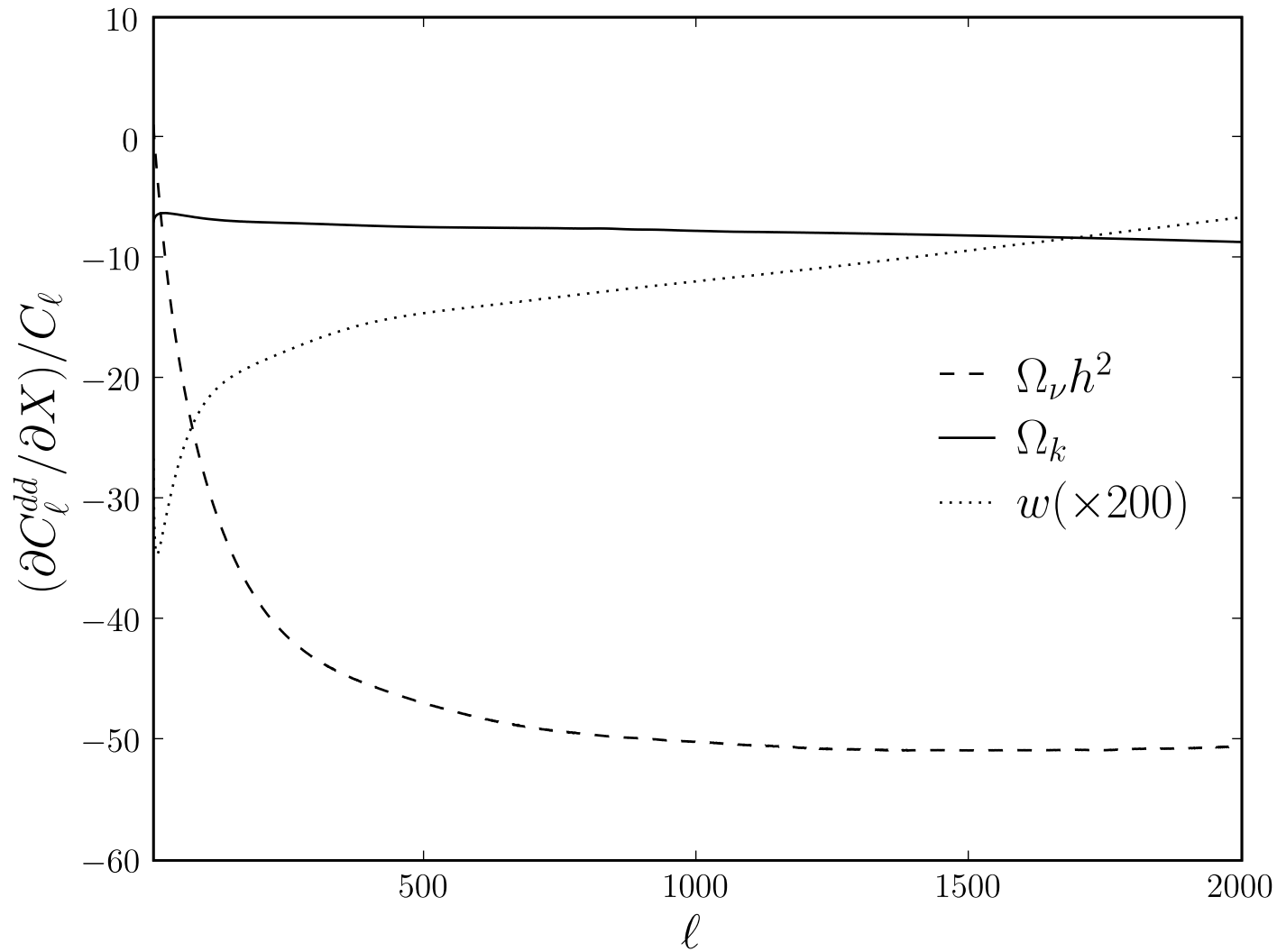


Fig. 6 *Planck* 2015 full-mission MV lensing potential power spectrum measurement, as well as earlier measurements using the *Planck* 2013 nominal-mission temperature data ([Planck Collaboration XVII 2014](#)), the South Pole Telescope (SPT, [van Engelen et al. 2012](#)), and the Atacama Cosmology Telescope (ACT, [Das et al. 2014](#)). The fiducial Λ CDM theory power spectrum based on the parameters given in Sect. 2 is plotted as the black solid line.

Parameter dependence



What is possible with S4?

Noise per Fourier mode in reconstructed lensing field

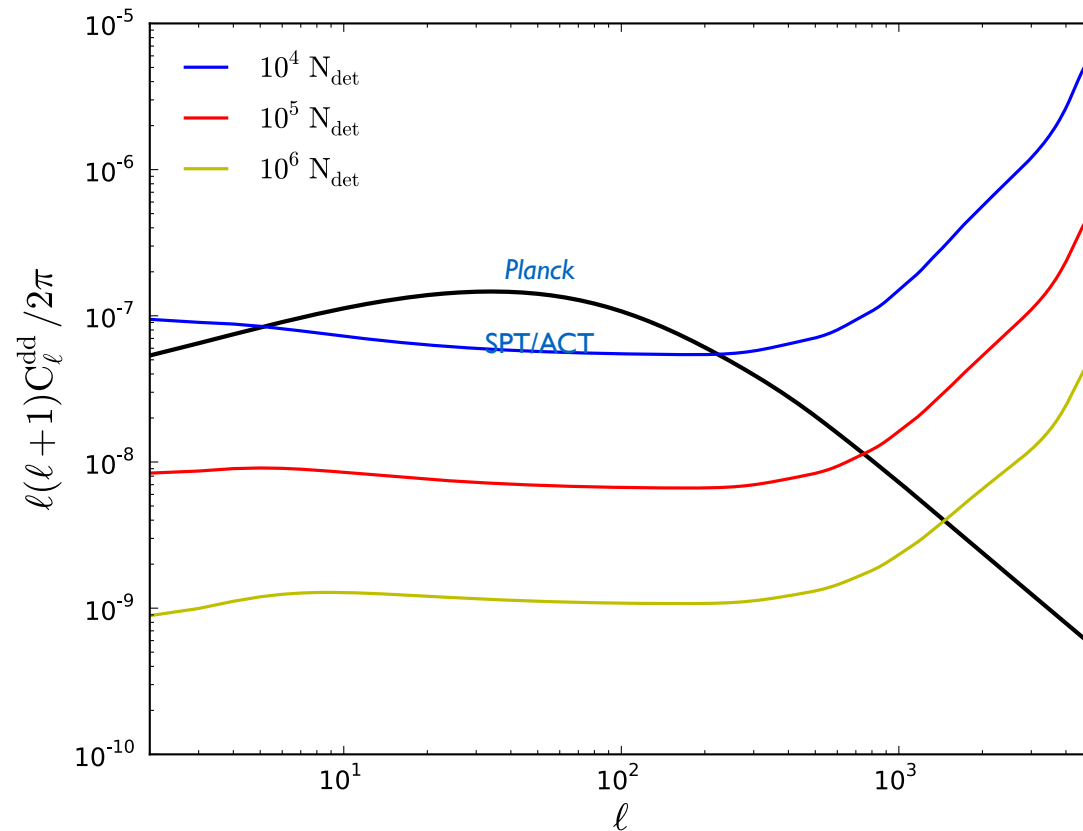
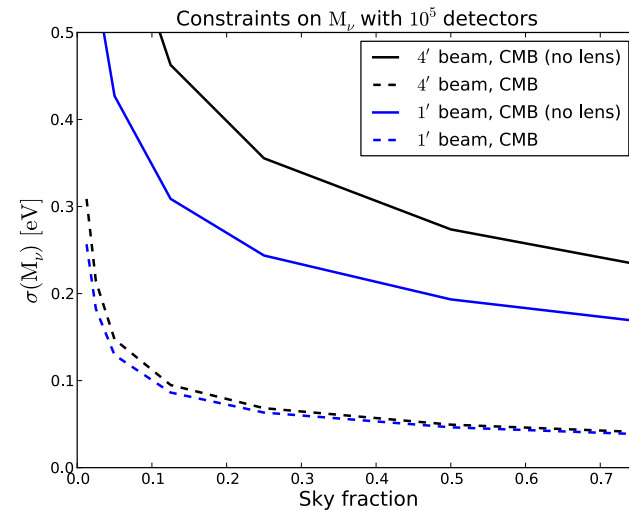


Figure 1: N_ℓ^{dd} for three N_{det} at $f_{\text{sky}} = 0.75$ and $1'$ beam size. The deflection angle spectrum C_ℓ^{dd} is shown in black as reference. C_ℓ^{dd} is related to the lensing power spectrum $C_\ell^{\phi\phi}$ by $C_\ell^{dd} = \ell(\ell+1)C_\ell^{\phi\phi}$.

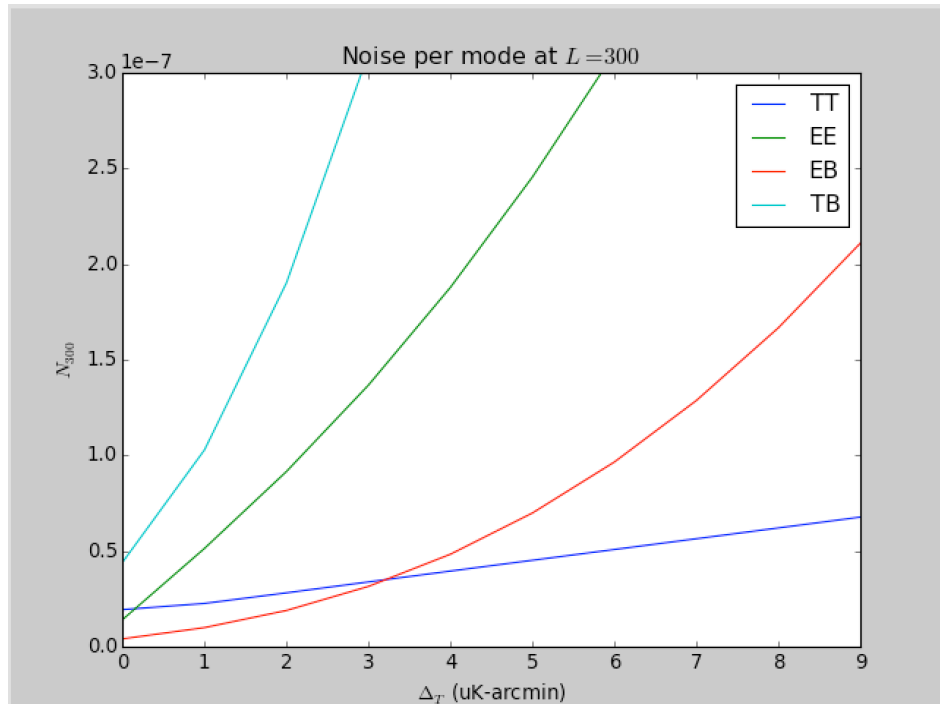
Mnu constraint vs. Beamsize

	CMB				CMB+BAO			
	1'	2'	3'	4'	1'	2'	3'	4'
10⁴ detectors								
$f_{sky} = 0.25$	71.7	72.8	74.4	76.6	22.8	23.0	23.4	23.9
$f_{sky} = 0.50$	54.7	55.7	57.2	59.2	20.6	20.9	21.3	21.9
$f_{sky} = 0.75$	48.1	49.0	50.5	52.5	20.1	20.4	20.9	21.5
10⁵ detectors								
$f_{sky} = 0.25$	63.3	65.2	66.7	68.3	19.7	19.8	19.9	20.1
$f_{sky} = 0.50$	46.4	47.2	48.2	49.4	16.9	17.0	17.1	17.2
$f_{sky} = 0.75$	38.5	39.2	40.0	41.0	15.7	15.8	15.9	16.0
10⁶ detectors								
$f_{sky} = 0.25$	54.9	58.1	62.2	64.7	19.1	19.2	19.3	19.4
$f_{sky} = 0.50$	40.8	42.7	45.1	46.5	16.4	16.4	16.5	16.6
$f_{sky} = 0.75$	34.1	35.7	37.2	38.3	15.1	15.2	15.3	15.3

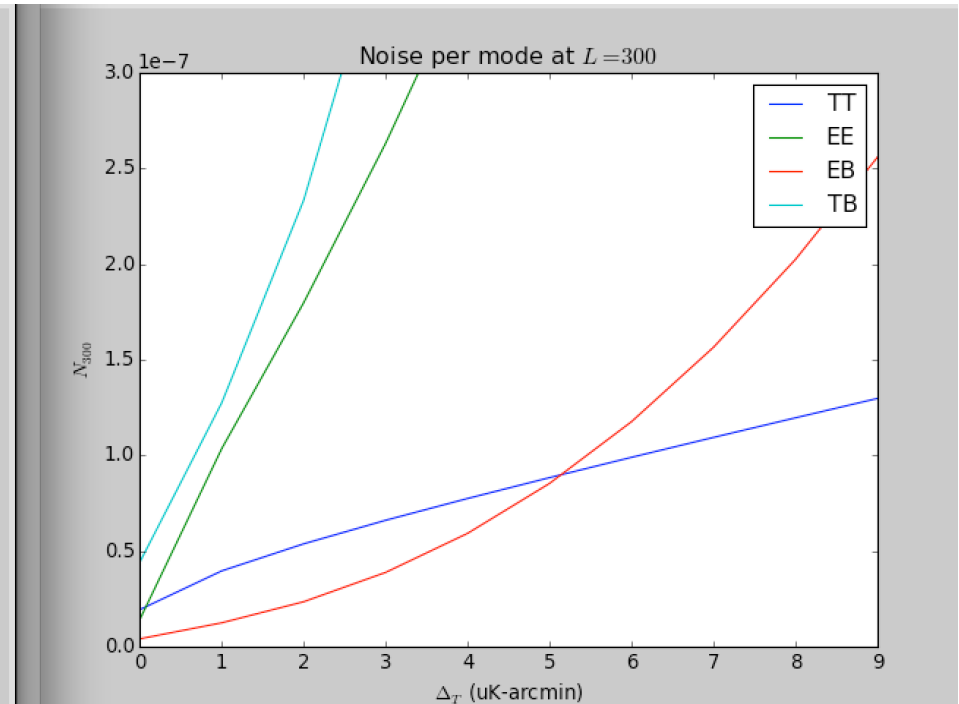
Table III: 1- σ constraints on M_ν , in units of meV, from CMB and from CMB+BAO. “CMB” includes lensing.



- To date, all results have been obtained with Hu and Okamoto quadratic estimator
- To date, lensing temperature has dominated S/N in results
(exception: Polarbear 2015, 4σ pol. lensing)
- At low noise these both change - we are in a new regime



4' beam



1.4' beam

Note: no iterative delensing here; factor of a few at low noise

Noise levels & Delensing

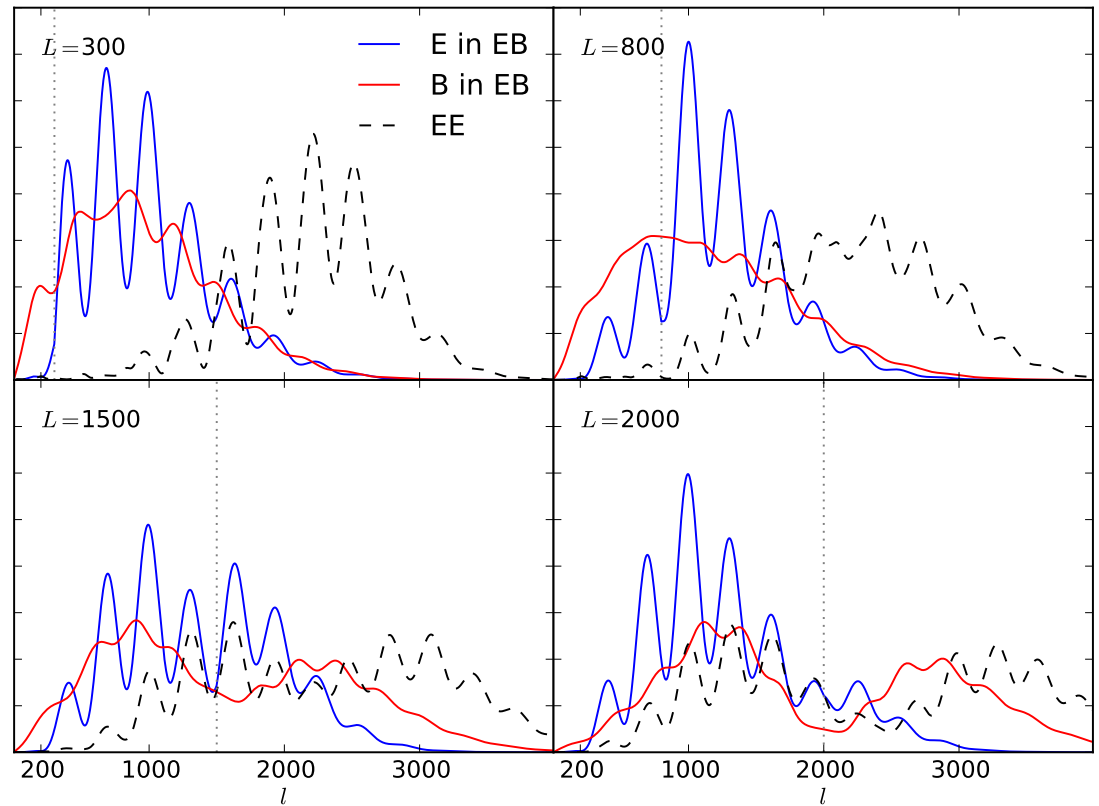
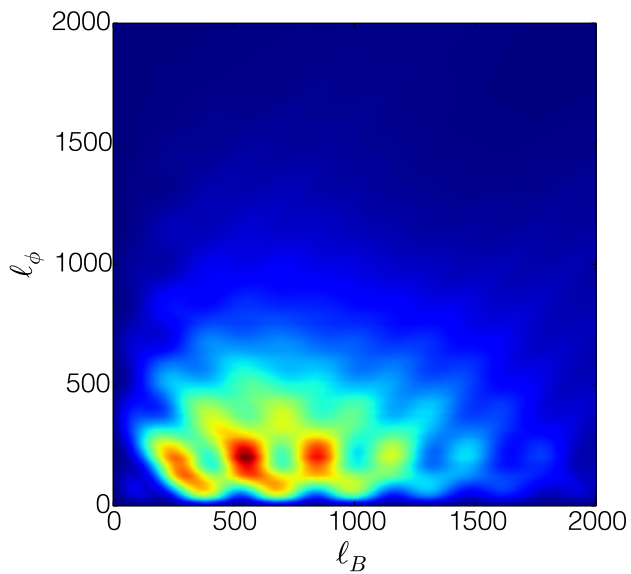
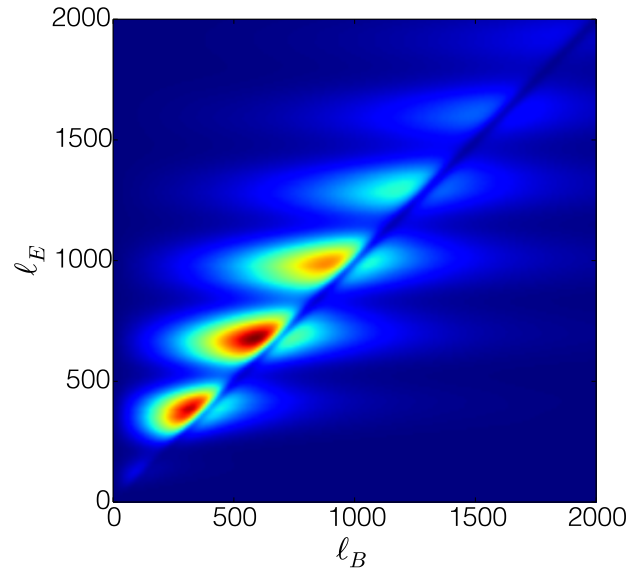
- Lensed B-modes give a **noise floor of 5 $\mu\text{K-arcmin}$**
- Hu & Okamoto quadratic estimator becomes non-optimal
 - Hirata & Seljak maximum likelihood method (or something like it) necessary
 - Reconstruction and Delensing strongly linked
- Forecasted lensing noise based on iterative delensing idea

$$N_{\ell}^{\phi\phi} = \left[\frac{1}{2\ell + 1} \sum_{\ell_1 \ell_2} |f_{\ell_1 \ell_2 \ell}^{EB}|^2 \left(\frac{1}{C_{\ell_1}^{B_{\text{res}}} + N_{\ell_1}^{BB}} \right) \left(\frac{(C_{\ell_2}^{EE})^2}{C_{\ell_2}^{EE} + N_{\ell_2}^{EE}} \right) \right]^{-1}$$

$$C_{\ell_1}^{B_{\text{res}}} = \frac{1}{2\ell_1 + 1} \sum_{\ell_2 \ell} |f_{\ell_1 \ell_2 \ell}^{EB}|^2 \left[C_{\ell_2}^{EE} C_{\ell}^{\phi\phi} - \left(\frac{(C_{\ell_2}^{EE})^2}{C_{\ell_2}^{EE} + N_{\ell_2}^{EE}} \right) \left(\frac{(C_{\ell}^{\phi\phi})^2}{C_{\ell}^{\phi\phi} + N_{\ell}^{\phi\phi}} \right) \right]$$

starting by taking $C_{\ell}^{B_{\text{res}}} = C_{\ell}^{B_{\text{len}}}$ in the first iteration.

Which CMB modes need to be measured?



$$A_{ij}(L, l_1) \propto \int l_1 d\varphi_{l_1} f_{ij}(\mathbf{l}_1, \mathbf{l}_2) W_{ij}(\mathbf{l}_1, \mathbf{l}_2)$$

$$\ell_B (\partial C_{\ell_B}^B / \partial C_{\ell_X}^X) C_{\ell_X}^X \text{ where } X \in \{E, \phi\}$$

Which algorithm to use?

- Hirata & Seljak (2003) global maximum likelihood
- Local maximum likelihood (Anderes+ 2011)
- Iterative template solution (Hanson, Smith, Dvorkin)
- Gibbs sampling (Anderes+ 2015)
- Others?

Extragalactic foregrounds?

- For single-frequency temperature maps, the **trispectra of point sources and tSZ** give few-%-level biases (van Engelen+2013, Osborne+2013)
 - size of bias depends strongly on both **beam size** (flux cut) and **map noise level**
 - clustering of sources and correlation with φ both give contributions

Projecting out the foregrounds

Temperature case: Osborne+ 2013

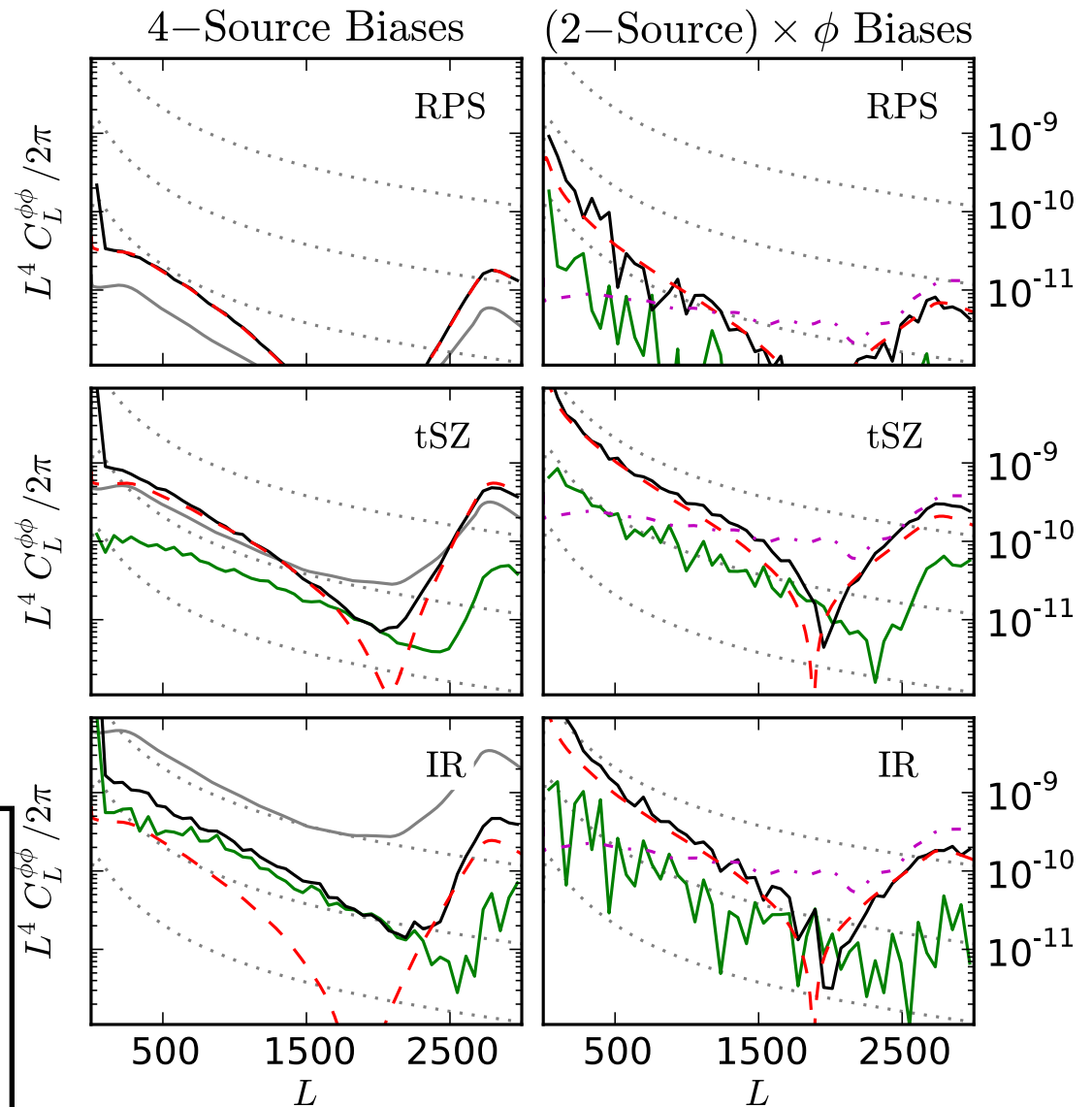
- Project data-derived $S^2 \times S^2$ and $S^2 \times \phi$ terms from the lensing estimate -- “bias-hardening”

Black: Sehgal 2010 sim

Green: Sehgal 2010, bias-hardened

Red: simple modelling

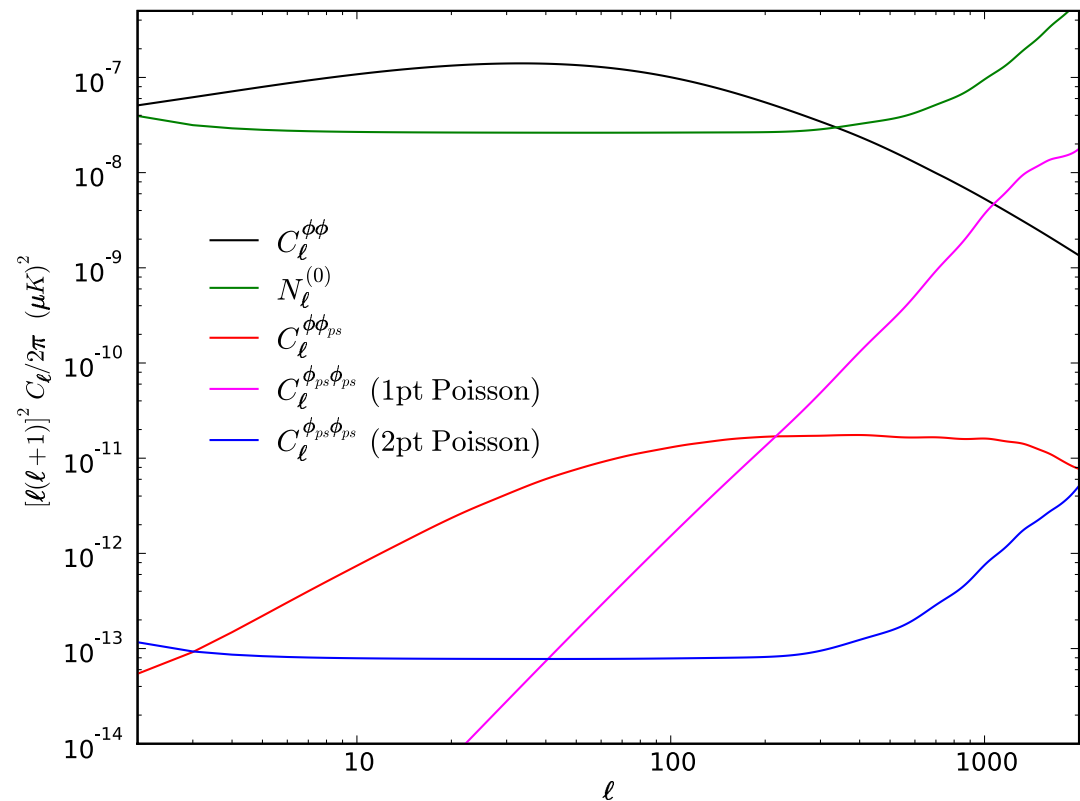
Grey: disconnected N0 bias



Here, $l_{\max} = 3000$, no noise

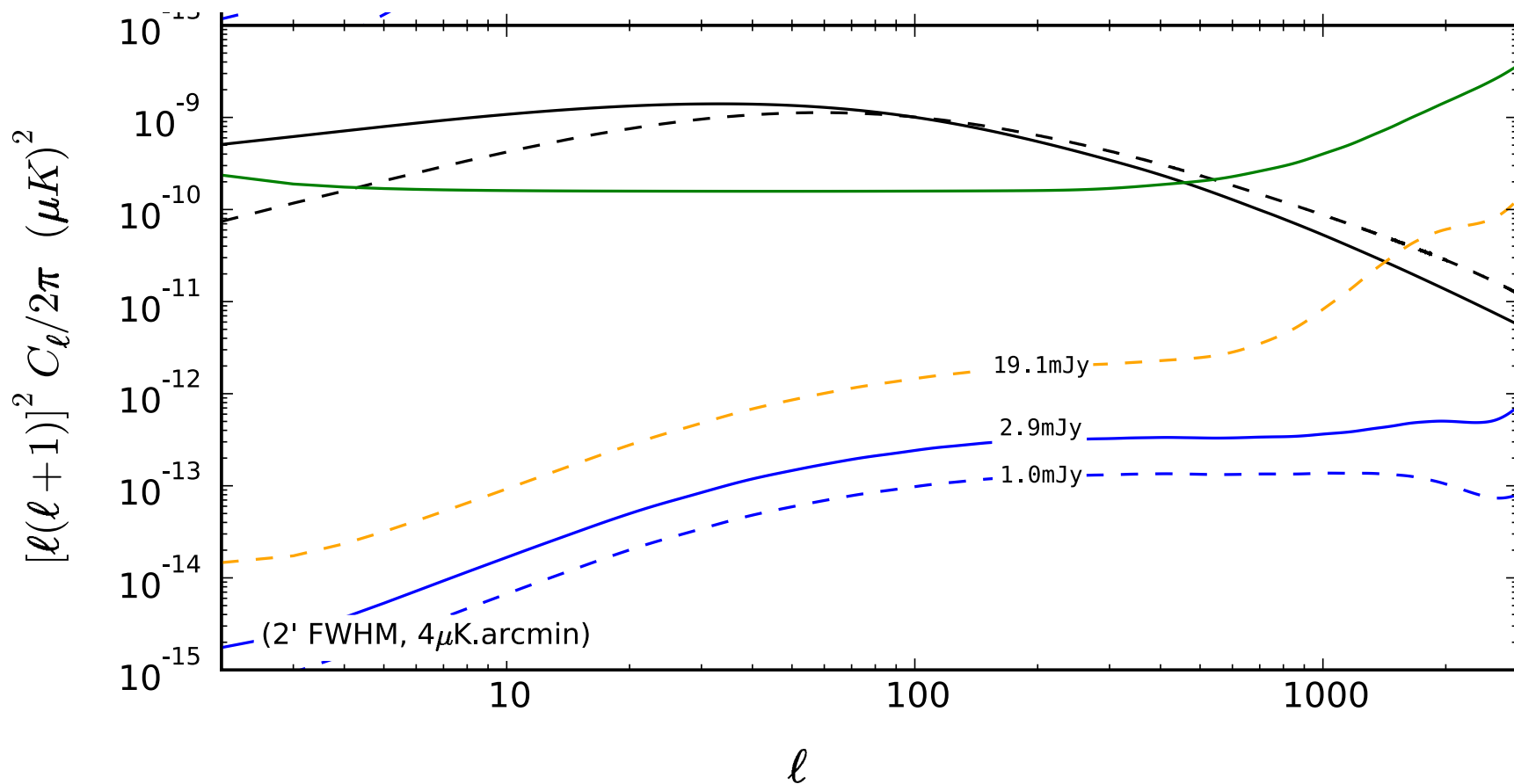
Polarized extragalactic sources

- CMBPol white paper (Smith+ 2008)
 - assume Poisson radio sources (but correlated with φ) at 150GHz
 - 10% pol. fraction
- Biases small



Polarized extragalactic sources

- Strong dependence on flux cut (beam size)



CMBPol white paper (Smith+ 2008)

Galactic Dust?

- How large is the four-point function of polarized galactic dust at high l ?

Instrumental Systematics

- What level of control do we need on these?
 - gain variations, monopole leakage, quadrupole leakage, pointing/beam offsets
- Is the BB power spectrum (or other quadratic estimators) a useful diagnostic after data are taken?

Impact of nonlinear growth?

- Bias from 2nd order perturbations (tree-level bispectrum)
- $\sim 1\%$ for an ACT-like survey

