

# Intermittent non-Gaussianity & Anomalies: rare patchy subdominants from Modulated Heating, Bubble Collisions & Oscillons



**Grand Unified Theory of Anomalies TBD**    *Anomalies in Polarization? TBD*

**anomalies are nonG, non-statistical-isotropy. just from broken Gaussianity?**

**WMAP cold spot anomaly: coherent in scale space 1:497 @826', 1:9 @360'**

power spectrum asymmetry: 7% at loL, unclear if any at hiL. Doppler dipole modulation exists

**P13 hiL nonG pattern constraints are restrictive, but open up with decoupled  $\zeta_{NL}$ , support( $\zeta_{NL}$ )<sup>3</sup> & need further exploration of nonG with a built-in scale, related to radically broken scale invariance**

**$\zeta_{NL}(x)$  from "isocon" degrees of freedom cf.  $\zeta_{NL}(x)$  from inflaton**

**modulated heating, ballistic chaos, caustics, shock-in-time,**

**modulators isocon  $\chi(x)$ , axionic-isocon(x) couplings  $g(x)$  super-horizon accessible**

**quantum tunneling landscape, inflating bubbles & bubble-bubble collisions**

**aka theory of nonlinear multi-field dynamics using lattice simulations. symplectic defrost++ code + new spectral code.**

**intermittent nonG:  $\exists$  a statistical landscape of possibilities.**

**allowed level highly constrained, but as observed anomalies?**

**unknown,  $\exists$  much to explore**

Bond, Huang 13a,b

Bond, Frolov, Huang, Kofman 09

Bond, Braden 13

**Bond, Braden, Frolov, Huang 13**

Bond, Braden, Frolov, Huang, Nolta 13

**Bond, Braden, Mersini 13a,b,c**

# **KITP Primordial Cosmology talks of relevance: nonG, Anomalies, ...**

4/08, Christopher Hirata The CMB power asymmetry

4/08, Eiichiro Komatsu Making sense of the "north-south" asymmetry

4/09, Jonathan Braden *Density perturbations from preheating caustics and the Shock-in-time*

4/16, Dick Bond Lunch discussion,  $p(\text{reheating})$ , perturbations and structure of models

4/17, Mustafa Amin *Nonlinear field dynamics after inflation*

## **Observations and Theoretical Challenges in Primordial Cosmology**

Paul Shellard, James Fergusson Non-Gaussian Inflation and Planck

Ben Wandelt *Non-Gaussianity*

Kris Gorski Erikson *Isotropy*

Leonardo Senatore Bottom up overview

Daniel Green Two Interpretations of the Bounds on Non-Gaussianity

Matthew Kleban Fundamental Physics from Cosmology

Antony Lewis, Duncan Hanson *Primordial and kinematic power modulation from Planck*

*Discussion: Cosmology: Where we go from here? Frolov, Contaldi*

## **May: much nonG from LSS observability discussion**

5/02, Marilena LoVerde *Non-Gaussian Mode Coupling and the Statistical Cosmological Principle*

5/14, Dmitri Pogosyan *Geometrical measures for (mildly) non-Gaussian cosmological fields*

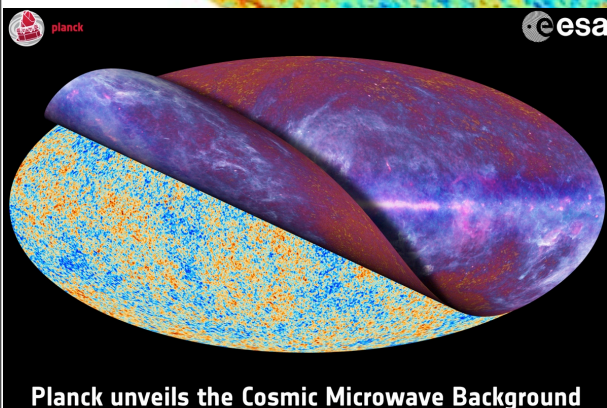
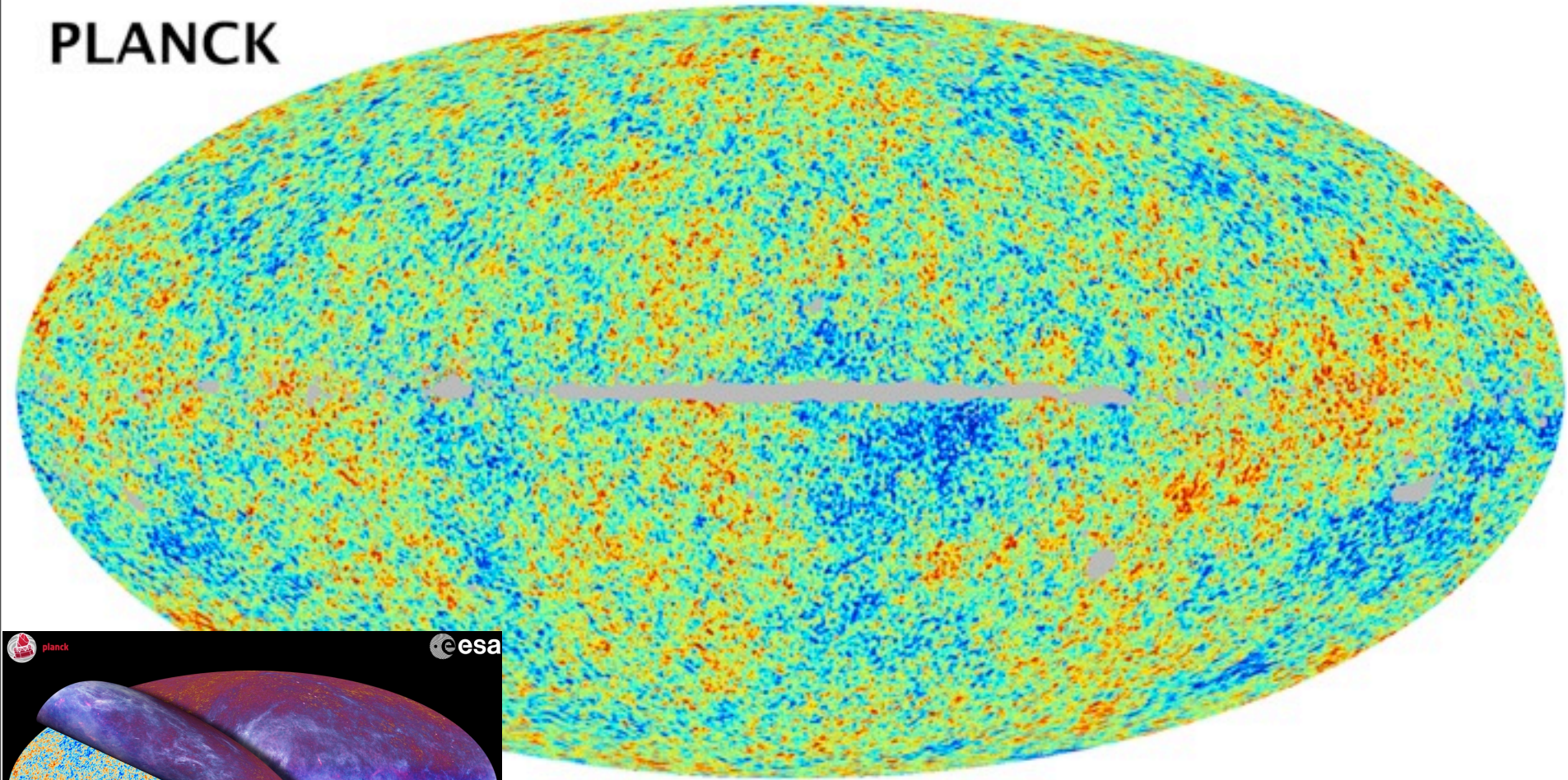
6/13, Matias Zaldarriaga *The effective theory of Large Scale Structure*

*6/25 Dick Bond Intermittent non-Gaussianity and Anomalies: rare patchy subdominants from Modulated Heating, Bubble Collisions & Oscillons*

# Planck SMICA Map

## *CMB-data Concordance*

PLANCK

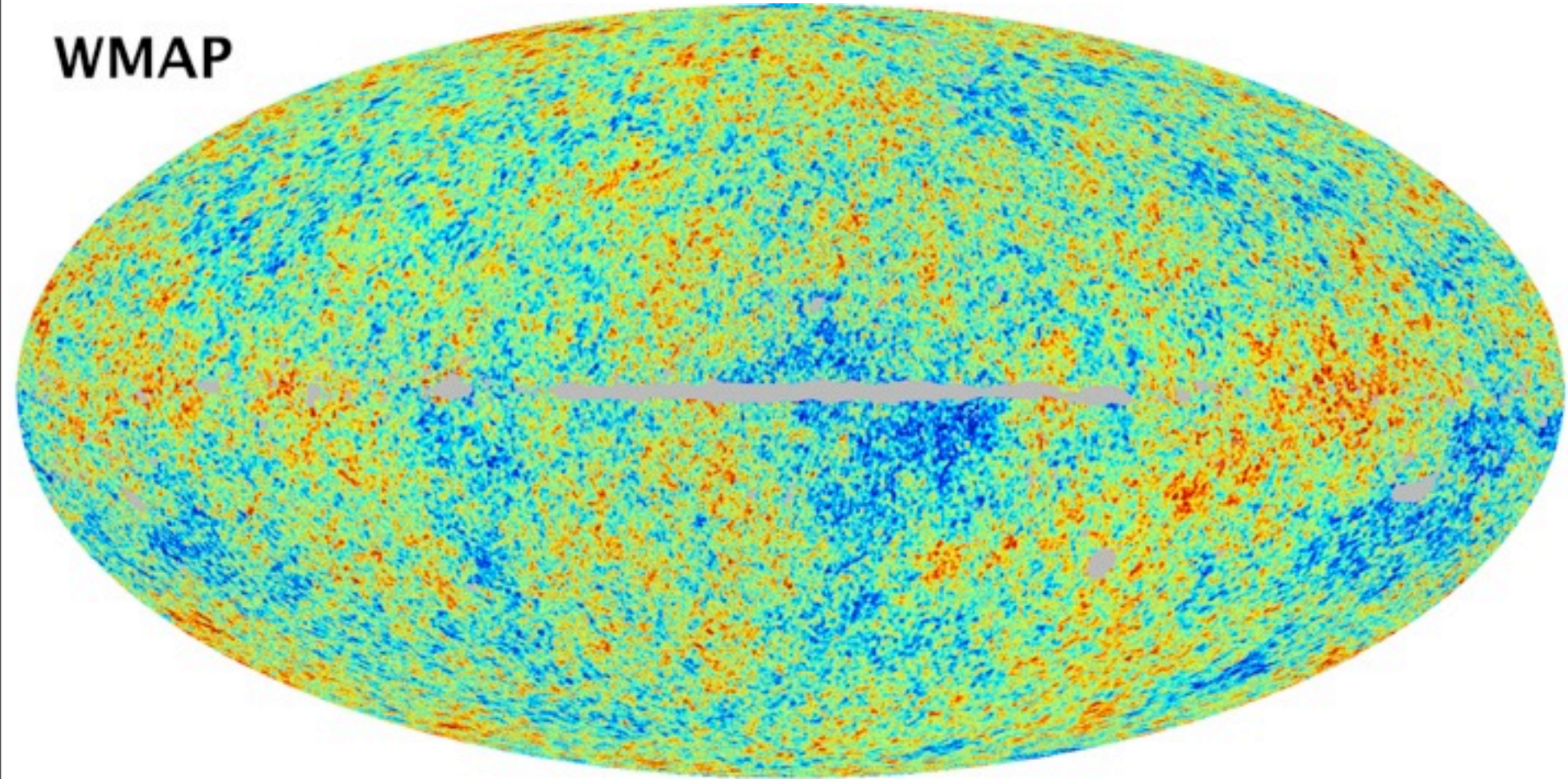


Planck/SMICA map, 5' resolution.

# WMAP W-band, Template Cleaned

## *CMB-data Concordance*

WMAP

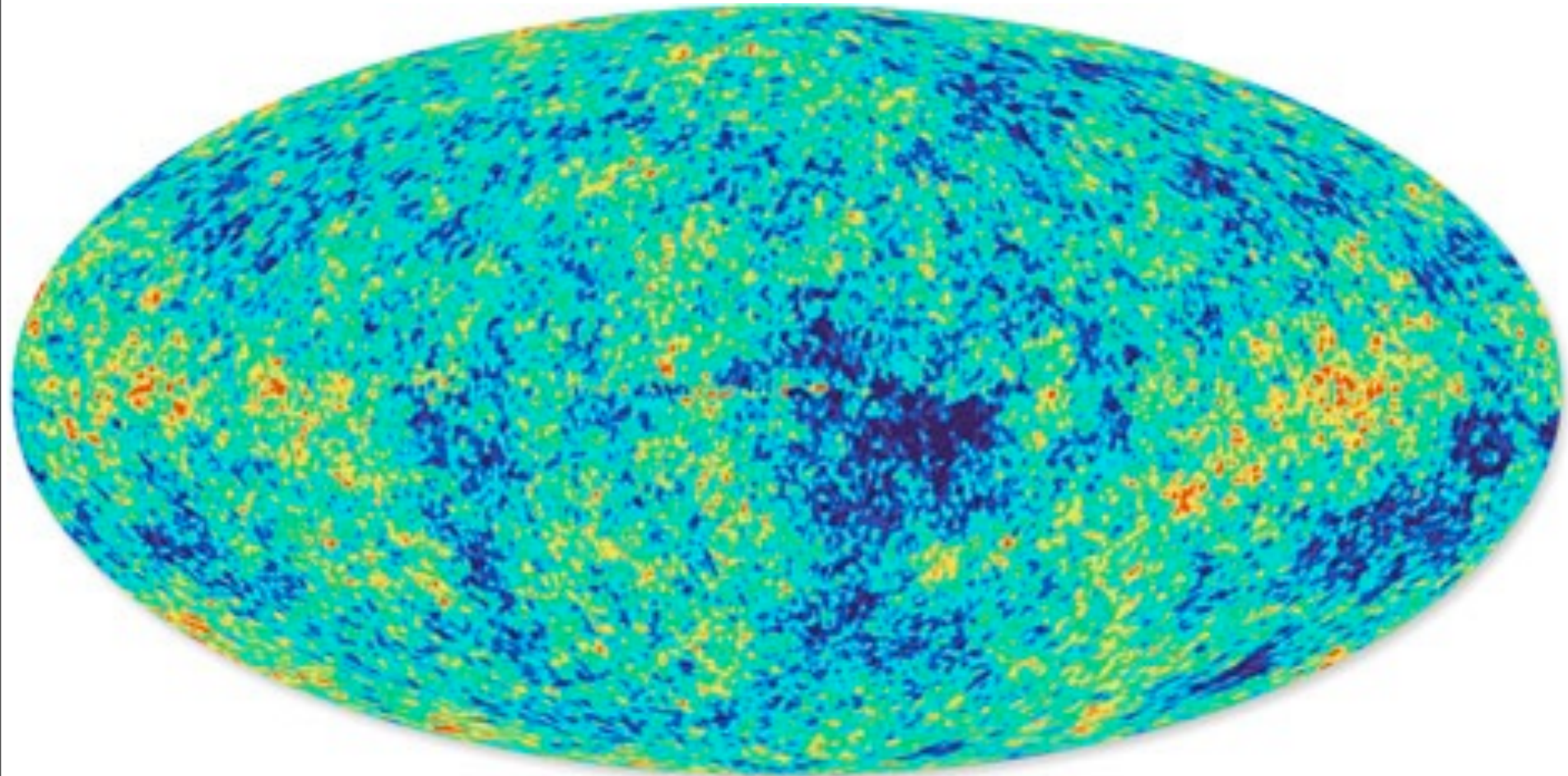


Cleaned with Planck 353 GHz dust map and low-frequency templates. 12' resolution.

**similar tremendous agreement with the much higher (5X) resolution ACT & SPT maps**  
*total focus on the 1.2% difference in "calibration" between P13 (HFI & LFI) & WMAP9*

# WMAP W-band, Template Cleaned

## *CMB-data Concordance*

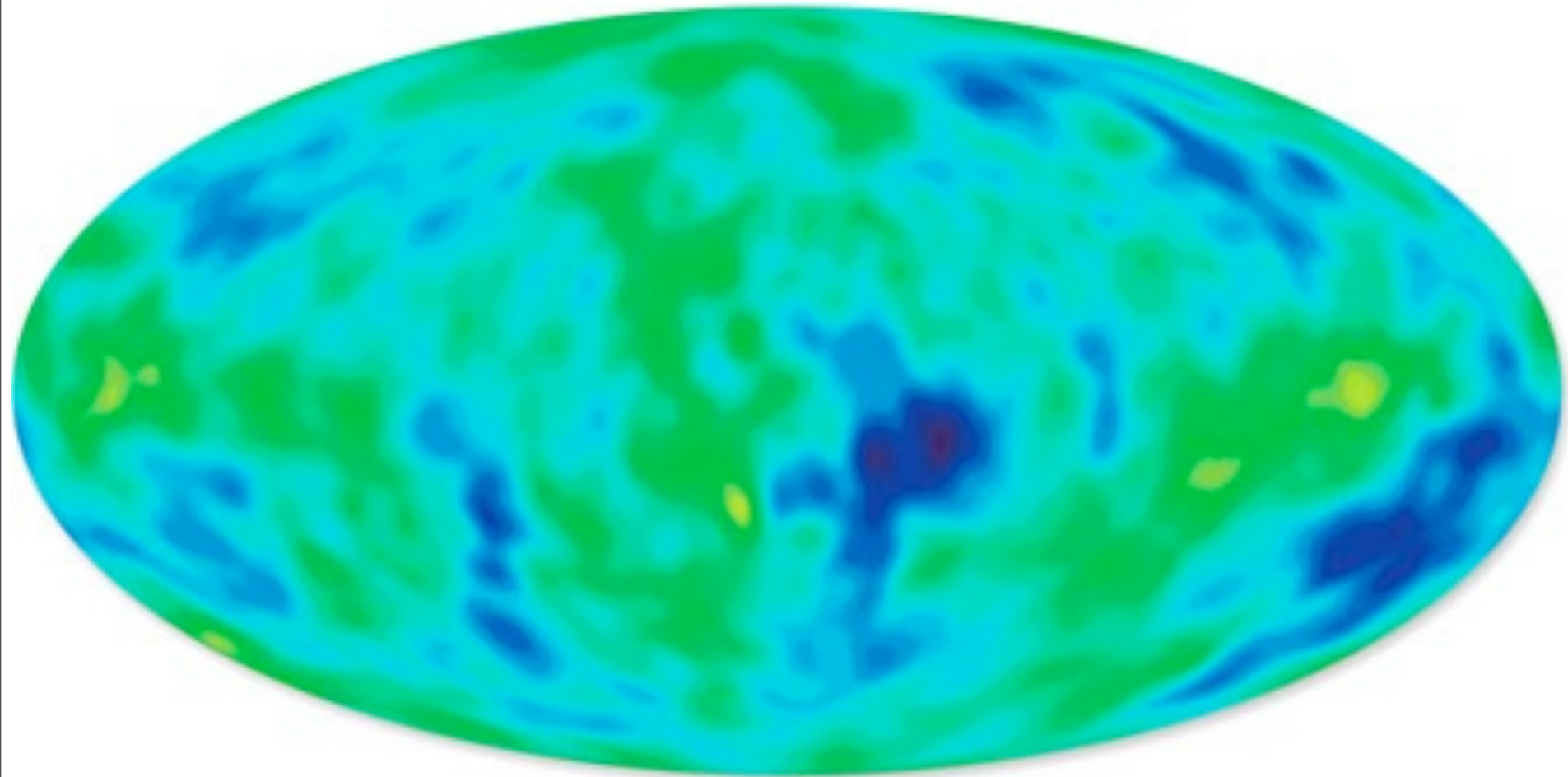


Cleaned with low-frequency templates only.

**similar tremendous agreement with the much higher (5X) resolution ACT & SPT maps**  
*total focus on the 1.2% difference in "calibration" between P13 (HFI & LFI) & WMAP9*

**COBE**

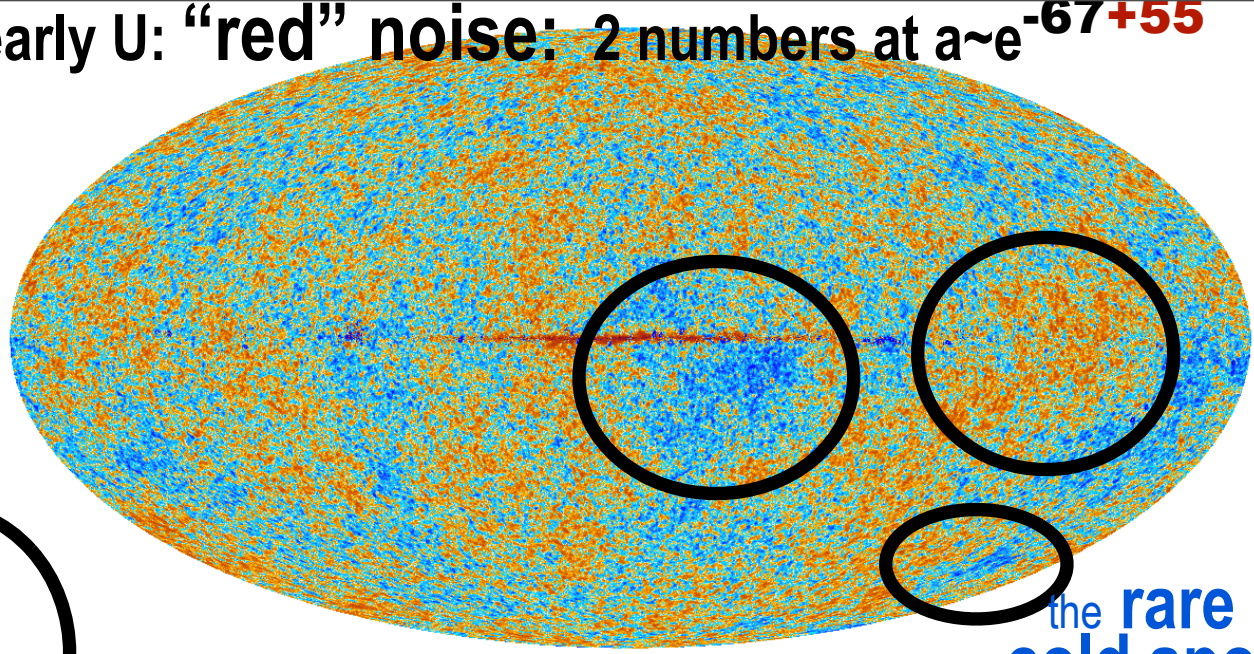
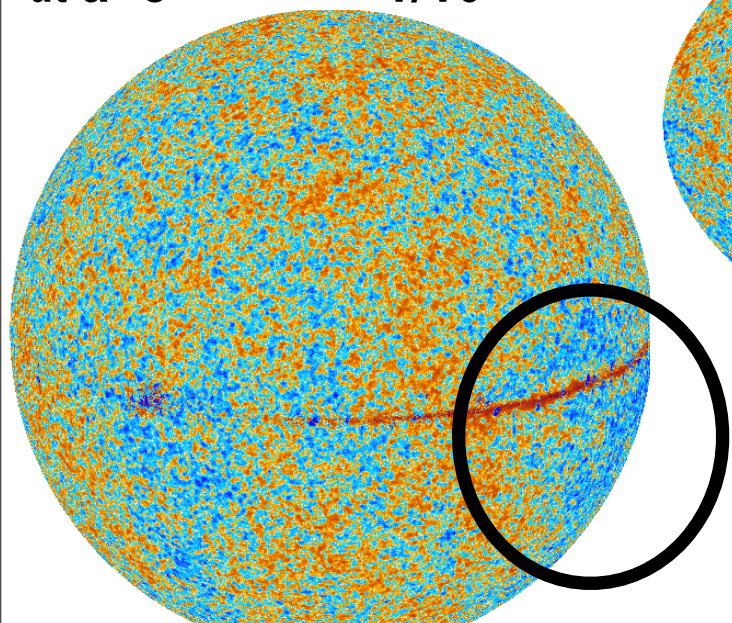
***CMB-data Concordance***



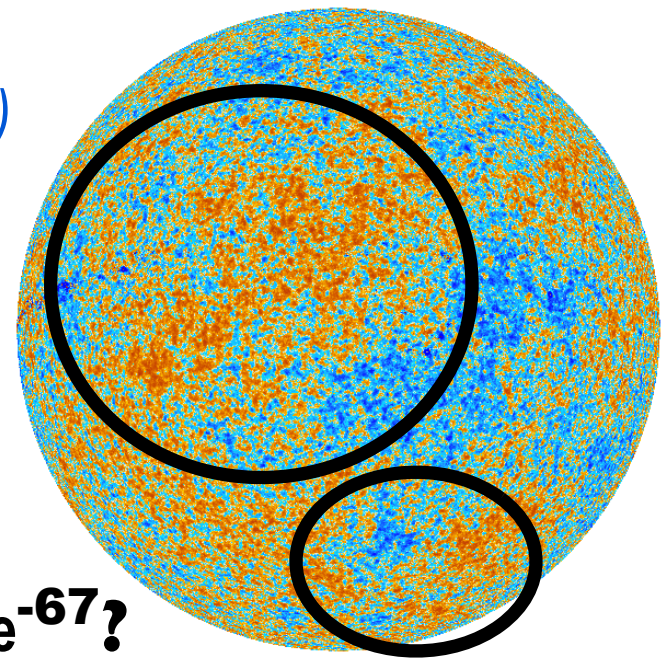
**SIMPLICITY** early U: "red" noise: 2 numbers at  $a \sim e^{-67+55}$

at  $a \sim e^{-7} \sim 1/1100 \Rightarrow$

at  $a \sim e^{-67+60} \sim 1/10^{30+25}$



the rare cold spot



**WHITEN  $\Rightarrow$  MASK  $\Rightarrow$  FILTER BANK** (*SSG42 filter*)

**$\Rightarrow$  EXTRACT PEAKS** (*hierarchical peak patches*)

*filter = extra dimension: scale space analysis ADS of our CFT*

*hot & cold spots agree with BE87 Gaussian stats  $n_{pk}(<v)$*

**PLANCK2013: 826', 105 peaks, coldest  $-4.97\sigma$  1:497**

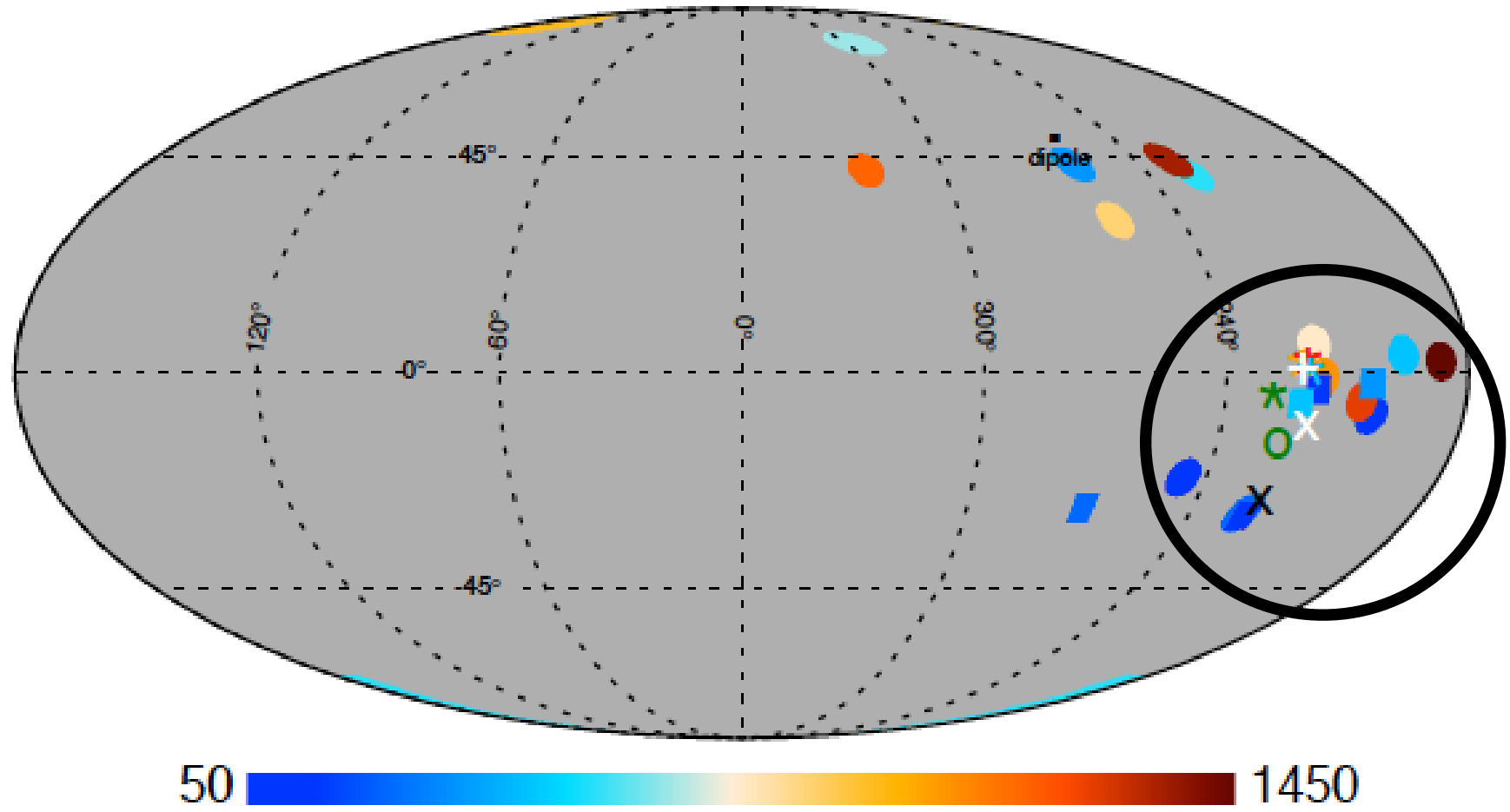
**WMAP7: 800', coldest  $-4.87\sigma$  significance 1:300**

**Anomalies in Polarization? TBD**

**+ anomalies = COMPLEXITY** at  $a \sim e^{-67}$ ?

**power spectrum @ $L < 400$  is low cf.  $L > 400$  forecast for tilted  $\Lambda$ CDM model**  
**power spectrum asymmetry: dipole near Galactic Equator points towards LSS anomaly**

$L < 400$  ~7% anomaly firm (P13&WMAP),  $L > 400$  <0.2% with  $L_{\max}=2000$ ? (**Doppler boost of P13 XXVII cf. P13 XXIII Isotropy & Statistics TBD**) dipole modulation  $(1 - (x \coth(x/2) - 1) \mathbf{q} \cdot \mathbf{v}) \Delta T(\mathbf{q})$ ,  $x = hv/T$  (it works, amp ~.003 to  $\sim 4\sigma$ ) aberration  $\mathbf{q} \Rightarrow \mathbf{q} + \nabla(\mathbf{q} \cdot \mathbf{v})$  -  $5\sigma$  detection of kinematic dipole effects



**Central Multipole**  
*also: octupole quadrupole alignment within ~10 deg;  
correlation function consistent with zero beyond 60 deg*



# primordial nonGaussianity

nonG 3-point-correlation-pattern measure

$f_{NL}$ :  $2.7 \pm 5.8$  local for Newton potential *cf.*  $\pm 5$  (Pext)

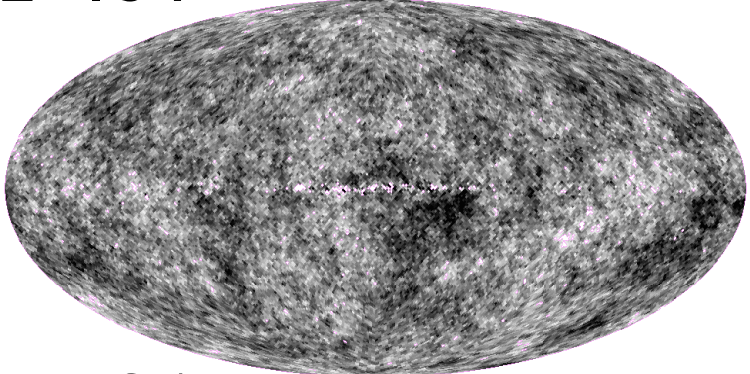
$\Rightarrow f_{NL}^* = 0.44 \pm 3.5$  for phonons/3-curvature

$-f_{NL}$ :  $42.3 \pm 75.2$  equil

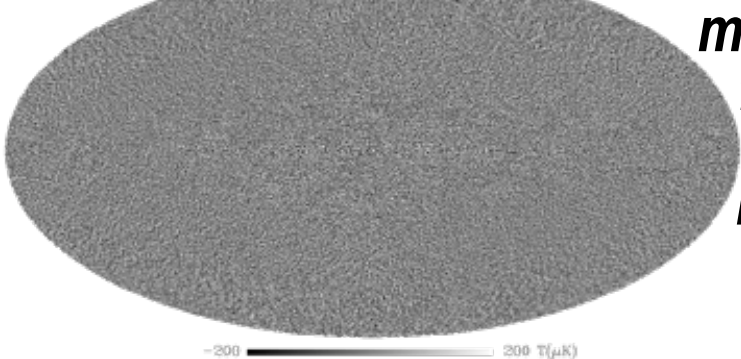
$-25.3 \pm 39.2$  ortho

phonon  $\sim \zeta_{NL} = \ln(\rho a^{3(1+w)})/3(1+w) \Rightarrow f_{NL}^* = 3/5 f_{NL} - 1$

$L < 134$  Planck smoothed to 1deg fwhm



$L > 134$



most nonG info from high L: why Planck improved so much over WMAP9

$$\zeta_{NL}(x) = \zeta_G(x) + f_{NL}^* (\zeta_G^2(x) - \langle \zeta_G^2 \rangle)$$

local smooth.  
use optimal pattern estimators

*cf.* DBI inflation: non-quadratic kinetic energy

$\zeta_{NL}(x) =$   
equilateral pattern & orthogonal pattern

scale (k) dependent patterns: connecting to power spectrum broken scale invariance. hint?

**cosmic/fundamental strings/defects**

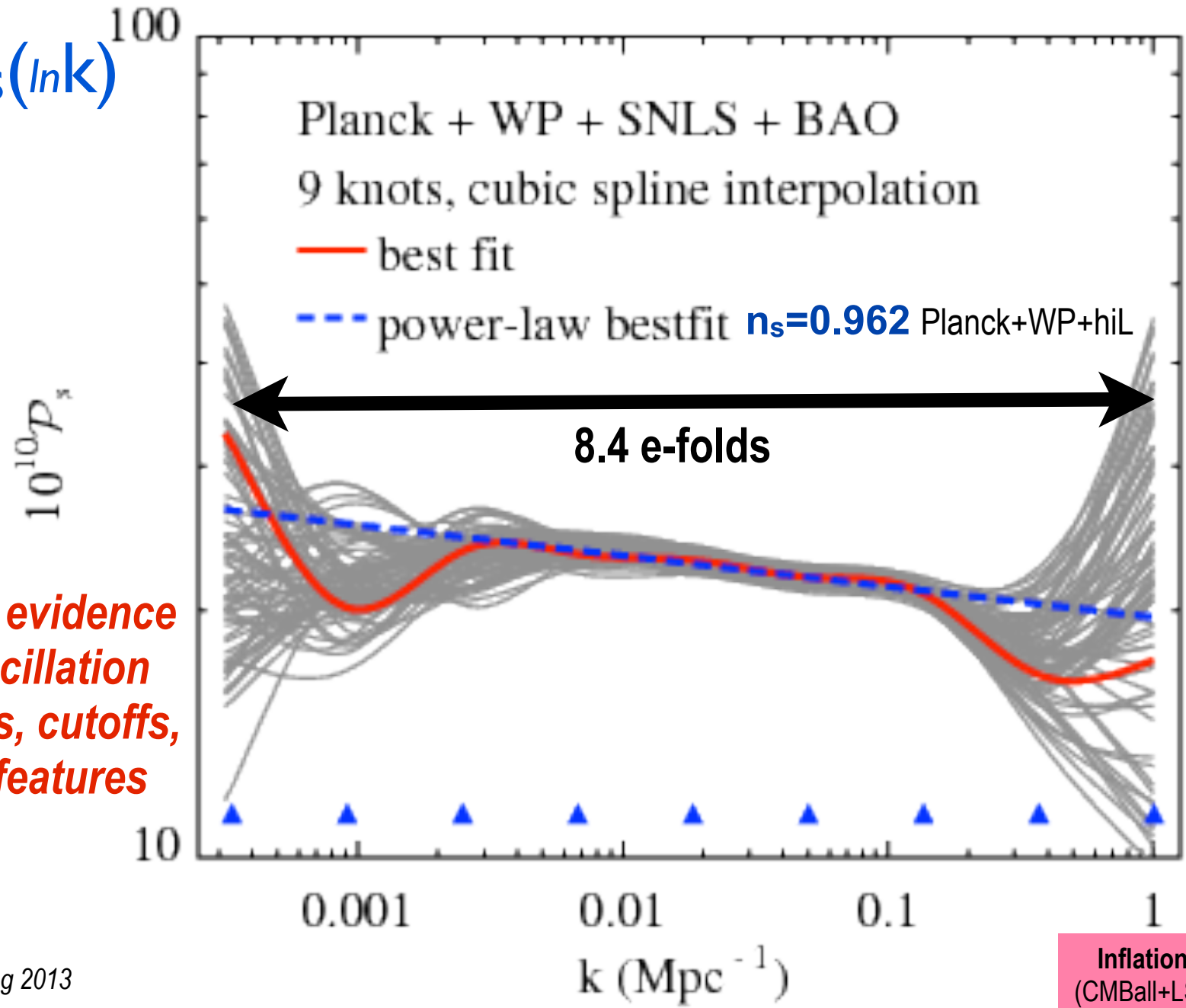
from end-of-inflation & preheating chaos

$\downarrow$   $F_{NL}(\chi_b(x))$   
**intermittent CMB power bursts from super-bias of a GRF modulating field landscape scan**

**bubble collisions CMB**  
Euclidean  $SO(4) \Rightarrow$  real  $SO(3,1) \Rightarrow SO(2,1)$  collisions, oscillon broken

scan  $\ln P_s(\ln k)/A_s$ ,  $\ln A_s = \ln P_s(k_{pivot,s})$ ,  $r(k_{pivot,t})$ ; consistency  $\Rightarrow$  reconstruct  $\epsilon(\ln H a)$ ,  $V(\psi)$

$\ln P_s(\ln k)$

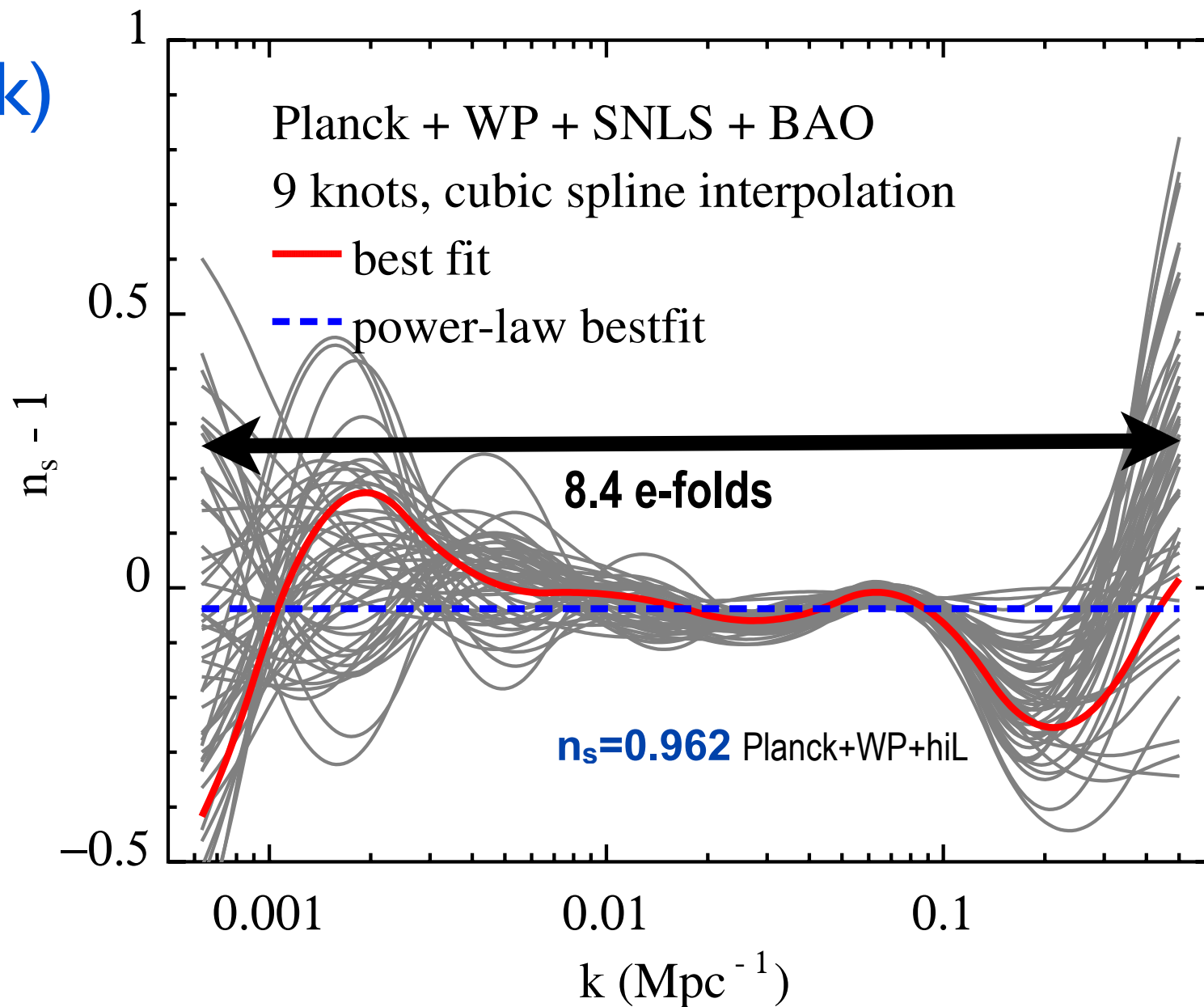


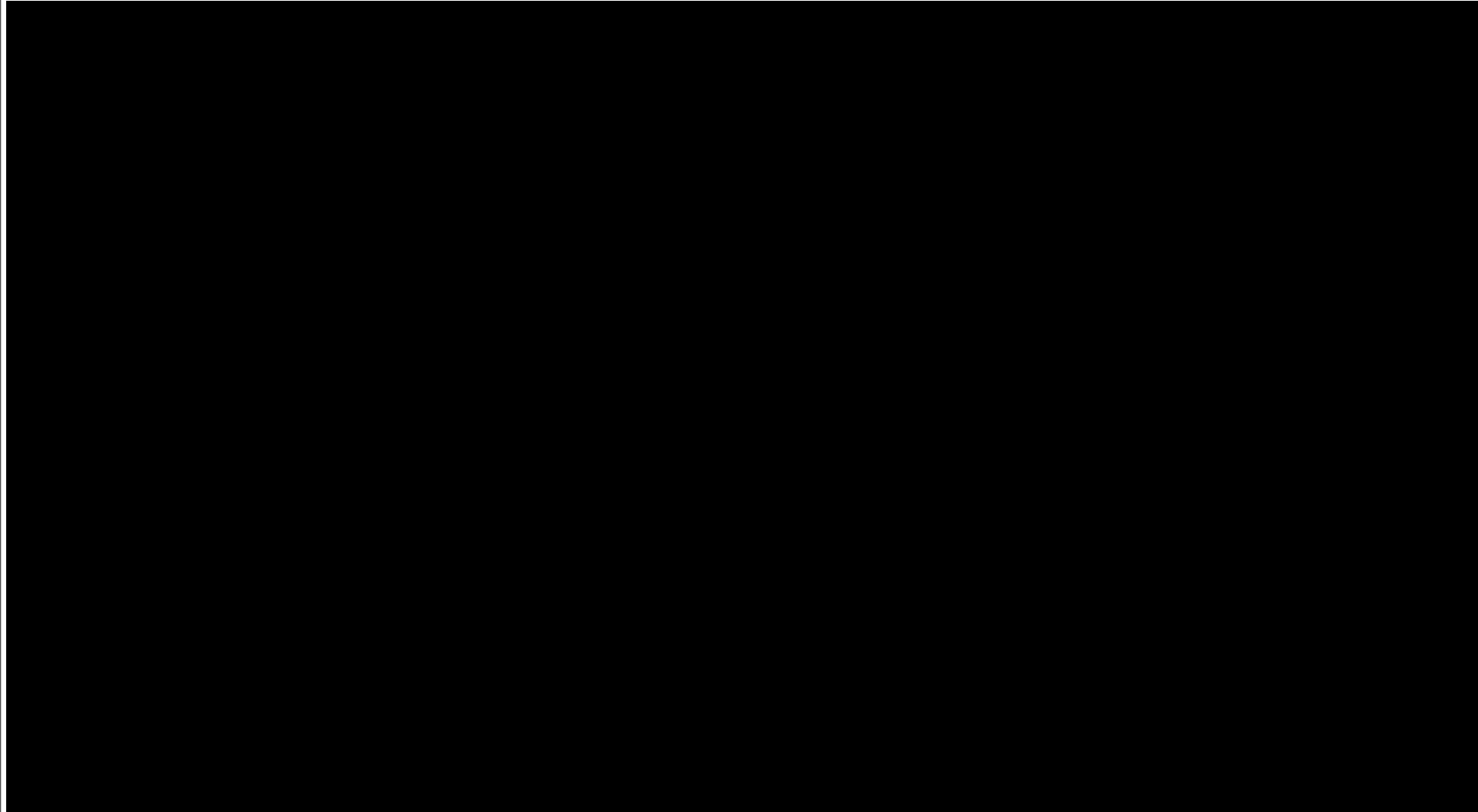
**no strong evidence for oscillation patterns, cutoffs, local features**

Inflation Histories (CMBall+LSS+SN+WL)

scan  $\ln P_s(\ln k)/A_s$ ,  $\ln A_s = \ln P_s(k_{pivot,s})$ ,  $r(k_{pivot,t})$ ; consistency  $\Rightarrow$  reconstruct  $\epsilon(\ln H a)$ ,  $V(\psi)$

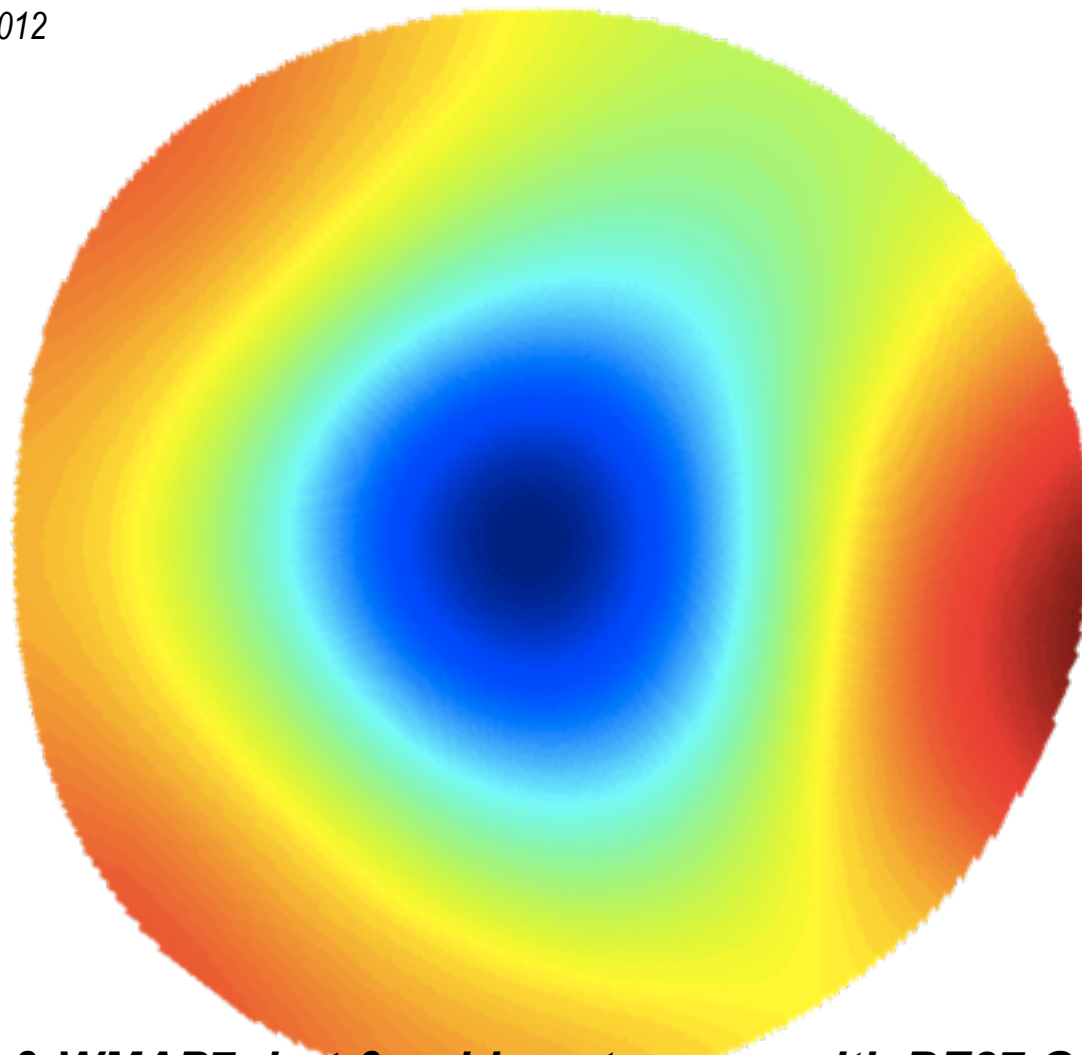
$n_s(\ln k)$





# closing in on cold spot structure (*the resolution dimension*)

Bond, Frolov, Nolta, 2012



13 deg

**PLANCK2013 & WMAP7: hot & cold spots agree with BE87 Gaussian stats  $n_{pk}(<v)$  except for one cold outlier out of Galactic plane (& others near the plane)**

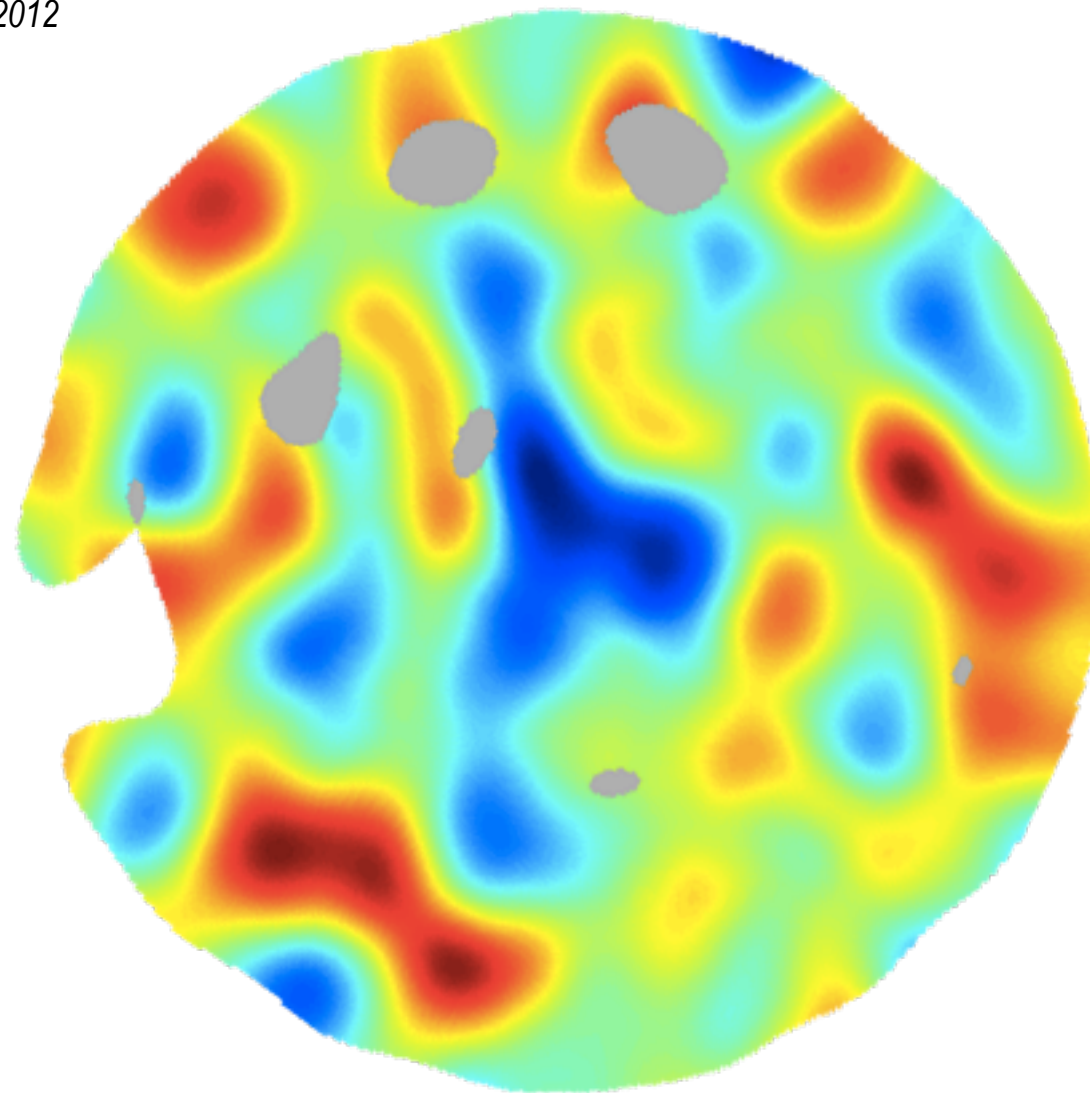
**PLANCK2013: 826', 105 peaks, coldest  $-4.97\sigma$**

**WMAP7: 800', 105 peaks, coldest  $-4.87\sigma$  significance 1:300**

**WMAP7: 360', 528 peaks, coldest  $-4.25\sigma$  significance 1:9.1**

# closing in on cold spot structure (*the resolution dimension*)

Bond, Frolov, Nolta, 2012



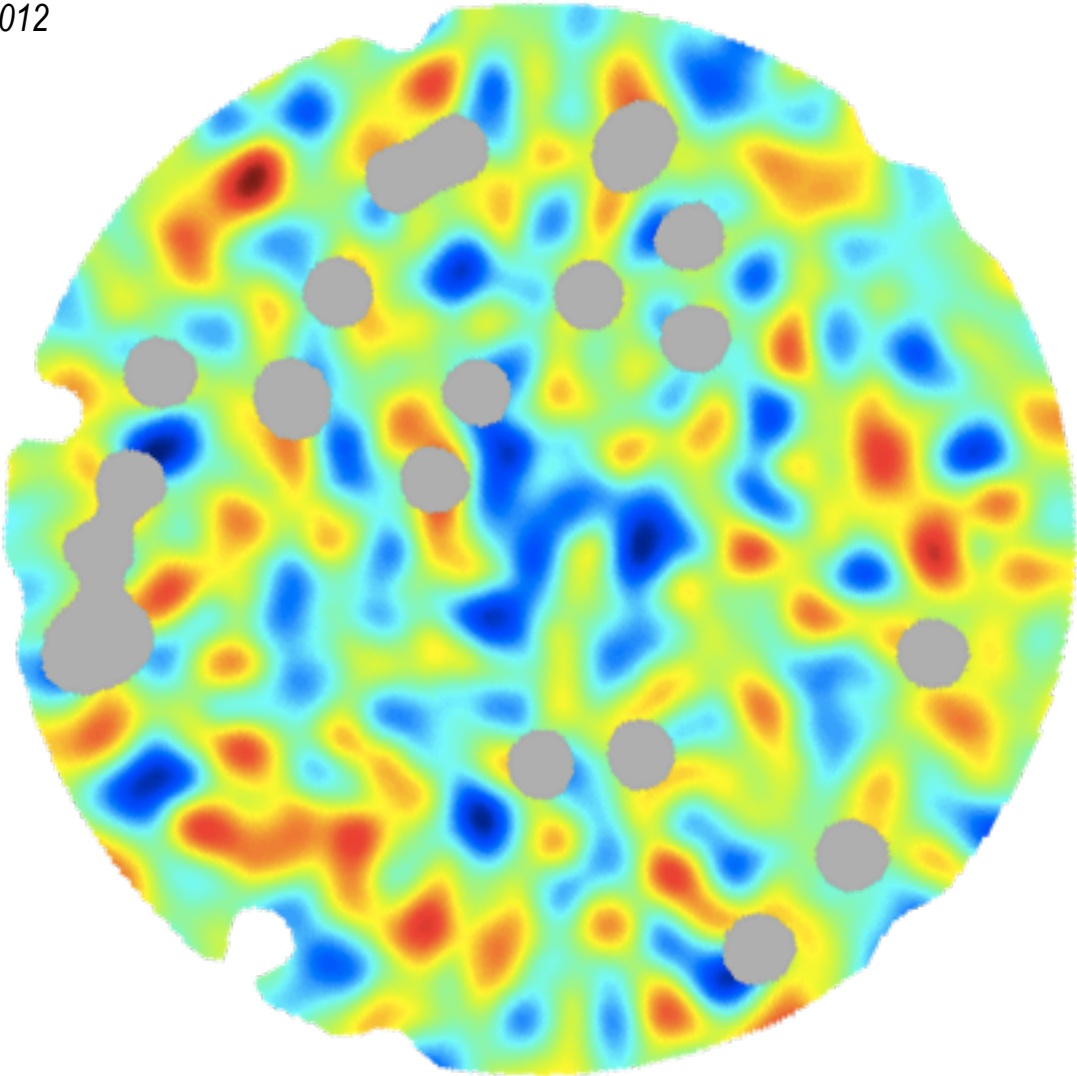
4 deg



14

# closing in on cold spot structure (*the resolution dimension*)

Bond, Frolov, Nolta, 2012

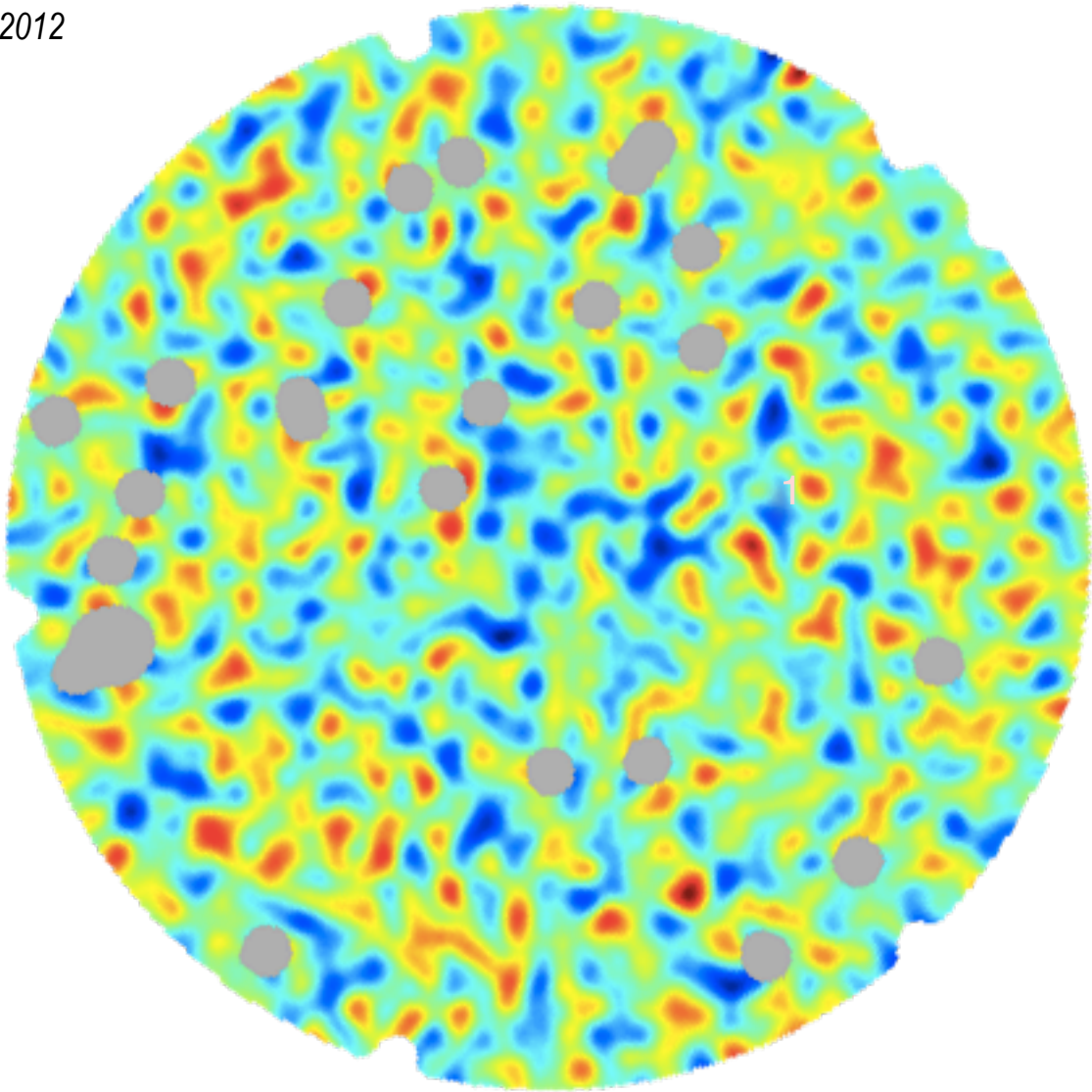


2 deg



# closing in on cold spot structure (*the resolution dimension*)

Bond, Frolov, Nolta, 2012

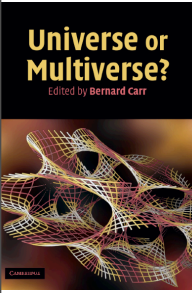


1 deg

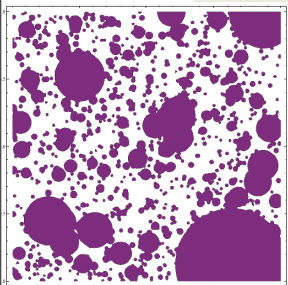




Horizons: the ultimate-speed constraint on light & information



higher dimensions  
6?

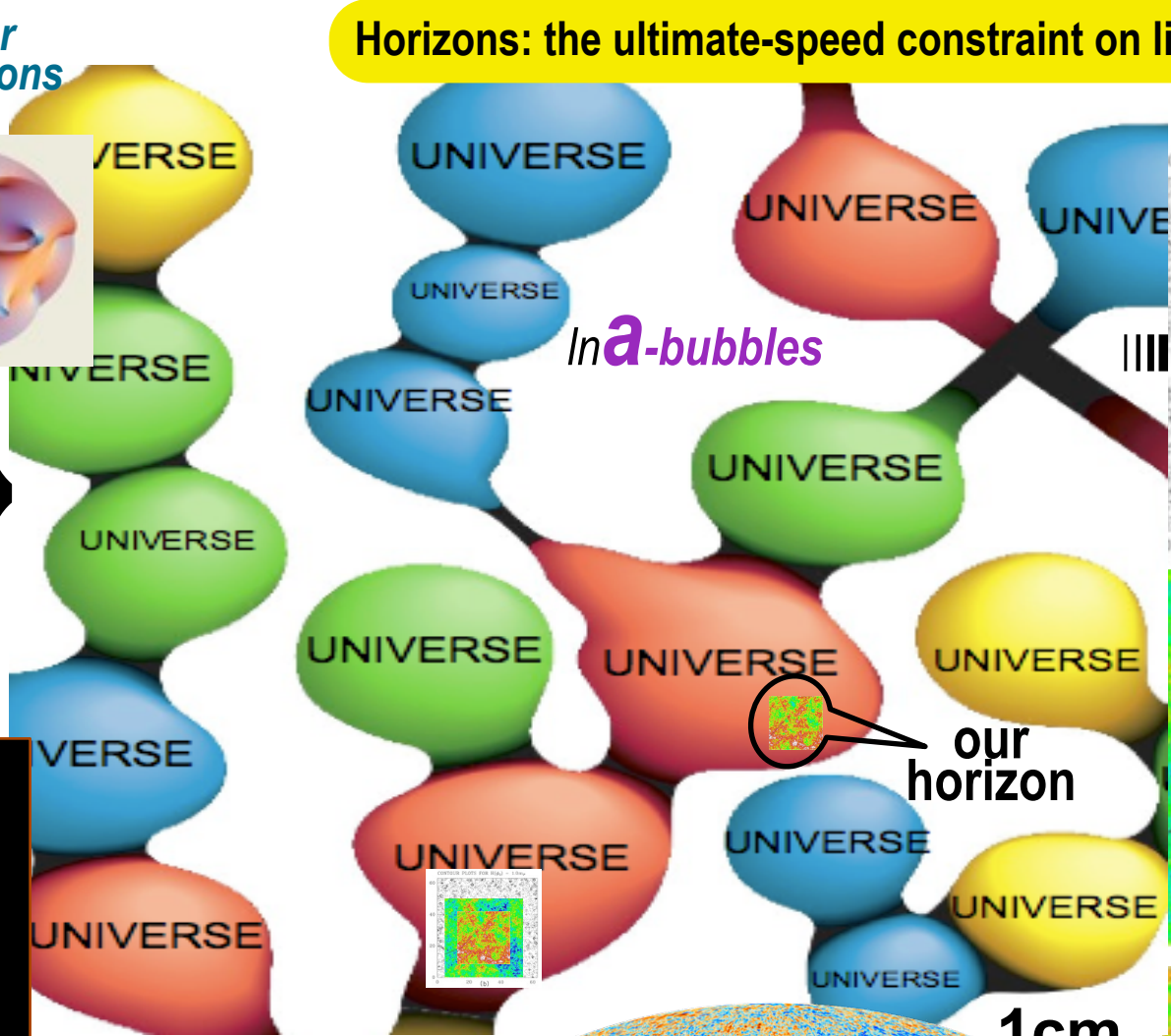


quantum tunnels  
= bubbly-U

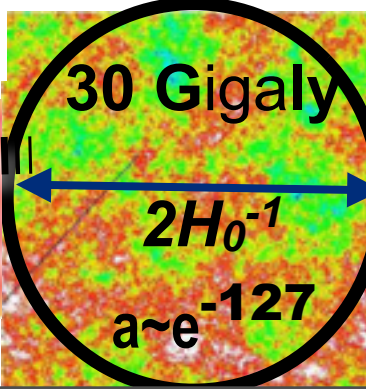
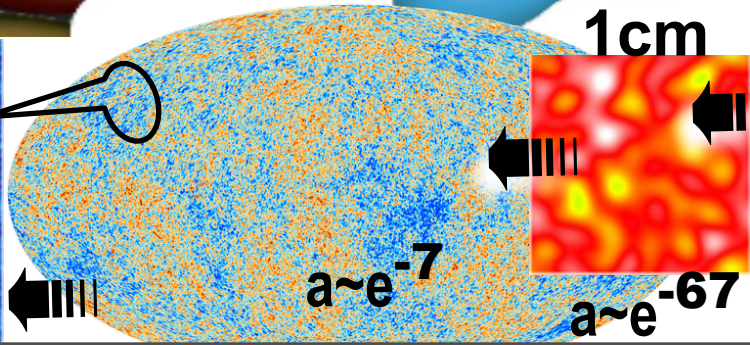
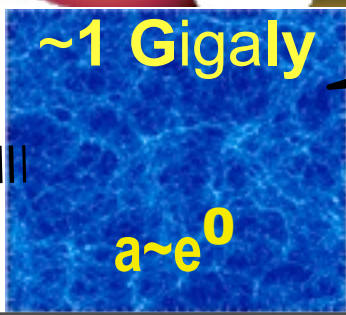
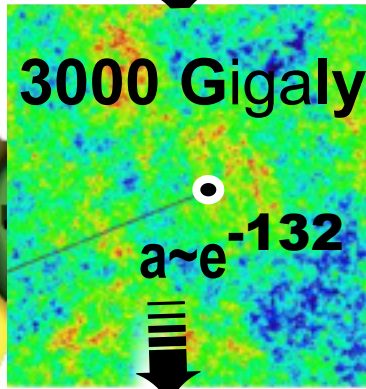
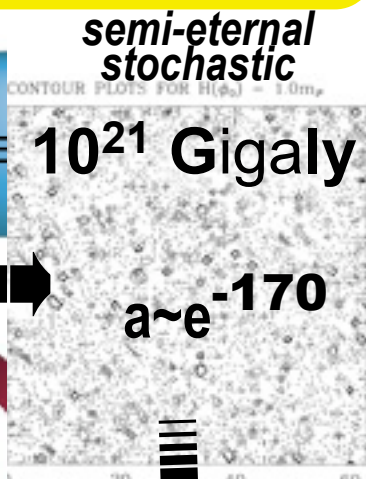
O dark dark dark. They all go into the dark, The vacant interstellar spaces, the vacant into the vacant ... So the darkness shall be the light



a future DE-Void



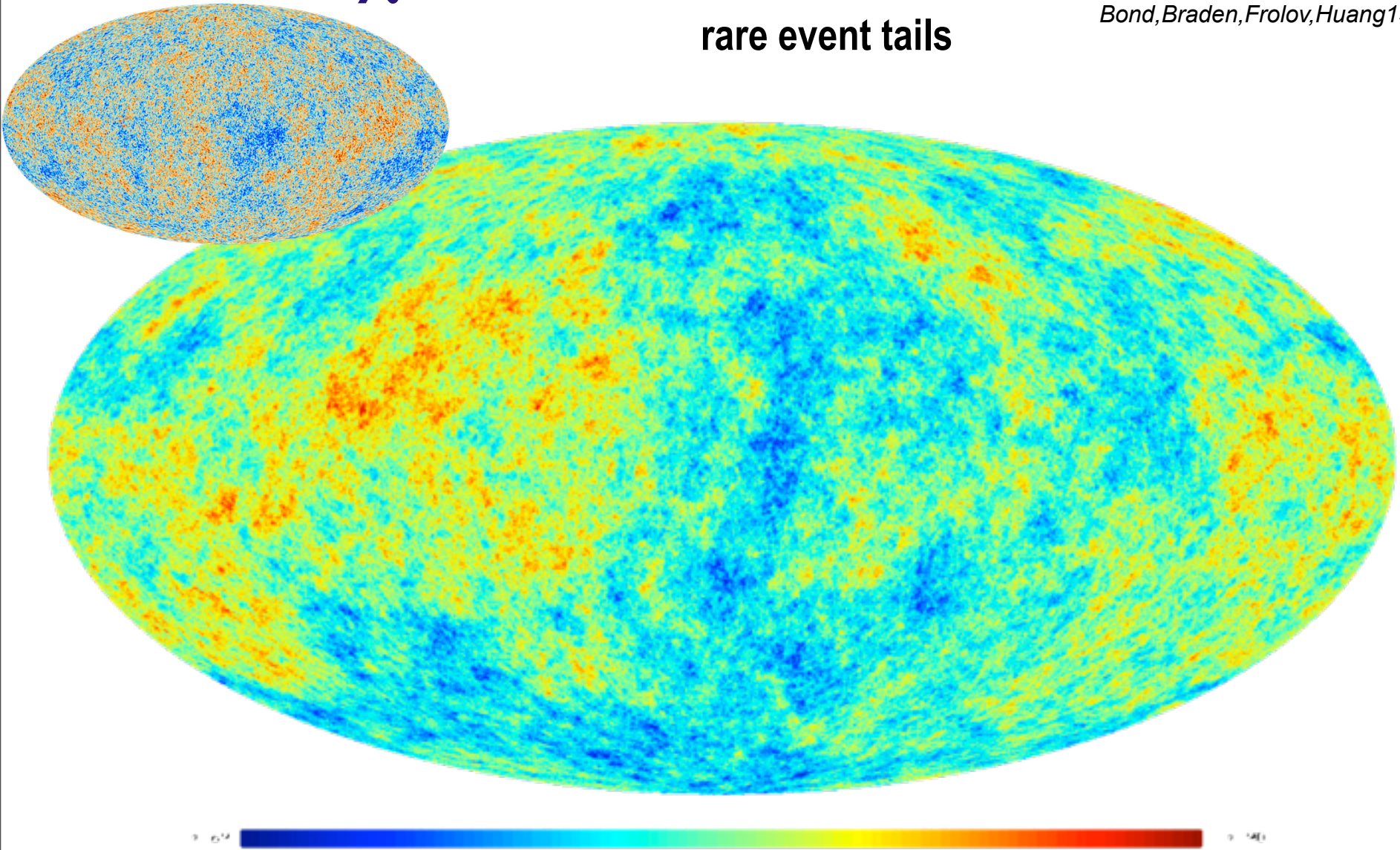
In *a*-bubbles



simulated sky with Gaussian inflaton-induced + **uncorrelated subdominant non-Gaussian isocon-modulated preheating**. Landscape-accessing super-horizon

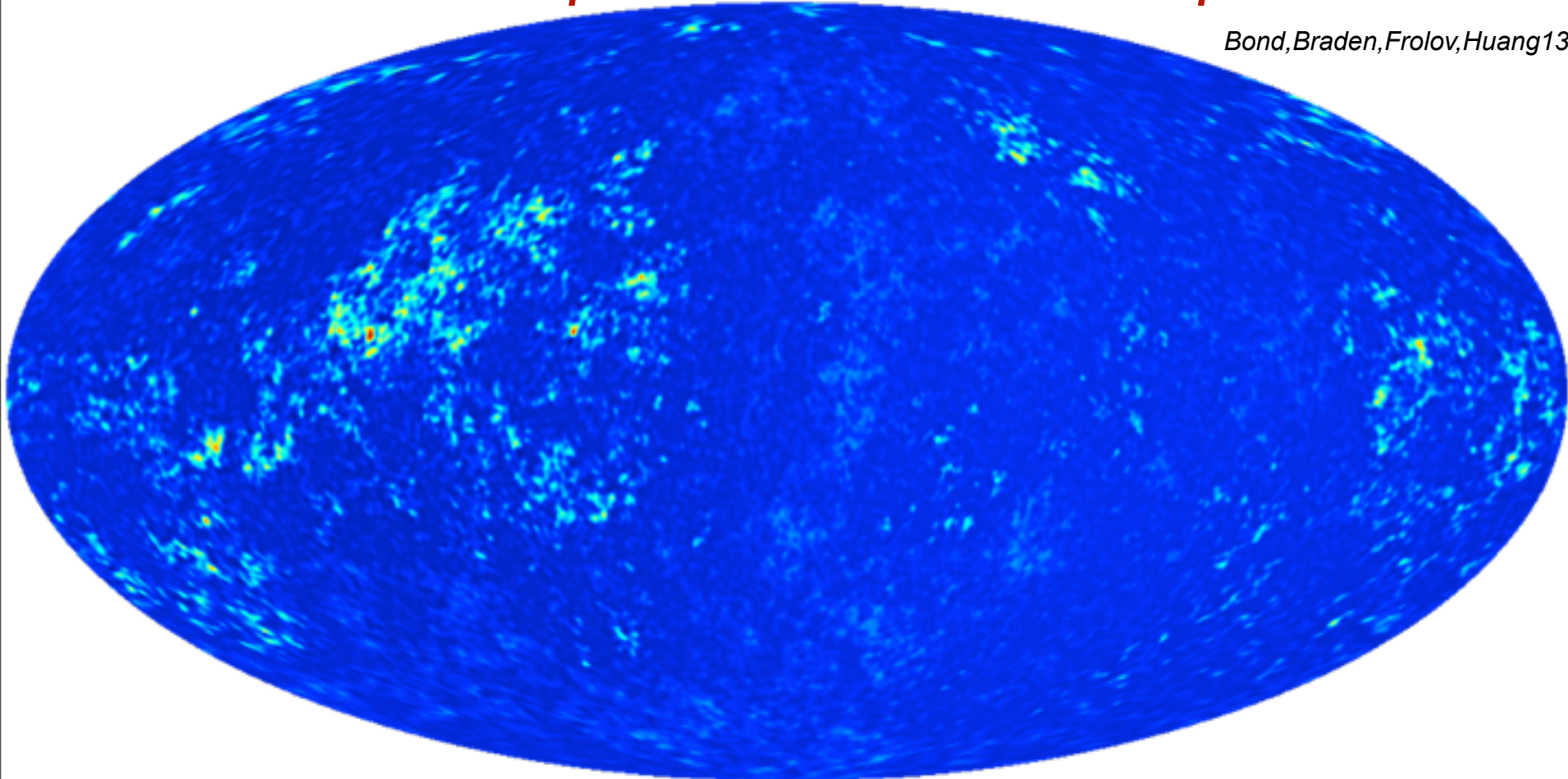
control variable =  $\chi > \mathbf{h} \Rightarrow$  ***super-bias, intermittent, extended source-like***  
**rare event tails**

*Bond, Braden, Frolov, Huang13*



bispectrum & 3-point  $\sim$  fsky,patches<sup>3</sup>  $\Rightarrow$  not overly constraining & standard  $f_{\text{NL}}$  method is *not how to pattern-search for intermittent power bursts*

Bond, Braden, Frolov, Huang 13

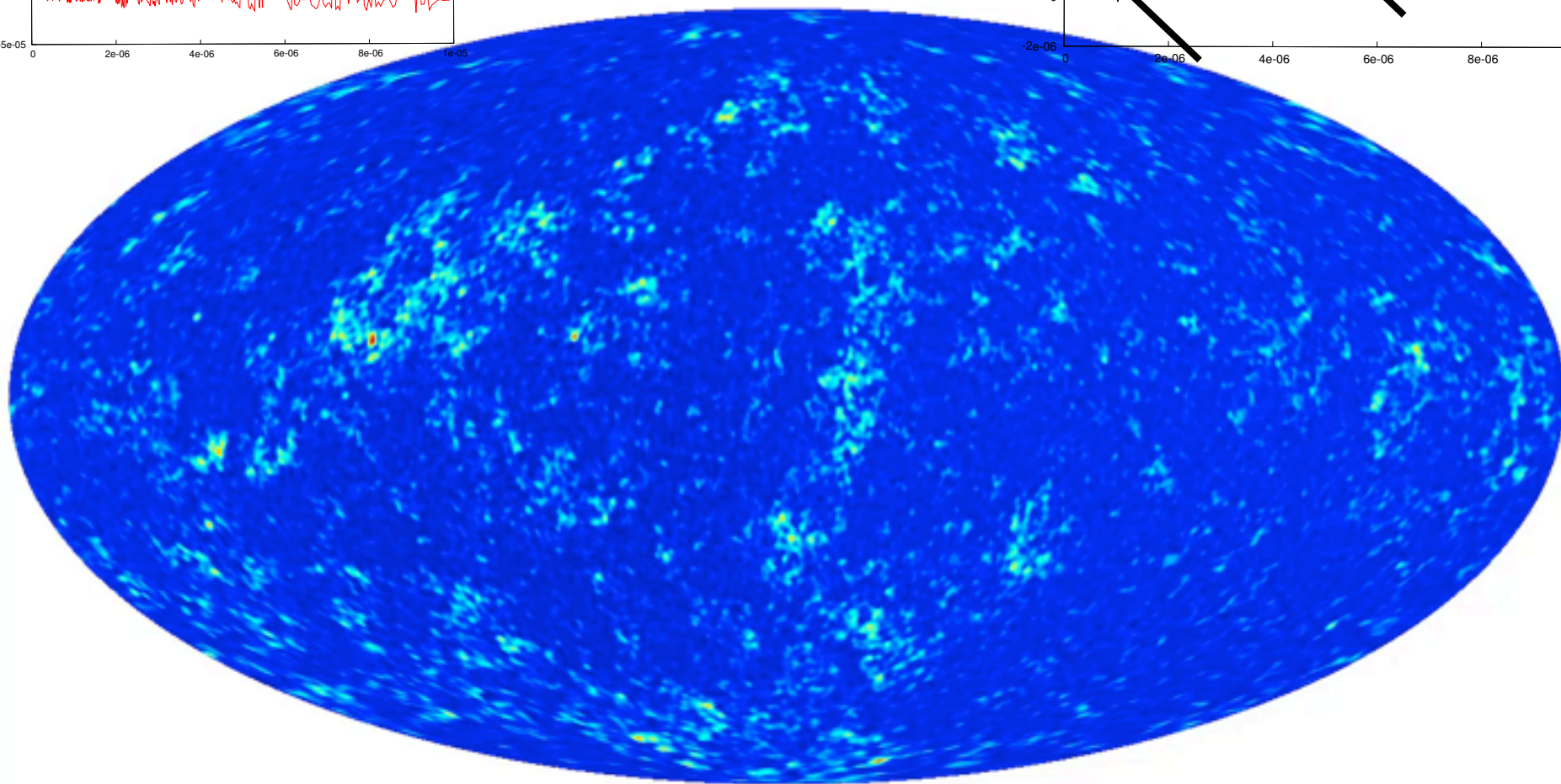
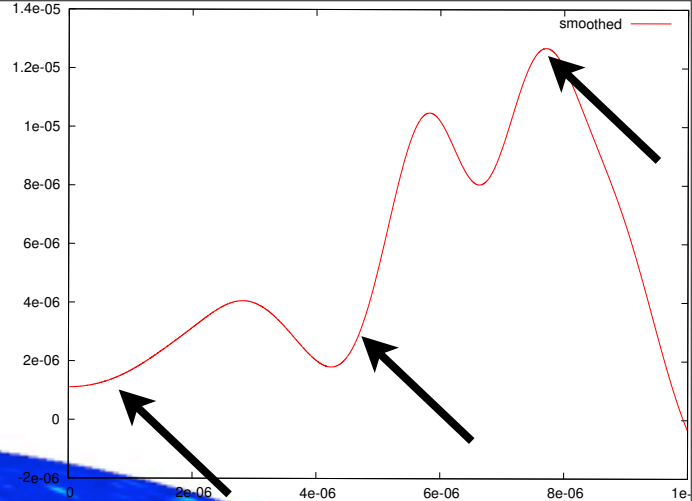
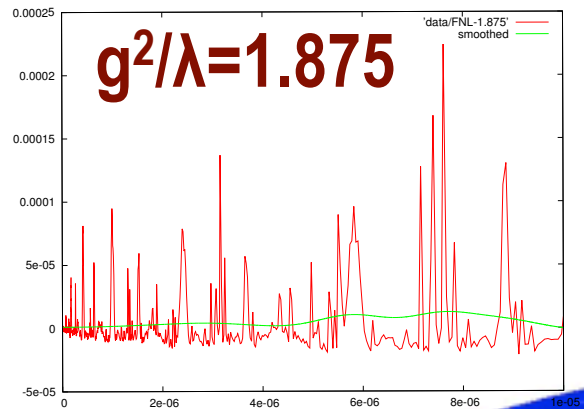


for some  $\chi_{>h}$  there is a perturbative regime:

$$f_{\text{NL}}^{\text{equiv}} = \beta \chi^2 f_\chi [P_\chi / P_\phi]^2(k_{\text{pivot}}) \Rightarrow \text{constrain } f_\chi^3 \chi_{>h}^2$$

# subdominant structure change as we scan $\chi > h$

Bond, Braden, Frolov, Huang13



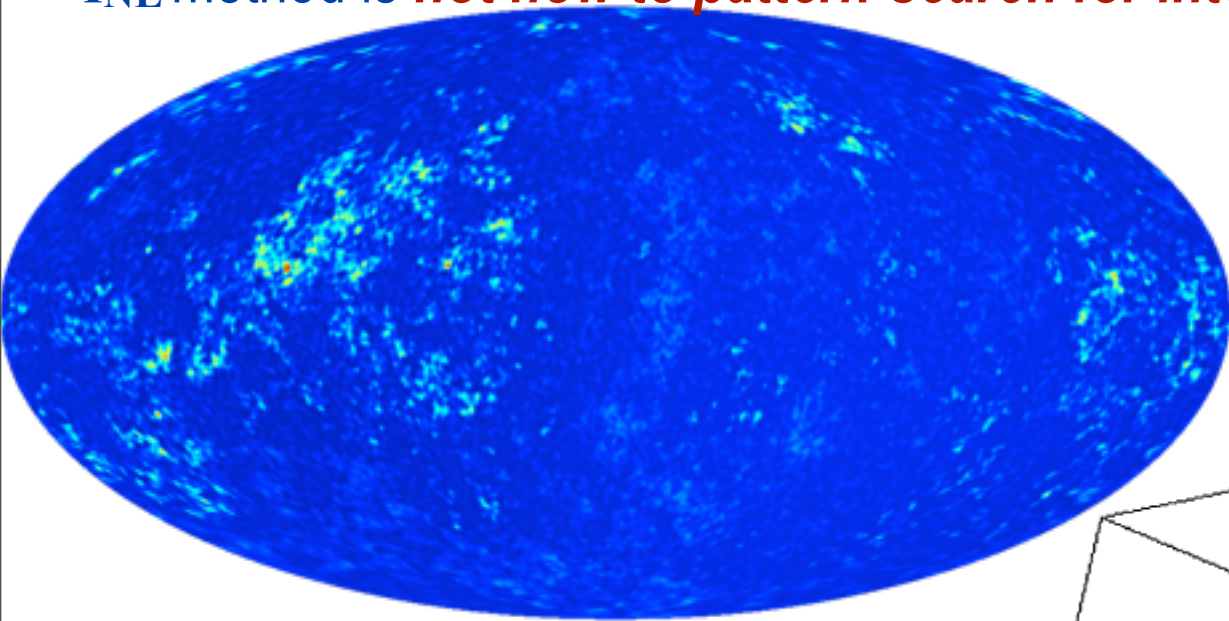
-1.203E-05



+7.520E-05

bispectrum & 3-point  $\sim$  fsky,patches<sup>3</sup>  $\Rightarrow$  not overly constraining & standard  $f_{NL}$  method is *not how to pattern-search for intermittent power bursts*

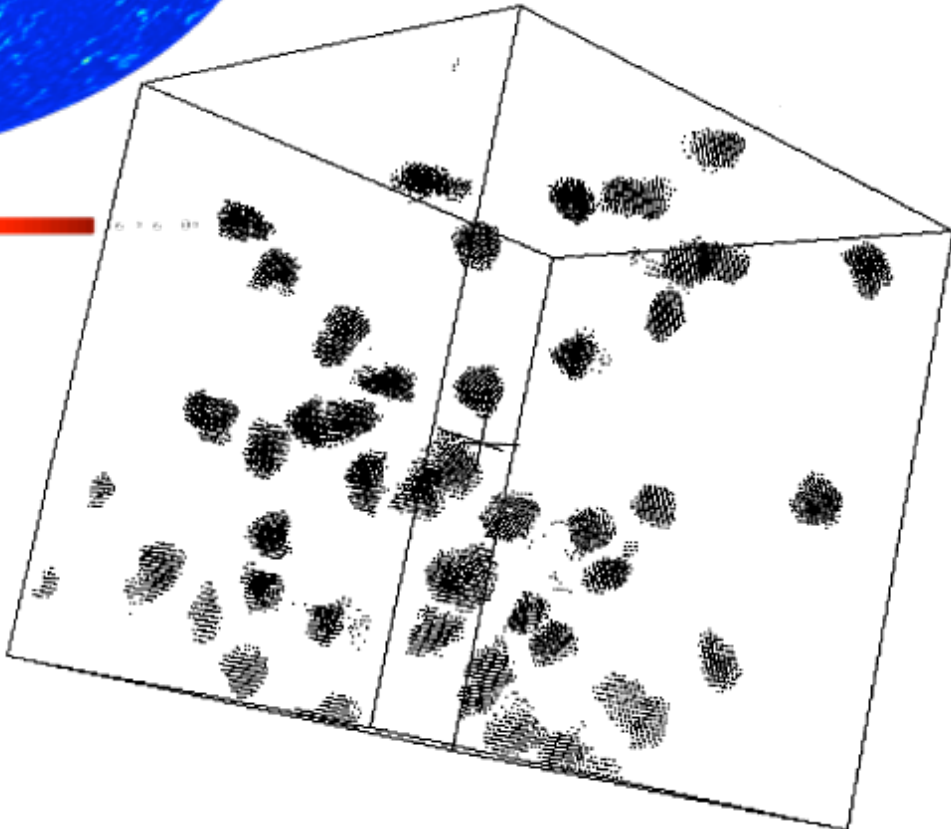
Bond, Braden, Frolov, Huang 13



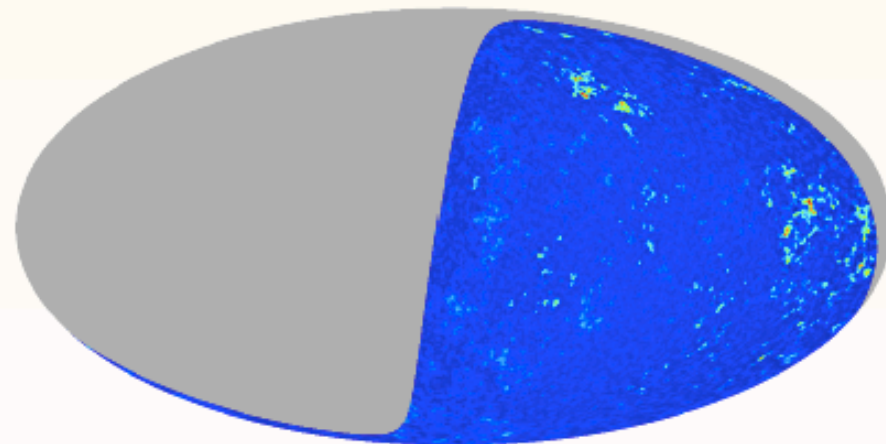
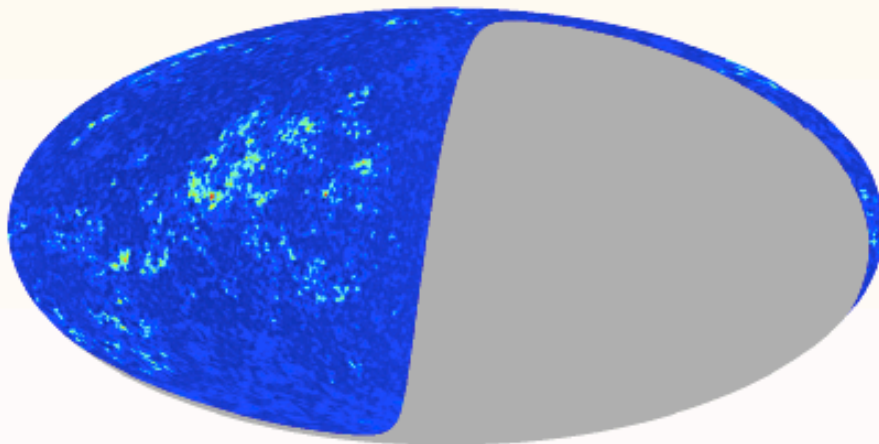
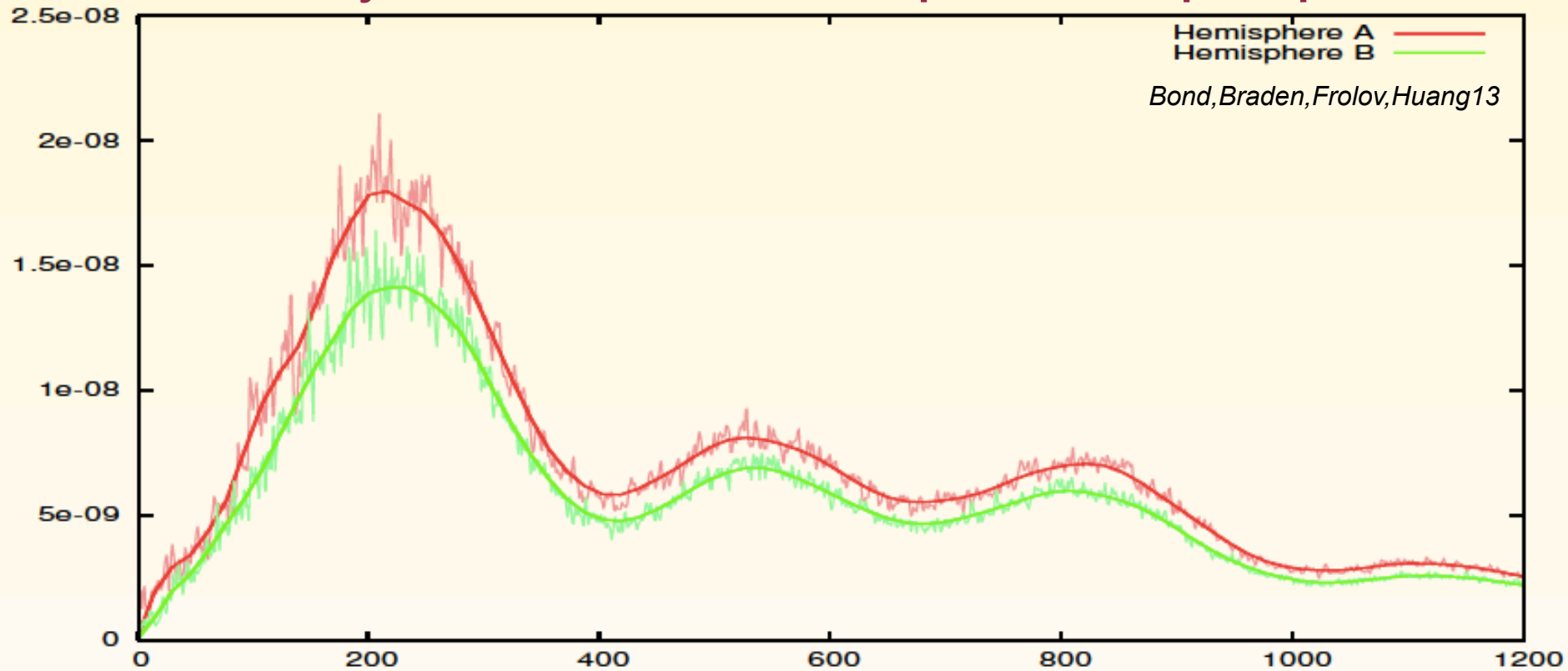
**intermittency** from steep threshold functions acting on a slightly red curvature field (gravitational potential) lead to very-large-scale splotch “anomalies”



cf. the more localized Lagrangian space **intermittency** from steep cluster-threshold functions acting on the **density field**. **Cluster-patches** lead to pressure intermittency and SZ sources in the CMB



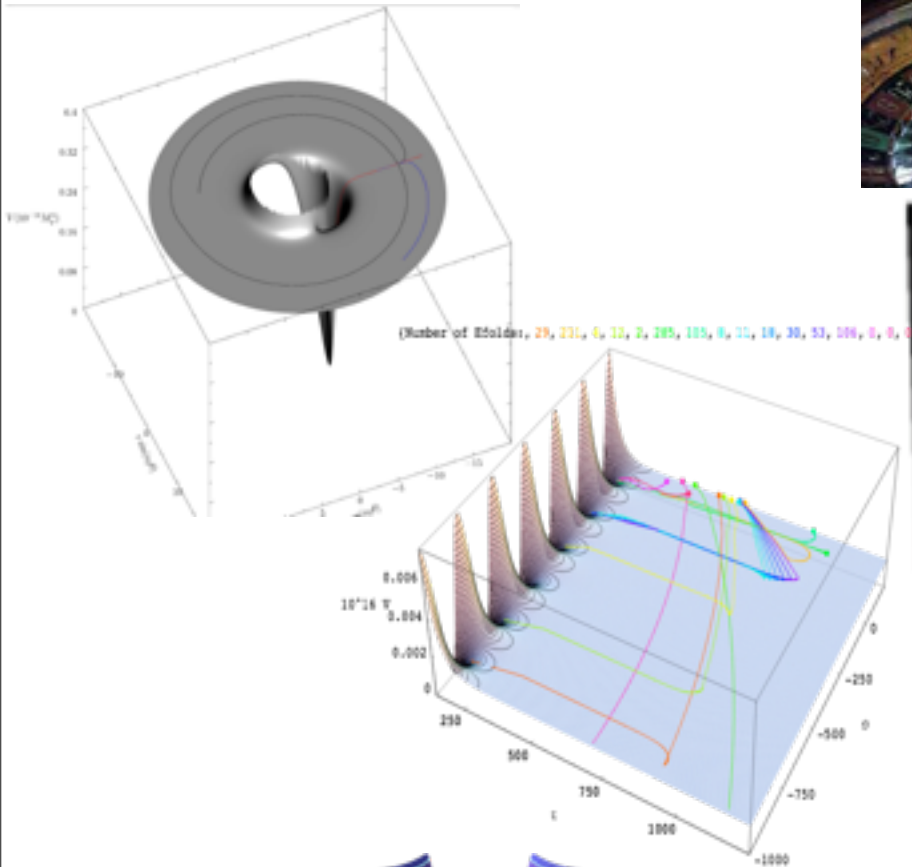
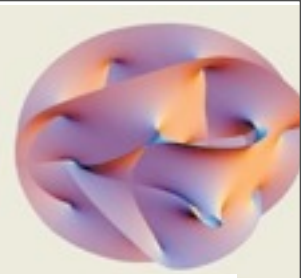
associated hemispherical power asymmetry extends to high  $L$ , though diminished. the symmetric inflaton-induced power swamp the power bursts



0.00000000 1.00000000 2.00000000 3.00000000 4.00000000

0.00000000 1.00000000 2.00000000 3.00000000 4.00000000

# non-Gaussianity



Preheating After  
Roulette Inflation

$$\langle \tau \rangle =$$

quantum  
diffusion  
spatial jitter

drift

$$\ln a(\mathbf{x}, \ln H)$$

entropy  
generation in  
preheating  
from the  
coherent  
inflaton  
(origin of all  
matter)

isocon directions,  
e.g., axion

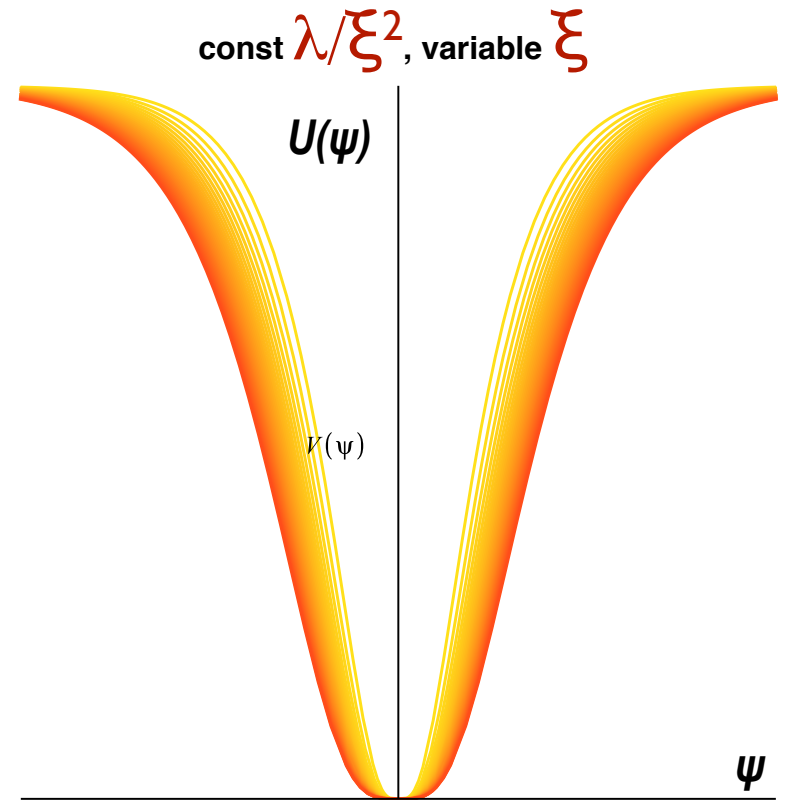
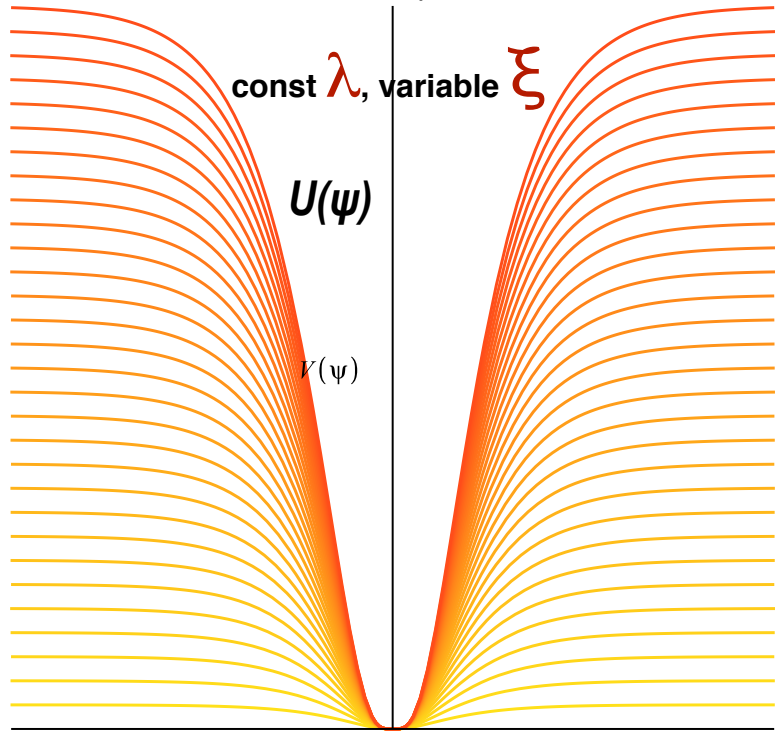
let there be  
heat

flattened  $V$  to satisfy P13

SEMI-INTERNAL INFLATION

$$V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$$

in Einstein frame for new (canonically normalized) field  $\psi$



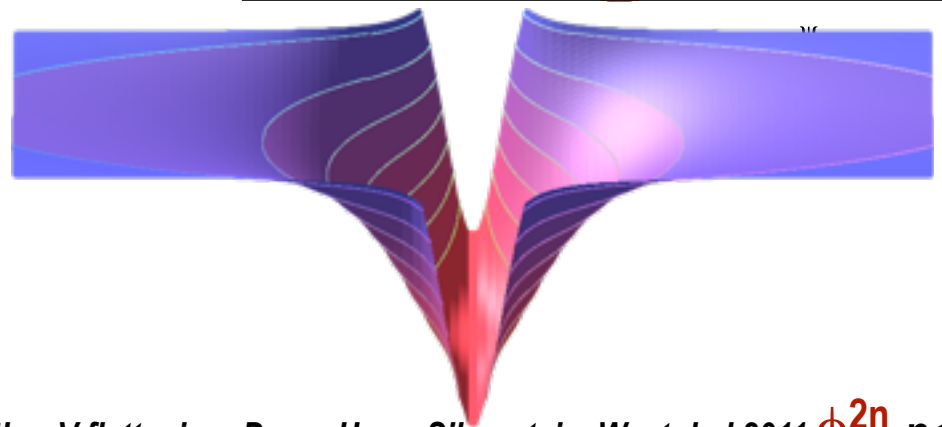
$$\psi \chi = \int [K^{11}(\phi)]^{1/2} d\phi,$$

$$K^{11} = \frac{\frac{m^2}{m_p^2} + 8\pi|\xi|(1+6|\xi|)\frac{\phi^2}{m_p^2}}{\left[\frac{m^2}{m_p^2} + 8\pi|\xi|\frac{\phi^2}{m_p^2}\right]^2}$$

$$U(\chi) = \left[\frac{m^2}{m_p^2} + 8\pi|\xi|\frac{\phi^2(\chi)}{m_p^2}\right]^{-2} V(\phi(\chi)).$$

conformal V-flattening of SBB89,

cf. Kallosh/Linde KITP 06/19  $\xi = 1/6 - \Delta$ ,  $\Delta$  small



other V-flattening: Dong, Horn, Silverstein, Westphal 2011  $\phi^{2n}$ ,  $n < 1 \Rightarrow$

$$r = 8n/(N_I + n/3) \quad 1 - n_s = (n+1)/(N_I - n/6)$$

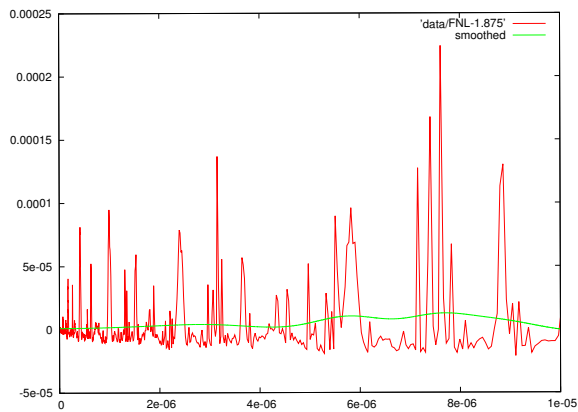
e.g., monodromy SW08  $p=1/3$ , MSW08  $p=1/2$  & cos = shift symmetry

V-flat natural in roulette inflation (Kahler moduli) BKKV



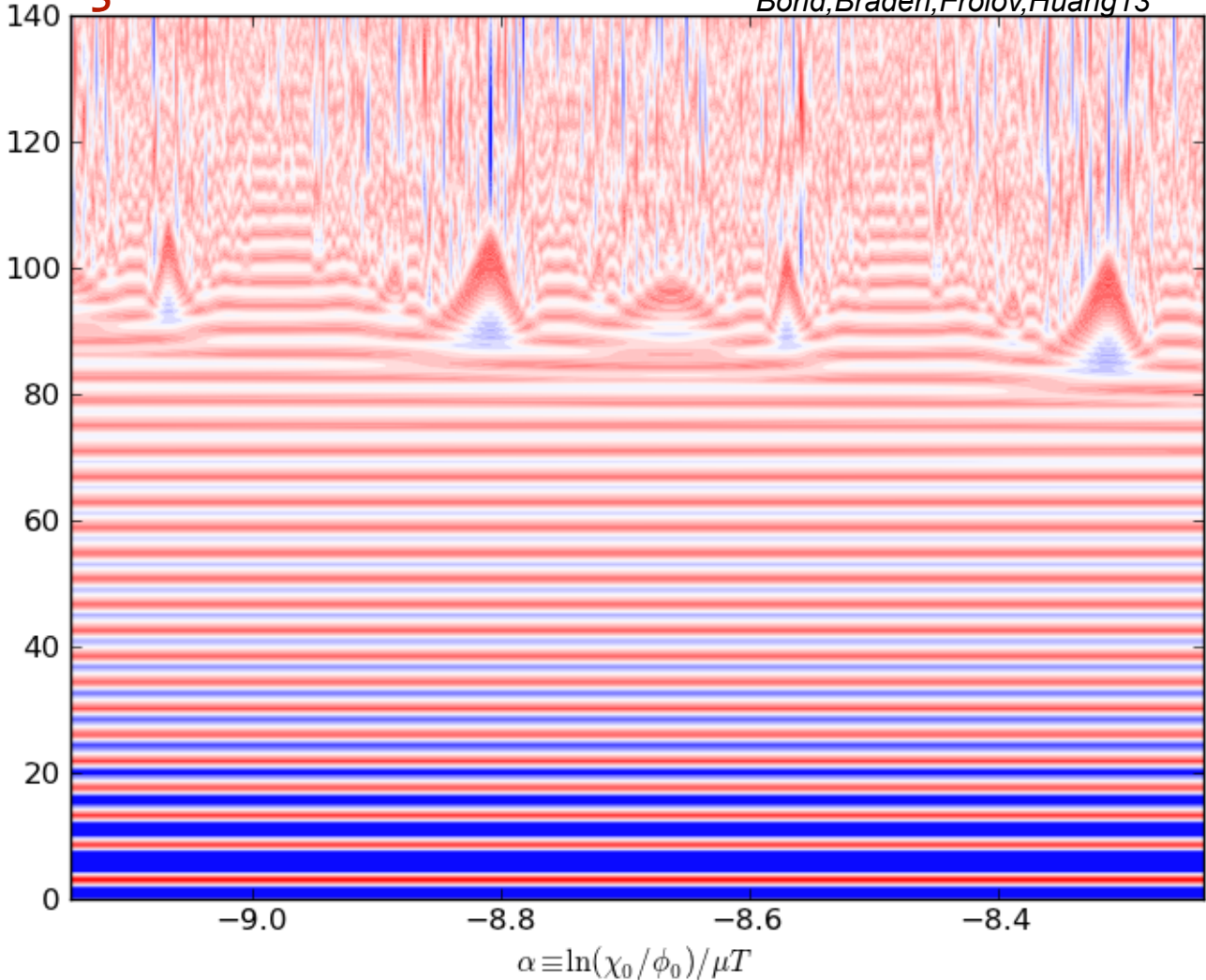
quartic inflaton variable Planck mass  $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$

**spikes persist with flattened effective potentials**  
*only the potential bowl at the bottom matters*



$\xi = -1$

Bond, Braden, Frolov, Huang13



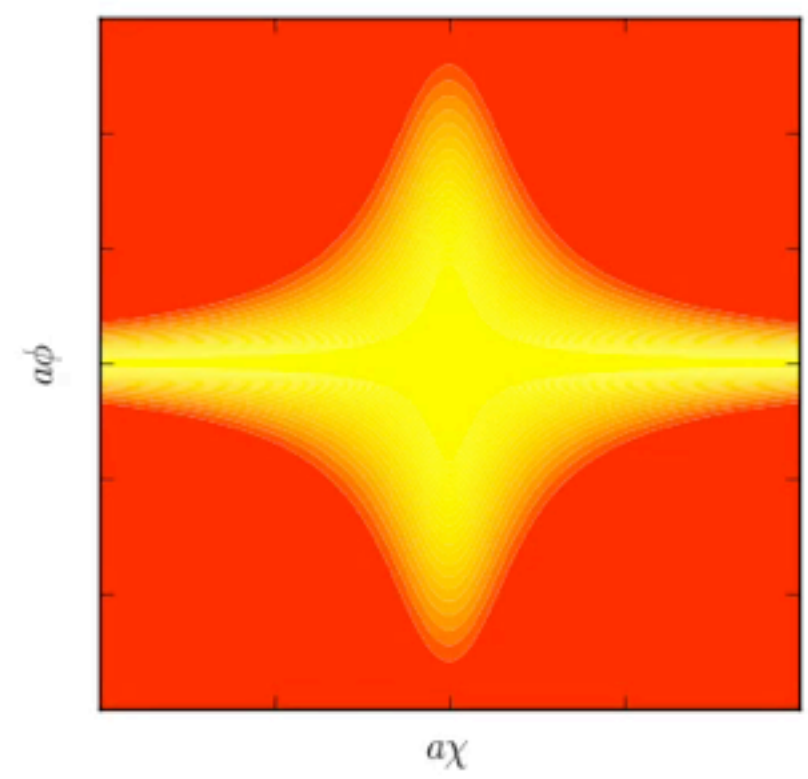
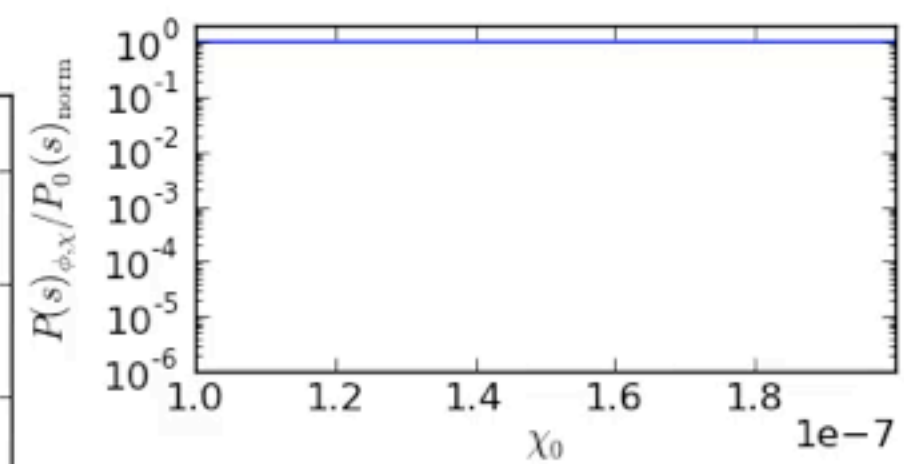
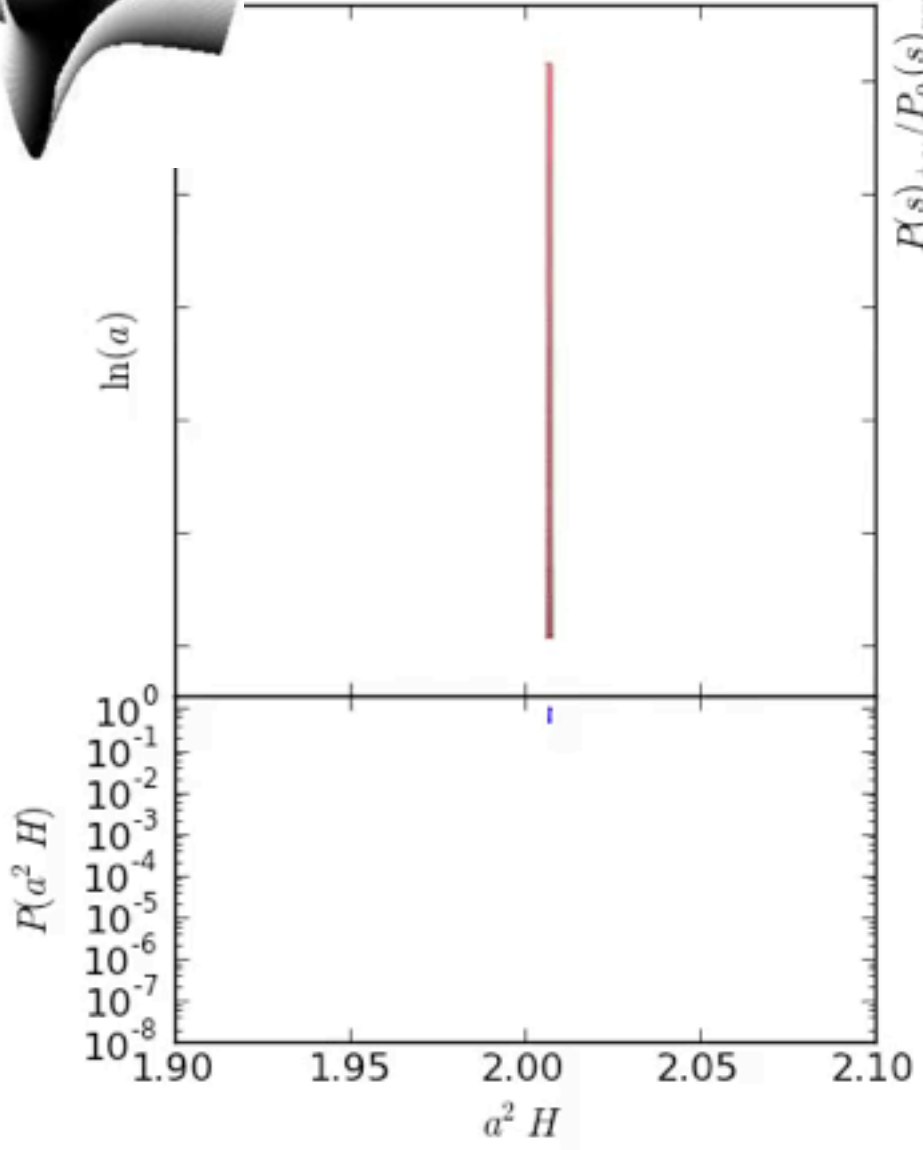
calculating ballistic evolution to caustics gives the spikes in perfect agreement with full nonlinear lattice simulations

(now being done for a suite of flattened potentials to better deal with the shock-in-time)

**nonG from post-inflation but pre-entropy generation ballistic trajectories can lead to pre-shock-in-time caustics and other phase space convergences in the deformations (!) Zeldovich map-ish**

$$\text{eg } \partial \ln a / \partial \chi_i(x), \partial \ln a / \partial g(x) \Rightarrow P[\ln a(x), t_{\text{shock}} \mid \chi_i(x), g(x), t_{\text{end-of-inflation}}]$$

initial conditions spanning (roughly) a single period (ie.  $\mu_0 T$  with  $\mu_0$  the Floquet exponent of  $\chi_0$ )

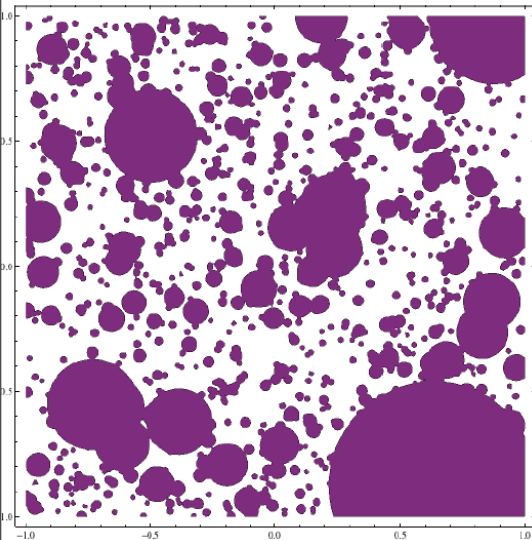


**distribution functions & trajectory caustics**

Bubblly U

Kleban11  
review

+ KITP13  
review



the **bubblly gospel**, a la Kleban11 + many

we live in a bubble, one among many, the nature of the universe **BUT stochastic semi-eternal inflation**

Coleman de Luccia instanton with  $SO(4)$  Euclidean symmetry =>  $SO(3,1)$  real symmetry is gospel **BUT thick wall bubbles may be endemic in the landscape, depends upon  $V$ . bubble formation fluctuations about instanton. multiple field instantons, always one dof Euclidean-stochastic path?**

negative curvature, initially  $\sim$  initial bubble radius, diminished by subsequent inflation. if  $\text{prob}(N \text{ efolds}) \sim 1/N^p$   $p \gg 1$  then  $N$  just enough => negative curvature likely observable **BUT it is not observed, our patch inflated alot if stochastic semi-eternal inflation**

all bubbles eventually collide **BUT with what probability: to see one seems quite unlikely**

look for  $SO(2,1)$  symmetric collision debris on the CMB sky (“cosmic wakes”) as circular spots, scale TBD **BUT improbable. But if probable, why subdominant and not booming. BUT 3D instabilities from inevitable quantum fluctuations make complex interiors, oscillons etc. CMB smoothing fuzzes over this always? searches to prove landscape exists too naive?.**

bubble collisions make largescale modulations possible **BUT too large?**

**here & in BBM13a,b,c we treat bubble creation and propagation as interesting nonlinear field theory problems in their own right, that may have a cosmological setting, still TBD. non-inflation domain walls and bubbles. now imbedding subdominant isocon-tunnels into an overall inflationary flow**

when domain walls (big bubbles) collide in full 3D lattice sims

with tiny zero point & wall fluctuations

=> burst of scalar radiation at  $c$  (with outgoing radiation BCs)

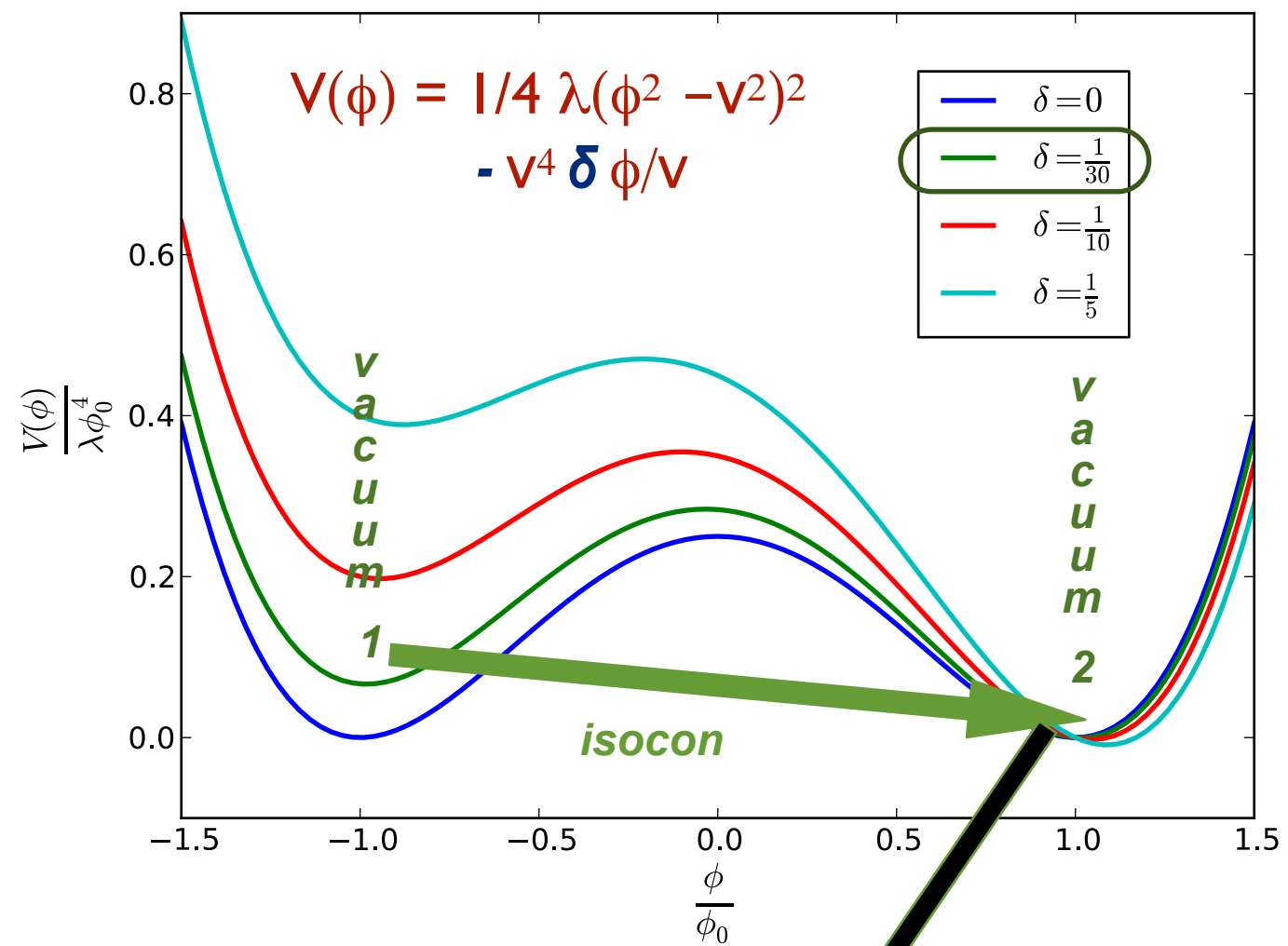
+ long-lived oscillons, size related to the mass

cf. 1D work that dominates the subject

Gleiser, Kleban+, Johnson, Peiris, Lehner, ..

an oscillon phenomenon is possible in preheating *Easther+*

CMB+ observables?

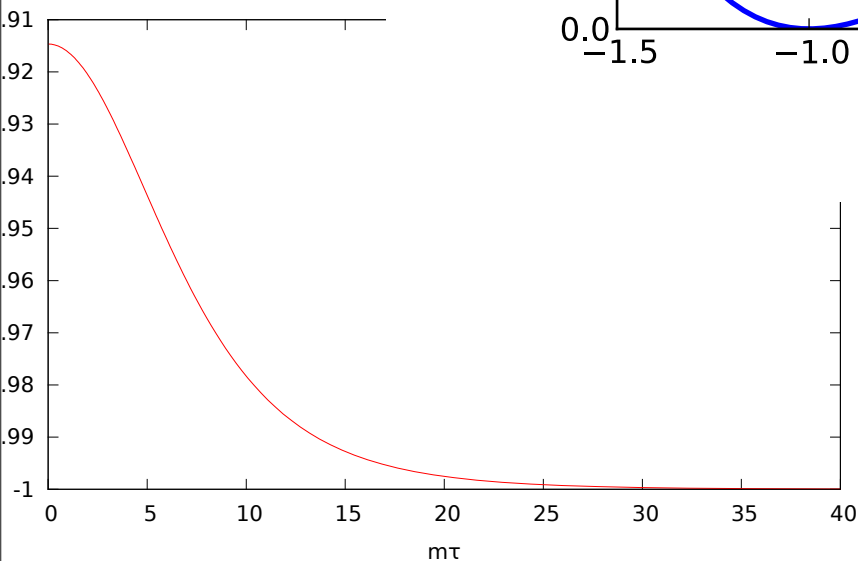
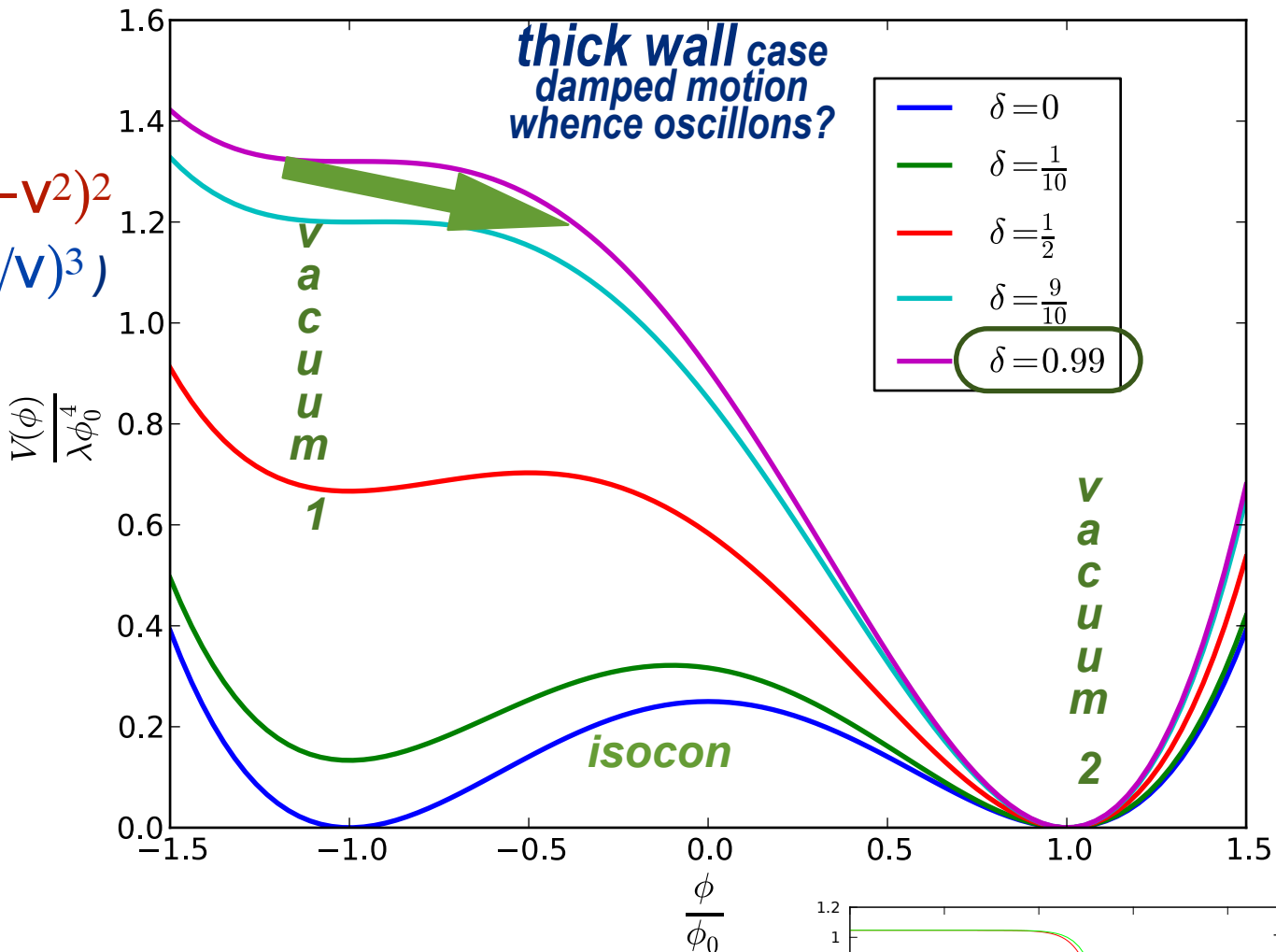


- $\delta = 0$
- $\delta = \frac{1}{30}$
- $\delta = \frac{1}{10}$
- $\delta = \frac{1}{5}$

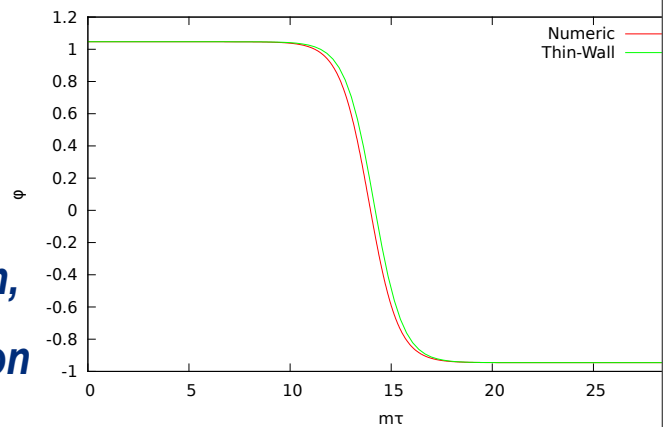
$$V(\phi) = 1/4 \lambda(\phi^2 - v^2)^2 - v^4 \delta (\phi/v - 2(\phi/v)^3)$$

large  $\delta$   
thick wall  
instanton

how important are  
fluctuations in the  
Euclidean trajectory  
from the (classical)  
instanton



small  $\delta$   
thin wall  
instanton  
OK approximation,  
but accurate  
numerical instanton  
is needed for  
instability work



Bond, Braden, Mersini 2013

**oscillon** in early universe, e.g., Amin++++, Gleiser, BBM13a,b,c

oscillatory, spatially local, long-lived, most work 1D, a few 3D sims for preheat + our bubbly sims

history: Bogolubsky+Makhankov76, Gleiser94, Copeland+95, ..., Amin+Shiokoff 10, Amin 13 - single 1D

oscillon blob

relation to Qballs?

small amp conditions

$(m^2 - \omega^2) \varphi + (-\nabla^2 \Phi) + (\partial V / \partial \varphi - m^2 \varphi) \sim 0$  freq ( $>0$ ) curvature ( $>0$ ) nonlinear (must be  $<0$ )

**BUT** no theorems (so far) for when oscillons arise.  $V$  shallow at large  $\phi$  **BUT not for bubbles**

Floquet analysis of  $\mu_k \gg H$ , exponential instability **BUT modified for bubbles and domain walls BBM1**

want  $\text{Re } \mu_k / H > 10$ ,  $M_P / m \gg 1$ , potential  $n < 1$  far out **BUT  $n$  varies**

shallow flattened  $V$  for preheating oscillons **BUT not for nearly symmetric bubble potentials**

energy fraction in oscillons  $> 80\%$ . Farhi et al 08 Amin+  $\gg 50\%$  **BUT not in our sims  $\sim 10\%$ , 90% scalar radiation**

preheat with pspectre pseudo spectral code Easter, Finkel, Roth 256<sup>3</sup> defrost (Frolov) LatticeEasy (Felder +Tkachev) **BUT defrost++ with symplectic integration + radiation boundary conditions + new (much) faster spectral code**

oscillons overdense by a few **BUT we see higher, though gravitational collapse not important**

Primordial Black Holes are hard to form **YES**

expansion history change **YES**

delayed preheating (store in oscillons) **YES**

number density modulation (using our nonG from preHeating ideas B+09) **YES, maybe**

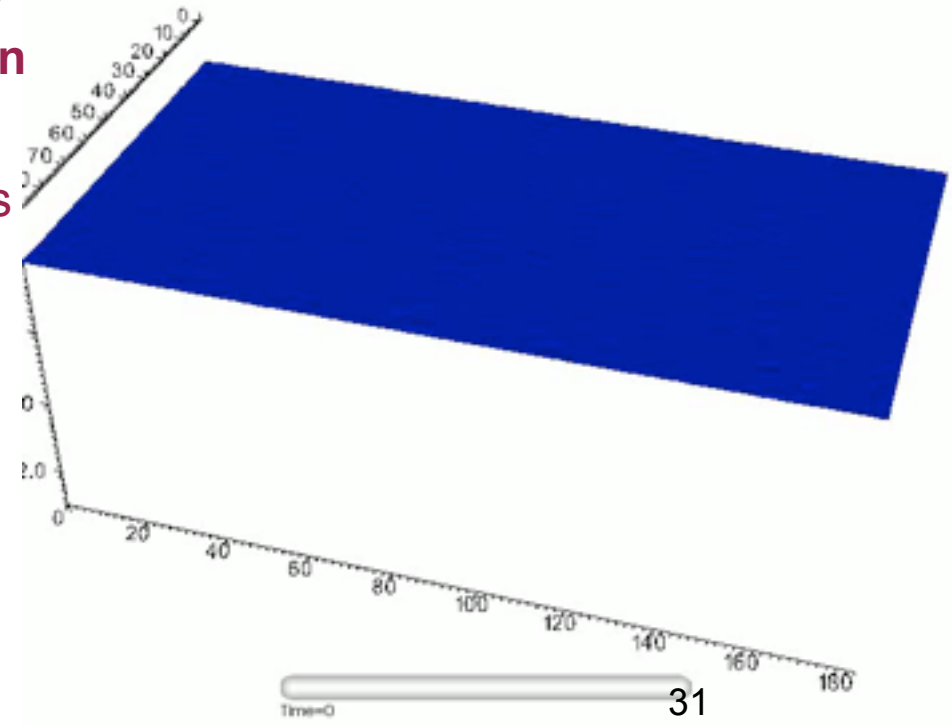
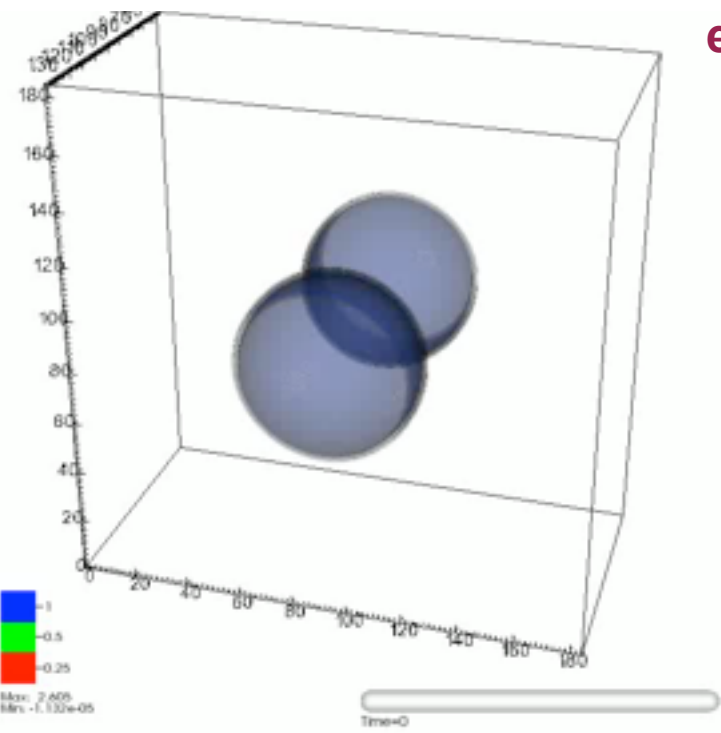
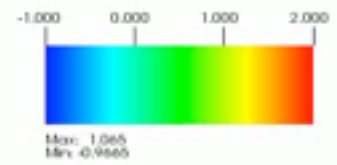
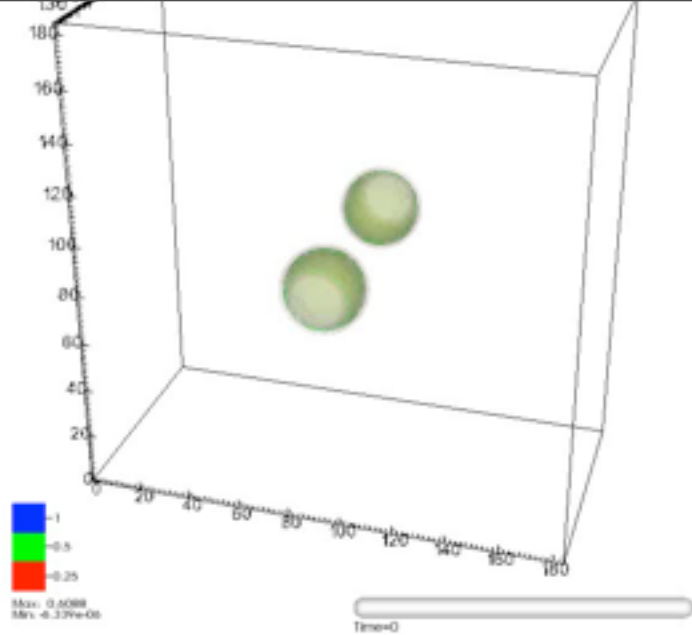
**when domain walls (big bubbles) collide in full 3D lattice sims**  
**with tiny zero point & wall fluctuations**  
**=> burst of scalar radiation at  $c$  (with outgoing radiation BCs)**  
**+ long-lived oscillons, size related to the mass**

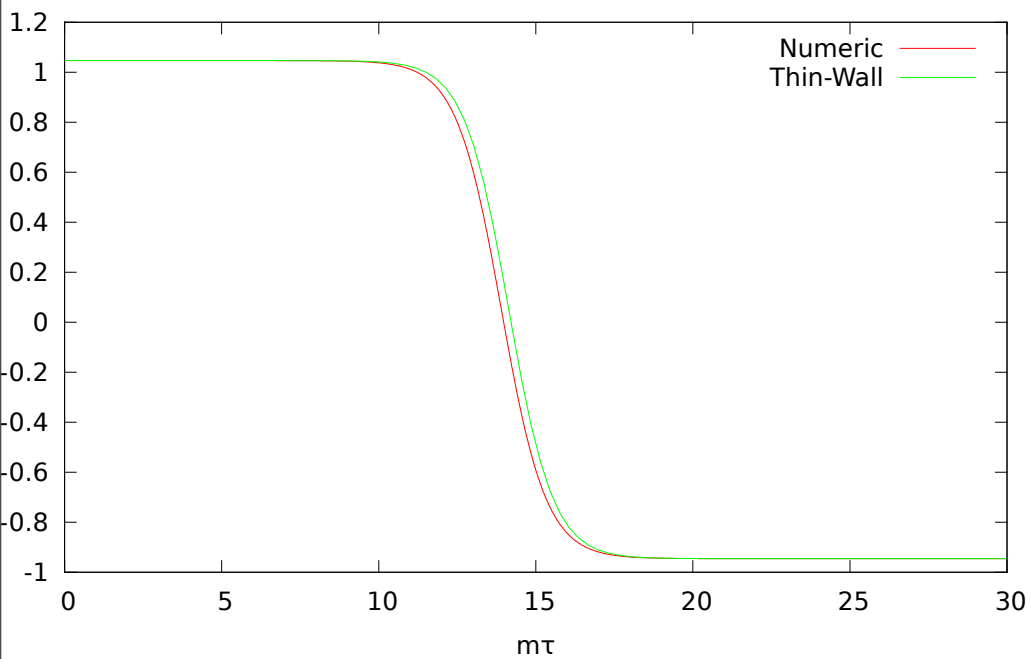
*cf. 1D work that dominates the subject Gleiser, Kleban+, Johnson, Peiris, Lehner,*  
*an oscillon phenomenon is possible in preheating CMB+ observables?*

**long-lived oscillon energy ~ 10%**

**energy  
density  
evolution**

**high  
contours**





the oft-used thin wall approximation to instantons is not accurate enough. a full numerical instanton solution is required. especially so for thick wall scenarios



*add  $H(t) = V_{inf}$  in  
inflation direction*

$$R_{\text{bubble},i} = 0.1 H^{-1}$$

$$\Delta X_{\text{bubble}} = 0.25 H^{-1}$$

*when domain walls (big bubbles) collide in full 3D lattice sims*

*with tiny zero point & wall fluctuations*

*=> burst of scalar radiation at  $c$  (with outgoing radiation BCs)*

*+ long-lived oscillons, size related to the mass*

*energy  
density  
evolution*

*high  
contours*

*does the **observable** universe  
use **double hubble bubble-**  
**iciousness? CMB intermittency?***

axionic potential

$$V \sim 1 - \cos(\theta)$$

kink -antikink instanton = IC

continued wall collisions  
because of periodicity =>  
amplification of quantum noise  
fluctuations  
not quite Kleban+ unwinding  
inflation of D-branes

# conclusions:

highly nonlinear field evolutions happened (Eol, bubble collisions).

do they lead to observable rare-event anomalies?

or just *weak* constraints on multifield potentials,  $>$  horizon fields, nucleation rates, *etc.*

*amusing subdominant patterns do arise!*

**END**