

from **SuperWeb simplicity** to **complex Intermittency** in the **Cosmic Web**

*Zeldovich 100th:
Moscow June 2014,
Tallin IAU 308 June 2014*

the Russian school & how Arnold fits into the evolving cosmic story 79-82 (Arnold, Shandarin & Zeldovich 1982)

our Hubble patch

Initial conditions: a Gaussian random field in energy density & spatial curvature

initial content: scalar fields (inflation) + gravity + ??

post-inflation heating content: the standard model of particle physics, quark/gluon plasma

content now: baryons in a gas, photons, neutrinos, (cold) dark matter, dark energy

linear evolution phase, to reheating $1/a \sim 10+$ when nonlinearity \Rightarrow the 1st stars form nonlinear SCALE grows, defining the evolving cosmic web

ingredients now: clusters/groups = halos of Dark Matter, filaments, membranes, voids; galaxies, stars

IN EVERY teaspoon of air ~ 5 cubic cm

Ordinary Matter $\sim \text{amu} / \text{nm}^3$ 4.8% O₂ N ; H,He

THE DARK

Dark Matter

$\sim \text{amu} / \text{m}^3$ $26.0 \pm 1\%$ compressed in MilkyWay $\sim 0.1 \text{ amu} / \text{cm}^3$;
for LHC@CERN-type relics ~ 1 every 10 cm

Dark Energy

\sim vacuum potential $\sim 3 \text{ amu} / \text{m}^3$ $69.2 \pm 1.0\%$

THE LIGHT

cosmic radiation

the 1st light of the universe $412 / \text{cm}^3$ 0.005%

cosmic neutrinos \sim cosmic photons $> 0.47\%$

cosmic gravity waves \ll cosmic photons

THE VACUUM

Higgs@CERN vacuum origin of mass

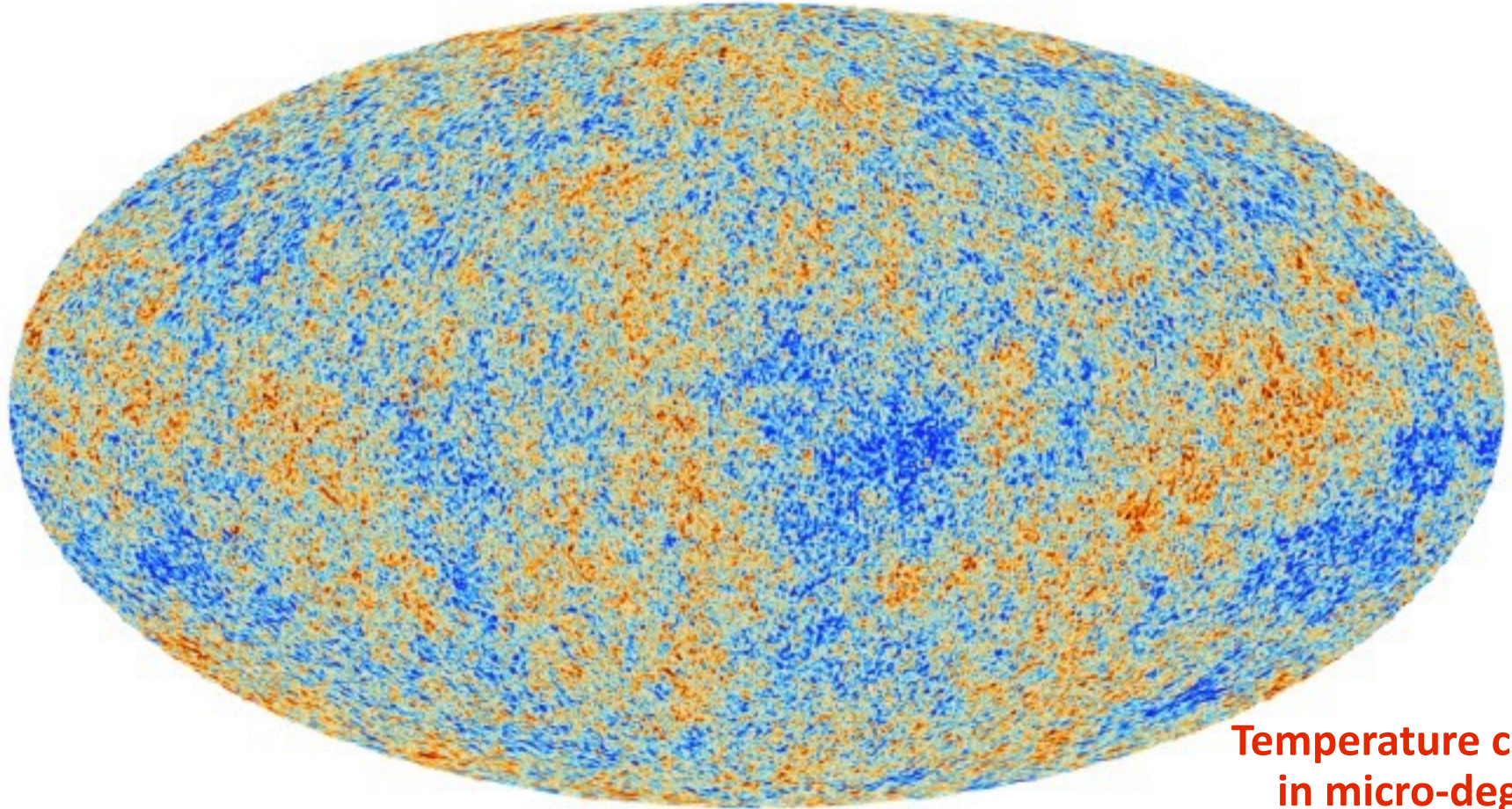
vacuum fluctuations origin of all the cosmic structure we see

Planck's primordial light unveiled, March 21, 2013 (Dec. 1, 2014)

reveals the **SIMPLICITY** of primordial cosmic structure
in 7+ numbers

=> learn **matter & energy content & structure** at $a \sim e^{-7}$ 380000 yr

=> infer structure **far far earlier** $a \sim e^{-127} \sim 1/10^{55}$ **in ~2 numbers**



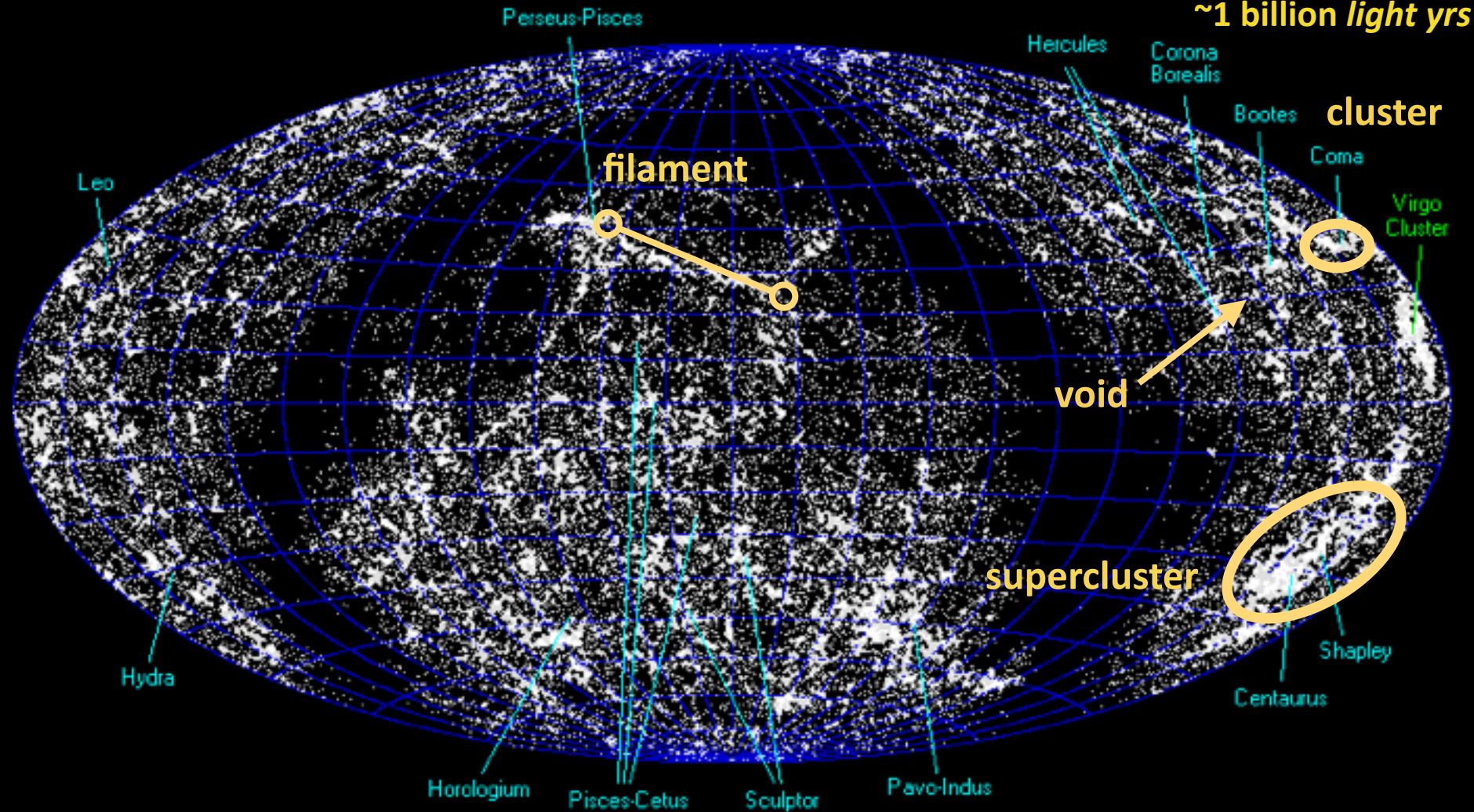
**Temperature changes
in micro-degrees**

**Gaussian 2D temperature field @ 370000 yrs => Gaussian
random 3D density field from the ultra-early universe**

Cosmic Web of 60,000 nearby galaxies: exhibits “local” COMPLEXITY

$$a \sim e^{-0.1} = 1/1.1$$

~1 billion light yrs

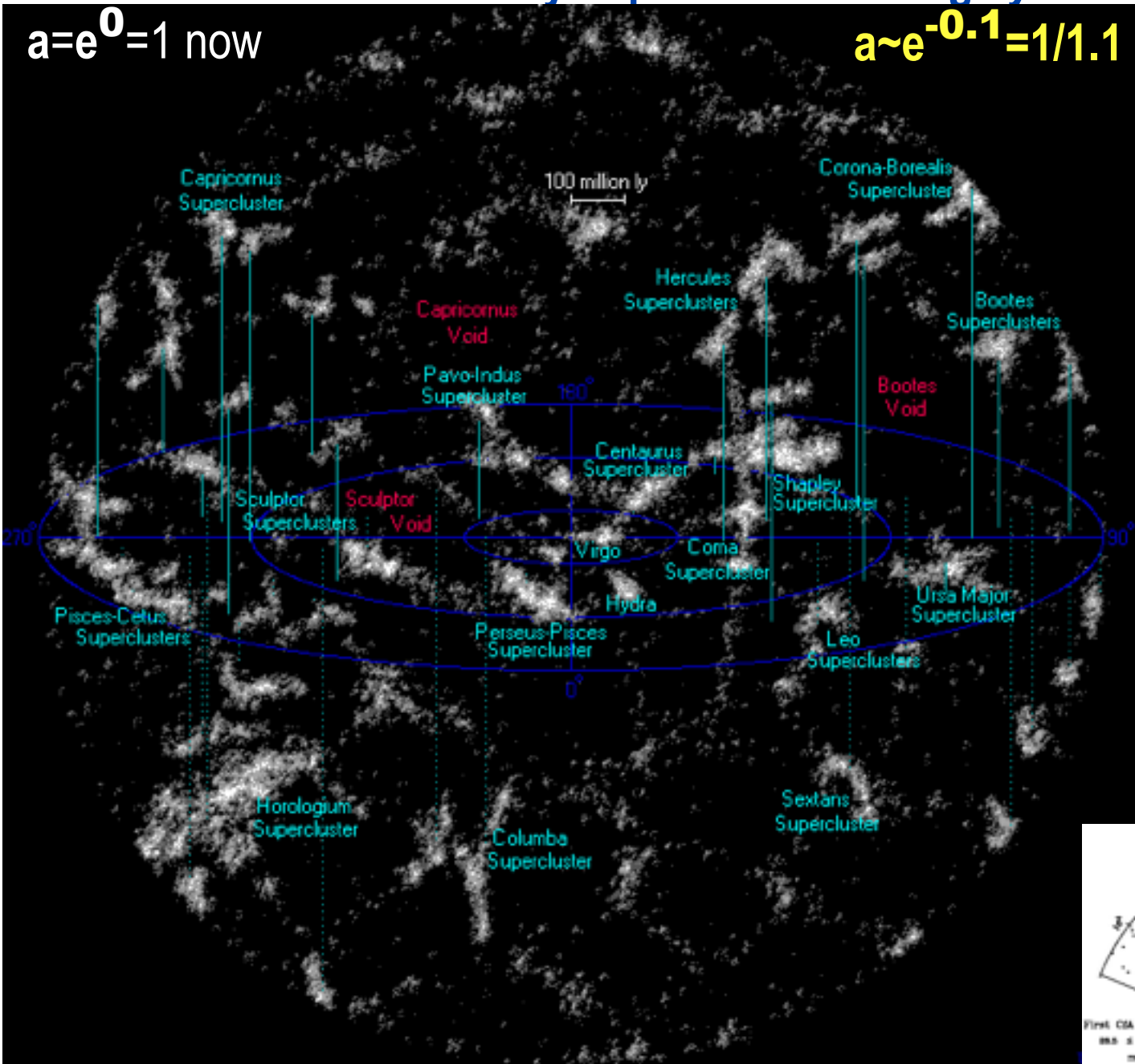


hard won observational emergence of the web. 79-81 sparse info, e.g., of Coma supercluster. So what Arnold, Shandarin and Zeldovich knew was very very much less, ie speculative theory

to $a \sim 0.9$ via **3D maps**
cosmic web of nearby superclusters < Giga/yr

$a=e^0=1$ now

$a \sim e^{-0.1} = 1/1.1$

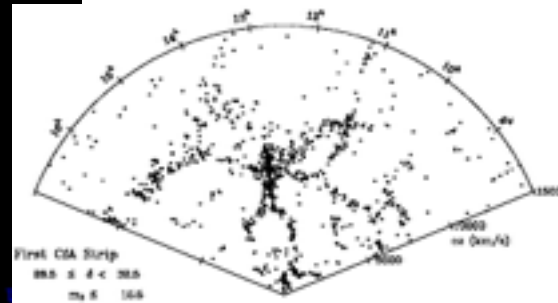


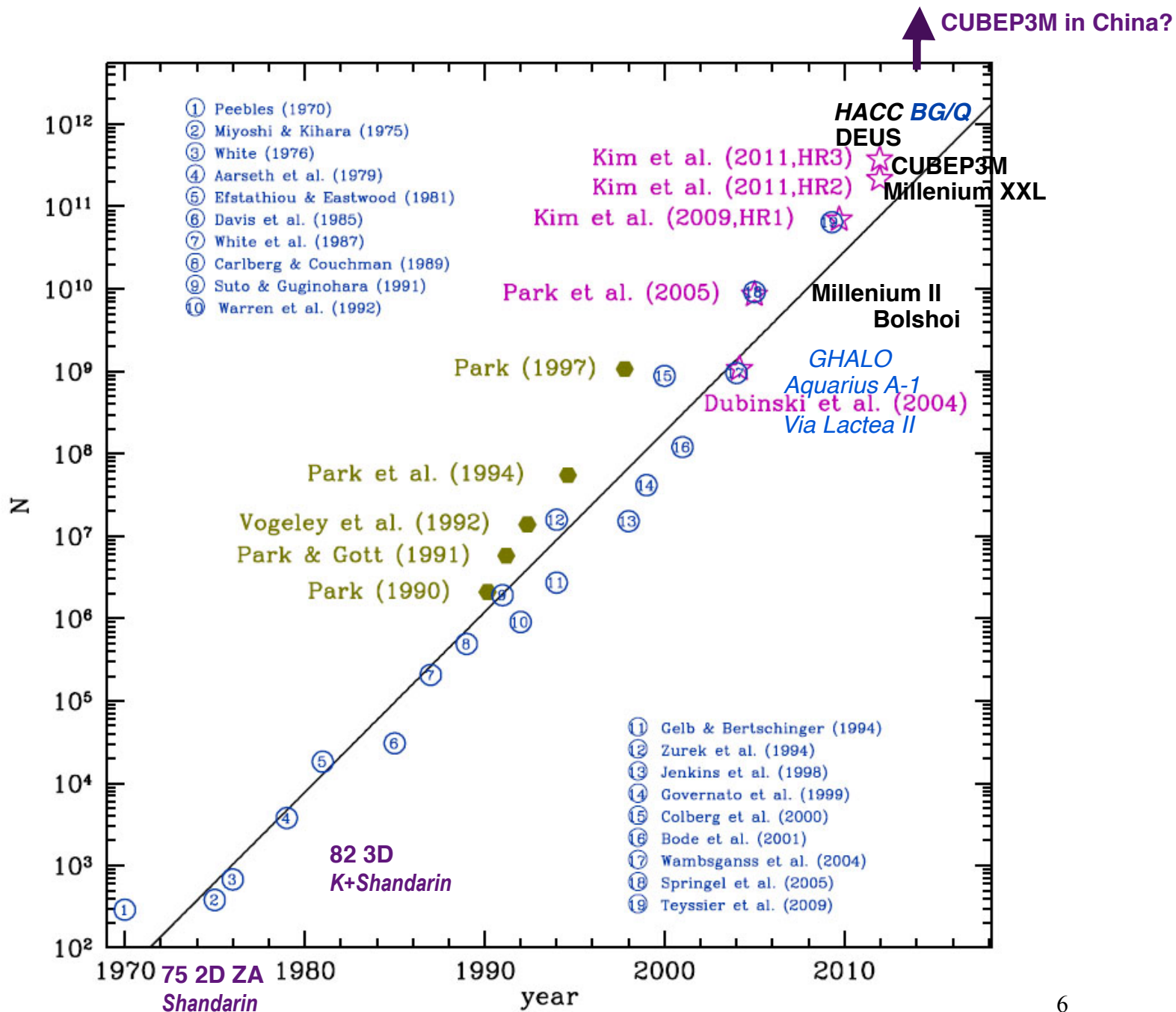
70s adiabatic
 pancake
 (physical filter)
 Doroshkevich, Zeldovich
 cf.

70s isoc B/BH
 (power law CorrFn)
 Basko

**miracle of
 CDM = grand
 unification
 of east & west
 ideas
 with ~ HSZ
 spectrum
 emergence of
 superclusters**

*Peebles vs.
 70s Einasto+..
 80 + Oort +*





Simulation of the 7⁺ numbers

begets the **Cosmic Web** of clusters now $a \sim 1$ & galaxies then $a \sim 1/4$

SIMPLICITY to COMPLEXITY under Gravity

void

filament

cluster

supercluster

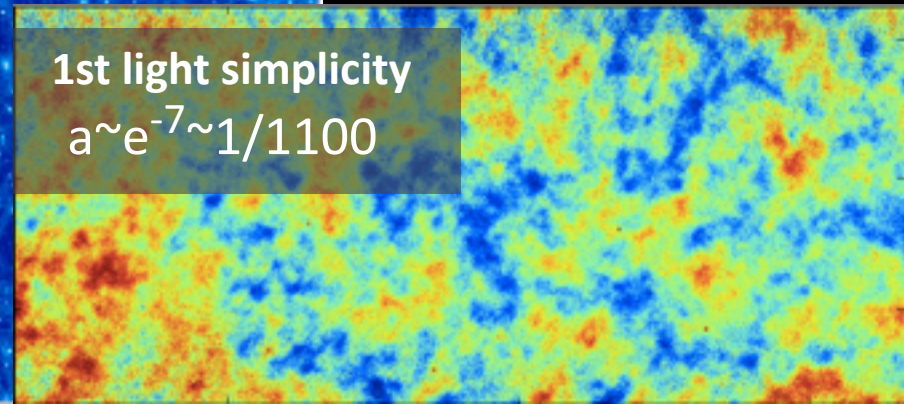
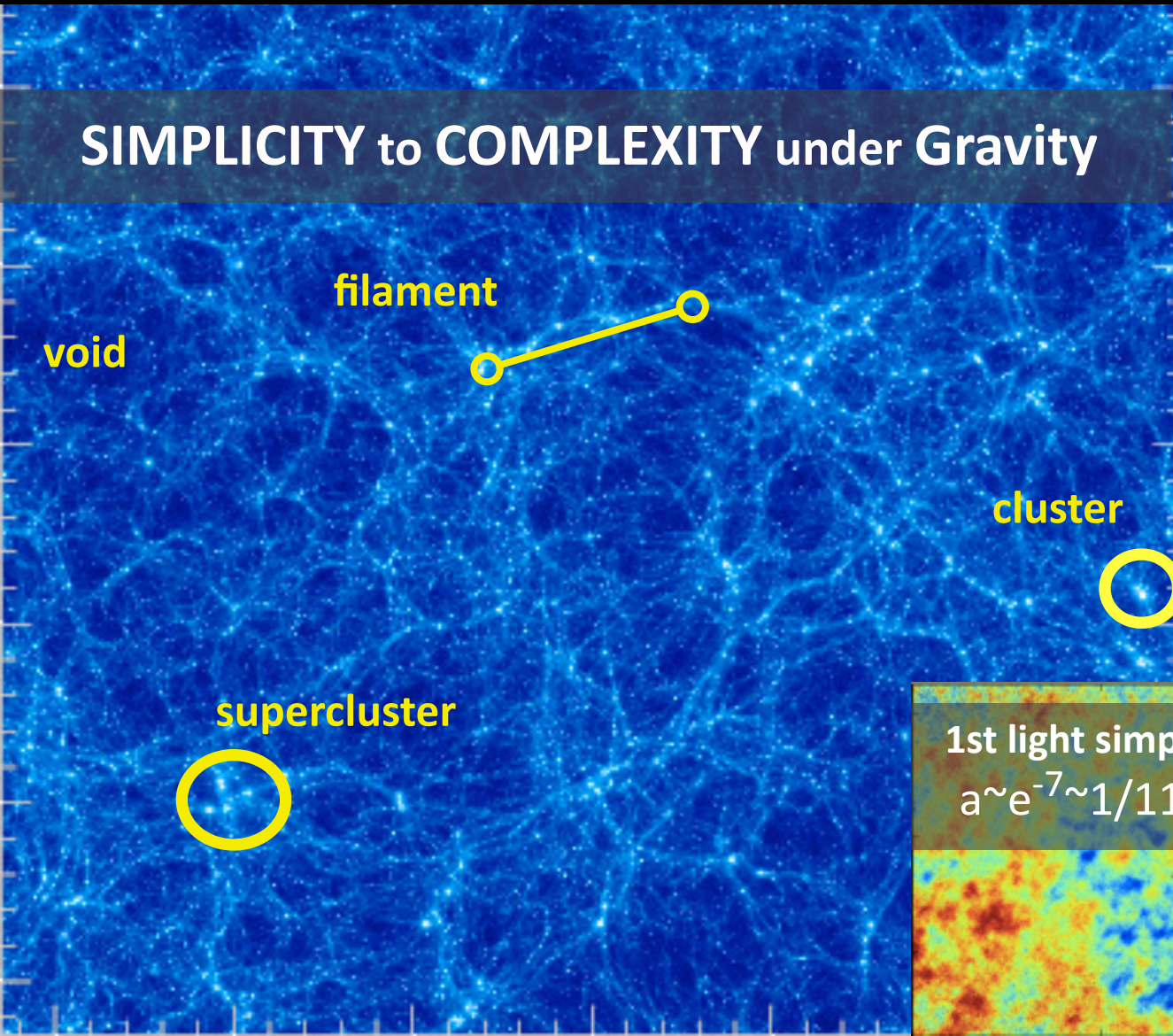
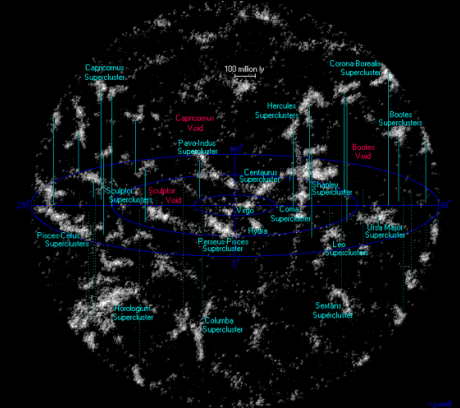
\sim billion light years

state of the art simulation
 $a \sim 1$ to $1/1.1$

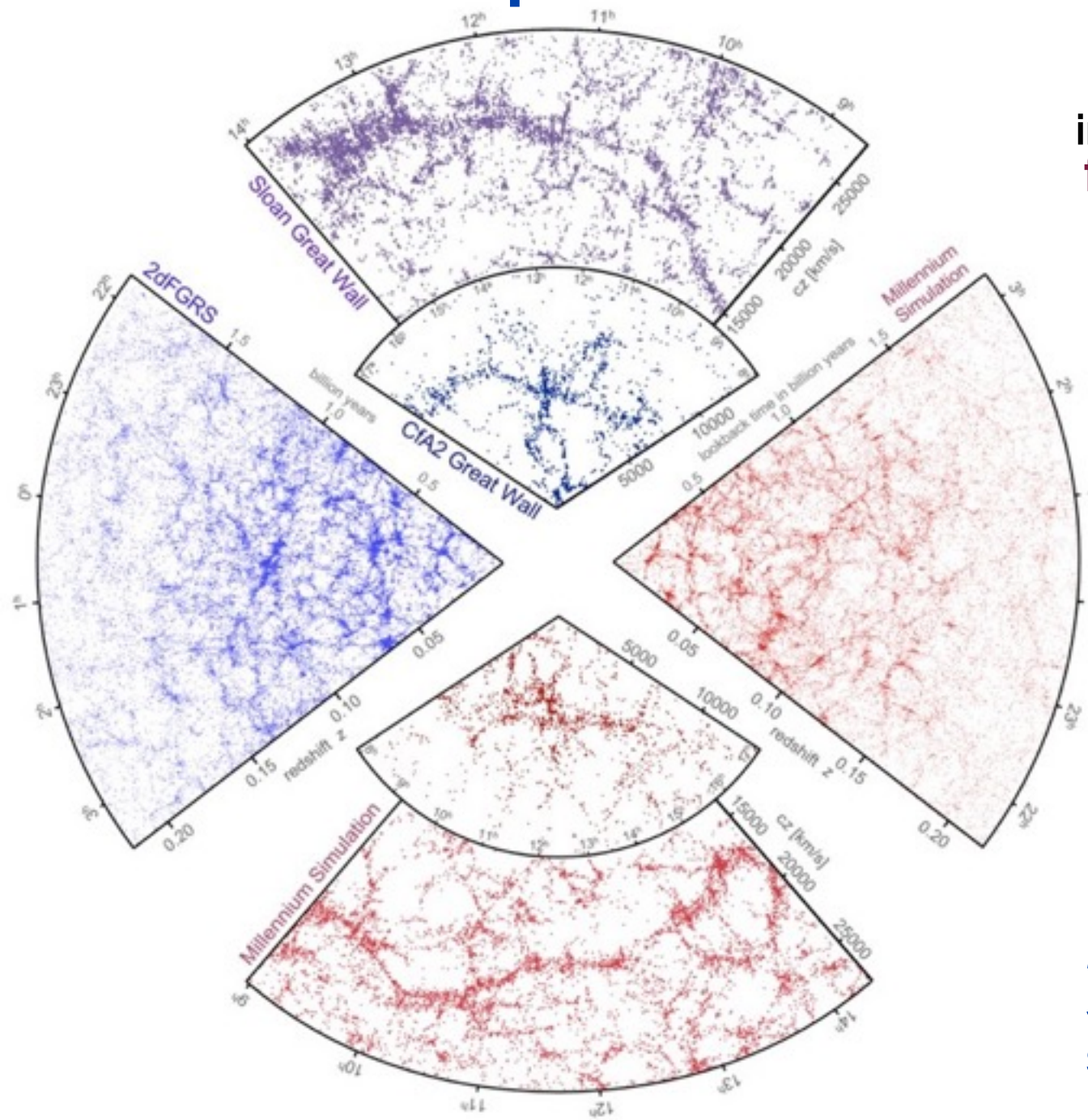
ordinary matter
dark matter
dark energy

1st light simplicity

$a \sim e^{-7} \sim 1/1100$



to $a \sim 0.8$ via 3D maps



Collisionless matter

Simulation of the initial **Gaussian random field** characterized by **7^+ numbers**

does indeed beget the **Cosmic Web**

Millennium simulation web site "propaganda" on sims cf. z-space data

and to **a ~ 0.7 to 0.5 via 3D maps**

VIPERS using VIMOS@VLT release Oct 4, 2013, 57K redshifts, $z=0.45$ to $z=0.95$, $6e7 (h^{-1}\text{Mpc})^3$, higher sampling than LRG BAO surveys Guzzo+13 cover CFHTLS wide fields, 64% done, 24 sq deg

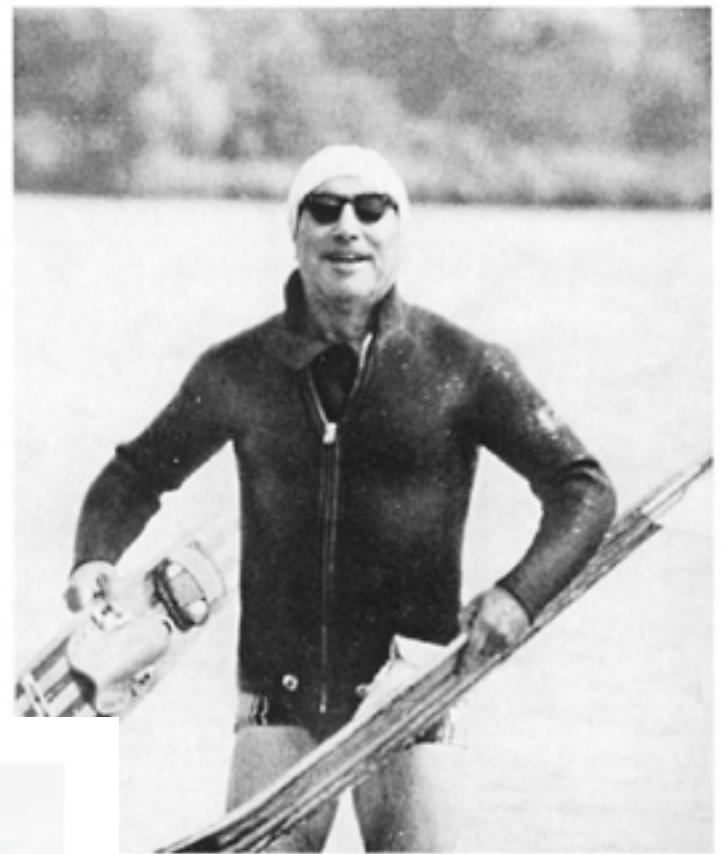
Field W1



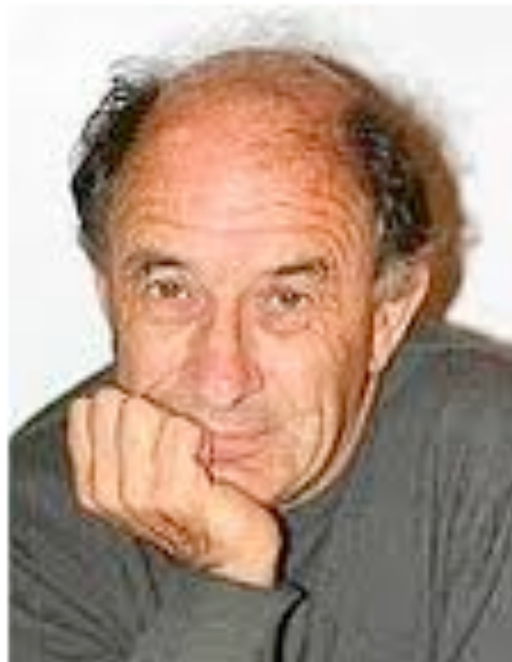
Field W4



Yakov Borisovich
Zel'dovich
1914 - 1987



Vladimir Igorevich
Arnold
1937 - 2010



На здравье

Terviseks



Z70,ZES82
AZS82
eJ



Zeldovich 1970 approximation $\mathbf{X}(\mathbf{r},t) = \mathbf{a}(t) (\mathbf{r} + \mathbf{s}(\mathbf{r},t))$
general map of a cold medium, an onto multi-stream map

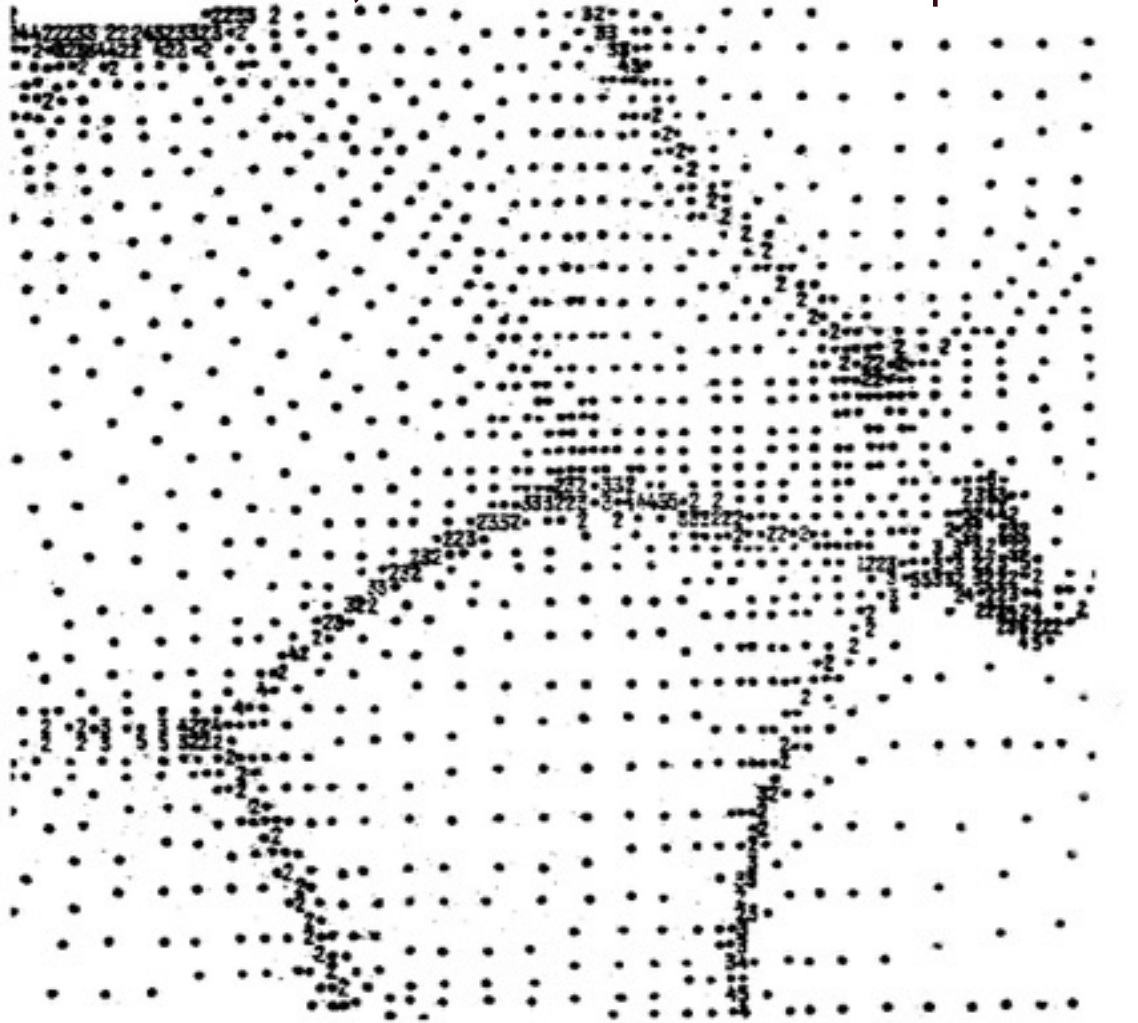
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influential for Arnold,
Shandarin Zeldovich 1982



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brief history of understanding objects and their distribution in the cosmic web

50s+ HALOS hierarchy, small round objects => large round objects

70s: Doroshkevich, Shandarin, Zeldovich: 1st order Lagrangian dynamics, statistics of 1D collapsing entities (caustics & pancakes) in a GRF; 80s: Arnold, Shandarin & Zeldovich: influential picture of 1st order catastrophes; $1D \Rightarrow 2D \Rightarrow 3D$ pancake \Rightarrow filament \Rightarrow cluster flows

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80s: hot, warm & **cold** collisionless **dark matter** paradigm \Rightarrow **Λ CDM**

87: **Λ** includes vacuum energy

90s-00s: data settled on **Λ +tilt \Rightarrow dark-energy +tilt**

$\mathbf{X}(\mathbf{r},t) = a(t) (\mathbf{r} + \mathbf{s}(\mathbf{r},t))$ general map of a cold medium, an onto multi-stream map;
 $dX^i/a = (V^i - HX^i)/a dt + \mathbf{e}_i^l(\mathbf{r},t) dr^l = v_{pec}^i dt + (\delta_i^l + \boldsymbol{\varepsilon}_i^l(\mathbf{r},t)) dr^l$, where
 $\rho_m / \langle \rho_m \rangle = 1 + \delta_m = 1 / \det(1 + \boldsymbol{\varepsilon}) \Rightarrow \ln \rho / \langle \rho \rangle = -\text{Trace} \ln(1 + \boldsymbol{\varepsilon})$ **$\boldsymbol{\varepsilon}$ = strain tensor**

Lagrangian 1st order linear $\mathbf{s}(\mathbf{r},t) = D(t)\mathbf{s}(\mathbf{r}) = -D(t)\nabla\psi_s(\mathbf{r})$ separable 1-1 & onto \Rightarrow caustics,

$\Delta\psi_s = \delta_L = -\text{Tr} \boldsymbol{\varepsilon} = \Phi_P (\mathbf{a}/D) / 4\pi G \langle \rho_m \rangle a^3$ $\boldsymbol{\varepsilon}$ ~ tidal tensor: velocity potential $\psi_v = -dD/dt \psi_s$, $d\boldsymbol{\varepsilon}/dt$ ~ shear

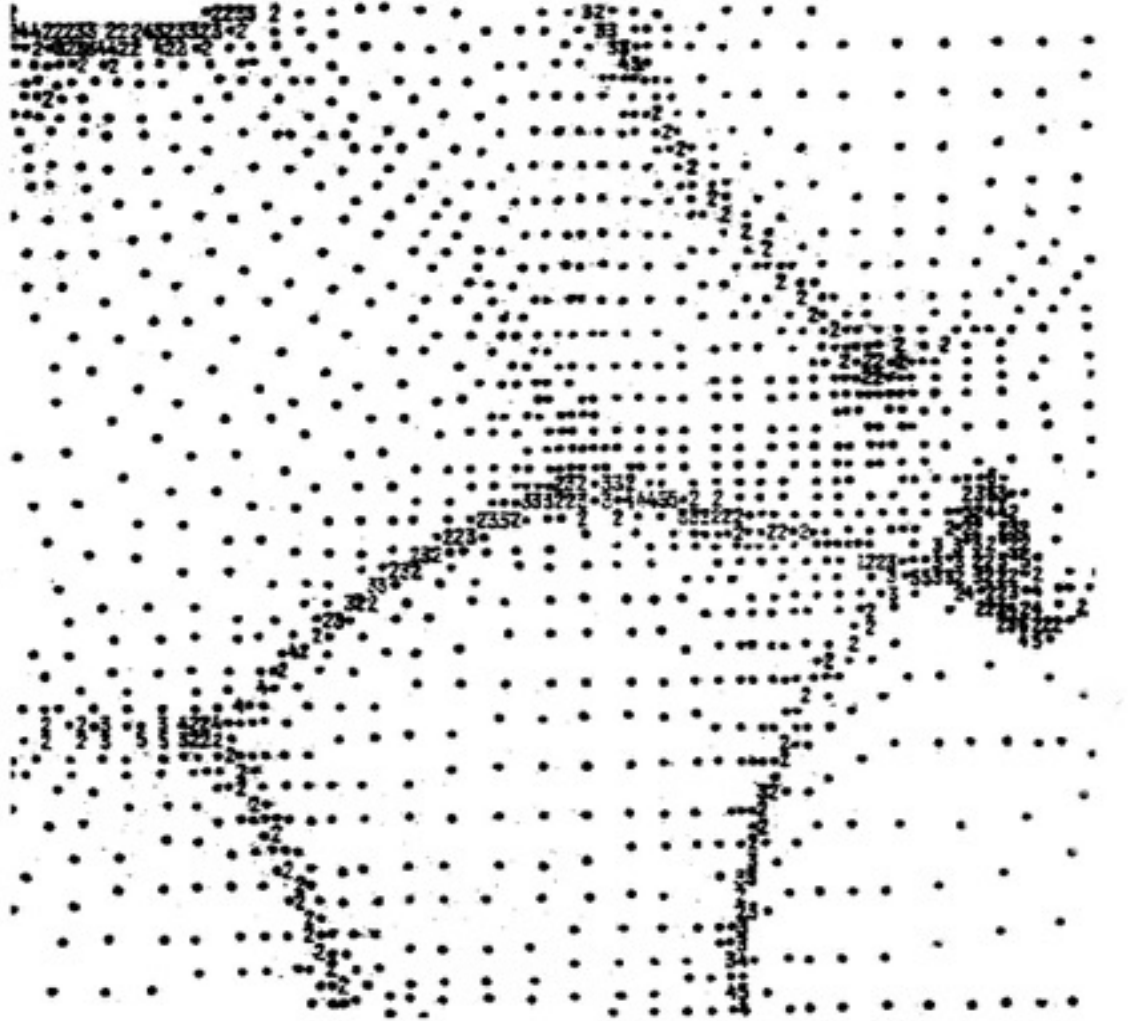
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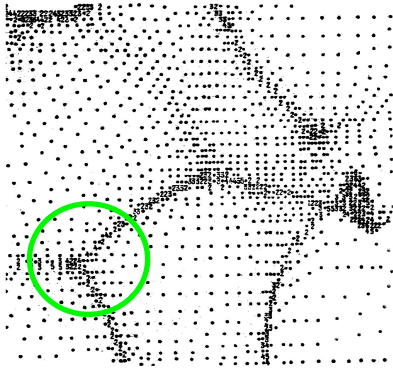
**Later in
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Shandarin 1978**

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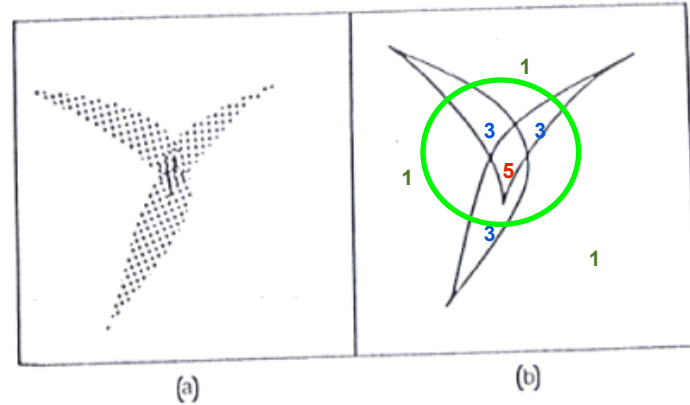


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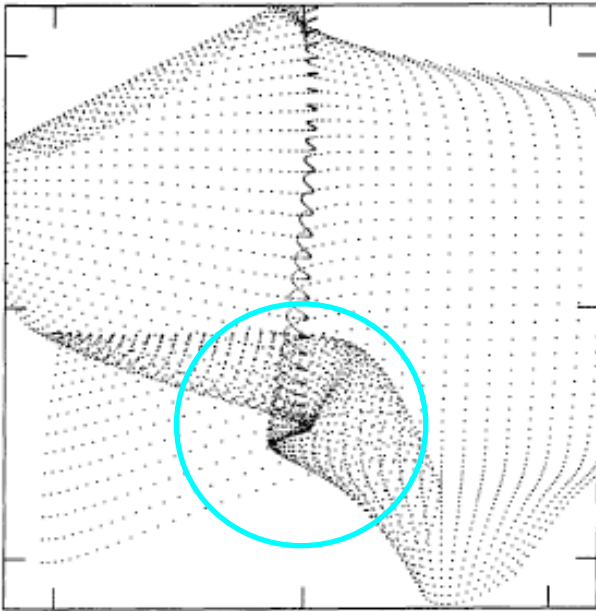
2D example: A4 (“swallow tail”) singularity



Shandarin 1975

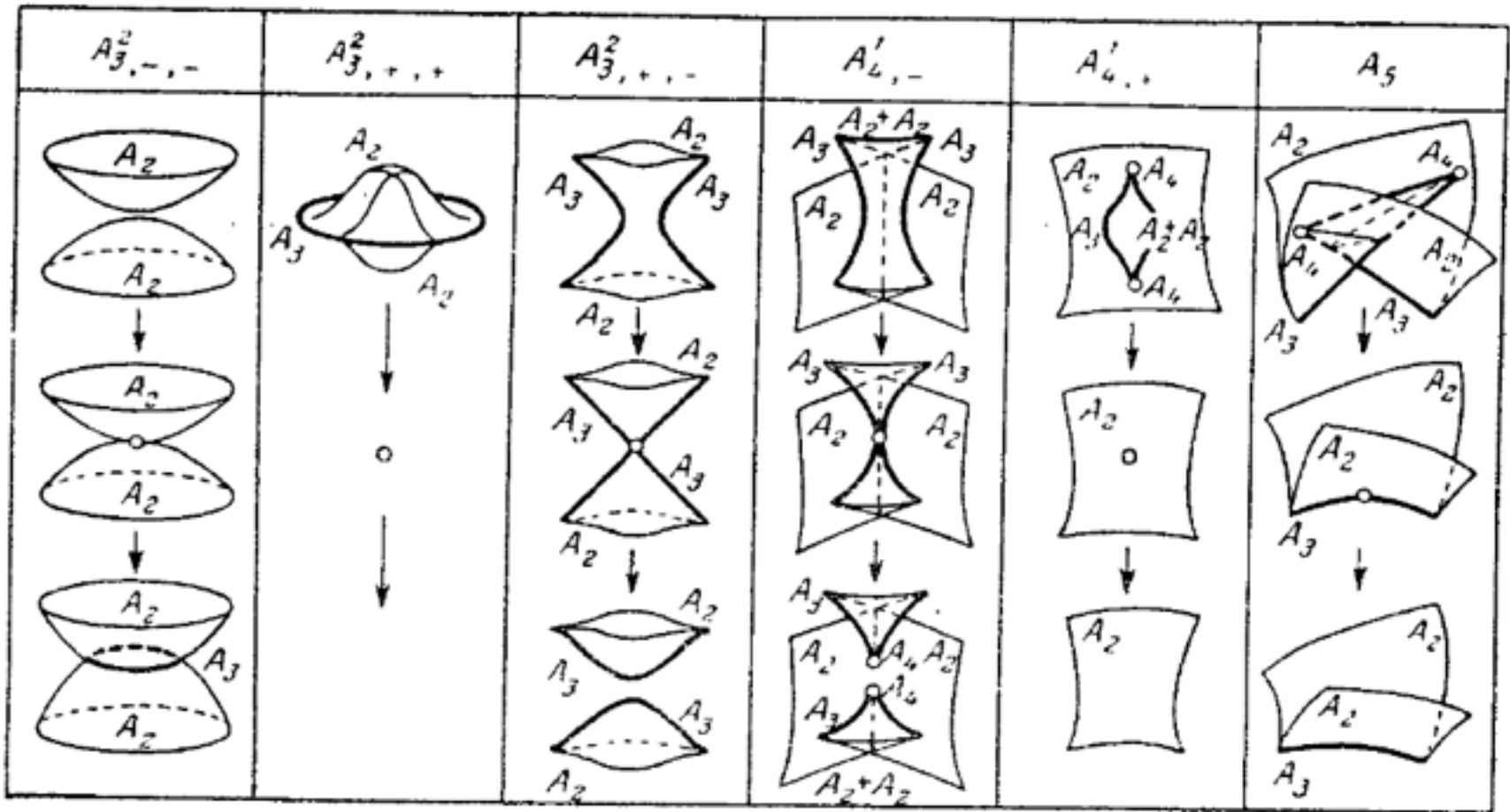


Arnold, Shandarin, Zel'dovich 1982



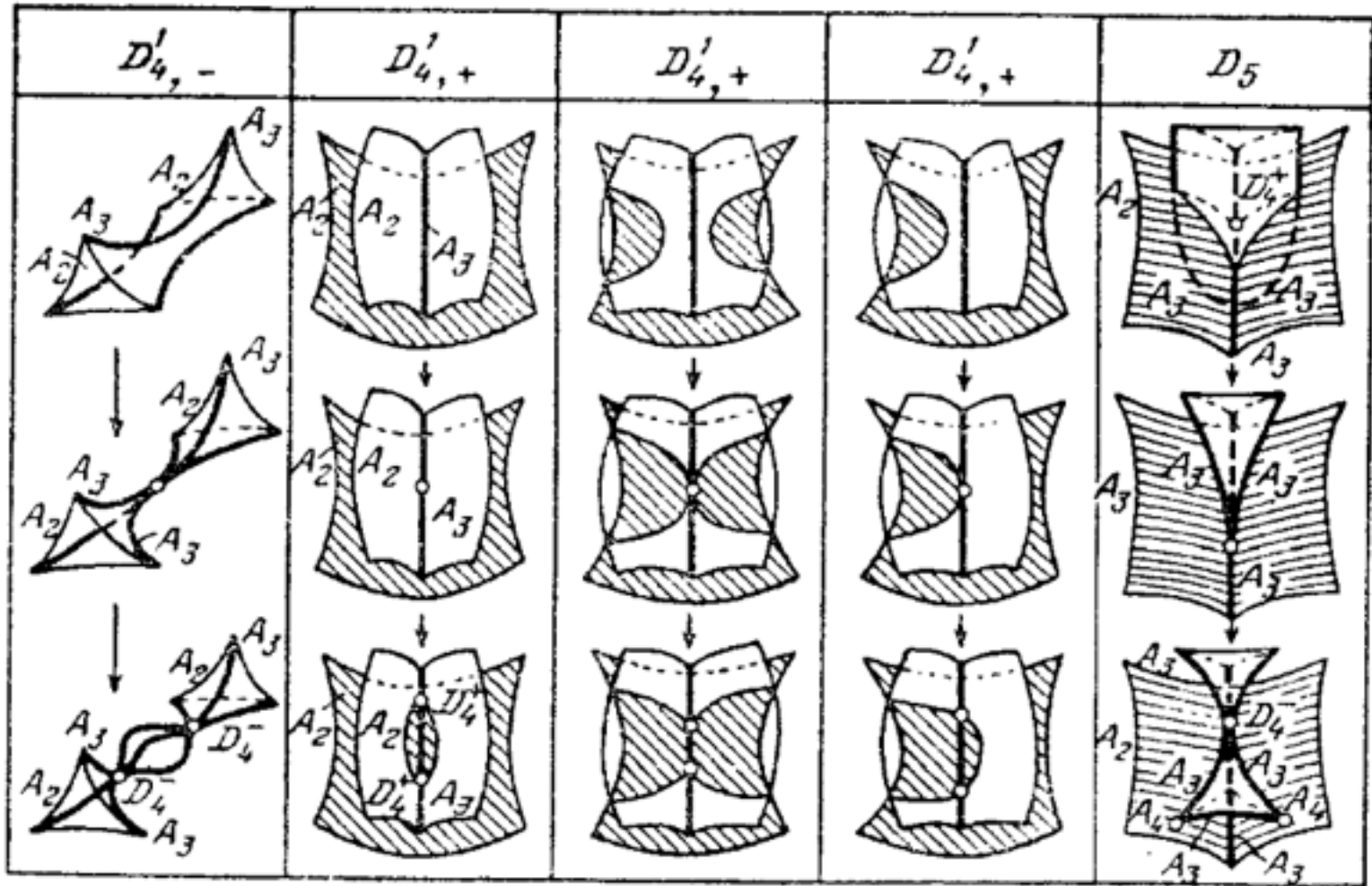
Nusser, Dekel 1990

A - caustics in 3D



Arnold, Shandarin & Zeldovich 1982

D - caustics in 3D



Arnold, Shandarin & Zeldovich 1982

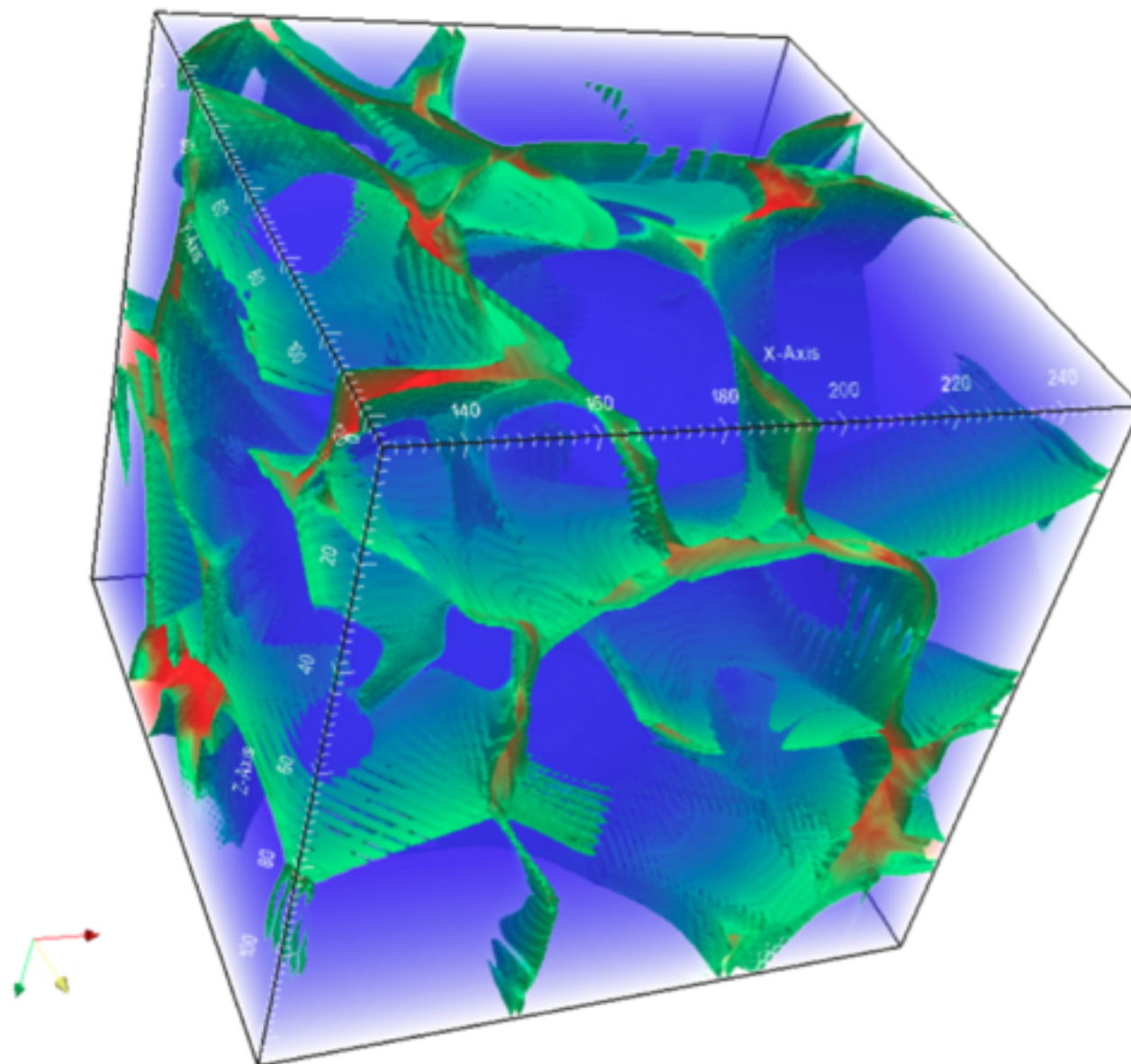
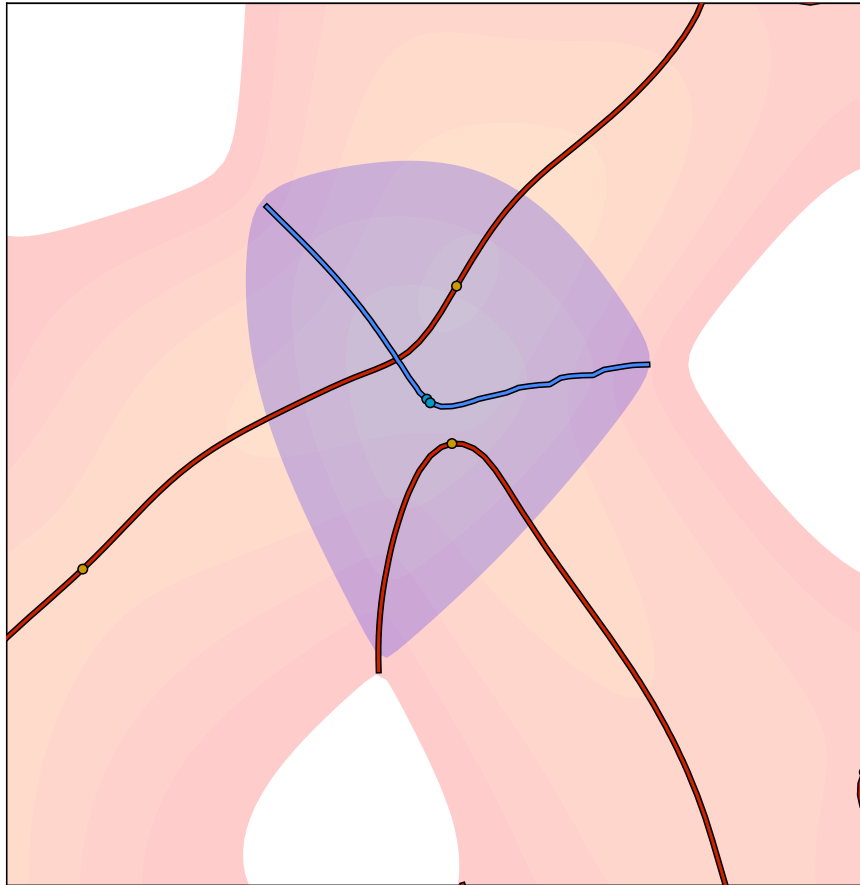


Figure 18. Caustic structure of ZA-evolved mass distribution in 3D. This is a three-dimensional analogy of the top right-panel in Fig. 1. The α -caustics are shown in green and β -caustics in red. The β -caustics are seen only through the openings in the surface of α -caustics by the box faces. This is the reason why one cannot see γ -caustics.

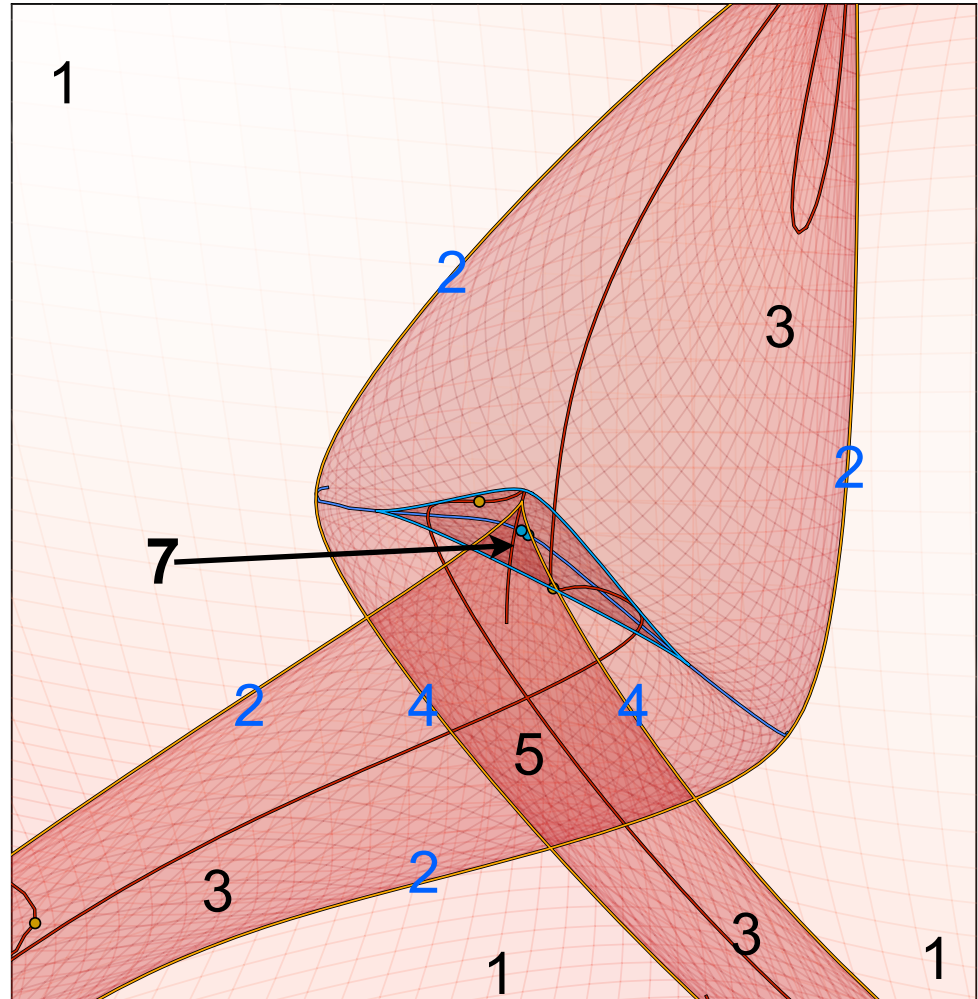
Complexity of caustics



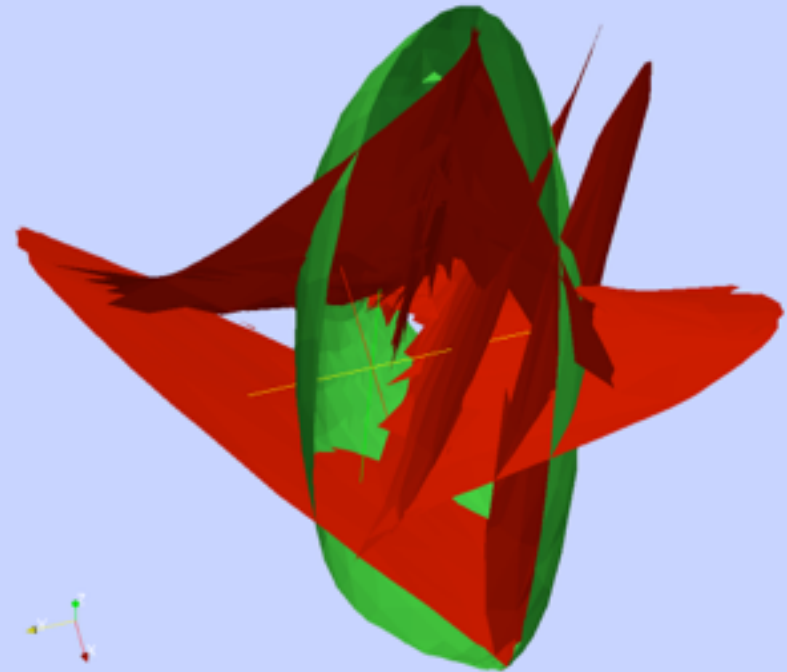
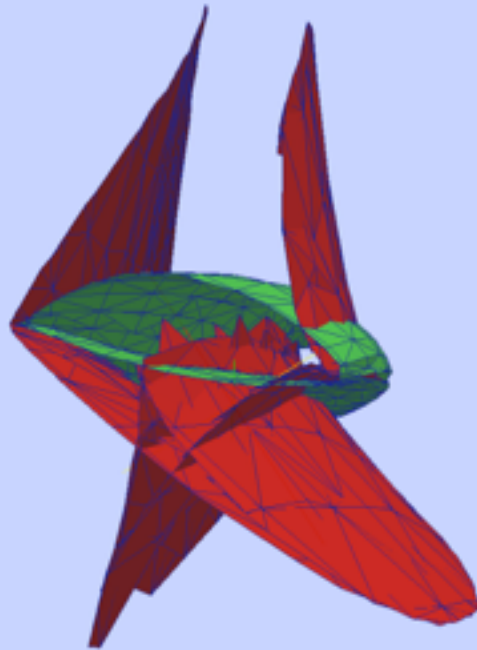
Lagrangian space

Hidding,
Shandarin,
van de Weygaert
2014

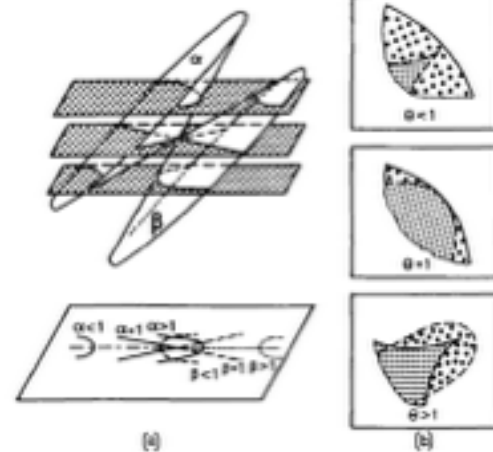
Number of streams
in Eulerian space



D₄ singularity in 3D space



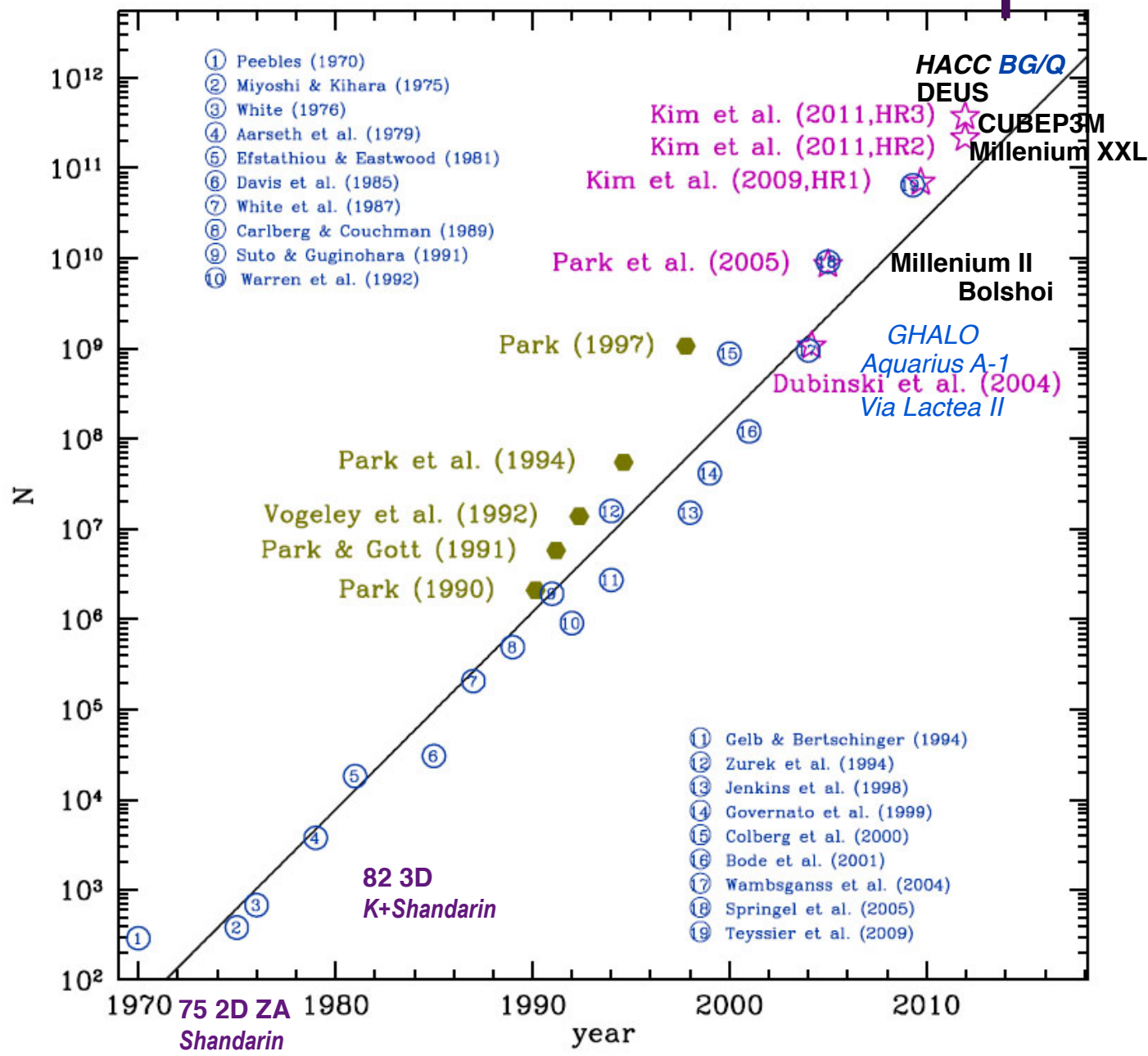
Hidding, Shandarin,
van de Weygaert
in preparation



Arnold,
Shandarin,
Zeldovich 1982

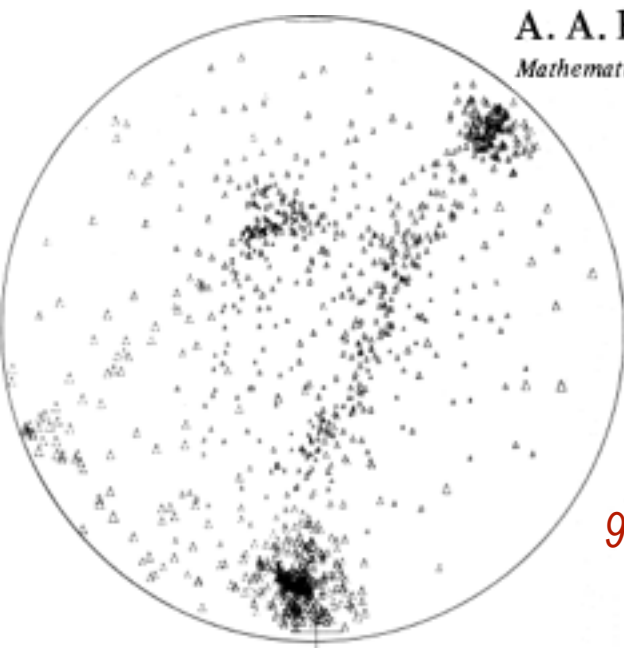
2D

CUBEP3M in China?



(Juhan Kim et al. 2011)

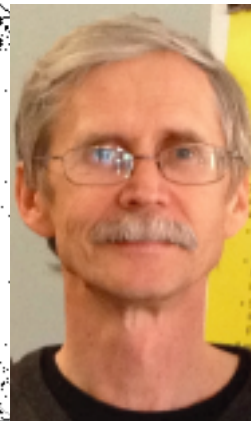
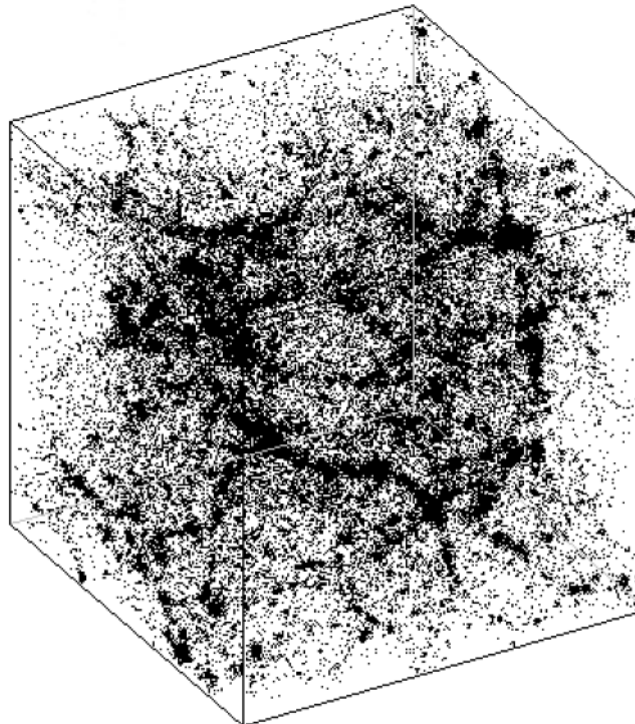
Received 1982 November 15; in original form 1982 April 28



*Klypin's vintage 82
160h⁻¹Mpc box 32³ hDM*

*It is possible to recognize
some webs connecting
these 'clusters of galaxies'*

90s Klypin to CITA, 'the west is best'



Klypin's vintage 93 50h⁻¹Mpc box 128³ sCDM = BKP98 web workhorse, Couchman's 128³ for BM91-96

entropy intermittency in the cosmic web, via gravitation-induced shocks (then E/S-feedback)

Secondary Anisotropies
(tSZ, kSZ, WL, reion, CIB; hydro)

$\Delta S_{\text{gas,th}} \approx 30$ Entropy-per-gas-baryon

$S_{\text{b,th}}(\mathbf{x}, \mathbf{t})$

baryons get entangled in the cosmic web

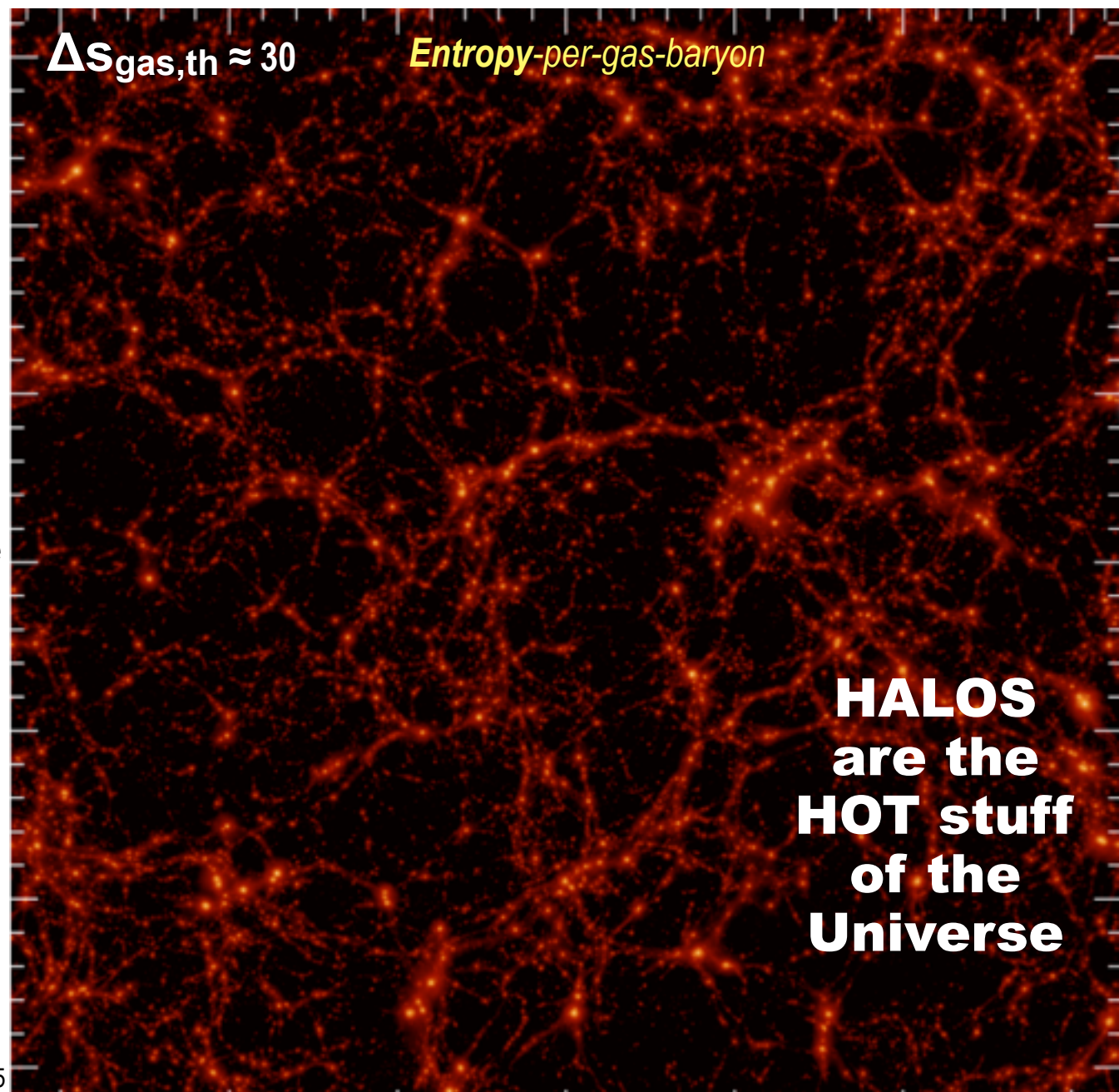
Let there be HEAT

$\rho_{\text{g}}(\mathbf{x}, \mathbf{t})$
 $\rho_{\text{stars}}(\mathbf{x}, \mathbf{t})$
 $\rho_{\text{e}}(\mathbf{x}, \mathbf{t})$
 $I_{\nu}(\mathbf{x}, \mathbf{t})$
 $n_{\text{dust}}(\mathbf{x}, \mathbf{t})$

HALOS
are the
HOT stuff
of the
Universe

non-Gaussian
CDM
entanglement
 $\rho_{\text{dm}}(\mathbf{x}, \mathbf{t})$

400 Mpc
 Λ CDM
WMAP5
gas pressure
Gadget-3
SF+
SN E+
winds
+CRs
 512^3
BBPSS10
BBPS1,2,3,4,5



Peak-patches = "hot" halos

B+Myers 91-96; BBKS 83-86

The Cosmic Web

B+Kofman+Pogosyan 96-99

"Molecular" Picture of LSS Filaments & Membranes

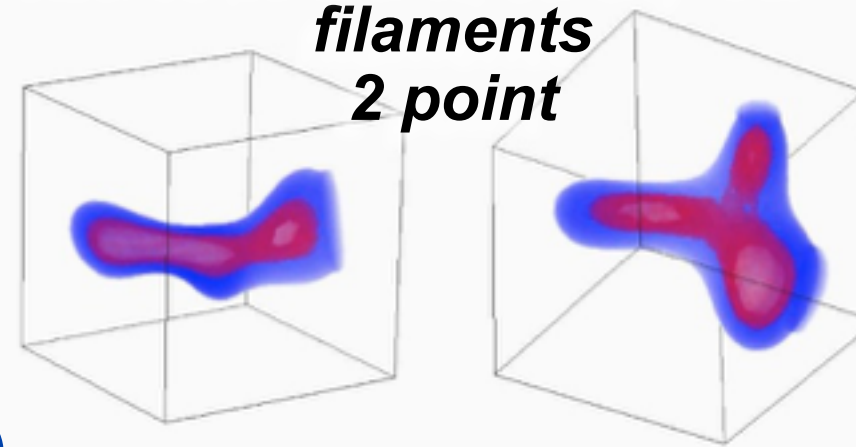
HALOS are dynamically HOT, the hierarchical standard model, Λ CDM, \Rightarrow scale space (3+1D \Rightarrow 4+1D) adaptive coarse-grain Zeldovich flows of Lagrangian peak-patches agree with N-body Eulerian halo simulations \Rightarrow fast mock surveys

marriage of halos & Zeldovich hot dynamics $\Rightarrow \mathbf{e}^i_{\mathbf{J}}(r_{pk}, t, R_{pk})$

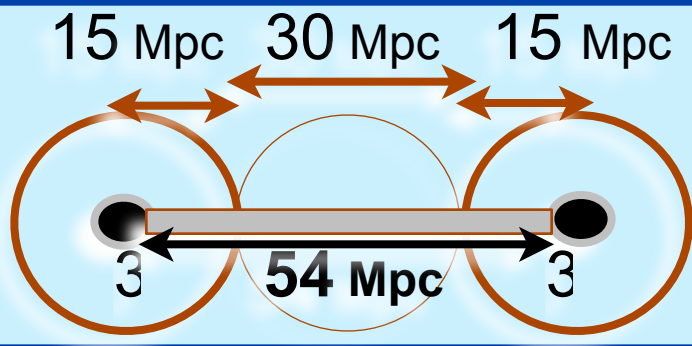
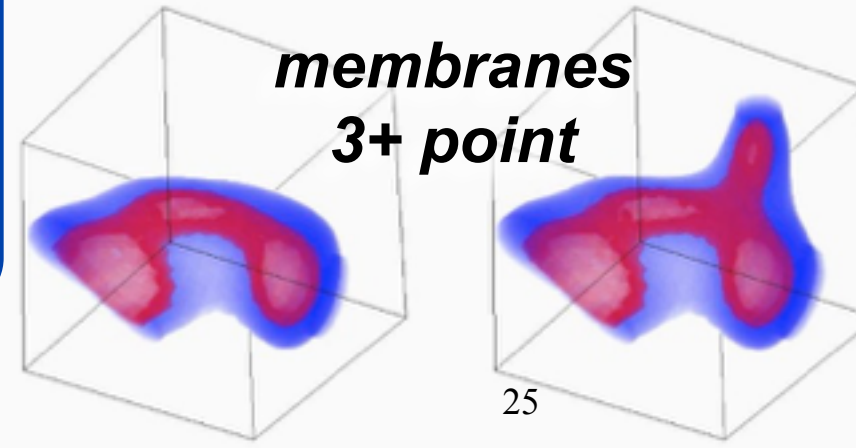


cool dynamics $\Rightarrow \mathbf{s}^i(r_{pk}, t, R_{pk})$

stacked (constrained) density fields filaments 2 point



membranes 3+ point



clusters
 $z \sim 0-1+$
 $\sim 10^{15} M_{sun}$

1 Mpc 2 Mpc 1 Mpc
3.6 Mpc

galaxies
 $z \sim 2-5$
 $\sim 10^{11.5} M_{sun}$

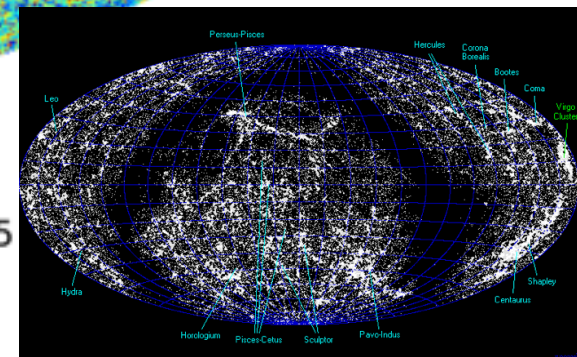
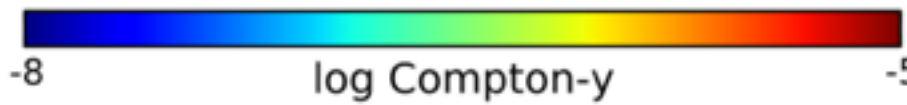
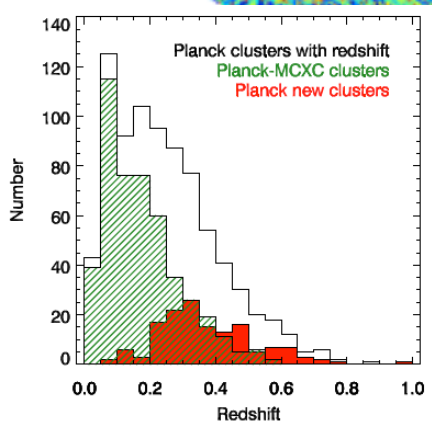
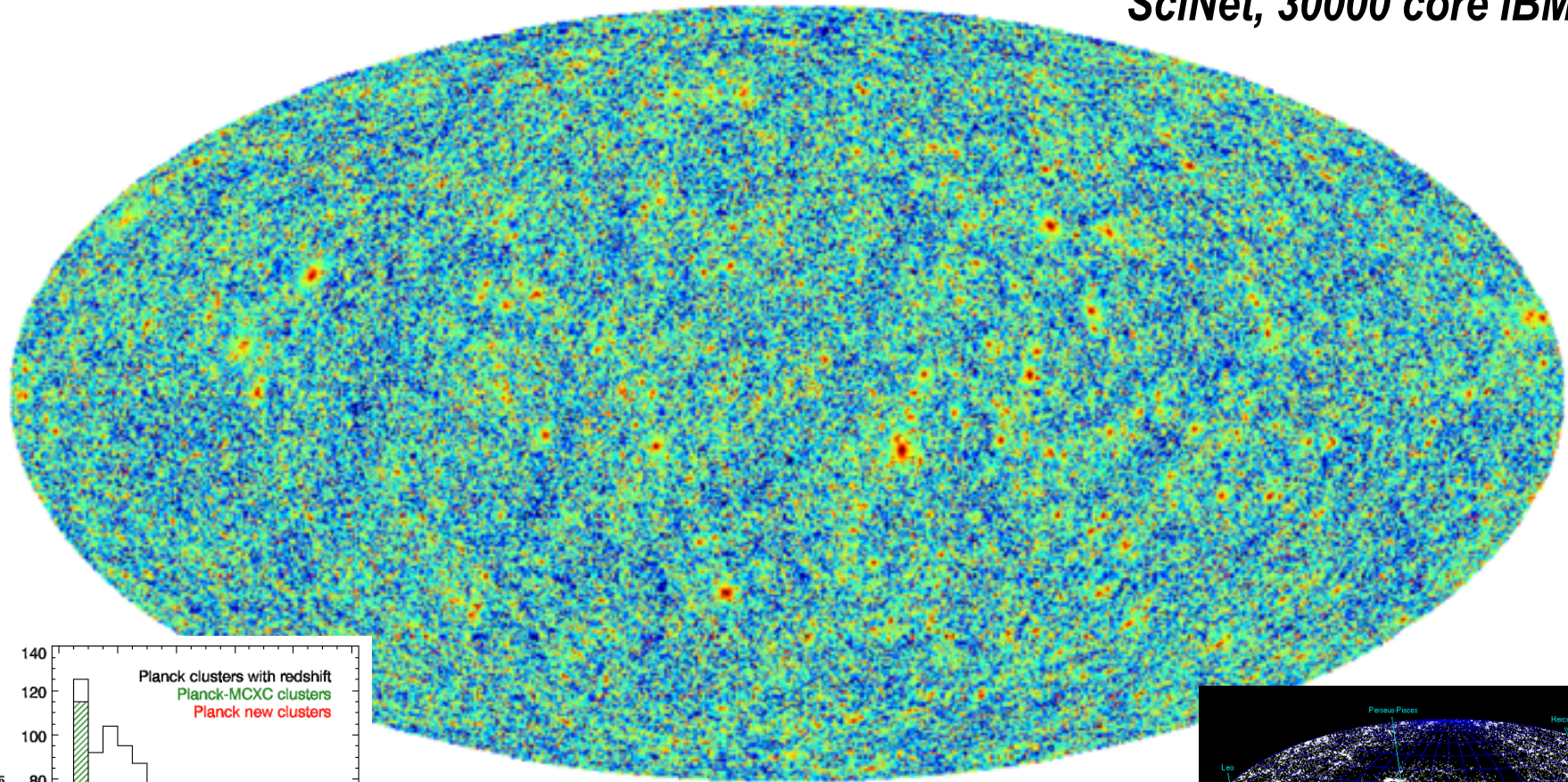
the Cosmic Web of Clusters, seen thru Compton cooling of high pressure electrons by the CMB

tSZ
effect

Lightcone Simulation of 35000 Clusters $> 1.5 \times 10^{13} M_{\text{sun}}$ to $z=0.5$ in projected pressure

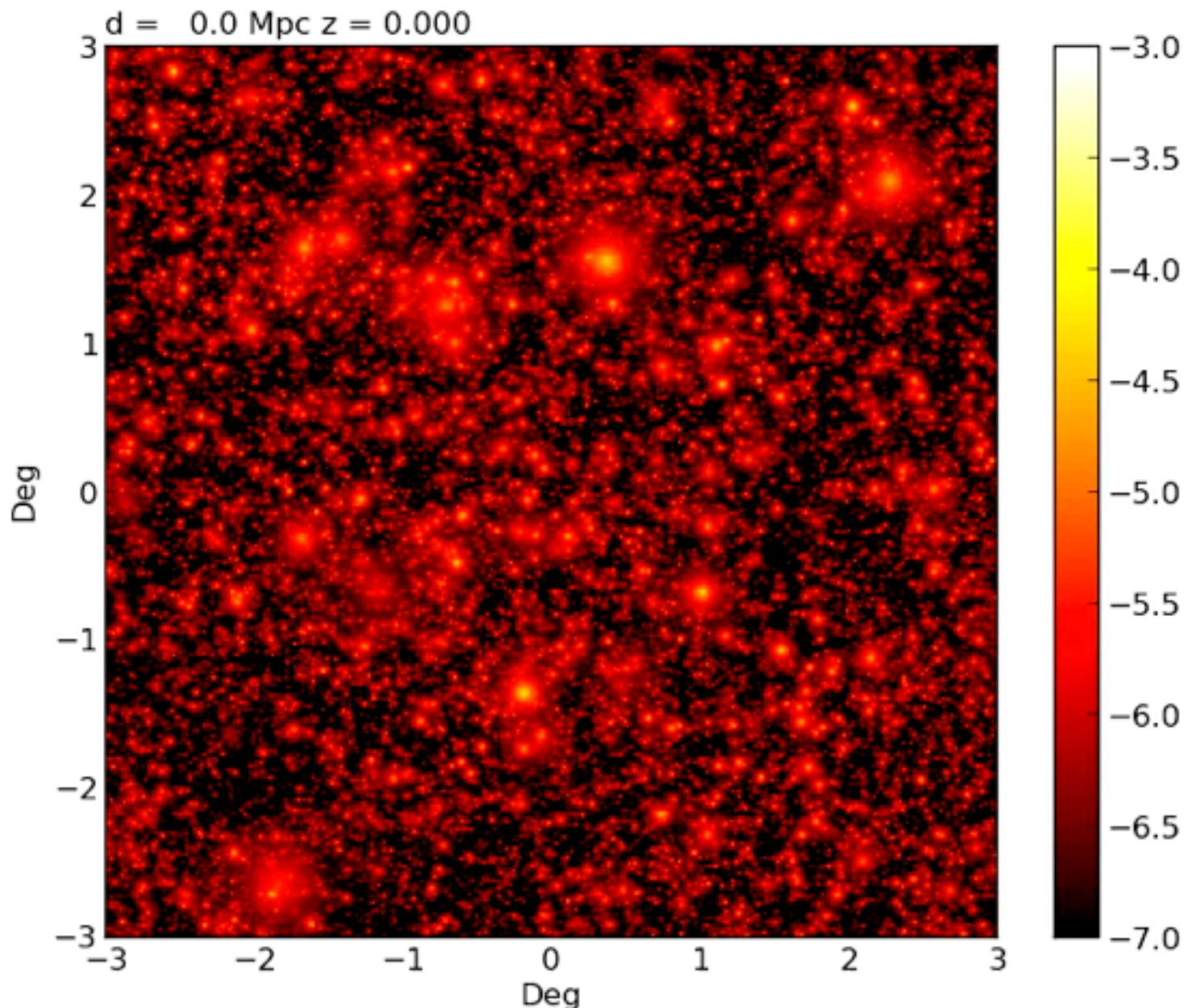
Alvarez, Bond, Hajian, Stein, Battaglia, Emberson,..2014

1.5 hours on 256 cores on
SciNet, 30000 core IBM GPC



Mocking Heaven: lightcone simulation for Λ CDM 36 sq deg to $z=2$

Planck all-sky tSZ mock 1.5 hours on 256 cores on SciNet, 30000 core IBM GPC



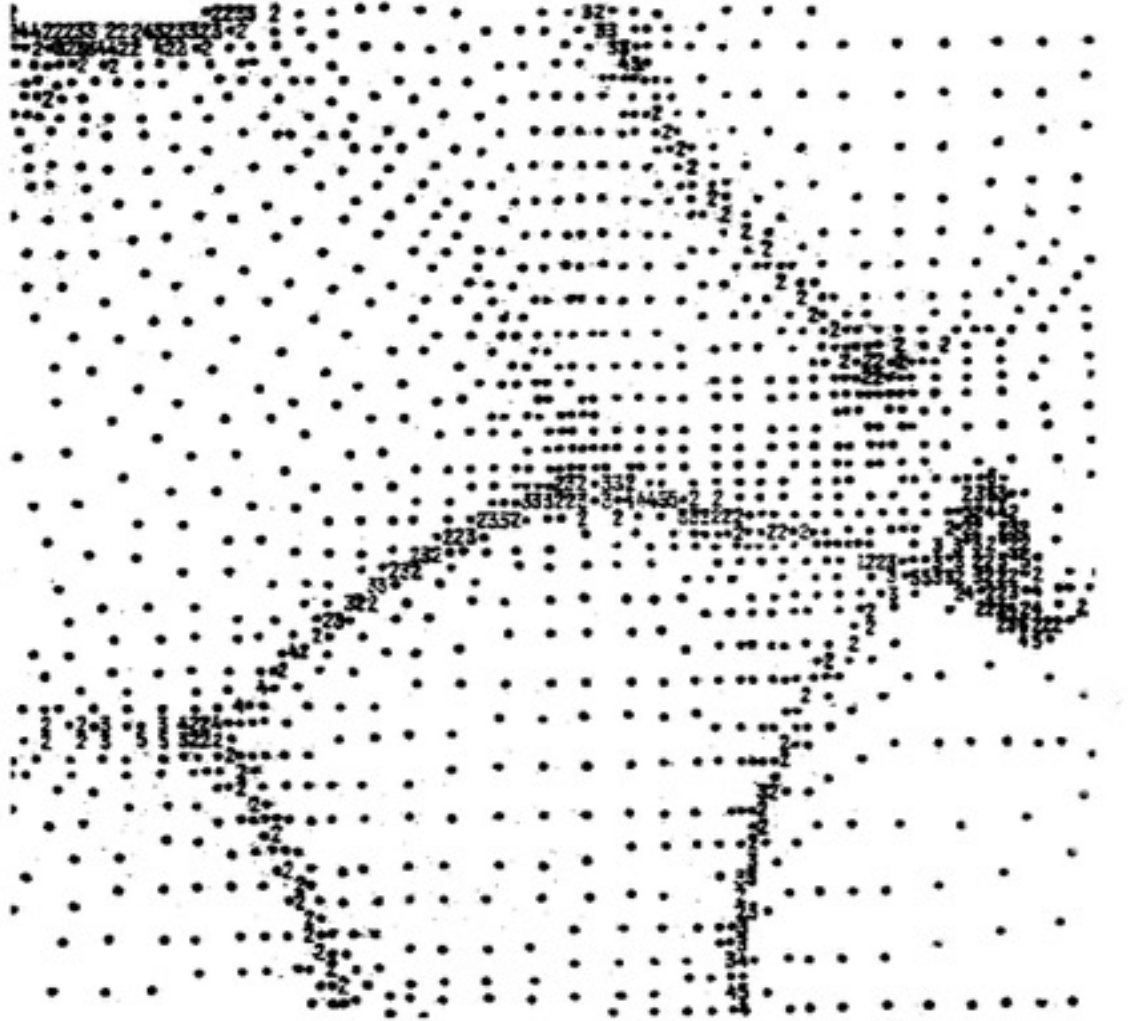
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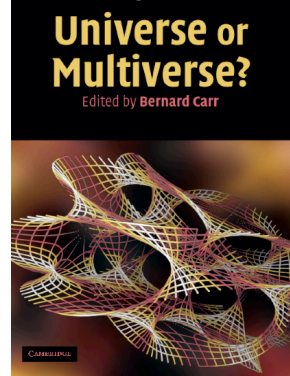


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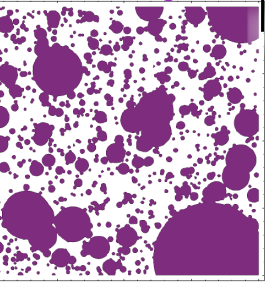
SuperWeb of ultra-Ultra Large Scale Structure of the Universe

Horizons: the ultimate-speed constraint on light & information

a highly strained & stressed state in the universe-at-large (very, very), randomly simple in our Hubble patch, and highly entangled on small to medium scales

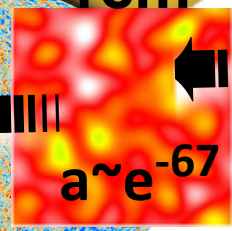
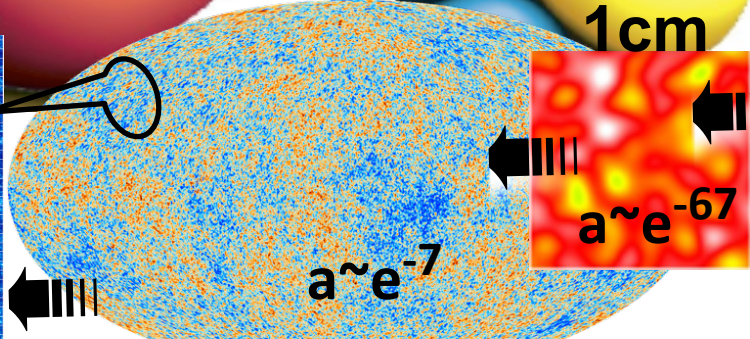
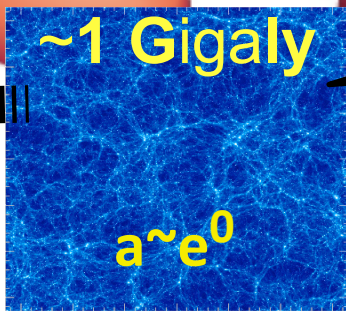
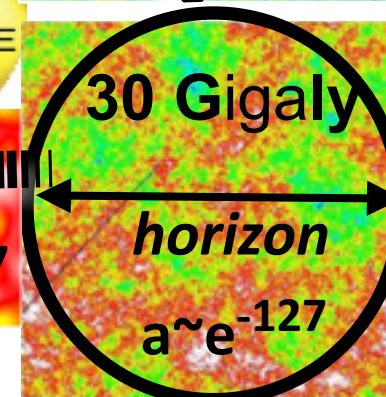
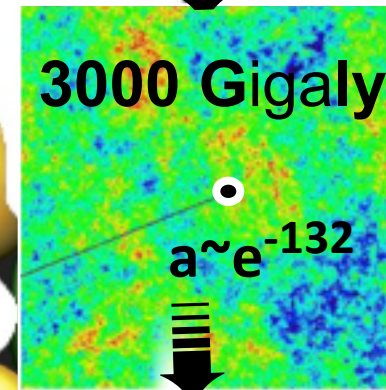
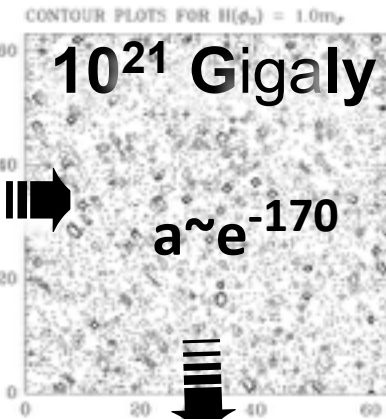
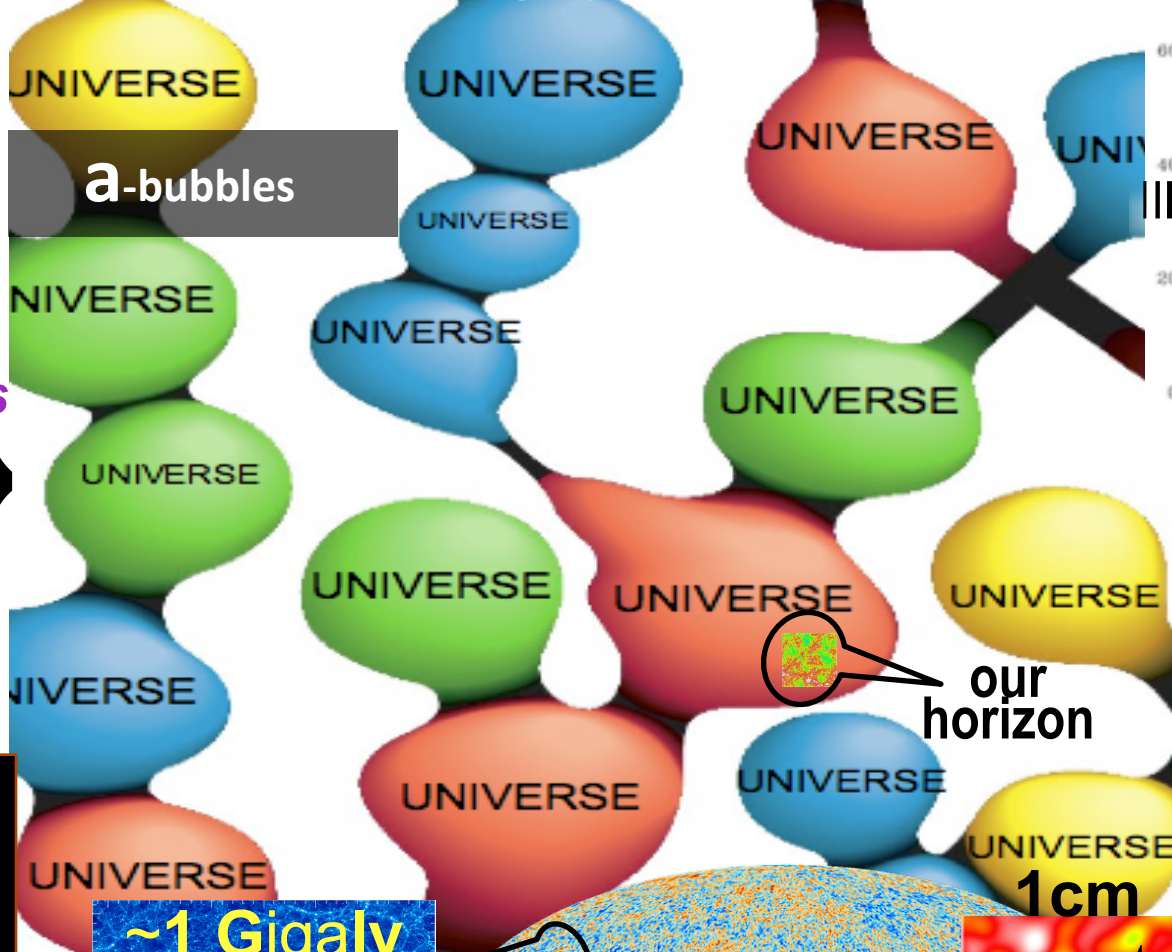


quantum tunnels = bubbly-U



END
a future DE-Void

$a \sim e^{+++}$



1cm

END