

**how** (most of) the **entropy** in matter =>

*GUT plasma/quark soup* =>  $S(\gamma, \nu)$  was

**generated** (through a **shock-in-time**)

**via nonlinear coupling** of the **inflaton** to **new**

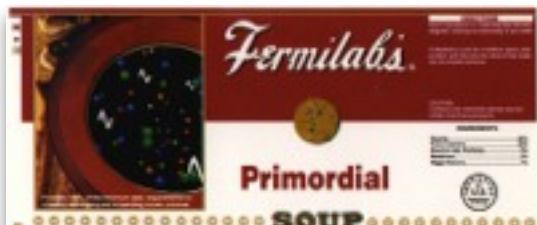
**interaction channels**  $g, \chi_a$   $V_{\text{eff}}(\varphi, \chi_a | g, \dots)$  aka

$V_{\text{eff}}(r, \theta_a | g, \dots)$  ultimately to **standard model degrees of freedom**

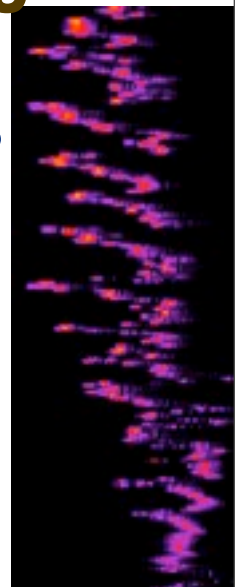
∃ a role for *decaying particles, 1st order phase transitions?*

**exactly who, what, where, when, why?**

*we search for fossil "non-Gaussian" structures from this period with Planck +WMAP9*



$a_{\text{Shock}}(g)$



## Potentials at the End of *Inflation with Physical Motivation*

**HEATING:** how to damp coherent ballistic trajectories into high-k entropy.

old, eg SBB89  $\Gamma$  (KE+PE). still used! e.g., warm inflation  $J_j = \Gamma_j \dot{\phi}_j$ ,  $\dot{\phi}_j \equiv \text{sgn}(\dot{\phi}_j) |\partial_\mu \phi_j \partial^\mu \phi_j|^{1/2}$

$$\Gamma_j = f_j M_j \cdot \quad \frac{1}{a^4} \frac{da^4 \rho_r}{dt} = \sum_i \Gamma_i \dot{\phi}_i^2$$

decay rates (Feynman diagrams) and transport theory difficult to make accurate through preheating

rather fundamental scalar field nonlinear evolution equations (inflaton, isocons) & effective potentials & kinetic energies

post KLS93: via inflaton self-couplings; isocon-inflaton field couplings, fermion-bar fermion, gauge fields, pseudo-scalar\*FFdual,

$$V(\phi_1, \phi_2) = \frac{m_2^2 \phi_2^2}{2} + \frac{\lambda_2 \phi_2^4}{4} + \frac{m_1^2 \phi_1^2}{2} + \frac{\lambda_1 \phi_1^4}{4} - \frac{\nu \phi_1^2 \phi_2^2}{2} + V_0 - \mu_1 \phi_1 \phi_2^2$$

tachyonic instability:  $m_{\text{eff}}^2 < 0$  single field can preheat fast with only a few oscillations, eg roulette in the groove, trilinear

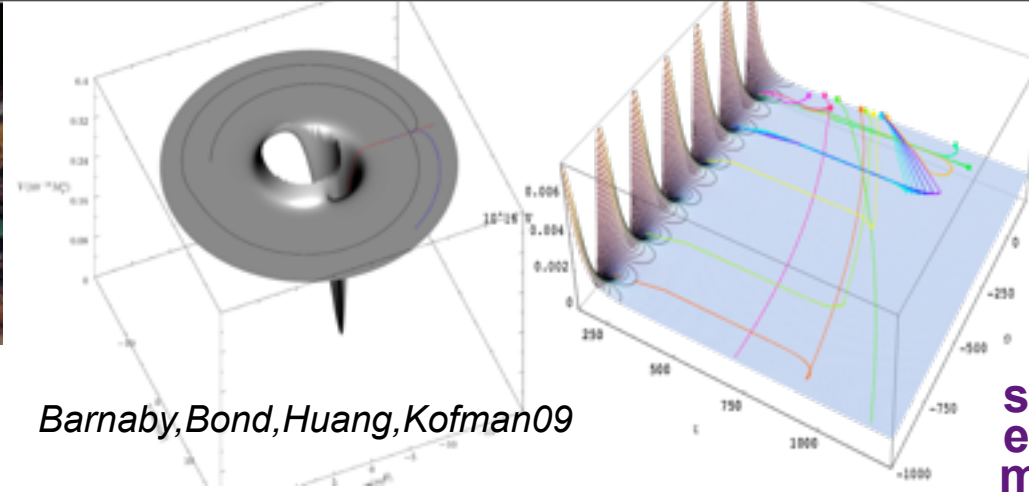
**Stochastic inflation works:** ballistic trajectories for fields  $q_x$  with kicks from sub-horizon waves  $dW_x$  causing nearby trajectories to deviate,  $\zeta_{\text{NL}}$  like  $dE+pdV$  a near-adiabatic invariant, sourced by stress\*strain-rate & energy currents (regularizer between nearby positions X).

$\epsilon = -3/2 d \ln \rho / d \ln a^3 = 1$  defines End of Inflation (cf.  $\epsilon < .0075$  now!), but it is not a magic boundary, dragged trajectories break into (spatially independent) oscillations. weak point-to-point coupling until ...

new picture: ballistic until the shock-in-time = huge time-localized non-eq entropy generation; slow S-evolution after which is V-dependent. only weak-coupling of nearby points before. ULSS & LSS & SSS modulator field  $\zeta_{\text{NL}}(\text{modulator}(x))$ , e.g. modulator =  $\chi_i(x)$ ,  $g(x)$

**entropy generation in preheating from the coherent inflaton (origin of all matter & radiation), nonG from post-inflation but pre-entropy generation (B<sup>2</sup>FH13) drift trajectories can lead to pre-shock-in-time caustics and other phase space convergences in the deformations**

$$\partial \ln a / \partial \chi_i(x), \partial \ln a / \partial g(x) \Rightarrow$$



Barnaby, Bond, Huang, Kofman09

**NL, nonG curvature distribution( $\chi_i(x), g(x), \dots$ )**

**quantum diffusion spatial jitter**  
**drift** ← ↔

roulette oscillations highly damped  
 => no-non-G  
 if redirect by  $\chi_i, g$   
 => non-G

**let there be heat**

SEMITELLERIAL INFLATION

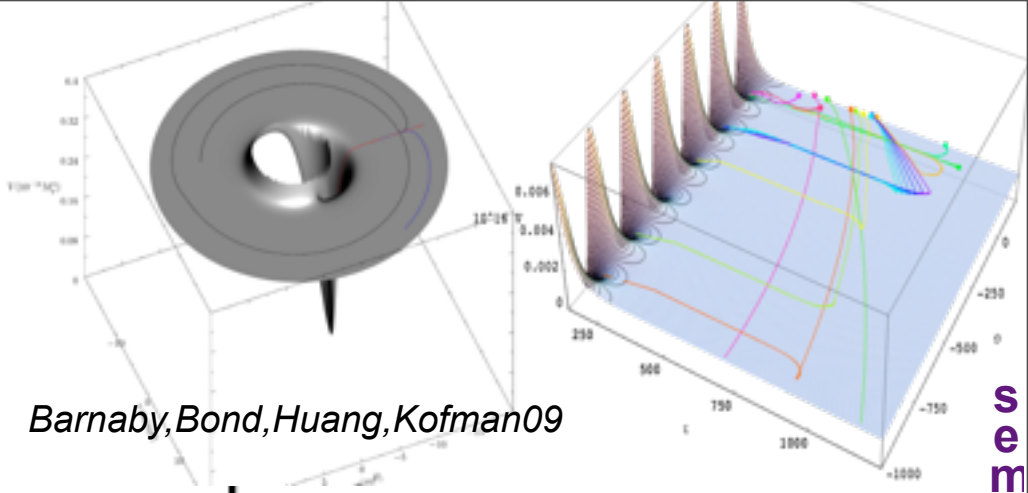
**entropy generation in preheating from the coherent inflaton (origin of all matter & radiation), nonG from post-inflation but pre-entropy generation (B<sup>2</sup>FH13) drift trajectories can lead to pre-shock-in-time caustics and other phase space convergences in the deformations**

$$\partial \ln a / \partial \chi_i(x), \partial \ln a / \partial g(x) \Rightarrow$$

$$a = 1$$

**NL, nonG curvature distribution ( $\chi_i(x), g(x), \dots$ )**

A visualized 2D slice in lattice simulation



Barnaby, Bond, Huang, Kofman 09

Preheating After Roulette Inflation

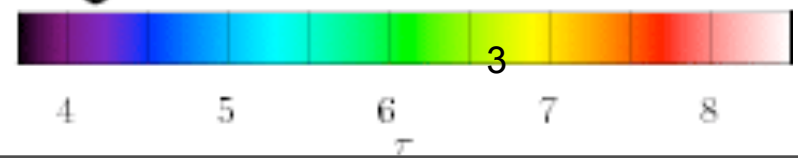
$$\langle \tau \rangle =$$

quantum diffusion spatial jitter

drift

roulette oscillations highly damped => no-non-G if redirect by  $\chi_i, g$  => non-G

let there be heat



SEMILINEAR INFLATION



# modulating post-inflation entropy generation shocks via longrange fields

isocon

$\chi(\mathbf{x})$

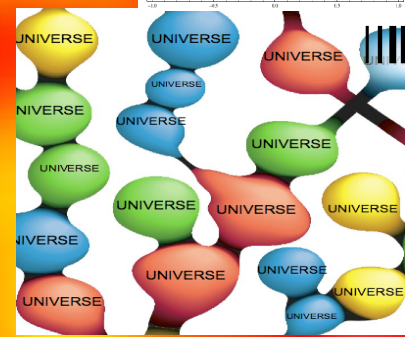
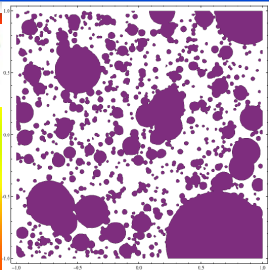
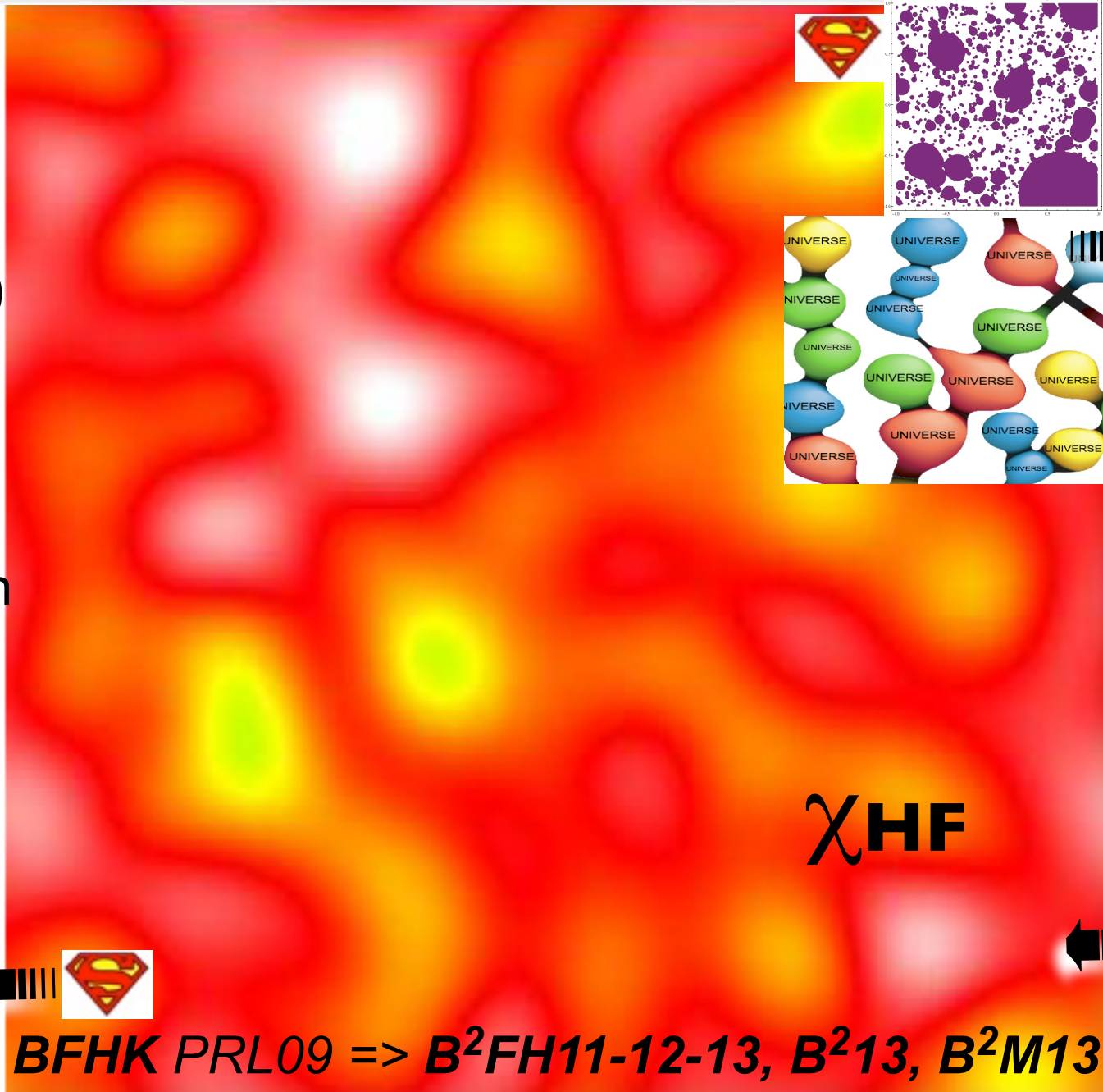
or  
 $g(\sigma(\mathbf{x}))$   
 or..

$\phi$

inflaton

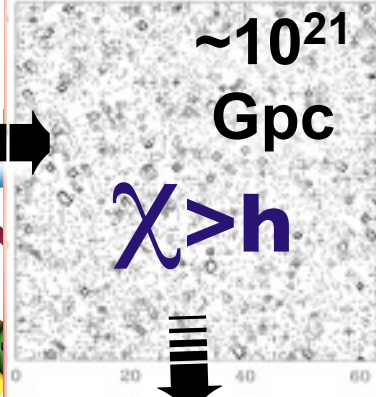
pre-heating  
 patch  
 (~1cm)

$S_{U,m+r}$   
 $\sim 10^{88.6}$



$S_{U,uuUULSS}$

CONTOUR PLOTS FOR  $H(\phi_0) = 1.0m_p$



$\chi > h$

1000 Gpc

$\chi > h$

$\chi_{HF}$

10 Gpc

$\chi_b$

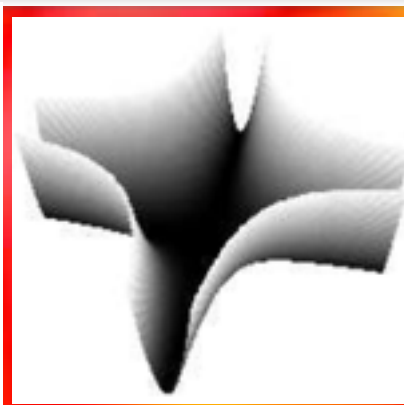
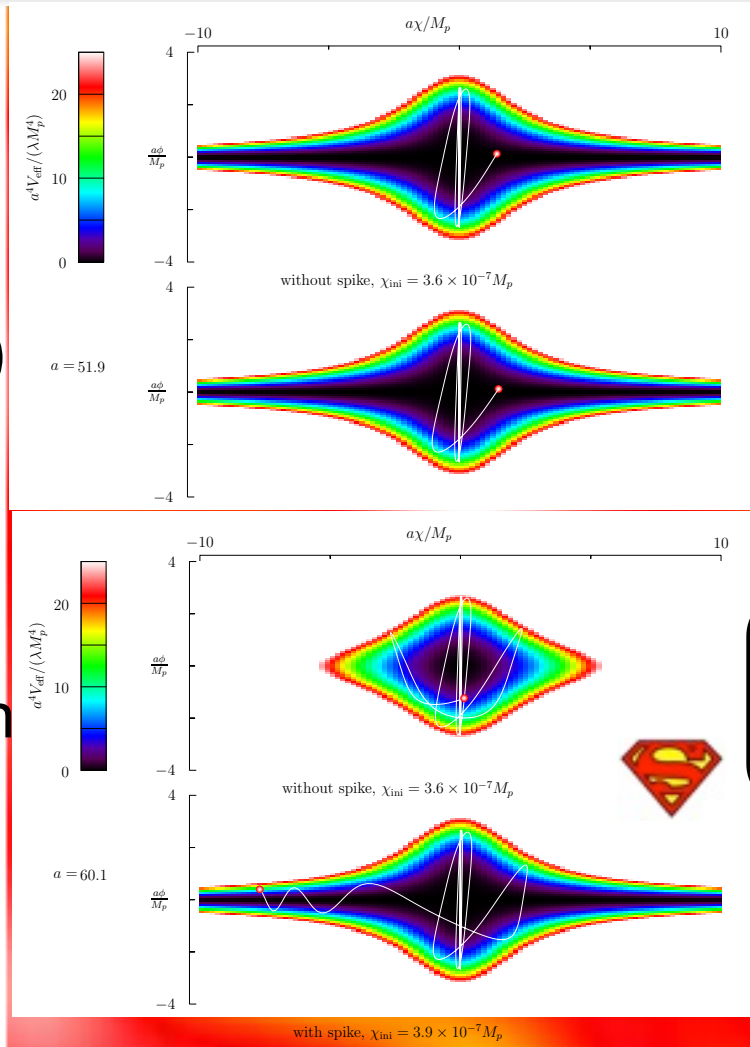
***BFHK PRL09 => B<sup>2</sup>FH11-12-13, B<sup>2</sup>13, B<sup>2</sup>M13***

# modulating post-inflation entropy generation shocks *via* longrange fields

isocon  
 $\chi(\mathbf{x})$   
 or  
 $\mathbf{g}(\sigma(\mathbf{x}))$   
 or..

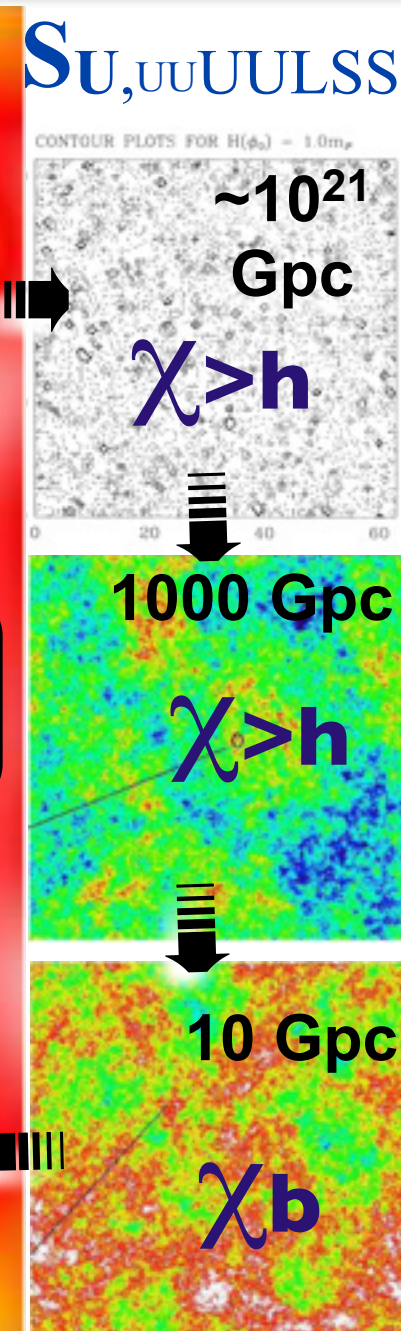
$\phi$   
 inflaton  
 pre-heating patch  
 (~1cm)

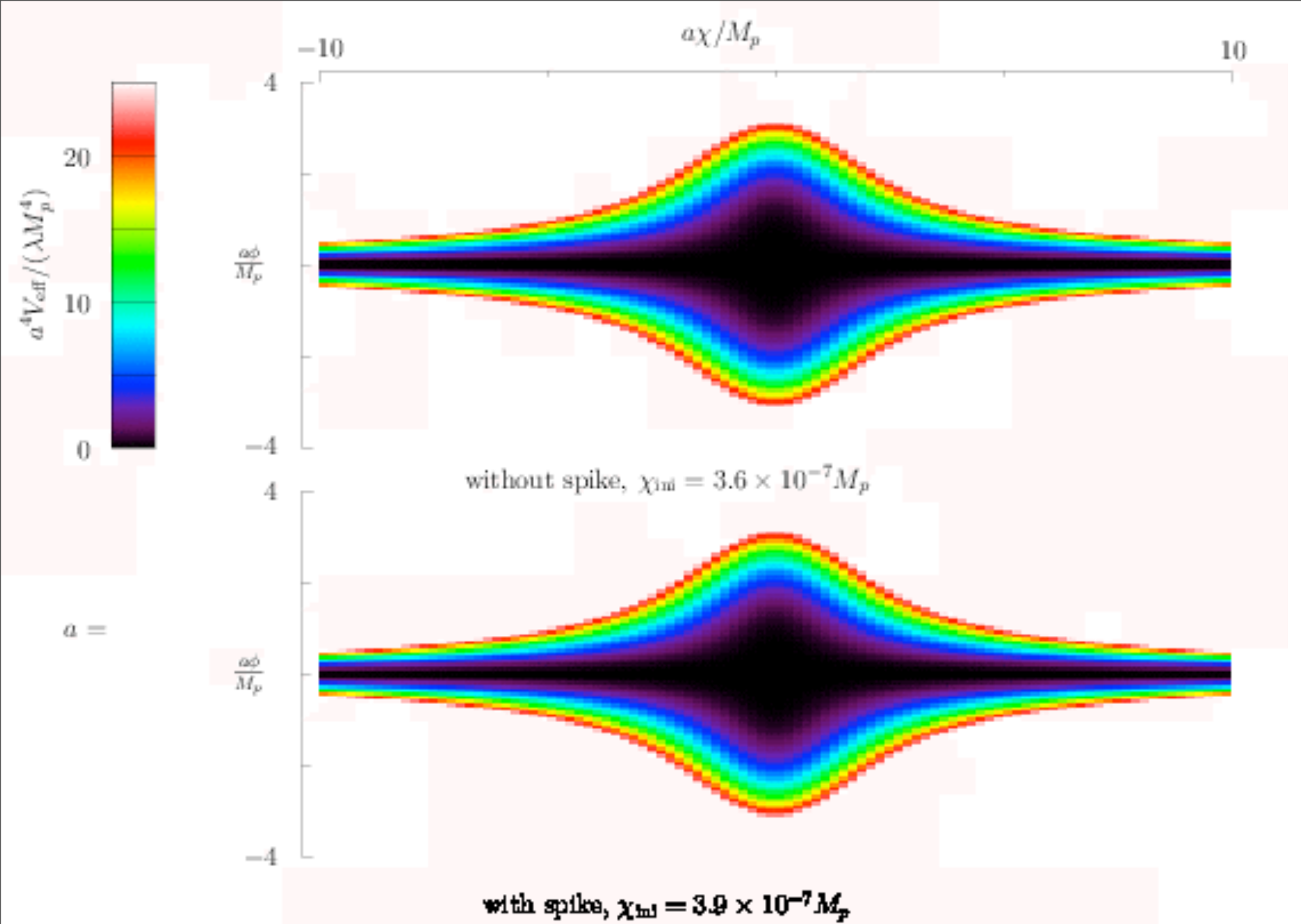
$S_{U,m+r}$   
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Parametric Resonance

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$





**$V_{\text{eff}}$  is trajectory dependent**



# modulating post-inflation entropy generation shocks via longrange fields

isocon

$\chi(\mathbf{x})$

or

$\mathbf{g}(\sigma(\mathbf{x}))$

or..

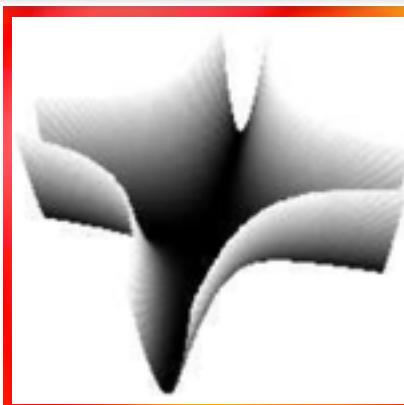
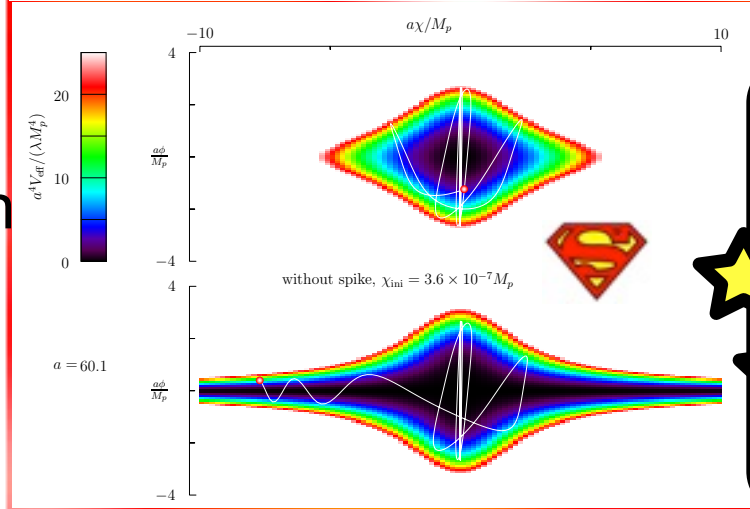
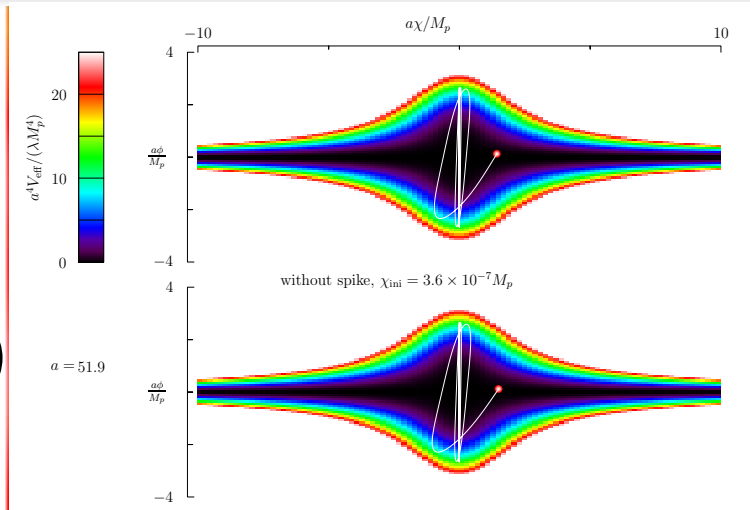
$\phi$

inflaton

pre-heating patch (~1cm)

$S_{U,m+r}$

$\sim 10^{88.6}$



How general? We now think very - basins at the end of inflation

$V(\phi, \chi)$  ★

$= 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$

★  $1/2 m^2 \phi^2 + 1/2 g^2(\sigma) \phi^2 \chi^2$

★  $= 1/4 \lambda (r^2 - v^2)^2 U$

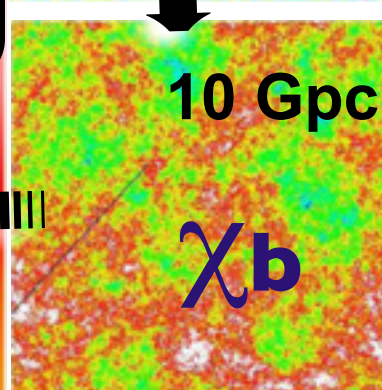
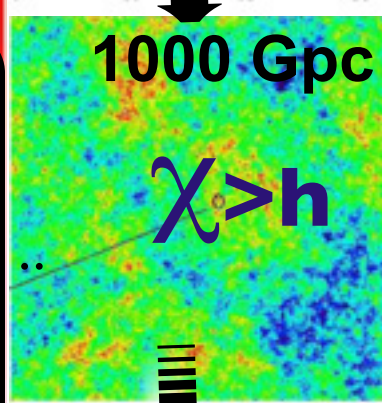
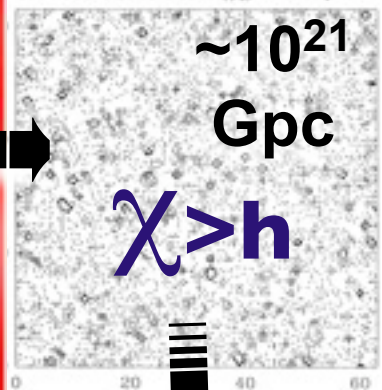
$V(r)U(\cos\theta), r^2 = \phi^2 + \chi^2$

$V(r, \theta) = \sum_M V_M(r) \cos(m\theta)$  pNGB, Roulette r-hole size

3D  $\phi \chi \sigma$  fields  $V(r, \mathbf{n}) = \sum_{LM} V_{LM}(r) Y_{LM}(\mathbf{n})$

$S_{U, \text{UUULSS}}$

CONTOUR PLOTS FOR  $H(\phi_s) = 1.0m_p$





# modulating post-inflation entropy generation shocks via longrange fields

isocon

$\chi(\mathbf{x})$

or

$\mathbf{g}(\sigma(\mathbf{x}))$

or..

$\phi$

inflaton

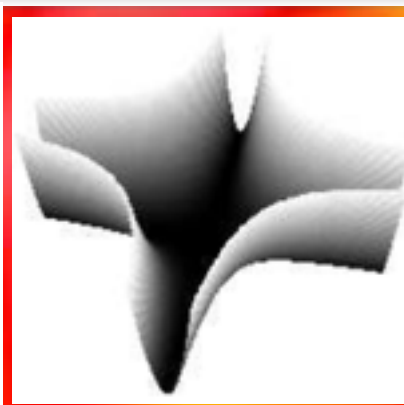
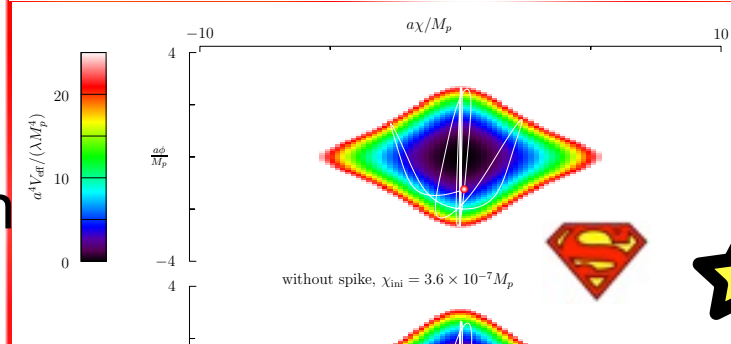
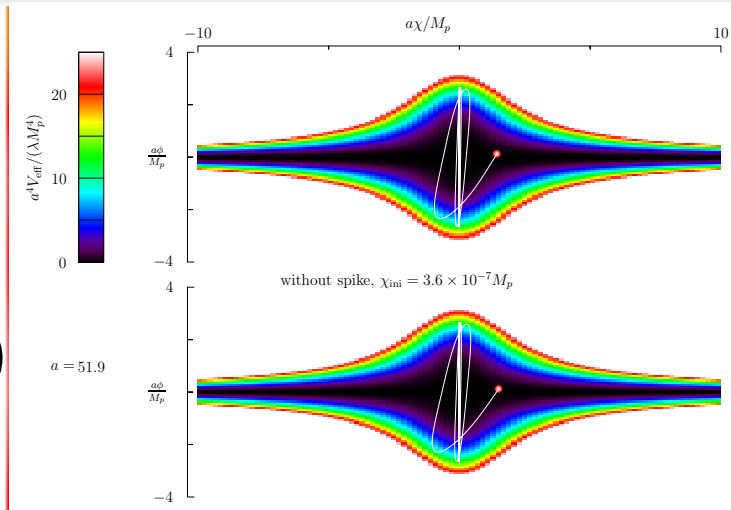
pre-

heating patch

(~1cm)

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How general? We now think very - basins at the end of inflation

$V(\phi, \chi)$  ★

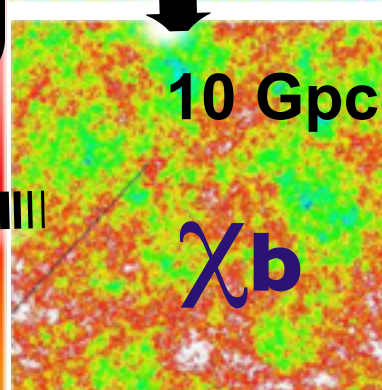
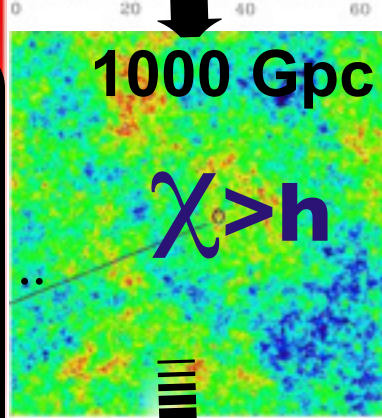
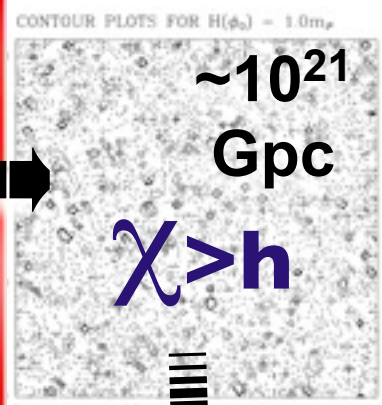
$= 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$

★  $1/2 m^2 \phi^2 + 1/2 g^2(\sigma) \phi^2 \chi^2$

★  $= 1/4 \lambda (r^2 - v^2)^2 U$

$V(r, \theta) U(\cos \theta), r^2 = \phi^2 + \chi^2$

$S_{U, \text{UUUULSS}}$



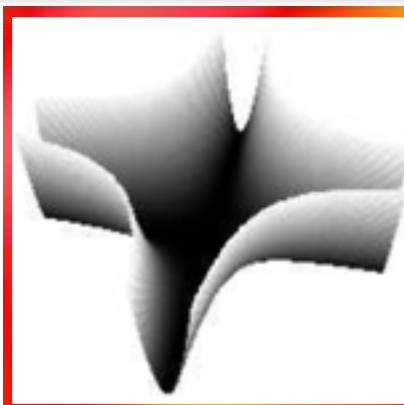
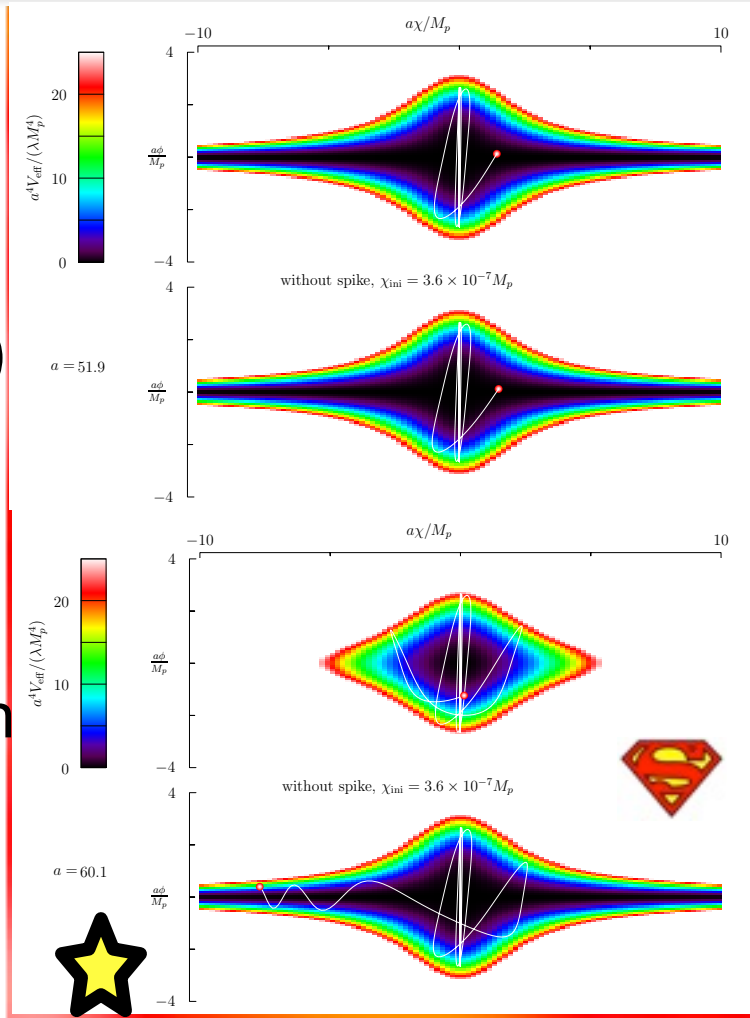
dynamical stringy energy & 3D oscillons store energy, curvaton-ish but not

$V(r, \theta) = \sum_M V_M(r) \cos(m\theta)$  pNGB, Roulette r~hole size

3D  $\phi \chi \sigma$  fields  $V(r, n) = \sum_{LM} V_{LM}(r) Y_{LM}(n)$

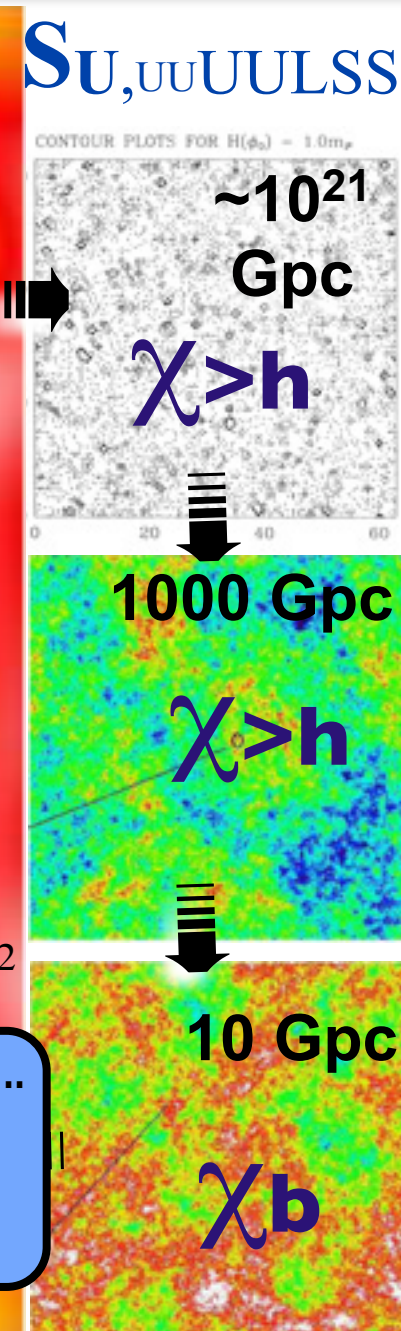
# modulating post-inflation entropy generation shocks *via* longrange fields

isocon  
 $\chi(\mathbf{x})$   
 or  
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 $\phi$   
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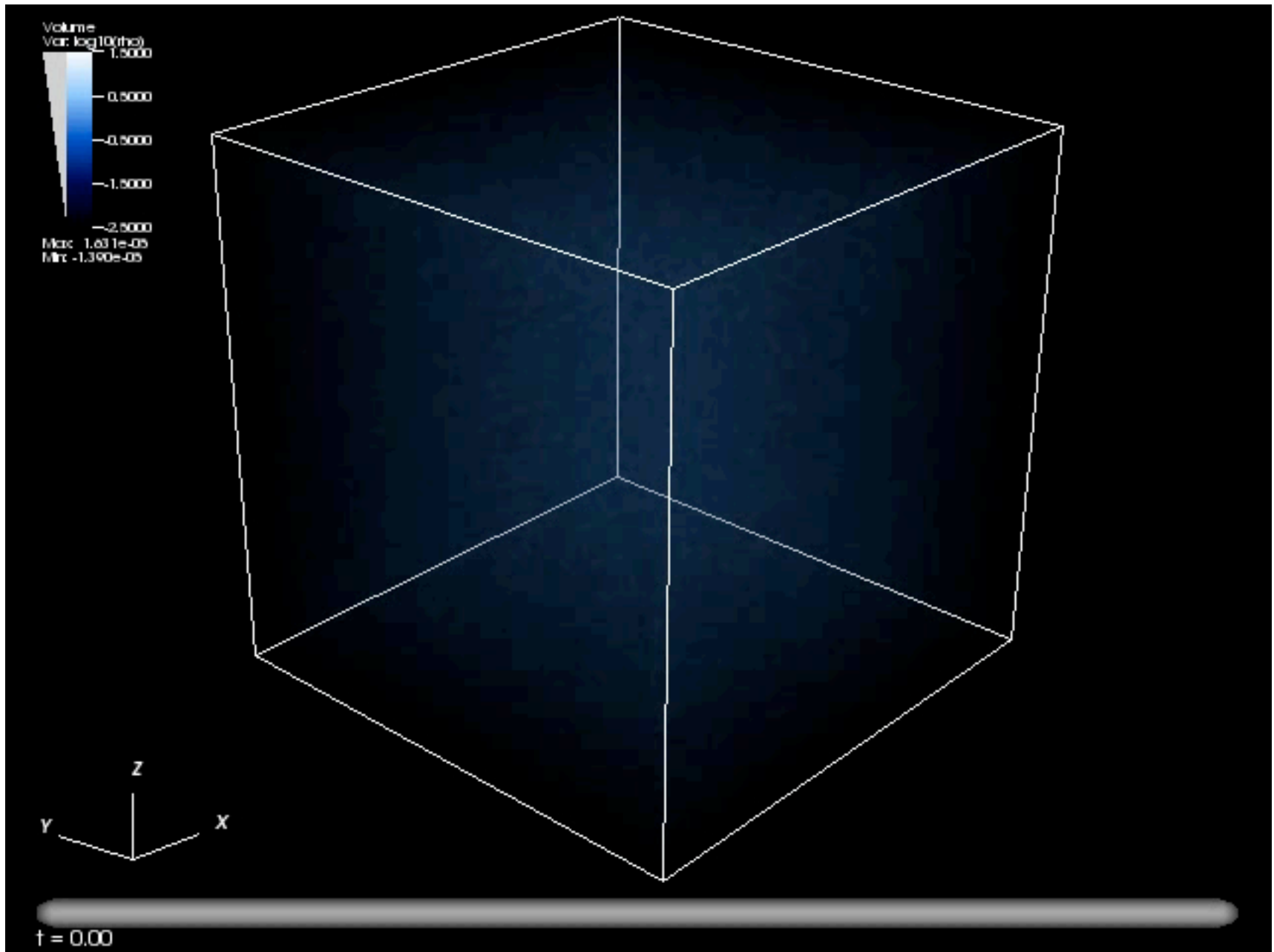
How general? We now think very - basins at the end of inflation

$$V(\mathbf{r})U(\cos\theta), r^2 = \phi^2 + \chi^2$$



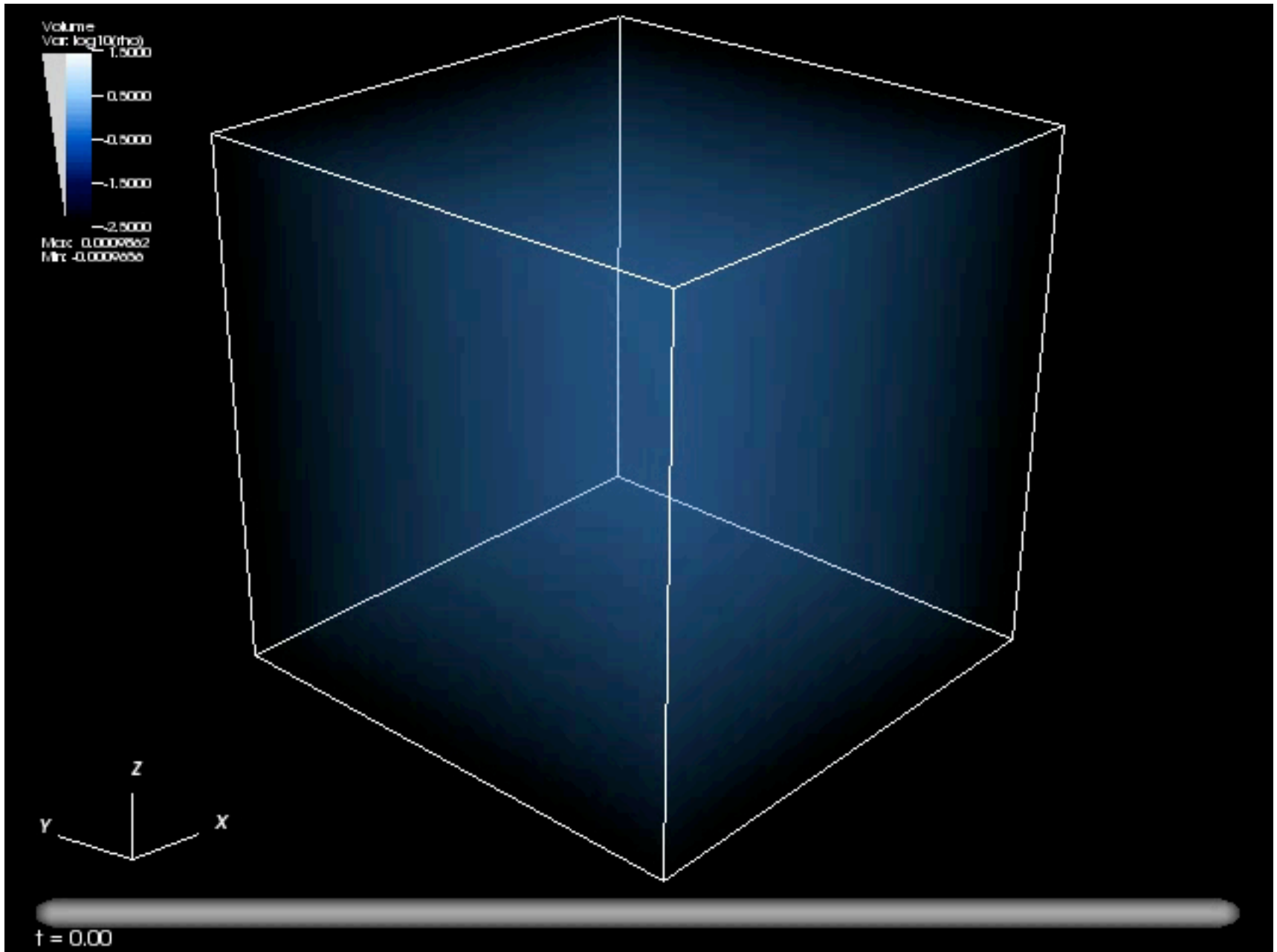
angular variables pNGB natural inflation, racetrack, monodromy, ..  
 $V(\mathbf{r}, \theta) = \sum_M V_M(\mathbf{r}) \cos(m\theta)$  pNGB, Roulette  $r \sim$  hole size  
 3D  $\phi \chi \sigma$  fields  $V(\mathbf{r}, \mathbf{n}) = \sum_{LM} V_{LM}(\mathbf{r}) Y_{LM}(\mathbf{n})$

$$\text{quartic inflaton } V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



*log-normal pdf (density), in k-bands too; normal pdf (velocity)*

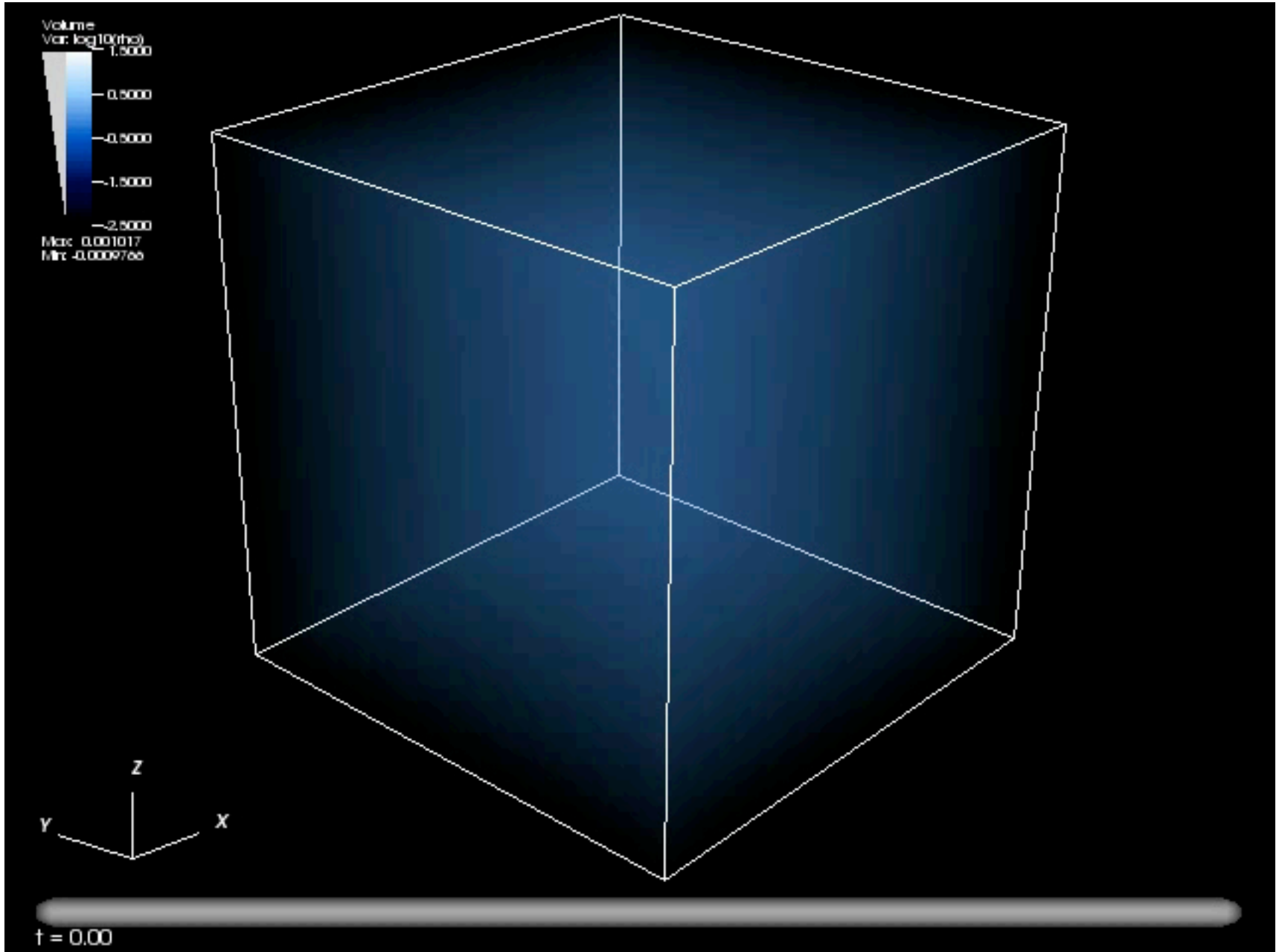
$$\text{quadratic inflaton } V(\phi, \chi) = \frac{1}{2} m^2 \phi^2 + \frac{1}{2} g^2(\sigma) \phi^2 \chi^2 \dots$$



*log-normal pdf (density), in k-bands too; normal pdf (velocity)*



quadratic inflaton trilinear coupling  $V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 \sigma \phi \chi^2 + 1/4 \lambda \chi^4$



*log-normal pdf (density), in k-bands too; normal pdf (velocity)*

### Designing density fluctuation spectra in inflation

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(Received 3 November 1988)

obeying Gaussian statistics independently of initial conditions. Since observations only probe a narrow patch of the potential surface, it is possible that it is littered with moguls, leading to arbitrarily complex "mountain range" spectra that can only be determined phenomenologically. We also construct an inflation model which houses the chaotic inflation picture within the grand unified theory (GUT) framework. The standard chaotic picture requires an unnaturally flat scalar field potential,  $\lambda \approx 5 \times 10^{-14}$ , and a strong curvature coupling parameter bound,  $\xi < 0.002$ . By allowing the Higgs field to be strongly coupled to gravity through a large negative curvature coupling strength,  $\xi \sim -10^4$ , so the Planck mass depends on the GUT Higgs field, the Higgs field can be strongly coupled to matter fields [with  $\lambda \sim (\xi/10^5)^2$ ]. This leads to both a flat Zeldovich spectrum of the "observed" amplitude and a high reheating temperature ( $\sim 10^{15}$  GeV), unlike the  $\lambda \sim 10^{-13}$  standard case. The large  $-\xi$  would be related to the ratio of the Planck scale to a typical GUT scale. Although a single dynamically important Higgs multiplet gives flat spectra, a richer Higgs sector could lead to broken scale invariance.

### APPENDIX B: INDUCED GRAVITY IN A GUT FRAMEWORK

In Sec. VII we claimed that if the curvature coupling constant was chosen to be  $\xi = -2 \times 10^4$ , inflation could be incorporated within a grand unified theory. However, the simplified analysis of that section utilized a single complex scalar field coupled to a U(1) gauge field, and we now wish to consider the physically more interesting case of non-Abelian gauge fields. We concentrate on the well-studied minimal SU(5) model, although any gauge group could be incorporated. In SU(5), the Higgs field,  $H$ , and the gauge field,  $A_\mu$ , both in the adjoint representation,

We now consider the cosmological consequences of the four fields that parametrize the diagonal Higgs field,  $H = \sqrt{2} \phi_i \tau^i$ . It proves convenient to choose the diagonal basis

$$\begin{aligned}\tau^1 &= \text{diag}[2, 2, 2, -3, -3]/\sqrt{60}, \\ \tau^2 &= \text{diag}[0, 0, 0, 1, -1]/2, \\ \tau^3 &= \text{diag}[1, -1, 0, 0, 0]/2, \\ \tau^4 &= \text{diag}[1, 1, -2, 0, 0]/(2\sqrt{3}),\end{aligned}\tag{B14}$$

and then express the  $\phi_i$  in hyperspherical coordinates,

$\phi, \theta_1, \theta_2, \theta_3$ : *angle variables in SU(5)*

$$\begin{aligned}\phi_1 &= \phi \cos \theta_1, \\ \phi_2 &= \phi \sin \theta_1 \cos \theta_2, \\ \phi_3 &= \phi \sin \theta_1 \sin \theta_2 \cos \theta_3, \\ \phi_4 &= \phi \sin \theta_1 \sin \theta_2 \sin \theta_3.\end{aligned}\tag{B15}$$

We find that the scalar field part of the Lagrangian density, (B2), is

$$\begin{aligned}\mathcal{L}_\phi &= -\frac{1}{2} \chi_{,\mu} \chi^{,\mu} - \frac{1}{2} \frac{m_P^2 \phi^2}{16\pi f} (\theta_{1,\mu} \theta_1^{,\mu} + \sin^2 \theta_1 \theta_{2,\mu} \theta_2^{,\mu} \\ &\quad + \sin^2 \theta_1 \sin^2 \theta_2 \theta_{3,\mu} \theta_3^{,\mu}) \\ &\quad - \left[ \frac{m_P^2}{16\pi f} \right]^2 V(H),\end{aligned}\tag{B16a}$$

where

$$V(H) = -m_1^2 \phi^2 + \phi^4 [\lambda_1 + \lambda_2 g(\theta_i)],\tag{B16b}$$

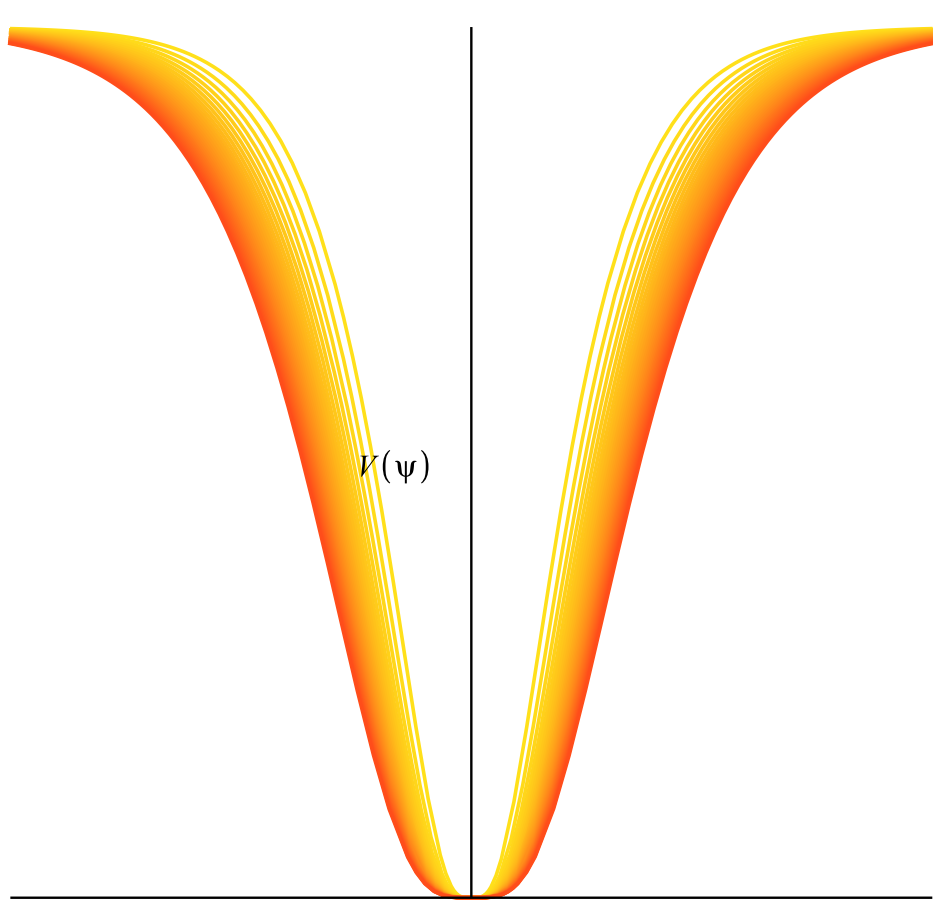
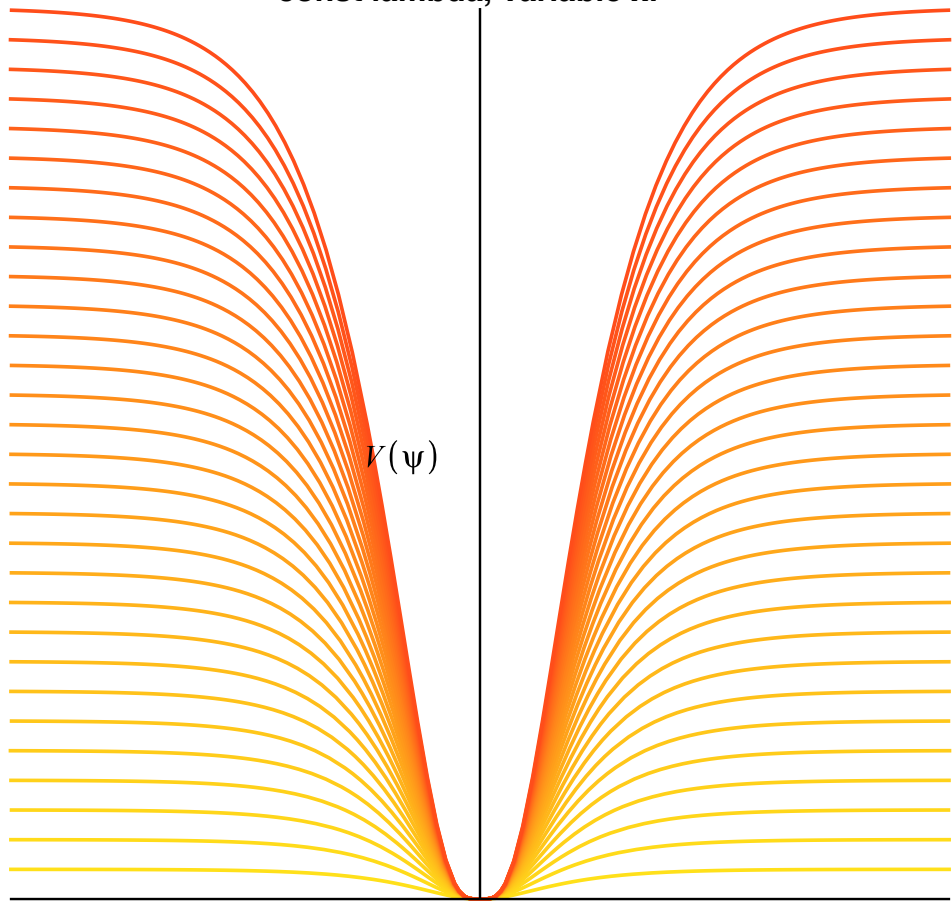
$$g(\theta_i) = \frac{7}{30} + \frac{4}{3} \sin^2 \theta_1 - \frac{16}{15} \sin^4 \theta_1 + \sin^2 \theta_1 \sin^2 \theta_2$$

$$\begin{aligned}&\times \left[ -1 + \sin^2 \theta_1 \sin^2 \theta_2 \right. \\ &\quad \left. + \frac{4\sqrt{5}}{15} \cos \theta_1 \sin \theta_1 \sin \theta_2 \sin(3\theta_3) \right],\end{aligned}\tag{B16c}$$

$L = (1-xi \phi^2) R/2 - (\text{nabla} \phi)^2/2 - \text{lambda} \phi^4/4$   
 in Einstein frame and for new (canonically normalized) field  $\psi$

**const lambda, variable xi**

const lambda/xi^2, variable xi



$\psi$

$\psi$

$$\chi = \int [K^{11}(\phi)]^{1/2} d\phi,$$

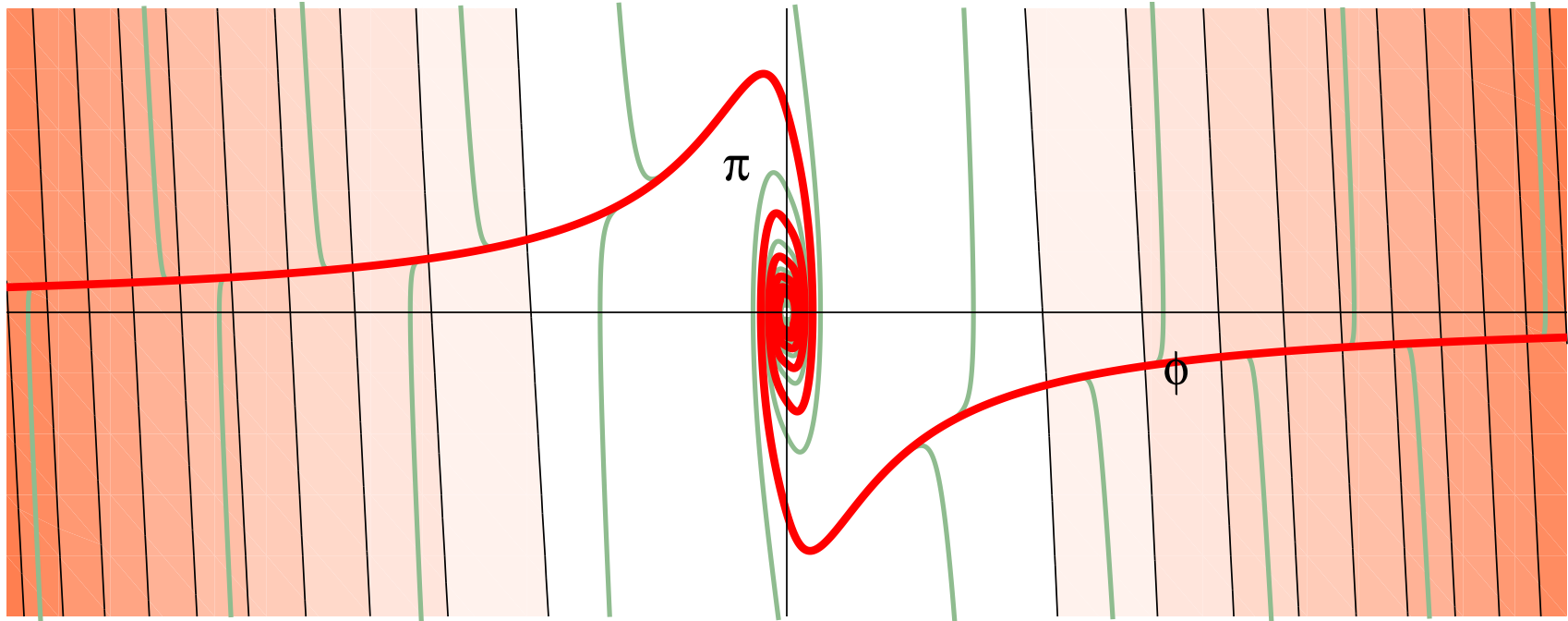
$$U(\chi) = \left[ \frac{m^2}{m_p^2} + 8\pi |\xi| \frac{\phi^2(\chi)}{m_p^2} \right]^{-2} V(\phi(\chi)).$$

$$K^{11} = \frac{\frac{m^2}{m_p^2} + 8\pi |\xi| (1 + 6|\xi|) \frac{\phi^2}{m_p^2}}{\left[ \frac{m^2}{m_p^2} + 8\pi |\xi| \frac{\phi^2}{m_p^2} \right]^2}.$$

quartic inflaton variable Planck mass  $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$

$$\xi = -1$$

shading =  $\ln a(\phi, \pi)$

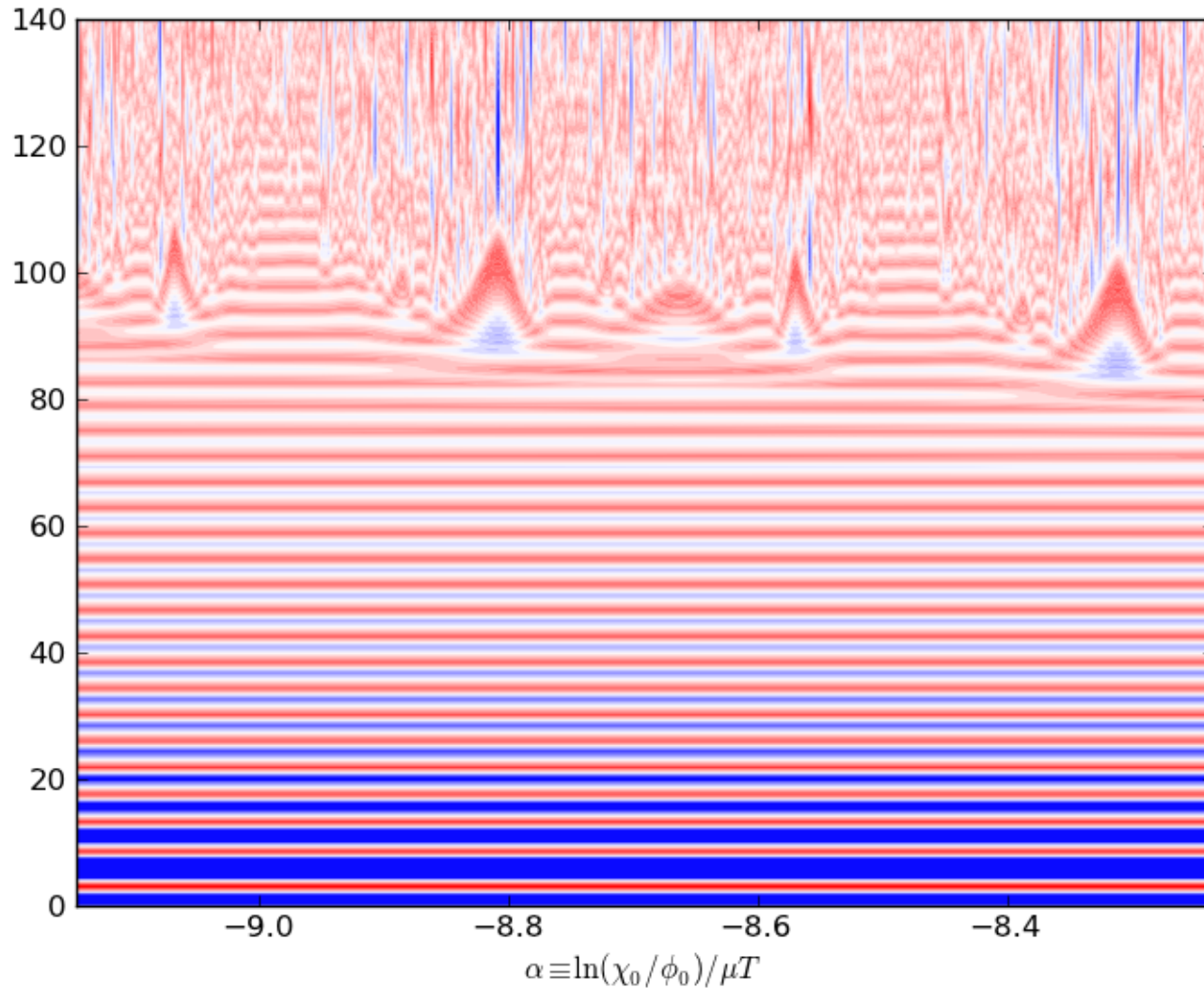


*spikes persist with flattened effective potential*



quartic inflaton variable Planck mass  $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$

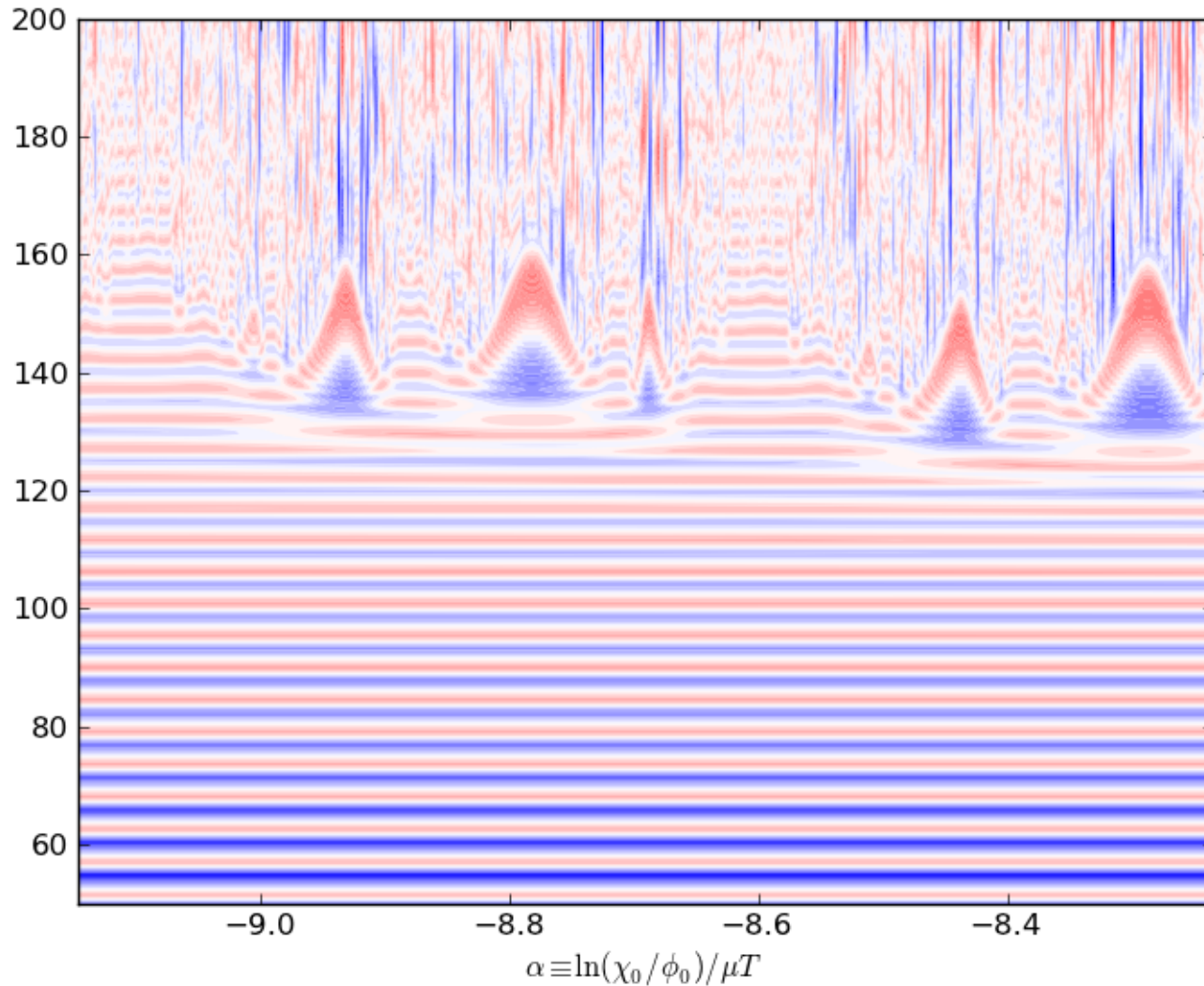
$$\xi = -1$$



*spikes persist with flattened effective potential*

quartic inflaton variable Planck mass  $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$

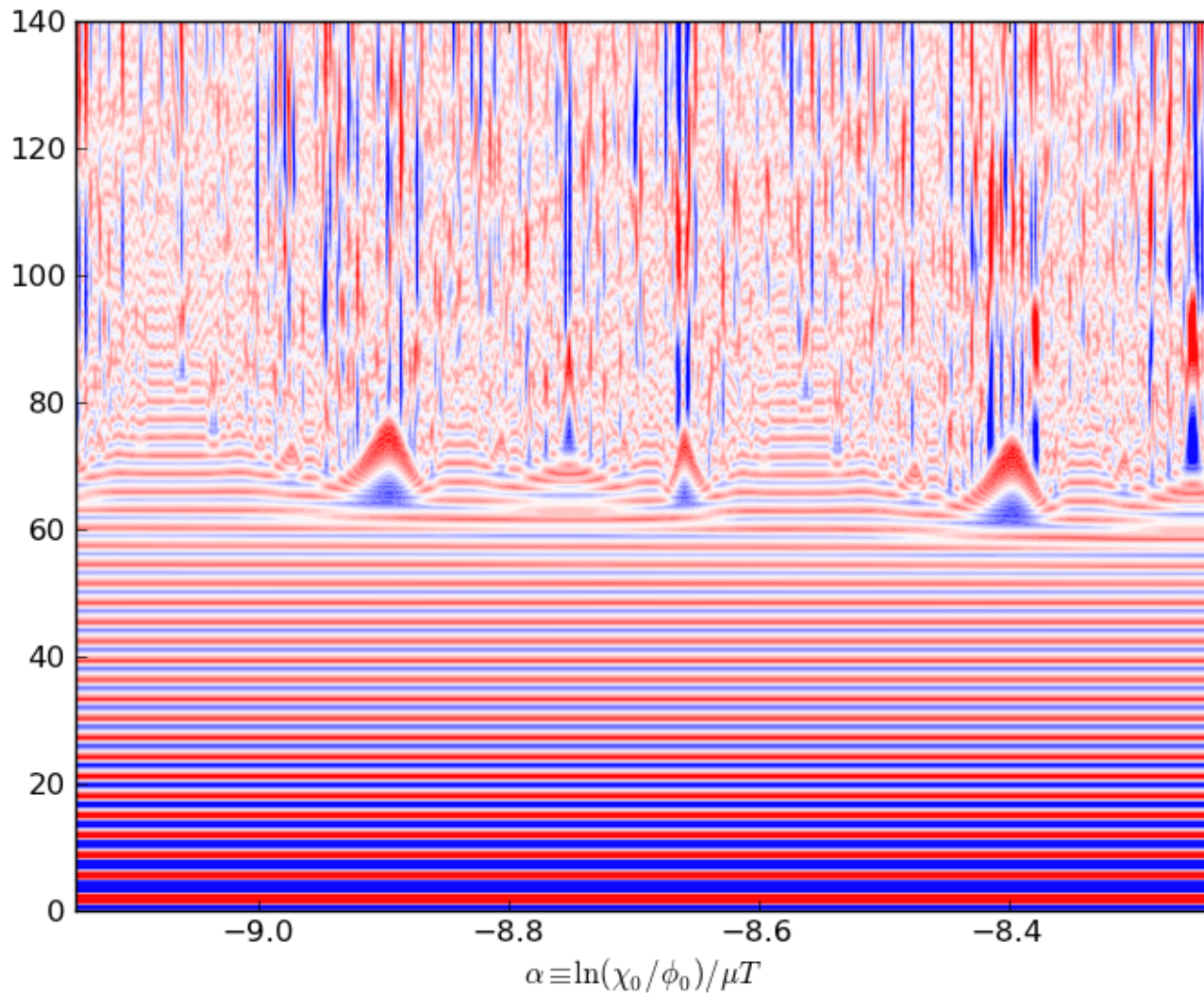
$\xi = -2$



*spikes persist with flattened effective potential*

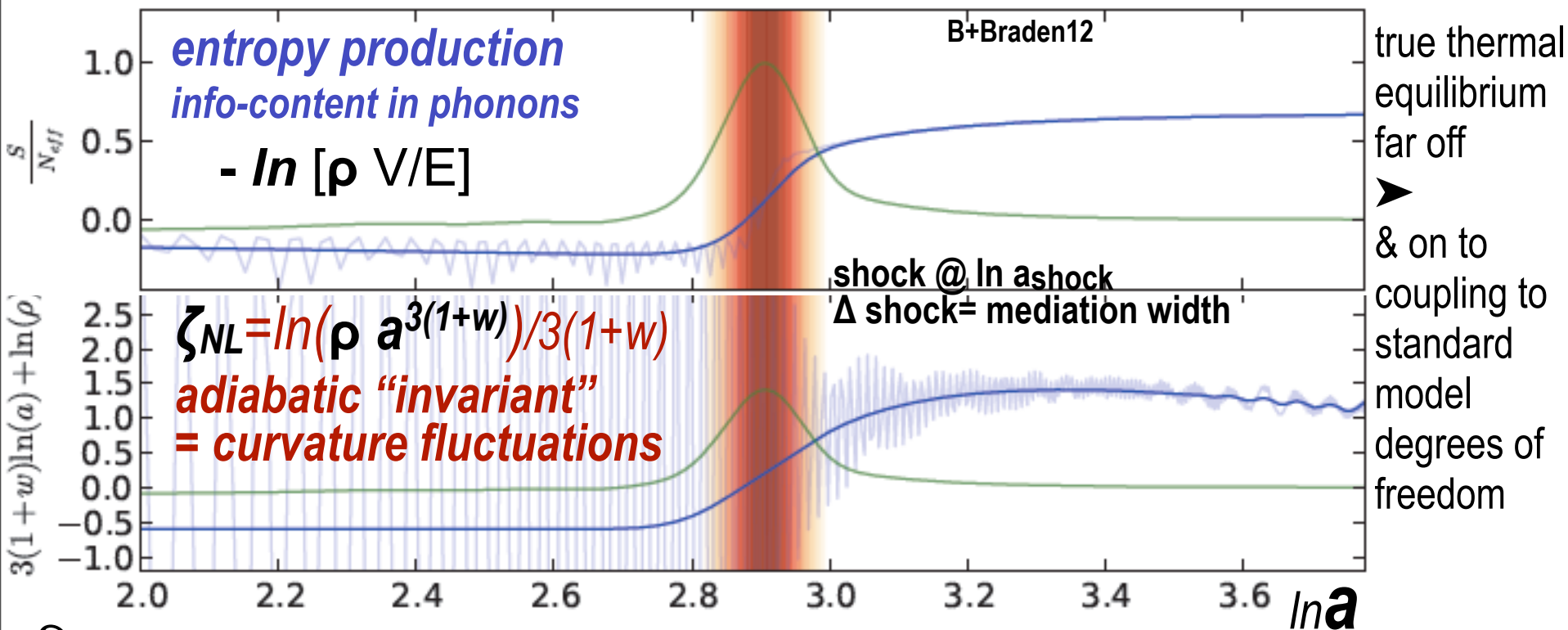
quartic inflaton variable Planck mass  $V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$

$$\xi = -1/2$$



*spikes persist with flattened effective potential*

# nonG from large-scale modulations of the shock-in-times of preheating



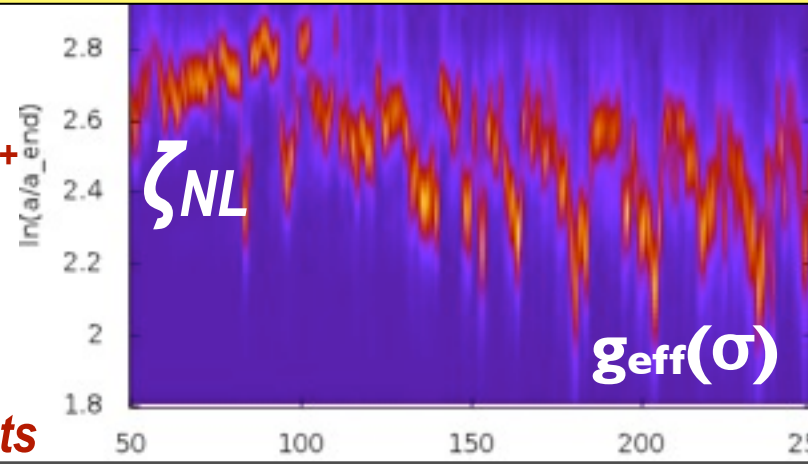
$\delta\zeta_{NLshock}(\mathbf{g}(\sigma(\mathbf{x}))) \Rightarrow$  modulated non-G

$g_0 + g_1 \sigma/M_P, g_0 \exp[\gamma_1 \sigma/M_P], ..$

$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g_{eff}(\sigma)^2 \phi^2 \chi^2$

$\delta\zeta_{NLshock}(\chi_i(\mathbf{x}) | g^2/\lambda) \Rightarrow$  NonG cold spots ++

$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$

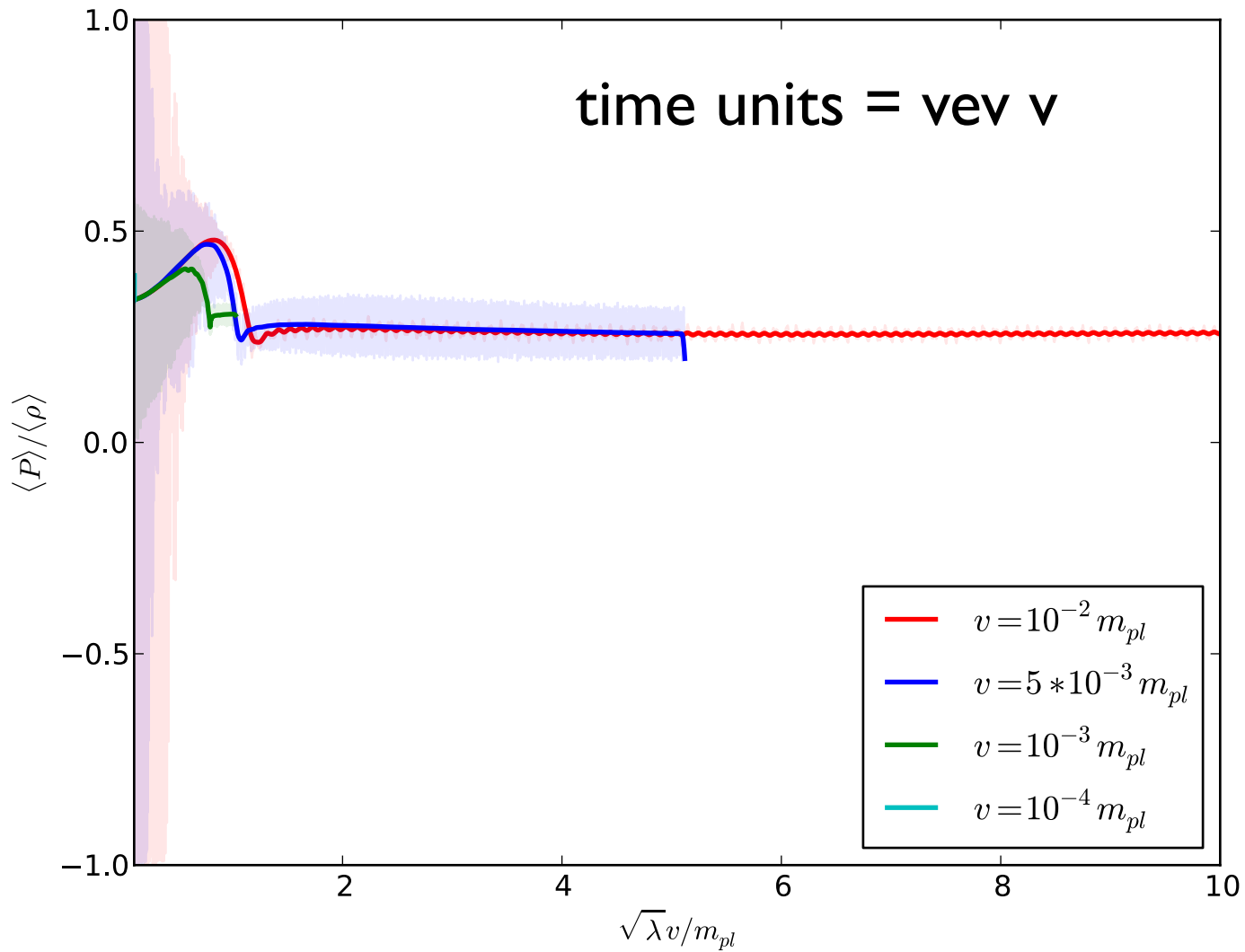


**V<sub>eff</sub> is dynamical** Bond, Braden, Frolov, Huang13  
*unconventional local non-G: no scale built into V;*  
*perturbative isocon-based f<sub>NL</sub>; rare event cold spots*



$$V(\phi, \chi) = 1/4 \lambda (r^2 - v^2)^2 U$$

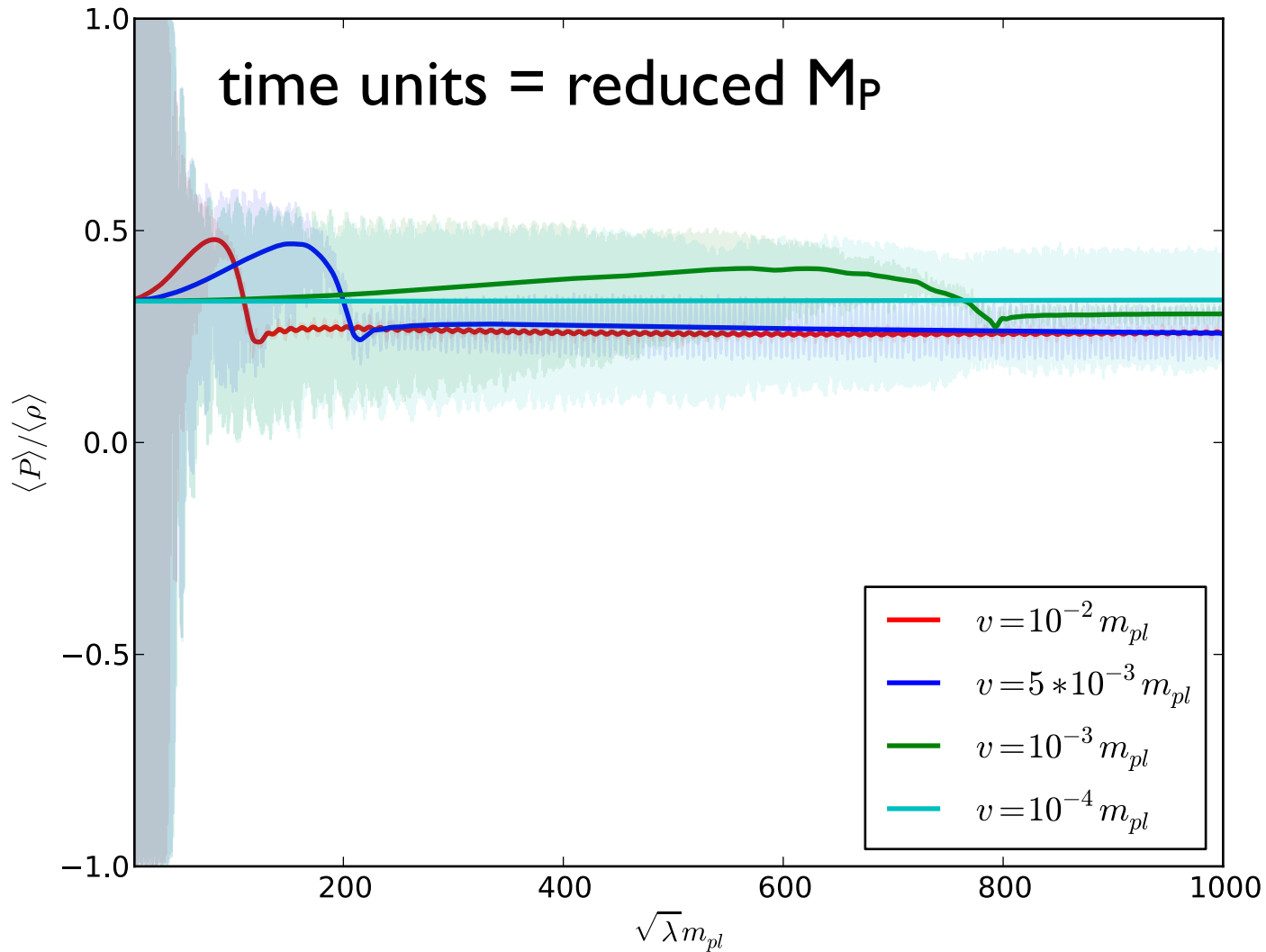
$$V(\mathbf{r})U(\cos\theta), r^2 = \phi^2 + \chi^2$$



***string-like field configurations mediate the EoS for a long time***

$$V(\phi, \chi) = 1/4 \lambda (r^2 - v^2)^2 U$$

$$V(r)U(\cos\theta), r^2 = \phi^2 + \chi^2$$



***string-like field configurations mediate the EoS for a long time***

**from**

$$\text{quartic inflaton } V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

$$\text{quadratic inflaton } V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2(\sigma) \phi^2 \chi^2 \dots$$

$$\text{quadratic inflaton trilinear coupling } V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 \sigma \phi \chi^2 + 1/4 \lambda \chi^4$$

$$\text{quartic inflaton variable Planck mass } V(\phi, \chi) = 1/4 \lambda \phi^4 - 1/2 \xi \phi^2 R + 1/2 g^2 \phi^2 \chi^2$$

aka Higgs inflation. flattened effective potential in the Einstein frame

**to**

**angular variables** *pNGB natural inflation, racetrack, monodromy, ..*

**2 field:**  $V(\mathbf{r}, \theta) = \sum_M V_M(\mathbf{r}) \cos(m\theta)$  *pNGB, Roulette  $r \sim$  hole size*

**3 field:** 3D  $\phi \chi \sigma$  fields  $V(\mathbf{r}, \mathbf{n}) = \sum_{LM} V_{LM}(\mathbf{r}) Y_{LM}(\mathbf{n})$

**5 field:** *angle variables in SU(5) & etc.*

**to?**

Simple exercises to flatten your potential

Xi Dong, Bart Horn, Eva Silverstein, and Alexander Westphal 2011