

the **Cosmology** of **now** & **then** through **first light**

Dick Bond Canadian Institute for Theoretical Astrophysics, University of Toronto

Cosmic history: what is U made of?

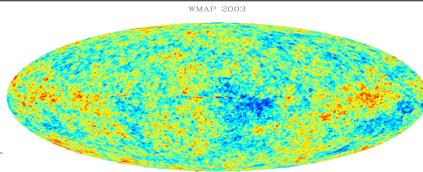
How Structure in the Universe Arose:

Inflation & the Cosmic Web

CMB & Λ CDM, $x = \Lambda + \text{tilt}$,

status@Jan09

is there a y to x?@Jan12

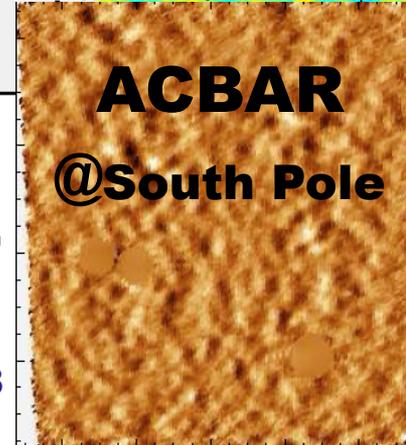
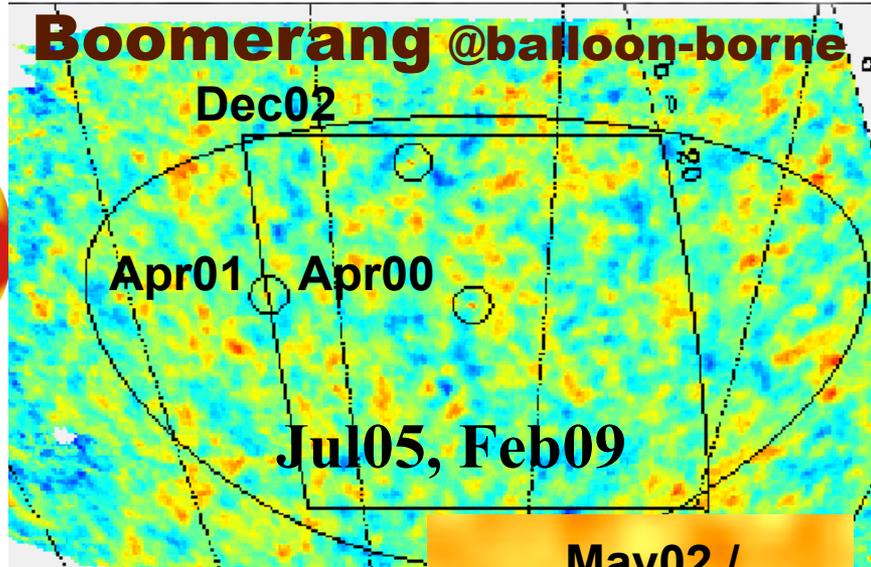
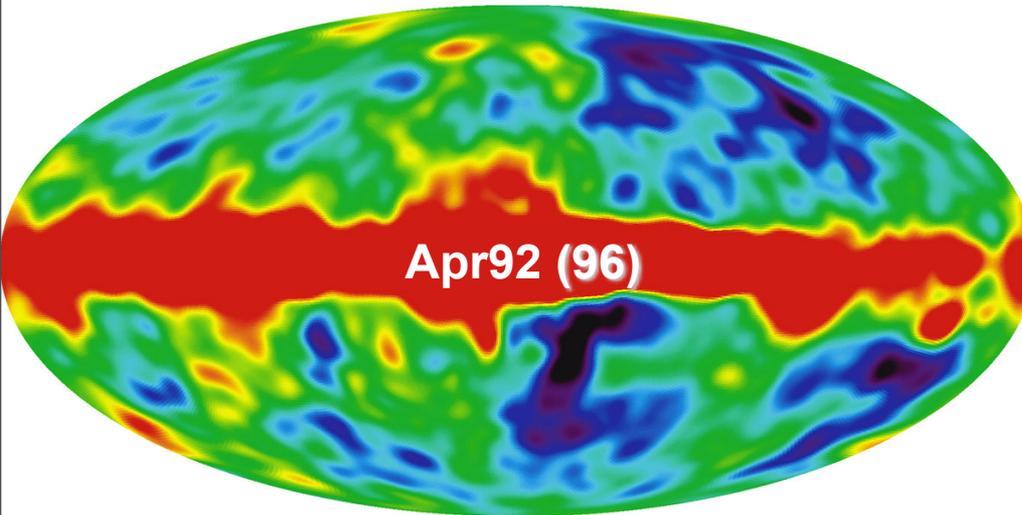


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COBE Nobel+Gruber 2006

13.65 -0.00038 billion years ago



Cosmic history: what is U made of?
How Structure in the Universe Arose:

Inflation & the Cosmic Web
CMB & Λ CDM, $x = \Lambda + \text{tilt}$,
status@Jan09

is there a y to x?@Jan12

Dec02,
Oct06,
Jan08,
Sept08

ACBAR

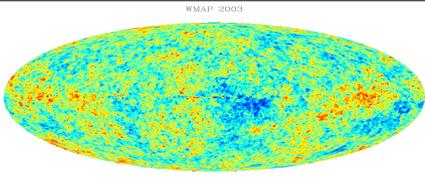
@South Pole

May02 /
Feb04

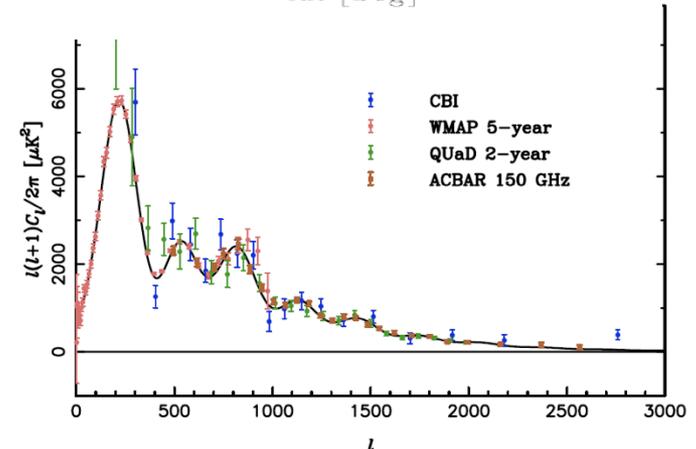
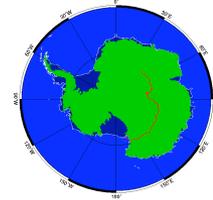
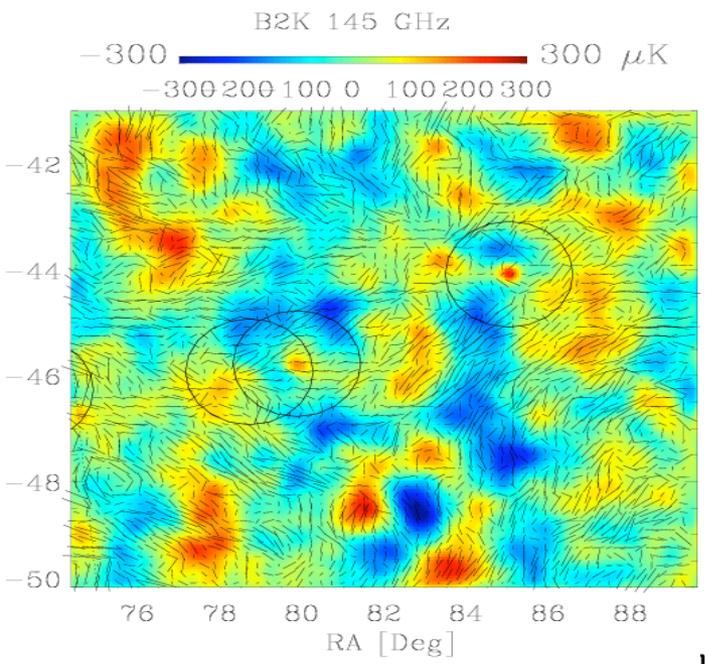
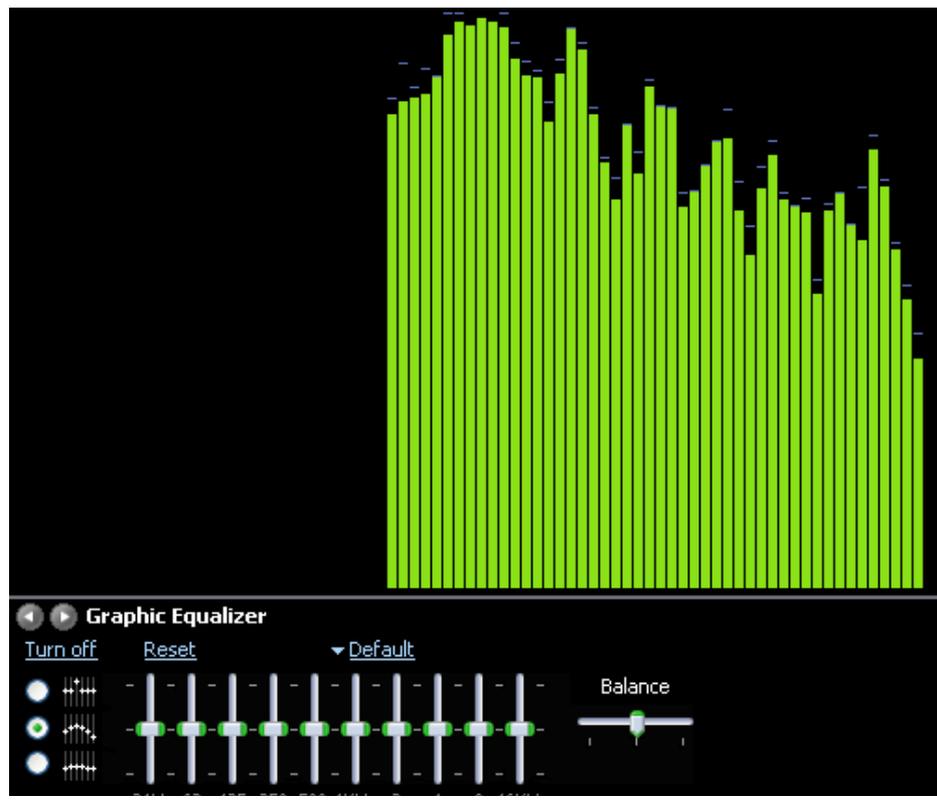
Sept04/05 Jan09

CBI: Cosmic
Background Imager
Atacama, Chile

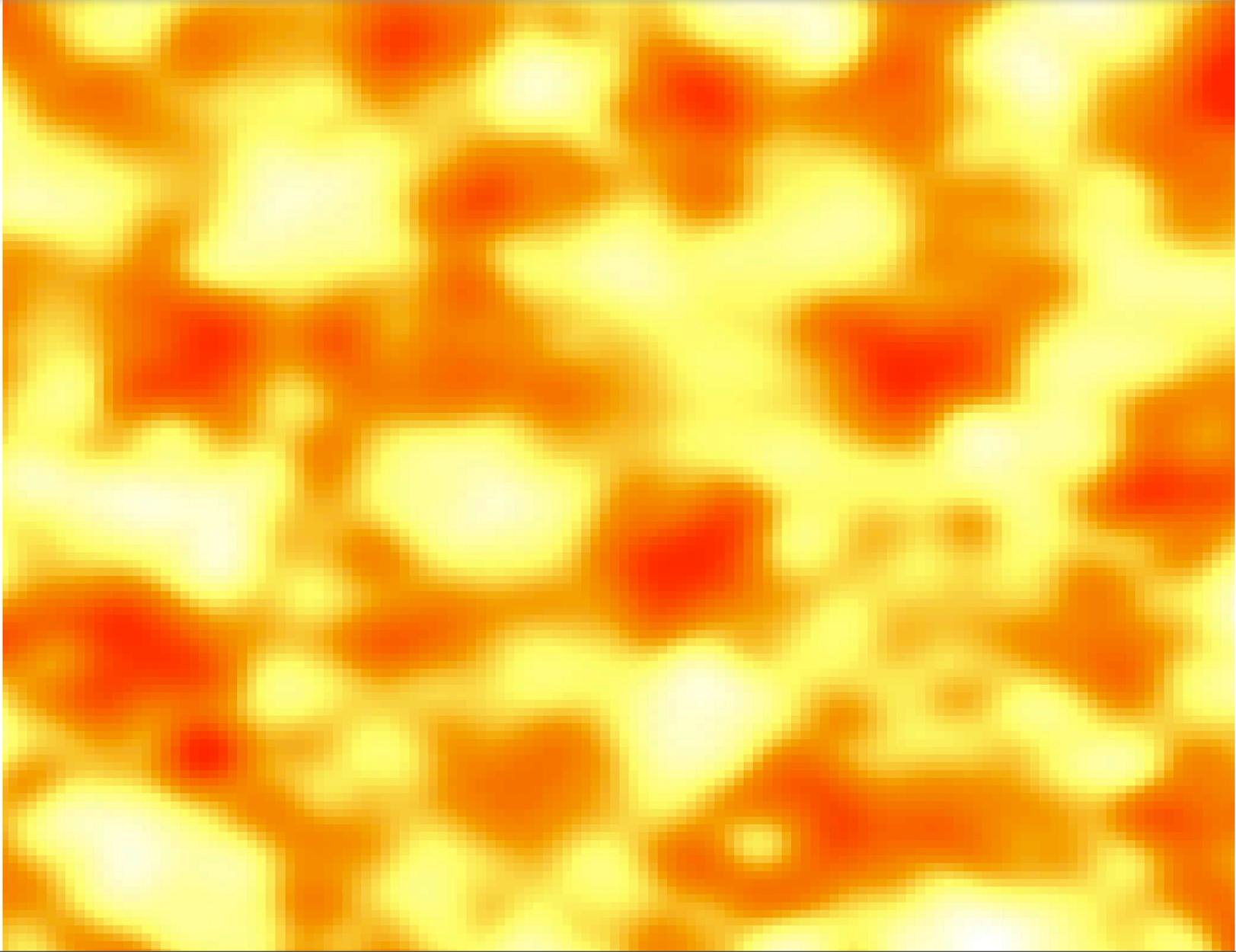
@5040m



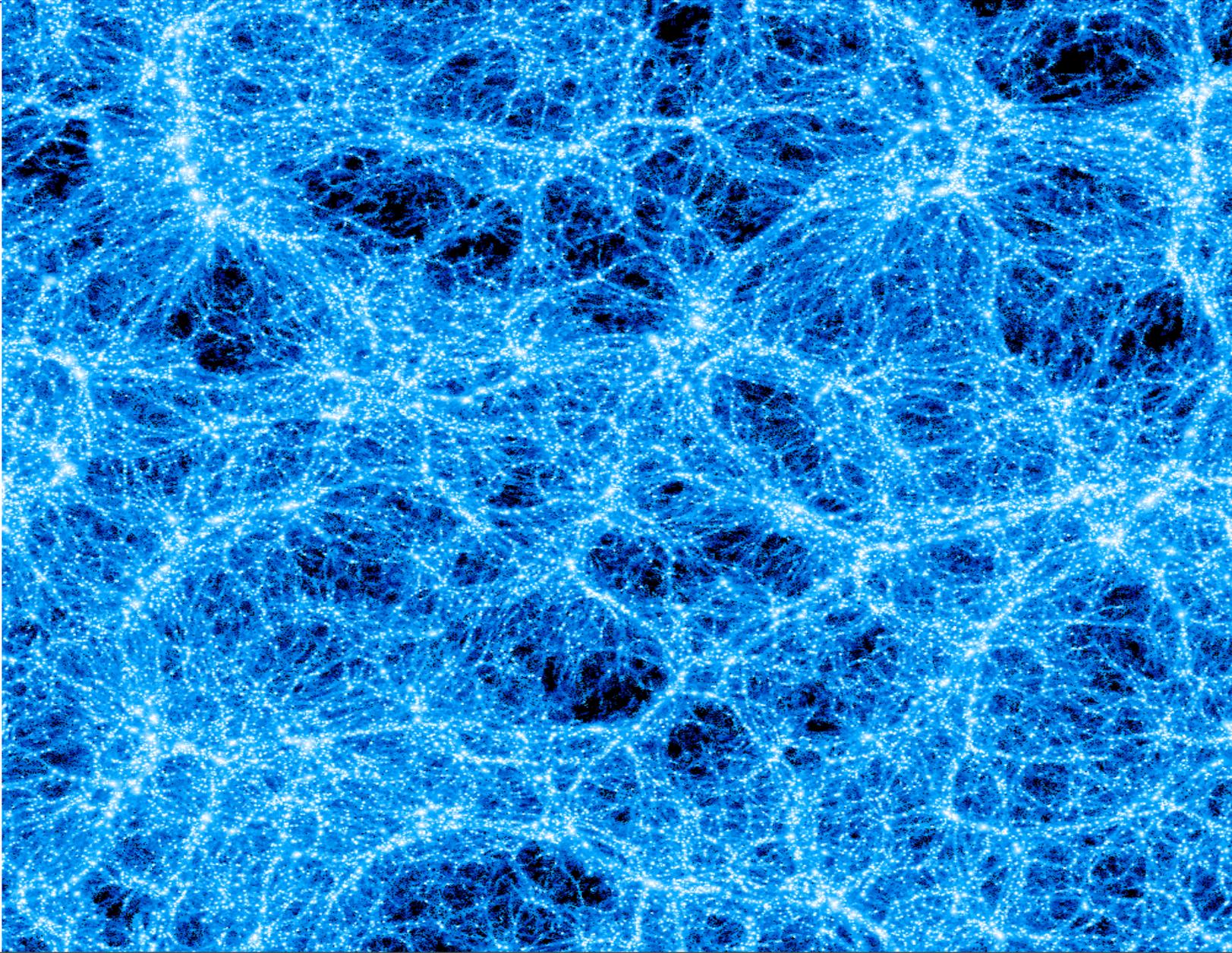
13.65 - 0.00038 billion years ago
Boom05 deep Jul05, Feb09



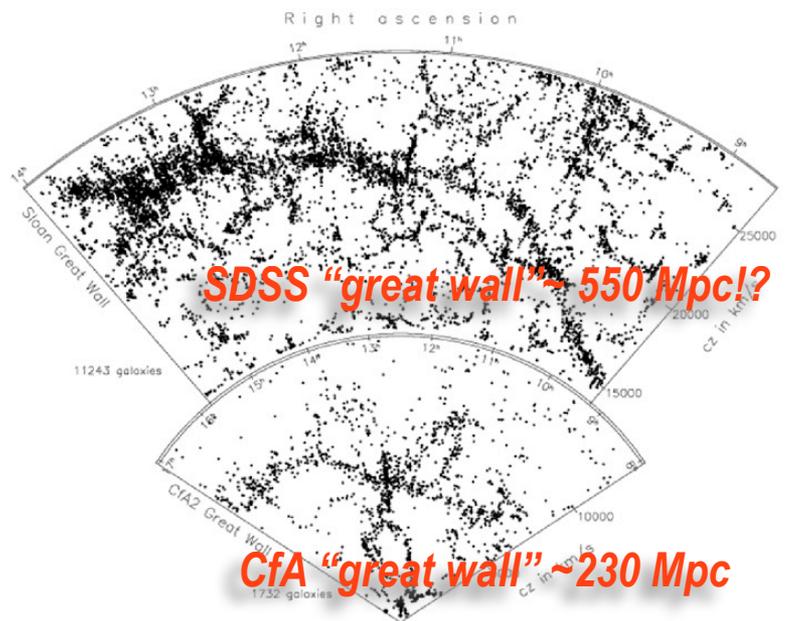
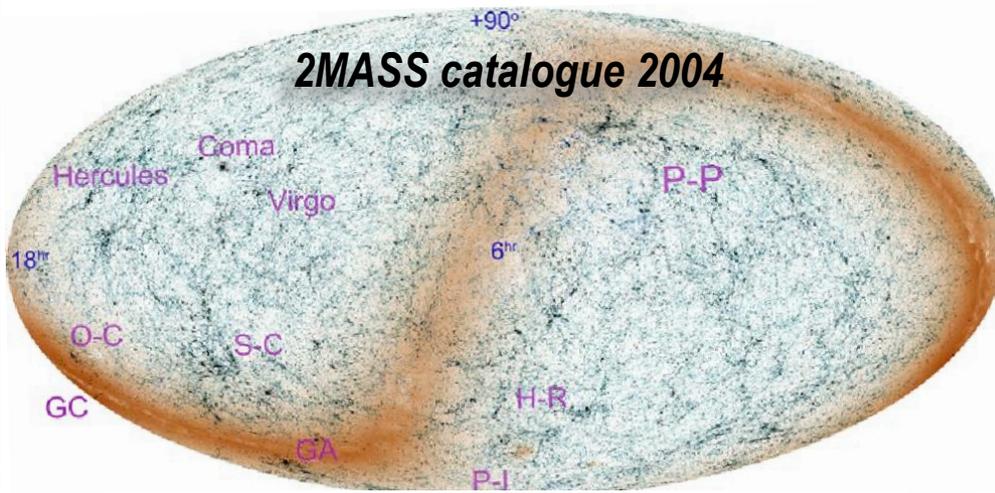
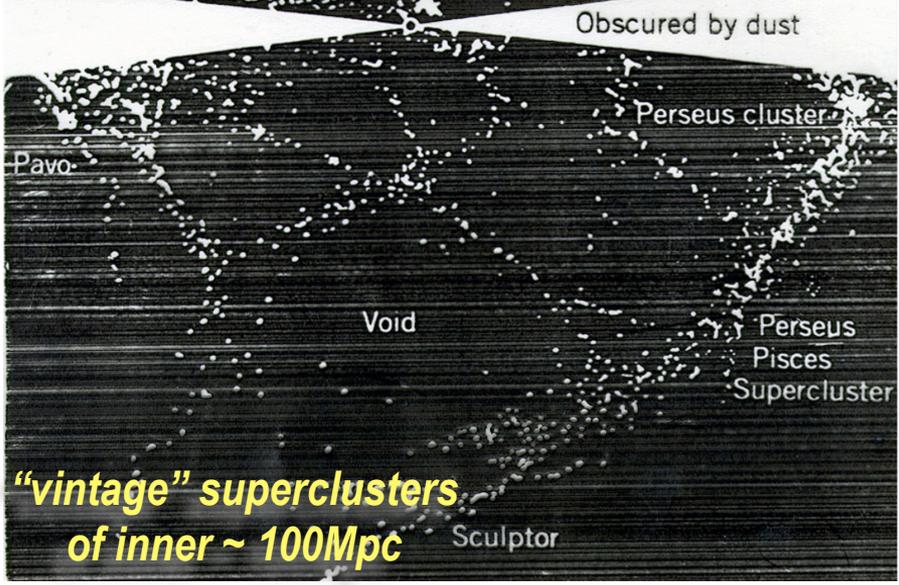
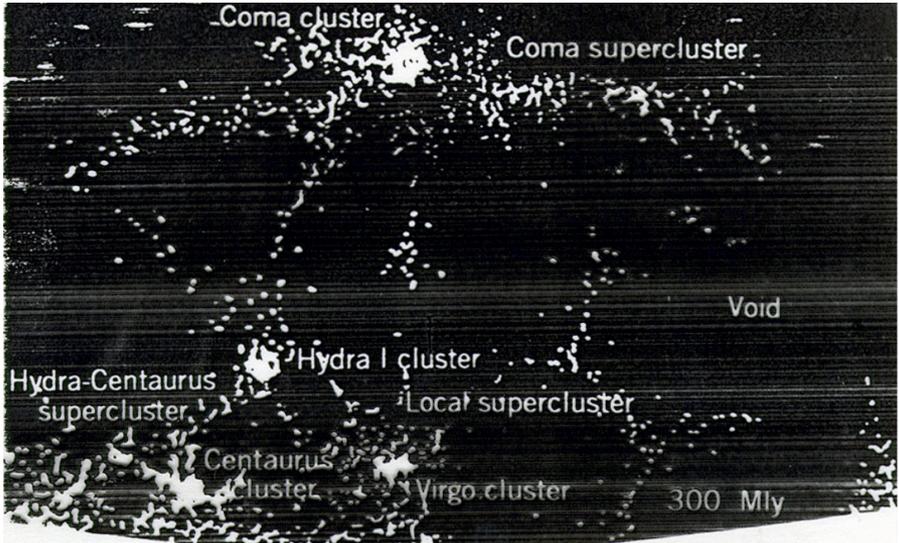
nonlinear Gas & Dark Matter Structure in the Cosmic Web the cluster/gp web “now”, the galaxy/dwarf system “then”



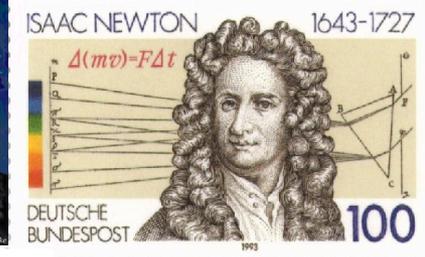
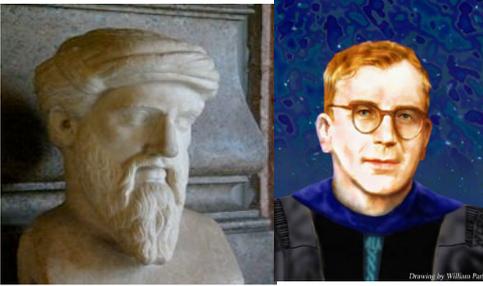
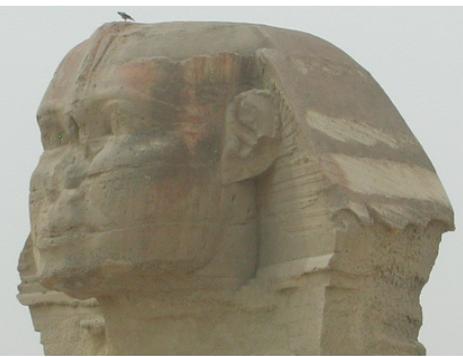
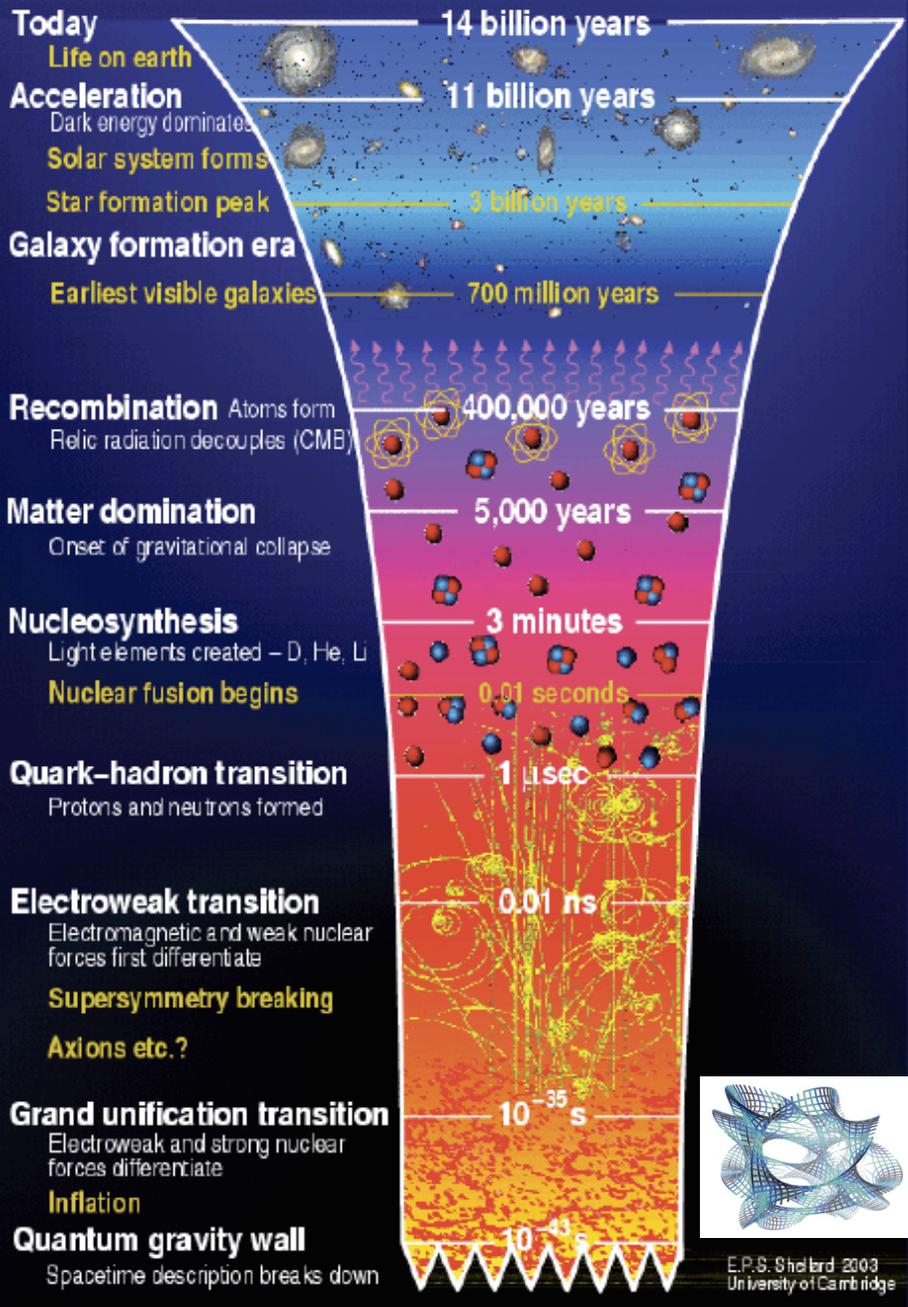
nonlinear Gas & Dark Matter Structure in the Cosmic Web the cluster/gp web “now”, the galaxy/dwarf system “then”



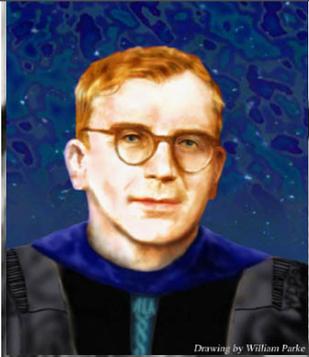
Cosmic Web & Superclustering: a natural consequence of the gravitational instability of a hierarchical Gaussian random density field



IT from BIT



*the Meaning
may change
but the Facts
will remain*



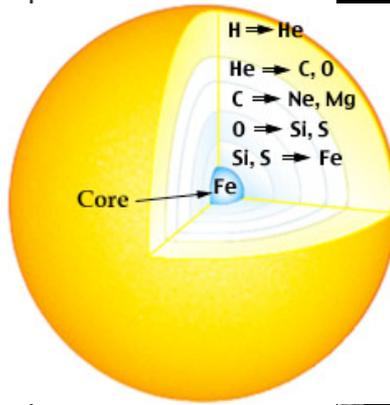
Drawing by William Parke



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**

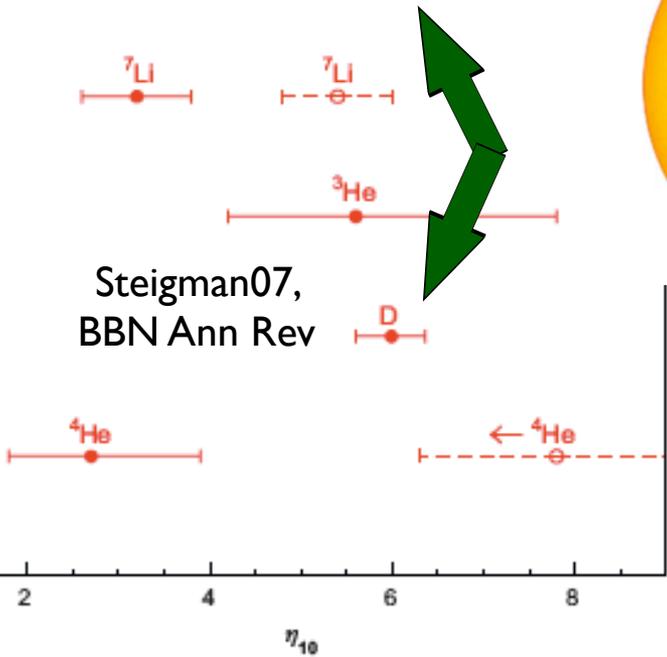
Baryometers

CMB/LSS
↔



Nobel Prize 84
Willy Fowler + Chandrasekhar

Steigman07,
BBN Ann Rev



$$\eta_{10} \equiv 10^{10} (n_B/n_\gamma) \equiv 274 \Omega_B h^2$$

	January 2000	January 2002	June 2002	January 2003	March 2003
$\Omega_b h^2$	$0.0339^{+0.0443}_{-0.0246}$	$0.0222^{+0.0025}_{-0.0021}$	$0.0221^{+0.0024}_{-0.0020}$	$0.0221^{+0.0023}_{-0.0018}$	$0.0233^{+0.0013}_{-0.0013}$

$$0.0223 \pm 0.0007$$

$$0.0226 \pm 0.0006 \text{ wmap3+acbar+cbi+... LSS}$$

$$\mathbf{0.0233 \pm 0.0005 \text{ wmap5+acbar+cbi+b03+.+WL+LSS+SNI+Lya}}$$

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extra-“ordinary” matter

Fermilab's

Primordial

SOUP

DIRECTIONS
Heat ingredients to 3,000,000,000,000,000 degrees, stirring occasionally if you wish.

If allowed to cool for 14 billion years, this product will become the atoms that make up our known universe.

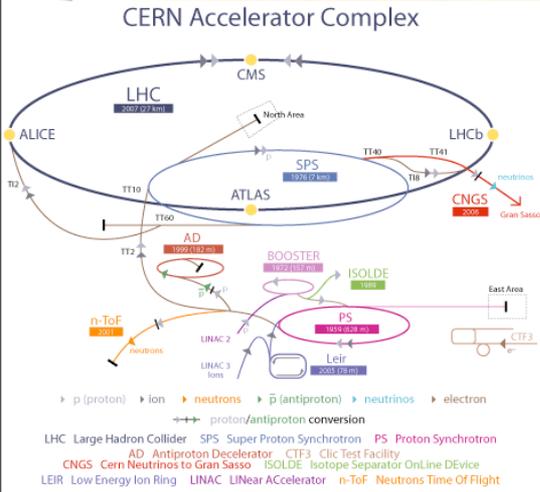
CAUTION:
Contents are extremely dense and are under enormous pressure.

INGREDIENTS

Quarks	56%
Force Carriers	29%
Electron-like Particles	9%
Neutrinos	5%
Higgs Bosons	1%

INSPECTED BY U.S. Department of Energy

Provides 100% of the minimum daily requirements for a healthy developing and expanding known universe.



Galileo's Accelerator

LHC “first light” 08.9 09.7
 @CERN’s “cosmic” accelerator

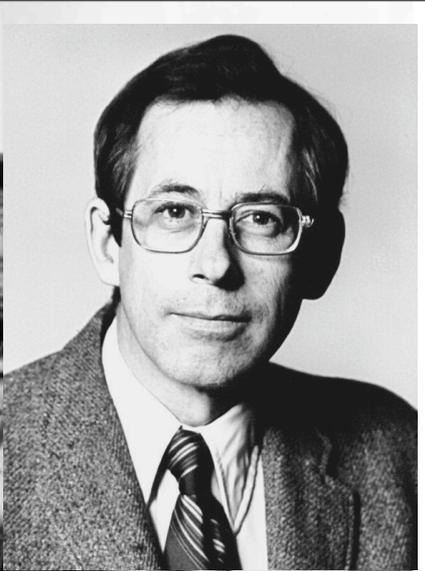
what is mass?

dark matter

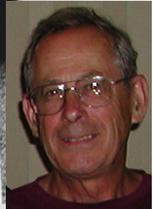
antimatter

asymmetry

extra dimensions



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**

Delta T over Tea Toronto May 1987: first dedicated CMB conference, exptalists+theorists, primary+secondary $\Delta T/T$

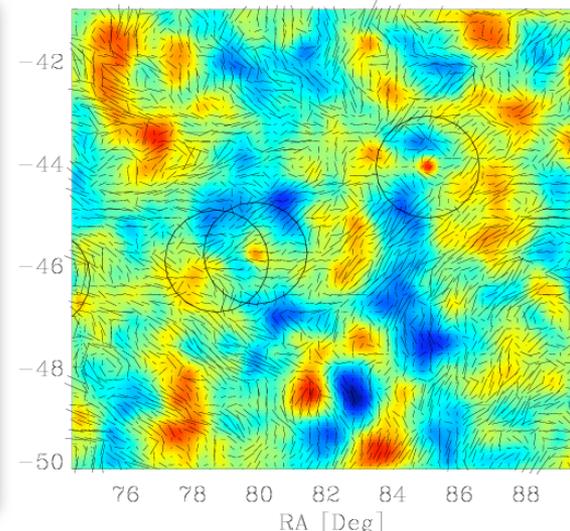
Primary Cosmic Microwave Background Radiation ~ a statistically isotropic all-sky GRF on the 2-sphere $C_L = \langle |\Delta T(LM)|^2 \rangle$ with target C_L shapes

A tentative list of topics organized according to angular scale, with theory and observation intertwined, is:

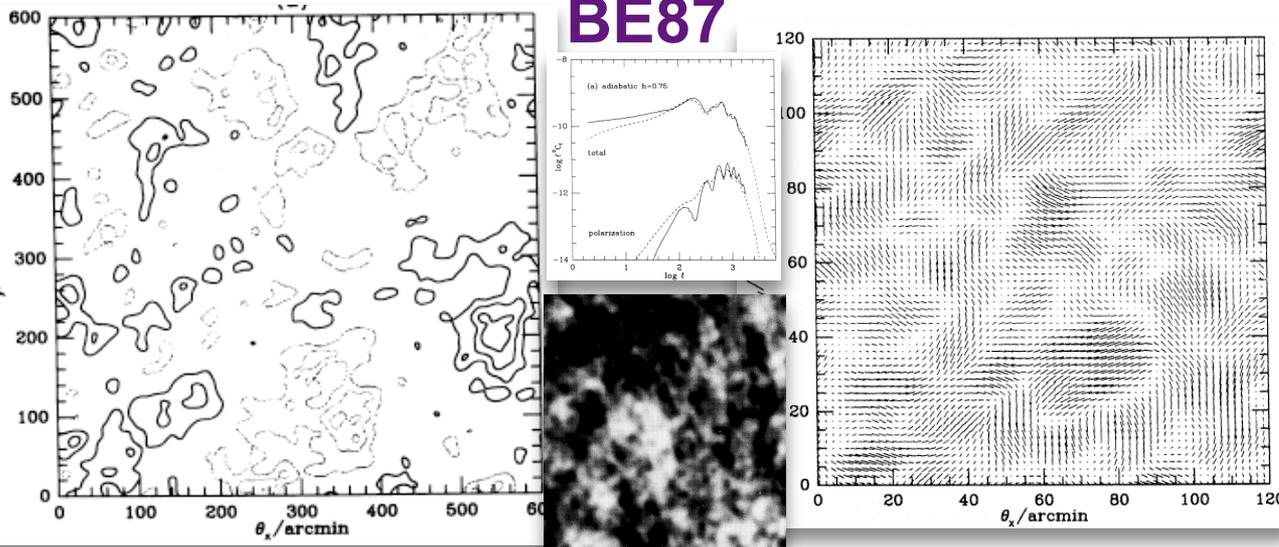
- very small angle anisotropies - VLA results, secondary fluctuations via the Sunyaev-Zeldovich effect, primeval dust emission, and radio sources
- small angle anisotropies - current results, optimal measuring strategies, statistical methods for small signals in larger noise, which universes can we rule out, the reheating issue, future detectors and techniques, **CMB map statistics, polarization**
- intermediate and large angle anisotropies - $5^\circ - 10^\circ$ results, future experiments at $\sim 1^\circ$, COBE and other large angle analyses, theoretical $C(\theta)$'s and their angular power spectra, Sachs-Wolfe effect in open Universes, the isocurvature CDM and baryon stories, $\Delta T/T$ from gravitational waves, the cosmic string story.

Boom05 deep

-300 200 100 0 100 200 300 μK



BE87



DELTA T OVER TEA WORKSHOP

1-2 May, 1987
Toronto, Canada

Sponsored by

The Canadian Institute for Theoretical Astrophysics and
The Canadian Institute for Advanced Research

Topics

*Present and Future Experiments of
Cosmic Microwave Background Anisotropies and
Their Theoretical Interpretation
on very small ($< 1'$), small ($1' - 1^\circ$),
intermediate ($1^\circ - 10^\circ$) and large ($> 10^\circ +$ multipole
angular scales*

Contact: Dick Bond

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60 St George St., Toronto, Ontario, Canada, M5S 1A1

Phone (416) 978 6879 or 6874

Bitnet BOND@UTORPHYS

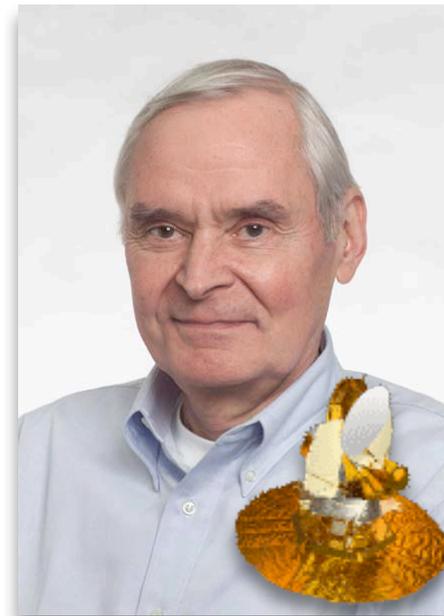
Organizers: J.R. Bond (CITA), D.T. Wilkinson (Princeton)

Delta T over Tea Workshop Participants

Bennett, Chuck, Goddard
Birkinshaw, Marc, Harvard *
Bond, Dick, CITA
Boughn, Steve, Haverford
Boynton, Paul, University of Washington
Cannizzo, John, McMaster
Carlberg, Ray, York
Cheng, Ed, MIT
Couchman, Hugh, CITA
Cottingham, David, Princeton
Daly, Ruth, Boston U
Davies, Rod, Jodrell Bank
Davis, Marc, Berkeley
Dragovan, Marc, Bell Labs
Dyer, Charles, U of Toronto
Efstathiou, George, Cambridge
Fitchett, Mike, CITA
Fomalent, Ed, NRAO
Gorski, Chris, Berkeley
Gulkis, Sam, Caltech
Gush, Herb, UBC
Halpern, Marc, UBC
Ip, Peter, U of Toronto
Juszkiewics, Roman, Berkeley
Henriksen, Dick, Queens
Kaiser, Nick, Cambridge
Kellerman, K, NRAO
Kronberg, Phil, Toronto
Lang, Andrew, Berkeley
Lasenby, Anthony, Cambridge
Lawrence, Charles, Caltech
Lee, Hyung-Mok, CITA
Legg, Tom, Herzberg Institute, Ottawa
Little, Blaine, Toronto
Lubin, Phil, Santa Barbara
Matarrese, Sabino, Padova
Mather, John, Goddard
Meyer, Steve, MIT
Meyers, Steve, Caltech
Moseley, Harvey, Goddard
Nelson, Lorne, CITA
Noriega-Crespo, Alberto, CITA
Occhionero, F., Rome *
Ostriker, Jerry, Princeton
Page, Lyman, MIT
Partridge, Bruce, Haverford
Peterson, J.B., Princeton
Radford, Simon, IRAM, France
Readhead, Tony, Caltech

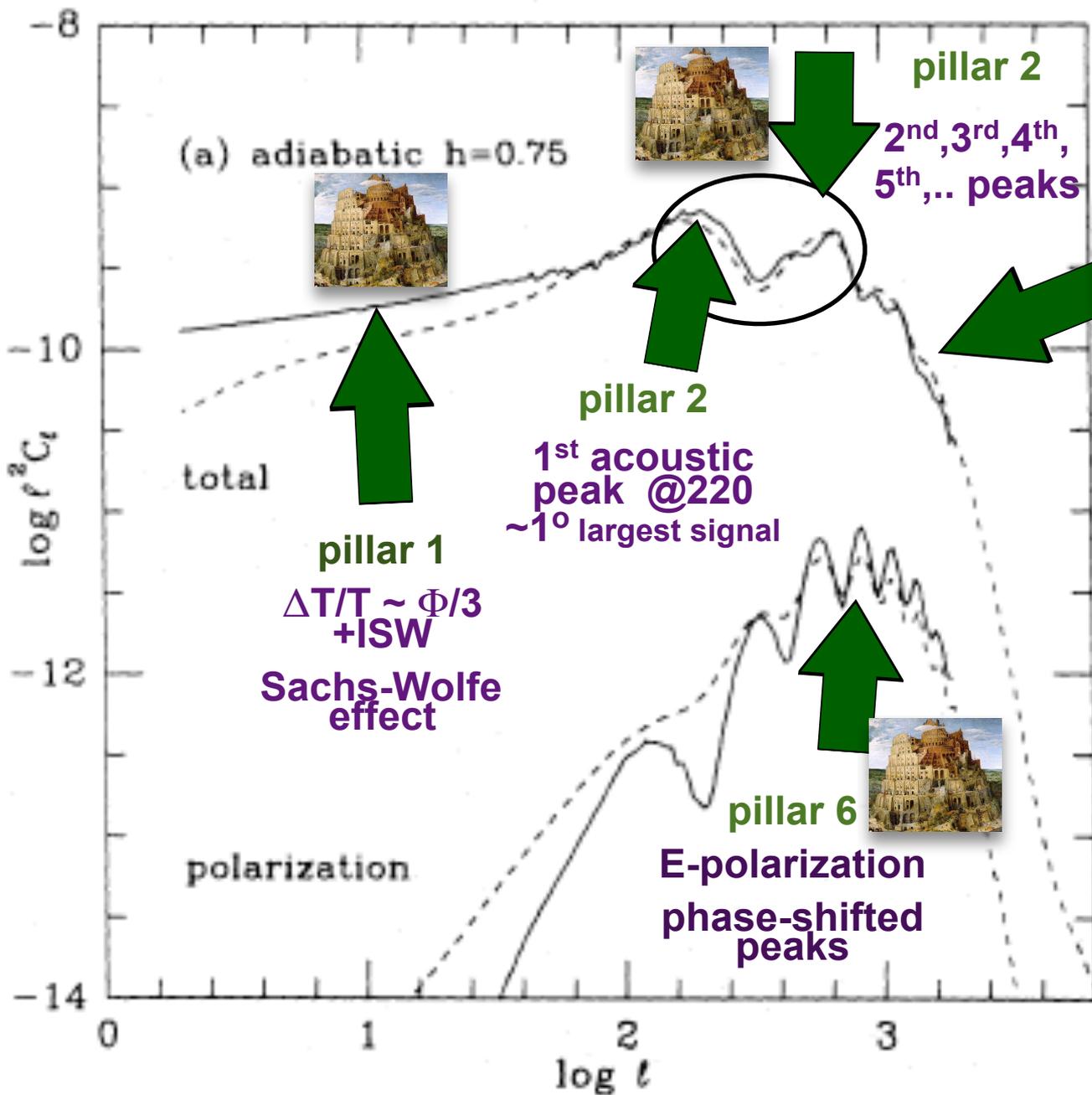
Richards, Paul, Berkeley
Salopek, Dave, Toronto
Sargent, Wal, Caltech *
Schaeffer, Bob, Goddard
Silk, Joe, Berkeley
Silverberg, Bob, Goddard
Stebbins, Albert, Fermilab
Suto, Yasushi, Berkeley
Timby, Peter, Princeton
Tremaine, Scott, CITA
Timusk, Tom, McMaster
Unruh, Bill, UBC
Vishniac, Ethan, U. Texas Austin
Vittorio, Niccolo, Rome
Wilkinson, Dave, Princeton
Webster, Rachel, Toronto

Dave Wilkinson



Wilkinson Microwave
Anisotropy Probe

the "Seven Pillars"



pillar 4

Gaussianity
 maximal
 randomness
 for given CL



pillar 5

secondary ΔT
 nonlinear
 Compton SZ
 weak lensing..

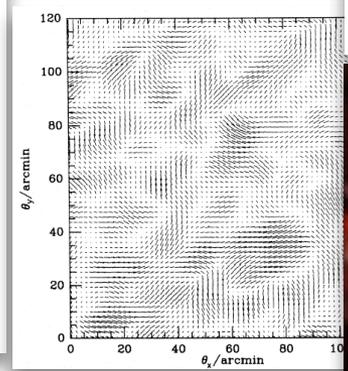


pillar 3

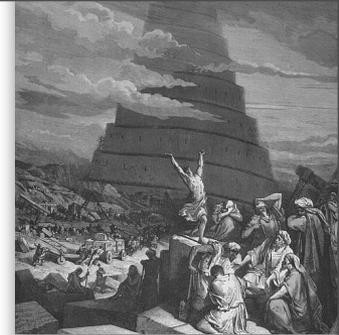


pillar 7

B-polarization
 Gravity Waves



COSMIC PARAMETERS THEN



e.g., **BBE1987** vary x in $x\text{CDM}$

for $x\text{CDM}$, predict CMB (6deg, 5min); LSS cluster-cluster, cluster-galaxy, bulk flows,

14 Gyr, $\Omega_\Lambda=0.8$, $H_0=75$, $b\sim c$,
 $50\mu\text{K}$ cf $30\mu\text{K}$ coBE, $\sigma_8\sim 0.72$

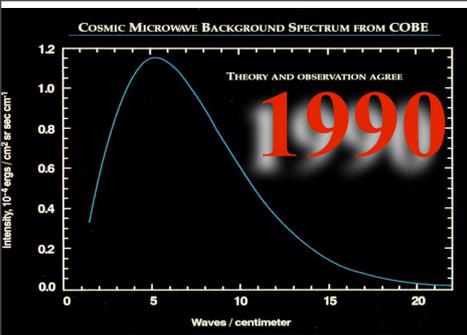
σ_8 : redshift of “galaxy formation”

X = s / H_0 / Λ / Open / is / is+ad / h-c / h+ / b / b / **$\Lambda+b$** / Op+b / τ / BSI / BSI2

PREDICTIONS FOR MODELS

Parameter	OBS	CDM	C40	VAC/C	OP/C	ISO/C	ISO/AD	HOT	HC	C + B	B + C	BCV	BCO	CDM + dec	(CDM + X) ₁ ($k_s^{-1} = 300$)	(CDM + X) ₂ ($k_s^{-1} = 200$)
Ω, Ω_b, H_0											1, 0.1, 75				
$\Omega_s(\Omega_v), \Omega_{vac}$											0.1, 0.8				
b											1				
t_0 (by)	GC: 14–22 NC: 13–26											14				
$\sigma_0(R_g = 0.35)$											2.4				
z_g											1.3				
$\sigma_0(R_{cl} = 5)$											0.72				
$\langle v \rangle_c$											2.8				
$\xi_{cc}(20)$	1.5											2.2				
$\xi_{cc}(25)$	1.0											1.7				
$\xi_{cc}(30)$	0.72											1.4				
$\xi_{cc}(50)$	0.29											0.59				
$\xi_{cc}(100)$	0.08											0.36				
$\xi_{cg}(20)$	0.49											0.76				
$\xi_{cg}(25)$	0.33											0.54				
$\xi_{cg}(30)$	0.24											0.41				
$\xi_{cg}(40)$	0.14											0.26				
$\tau(R_f = 3.2)$	610 ± 50											232–1120				
$\tau(R_f = 15)$	599 ± 104											206–987				
$\tau(R_f = 25)$												186–894				
$\tau(R_f = 40)$	970 ± 300											160–771				
$\Delta T/T$ (4:5)	< 25											10				
$\times 10^6$ (6°)	< 48											25				



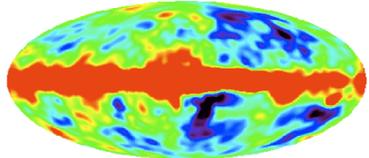
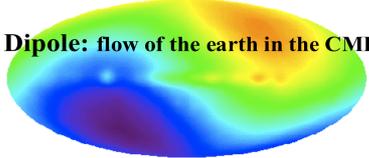


CMB

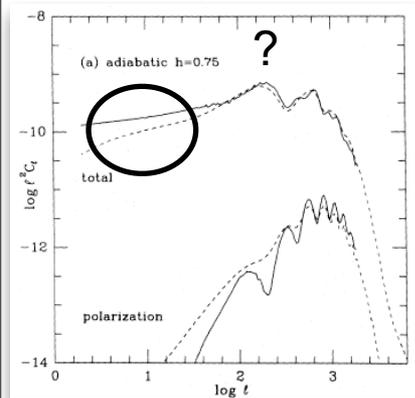
1992/96

Nearly Perfect Blackbody
 $T = 2.725 \pm .001$ K COBE/FIRAS

Dipole: flow of the earth in the CMB



COBE/DMR:
 CMB + Galactic @7°



100
80
60
40
20
0

BJK "radically compressed bandpowers" an up & down in power offset log-normal plus correlations

COBE, FIRS, +

SK95, **1998**

max, msam, +

flat

CAT

ovro

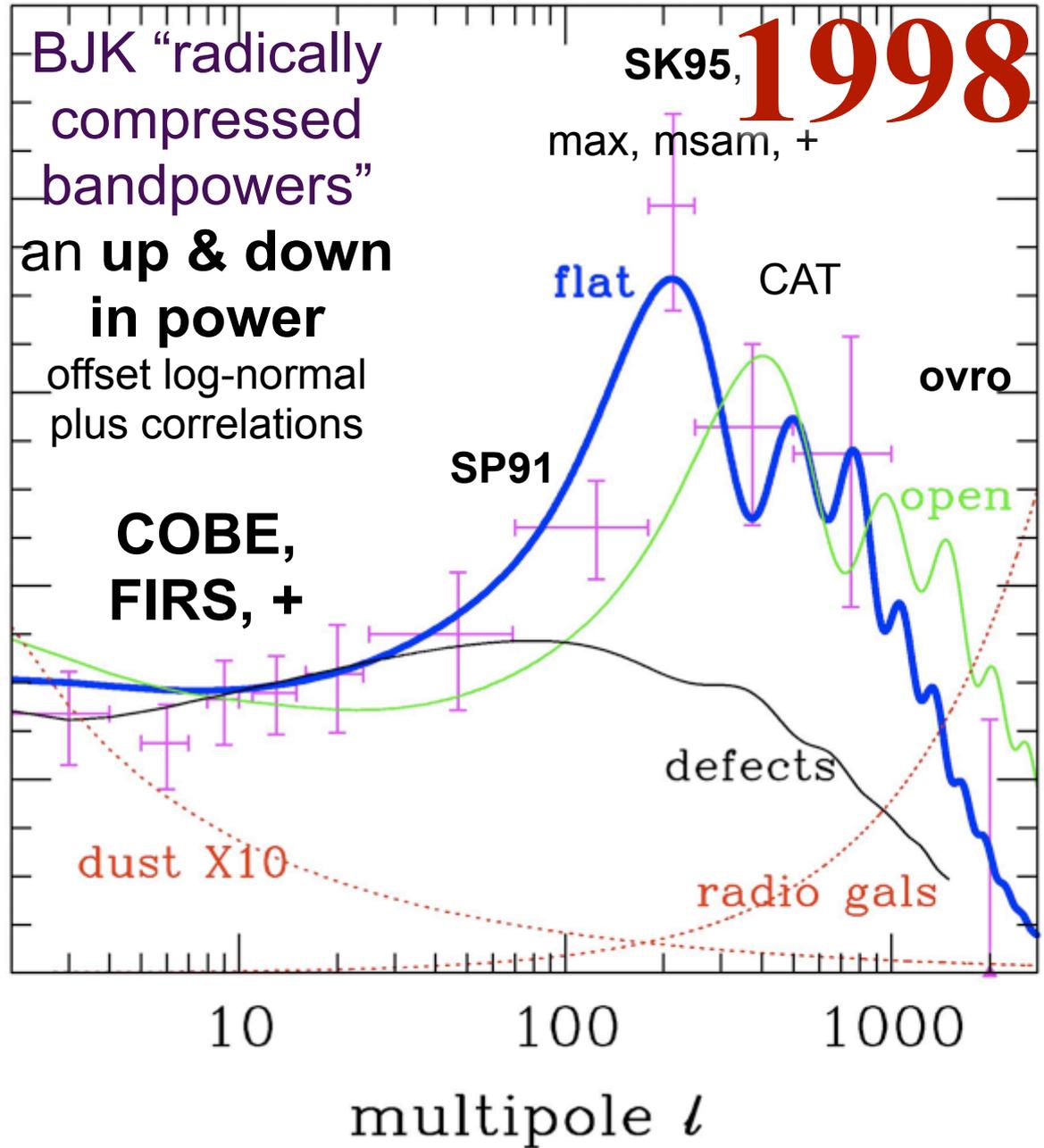
open

defects

dust X10

radio gals

multipole l



CMB CMB ⊕ LSS
 ↓ ↓

$$n_s \approx 1 \pm .05$$

nearly SCALE INVARIANT FLUCTUATIONS

CMB ⊕ LSS SNIa high z CLUSTERS
 ↓ ↓ ↓
 oCDM << ΛCDM

$\Omega_{cdm} \sim .3$
 $\Omega_b \sim .04$
 $H_0 \sim 65-70$
 $t_0 \sim 12-14 \text{ Gyr}$

$$\Omega_{\Lambda} \approx \frac{2}{3} \quad (\underline{x}, t)$$

vac
 PLATE TIME

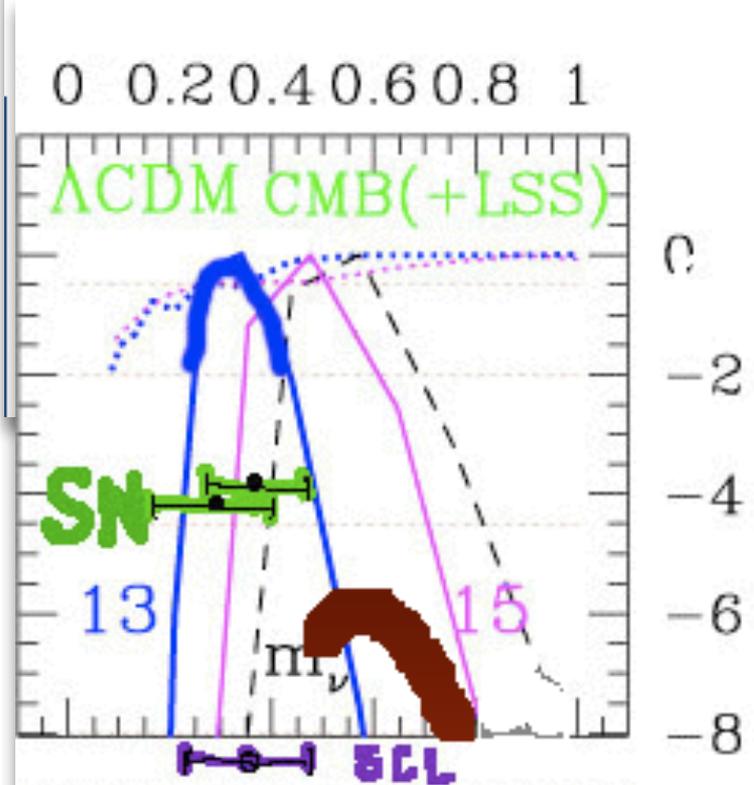
$\Omega_{\nu} \sim .0014$
 $\left(\frac{m_{\nu}}{0.07 \text{ eV}}\right)^2$ INFLATION is NOW
 $\rho \sim \text{milli eV}$

vintage 98 conclusions

B+Jaffe '96, '98 (13 Gyr/ t_0)

$\Omega_{\Lambda} \approx 2/3 \pm .07$ +LSS

$n_s =$
 $.98 \pm .07$
 $.96 \pm .06$



BOOM

2000

TOCO, Boom test 1999

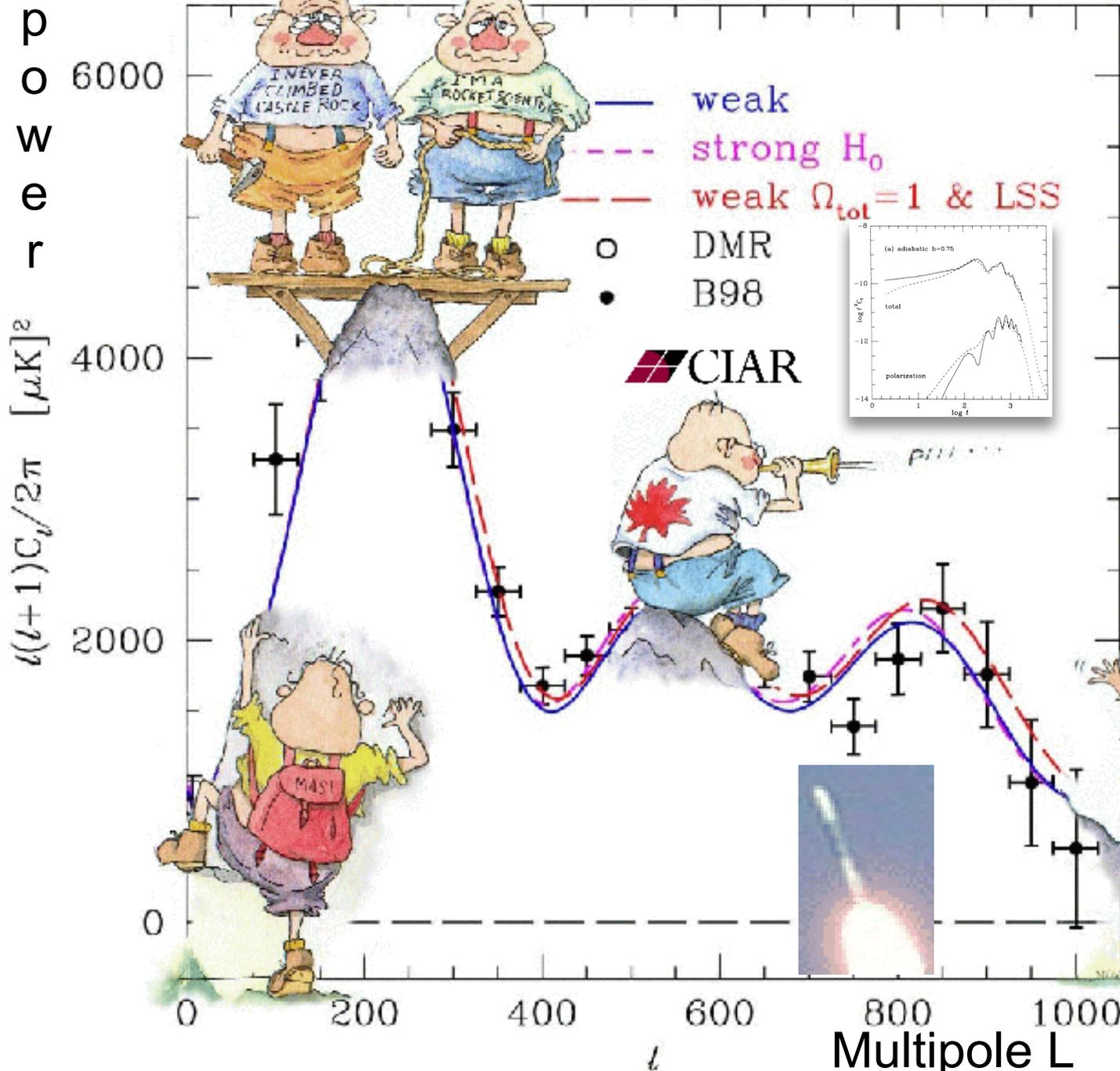
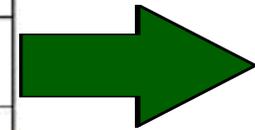
Maxima 2000

2001

CBI, ACBAR

Boom2003.1

VSA



+DASI 2001

2002

NSF/Caltech
/CITA/CIAR

May 23, 2002

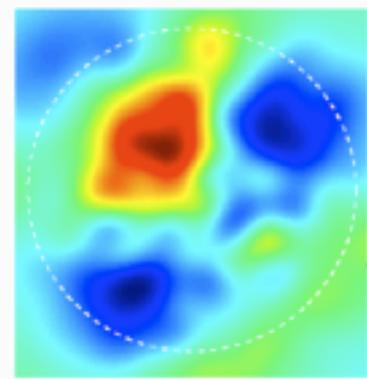
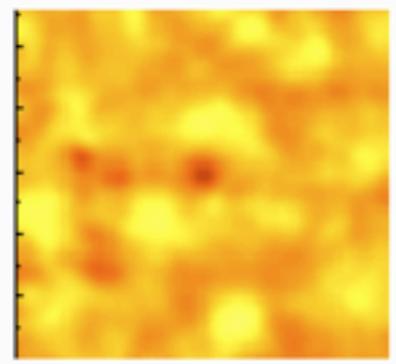
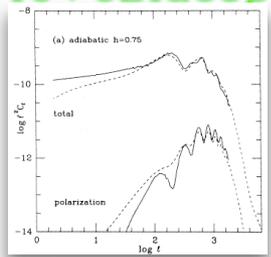
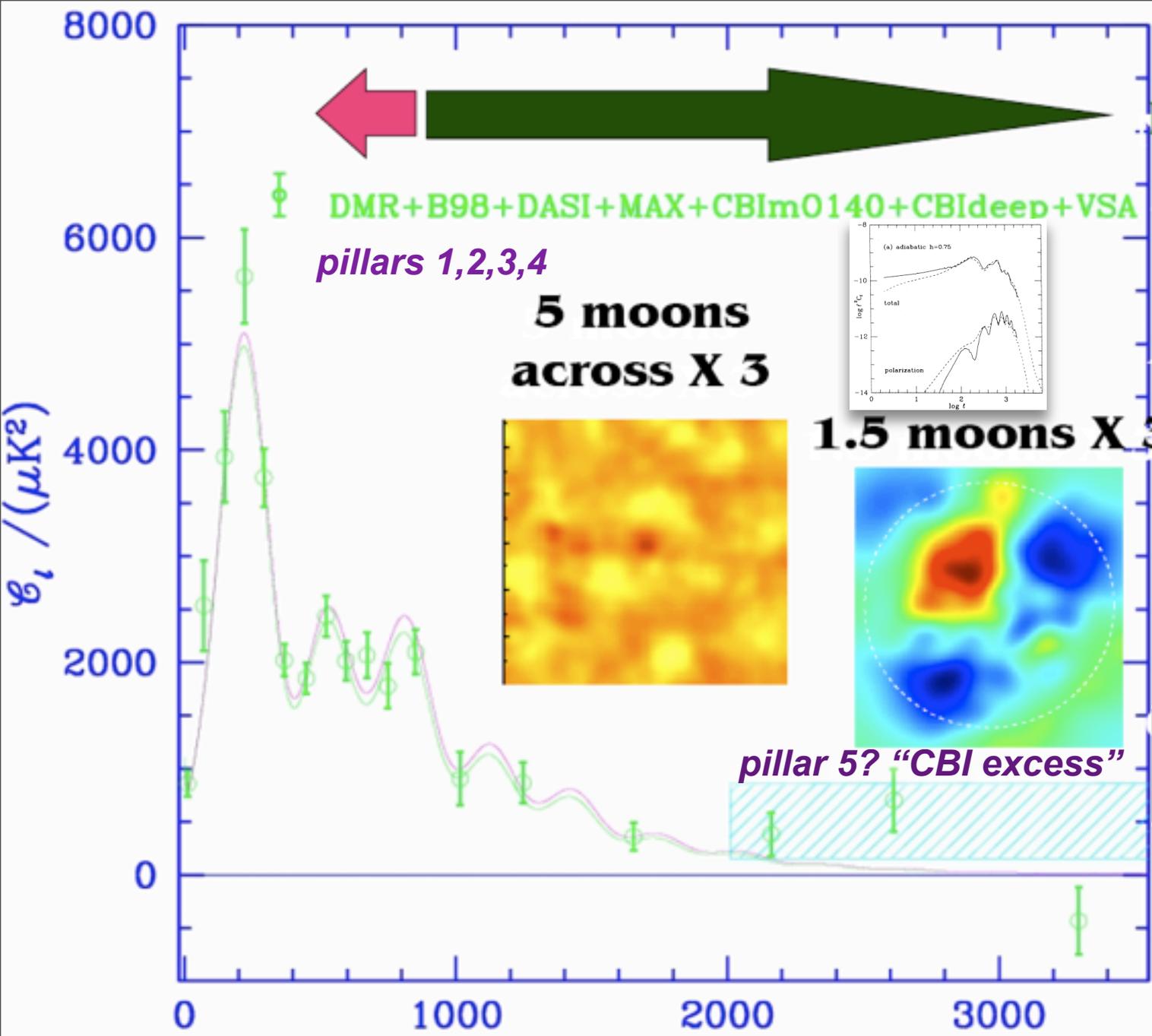
AAS Jun02

Grand
unified
spectrum

Adds

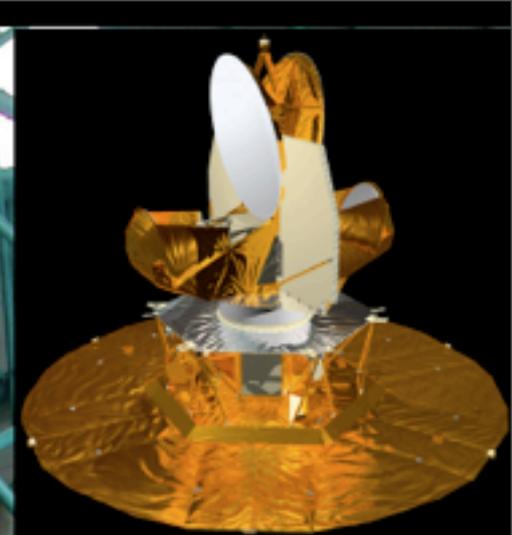
CBI mosaic
+ CBI deep

+ VSA



pillar 5? "CBI excess"

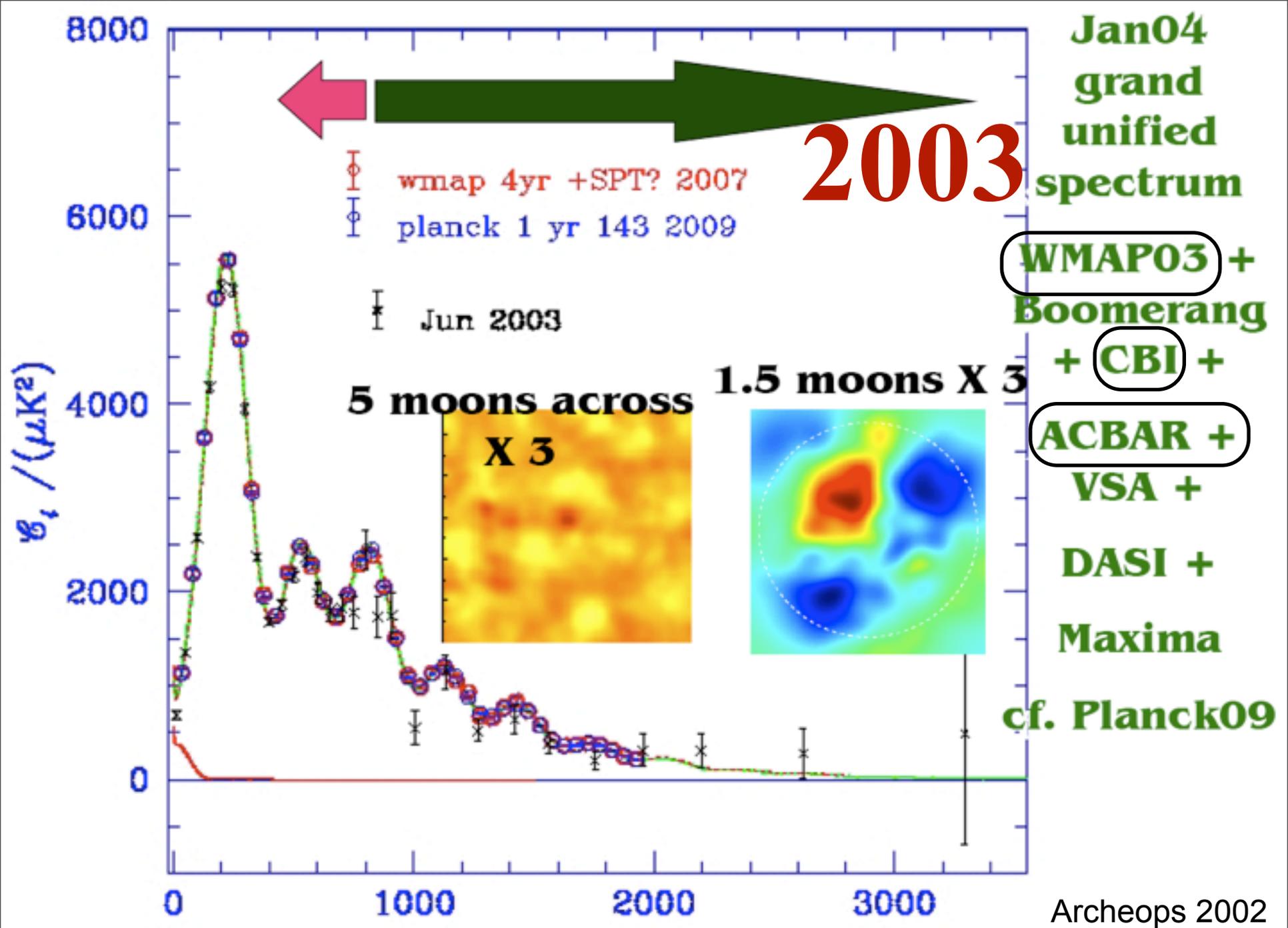
WMAP launch 2001.6

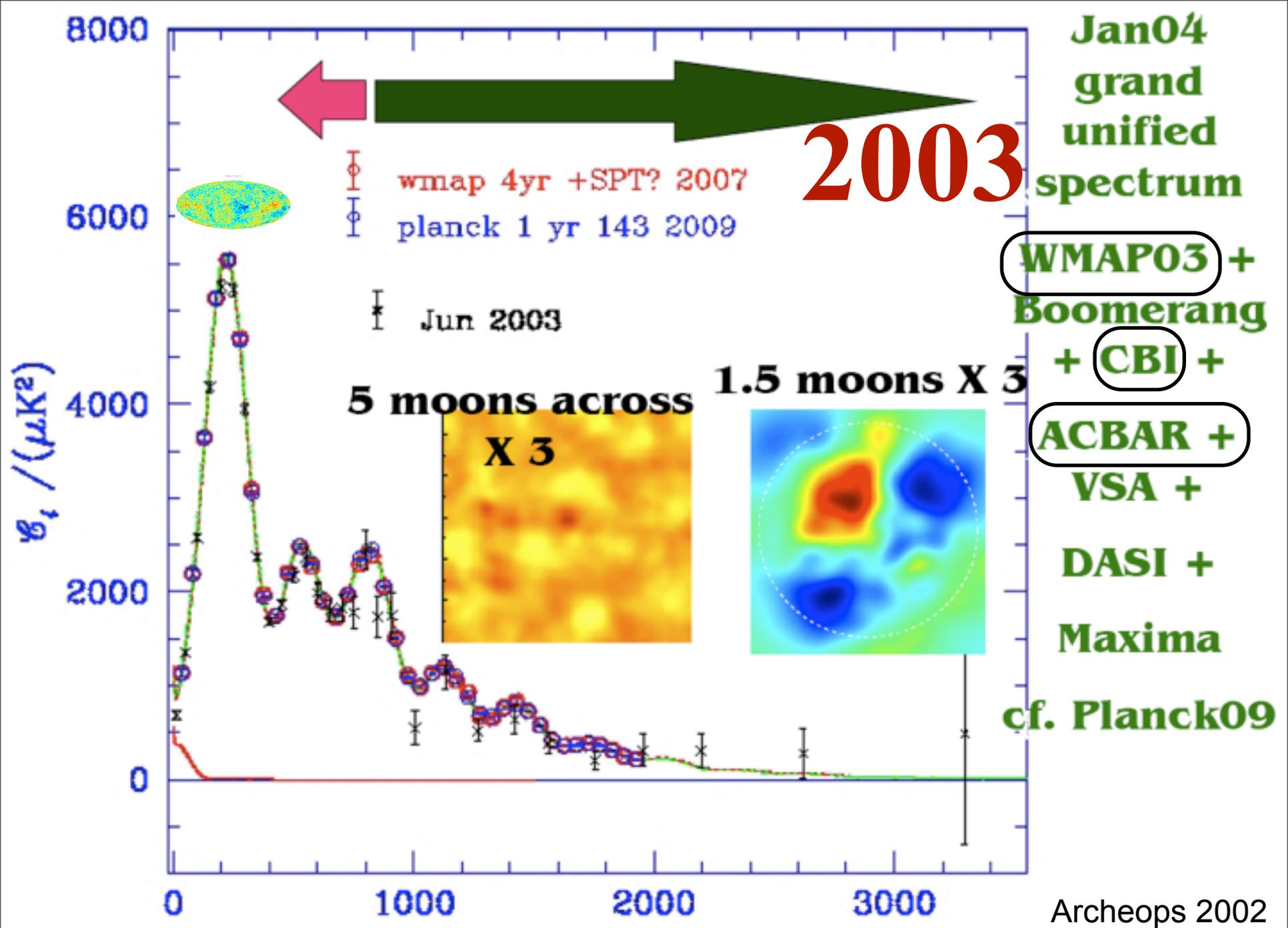


Text

Dave Wilkinson

Rashid Sunyaev





CMB NOW 2009.1

$$\langle |\Delta T_{(LM)}|^2 \rangle L(L+1)/2\pi$$

$l(l+1)C_l/2\pi$ [μK^2]

-  CBI
-  WMAP 5-year
-  QUaD 2-year
-  ACBAR 150 GHz



pillars 1,2,3

1st 2nd 3rd 4th 5th peaks
& damping tail



pillar 5? "CBI excess"



COBE regime



pillar 4: as random as can be given this spectrum

0 500 1000 1500 2000 2500 3000

l

CMB NOW 2009.1

$$\langle |\Delta T_{(LM)}|^2 \rangle L(L+1)/2\pi$$

$l(l+1)C_l/2\pi$ [μK^2]

-  CBI
-  WMAP 5-year
-  QUaD 2-year
-  ACBAR 150 GHz



pillars 1,2,3

1st 2nd 3rd 4th 5th peaks
& damping tail



pillar 5? "CBI excess"



COBE regime

0



500



1000

1500

2000

2500

3000

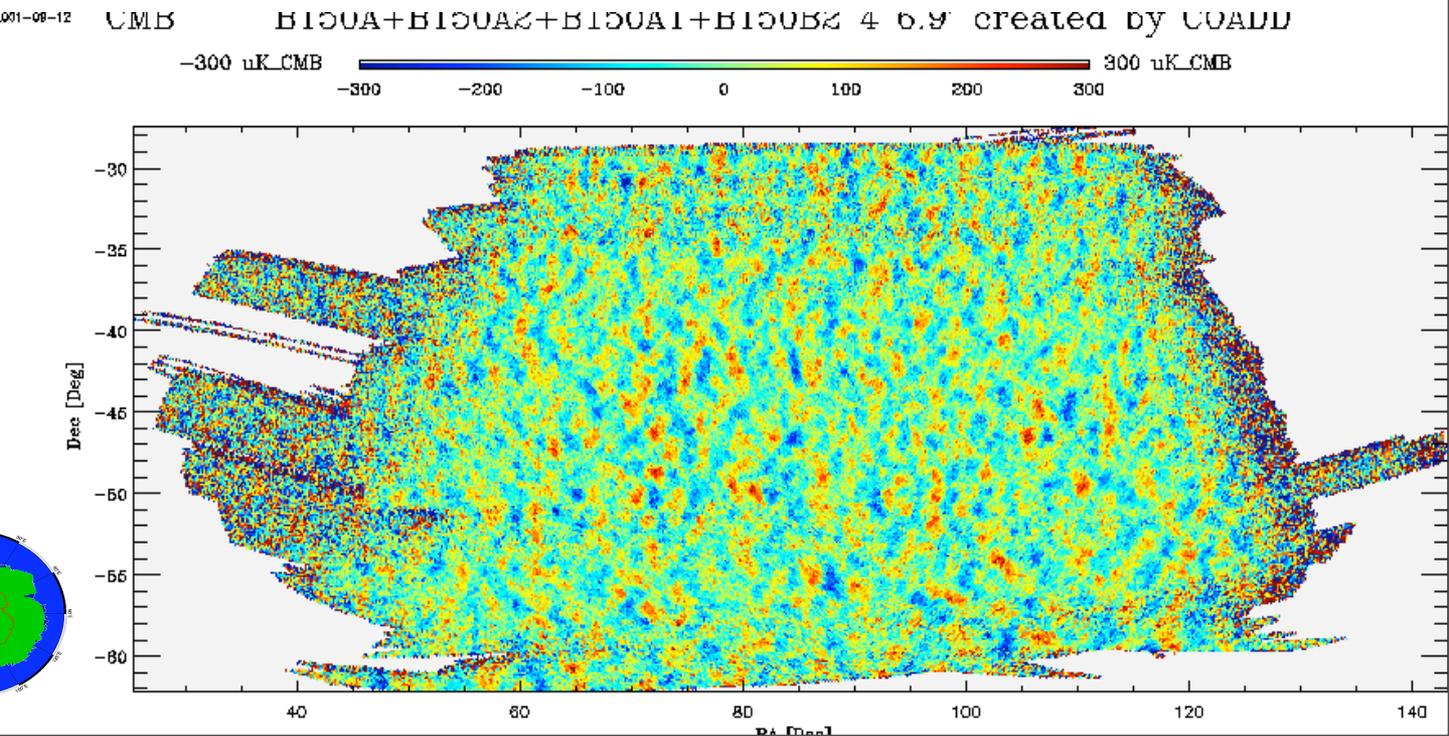
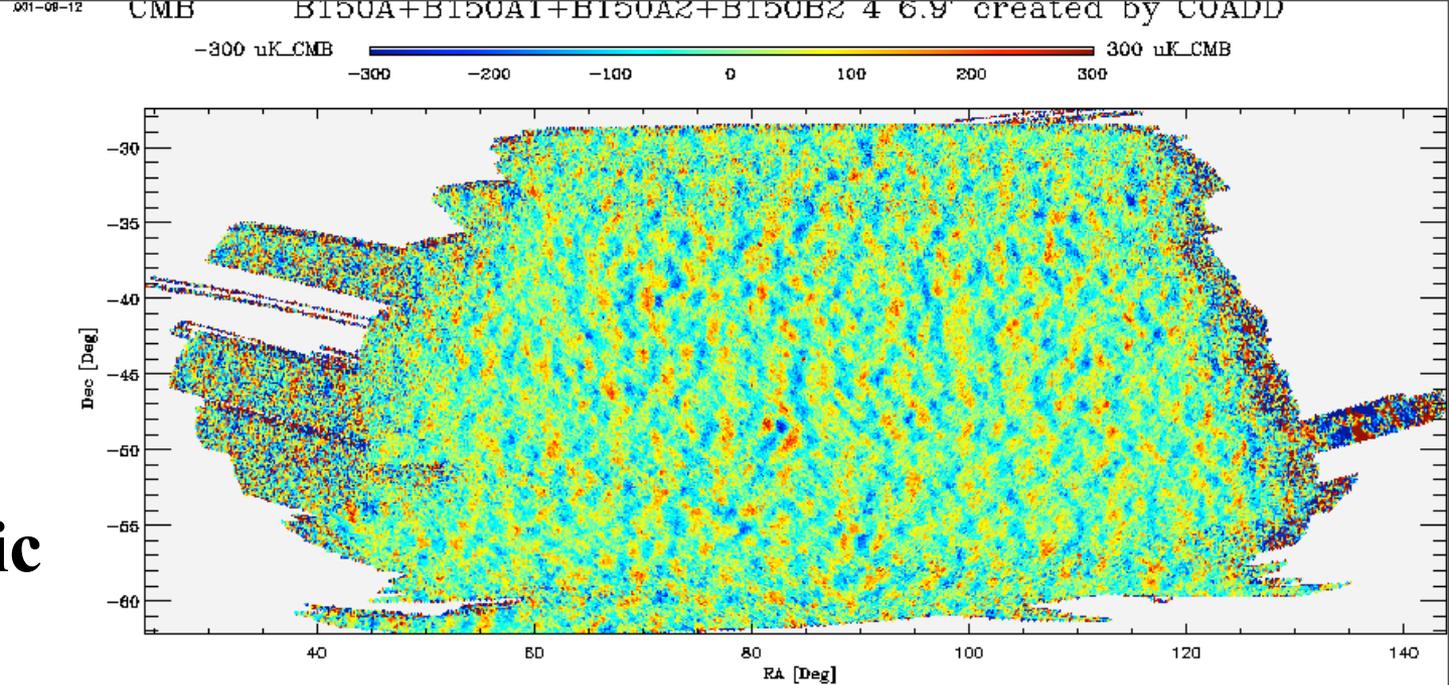
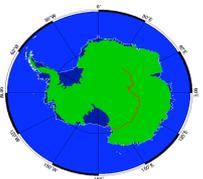
l

pillar 4: as random as can be given this spectrum

Boomerang
@150GHz is
(nearly)
Gaussian:
Simulated vs
Real

thermodynamic
CMB

temperature
fluctuations
2.9% of sky
 $\Delta T \sim 30$ ppm





**I
N
F
L
A
T
I
O
N**

**the nonlinear
COSMIC WEB**

Primary Anisotropies

- Tightly coupled Photon-Baryon fluid oscillations
- viscously damped
- Linear regime of perturbations
- Gravitational redshifting

Decoupling LSS

17 kpc
(19 Mpc)

Secondary Anisotropies

- Non-Linear Evolution
- Weak Lensing
- Thermal and Kinetic SZ effect
- Etc.

$L_{\text{sound}}/k_{\text{sound}}$

z=0

reionization

z ~ 1100 redshift **z**

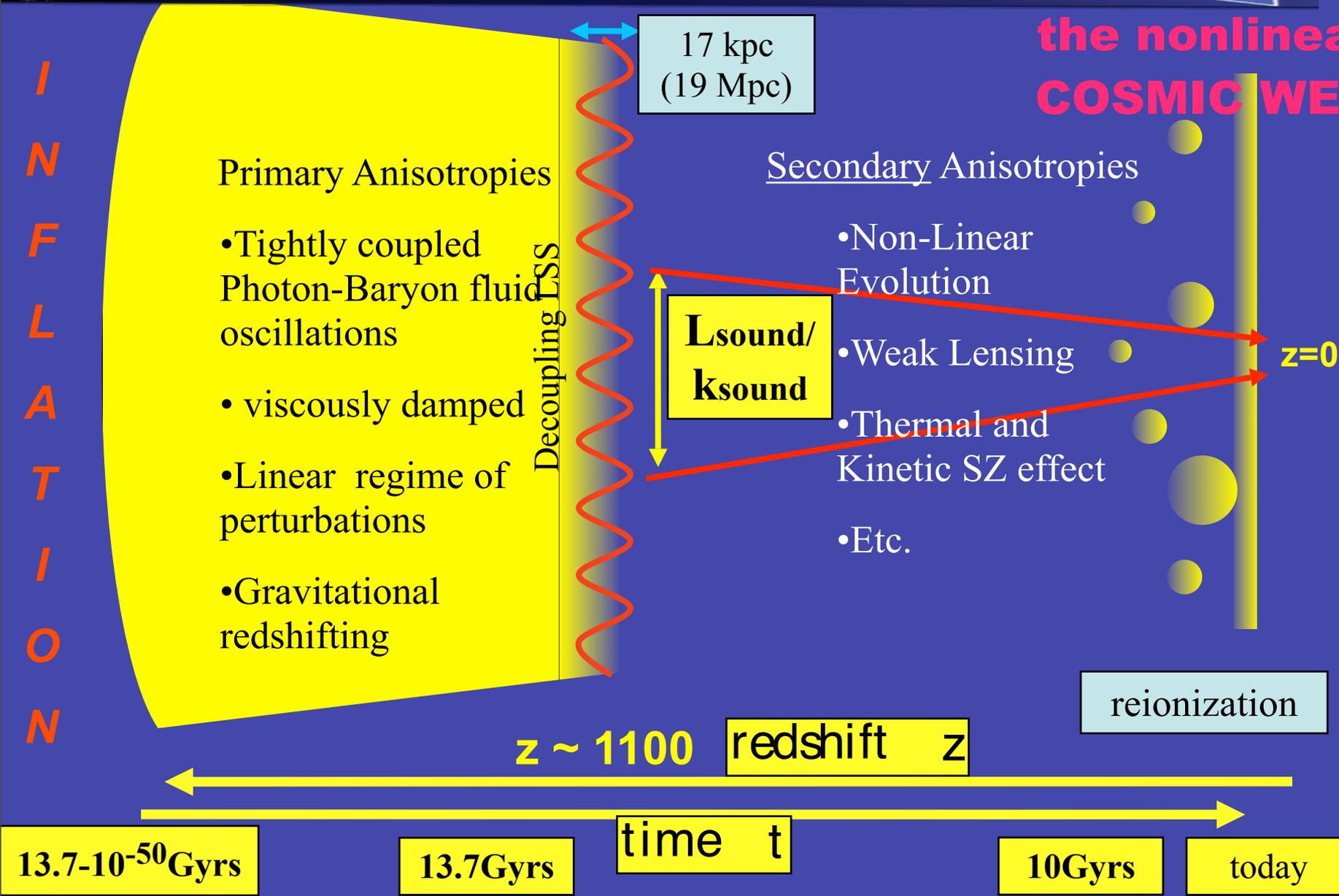
13.7-10⁻⁵⁰Gyrs

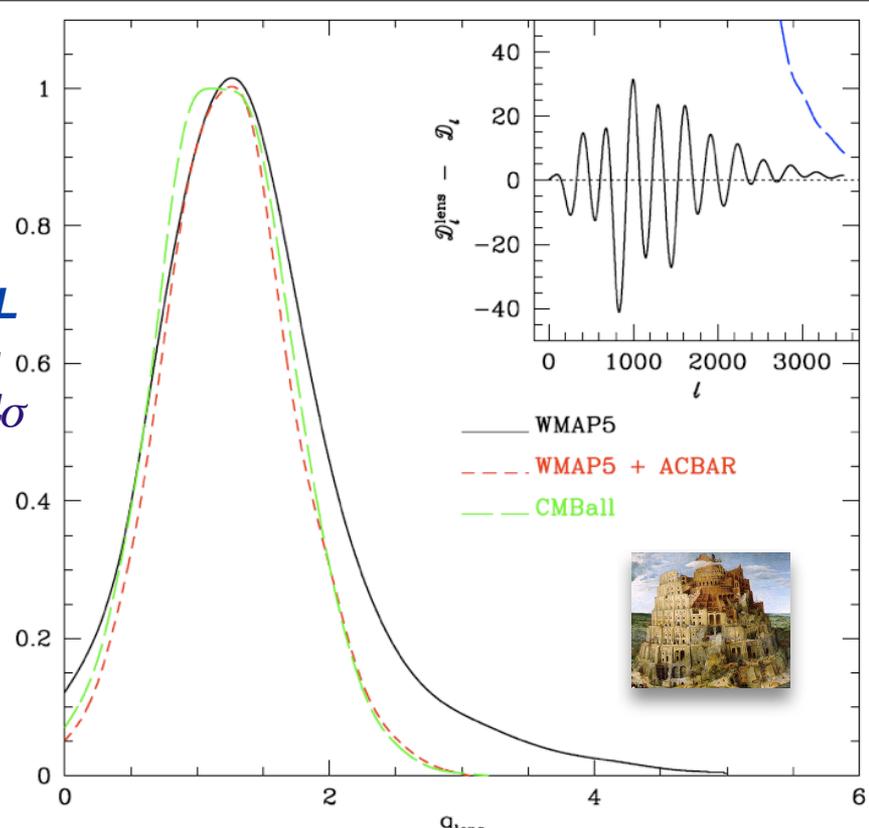
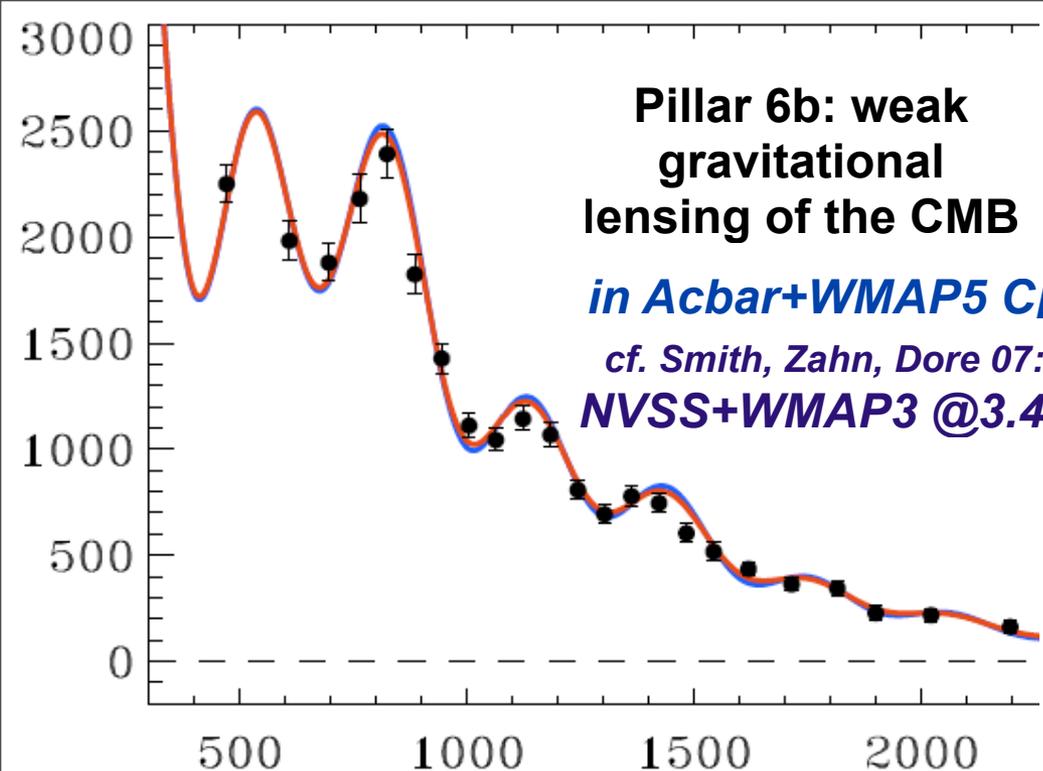
13.7Gyrs

time **t**

10Gyrs

today





$$C_{\ell}^{\text{lens}} = C_{\ell}^{\text{no-lens}} + q_{\text{lens}} \Delta C_{\ell}^{\text{lens}}$$

$$\Delta \ln \mathcal{E} = \ln [P(\text{lens} | \text{data}, \text{theory}) / P(\text{no-lens} | \text{data}, \text{theory})]$$

wmap5 $q_{\text{lens}} = 1.34^{+0.27(+1.51)}_{-0.26(-0.85)}$

wmap5+acbar $q_{\text{lens}} = 1.23^{+0.21(+0.83)}_{-0.23(-0.76)}$

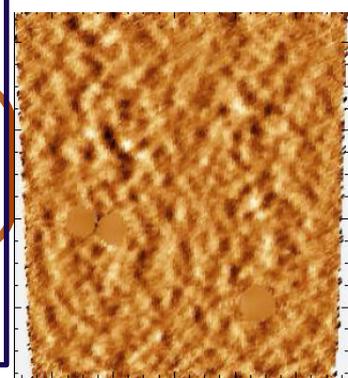
CMBall $q_{\text{lens}} = 1.21^{+0.24(+0.82)}_{-0.24(-0.76)}$

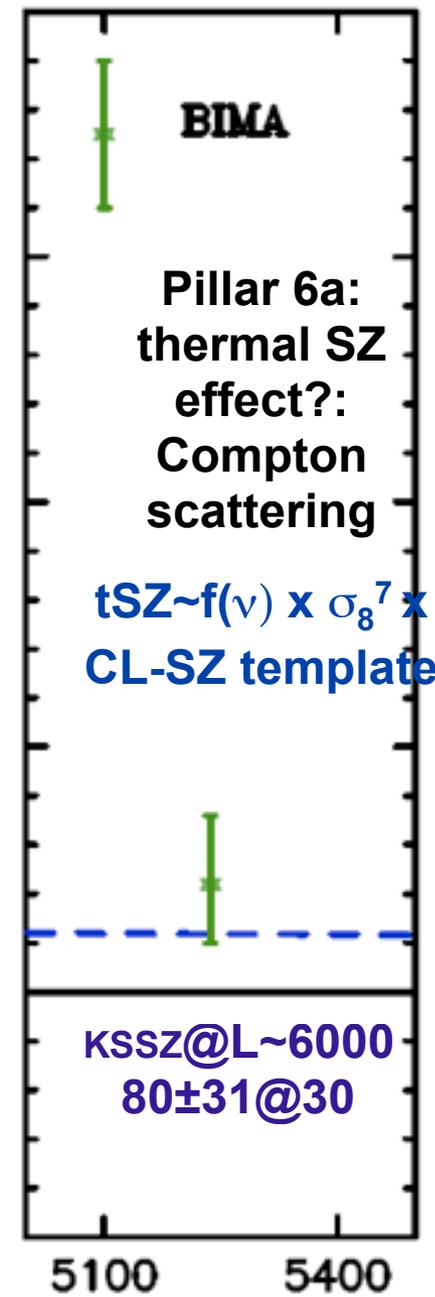
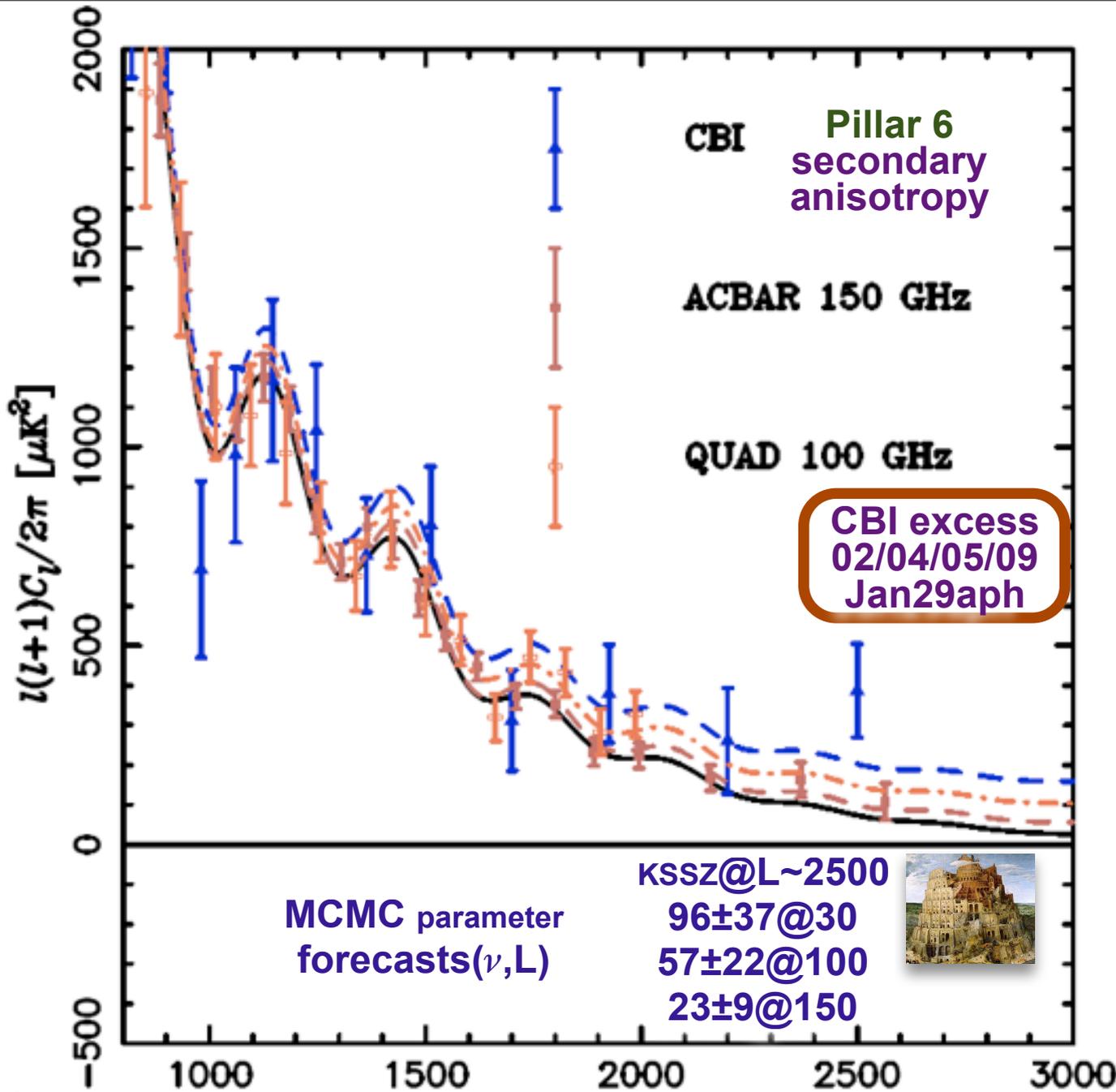
Bayesian evidence

$\Delta \ln \mathcal{E} = 2.04$

$\Delta \ln \mathcal{E} = 2.89$

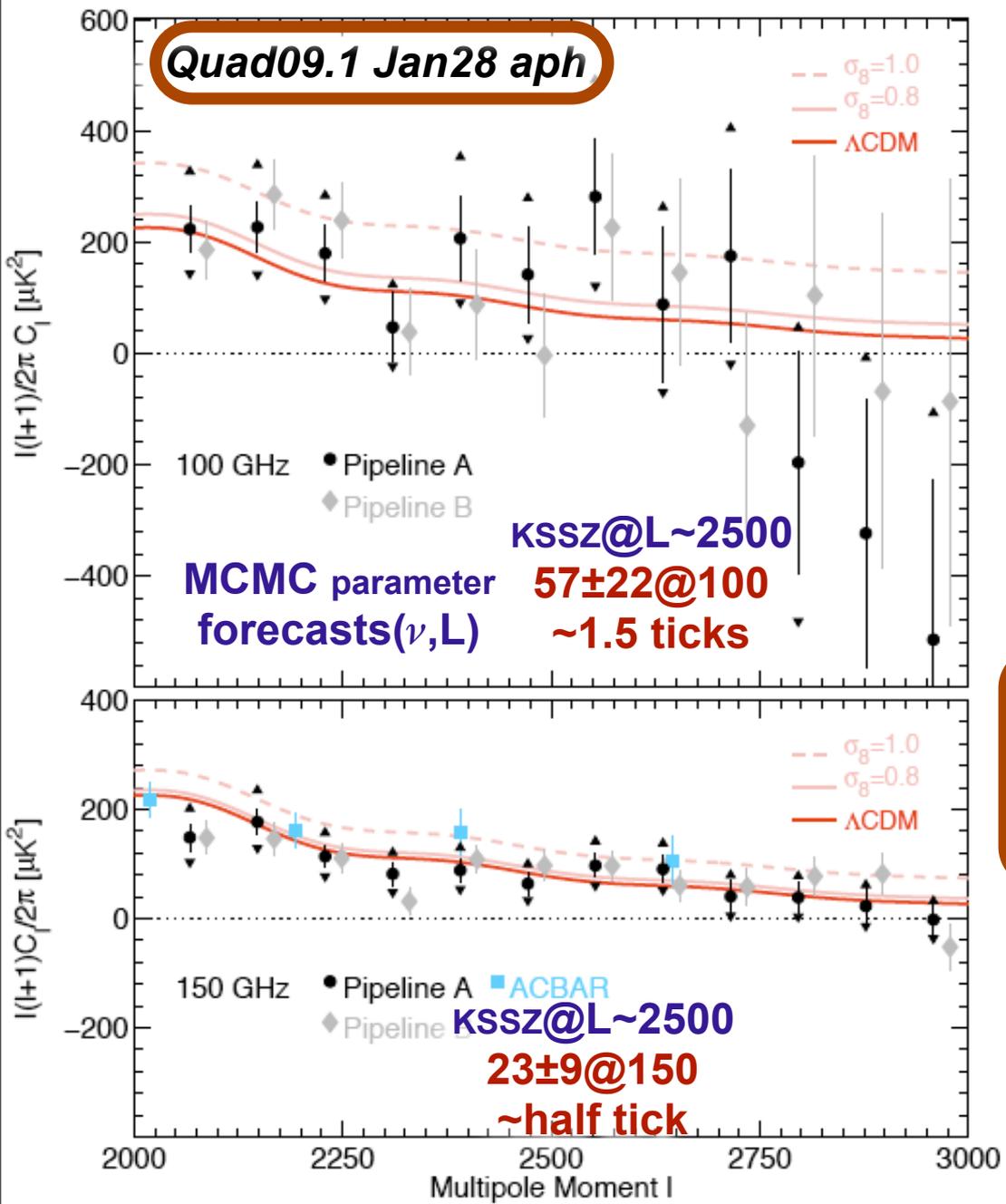
$\Delta \ln \mathcal{E} = 2.63$





09Jan29 aph SZA@L~4066 60+65-55@30 \Rightarrow 34±60 cf. 92±35@30 KSSZ@L~4000

Quad09.1 Jan28 aph



Pillar 6
secondary
anisotropy

CBI excess
02/04/05/09.1

Pillar 6a:
thermal SZ
effect?:
Compton
scattering

$tSZ \sim f(\nu) \times \sigma_8^7 \times$
CL-SZ template

Conclude: QuAD is consistent with the SZ-frequency-scaled CBI excess



ACT@5170m



why Atacama? driest desert in the world. thus: cbi, toco, apex, asti, act, alma, quiet, clover

CBI2@5040m



CBI pol to Apr'05 @Chile **CBI2**

QUaD @SP

Quiet1

@Chile

Quiet2

1000 HEMTs

Boom03@LDB

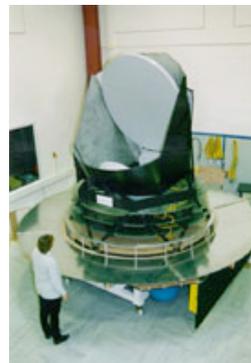
Bicep @SP

Bicep2

Keck/Spud

WMAP @L2 to 2009-2013?

Planck09.3



EBEX
@LDB

Spider

2312 bolos
@LDB



DASI @SP

CAPMAP

(52 bolometers)
+ HEMTs @L2
9 frequencies

Herschel

BLAST

CHIP

2004

2006

2008

LHC

2011

Bpol

@L2

2005

2007

2009

Acbar to Jan'06, 08f @SP

SPT

1000 bolos

@SPole

BLASTpol

Clover

@Chile

SZA

@Cal



APEX

~400 bolos

@Chile

ACT

3000 bolos

3 freqs @Chile

Polarbear

300 bolos

@Cal/Chile

AMI

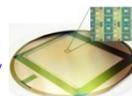


GBT

SCUBA2

12000 bolos

JCMT @Hawaii



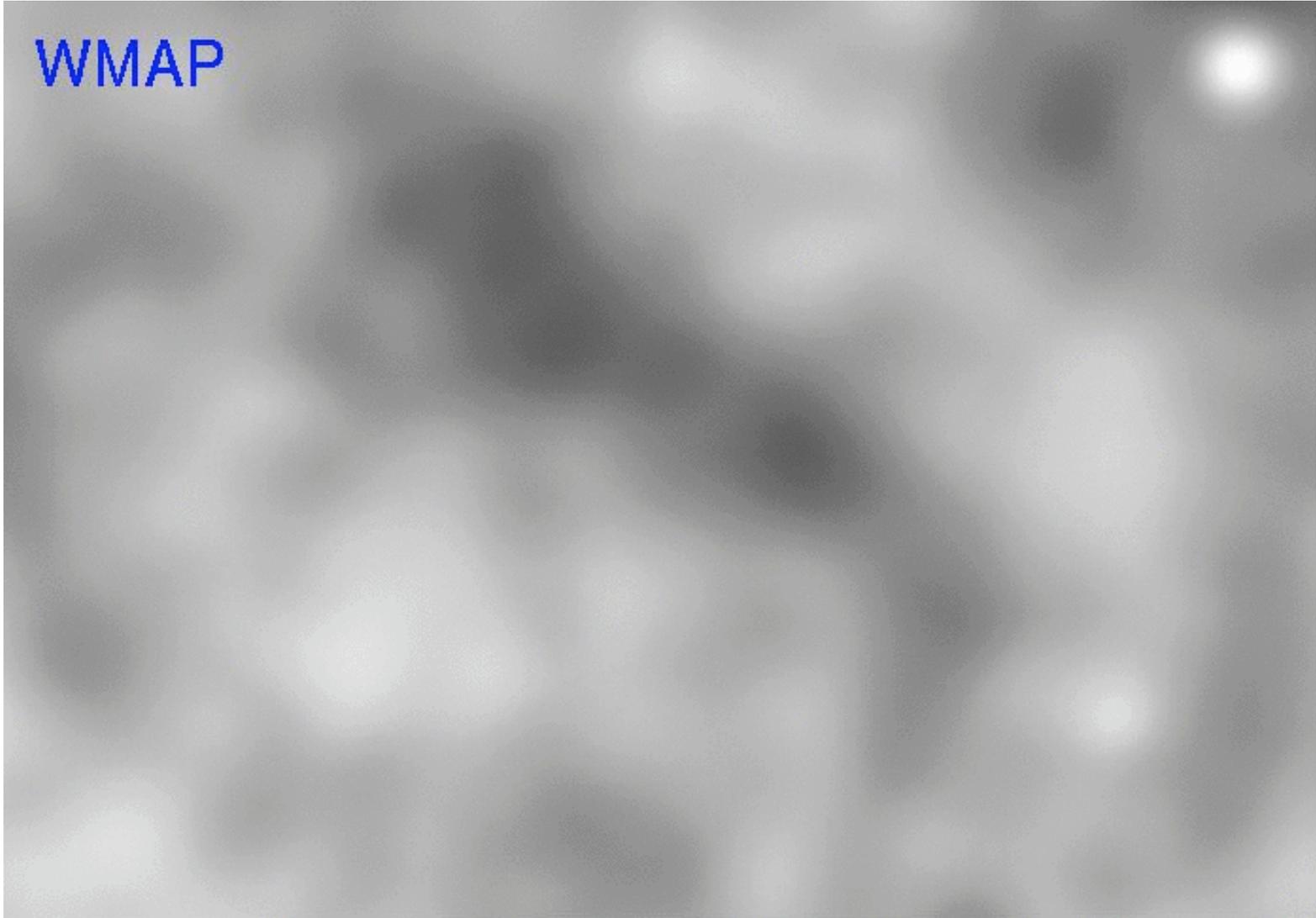
ALMA

@Chile

LMT@Mexico

WMAP \Rightarrow BOOM \Rightarrow ACBAR \Rightarrow ACT the high resolution CMB frontier

WMAP



Toby
Marriage,
ACTor



Peebles, Page, Partridge, *Finding the Big Bang*, Feb09 CUP

Rees 1968: CMB should be polarized; detection 2002 DASI

Kaiser83, pol via line-of-sight integration

BE84: pol via Boltzmann transport, ~7% target, effect on shear viscosity, damping tail, “E” mode

BE87: low to high L full CLpol, maps

Crittenden & Turok 96: TE correlation DASI02, WMAP03

Kaiser95, Stebbins96: rotate lensing E to B, a null test

Kamionkowski, Kosowsky & Stebbins97 & Seljak & Zaldarriaga97: apply to CMB E/B modes. emphasize as gravity wave discriminator

Zaldarriaga & Seljak98 lensing distorts E into B

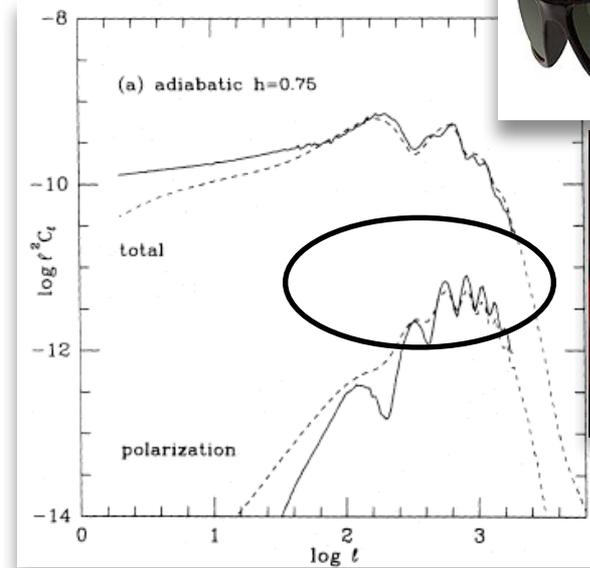
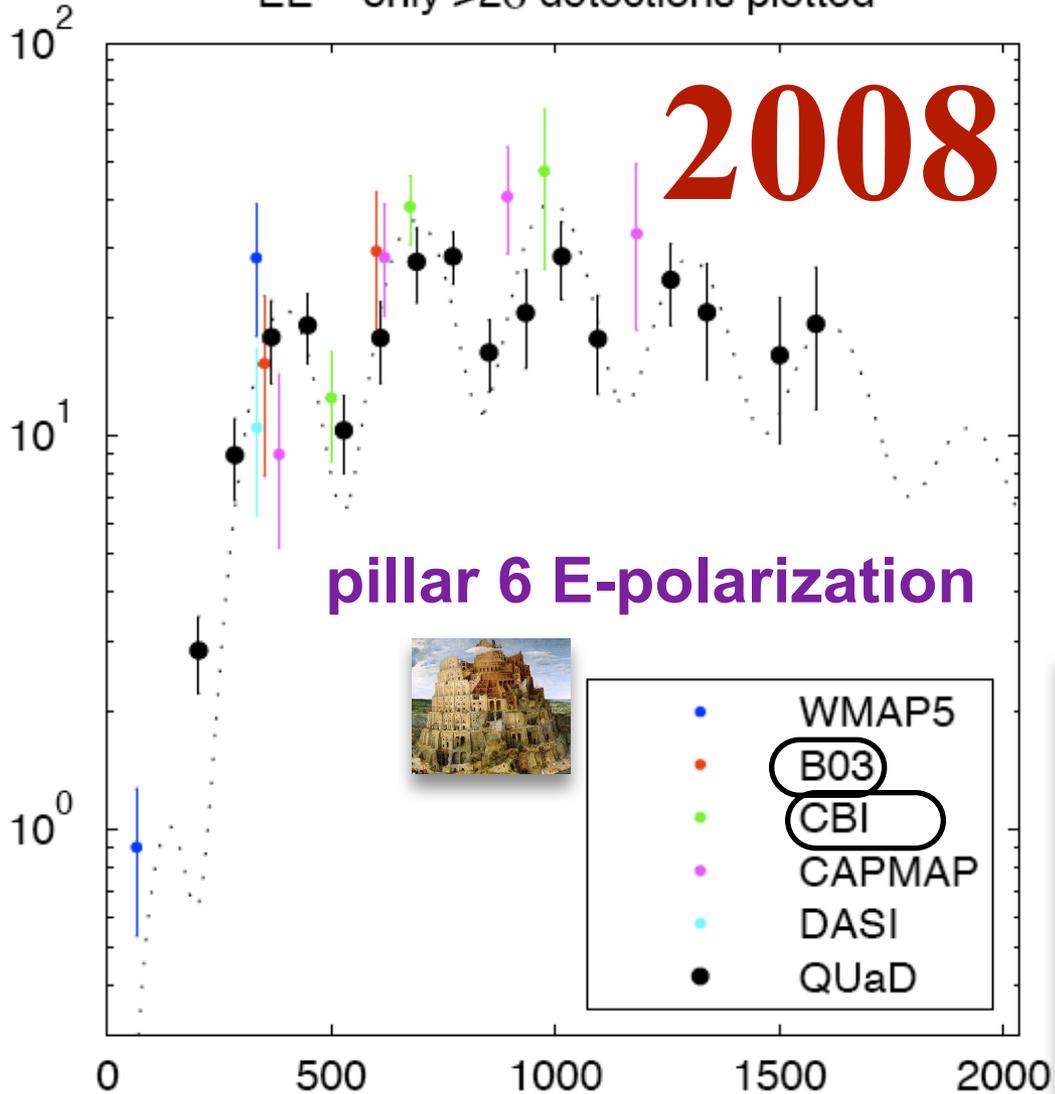


First E detection DASI 2002; CBI04/05, Boom05, WMAP06, Capmap08, QuAD08; **BICEP09?**

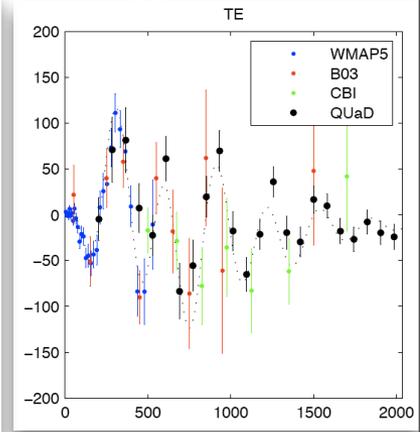
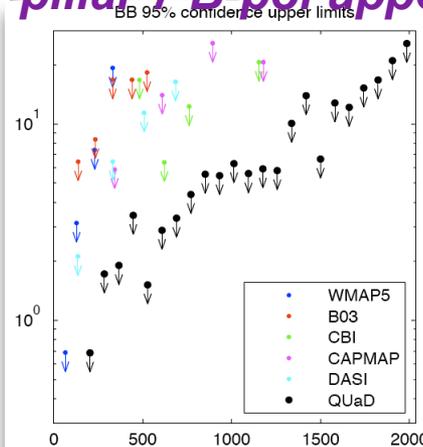
emergence of **CMB polarization** power

DASI02,04 CBI04 Boom05 CBI05 WMAP3,5 QUaD07,08

EE – only $>2\sigma$ detections plotted



pillar 7 B-pol upper limits



What is the Universe made of?

NOW: baryons + (cold-ish) dark matter + dark energy/inflaton + tiny curvature energy (+light neutrinos+photons). ??a bit of strings/textures/PBHs?? web of galaxies/clusters

THEN: coherent inflaton / "vacuum" energy plus **zero-point fluctuations** in all fields (\approx Gaussian RF) & then preheat via mode coupling to incoherent cascade to thermal equilibrium aka **quark-gluon plasma** & *how was it, is it & will it be distributed?*

very early U early to middle to now U **very late U**

string theory/landscape/higher dimensions

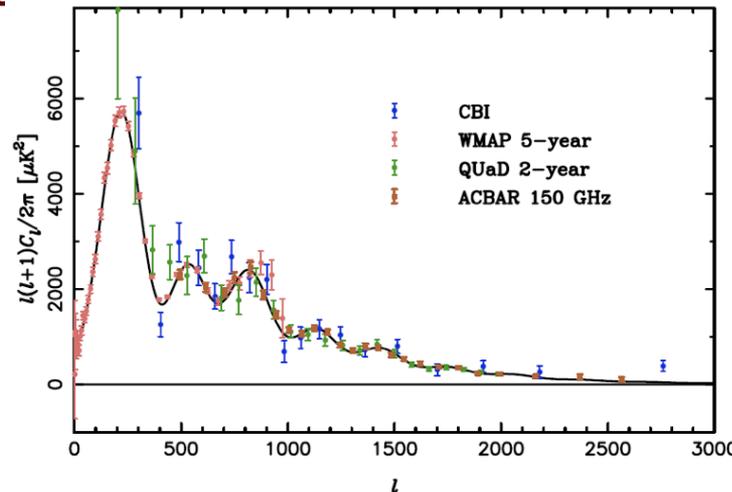
inflation cyclic baryogenesis dark matter BBN γ dec **dark energy**

$V_{\text{eff}}(\psi_{\text{inf}}) ?$

$K_{\text{eff}}(\psi_{\text{inf}}) ?$

$V_{\text{eff}}(\psi_{\text{inf}}) ?$

$K_{\text{eff}}(\psi_{\text{inf}}) ?$



cosmic mysteries

n_b/n_γ ρ_{dm}/ρ_b $z_{\text{eq}}/z_{\text{rec}}$ ρ_{curv} $\rho_{\text{de}}/\rho_{\text{dm}}$ $\rho_{\text{de}} \sim H^2 M_{\text{Planck}}^2$ $\rho_{\text{mv}}/\rho_{\text{stars}}$

⇒ exquisite & increasingly precise determination of cosmic parameters

dark matter abundance $\Omega_m = 0.268 +0.012 -0.012$

	January 2000	January 2002	June 2002	January 2003	March 2003
$\Omega_{\text{cdm}} h^2$	$0.198^{+0.088}_{-0.080}$	$0.130^{+0.031}_{-0.028}$	$0.124^{+0.026}_{-0.025}$	$0.125^{+0.021}_{-0.022}$	$0.111^{+0.010}_{-0.010}$

CMB-only history (weak-h prior). LSS-then drove to near current

$\Omega_{\text{dm}} h^2$ **0.1145 ± 0.0023** CMBall+WL+LSS+SN+Lya
 $\Omega_{\text{b}} h^2$ **0.0233 ± 0.0005** ordinary matter abundance (baryons)

⇒ $\rho_{\text{dm}}/\rho_{\text{b}} = 5.1$

Ω_{Λ}	$0.34^{+0.28}_{-0.24}$	$0.52^{+0.17}_{-0.20}$	$0.53^{+0.17}_{-0.19}$	$0.57^{+0.14}_{-0.19}$	$0.73^{+0.06}_{-0.10}$
--------------------	------------------------	------------------------	------------------------	------------------------	------------------------

CMB-only history (weak-h prior). LSS-then drove to near current value

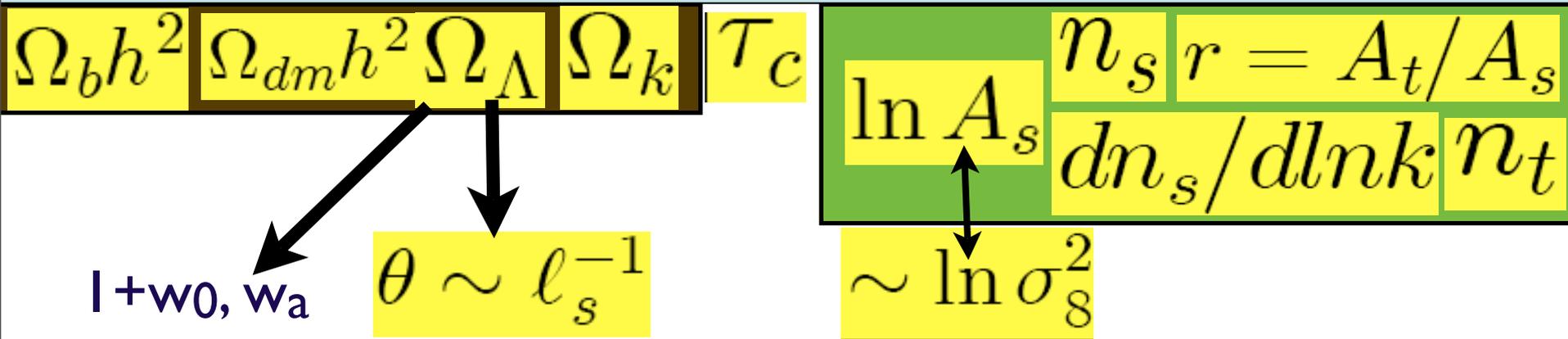
dark energy abundance $\Omega_{\Lambda} = 0.736 +0.012 -0.012$

& $H_0 = 72 \pm 1$ CMBall+WL+LSS+SN+Lya

⇒ $\rho_{\text{m}}/\rho_{\text{de}} = .30$

$\mathcal{E} = -d \ln H / d \ln a = 1 + q$: now $= 3/2 [\Omega_{\text{m}0} + (1+w)(1-\Omega_{\text{m}0})]$ ~0.40?, to 0?

Standard & Parameters of Cosmic Structure Formation



+ subdominant isocurvature/ cosmic string & fgnds, tSZ, kSZ, ...

+ primordial non-Gaussianity

$$\Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + \mathbf{f}_{NL} (\Phi_G^2(\mathbf{x}) - \langle \Phi_G^2 \rangle)$$

local smooth

$$\Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + \mathbf{F}_{NL}(\chi_b) - \langle \mathbf{F}_{NL} \rangle$$

resonant preheating

new parameters: trajectory probabilities for early-inflatons & late-inflatons
 (partially) blind cf. informed “theory” priors

CBI pol to Apr'05 @Chile

QUaD @SP

Quiet1
@Chile

Quiet2
1000 HEMTs

Boom03@LDB

Bicep @SP

Bicep2

Keck/Spud

WMAP @L2 to **2009-2013?**

Planck09.3



(52 bolometers)
+ HEMTs @L2
9 frequencies

EBEX
@LDB

Spider

2312 bolos
@LDB



DASI @SP

CAPMAP

CHIP

2004

2006

2008

LHC

2011

Bpol
@L2

2005

2007

2009

BLASTpol

Clover
@Chile

Polarbear

300 bolos
@Cal/Chile

SPTpol



INFLATION THEN PROBES NOW

“standard inflation space”: n_s $dn_s/d\ln k$ r @k-pivots

$$n_s(k_p) = .962 \pm .013 \text{ (+-.005 Planck1)} \quad .959 \pm .011 \text{ all data}$$

$$r = P_t/P_s(k_p) < 0.40_{\text{cmb}} \text{ 95\% CL (+-.03 P1, +- .01 Spider+P2.5)}$$

$$dn_s/d\ln k(k_p) = -.016 \pm .019 \text{ (+-.005 Planck1)}$$

(partially) blind trajectories e.g., $n_s(k)$ and $r(k_p)$, are better

local quadratic non-G constraint: $-9 < f_{NL} < 111 \Rightarrow -4 < f_{NL} < 80$ WMAP5 ($\pm 5-10$ Planck1yr)

CBI10: add a cosmic string template $\Rightarrow n_s < 1$ @ 2σ & string tension limit $G\mu < 2.8 \times 10^{-7}$

INFLATION THEN

WHAT IS PREDICTED?

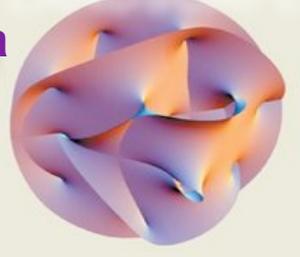
Smoothly broken scale invariance
by nearly uniform braking (standard
of 80s/90s/00s) $r \sim 0.03-0.5$

or highly variable braking r tiny
(stringy cosmology) $r < 10^{-10}$

Old view: Theory prior = delta function of THE correct one and only theory

New: Theory prior = probability distribution of late-flows on an energy LANDSCAPE

6/7 tiny extra dimensions



1980

R^2 -inflation

Old Inflation

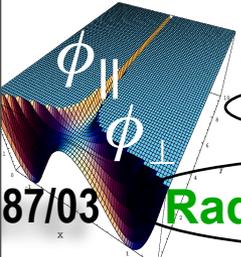
Chaotic inflation

New Inflation

Double Inflation

Power-law inflation

SUGRA inflation



87/03

Radical BSI inflation

variable M_p inflation

Extended inflation

1990

Natural pMGB inflation

Hybrid inflation

SUSY F-term inflation

SUSY D-term inflation

Assisted inflation

Brane inflation

2000

SUSY P-term inflation

Super-natural Inflation

K-fation

2003 KKL

N-fation

D3,D7 brane inflation

DBI inflation

ekpyrotic/cyclic

moving brane separations

Racetrack inflation

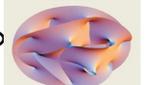
Tachyon inflation

Warped Brane inflation

moduli fields

monodromy

Roulette inflation Kahler moduli/axion



very early U

early to middle to now U

very late U

inflation

string theory/landscape/higher dimensions

dark energy

$V_{\text{eff}}(\psi_{\text{inf}})$? partial shape reconstruction
 $K_{\text{eff}}(\psi_{\text{inf}})$?

reconstruct gradient $V_{\text{eff}}(\psi_{\text{inf}})$?
 $K_{\text{eff}}(\psi_{\text{inf}})$?

trajectory probability

$$-d \ln \rho_{\text{tot}} / d \ln a \ / 2$$

$$= \mathcal{E}(k) = 1 + q, \quad k \sim H a$$

$$\Rightarrow P_s, P_t$$

$$V_{\text{eff}}(k), \psi_{\text{inf}}(k)$$

trajectory probability

$$-d \ln \rho_{\phi} / d \ln a \ / 2 \Rightarrow$$

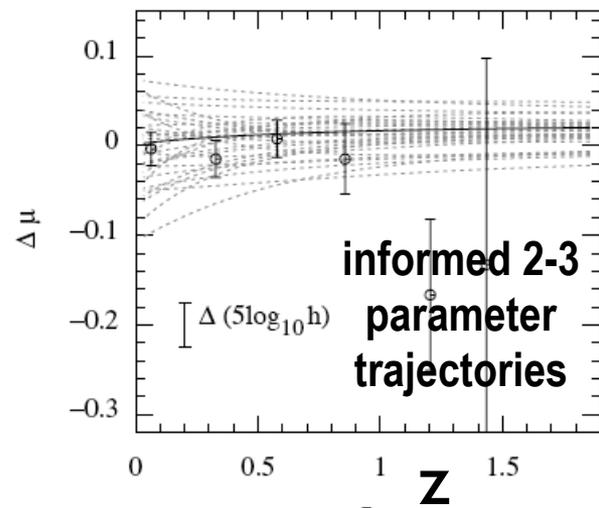
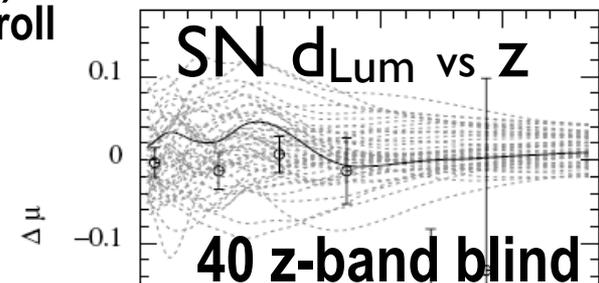
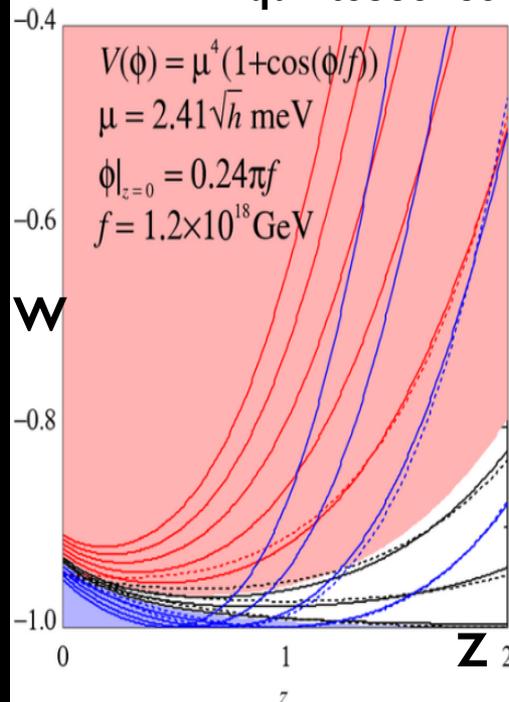
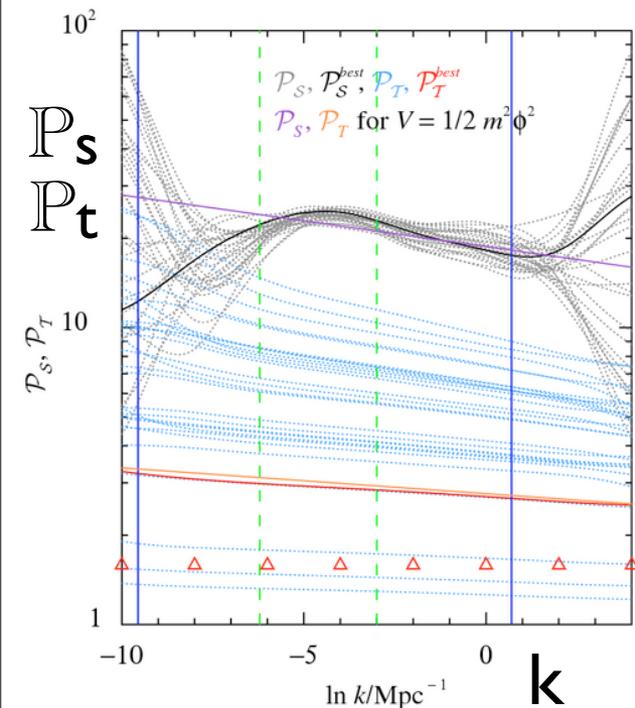
$$= \mathcal{E}_{\phi}(a) = (1 + w) / 2 / 3$$

slow-to-moderate roll
quintessence

$$\epsilon_s = (d \ln V / d \psi)^2 / 4$$

@pivot a_{eq} **yes**

$d^2 \ln V / d \psi^2 / 4$ **no**

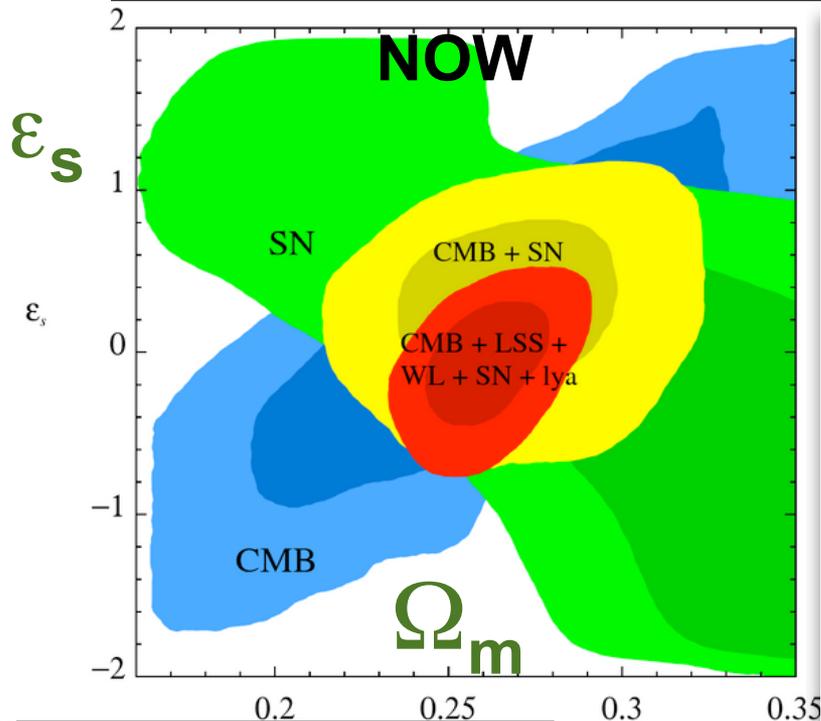


**INFLATION
NOW**

**PROBES
NOW & THEN**

Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)

+ **DUNE-WL** (50% sky, gals @z = 0.1-1.1, 35/min²) + **Planck1yr**
 now ESA /Eucid ESA (+NASA/CSA)

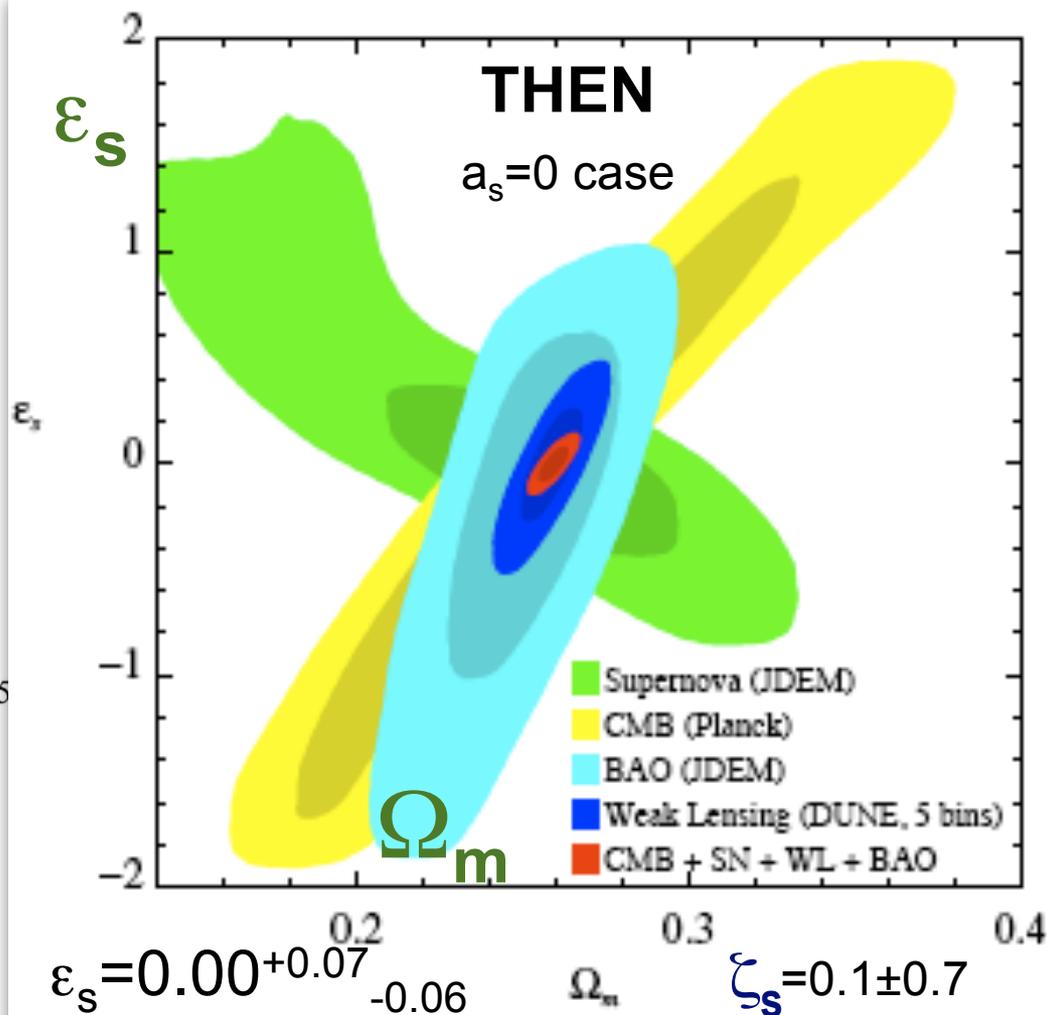


$$1 + w_0 = -0.0 \pm 0.06$$

$$\epsilon_s = \frac{(d \ln V / d \psi)^2}{4} \text{ @pivot } a_{eq}$$

$$= -.03 + .26 \quad -.30 \quad 2$$

$$\zeta_s = \pm 1.001 d^2 \ln V / d \psi^2 / 4 = 0.1 \pm 0.7$$



$$\epsilon_s = 0.00^{+0.07}_{-0.06} \quad \Omega_m \quad \zeta_s = 0.1 \pm 0.7$$

cannot reconstruct the quintessence potential, just the slope ϵ_s & ~hubble drag

INFLATION

THEN

PROBES

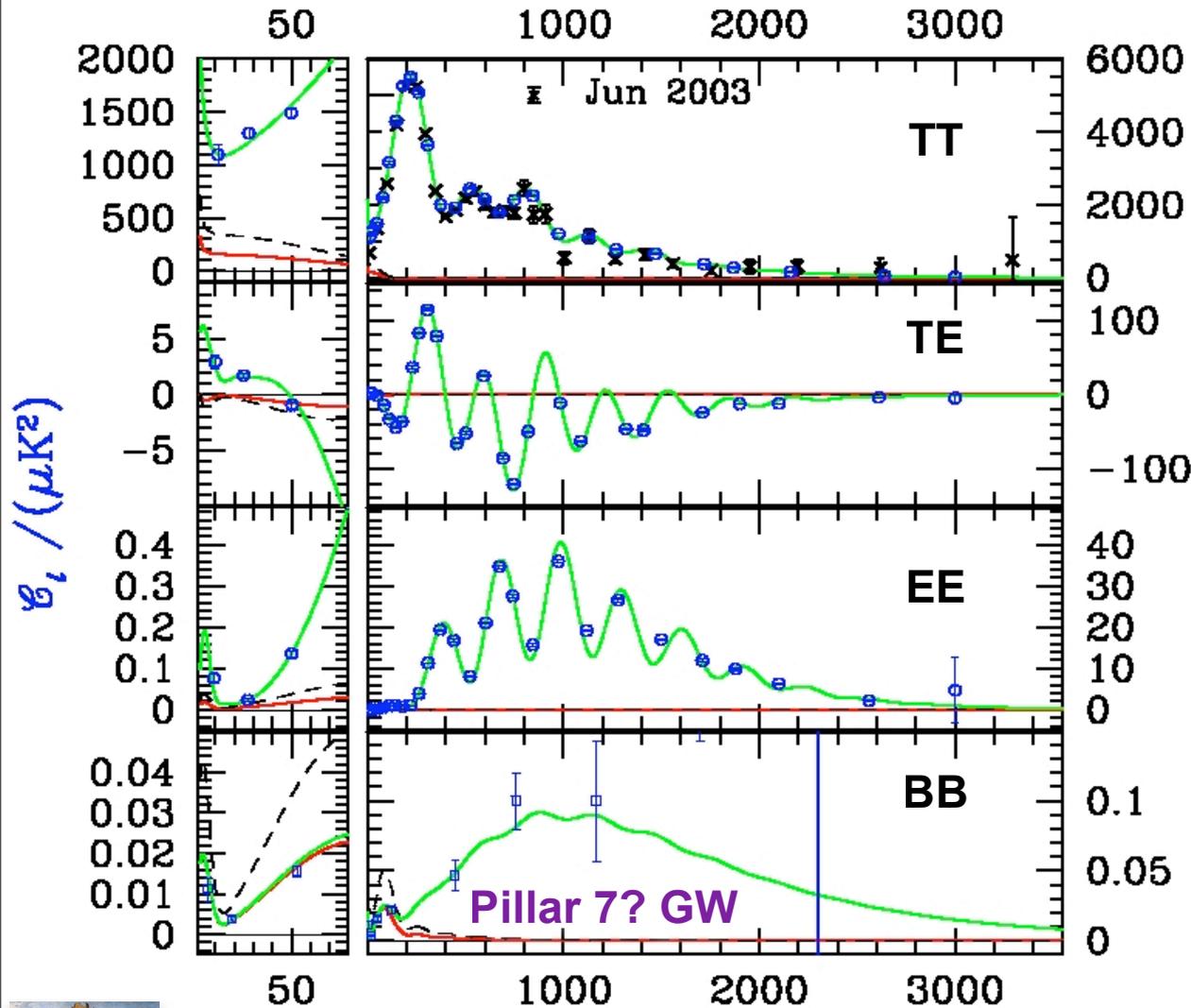
THEN

PRIMARY END @ 2012?

CMB ~2009+ Planck1+WMAP8+SPT/ACT/Quiet+Bicep/QuAD/Quiet +Spider+Clover



Pillar 7? Gravity Waves



+ Pillar 4: primordial non-Gaussianity

$-9 < f_{NL} < 111$ (+- 5-10 Planck1)



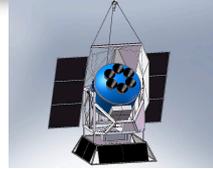
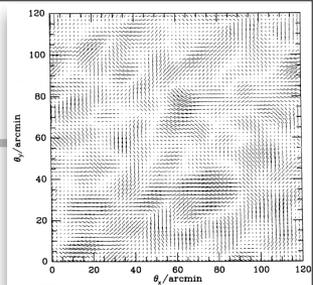
SPIDER Tensor Signal

Gravity Waves from Inflation

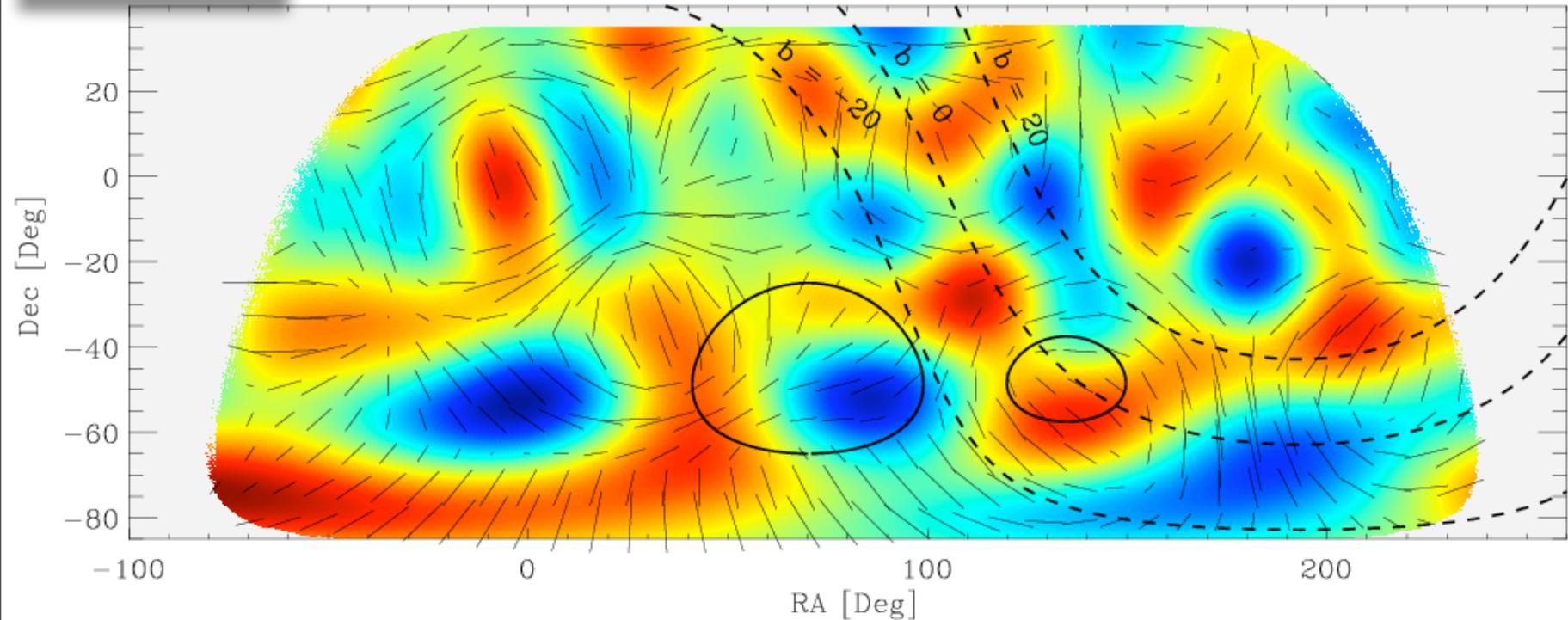
- Simulation of large scale polarization signal

http://www.astro.caltech.edu/~lgg/spider_front.htm

$$\frac{A_T}{A_S} = 0.1$$



Tensor



GW/scalar curvature: current from CMB+LSS: $r < 0.3$ 95%; good shot at **0.02** 95% CL with **BB polarization** (+- .02 PL2.5+Spider), .01 target; **Bpol .001 BUT** foregrounds/systematics? **But $r(k)$, low Energy inflation**

SPIDER Tensor Signal

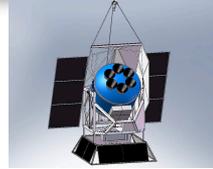
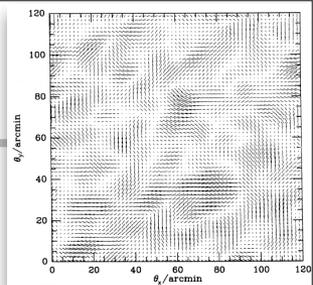
Gravity Waves from Inflation

- Simulation of large scale polarization signal

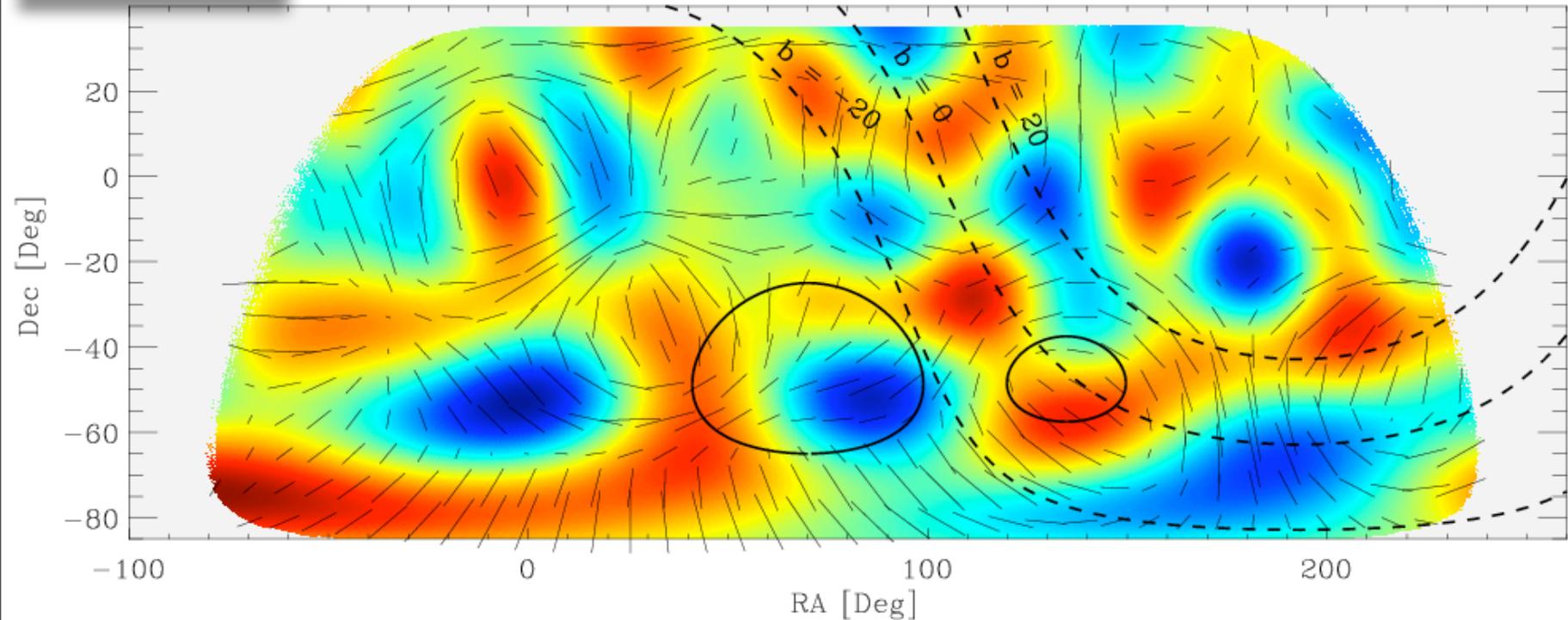
http://www.astro.caltech.edu/~lgg/spider_front.htm



$$\frac{A_T}{A_S} = 0.1$$



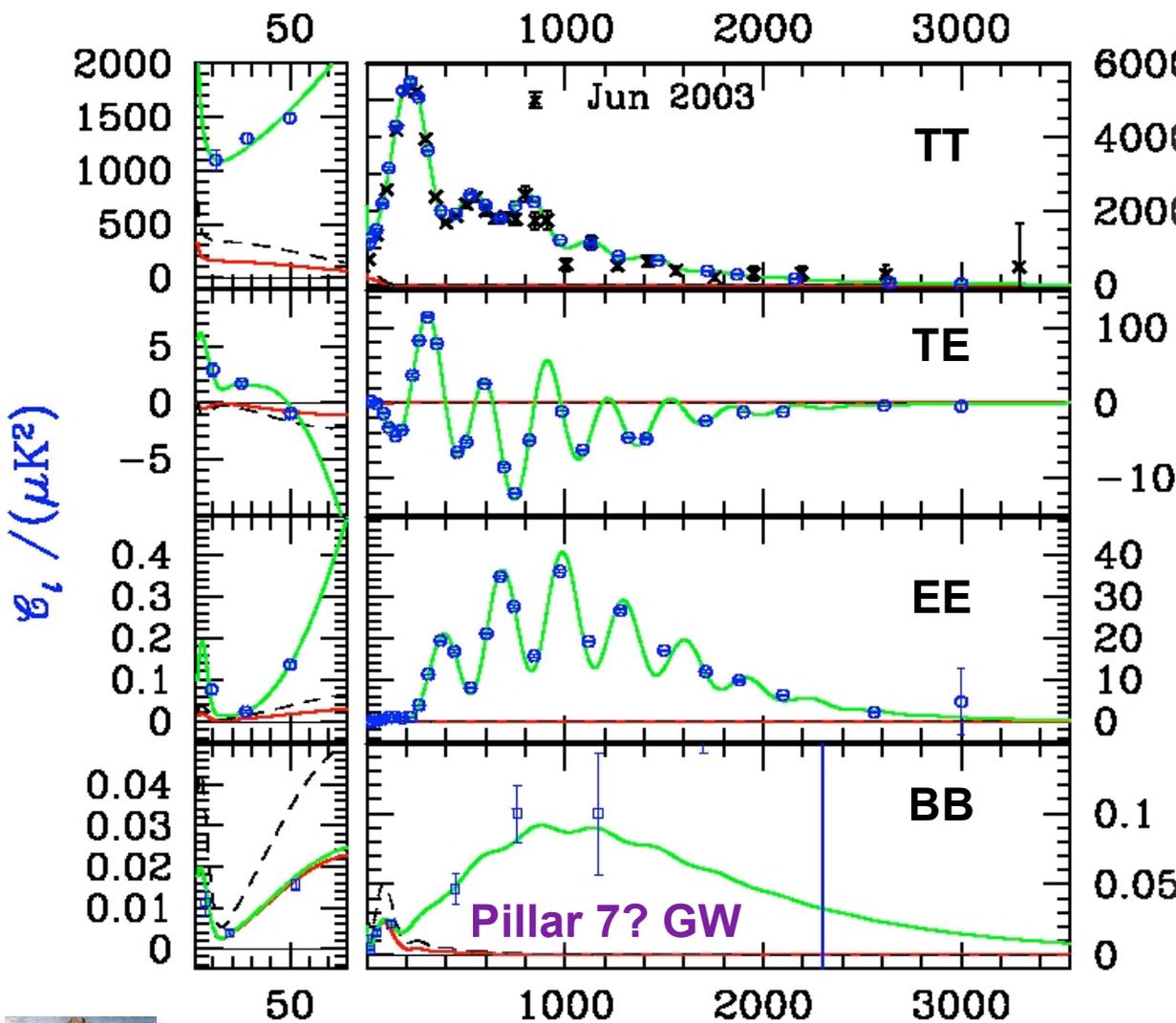
No Tensor



GW/scalar curvature: current from CMB+LSS: $r < 0.3$ 95%; good shot at **0.02** 95% CL with **BB polarization** (+ .02 PL2.5+Spider), .01 target; **Bpol .001** BUT foregrounds/systematics? But $r(k)$, low Energy inflation

PRIMARY END @ 2012?

CMB ~2009+ Planck1+WMAP8+SPT/ACT/Quiet+Bicep/QuAD/Quiet +Spider+Clover



Pillar 7? Gravity Waves

An ensemble of trajectories arises in many-moduli string models, whether braney or holey. Roulette inflation: complex hole sizes in 6D TINY $r < 10^{-10}$ & n_s from data-selected braking! ('theorem': $\Delta\psi < 1 \rightarrow r < .007$)

nearly uniform acceleration (power law, exp, PNGB, ..potentials) $r \sim .03-.3!$ is $\Delta\psi \sim 10$ deadly?

Even with low energy inflation, the prospects are good with Spider plus Planck to either detect the GW-induced B-polarization or set a strong blind upper limit $r < 0.02$ indicating stringy or other exotic models. Both experiments have strong Cdn roles. Bpol 2020?, to $r \sim 0.002$

+ Pillar 4: primordial non-Gaussianity

$-4 < f_{NL} < 80$ (+- 5-10 Planck1)



end1

The Past, Present & Future of Random Fields in Cosmology

What is the Universe made of & how was it, is it & will it be distributed?

NOW: baryons/leptons + (cold-ish) dark matter + dark energy/inflaton + tiny curvature energy (+photons+light neutrinos + gravity waves). ??a bit of strings/textures/PBHs?? *web of galaxies/clusters*

THEN: coherent inflaton /“vacuum” energy + **zero-point fluctuations** in all fields (*Gaussian RF*) & then preheat via mode coupling to incoherent cascade to thermal equilibrium soup

very early U early to middle to now U **very late U**

string theory/landscape/higher dimensions

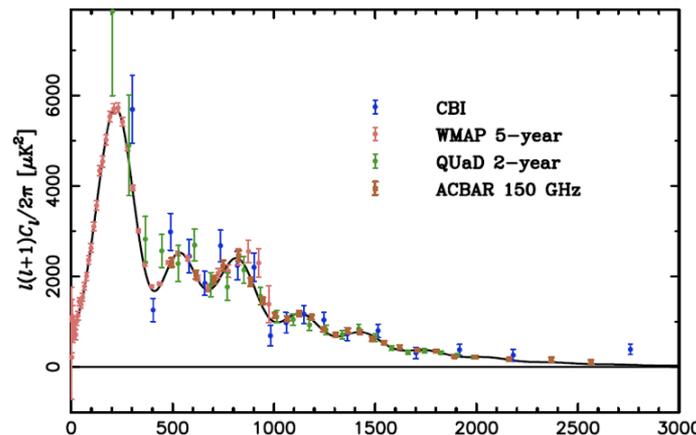
inflation cyclic baryogenesis dark matter BBN γ dec **dark energy**

$V_{\text{eff}}(\psi_{\text{inf}}) ?$

$K_{\text{eff}}(\psi_{\text{inf}}) ?$

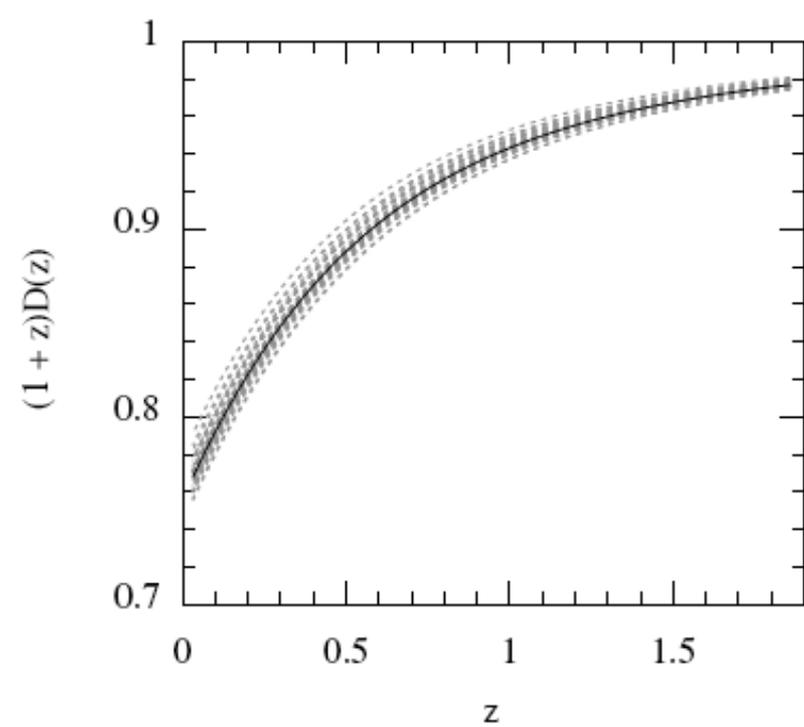
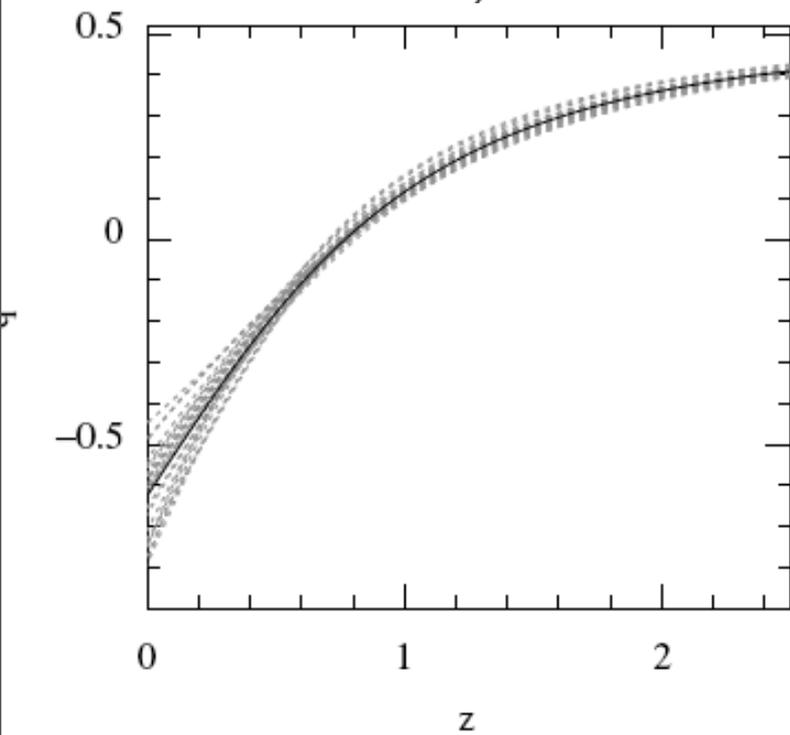
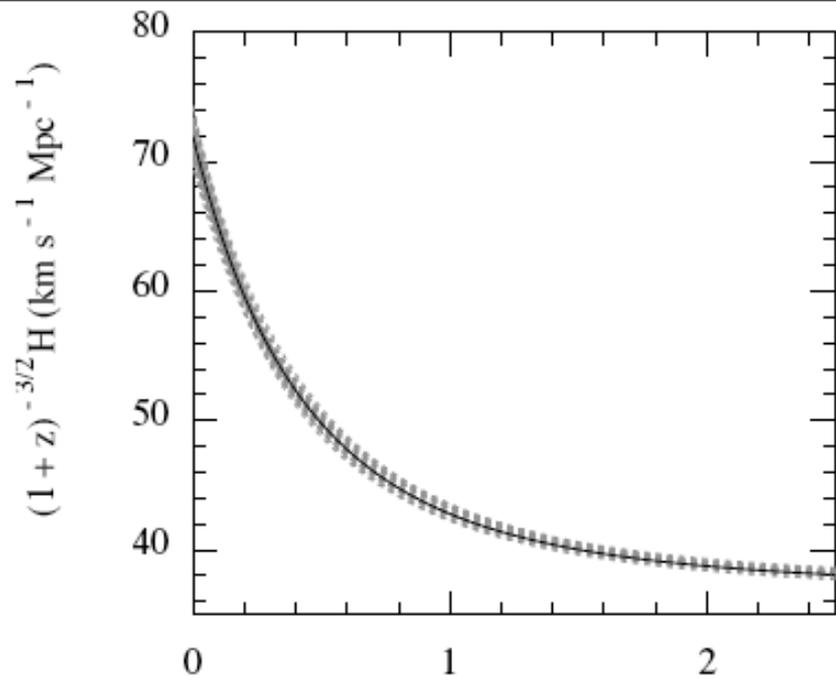
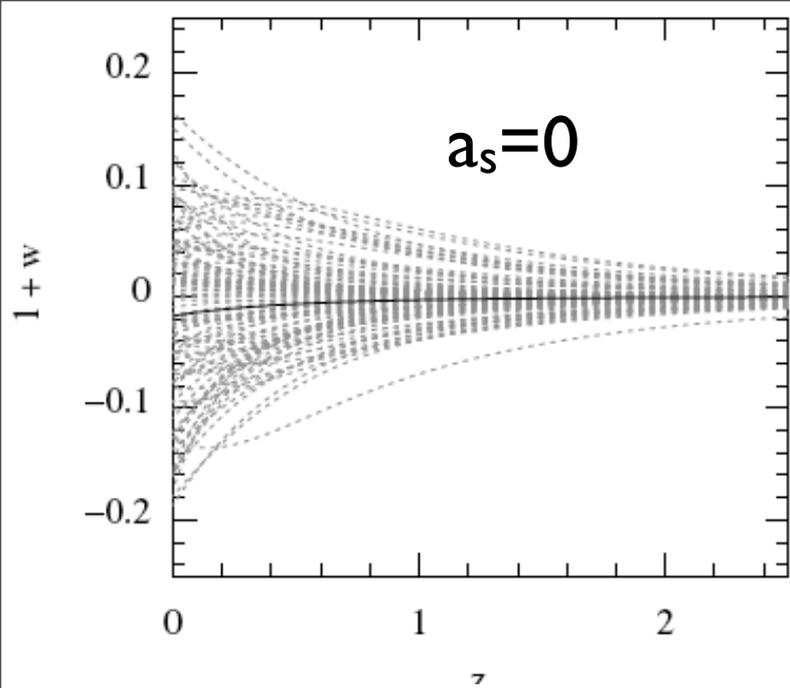
$V_{\text{eff}}(\psi_{\text{inf}}) ?$

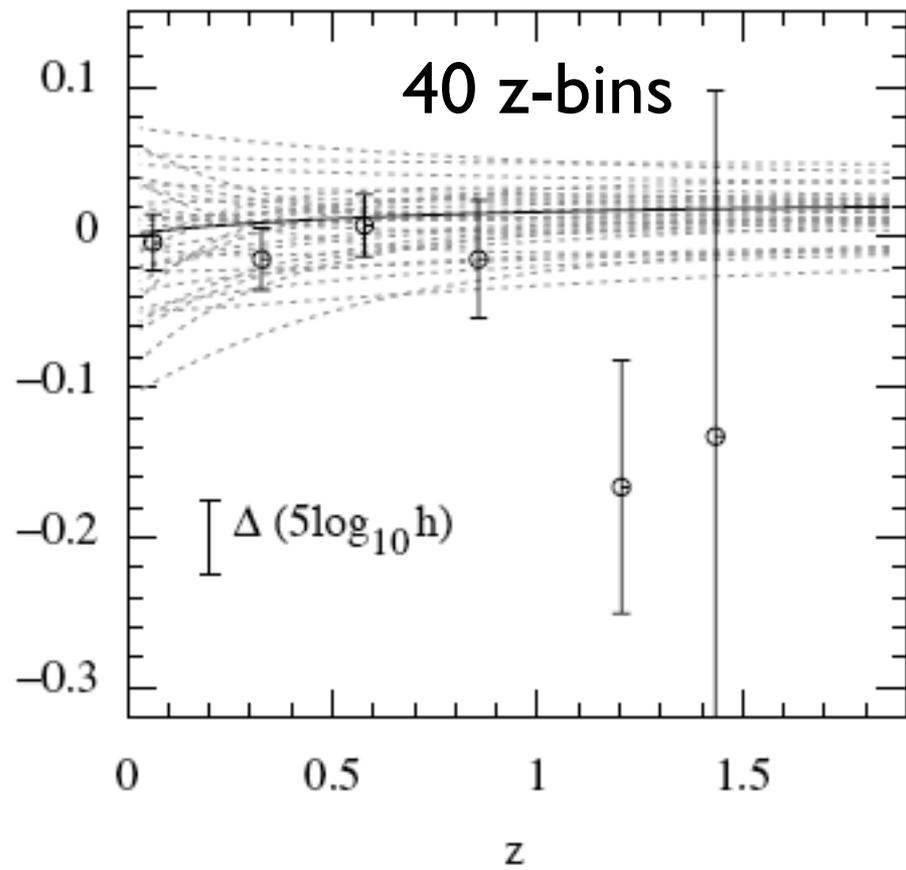
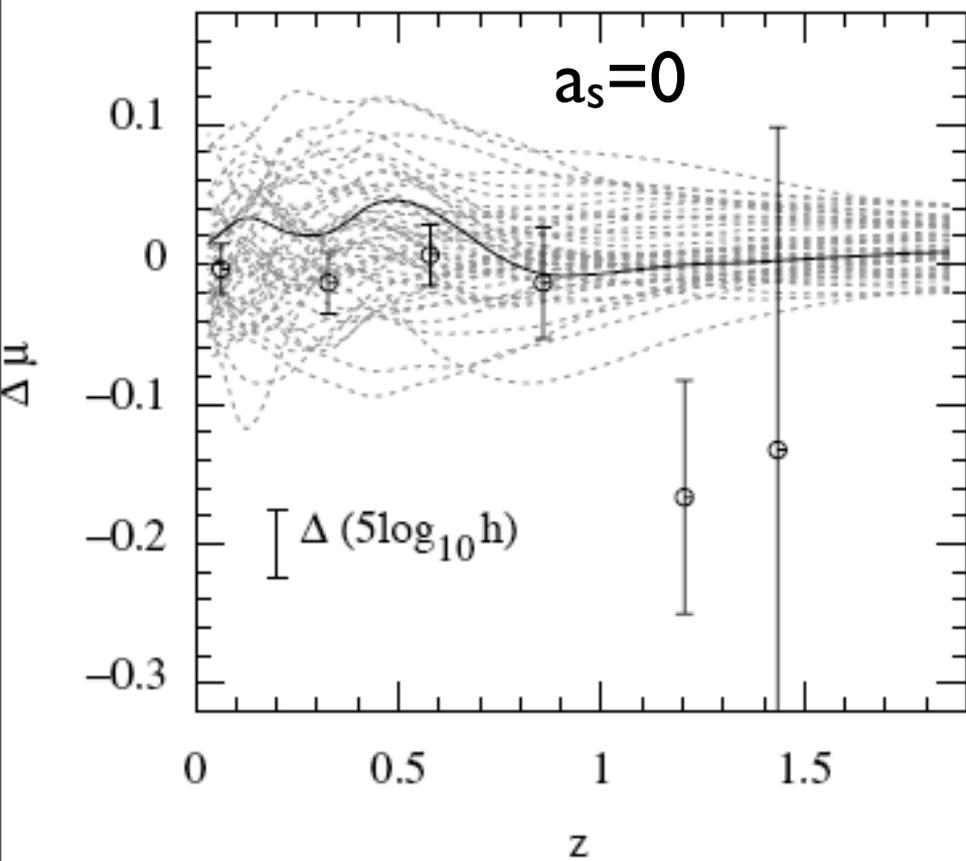
$K_{\text{eff}}(\psi_{\text{inf}}) ?$



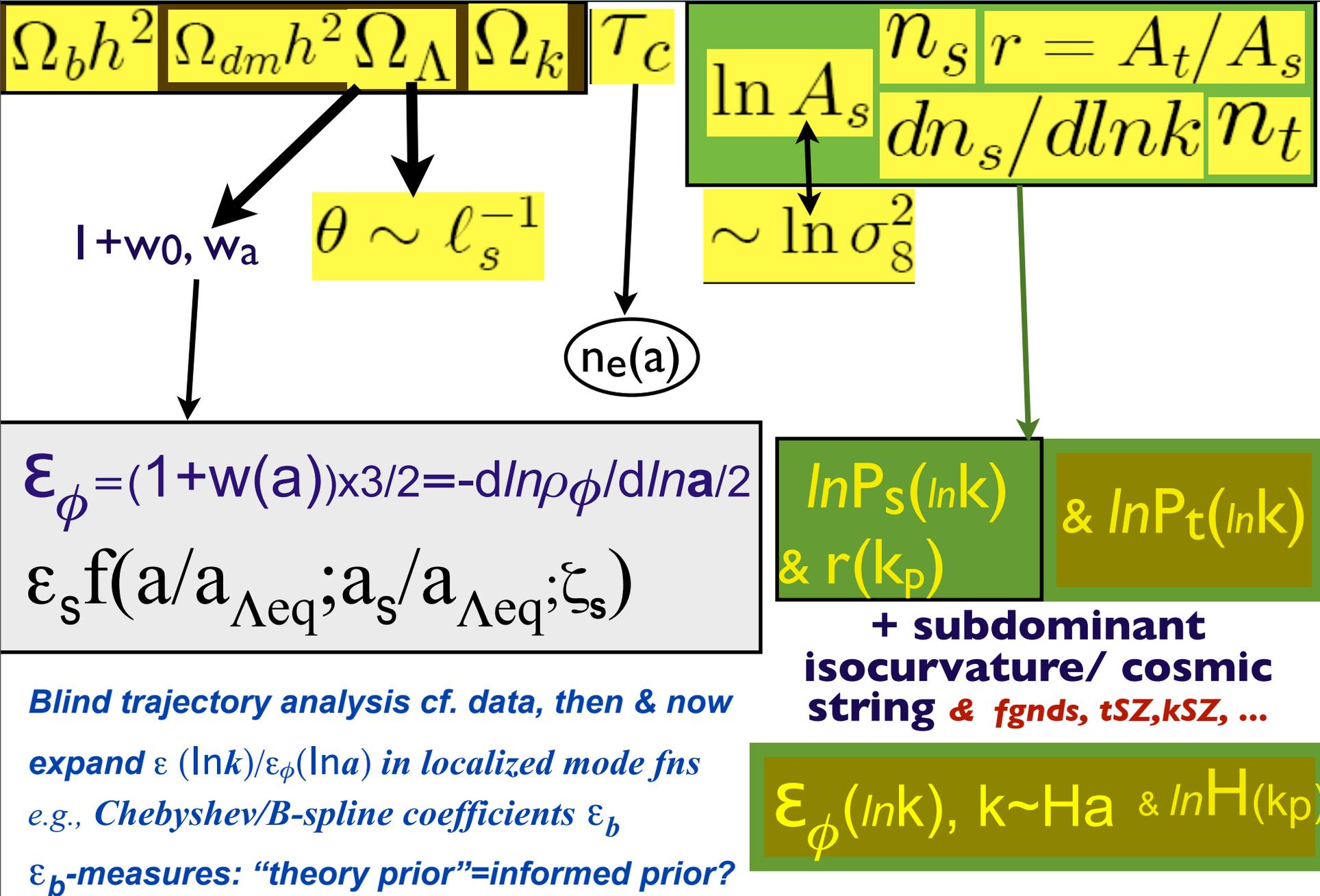
cosmic mysteries

n_b/n_γ ρ_{dm}/ρ_b $z_{\text{eq}}/z_{\text{rec}}$ ρ_{curv} $\rho_{\text{de}}/\rho_{\text{dm}}$ $\rho_{\text{de}} \sim H^{-1} |V|^2$ Planck $\rho_{\text{mv}}/\rho_{\text{stars}}$



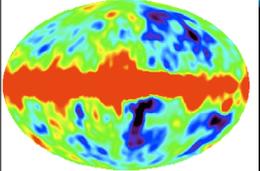


Standard & New Parameters of Cosmic Structure Formation



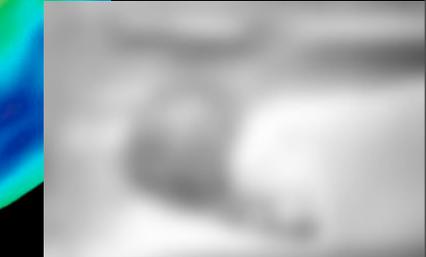
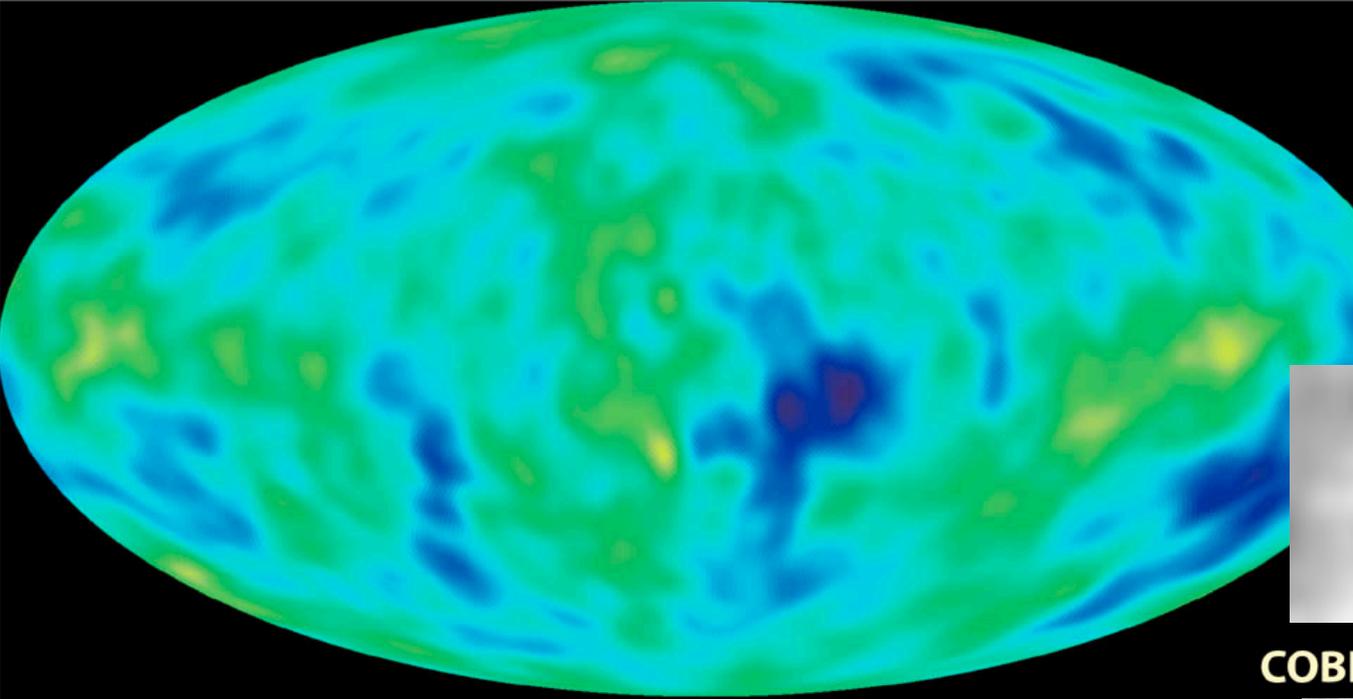
CMB
Nearly Perfect Blackbody
 $T=2.725 \pm .001$ K COBE/FIRAS

Dipole: flow of the earth in the CMB

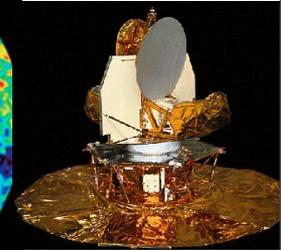
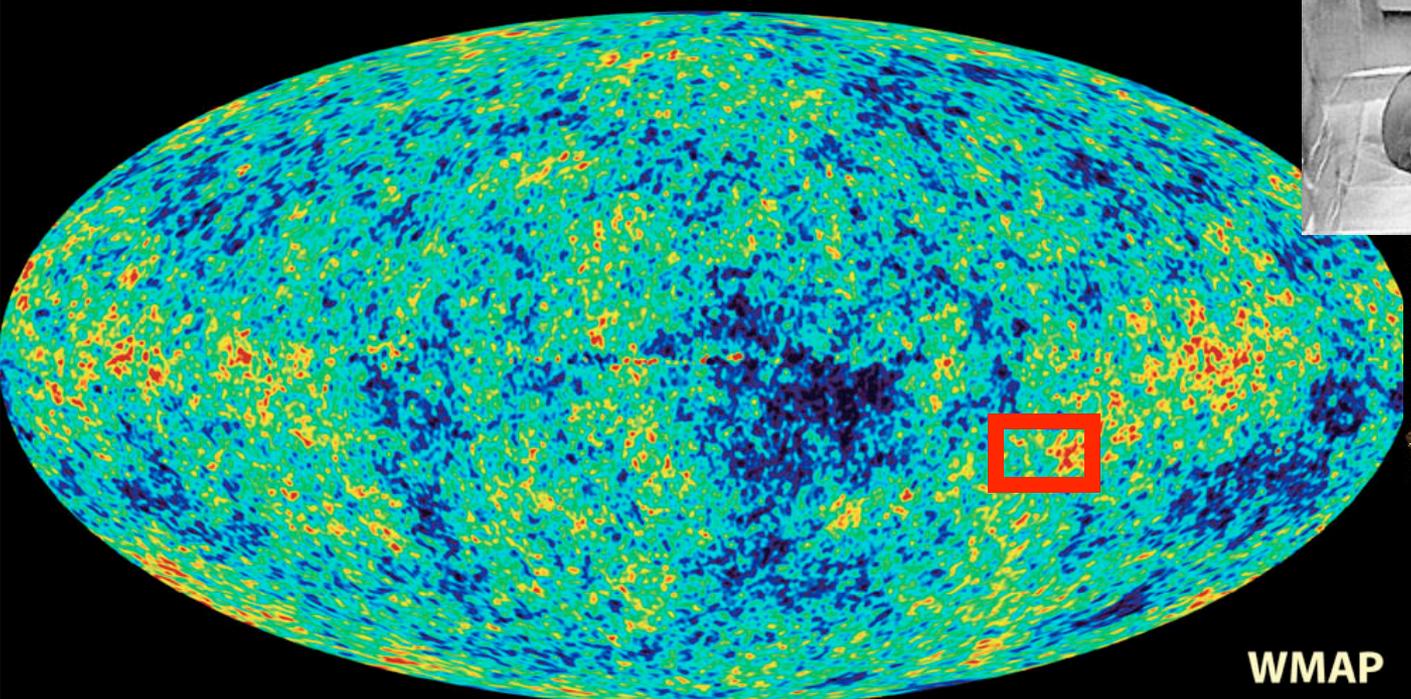


COBE/DMR:
CMB + Galactic @ 7°

is this a statistically isotropic Gaussian random field, when account is taken of the Milky Way emissions & extra-galactic sources?
yes! maybe?



COBE 1992/96



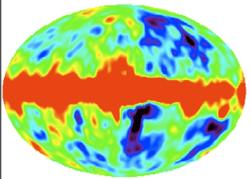
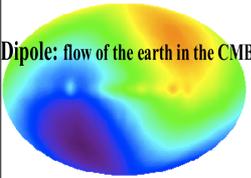
**Feb03
Mar06
Mar08**

WMAP

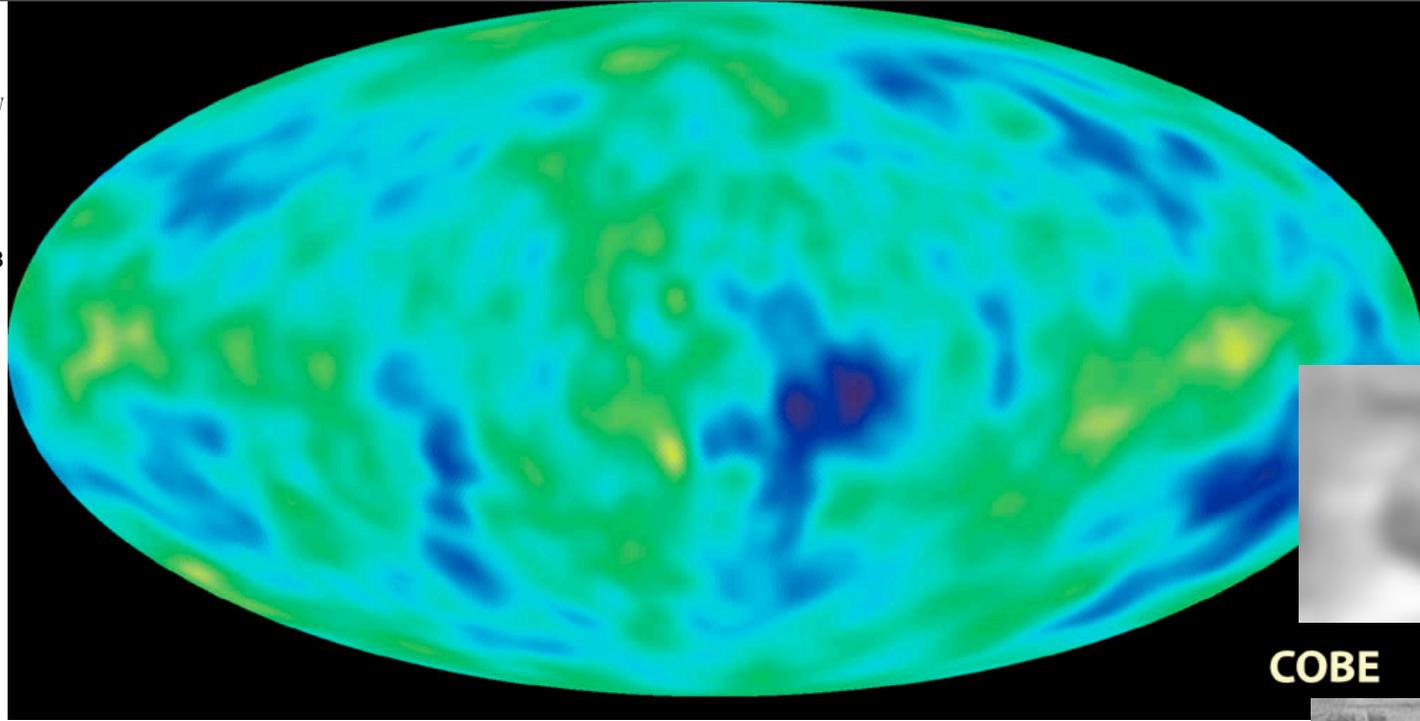
CMB

Nearly Perfect Blackbody
 $T=2.725 \pm .001$ K COBE/FIRAS

Dipole: flow of the earth in the CMB



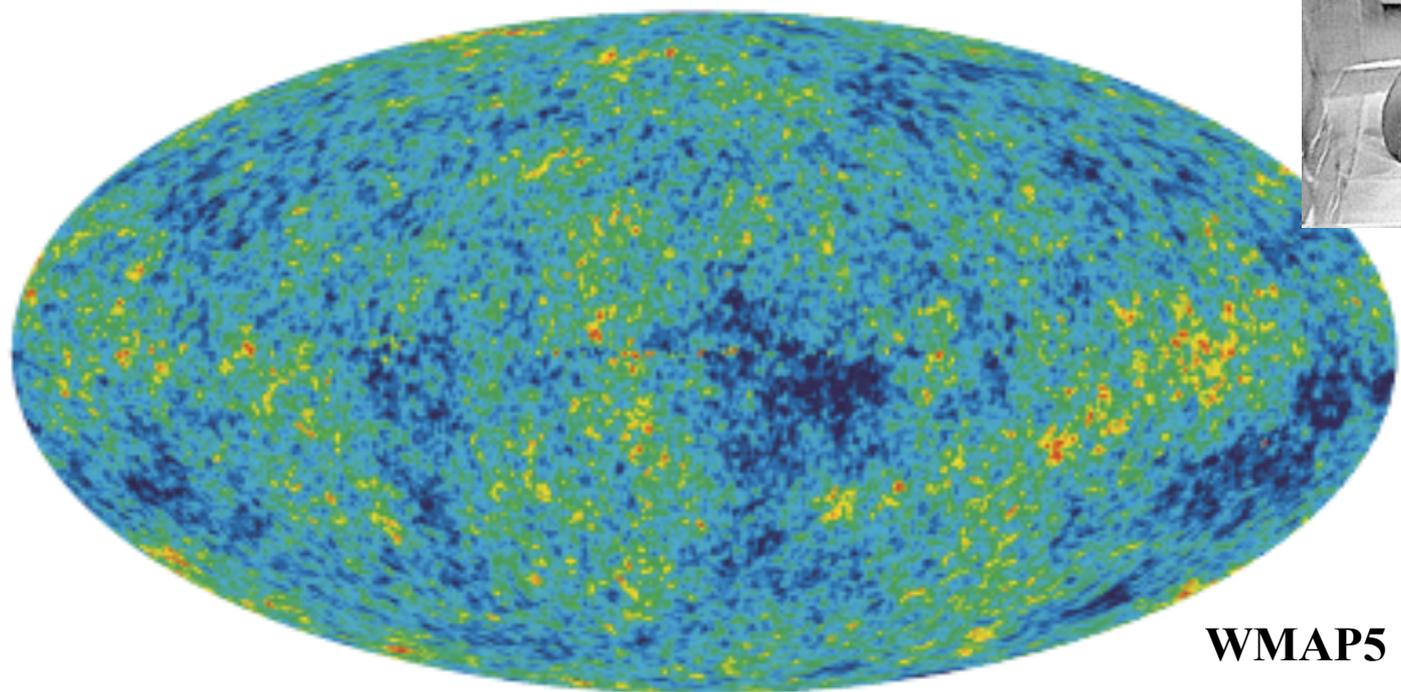
COBE/DMR:
CMB + Galactic @7°



COBE 1992/96



**Planck satellite
April09
launch**

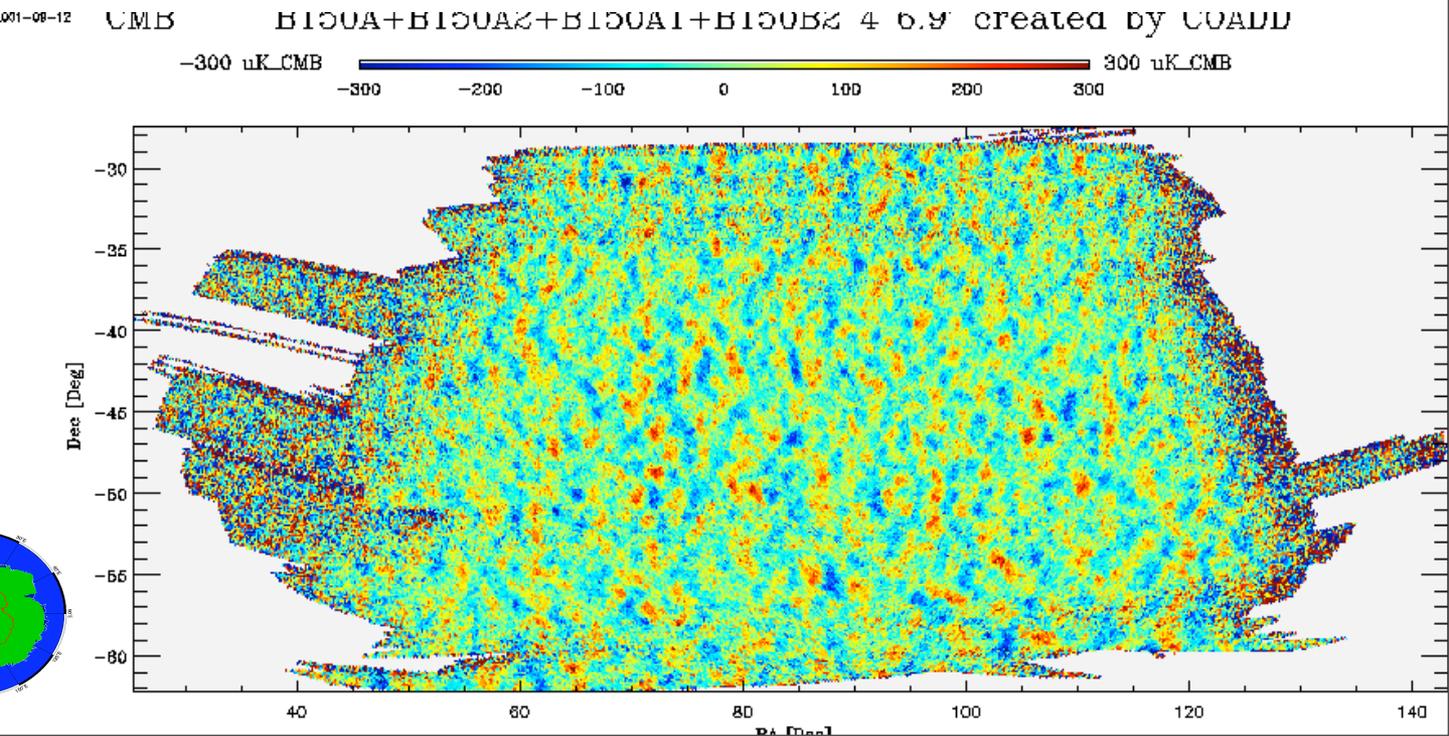
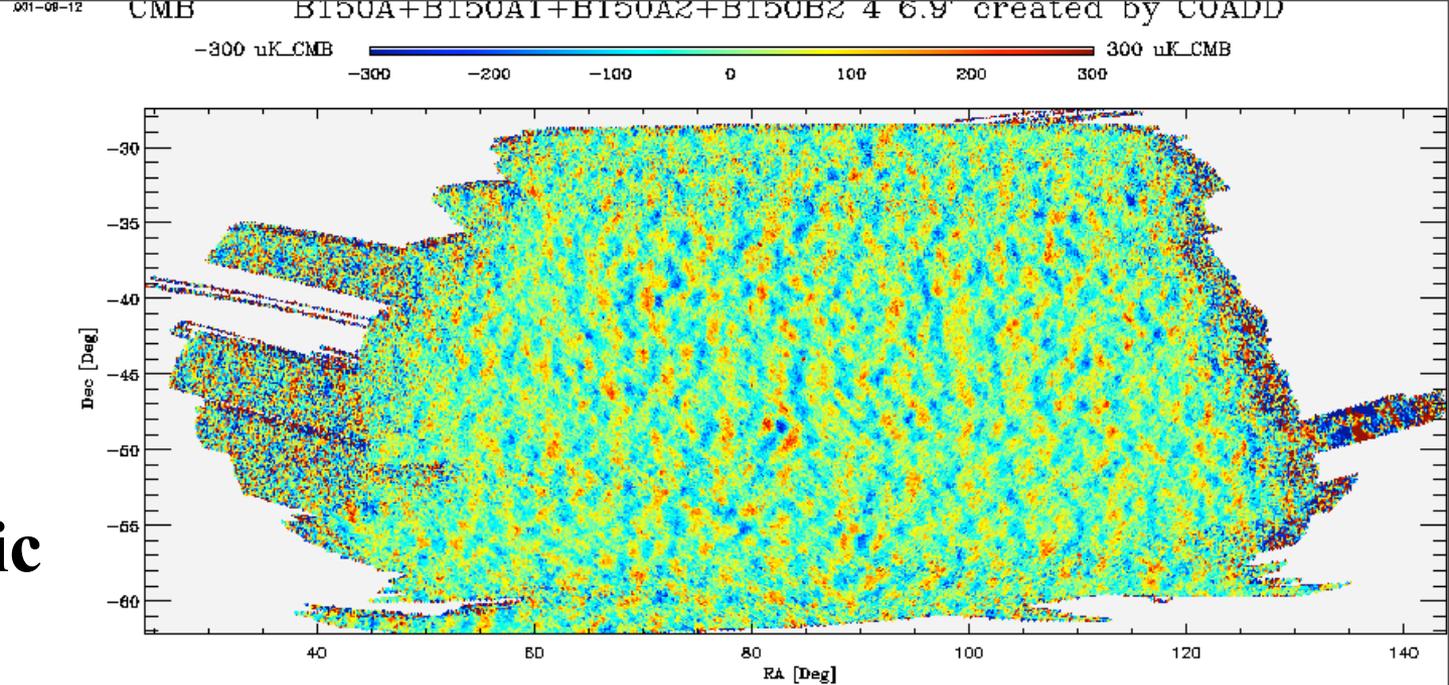
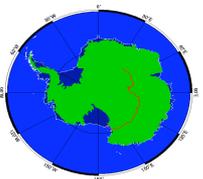


**WMAP5
Feb03
Mar06
Mar08**

Boomerang
@150GHz is
(nearly)
Gaussian:
Simulated vs
Real

thermodynamic
CMB

temperature
fluctuations
2.9% of sky
 $\Delta T \sim 30$ ppm



Random Fields in Early Universe Cosmology

Dick Bond @



CITA
ICAT

Canadian Institute for
Theoretical Astrophysics
L'institut canadien
d'astrophysique theorique



What was the Universe made of & how was it distributed?

Are there primordial non-Gaussian components - subdominant inflation-induced, preheating-induced or cosmic-string induced?

THEN: coherent inflaton / "vacuum" energy + **zero-point fluctuations** in all fields (*Gaussian RF*) & then preheat via mode coupling to incoherent cascade to thermal equilibrium soup

very early U early to middle to now U **very late U**

string theory/landscape/higher dimensions

inflation cyclic

$$V_{\text{eff}}(\psi_{\text{inf}}) ?$$

$$K_{\text{eff}}(\psi_{\text{inf}}) ?$$

trajectory
probability

$$-d \ln \rho_{\text{tot}} / d \ln a \quad / 2$$

$$= \mathcal{E}(k) = 1 + q, \quad k \sim H a$$

baryogenesis dark matter BBN γ dec

dark energy

$$V_{\text{eff}}(\psi_{\text{inf}}) ?$$

$$K_{\text{eff}}(\psi_{\text{inf}}) ?$$

cosmic mysteries

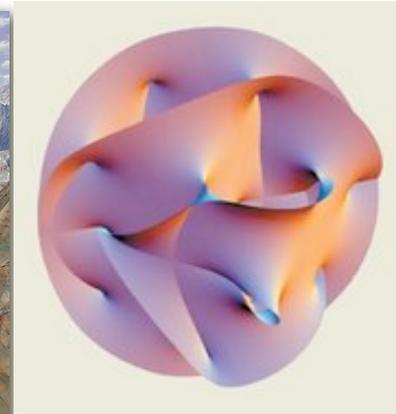
$$n_b/n_\gamma \quad \rho_{\text{dm}}/\rho_b \quad z_{\text{eq}}/z_{\text{rec}} \quad \rho_{\text{curv}} \quad \rho_{\text{de}}/\rho_{\text{dm}} \quad \rho_{\text{de}} \sim H^2 M_{\text{Planck}}^2 \quad \rho_{\text{mv}}/\rho_{\text{stars}}$$

Old view: Theory prior = delta function of THE correct one and only theory

New view: Theory prior = probability distribution on an energy landscape whose features are at best only glimpsed,

huge number of potential minima, inflation the late stage flow in the low energy structure toward these minima. Critical role of collective coordinates in the low energy landscape:

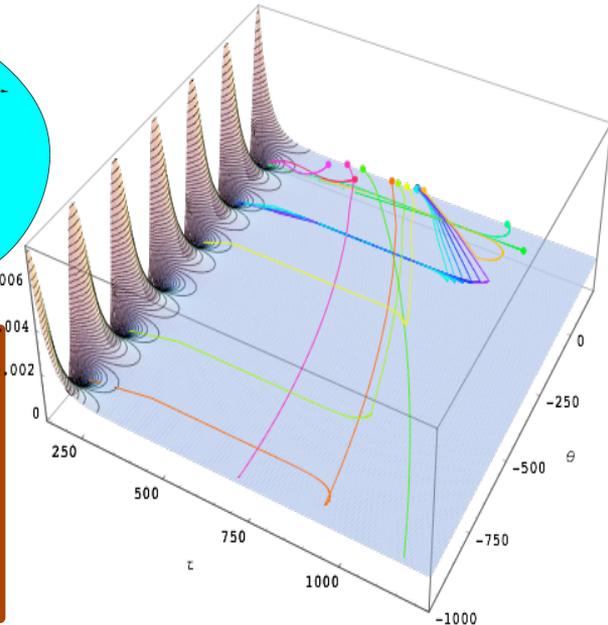
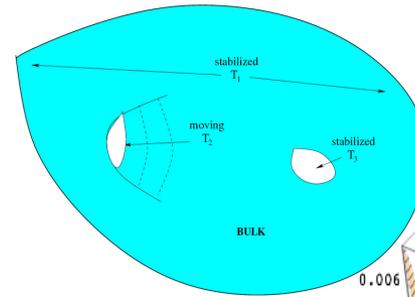
moving brane/antibrane separations (D3,D7) moduli fields, sizes and shapes of geometrical structures such as holes in a dynamical extra-dimensional (6D) manifold approaching stabilization



Roulette inflation Kahler moduli/axion

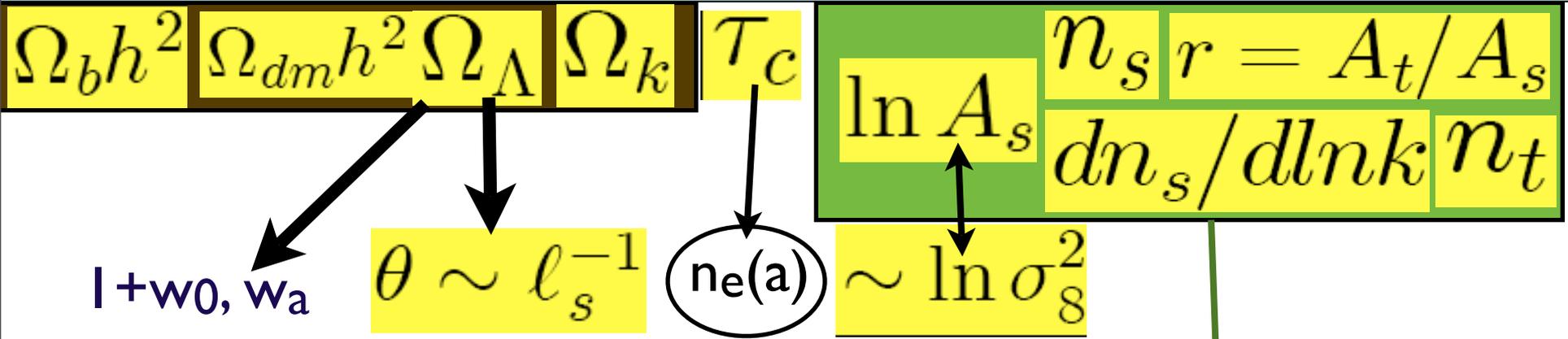
The 'house' does not just play dice with the world.

{Number of E-folds: 29, 211, 4, 12, 2, 285, 105, 8, 11, 18, 30, 53, 106, 0, 0, 0}



theory prior ~ probability of trajectories given potential parameters of the collective coordinates
X probability of the potential parameters X
probability of initial conditions

Standard Parameters of Cosmic Structure Formation



primordial non-Gaussianity
 $\Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + \mathbf{f}_{NL} (\Phi_G^2(\mathbf{x}) - \langle \Phi_G^2 \rangle)$
 local smooth \rightarrow

DBI inflation: non-quadratic kinetic energy
 cosmic/fundamental strings/defects
 from end-of-inflation & preheating

$\Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + F_{NL}(\chi_b) - \langle F_{NL} \rangle$
 resonant preheating

$\ln P_s(\ln k)$ & $\ln P_t(\ln k)$
 & $r(k_p)$

+ subdominant
 isocurvature/ cosmic
 string/ tSZ ...

Observables and conclusions

$$\Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + f_{\text{NL}} (\Phi_G^2(\mathbf{x}) - \langle \Phi_G^2 \rangle)$$

local quadratic non-G constraint: $-9 < f_{\text{NL}} < 111 \Rightarrow -4 < f_{\text{NL}} < 80$ WMAP5 ($\pm 5-10$ Planck1yr)

$$\Rightarrow \Phi(\mathbf{x}) = \Phi_G(\mathbf{x}) + F_{\text{NL}}(\chi_b) - \langle F_{\text{NL}} \rangle$$

resonant preheating form

modulated curvature fluctuations from preheating are superimposed on the usual curvature fluctuations from the inflaton

the peak values have $\delta \ln a \sim 10^{-5} \Rightarrow$ comparable to standard Gaussian

temperature fluctuations, but spiky $F_{\text{NL}} \Rightarrow$ non-Gaussian?

As long as $g^2/\lambda \leq O(1)$, the χ field has very long wavelength perturbations (similar to, but uncorrelated with, the inflaton field)

Large Scale Structure statistics of spiky F_{NL} mapping: under investigation

Rich possibilities in theory space & on the sky

e.g., $F_{\text{NL}}(\chi) \sim \sum_p F_p \exp(-(\chi_p - \chi)^2 / 2\gamma_p^2) \Rightarrow$ e.g., $\langle \delta F_{\text{NL}} | \chi_{\text{LF}} \rangle \sim \sum_p \beta_p \chi_{\text{LF}}$,
but non-G is possible.

INFLATION NOW

PROBES NOW

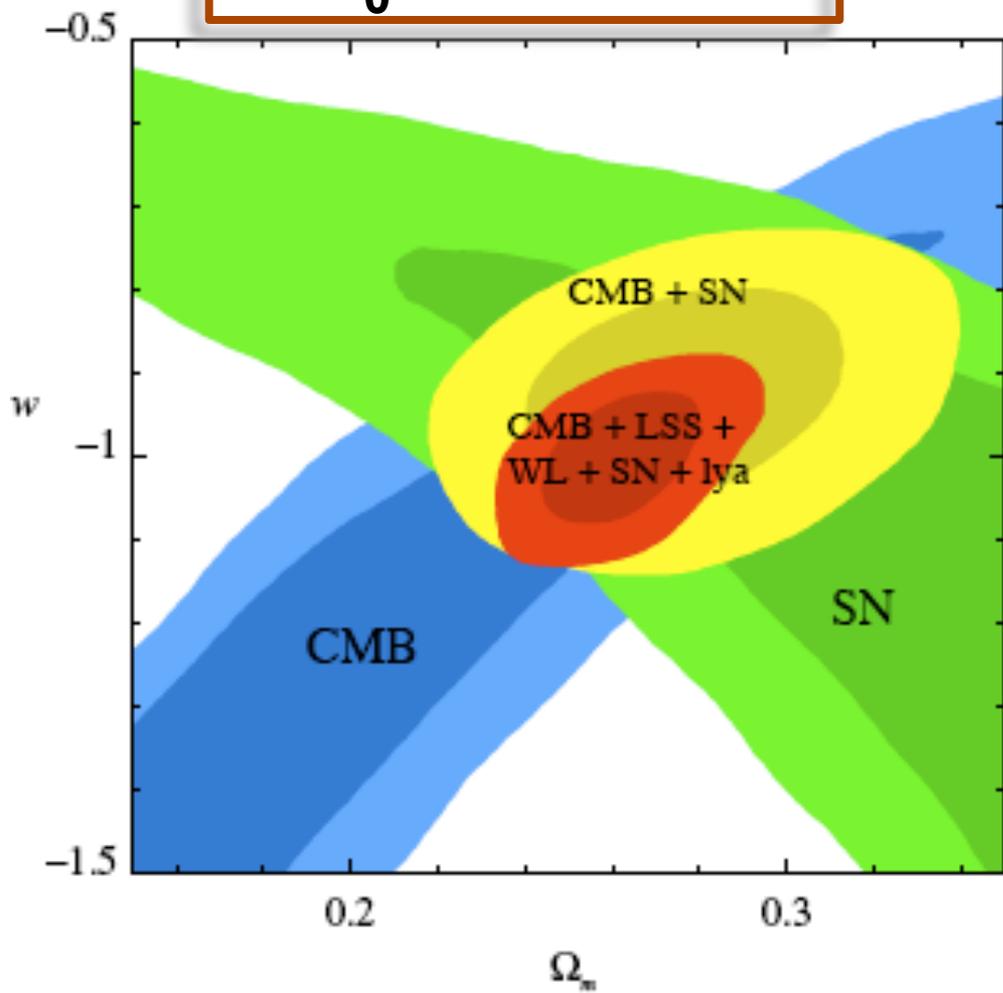
$$1 + \mathbf{w}_0 = -0.0 \pm 0.06$$

$$w(a) \equiv \frac{p(a)}{\rho(a)}$$

$$\mathbf{w}(a) = \mathbf{w}_0 + \mathbf{w}_a(1-a)$$

$$1 + \mathbf{w}_0 = -0.01 \pm 0.19$$

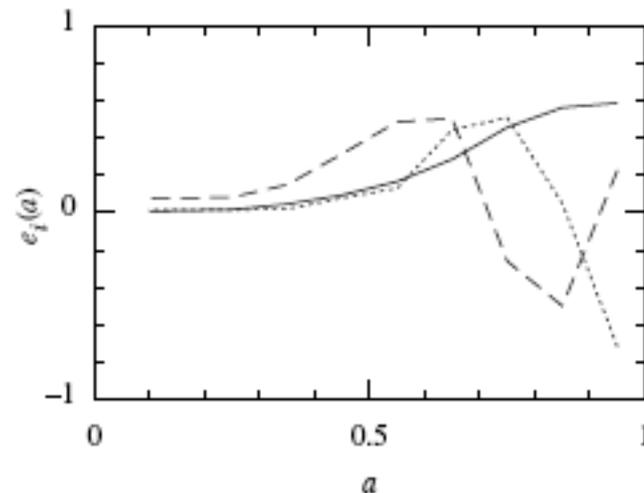
$$\mathbf{w}_a = 0.0 + 0.6 - 0.8$$



piecewise parameterization
 4,9,40 modes in redshift
 9 & 40 into Parameter eigenmodes

data cannot determine >2 EOS parameters
 DETF Albrecht etal06, Crittenden etal06, hbk08

$$\sigma_1 = 0.13 \quad \sigma_2 = 0.33 \quad \sigma_3 = 0.58$$



$$\epsilon_{\phi_0} = 0.0 \pm 0.09 \text{ if constant, } \epsilon_{\phi_0} = -0.015 \pm 0.3 \text{ if a-linear model}$$

➤ Cosmological
Constant ($w=-1$)

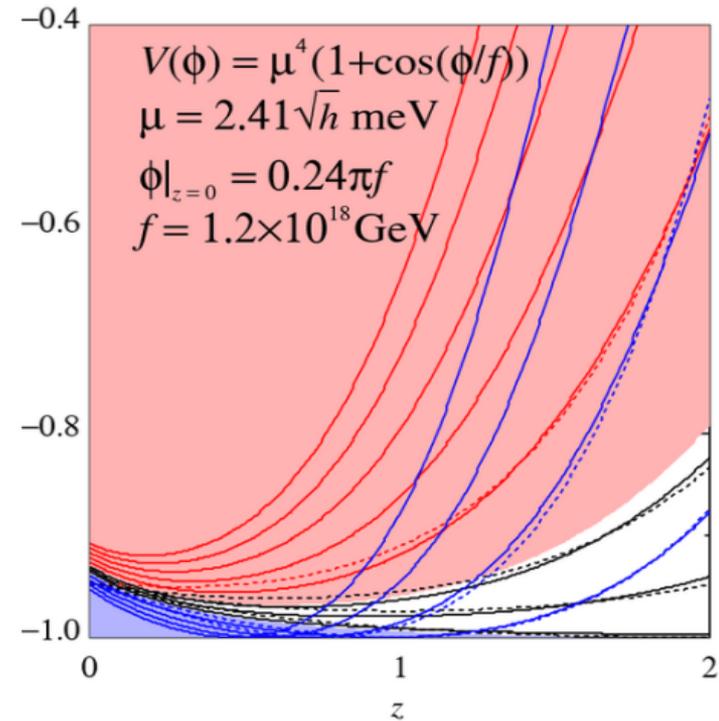
➤ Quintessence
($-1 \leq w \leq 1$)

➤ Phantom field
($w \leq -1$)

➤ Tachyon fields
($-1 \leq w \leq 0$)

➤ K-essence
(no prior on w)

INFLATION NOW PROBES NOW



trajectory probability: ~ 1 e-fold \Rightarrow blind is bad \Rightarrow slow-to-moderate roll $++$

$$-\frac{d \ln \rho_\phi}{d \ln a} / 2$$

$$= \epsilon_\phi(a) = (1+w)/2$$

$$= \epsilon_s f(a/a_{\Lambda \text{eq}}; a_s/a_{\Lambda \text{eq}}; \zeta_s)$$

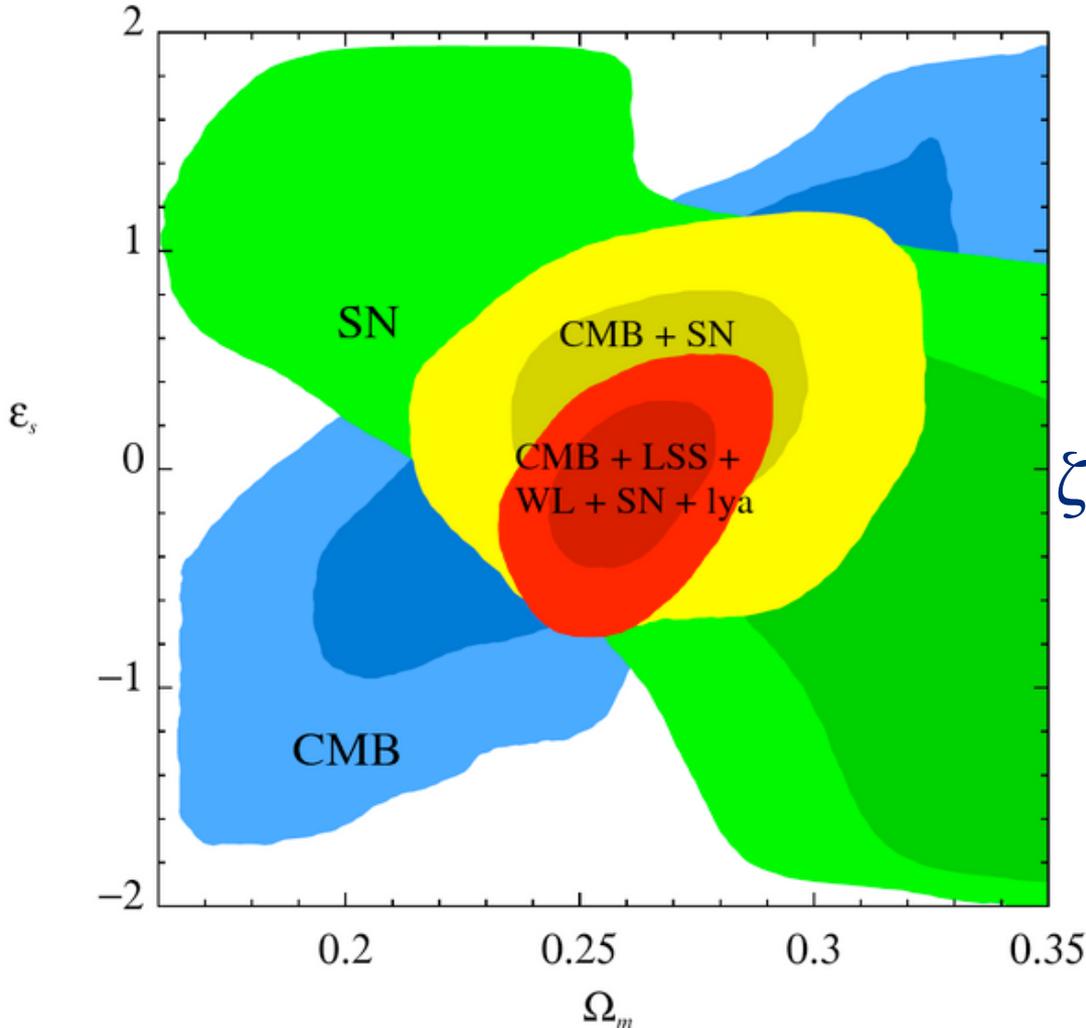
$$\epsilon_s = (d \ln V / d \psi)^2 / 4 @ \text{pivot } a_{\text{eq}}$$

$$\zeta_s = \pm 1.001 d^2 \ln V / d \psi^2 / 4 @ \text{pivot } a_{\text{eq}}$$

$$\zeta_s = d \ln \epsilon_s / d \ln a \times 1/2 @ \text{pivot } a_{\text{eq}}$$

measuring ϵ_s ζ_s $a_s=0$ tracking (SNe_{union}+CMB

wmap5+acbar+cbi5yr+b03+ **+WL**_{cfhtls+cosmos} **+LSS**_{sdssRG+2dF+Lya})



$$\epsilon_s = (d \ln V / d \psi)^2 / 4 \text{ @pivot } a_{eq}$$

$$\epsilon_s = .01 + .25 - .28 \quad 1$$

$$-.03 + .21 - .25 \quad 3$$

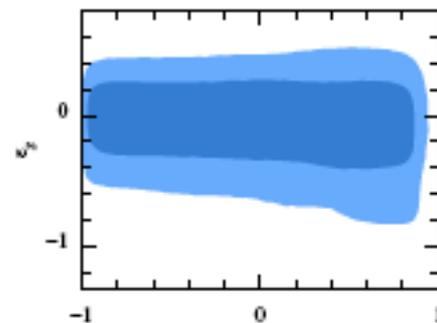
$$-.03 + .26 - .30 \quad 2$$

$$\zeta_s = +1.001 d^2 \ln V / d \psi^2 / 4 \text{ @pivot } a_{eq}$$

$$\zeta_s = d \ln \epsilon_s / d \ln a \times 1/2 \text{ @pivot } a_{eq}$$

ill-determined now

$$0.1^{+0.6}_{-0.7}$$



cannot reconstruct the quintessence potential, just the slope ϵ_s & ~hubble drag

Beyond Einstein panel: LISA+JDEM

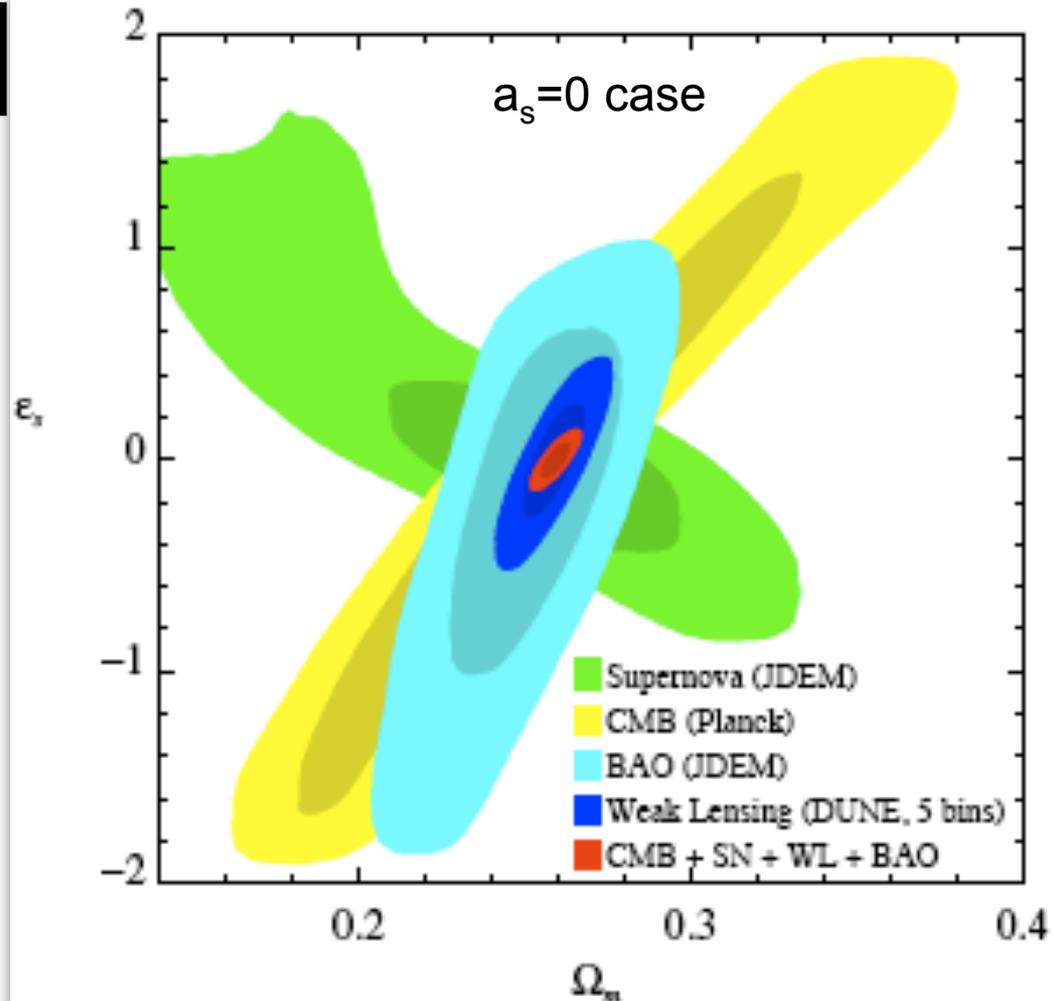
Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)

+ **DUNE-WL** (50% sky, gals @z = 0.1-1.1, 35/min²) + **Planck1yr**
now ESA /Eucid ESA (+NASA/CSA)

INFLATION NOW PROBES THEN

$$\epsilon_s = 0.00^{+0.07}_{-0.06}$$

$$\zeta_s \sim d \ln \epsilon_s / d \ln a \approx 0.1^{+0.6}_{-0.7}$$



cannot reconstruct the quintessence potential, just the slope ϵ_s & ~hubble drag

end2

**FLUCTUATION
GENERATOR**



**LINEAR
AMPLIFIER**



**NONLINEAR
DISSIPATIVE
AMPLIFIER**

statistically homogeneous & isotropic
Gaussian Random Fields => 2-point
power spectra fns of 3D wavenumber $|\mathbf{k}|$

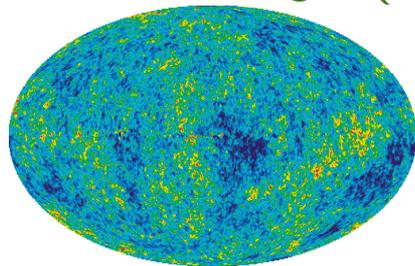
quantum noise

$P_{\Phi}(\mathbf{k}), P_{\text{GW}}(\mathbf{k})$

$\Delta T_{(\text{LM})}$

$P_{\rho}(\mathbf{k}), P_{\mathbf{v}}(\mathbf{k})$

$P_{\text{gal}}(\mathbf{k}), P_{\text{cl}}(\mathbf{k})$

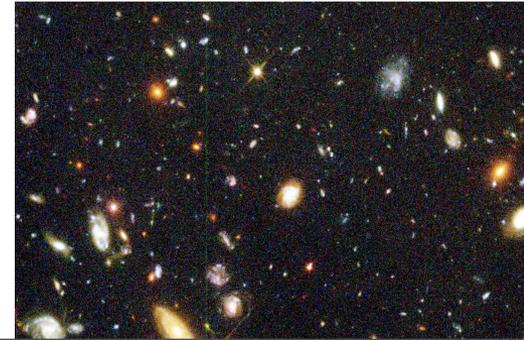


Cosmic Microwave Background Radiation
statistically isotropic all-sky GRF on the 2-sphere

$$C_L = \langle |\Delta T_{(\text{LM})}|^2 \rangle, \quad k_{2D} \sim L + 1/2$$

gastro-physics
aka "sub-grid" aka astronomy
nonlinear objects of various
types & their clustering
properties, N-point statistics

$n_{\text{gal}} \quad n_{\text{cl}} \dots$
 $n_{\text{halos}} \quad n_{\text{peaks}}$



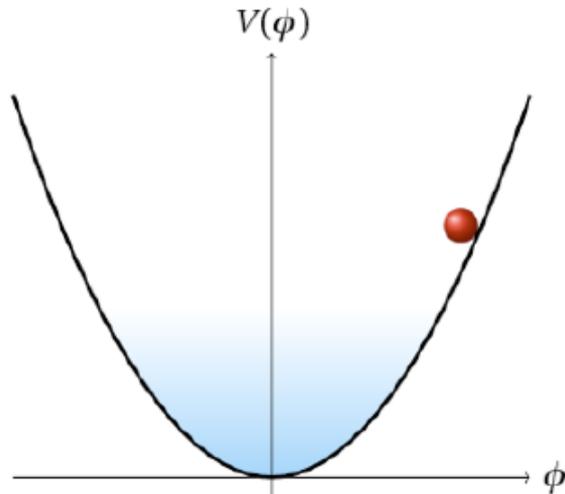
preheating

Parametric resonance

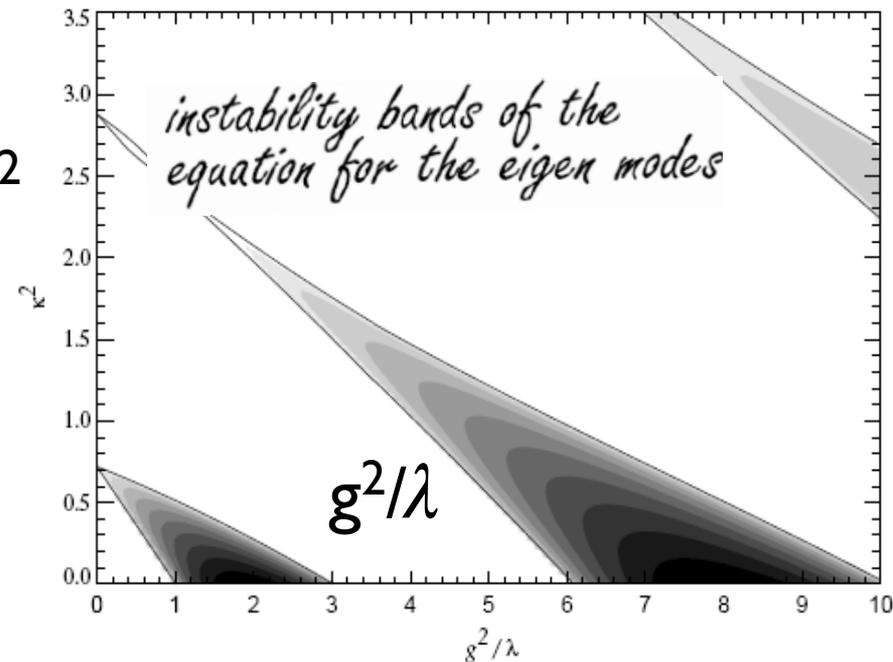
$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

90s Kofman, Linde, Starobinsky, ..., Greene, Felder, Frolov, ... 00s

$$\ddot{\chi}_k + 3\frac{\dot{a}}{a}\dot{\chi}_k + \left(\frac{k^2}{a^2} + g^2\phi^2\right)\chi_k = 0$$



$\sim k^2$

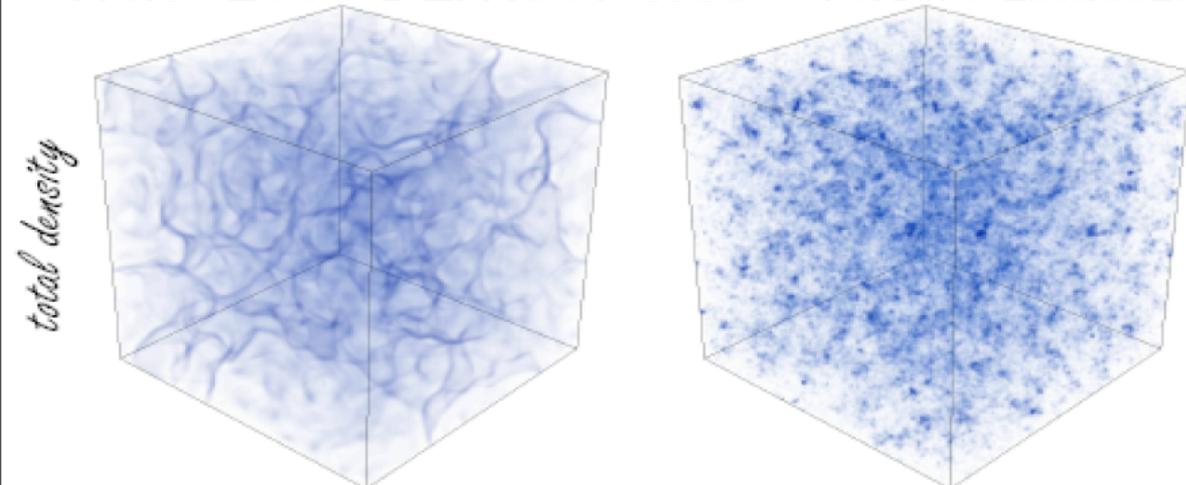
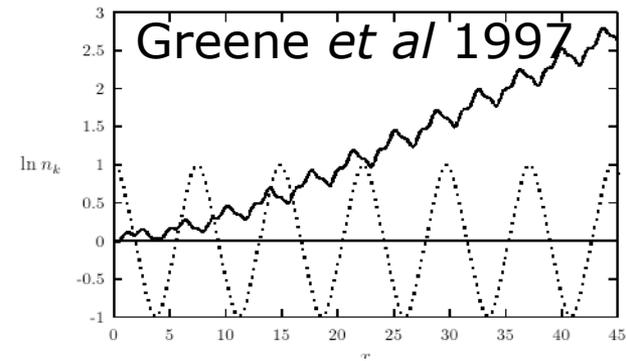


The oscillating inflaton modulates the mass of the fields coupled to it, and becomes unstable through parametric resonance.

Formation of Structure

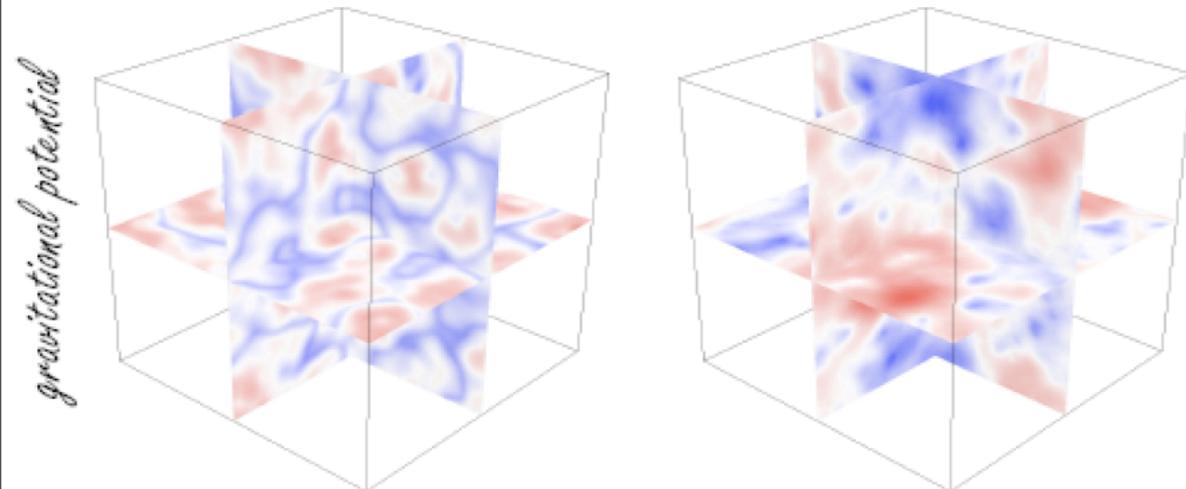
*Linear instability amplifies seed fluctuations and creates structure;
its non-linear evolution looks like LSS but is driven by repulsion!*

Frolov 2008 DEFROST code \approx Felder's LatticeEasy



bubbles form...

... then break into blobs



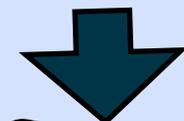
potential traces dense bubble walls and empty interiors...

... the structure grows larger due to repulsive field interactions

Bond, Andrei Frolov, Zhiqi Huang, Kofman 09:

results depend upon the input value of a uniform χ_b , a random Gaussian variable with variance $\sim H_b/2\pi$

(uncorrelated with inflaton $\delta\phi \sim H_b/2\pi$ fluctuations)

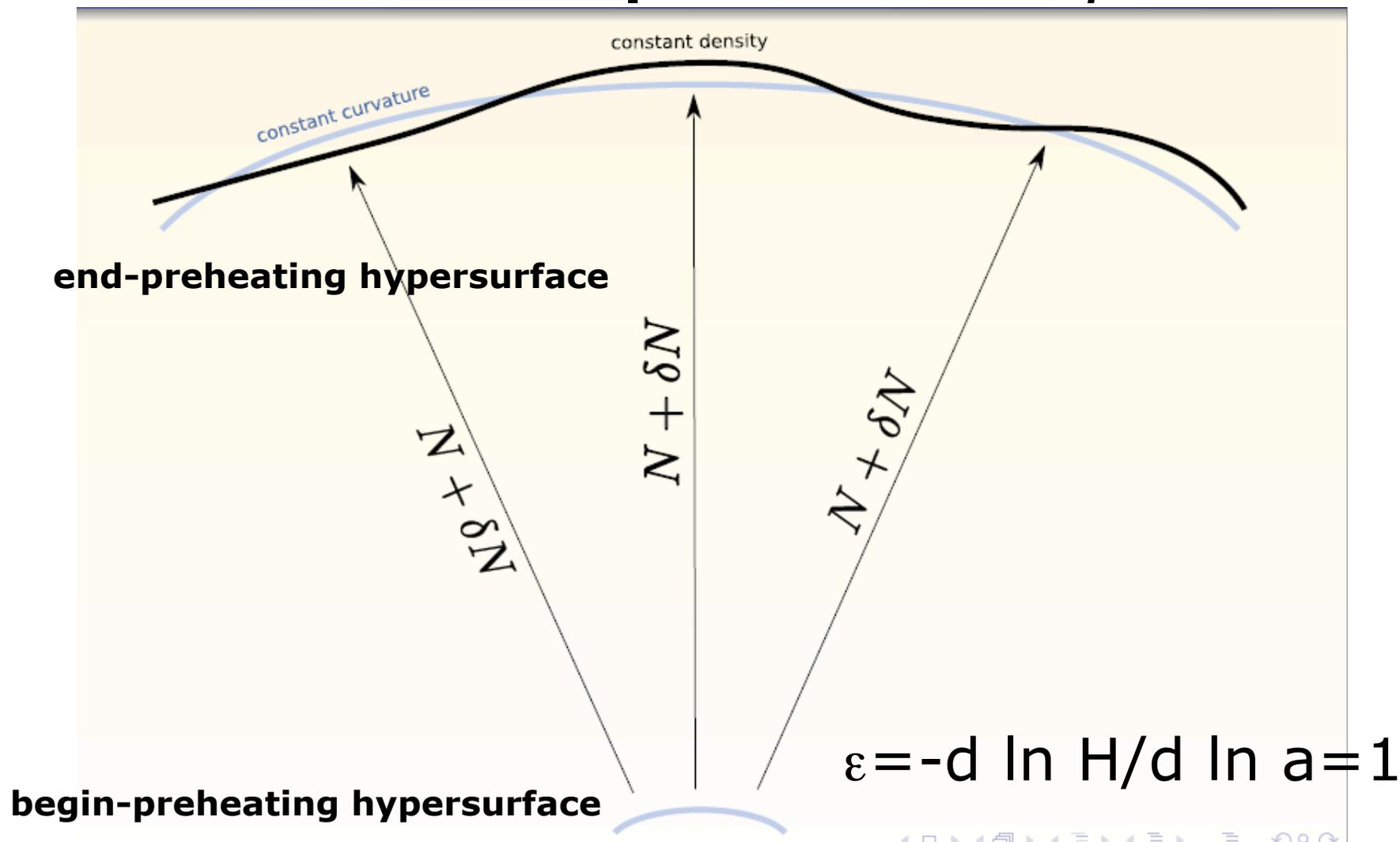


non-Gaussianity from preheating

$$\chi_b(x,t) + \chi_f$$

calculate how the time from the end of accelerated expansion (end of inflation) to the onset of thermal equilibrium depends on $\chi_b(\mathbf{x}, t)$

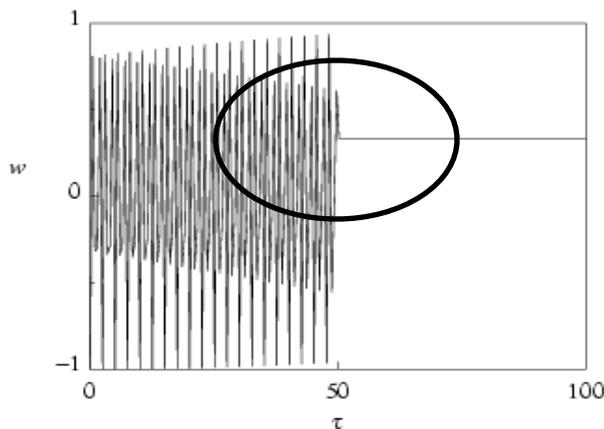
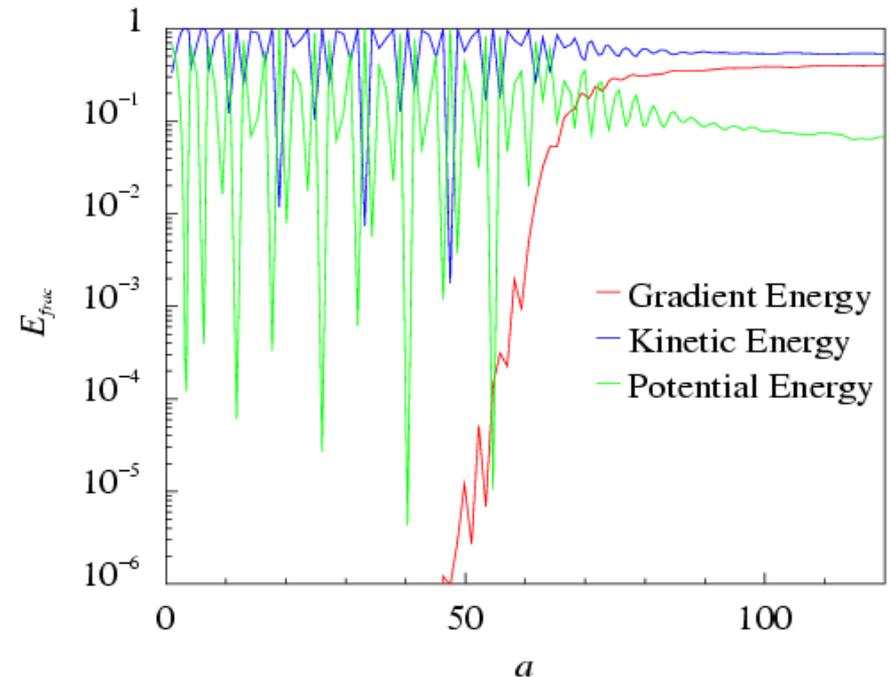
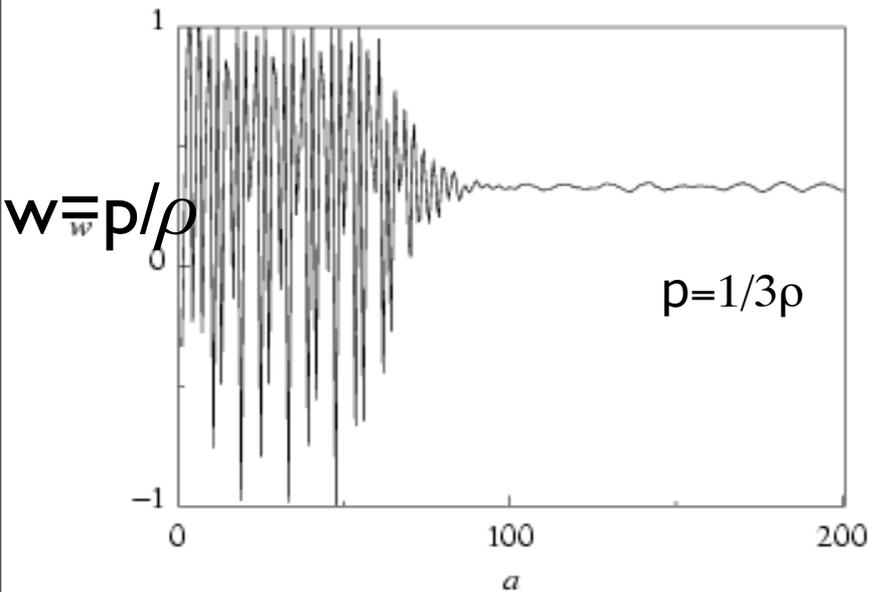
$$-\delta N = \delta \ln a|_H = \text{curvature fluctuation}$$



equation of state evolution via simulation: pass from $w \approx -1$ potential-dominated coherence via oscillation & mode cascade to $w=1/3$ thermal equilibrium

simulation size 128^3

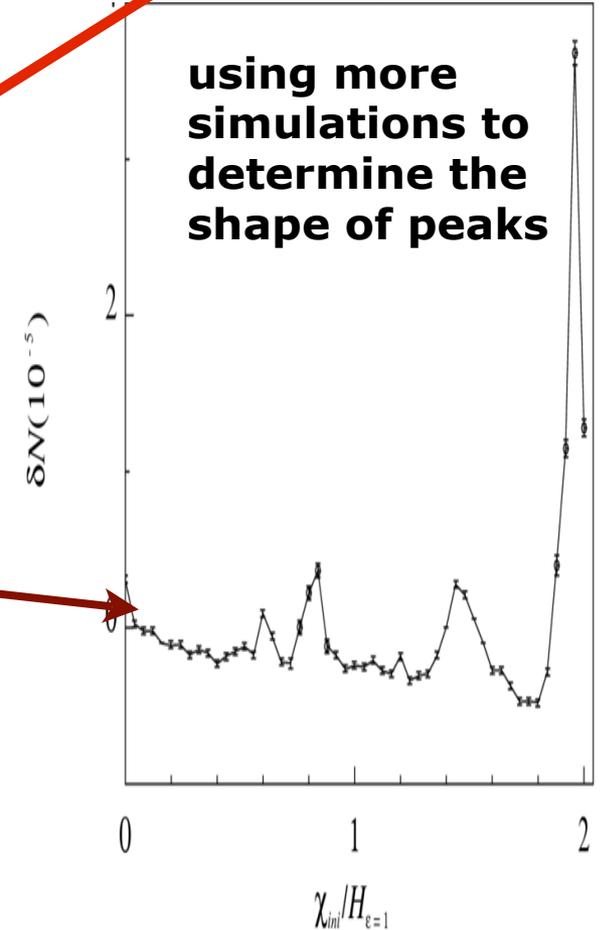
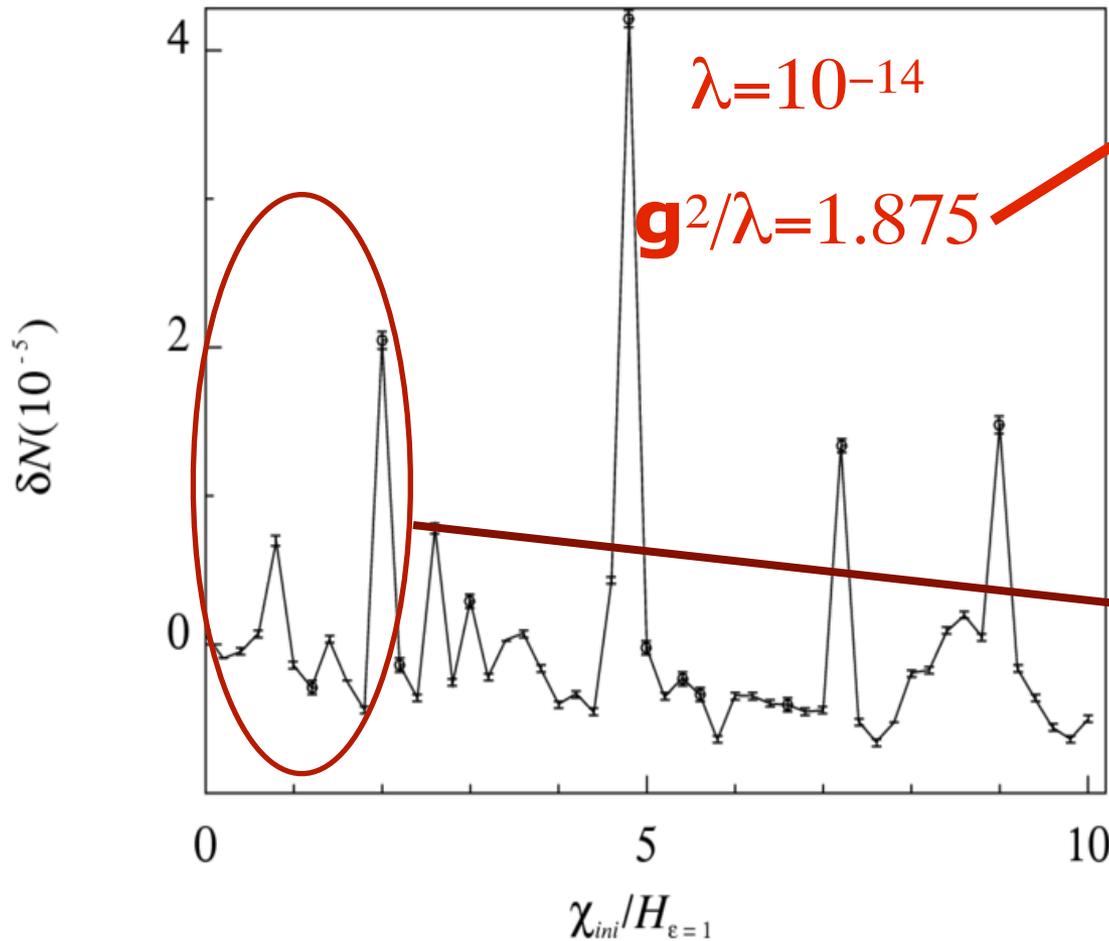
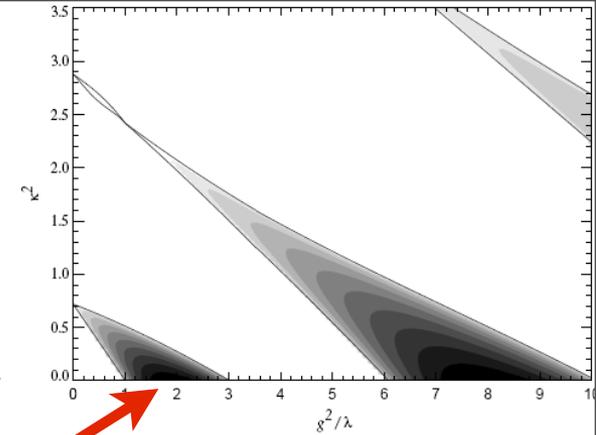
$\chi_b = 0$



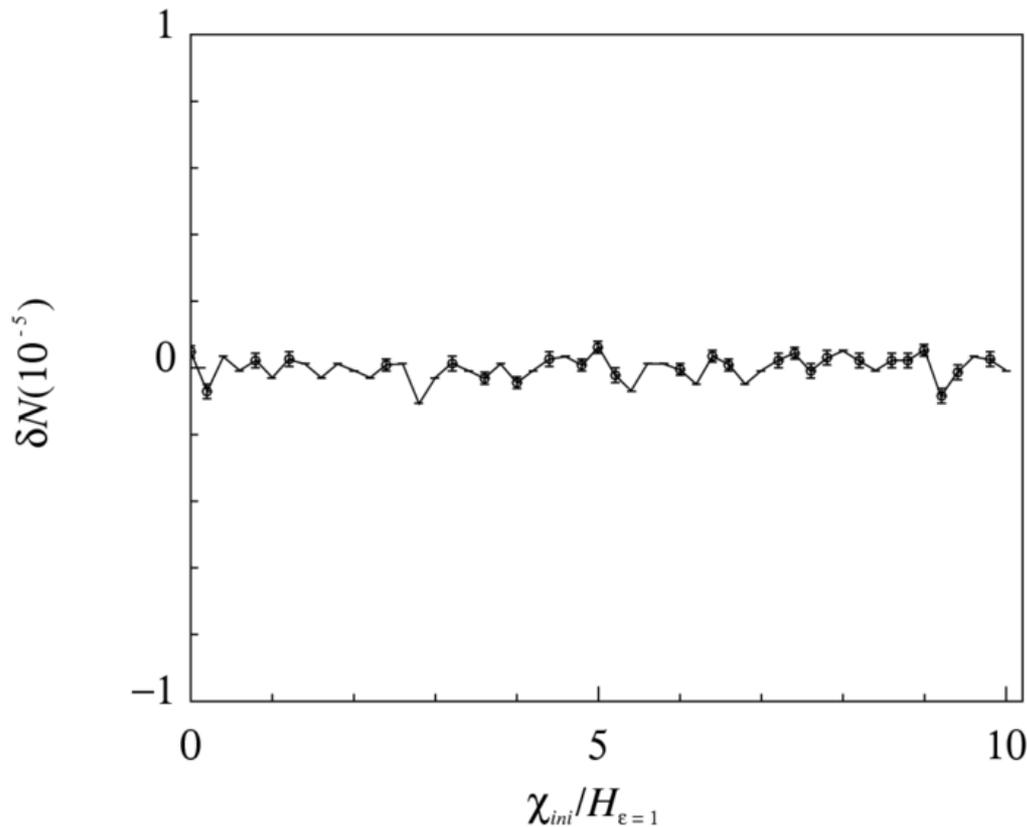
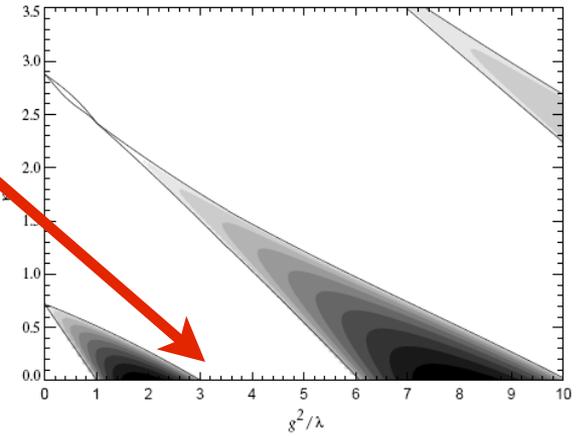
We search for ppm effects
 \Rightarrow Symplectic DEFROST:

energy conservation $\sim 10^{-13}$ level!!
 cf. DEFROST $\sim 10^{-5}$ level & Felder's LatticeEasy
 $\sim 10^{-4}$ level.

$\delta \ln a(\chi_b)$ modulation: response to varying $\chi_b(x, t_e)$



if the $k=0$ mode is not in the parametric resonance bands ($g^2/\lambda=3$ example)
then $\delta \ln a$ is not modulated by χ_b



Other tests: UV and IR cutoffs ok →

END

Constraining Trajectories of Dark Energy Inflatons

Inflation Now $\epsilon_\phi(a) = \epsilon_s f(a/a_{\Lambda\text{eq}}; a_s/a_{\Lambda\text{eq}}; \xi_s)$

$\epsilon_\phi = -d \ln \rho_\phi / d \ln a / 2 \sim 0$ now, to $\epsilon = -d \ln \rho_{\text{tot}} / d \ln a / 2 \sim 0$ to 2, 3/2, $\sim .4$

cf. $w(a)$: w_0, w_a ; w in z-bands or z-modes; $\epsilon(a)$: in modes, jerk

~ 1 good e-fold. only ~ 2 params. priors matter

Inflation Then $\epsilon(k) = (1+q)(a) =$ mode expansion in resolution ($\ln H a \sim \ln k$)
 $\sim r/16$ (Tensor/Scalar Power & gravity waves) ~ 10 good e-folds CMB+LSS

Cosmic Probes Now CMB(Apr08), CFHTLS SN(Union 307), WL, LSS/BAO, Ly α

Cosmic Probes Then JDEM-SN + DUNE-WL + Planck1

Zhiqi Huang, Bond & Kofman 09 $\epsilon_s = -0.03 \pm 0.28$ now, inflaton (potential gradient)²

to ± 0.07 then Planck1+JDEM SN+DUNE WL, weak $a_s < 0.36$ now < 0.21 then

3-parameter formula

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

+ Friedmann Eqn+DM+B

$$\theta \equiv \begin{cases} \sin^{-1} \frac{\dot{\phi}}{\sqrt{2\rho_{\phi}}} \\ \sinh^{-1} \frac{\dot{\phi}}{\sqrt{2\rho_{\phi}}} \end{cases}$$

$$w(a) = -1 + \frac{2\epsilon_s}{3} \left\{ \frac{\left(\frac{a_s}{a}\right)^{3-3.6a_s|\epsilon_s|(1-\Omega_{m0})}}{\sqrt{1 + \frac{\epsilon_s}{3|\epsilon_s|} \left(\frac{a_s}{a}\right)^{6-7.2a_s|\epsilon_s|(1-\Omega_{m0})}}} \frac{1}{\sqrt{|\epsilon_s|}} \right. \\ + \left[\sqrt{1 + \left(\frac{a_{eq}}{a}\right)^3} - \left(\frac{a_{eq}}{a}\right)^3 \ln\left(\left(\frac{a}{a_{eq}}\right)^{\frac{3}{2}} + \sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3}\right) \right] (1 - \zeta_s) \\ + 0.36\epsilon_s(1 - \Omega_{m0}) \frac{\left(\frac{a}{a_{eq}}\right)^2}{1 + \left(\frac{a}{a_{eq}}\right)^4} \left[0.9 - 0.7\frac{a}{a_{eq}} - 0.045\left(\frac{a}{a_{eq}}\right)^2 \right] \\ \left. + \frac{2\zeta_s}{3} \left[\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 2\left(\frac{a_{eq}}{a}\right)^3 \left(\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 1 \right) \right] \right\}^2$$

accurate fits to slow-to-moderate roll & even wild rising baroque late-inflaton trajectories + thawing & freezing trajectories. non-oscillating

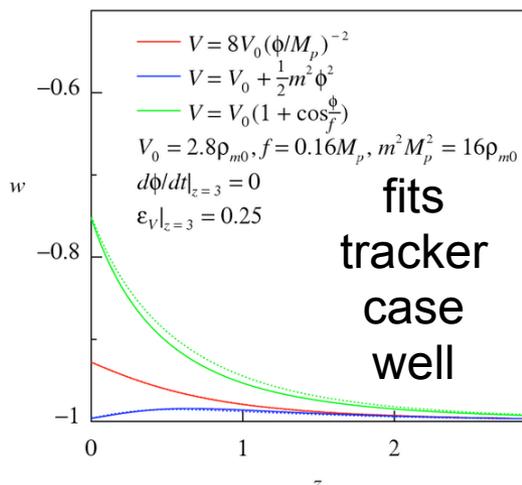
where

- ~15% thawing, 8% freezing, with flat priors

$$a_{eq} \equiv \left(\frac{\Omega_{m0}}{1 - \Omega_{m0}} \right)^{\frac{1}{3[1-0.36\epsilon_s(1-\Omega_{m0})]}}$$

$$a_s \geq 0$$

$$\sqrt{|\epsilon_V|} = \sqrt{|\epsilon_s|} \left[1 + \zeta_s \left(\left(\frac{a}{a_{eq}} \right)^{\frac{3}{2}} - 1 \right) \right] \quad -1 < \zeta_s < 1$$



very early U

early to middle to now U

very late U

inflation

string theory/landscape/higher dimensions

dark energy

$V_{\text{eff}}(\psi_{\text{inf}})$? partial shape reconstruction

reconstruct gradient $V_{\text{eff}}(\psi_{\text{inf}})$?

$K_{\text{eff}}(\psi_{\text{inf}})$?

$K_{\text{eff}}(\psi_{\text{inf}})$?

$$1 - n_s \sim 2\varepsilon_s + 4\zeta_s \quad x.999 \quad \& \quad r \sim 16\varepsilon_s \quad \text{slow roll}$$

2 solutions: nearly uniform acceleration & small ζ_s

$$\varepsilon_s \sim .017 \pm .007; \quad \varepsilon_s < .025 \quad 95\% \text{ from } r$$

low energy inflation with tiny ε_s

$$2\zeta_s \sim .017 \pm .007$$

errors go to $\pm .0012$ Planck+JDEM+DUNE

$$\varepsilon_s = (d \ln V / d \psi)^2 / 4 \quad @ a_{\text{eq}}$$

$$\varepsilon_s \sim -.03 + .26 -.30$$

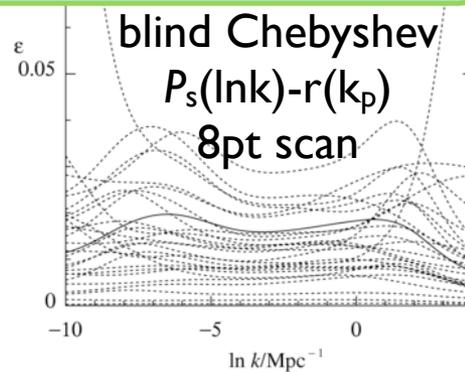
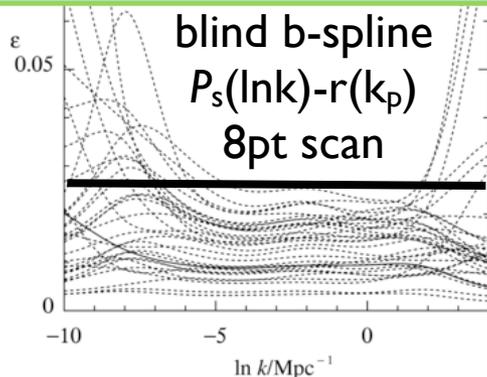
to $\pm .07$ Planck+JDEM+DUNE

$$\zeta_s = \pm 1.001 d^2 \ln V / d \psi^2 / 4 \quad @ a_{\text{eq}}$$

$$\zeta_s \sim 0.1 + .6 -.7$$

to $+.6-.7$ Planck+JDEM+DUNE **LCDM**

to $+.3-.3$ steep-ish $\exp[-\psi]$



very early U

early to middle to now U

very late U

inflation

string theory/landscape/higher dimensions

dark energy

$V_{\text{eff}}(\psi_{\text{inf}})$? partial shape reconstruction

reconstruct gradient $V_{\text{eff}}(\psi_{\text{inf}})$?

$K_{\text{eff}}(\psi_{\text{inf}})$?

$K_{\text{eff}}(\psi_{\text{inf}})$?

$$1 - n_s \sim 2\varepsilon_s + 4\zeta_s \quad x.999 \quad \& \quad r \sim 16\varepsilon_s \quad \text{slow roll}$$

2 solutions: nearly uniform acceleration & small ζ_s

$$\varepsilon_s \sim .017 \pm .007; \quad \varepsilon_s < .025 \quad 95\% \text{ from } r$$

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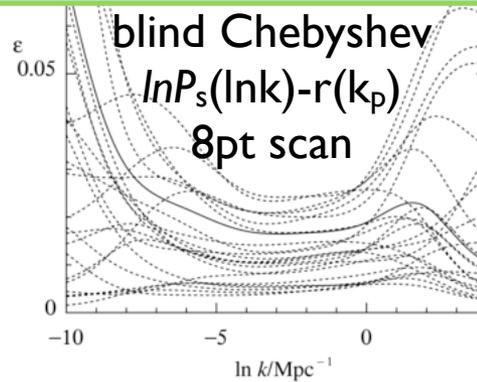
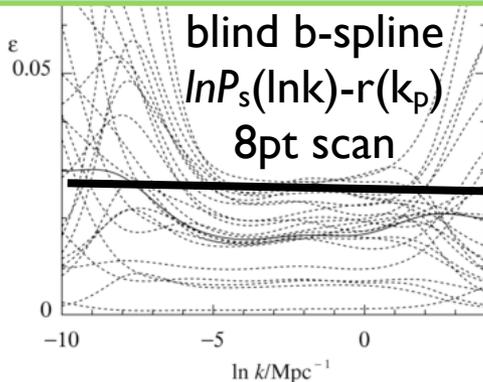
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$$\zeta_s \sim 0.1 \pm .6 \text{ } -.7$$

to $\pm .6 \text{ } -.7$ Planck+JDEM+DUNE **LCDM**

to $\pm .3 \text{ } -.3$ steep-ish $\exp[-\psi]$



very early U

early to middle to now U

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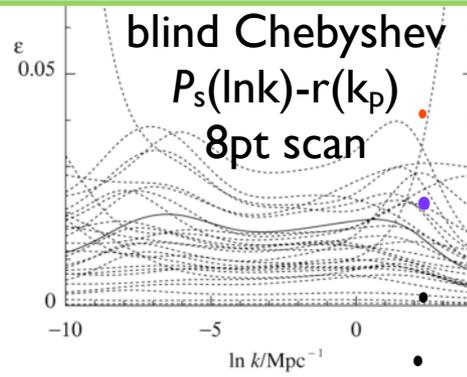
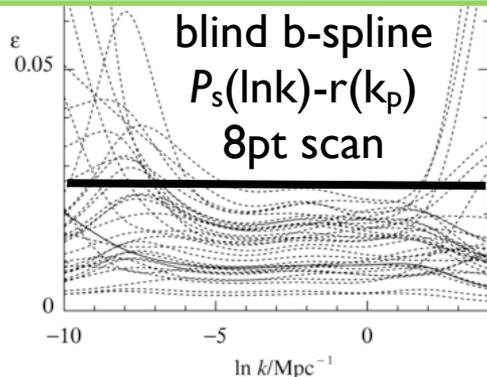
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$\zeta_s = \pm 1.001 d^2 \ln V / d \psi^2 / 4 @ a_{\text{eq}}$

$\zeta_s \sim 0.1 + .6 -.7$

to $+.6-.7$; $\pm .3$ Planck+JDEM+DUNE

$a_s < 0.36 (z_s > 2.0)$ • to a_s to $< 0.21 (z_s > 3.7)$

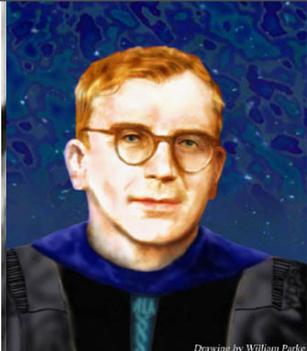


we ignore z_{dec} and z_{bbn} constraints on Ω_q (a)
much further trajectory extrapolation needed.

prior sensitivity $\sqrt{\epsilon}$: $\epsilon = 0.00 + .09 -.13$ &
 $\epsilon > 0$ (since phantom is ~ baroque): $\epsilon = 0.00 + .20$

late-inflaton field is $<$ Planck mass

coupled-DE 5th force constraints are strong



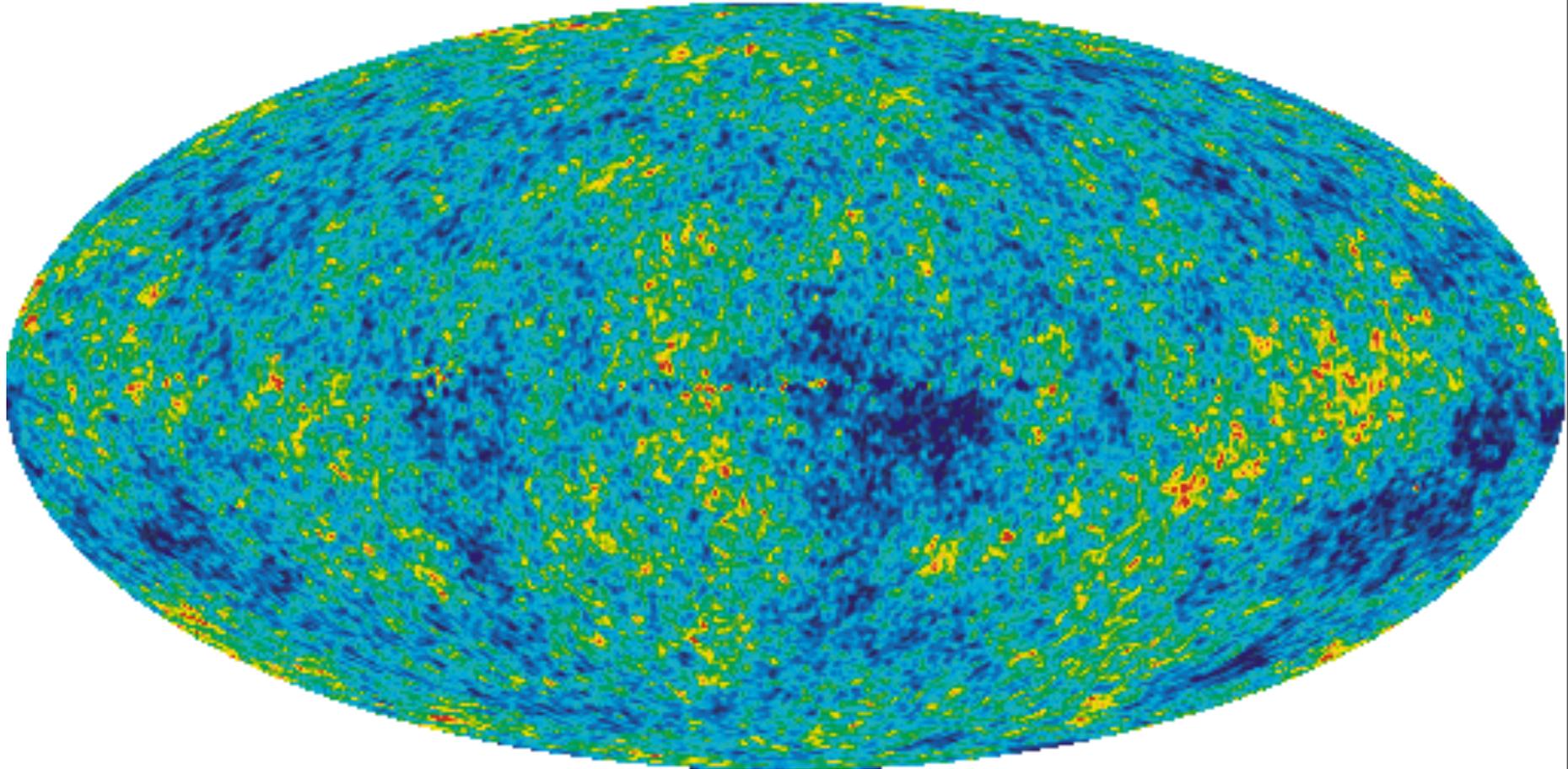
Drawing by William Park



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**

CMBology

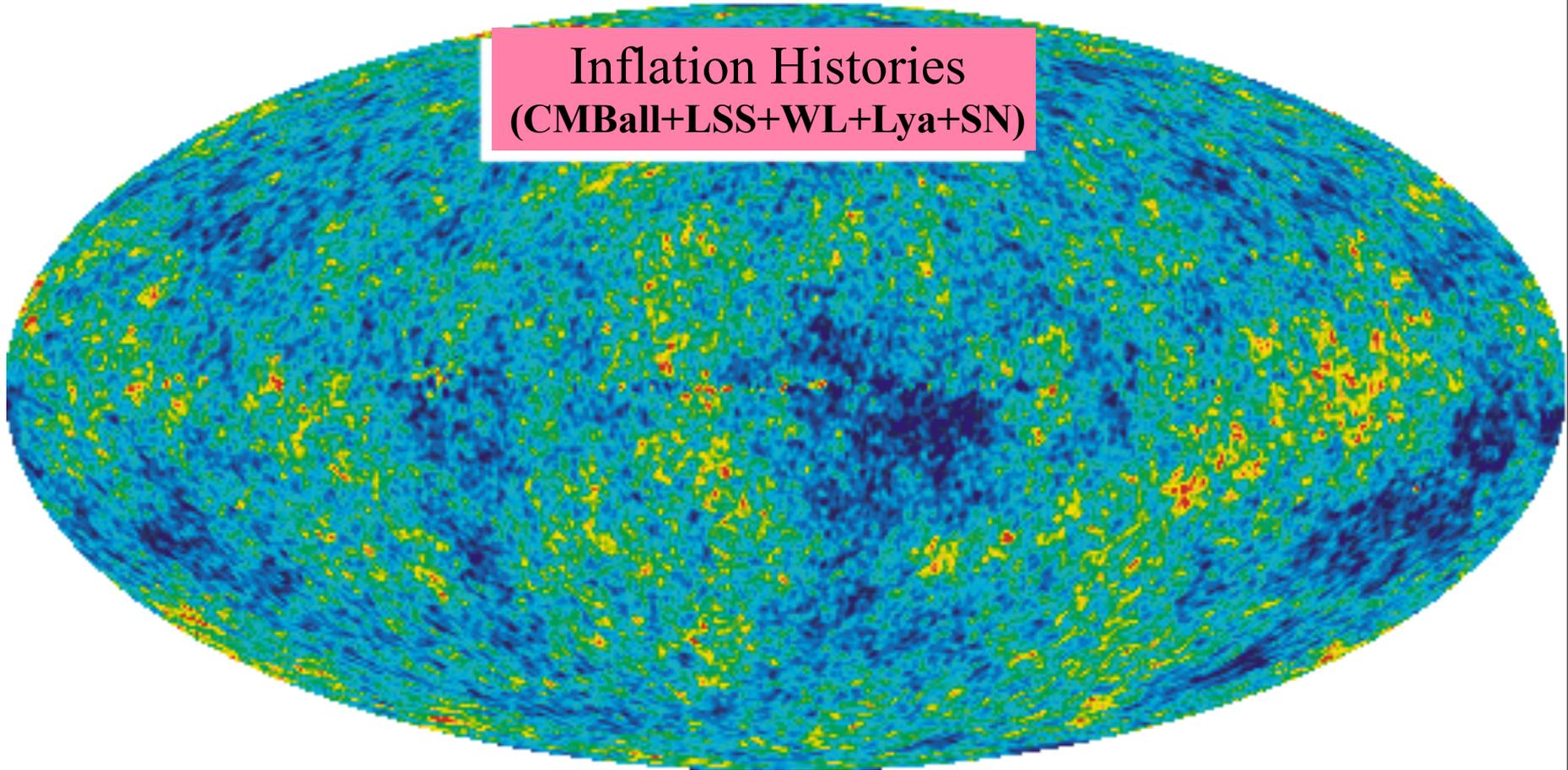
Probing the linear &
nonlinear cosmic web



CMBology

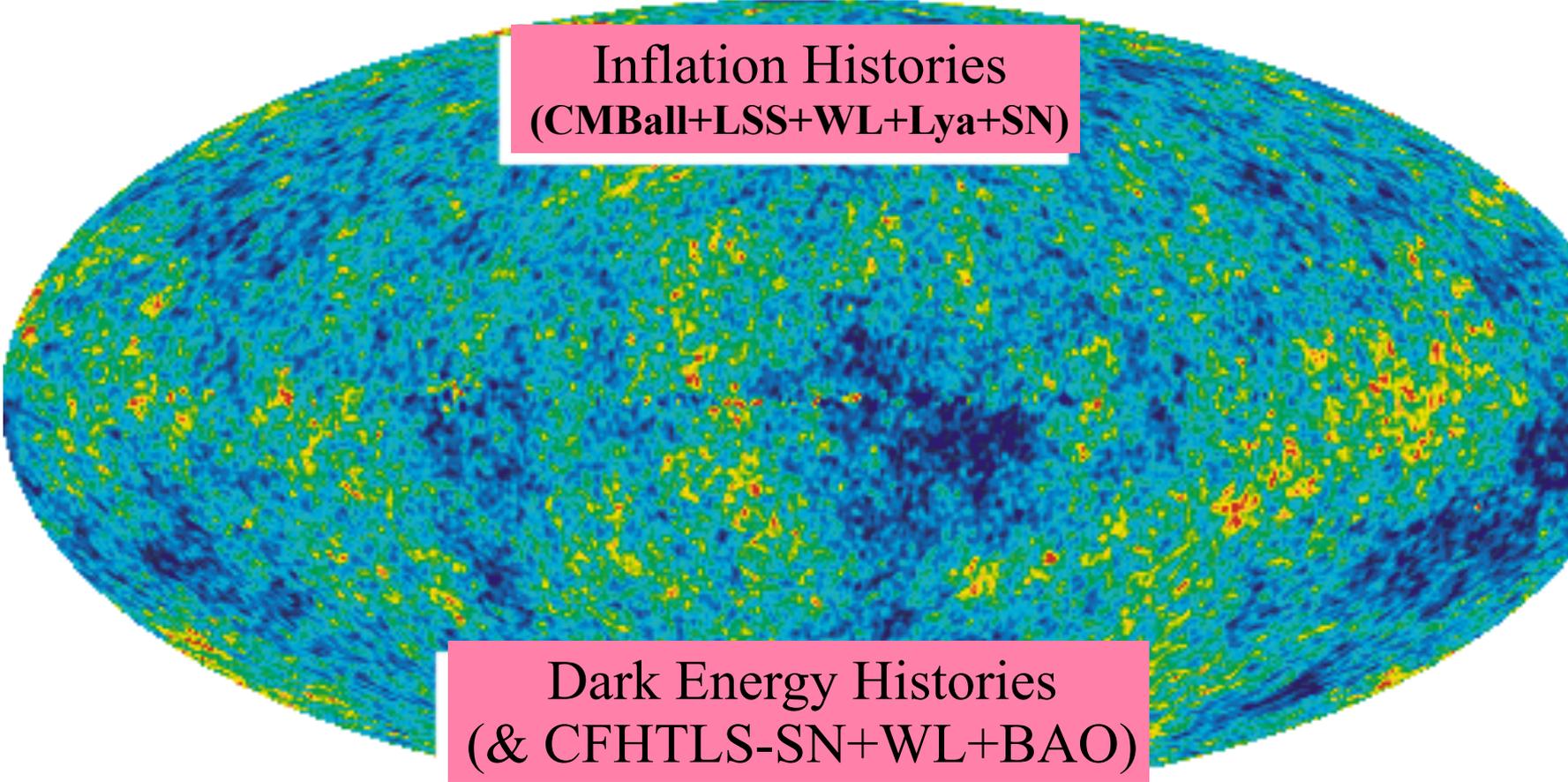
Probing the linear &
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Inflation Histories
(CMBall+LSS+WL+Lya+SN)



CMBology

Probing the linear &
nonlinear cosmic web

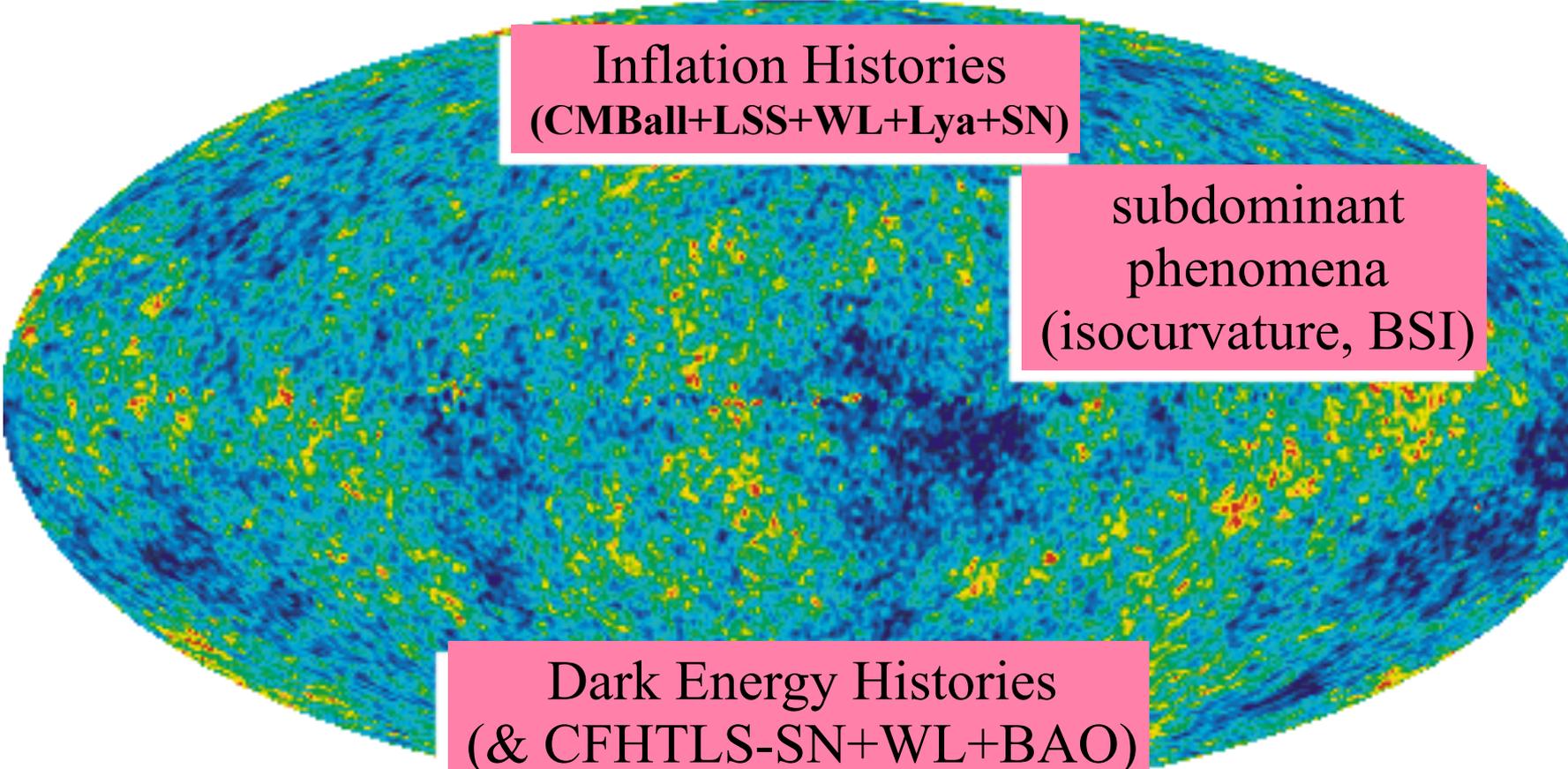


Inflation Histories
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Dark Energy Histories
(& CFHTLS-SN+WL+BAO)

CMBology

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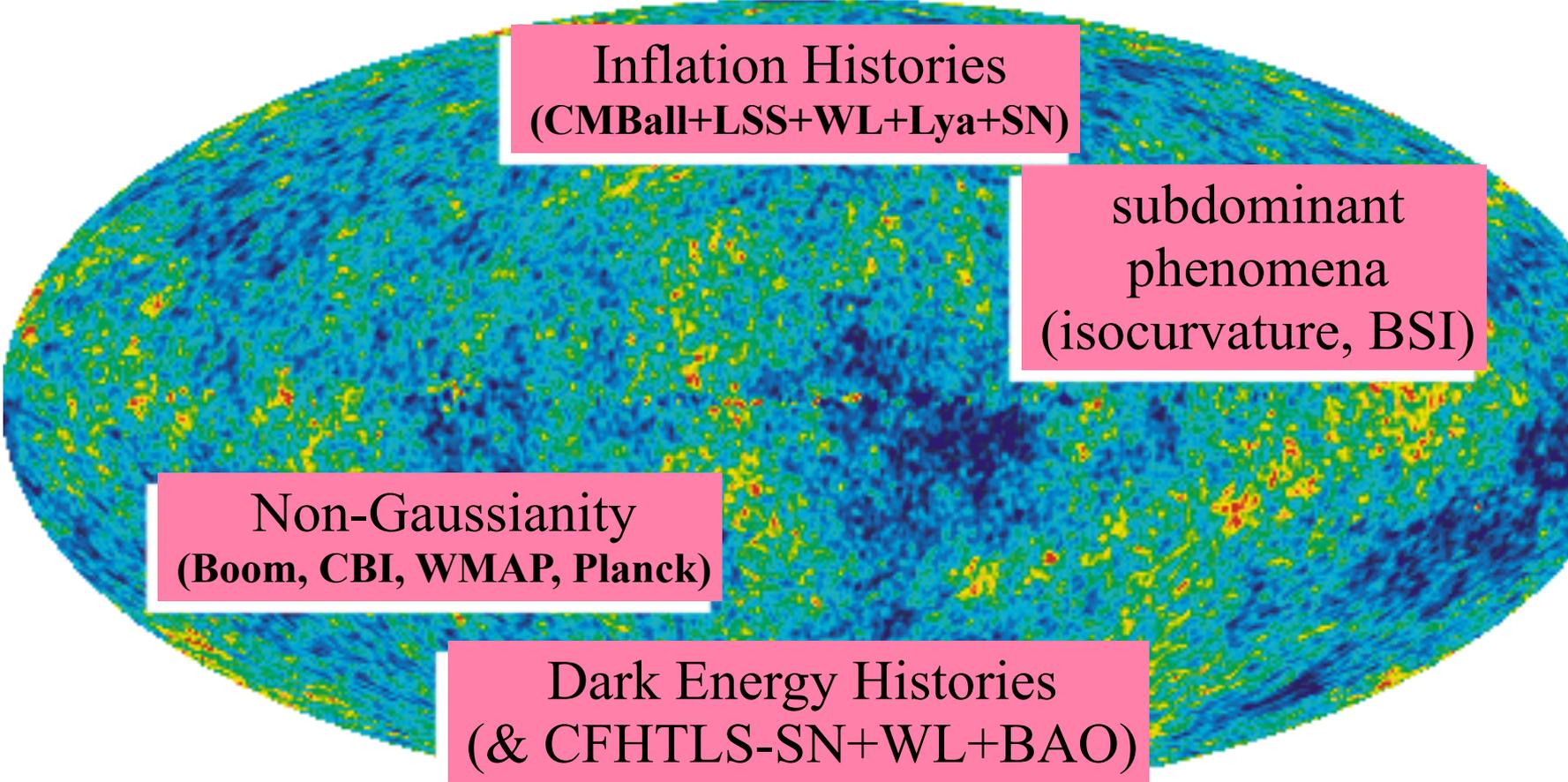
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subdominant
phenomena
(isocurvature, BSI)

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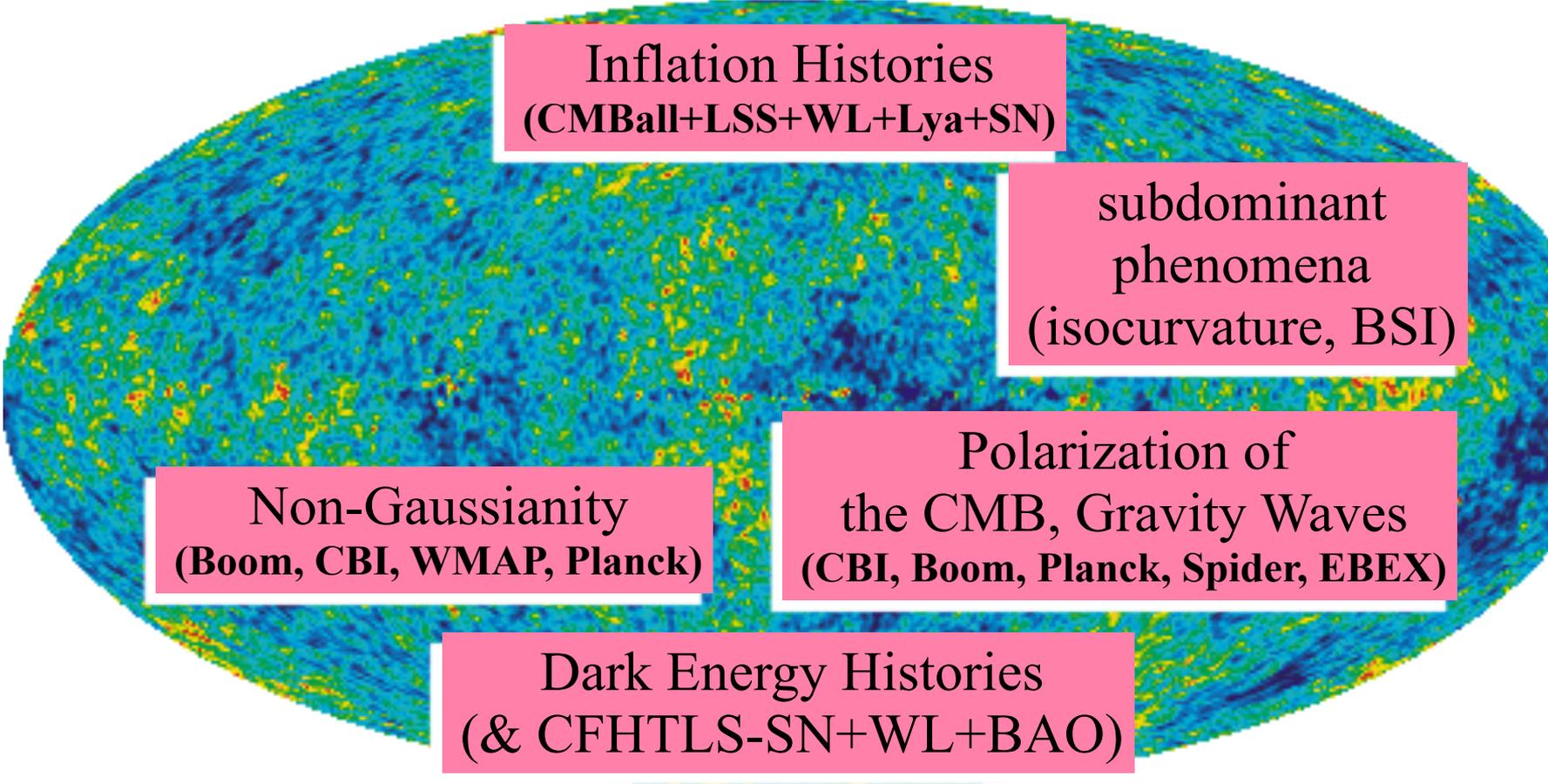
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Polarization of
the CMB, Gravity Waves
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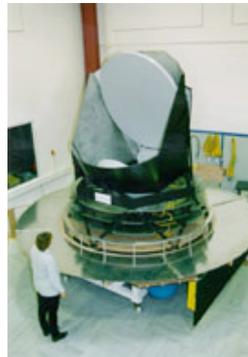
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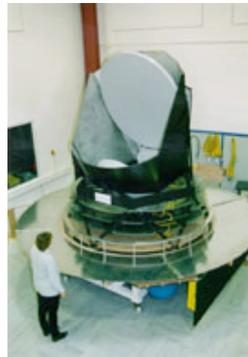
Secondary
Anisotropies (CBI,ACT)
(tSZ, kSZ, reion)

subdominant
phenomena
(isocurvature, BSI)

Non-Gaussianity
(Boom, CBI, WMAP, Planck)

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CMBology

Probing the linear & nonlinear cosmic web

Inflation Histories
(CMBall+LSS+WL+Lya+SN)

Foregrounds
CBI, Planck

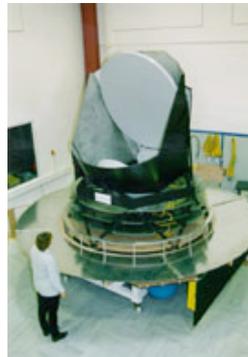
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Standard Parameters of Cosmic Structure Formation

$$\theta \sim \ell_s^{-1} \quad \sim \ln \sigma_8^2$$

$$\Omega_k \quad \Omega_b h^2 \quad \Omega_{dm} h^2 \quad \Omega_\Lambda \quad \tau_c \quad \ln A_s \quad n_s \quad r = A_t / A_s$$

$$1+w_0, w_a$$

$$dn_s / d \ln k \quad n_t$$

New Parameters of Cosmic Structure Formation:
early-inflaton & late-inflaton trajectories

$$\epsilon_\phi = (1+w(a)) \times 3/2 \quad \epsilon(k), \quad k \approx Ha \quad \ln H(k_p)$$

$$\epsilon_s f(a/a_{\Lambda eq}; a_s/a_{\Lambda eq}; \zeta_s) \quad \ln P_s(k) \quad \ln P_t(k)$$

+ subdominant isocurvature/cosmic string/ tSZ ...

CMB Polarization, Past, Present & Future

Dick Bond Canadian Institute for Theoretical Astrophysics, University of Toronto

theory of CMB polarization

E/B modes

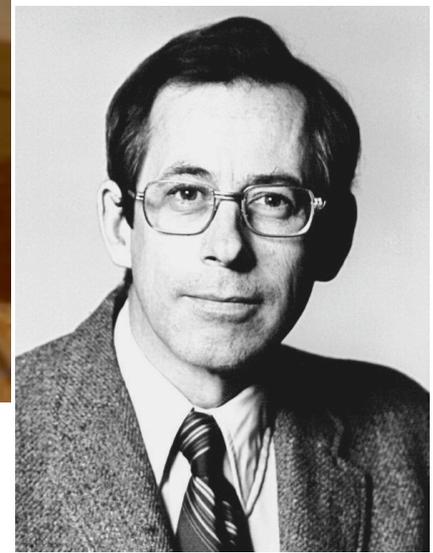
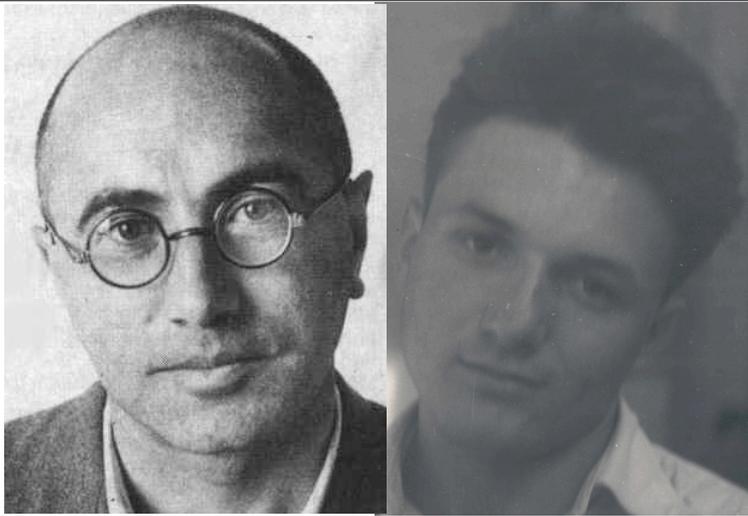
detection history

future CMB polarization experiments

reionization 'trajectories'

inflation & forecasts of the gravity wave level: is the energy scale of inflation high (80s/90s) or low (00s)?

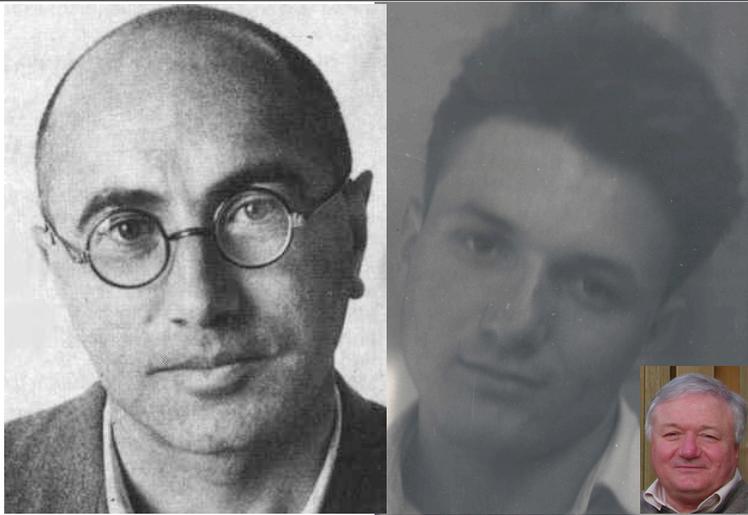
the quest for gravity wave induced B-modes



Peebles, Page, Partridge, *Finding the Big Bang*, Feb09 CUP

Rees 1968: CMB should be polarized; detection 2002 DASI





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redshift z

I
N
F
L
A
T
I
O
N

the nonlinear
COSMIC WEB

primary anisotropies

- linear perturbations: scalar/density, tensor/gravity wave
- tightly-coupled photon-baryon fluid: oscillations $\delta\gamma$ $v\gamma$ $\pi\gamma$
- viscously damped
- polarization $\pi\gamma$
- gravitational redshift Φ SW $d\Phi/dt$

$z \sim 1100$

Decoupling LSS



L_{sound}
k_{sound}

19 Mpc

secondary anisotropies

- nonlinear evolution
- weak lensing
- thermal SZ + kinetic SZ
- $d\Phi/dt$
- dusty/radio galaxies, dGs

reionization

$z \sim 10$

$z=0$

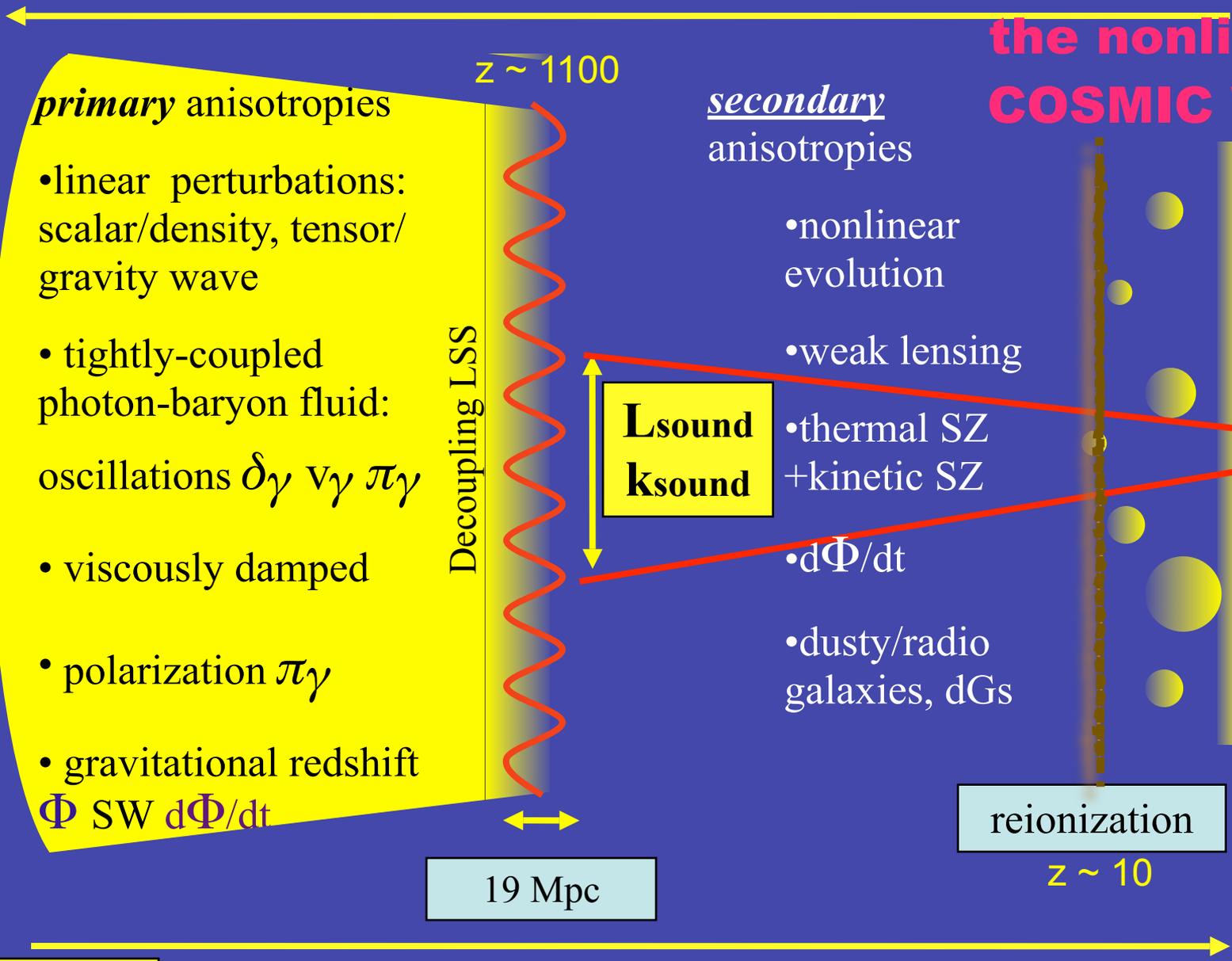
13.7-10⁻⁵⁰ Gyrs

13.7 Gyrs

time t

10 Gyrs

today





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Rees 1968: CMB should be polarized; detection 2002 DASI

Kaiser83, pol via line-of-sight integration

BE84: pol via Boltzmann transport, ~7% target,
effect on shear viscosity, damping tail, “E” mode

BE87: low to high L full CLpol, maps



**First E detection DASI 2002;
CBI04/05, Boom05, WMAP06,
Capmap08, QuAD08; BICEP09?**

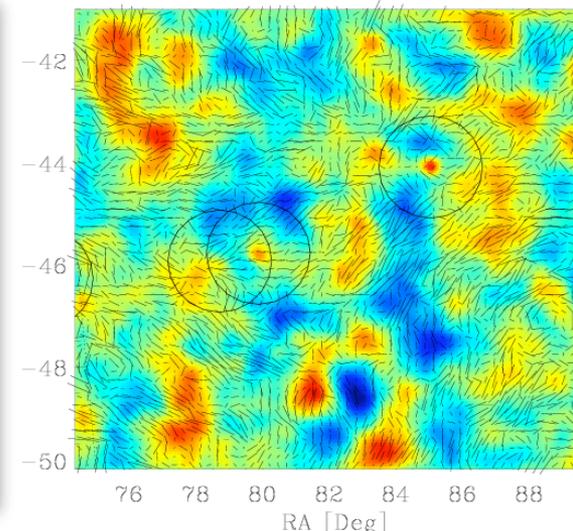
Delta T over Tea Toronto May 1987: first dedicated CMB conference, exptalists+theorists, primary+secondary $\Delta T/T$

A tentative list of topics organized according to angular scale, with theory and observation intertwined, is:

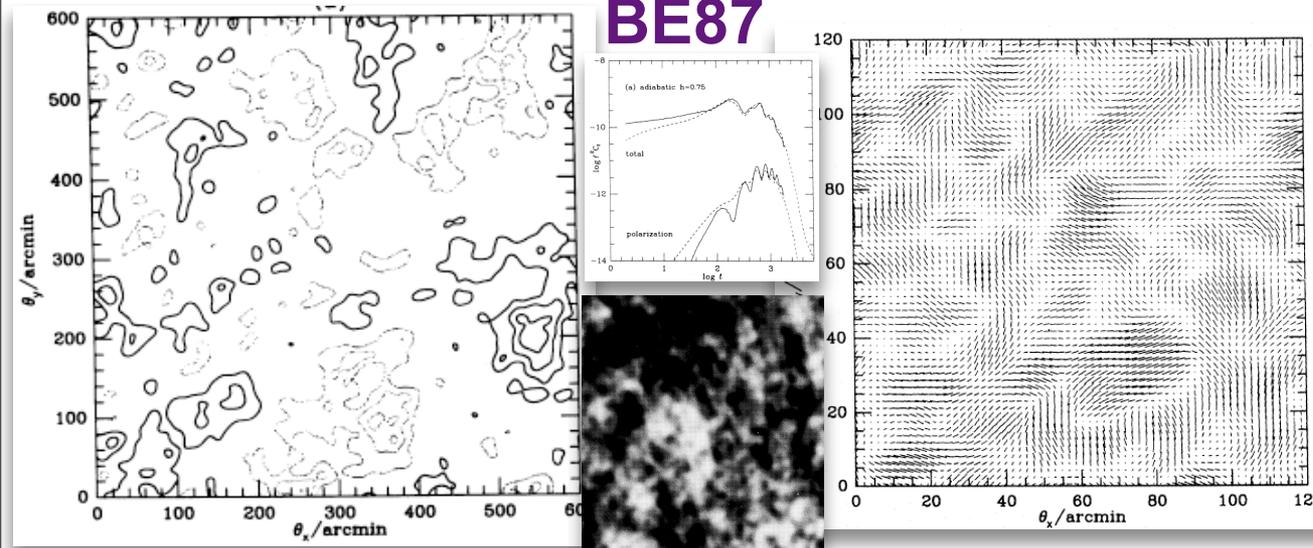
- very small angle anisotropies - VLA results, secondary fluctuations via the Sunyaev-Zeldovich effect, primeval dust emission, and radio sources
- small angle anisotropies - current results, optimal measuring strategies, statistical methods for small signals in larger noise, which universes can we rule out, the reheating issue, future detectors and techniques, **CMB map statistics, polarization**
- intermediate and large angle anisotropies - $5^\circ - 10^\circ$ results, future experiments at $\sim 1^\circ$, COBE and other large angle analyses, theoretical $C(\theta)$'s and their angular power spectra, Sachs-Wolfe effect in open Universes, the isocurvature CDM and baryon stories, $\Delta T/T$ from gravitational waves, the cosmic string story.

Boom05 deep

-300 200 100 0 100 200 300 μK

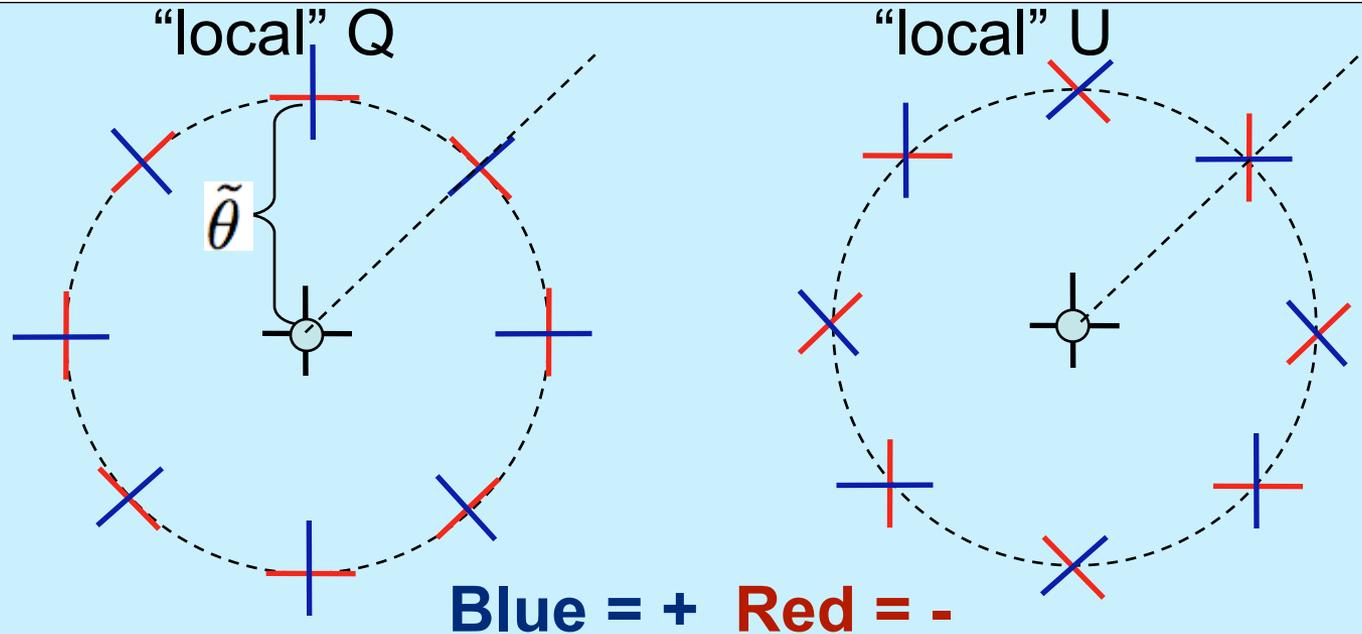


BE87



E and B modes: $f(\theta, \phi, \mathbf{x}_{\text{pt}})$ Stokes parameters I, Q, U, V with Q -only for Thompson scattering in a plane parallel atmosphere Chandrasekhar...BE84...
scalar polarization basis in Fourier space $E=Q(\mathbf{q}), B=U(\mathbf{q}), \mathbf{q}=L+1/2$

large sky patches: $Q + iU(\hat{\mathbf{n}}) = \sum_{lm} a_{lm} Y_{lm}$ $Q - iU(\hat{\mathbf{n}}) = \sum_{lm} -a_{lm} Y_{lm}$



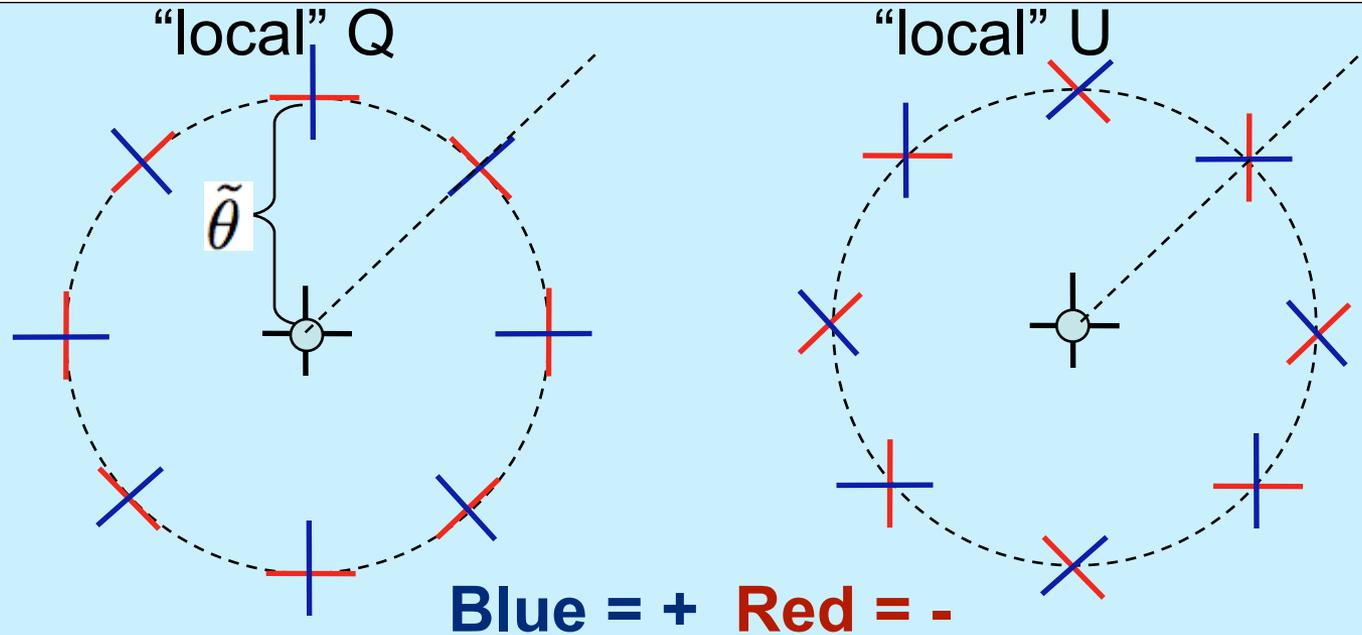
Tensor perturbations, transverse-traceless metric h_+, h_x & neutrino+photon anisotropic stress: U & Q in \mathbf{q} -space, i.e., **B & E**

“fgnd” lensing by the cosmic web shifts scalar E pattern inducing **B & E**

“fgnd” Galactic & extragalactic sources give B & E separate by frequency, spatial pattern

E and B modes: $f(ss', xpt)$ Stokes parameters I, Q, U, V with Q-only for Thompson scattering in a plane parallel atmosphere Chandrasekhar...BE84...
scalar polarization basis in Fourier space $E=Q(\mathbf{q}), B=U(\mathbf{q}), \mathbf{q}=L+1/2$

large sky patches: $Q + iU(\hat{\mathbf{n}}) = \sum_{lm} {}_2a_{lm} {}_2Y_{lm} \quad Q - iU(\hat{\mathbf{n}}) = \sum_{lm} -{}_2a_{lm} -{}_2Y_{lm}$



$$a_{lm}^E = -({}_2a_{lm} + -{}_2a_{lm})/2 \quad a_{lm}^B = i({}_2a_{lm} - -{}_2a_{lm})/2$$

Tensor perturbations, transverse-traceless metric h_+, h_x & neutrino+photon anisotropic stress: U & Q in \mathbf{q} -space, i.e., B & E

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BE87: low to high L full CLpol, maps

Crittenden & Turok 96: TE correlation DASI02, WMAP03

Kaiser95, Stebbins96: rotate lensing E to B, a null test

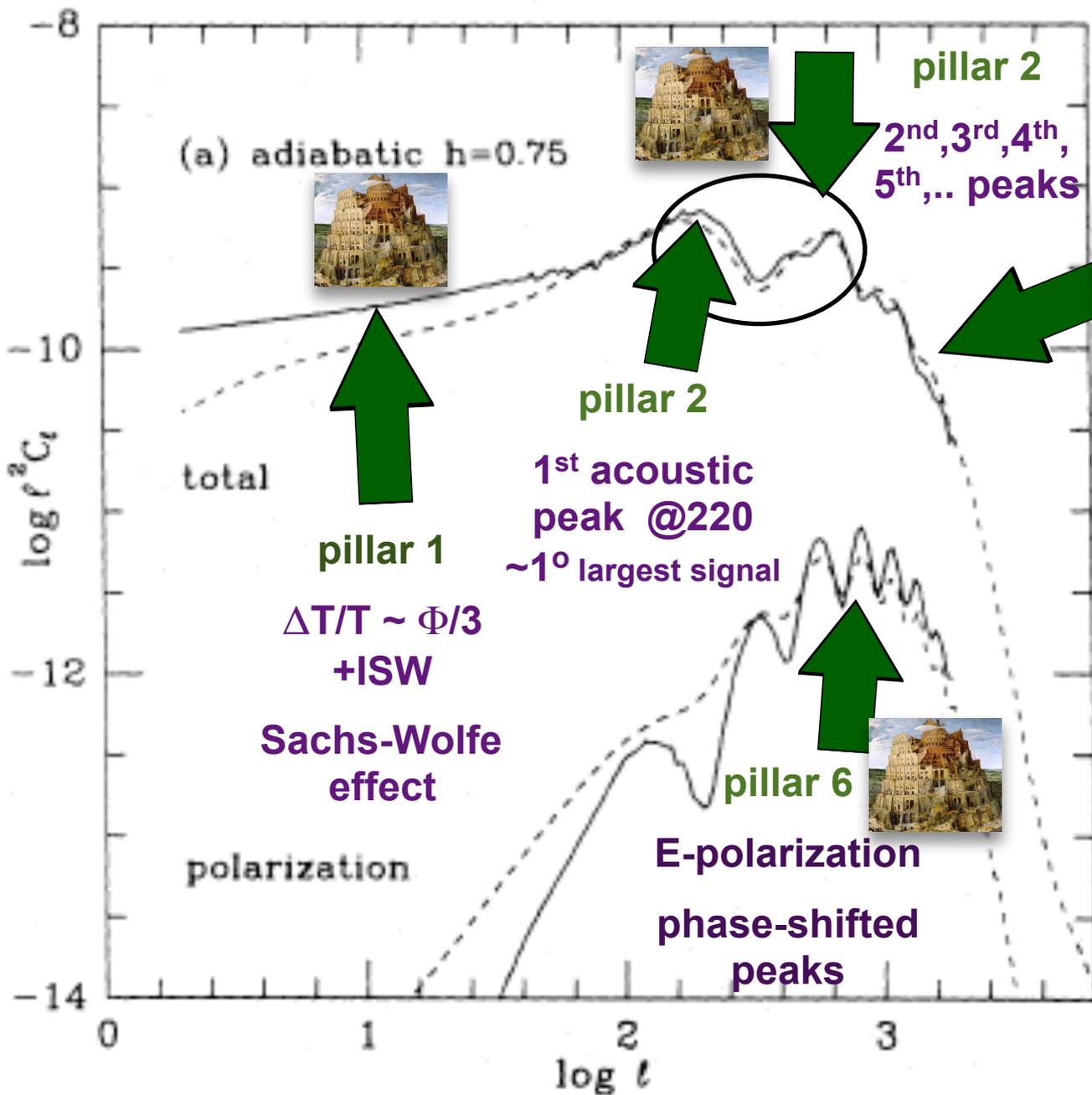
Kamionkowski, Kosowsky & Stebbins97 & Seljak & Zaldarriaga97: apply to CMB E/B modes. emphasize as gravity wave discriminator

Zaldarriaga & Seljak98 lensing distorts E into B



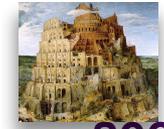
First E detection DASI 2002; CBI04/05, Boom05, WMAP06, Capmap08, QuAD08; **BICEP09?**

the "Seven Pillars"



pillar 4

Gaussianity
 maximal
 randomness
 for given CL



pillar 5

secondary ΔT
 nonlinear
 Compton SZ
 weak lensing..

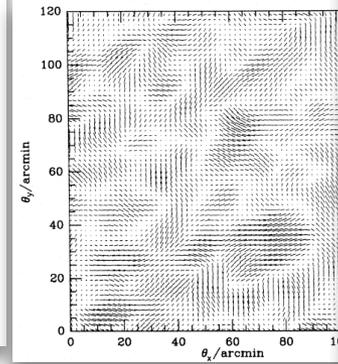


pillar 7

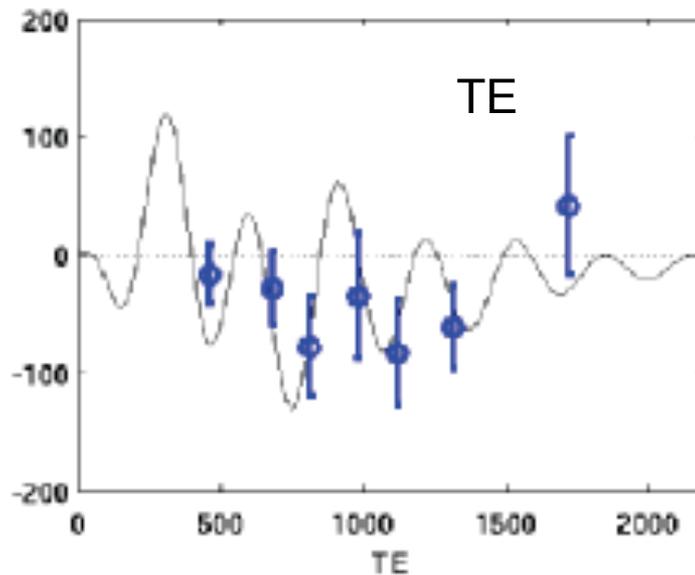
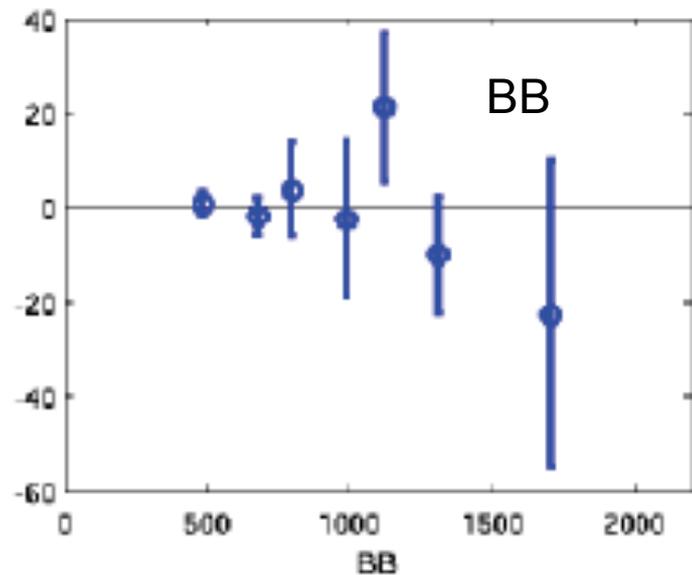
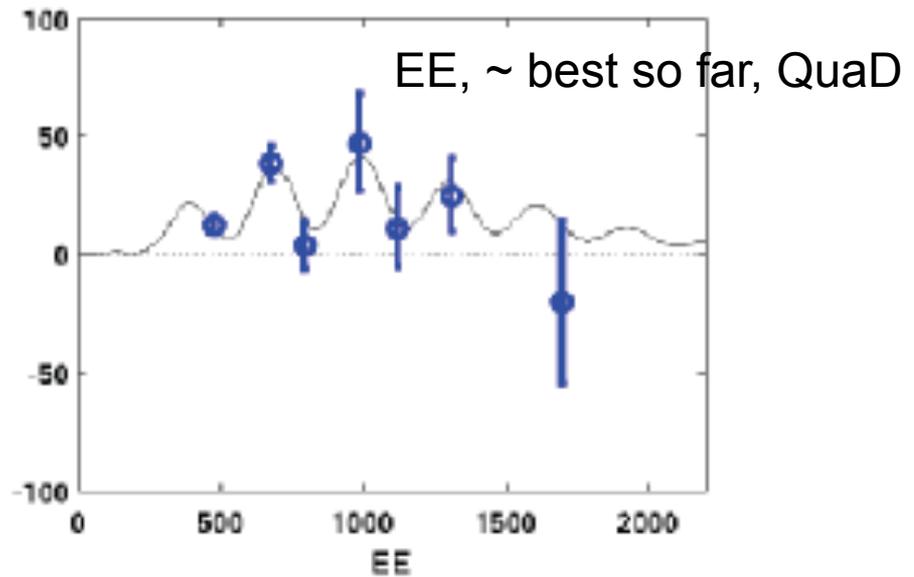
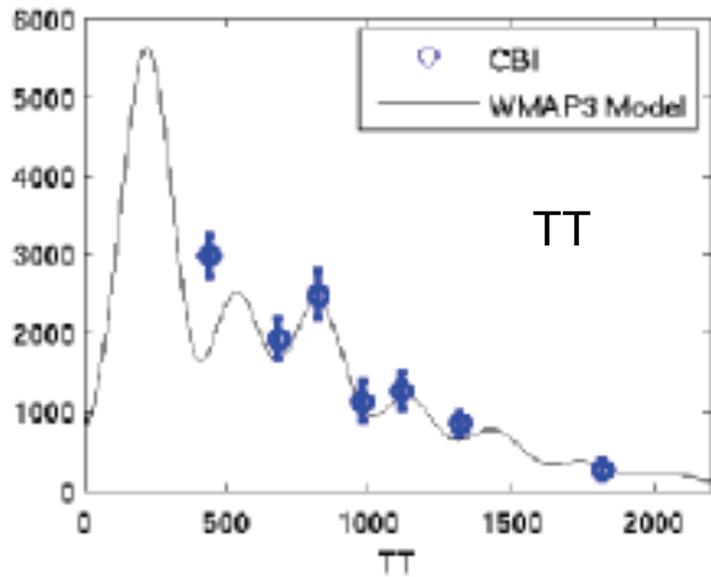
B-polarization
 Gravity Waves



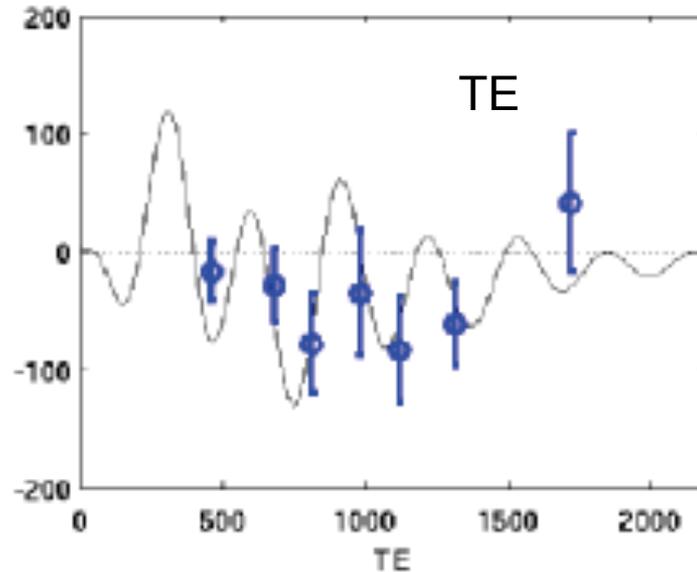
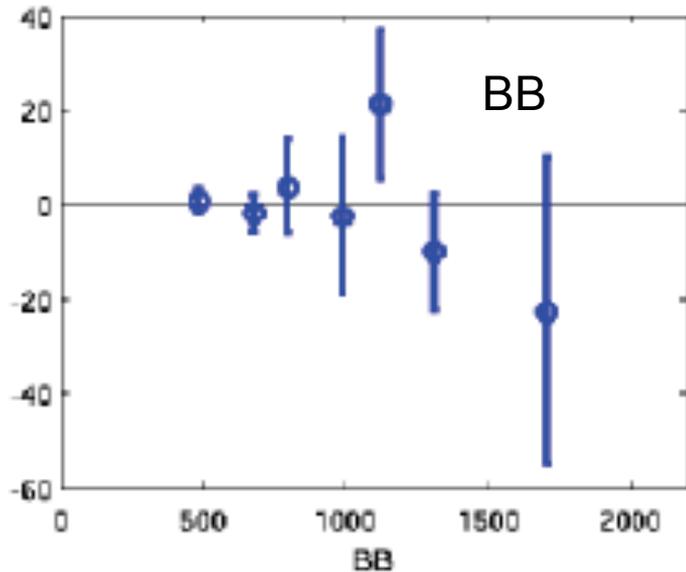
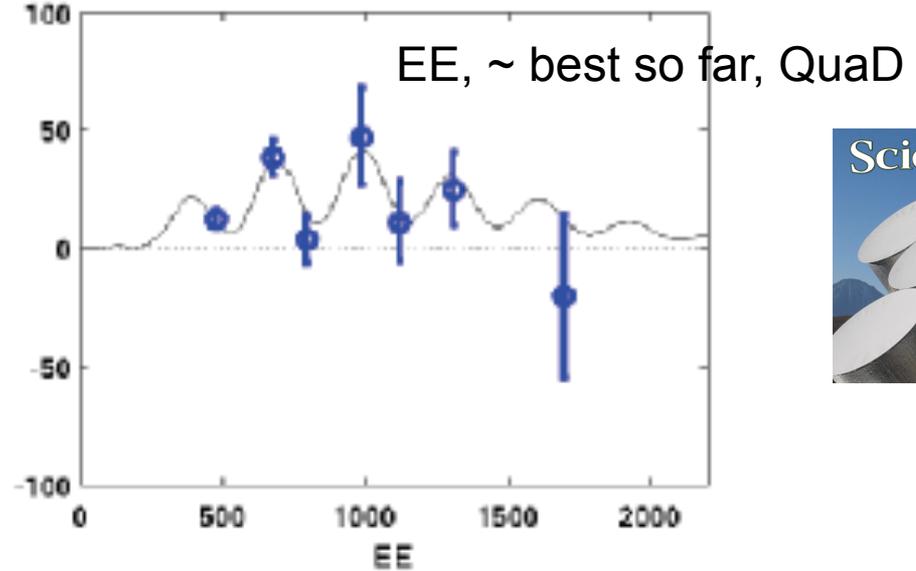
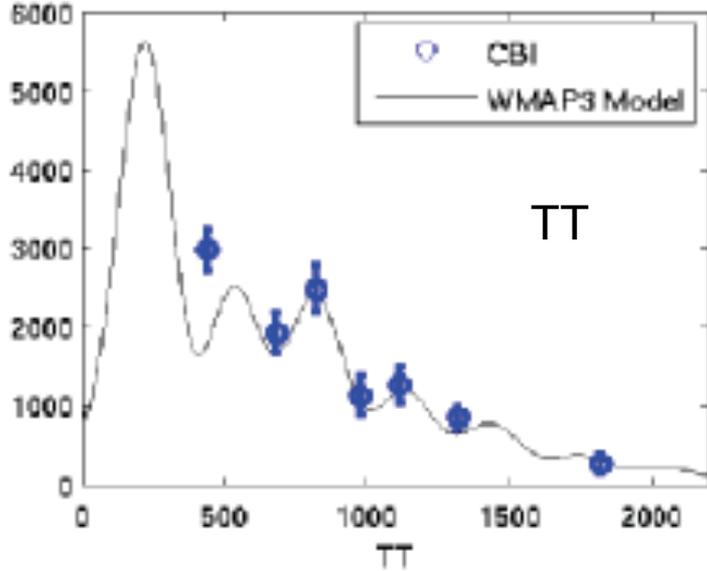
Polarized Smoke/Green Lenses



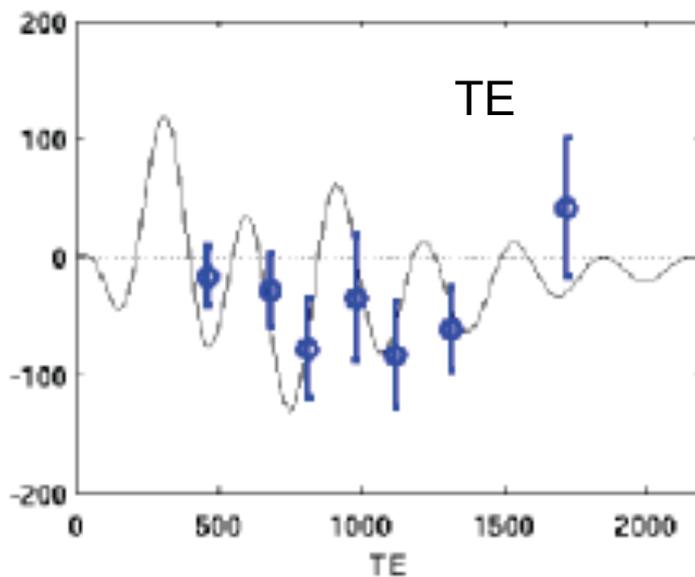
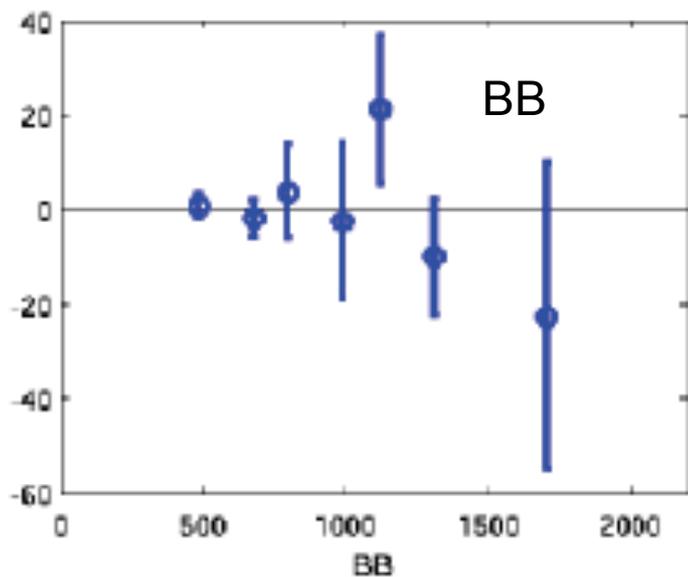
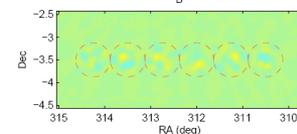
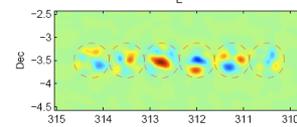
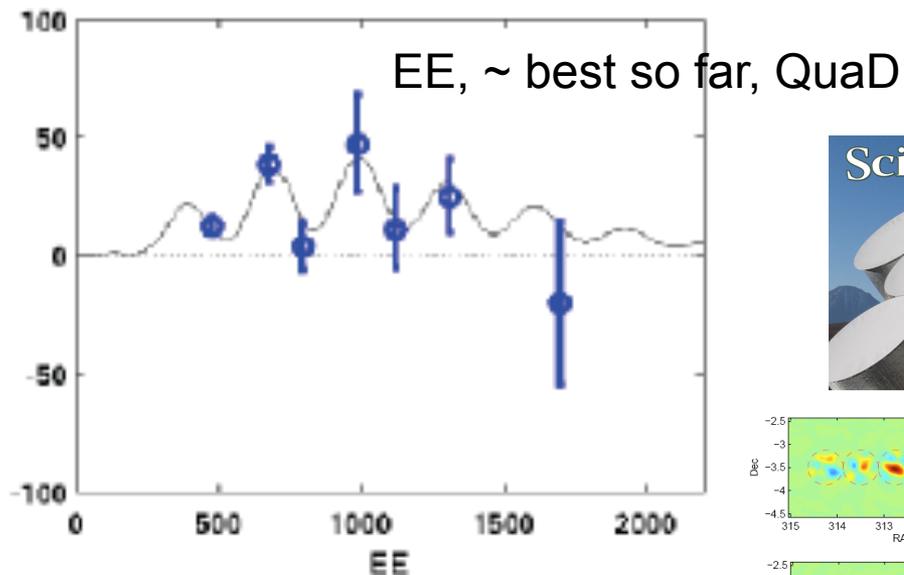
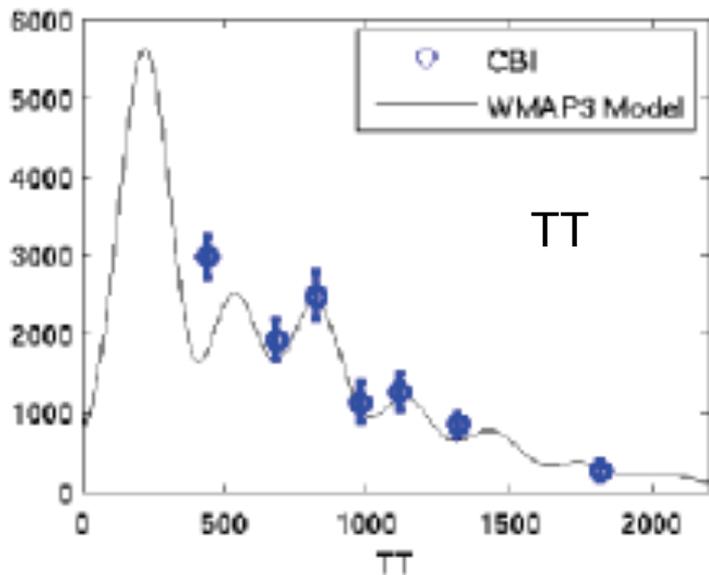
CBIpol 2.5yrs Sievers etal 05/06, Readhead etal 04



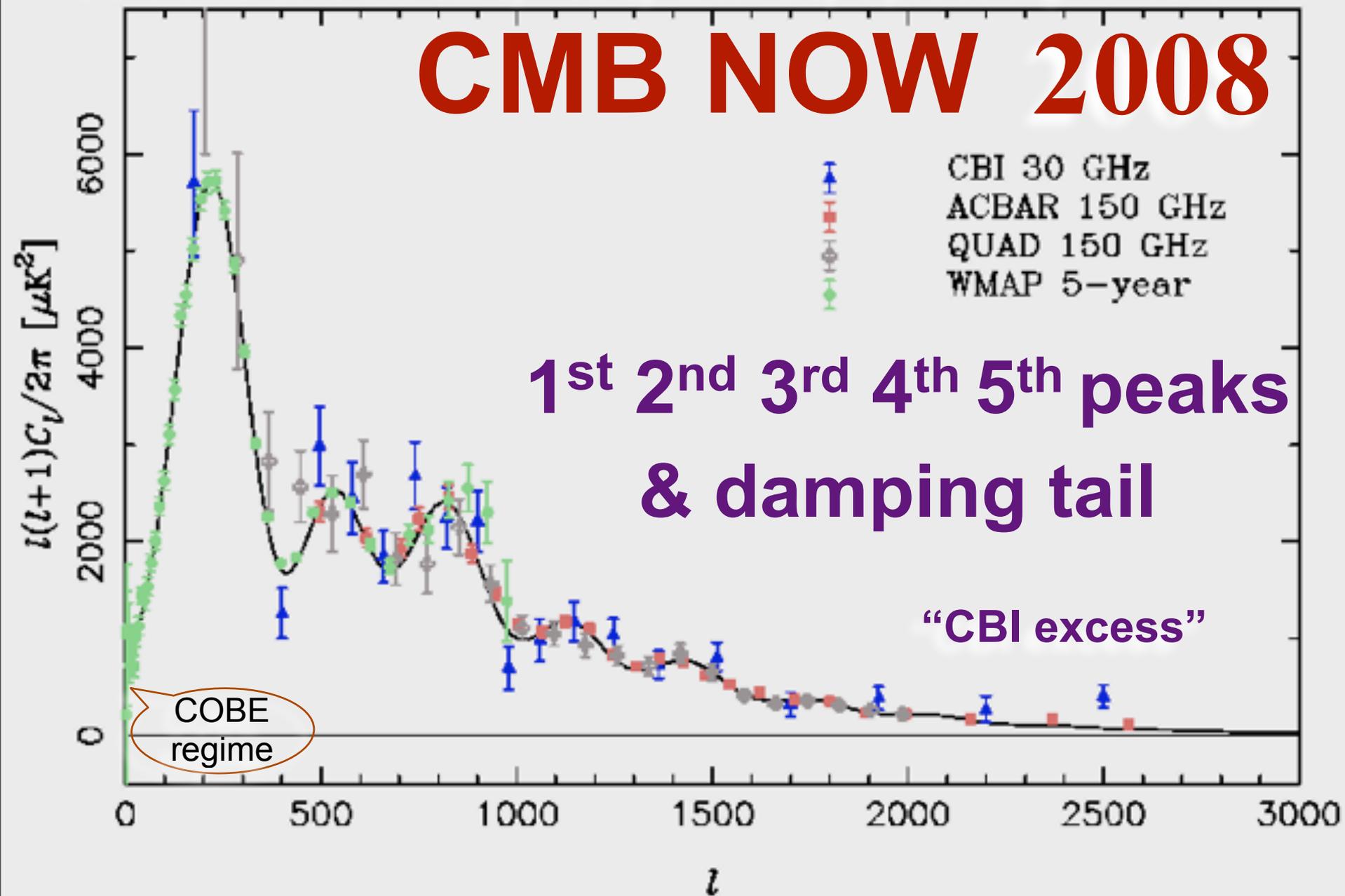
CBIpol 2.5yrs Sievers etal 05/06, Readhead etal 04



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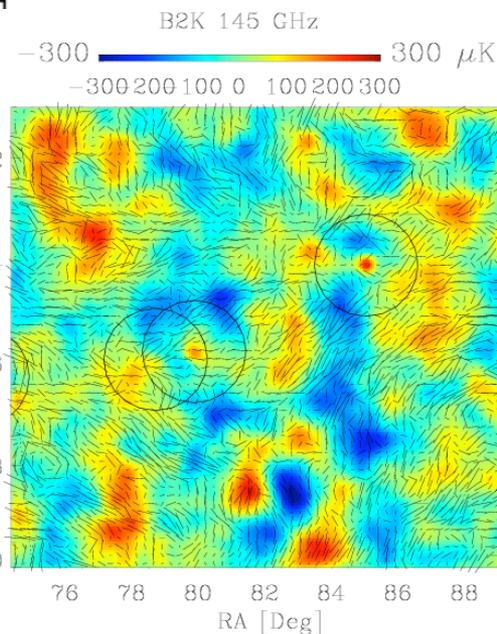
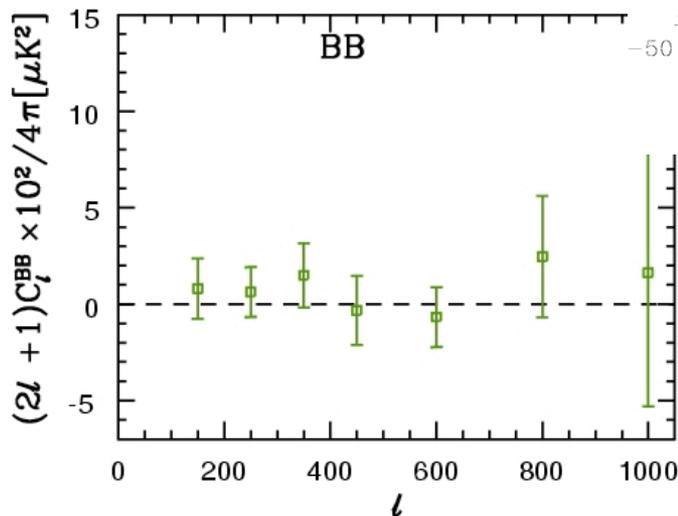
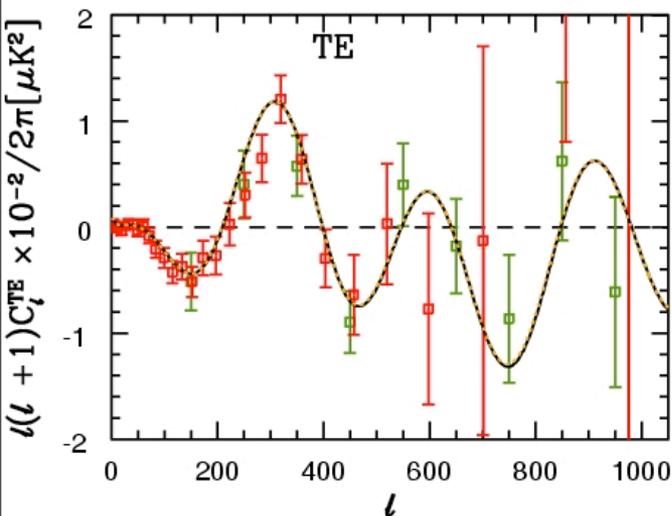
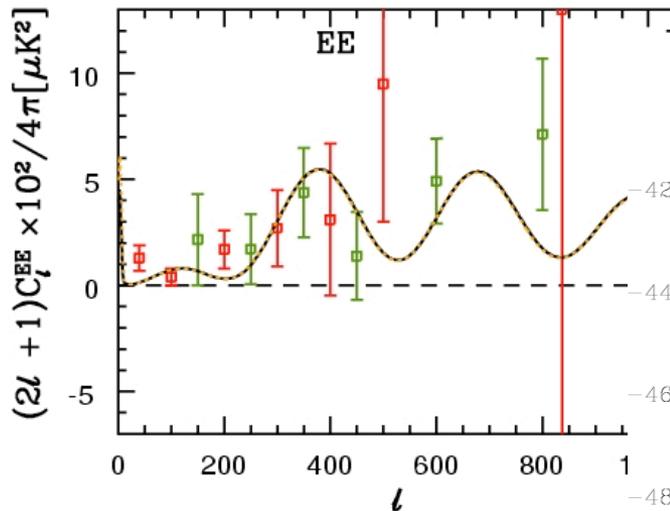
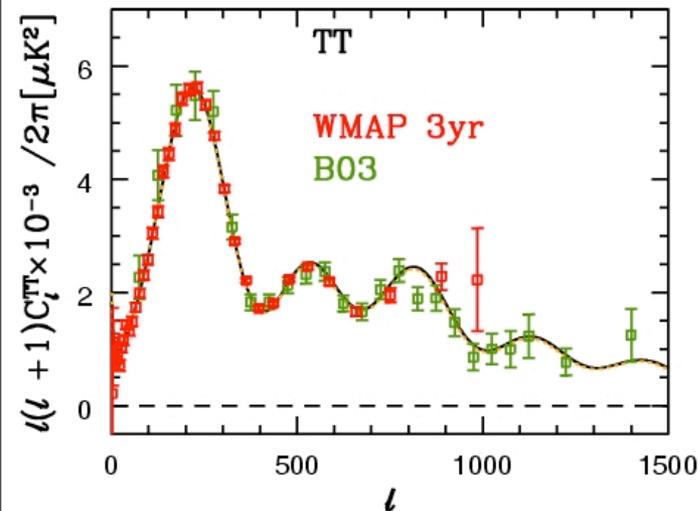
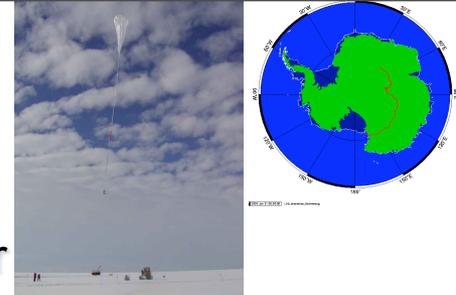


CMB NOW 2008



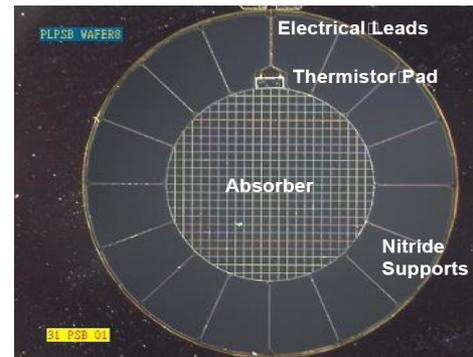
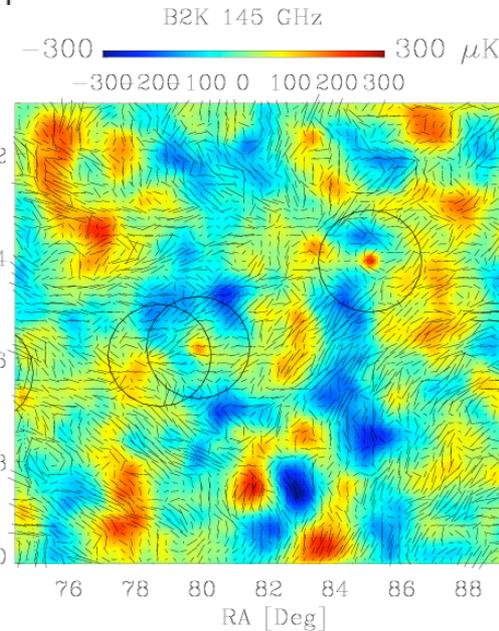
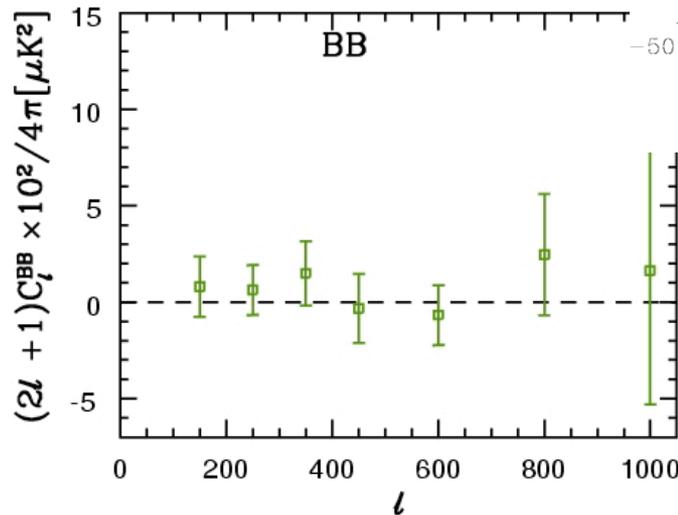
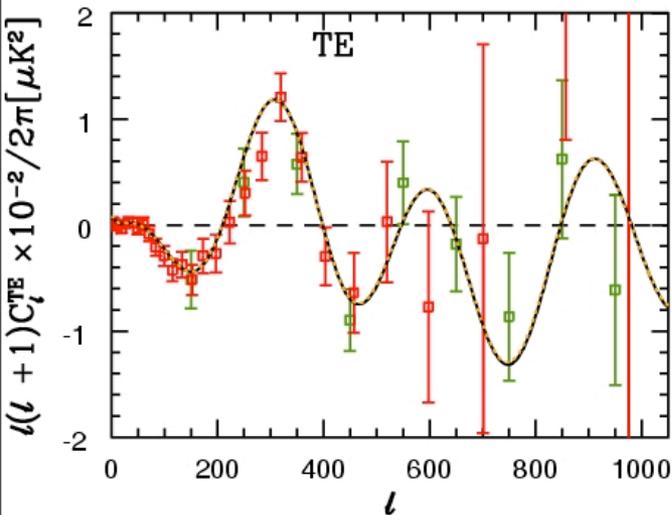
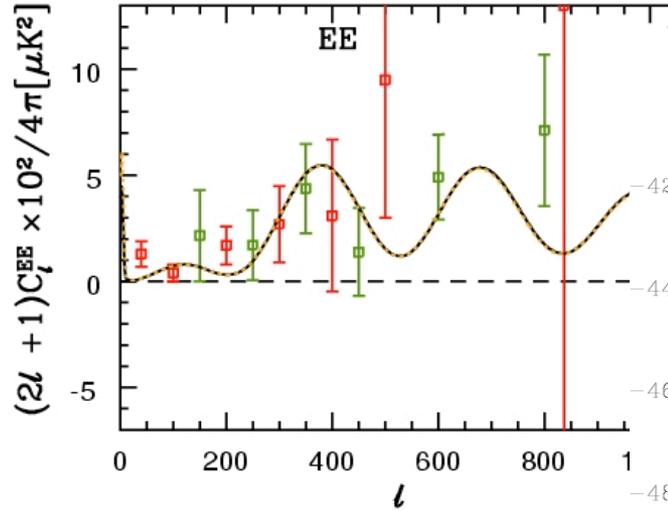
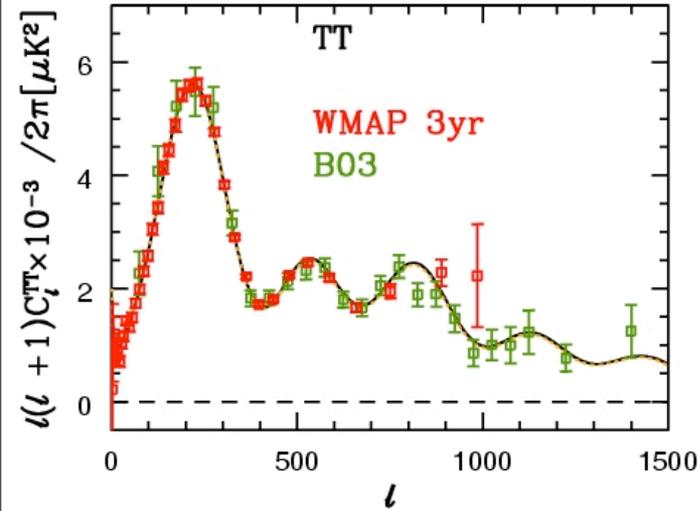
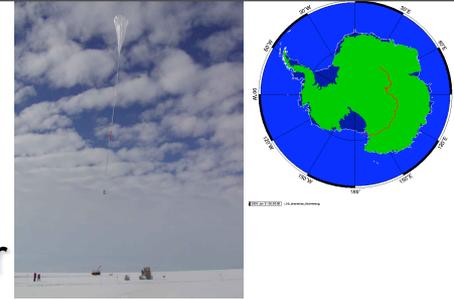
B03 pol TE, EE 2005 1st bolo detection

- ‘Shallow’ scan, 75 hours, $f_{\text{sky}}=3.0\%$, large scale TT
- ‘deep’ scan, 125 hours, $f_{\text{sky}}=0.28\%$ 115sq deg, $\sim 2 \times$ Planck2yr



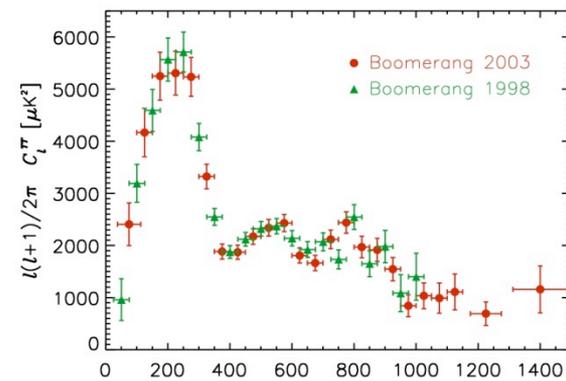
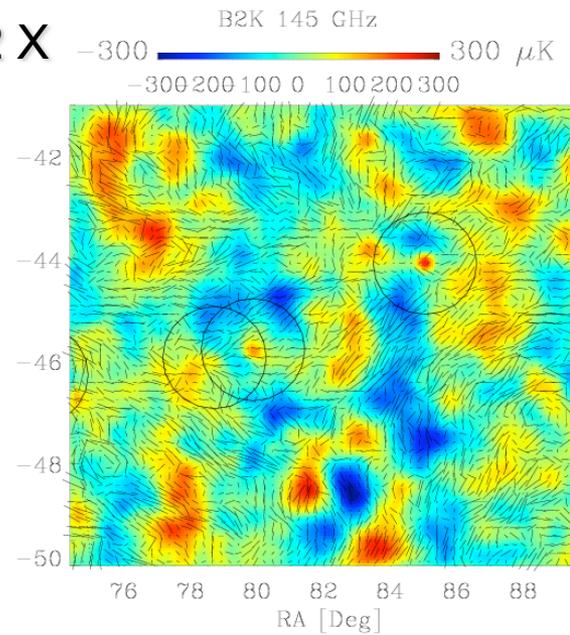
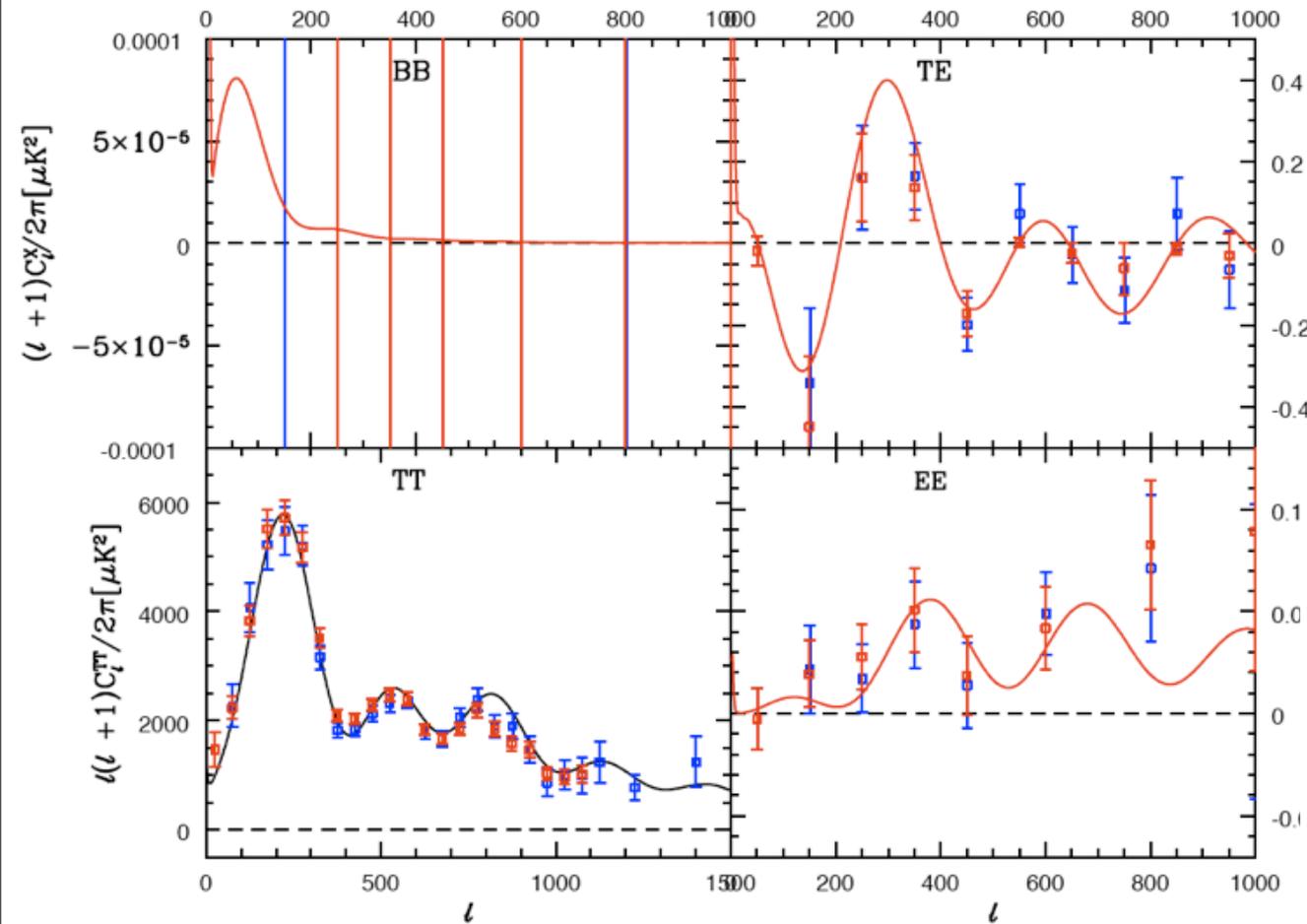
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B03+B98 *Contaldi et al 01..09! x faster! Boom/Planck/Spider workhorse*

- 'Shallow' scan, 75 hours, $f_{\text{sky}}=3.0\%$, large scale TT
- 'deep' scan, 125 hours, $f_{\text{sky}}=0.28\%$ 115sq deg, $\sim 2 \times$ Planck2yr

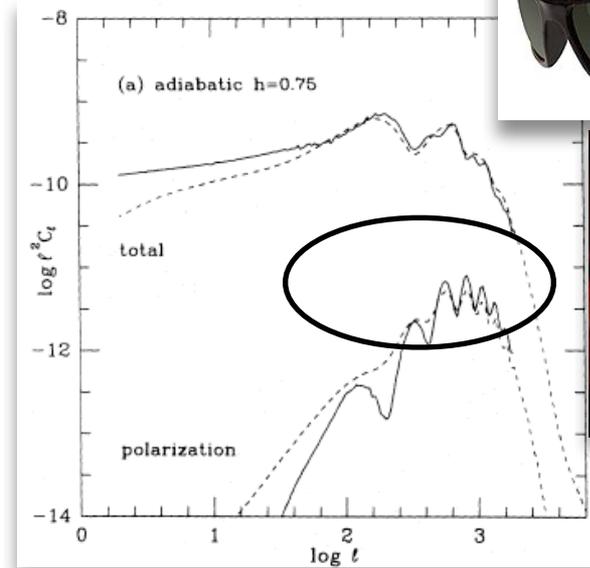
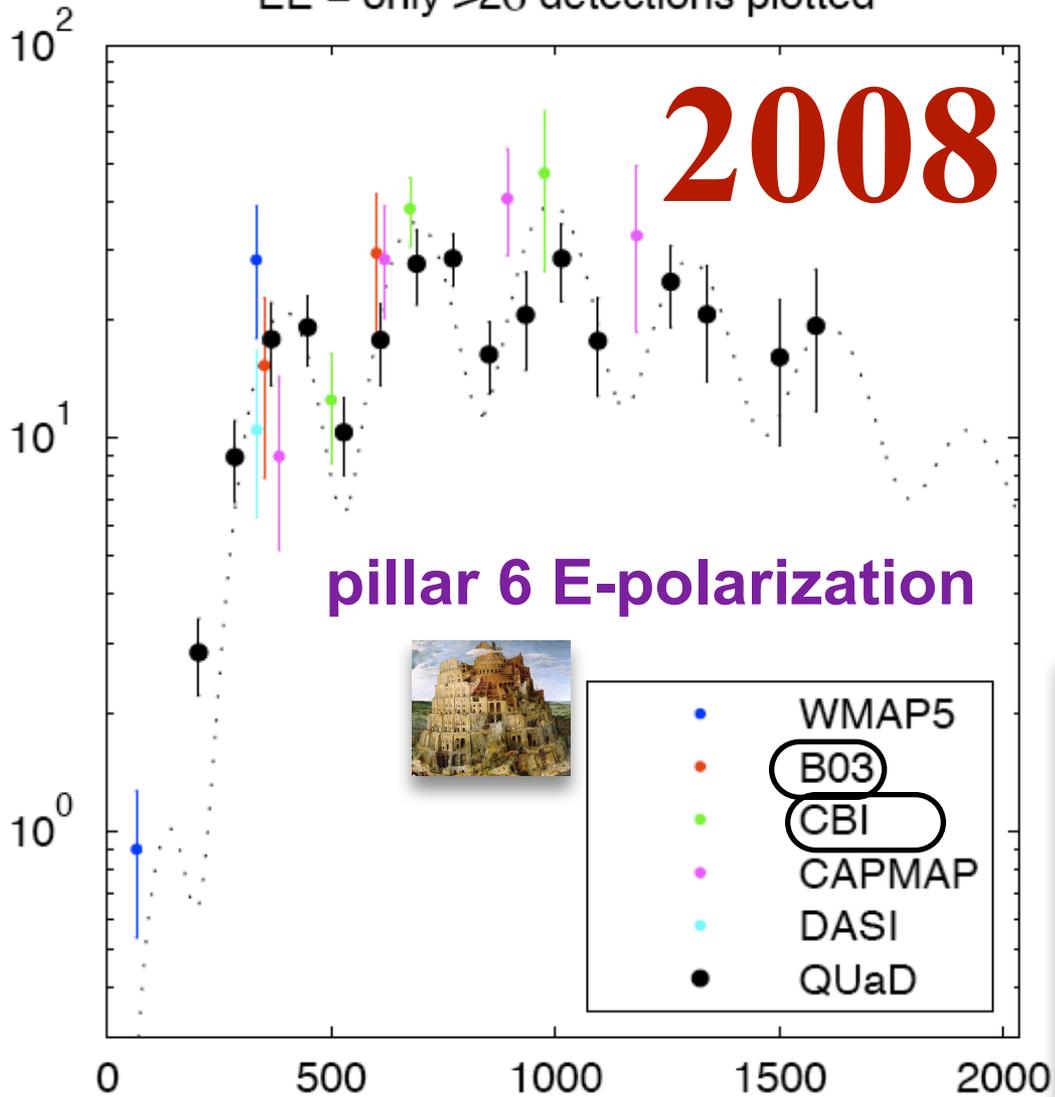


B03+B98 final soon

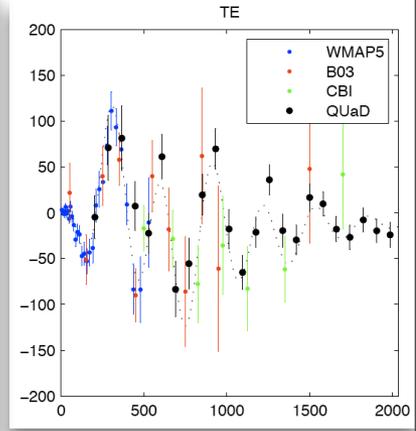
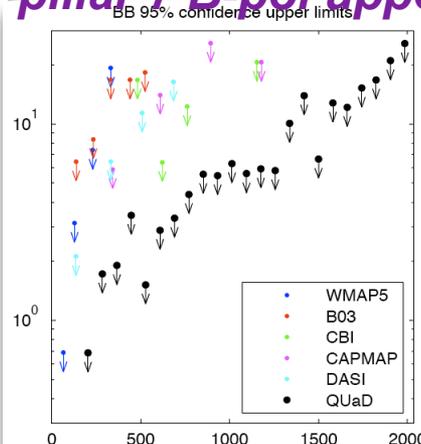
emergence of CMB polarization power

DASI02,04 CBI04 Boom05 CBI05 WMAP3,5 Capmap07 QUaD07,08

EE – only $>2\sigma$ detections plotted



pillar 7 B-pol upper limits



What do we learn from E polarization?

- 0 - EE/TE agree with TT forecasts! *pillar6: out-of-phase pks/valleys*
- 1 - constrain radically broken scale invariance *out-of-phase pks*
- 2 - constrain subdominant isocurvature modes CBI
- 3 - constrain anomalies *e.g., WMAP haze, COBE/WMAP "hole" TBD*
- 4 - aid in lensing reconstruction of lensed CMB *TBD*
- 5 - aid in separation of components, dust & synchrotron: *SZ*

WMAP1 .166+-.08 TE, WMAP3 .089+-.03 EE fgnd-clean,

WMAP5 .086+-.016, WMAP5 .090+-.019 GibbsMCMC; Planck1yr 09.3+1.5yr +-.005;

Spider test flight 2-6d, 2010.3, Alice Springs, +-.007

6- reionization epoch

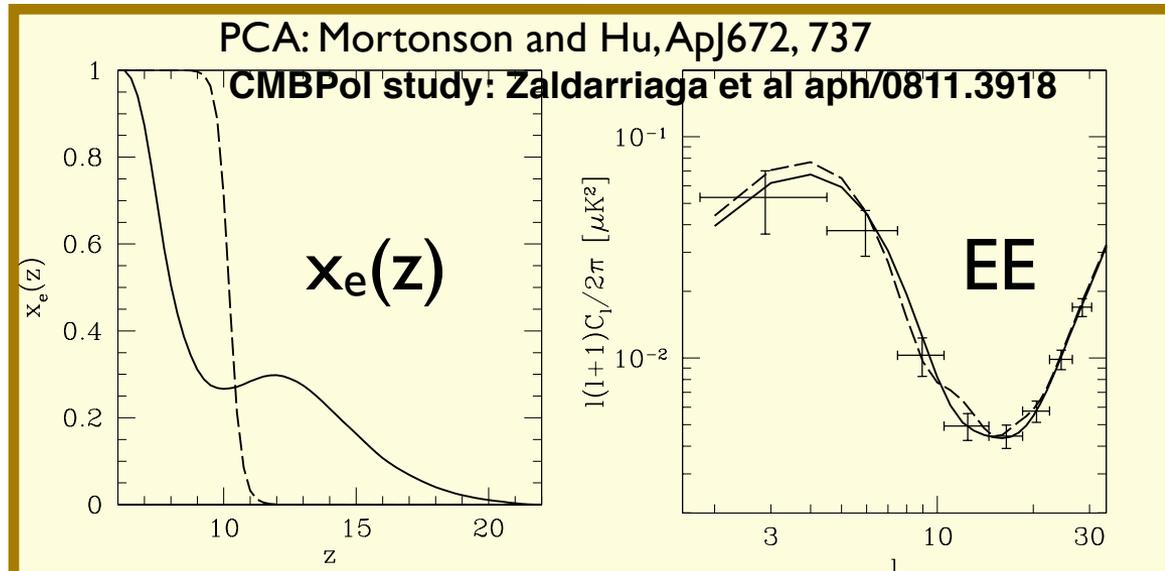
$$\tau_C = \int_{t_{\text{reion}}}^{\text{now}} n_e \sigma_T c dt$$

$$\sim .1 \left(\frac{1+z_{\text{reh}}}{15} \right)^{3/2}$$

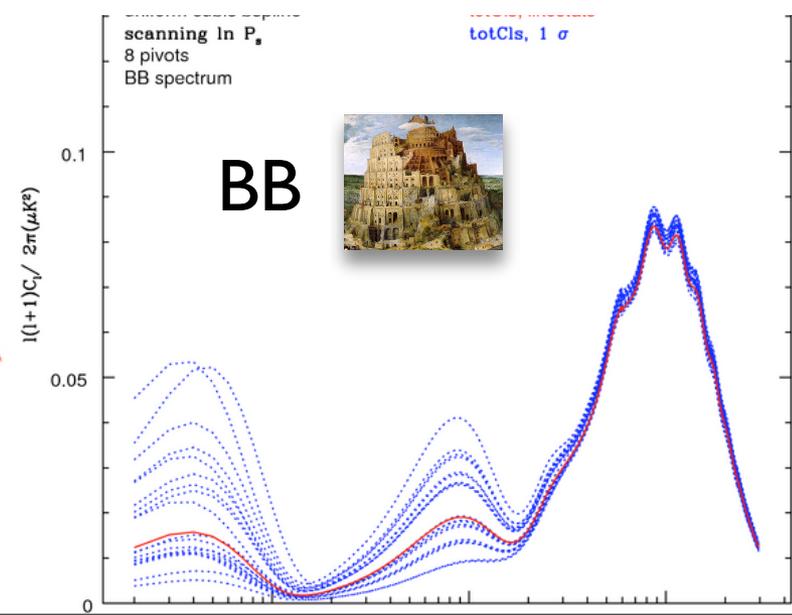
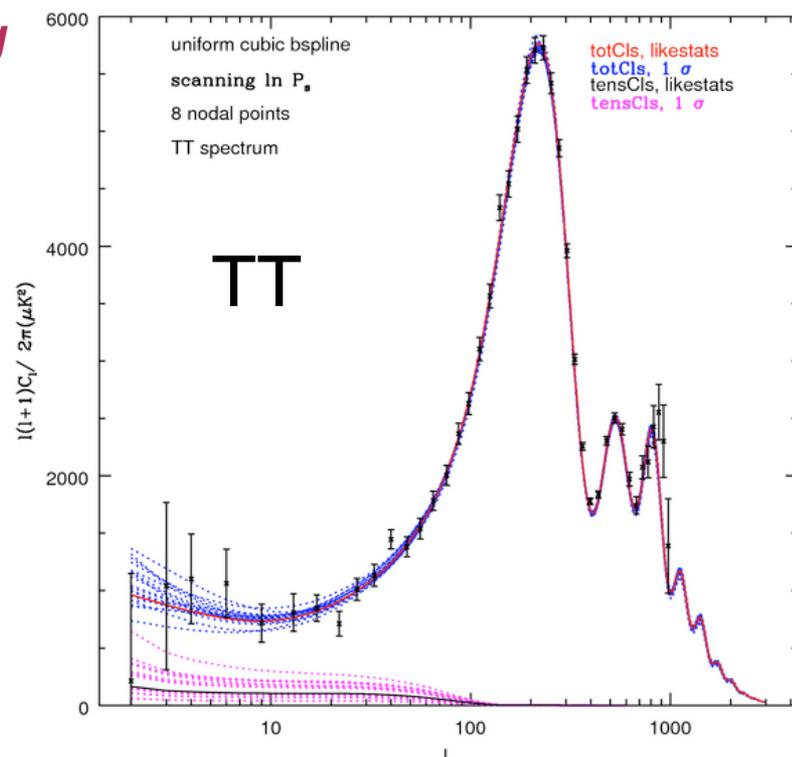
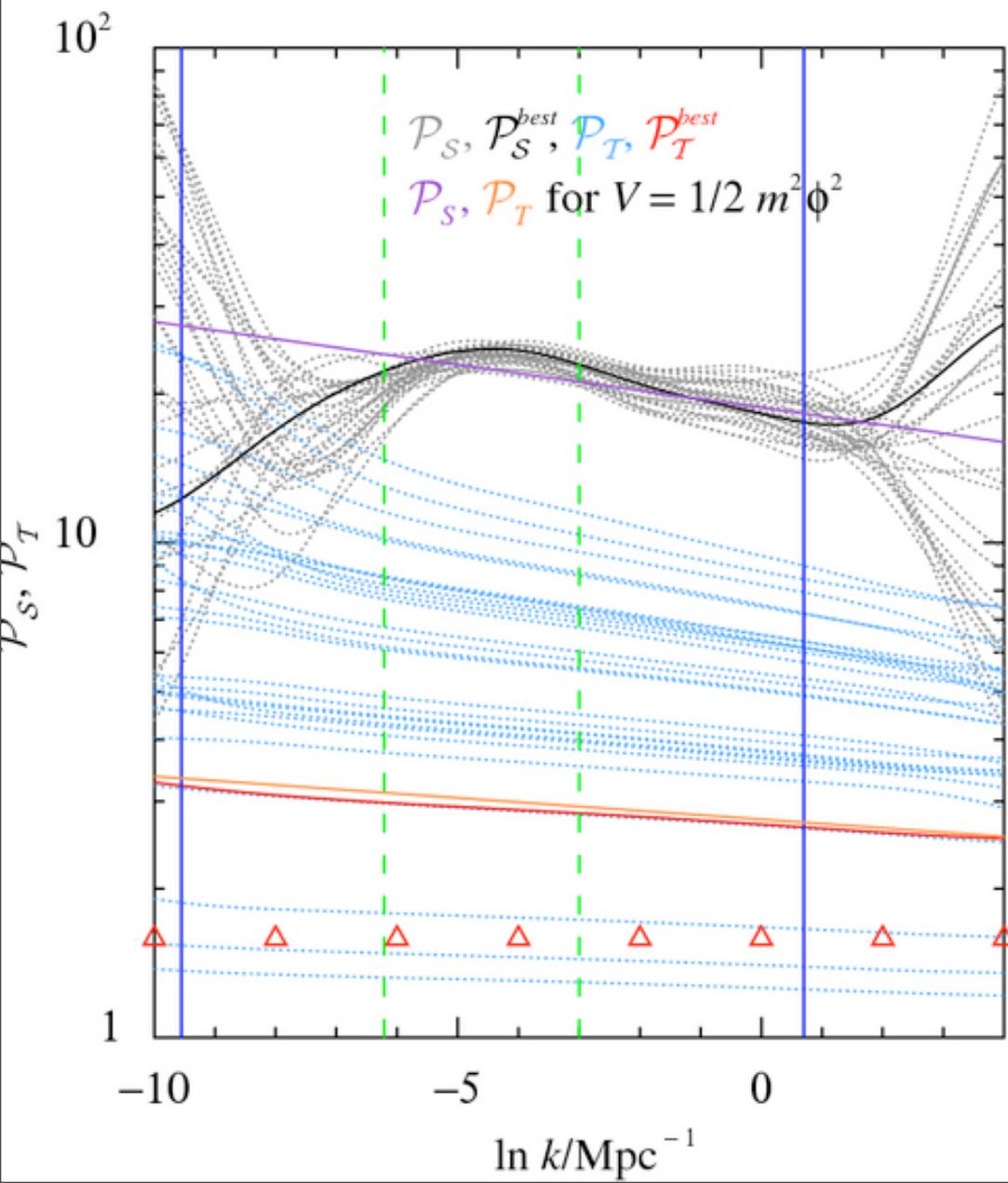
$$\left(\frac{\Omega_b h^2}{.02} \right) \left(\frac{\Omega_m h^2}{.15} \right)^{-1/2}$$

0.085+-.017 CMBall_{cbi10}

$z_{\text{reh}} = 0.8 \pm 1.5$

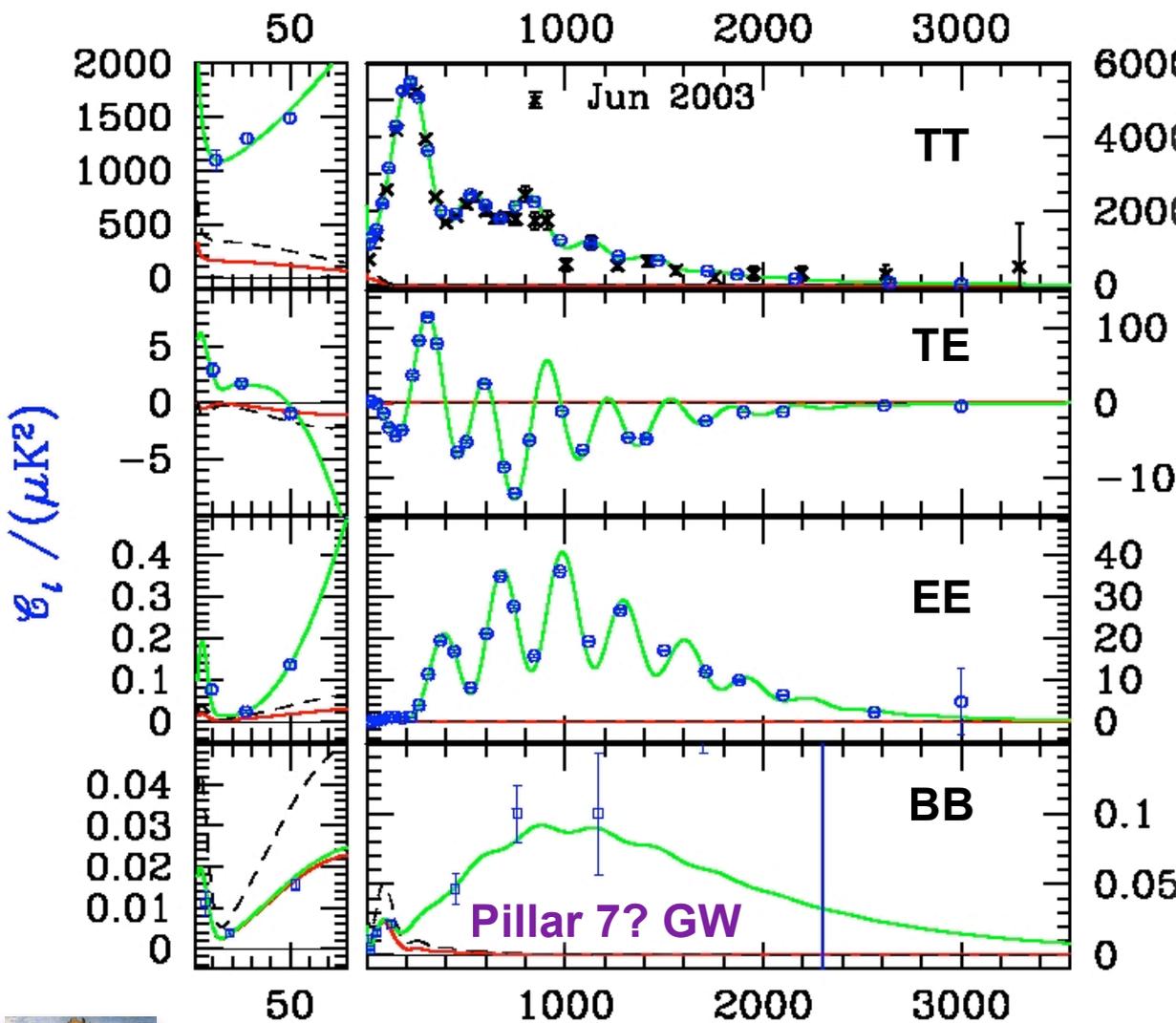


partially-blind acceleration trajectories obeying tensor/scalar consistency relation. May08 data



PRIMARY END @ 2012?

CMB ~2009+ Planck1+WMAP8+SPT/ACT/Quiet+Bicep/QuAD/Quiet +Spider+Clover



Pillar 7? Gravity Waves

An ensemble of trajectories arises in many-moduli string models, whether braney or holey. Roulette inflation: complex hole sizes in 6D TINY $r < 10^{-10}$ & n_s from data-selected braking! ('theorem': $\Delta\psi < 1 \rightarrow r < .007$)

nearly uniform acceleration (power law, exp, PNGB, ..potentials) $r \sim .03-.3!$ is $\Delta\psi \sim 10$ deadly?

Even with low energy inflation, the prospects are good with Spider plus Planck to either detect the GW-induced B-polarization or set a strong blind upper limit $r < 0.02$ indicating stringy or other exotic models. Both experiments have strong Cdn roles. Bpol 2020?, to $r \sim 0.002$

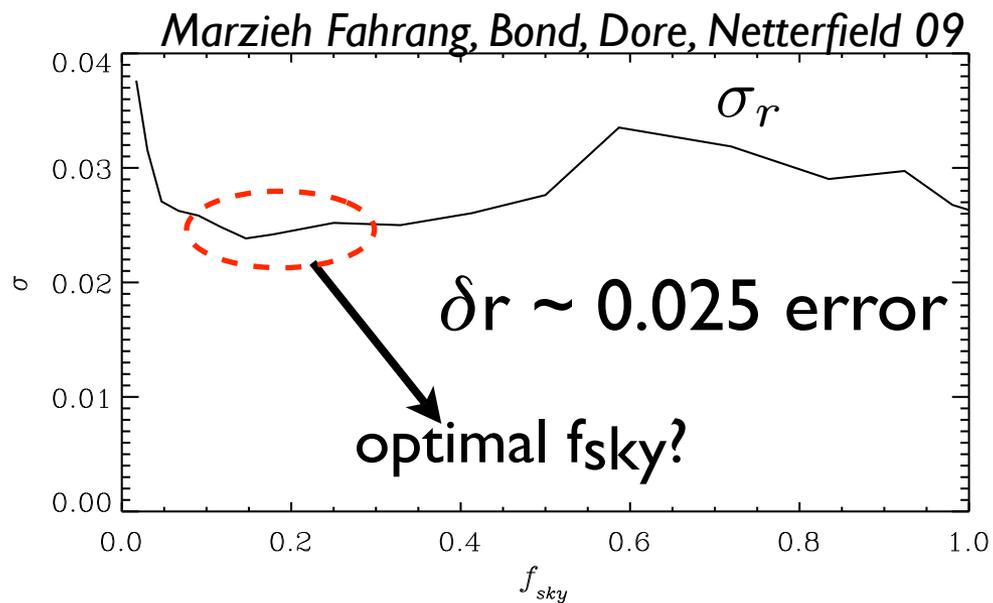
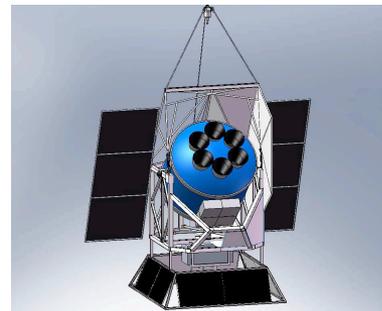
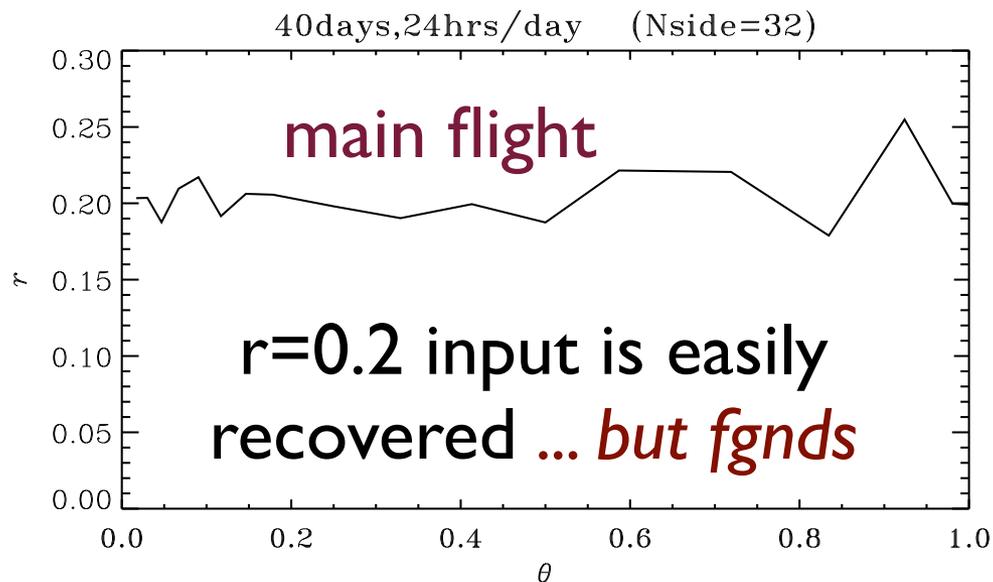
+ Pillar 4: primordial non-Gaussianity

$-9 < f_{NL} < 111$ (+- 5-10 Planck1)



Spider/Keck: best f_{sky} for E/B-demixing via direct max-L filters for r τ

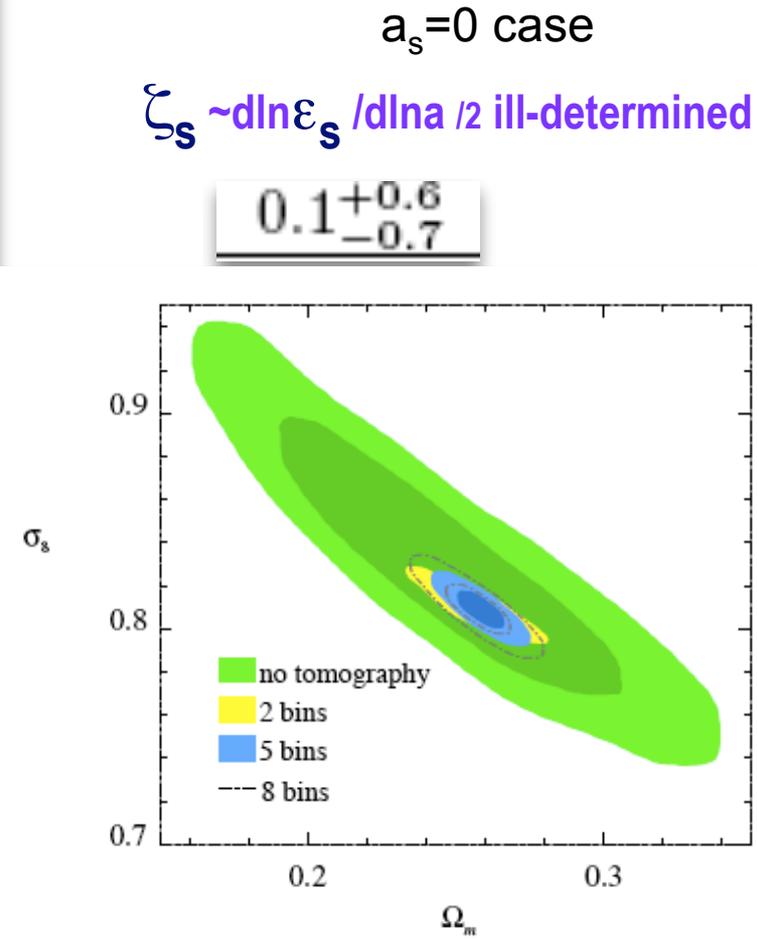
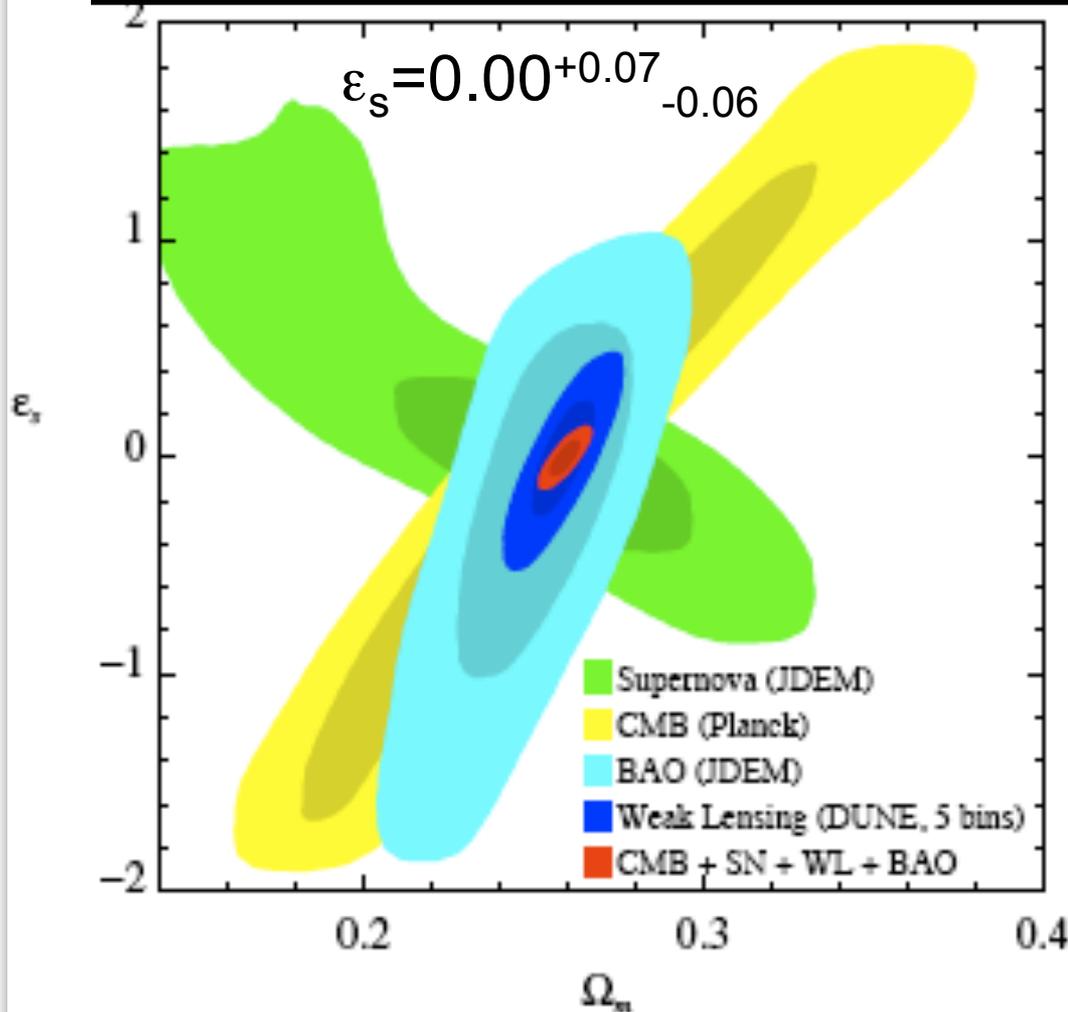
- ▶ test LDB flight: 2-6 days, 10.3 Alice Springs
- ▶ main LDB flight: 20-40 days, 11.9 Antarctica
 $N_t \sim 2.5$ Tbytes, $N_p \sim 10$ Mb



Beyond Einstein panel: LISA+JDEM

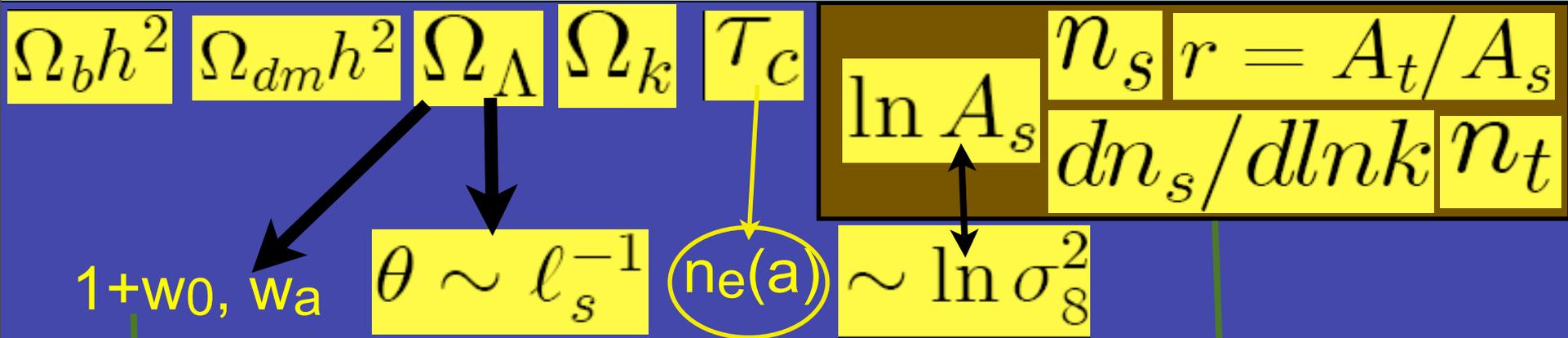
Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)

+ **DUNE-WL** (50% sky, gals @z = 0.1-1.1, 35/min²) + **Planck1yr**
now ESA /Eucid ESA (+NASA/CSA)



cannot reconstruct the quintessence potential, just the slope ϵ_s & ~hubble drag

Standard Parameters of Cosmic Structure Formation



New Parameters of Cosmic Structure Formation: early-inflaton & late-inflaton trajectories (& reionization histories)

$$\epsilon_\phi = (1+w(a)) \times 3/2 = -d \ln \rho_\phi / d \ln a / 2$$

$$\epsilon_s f(a/a_{\Lambda eq}, a_s/a_{\Lambda eq}, \xi_s)$$

$$\ln P_s(\ln k) \text{ \& } \ln P_t(\ln k)$$

$$\text{\& } r(k_p)$$

Blind trajectory analysis cf. data, then & now expand $\epsilon(\ln k) / \epsilon_\phi(\ln a)$ in localized mode fns e.g., Chebyshev/B-spline coefficients ϵ_b

ϵ_b -measures: "theory prior" = *informed prior*?

$$\epsilon_\phi(\ln k), k \sim H a \text{ \& } \ln H(k_p)$$

+ subdominant

isocurvature/ cosmic string/ tSZ ...