

What is the Universe made of?

NOW: Baryons + (cold-ish) dark matter + dark energy/inflaton + tiny curvature energy (+light neutrinos+photons). ??a bit of strings/textures/PBHs??

THEN: coherent inflaton /“vacuum” energy plus zero point fluctuations in all fields. & then preheat through mode coupling to incoherent cascade to thermal equilibrium.

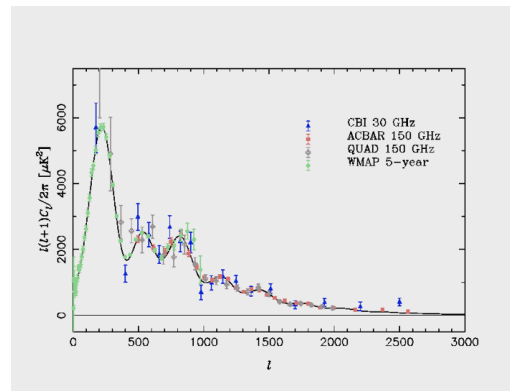
very early U early to middle to now U **very late U**

string theory/landscape/higher dimensions

inflation cyclic baryogenesis dark matter BBN γ dec **dark energy**

$V_{\text{eff}}(\phi_{\text{inf}}) ?$

$K_{\text{eff}}(\phi_{\text{inf}}) ?$



$V_{\text{eff}}(\phi_{\text{inf}}) ?$

$K_{\text{eff}}(\phi_{\text{inf}}) ?$

ρ_{curv} n_b/n_γ

ρ_{dm}/ρ_b $z_{\text{eq}}/z_{\text{rec}}$ $\rho_{\text{de}}/\rho_{\text{dm}}$ $\rho_{\text{de}} \sim H^2 M_{\text{Planck}}^2$ $\rho_{\text{mv}}/\rho_{\text{stars}}$

Standard Parameters of Cosmic Structure Formation

$$\theta \sim \ell_s^{-1} \quad \sim \ln \sigma_8^2$$

$$\Omega_k \quad \Omega_b h^2 \quad \Omega_{dm} h^2 \quad \Omega_\Lambda \quad \tau_c \quad \ln A_s \quad n_s \quad r = A_t / A_s$$

$$1+w_0, w_a$$

$$dn_s / d \ln k \quad n_t$$

New Parameters of Cosmic Structure Formation:
early-inflaton & late-inflaton trajectories

$$\epsilon_\phi = (1+w(a)) \times 3/2 \quad \epsilon(k), \quad k \approx Ha \quad \ln H(k_p)$$

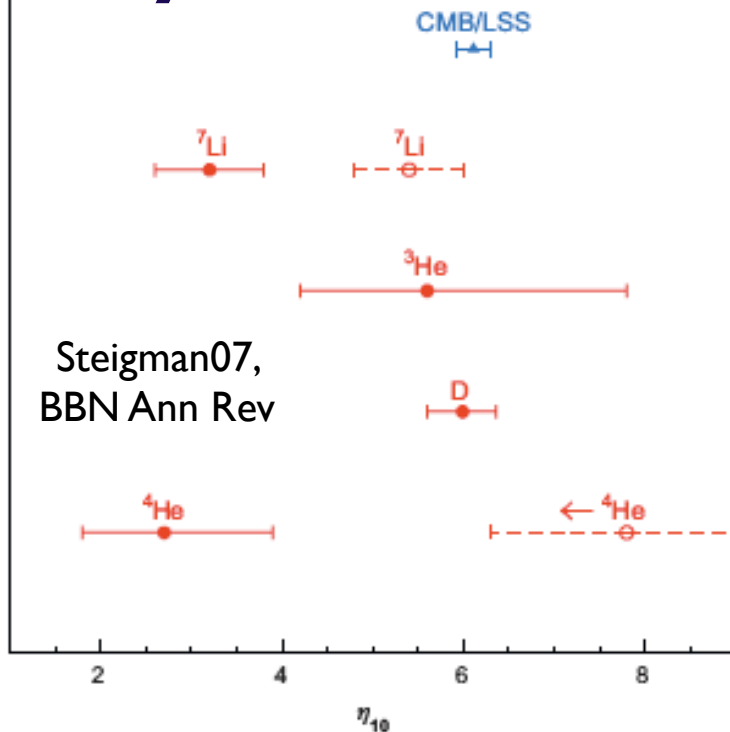
$$\epsilon_s f(a/a_{\Lambda eq}, a_s/a_{\Lambda eq}, \zeta_s) \quad \ln P_s(k) \quad \ln P_t(k)$$

+ subdominant isocurvature/cosmic string/ tSZ ...



IOTA 1967, Cambridge **B²FH 57, WFH 67, sn**

Baryometers



Nobel Prize 84
Willy Fowler + Chandra-sekhar

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$$\eta_{10} \equiv 10^{10} (n_B/n_\gamma) \equiv 274 \Omega_B h^2$$

	January 2000	January 2002	June 2002	January 2003	March 2003
$\Omega_b h^2$	$0.0339^{+0.0443}_{-0.0246}$	$0.0222^{+0.0025}_{-0.0021}$	$0.0221^{+0.0024}_{-0.0020}$	$0.0221^{+0.0023}_{-0.0018}$	$0.0233^{+0.0013}_{-0.0013}$
		boom98: Apr00/01/dasi	cbi: Jun02	acbar1: Dec02	WMAP1: Feb03

0.0223 ± 0.0007

0.0226 ± 0.0006 wmap3+acbar+cbi+... LSS

0.0233 ± 0.0005 wmap5+acbar+cbi+b03+...+WL+LSS+SNI+Lya

dark matter abundance $\Omega_m = 0.268 +0.012 -0.012$

	January 2000	January 2002	June 2002	January 2003	March 2003
$\Omega_{\text{cdm}} h^2$	$0.198^{+0.088}_{-0.080}$	$0.130^{+0.031}_{-0.028}$	$0.124^{+0.026}_{-0.025}$	$0.125^{+0.021}_{-0.022}$	$0.111^{+0.010}_{-0.010}$

CMB-only history (weak-h prior). LSS-then drove to near current
0.1145 +/- 0.0023 CMBall+WL+LSS+SN+Lya

$$\rho_{\text{dm}}/\rho_{\text{b}} = 5.1$$

Ω_{Λ}	$0.34^{+0.28}_{-0.24}$	$0.52^{+0.17}_{-0.20}$	$0.53^{+0.17}_{-0.19}$	$0.57^{+0.14}_{-0.19}$	$0.73^{+0.06}_{-0.10}$
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CMB-only history (weak-h prior). LSS-then drove to near current value

dark energy abundance $\Omega_{\Lambda} = 0.736 +0.012 -0.012$

& $H_0 = 72 \pm 1$ CMBall+WL+LSS+SN+Lya

$$\rho_{\text{m}}/\rho_{\text{de}} = .30$$

$\epsilon = -d \ln H / d \ln a = 1 + q$: now $= 3/2 [\Omega_{\text{m}0} + (1+w)(1-\Omega_{\text{m}0})]$ **$\sim 0.40?$, to 0?**

Constraining Trajectories of Dark Energy Inflatons

Inflation Now $\epsilon_\phi(a) = \epsilon_s f(a/a_{\Lambda\text{eq}}; a_s/a_{\Lambda\text{eq}}; \xi_s)$

$\epsilon_\phi = -d \ln \rho_\phi / d \ln a / 2 \sim 0$ now, to $\epsilon = -d \ln \rho_{\text{tot}} / d \ln a / 2 \sim 0$ to 2, 3/2, $\sim .4$

cf. $w(a)$: w_0, w_a, w in z-bins, w in modes, $\epsilon(a)$: in modes, jerk

~ 1 good e-fold. only ~ 2 params

Inflation Then $\epsilon(k) = (1+q)(a) =$ mode expansion in resolution ($\ln H a \sim \ln k$)
 $\sim r/16$ (Tensor/Scalar Power & gravity waves) ~ 10 good e-folds CMB+LSS

Cosmic Probes Now CMB(Apr08), CFHTLS SN(Union 307), WL, LSS/BAO, Ly α

Cosmic Probes Then JDEM-SN + DUNE-WL + Planck1

Zhiqi Huang, Bond & Kofman 08 $\epsilon_s = -0.03 \pm 0.28$ now, inflaton (potential gradient)²

to ± 0.07 then Planck1+JDEM SN+DUNE WL, weak $a_s < 0.36$ now < 0.21 then

Measuring w (SNe+CMB+WL+LSS+Lya)

$$w(a) \equiv \frac{p(a)}{\rho(a)}$$

$$w(a) = w_0 + w_a(1-a)$$

$$1 + w_0 = -0.0 \pm 0.06$$

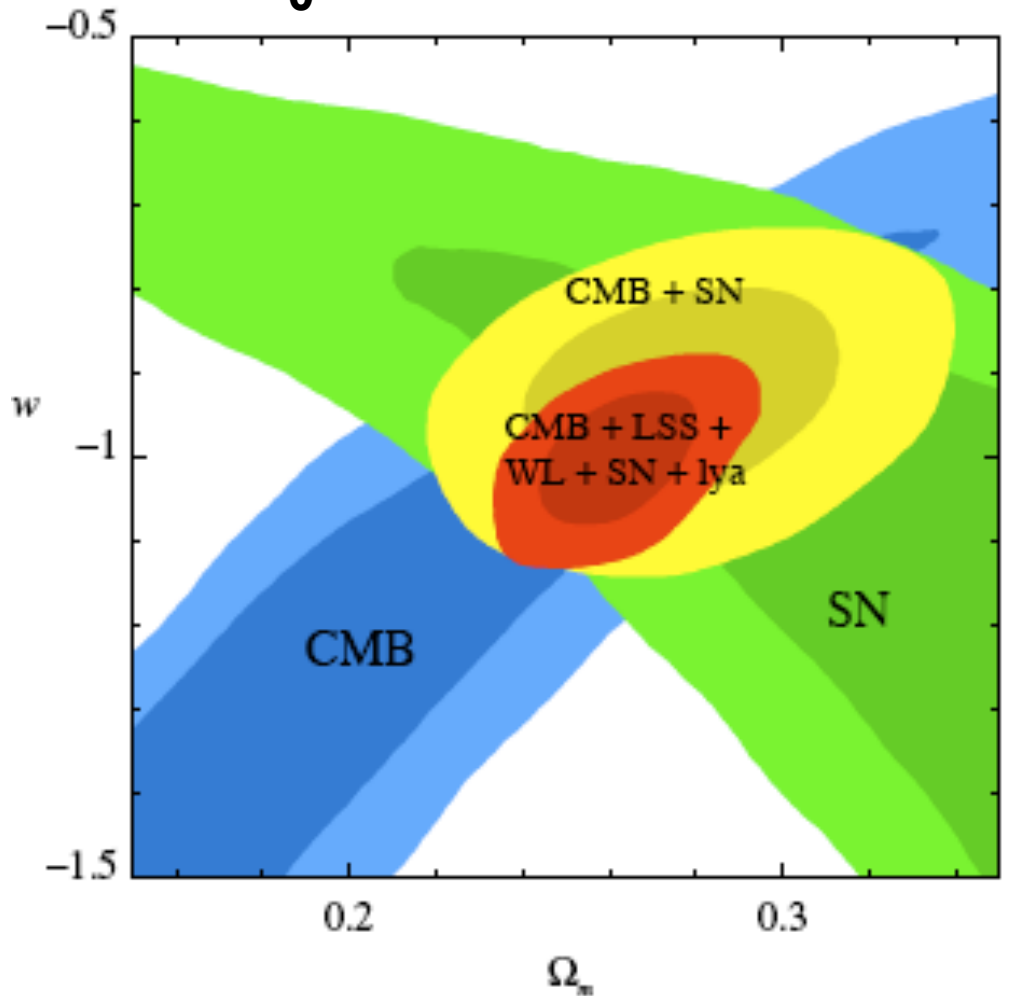
$$1 + w_0 = -0.01 \pm 0.19$$

$$w_a = 0.0 \pm 0.6 - 0.8$$

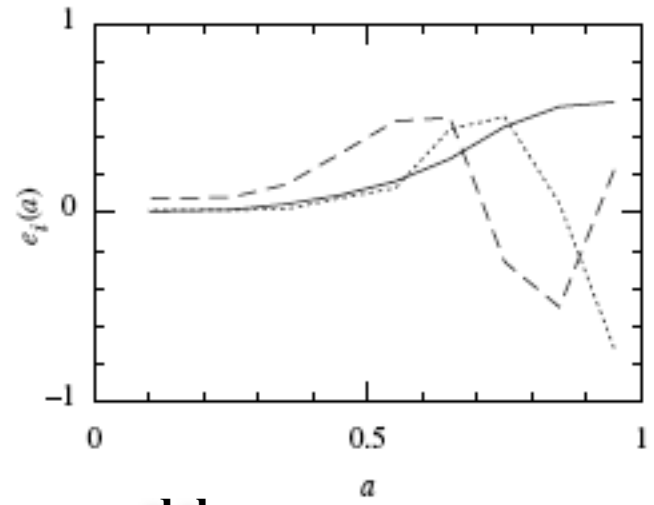
piecewise parameterization
4,9,40 modes in redshift

9 & 40 into Parameter eigenmodes

data cannot determine >2 EOS parameters
DETF Albrecht etal06, Crittenden etal06, hbk08

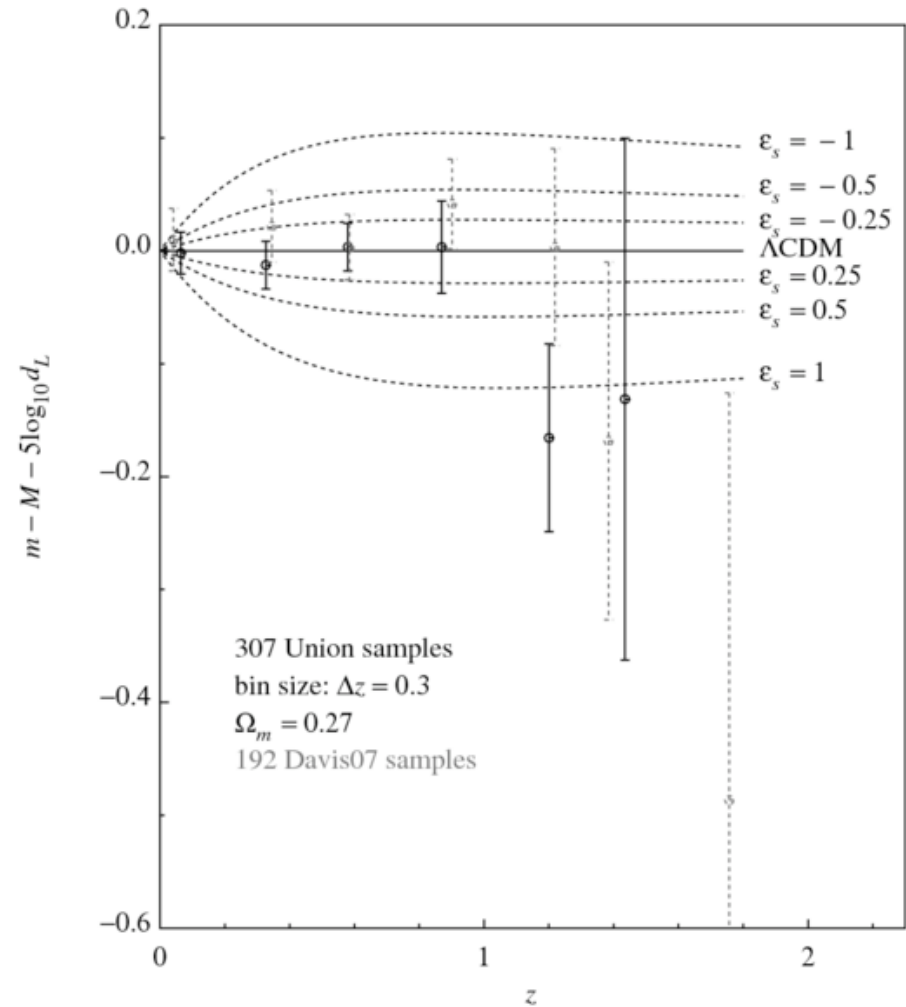
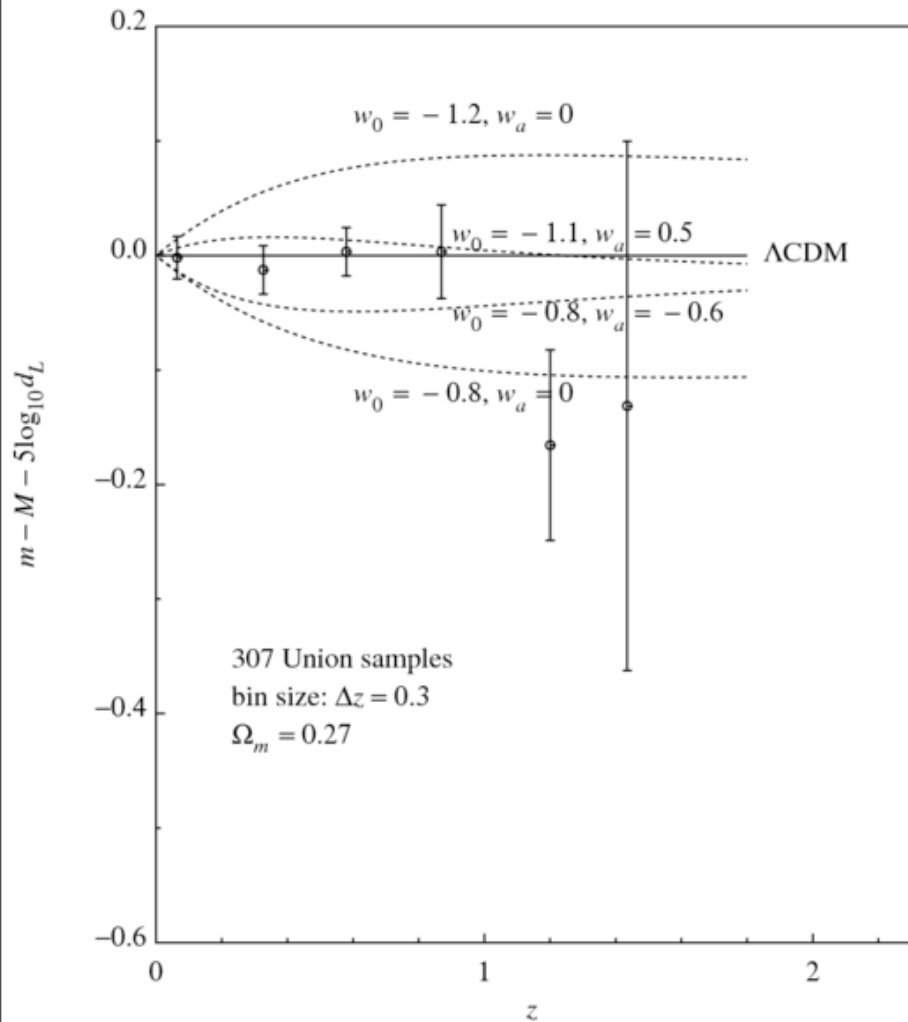


$\sigma_1=0.13$ $\sigma_2=0.33$ $\sigma_3=0.58$

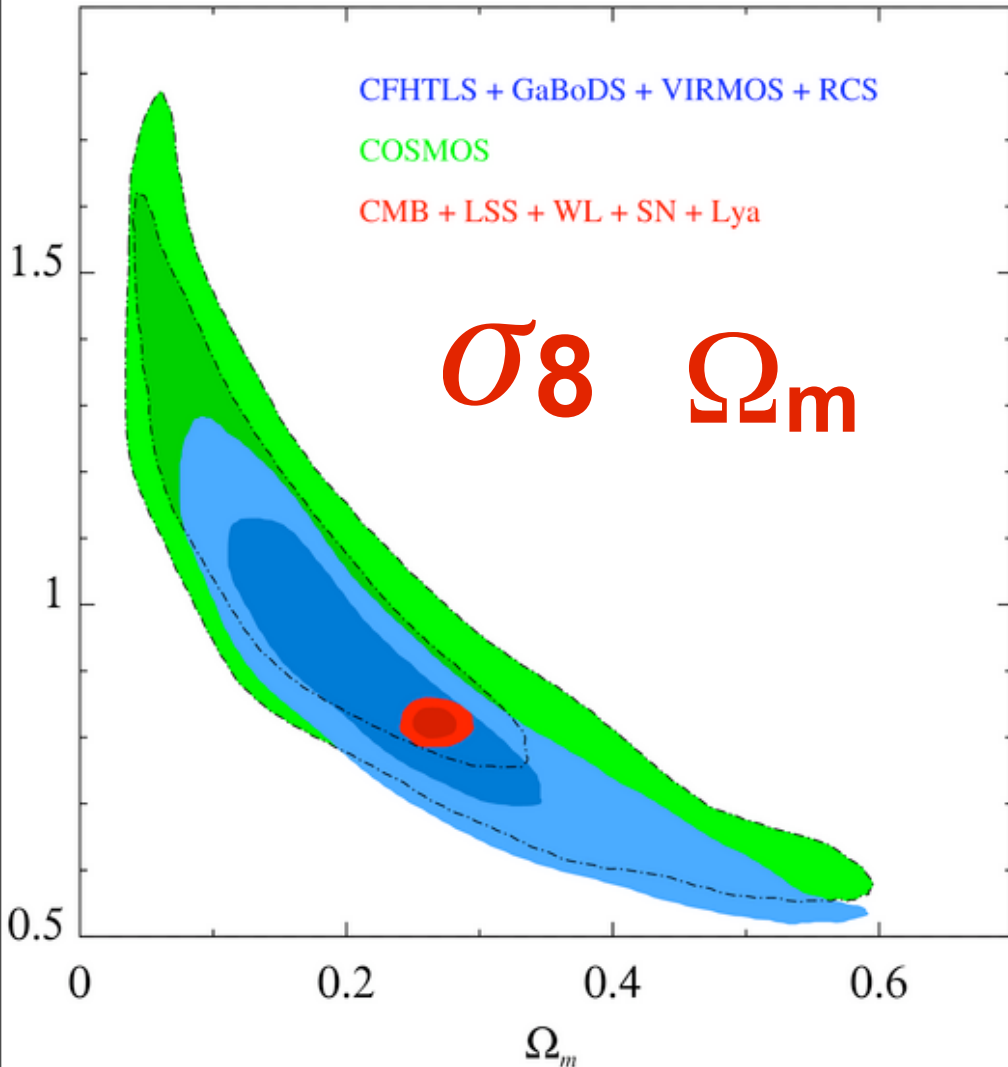


$\epsilon_{\phi_0} = 0.0 \pm 0.09$ if constant, $\epsilon_{\phi_0} = -0.015 \pm 0.3$ if a-linear model

SN1a now: Union sample 307 Apr08, partially unified. CFHT SNLS3 ~Jul08, ~4 x SNLS1, calibrated. Low z ~0.5yr



Weak Lens now: CFHTLS-wide(22sq deg)+GaBoDS (13) +Virgos-Descart(8)+RCS1(53) Apr07+ & COSMOS07



case	Ω_m	σ_8
LCDM	0.265 \pm .011	0.828 \pm .015
w0	0.265 \pm .013	0.829 \pm .025
w0-wa	0.265 \pm .014	0.831 \pm .027
ϵ_s	0.265 \pm .013	0.829 \pm .024
ϵ_s - a_s - ζ_s	0.265 \pm .013	0.832 \pm .025

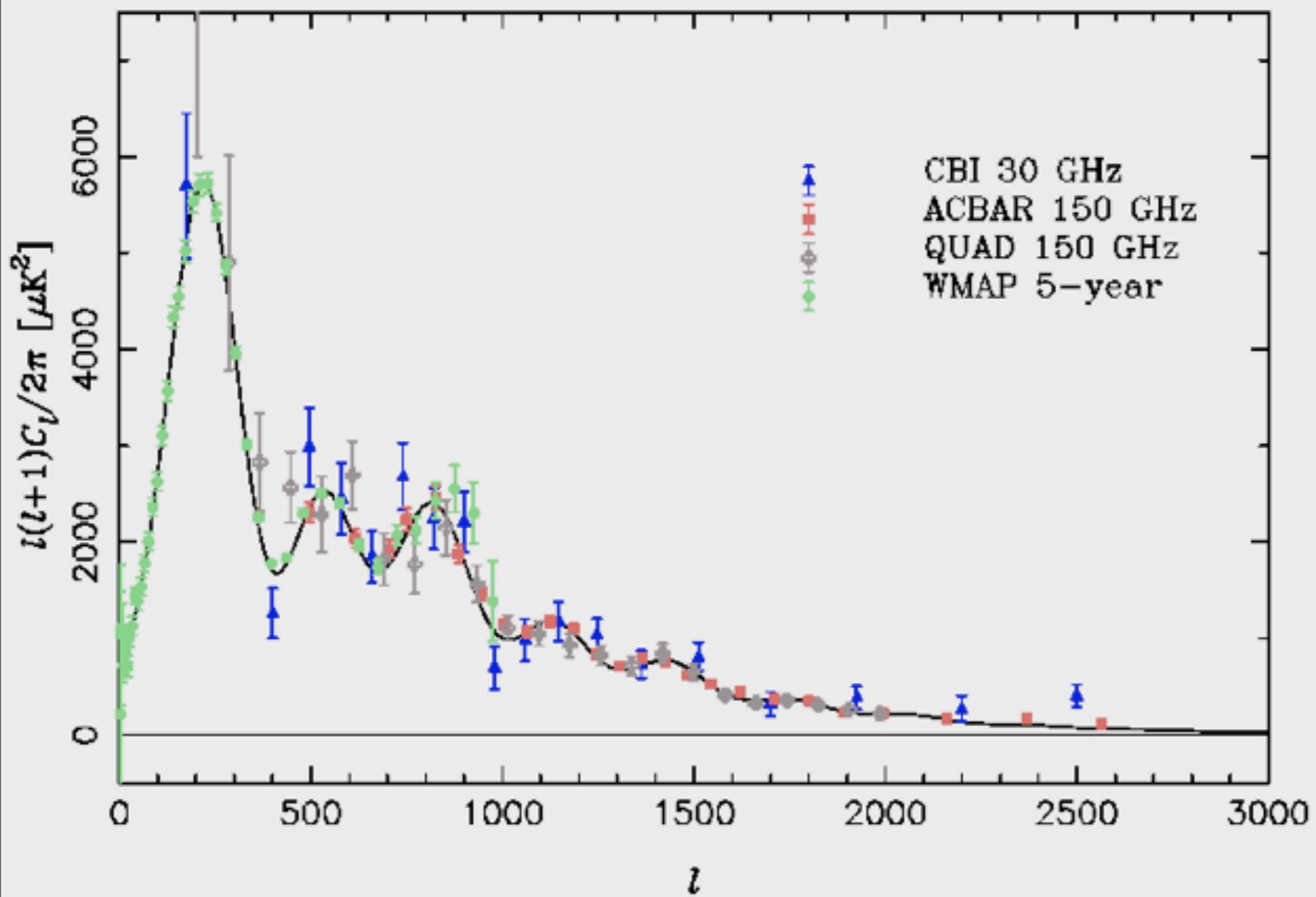
recent weak lensing "alone"

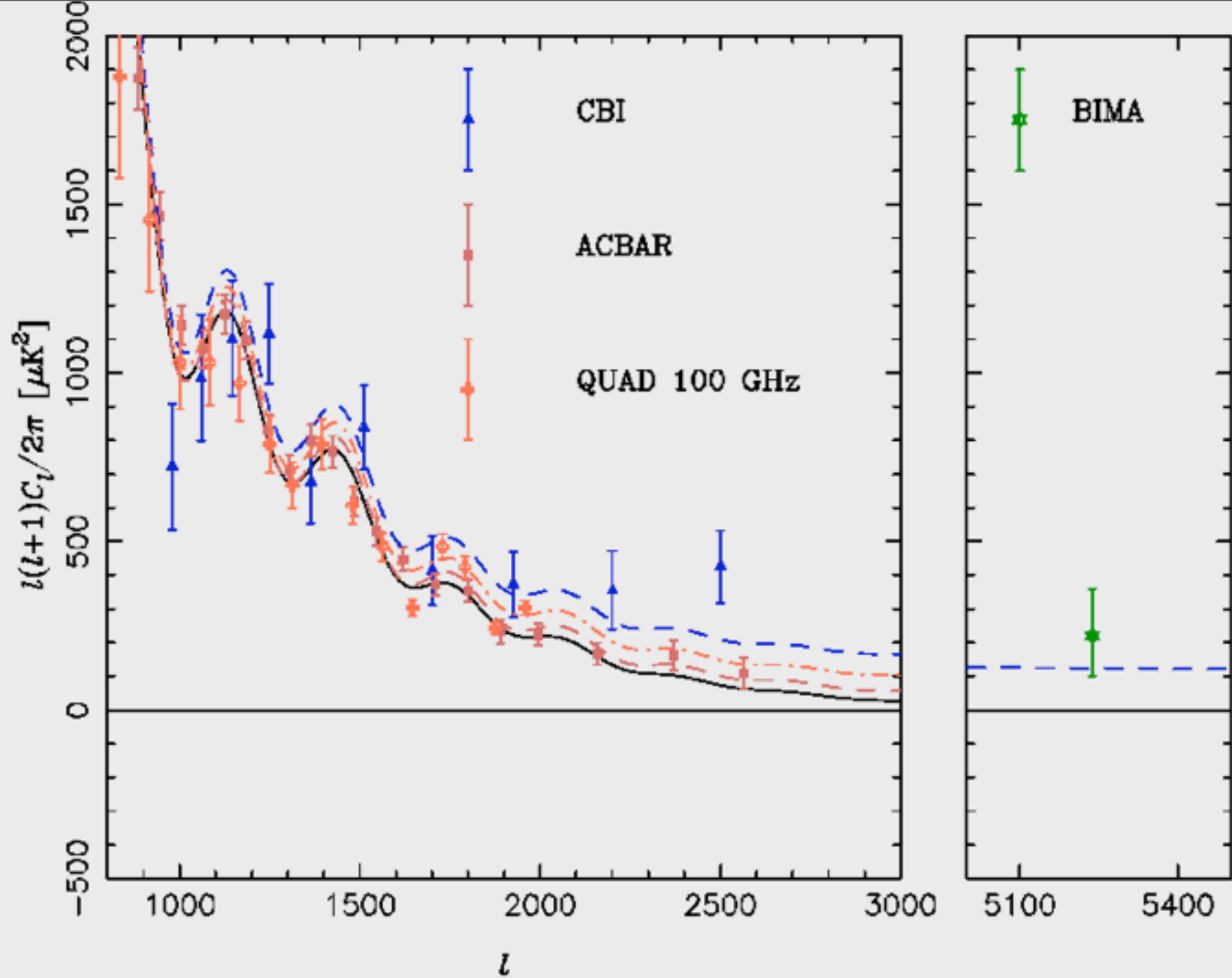
CFHTLS	0.26+	0.83+.04-.05
cf.		0.80+.05-.05
COSMOS	0.26+	0.88 \pm .07-.08
cf.		0.87 \pm .074

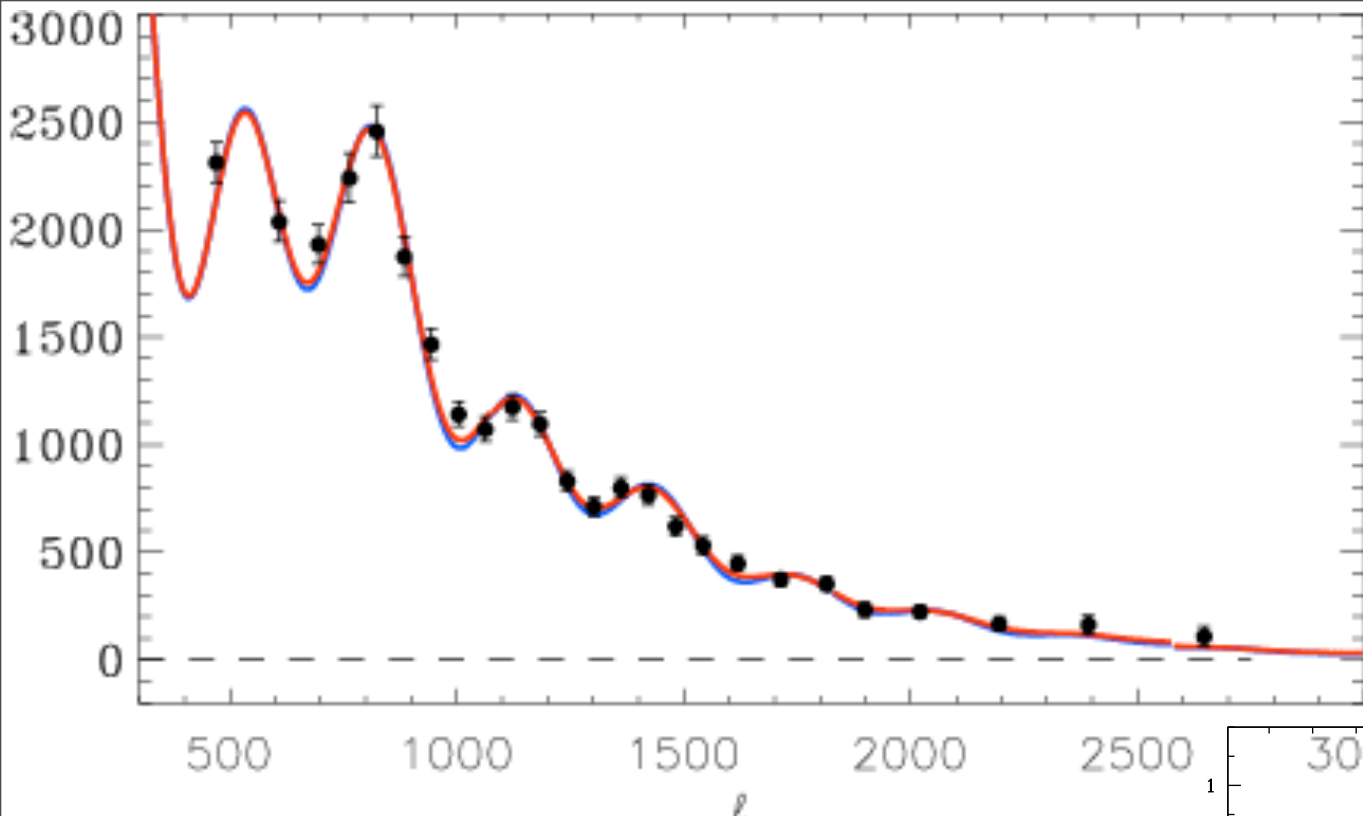
recent SZ CBlexcess "cmb-alone"

CBI+Acbar+Bima σ_8 **SZ** \sim .95 \pm .05 \pm .05

planck1+jdem+dune .260 \pm .004 .850 \pm .005
 ϵ_s - a_s - ζ_s case ϵ_s =.02+.07-.06







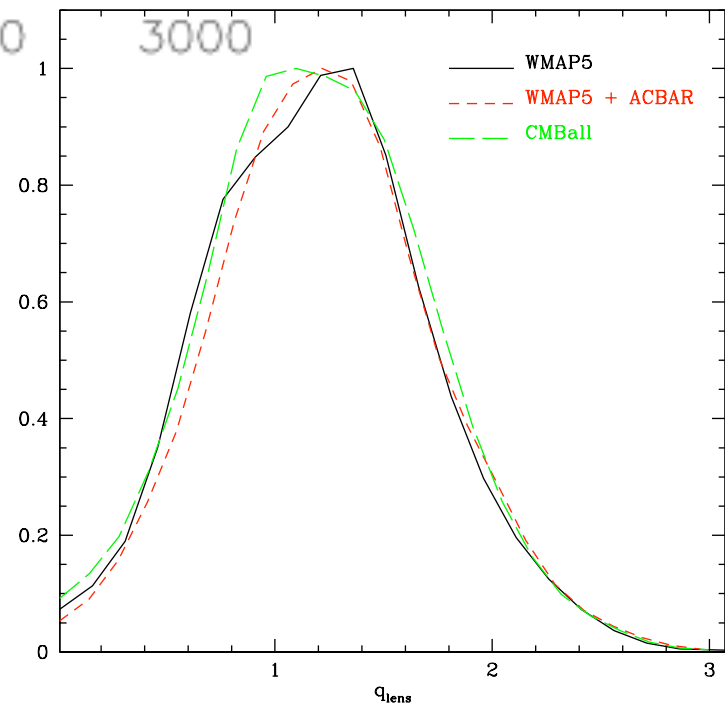
$$C_{\ell}^{\text{lens}} = C_{\ell}^{\text{no-lens}} + q_{\text{lens}} \Delta C_{\ell}^{\text{lens}}$$

**wmap5+
acbar**

$$q_{\text{lens}} = 1.23^{+0.22(+0.83)}_{-0.23(-0.76)}$$

CMBall

$$q_{\text{lens}} = 1.20^{+0.24(+0.84)}_{-0.24(-0.77)}$$



Old view: Theory prior = delta function of THE correct one and only theory

1980

R^2 -inflation

Old Inflation

Chaotic inflation

New Inflation

Double Inflation

Power-law inflation

SUGRA inflation

Radical BSI inflation

variable M_p inflation

Extended inflation

1990

Natural pNGB inflation

Hybrid inflation

SUSY F-term inflation

SUSY D-term inflation

Assisted inflation

Brane inflation

2000

SUSY P-term inflation

Super-natural Inflation

K-flaton

N-flaton

*ekpyrotic/
cyclic*

$D3 - D7$ inflation

DBI inflation

Warped Brane inflation

Tachyon inflation

Racetrack inflation

Roulette inflation Kahler moduli/axion

➤ **Cosmological Constant ($w=-1$)**

➤ **Quintessence $V(\psi)$ ($-1 \leq w \leq 1$)**

➤ **Phantom field $KE < 0$ & $V(\psi)$ ($w \leq -1$)**

➤ **Tachyon fields ($-1 \leq w \leq 0$)**

➤ **K-essence: KE not quadratic**

➤

$$V \sim \exp[..\psi],$$

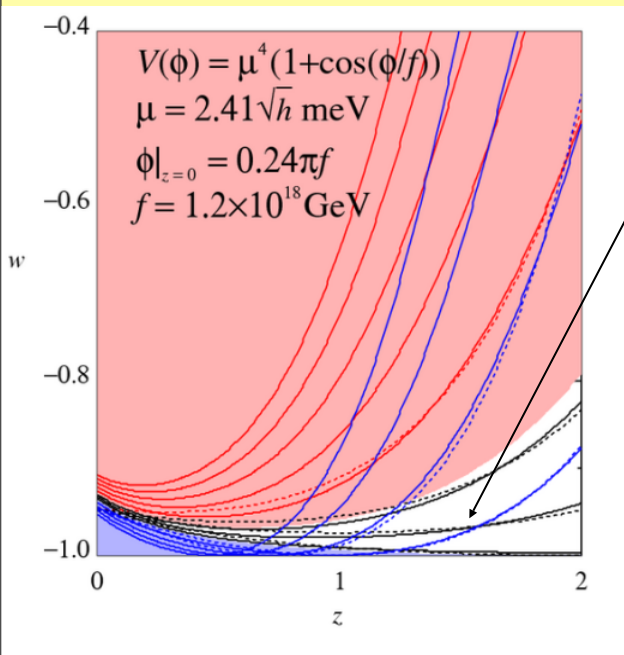
$$\psi^{-p} = 1, 2, 4, .., \quad V_0 + .. \psi^p = 1, 2, 4, ..,$$

$$V_{\text{pNGB}} \sim \sin^2 .. \psi, \quad V_{\text{holes}}, \quad V_{\text{branes}}, \\ (V_0 + .. [\psi - \psi_0]^2) .. \quad \& \text{ much more}$$

Late-Inflaton $\varepsilon_\phi(a) = \varepsilon_s f(a/a_{\Lambda\text{eq}}; a_s/a_{\Lambda\text{eq}}; \xi_s)$

3-param formula accurately fits **slow-to-moderate roll** & even wild rising baroque late-inflaton trajectories, as well as **thawing & freezing** trajectories. but not oscillating DE

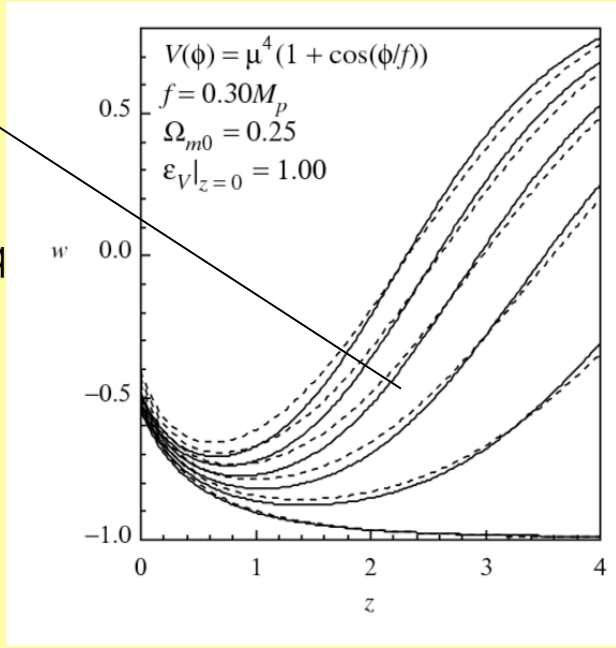
Cosmic Probes Now CFHTLS SN(Union~300), WL, CMB, BAO, LSS, Ly α



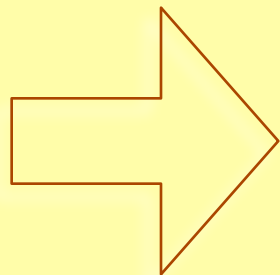
slow-to-moderate roll OK
wild rise & roll up/down OK

$\varepsilon_v = (\text{dln}V/\text{d}\psi)^2/4$ @pivot a_{eq}
 $\varepsilon_s = -0.03 \pm 0.25$ now
 $a_s < 0.36$ ($z_s > 2.3$) now

$\xi_s = \text{dln}\varepsilon_s / \text{dln}a \times 1/2$ @pivot a_{eq}
 ill-determined now



ε_s to ± 0.07 then
 Planck1+JDEM SN+DUNE WL,
 weak $a_s < 0.21$ then, ($z_s > 3.7$)
 3rd param ξ_s ill-determined then



cannot reconstruct the quintessence potential, just the slope ε_s & hubble drag info
 (late-inflaton field $<$ Planck mass, but sometimes not by a lot)

3-parameter parameterization $\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$ + Friedmann Equation + DM+B

$$w(a) = -1 + \frac{2\epsilon_s}{3} \left\{ \frac{\left(\frac{a_s}{a}\right)^{3-3.6a_s|\epsilon_s|(1-\Omega_{m0})}}{\sqrt{1 + \frac{\epsilon_s}{3|\epsilon_s|} \left(\frac{a_s}{a}\right)^{6-7.2a_s|\epsilon_s|(1-\Omega_{m0})}}} \frac{1}{\sqrt{|\epsilon_s|}} \right. \\ + \left[\sqrt{1 + \left(\frac{a_{eq}}{a}\right)^3} - \left(\frac{a_{eq}}{a}\right)^3 \ln\left(\left(\frac{a}{a_{eq}}\right)^{\frac{3}{2}} + \sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3}\right) \right] (1 - \zeta_s) \\ + 0.36\epsilon_s(1 - \Omega_{m0}) \frac{\left(\frac{a}{a_{eq}}\right)^2}{1 + \left(\frac{a}{a_{eq}}\right)^4} \left[0.9 - 0.7\frac{a}{a_{eq}} - 0.045\left(\frac{a}{a_{eq}}\right)^2 \right] \\ \left. + \frac{2\zeta_s}{3} \left[\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 2\left(\frac{a_{eq}}{a}\right)^3 \left(\sqrt{1 + \left(\frac{a}{a_{eq}}\right)^3} - 1 \right) \right] \right\}^2$$

where

$$a_{eq} \equiv \left(\frac{\Omega_{m0}}{1 - \Omega_{m0}} \right)^{\frac{1}{3[1-0.36\epsilon_s(1-\Omega_{m0})]}}$$

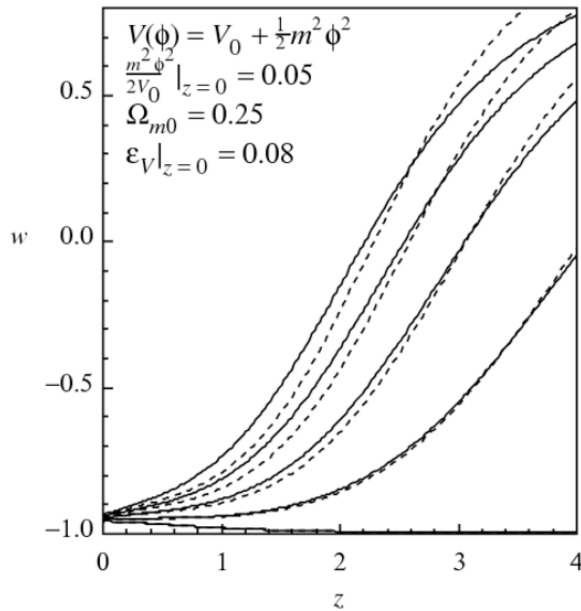
$$a_s \geq 0$$

$$\sqrt{|\epsilon_V|} = \sqrt{|\epsilon_s|} \left[1 + \zeta_s \left(\left(\frac{a}{a_{eq}} \right)^{\frac{3}{2}} - 1 \right) \right] \quad -1 < \zeta_s < 1$$

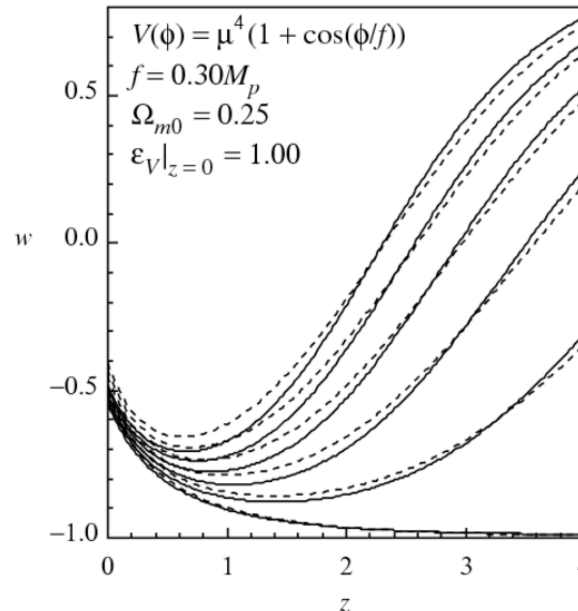
- ~15% thawing,
8% freezing,
with flat priors

sample $w(z)$ -trajectories for $V(\psi)$, back-integrate now to then

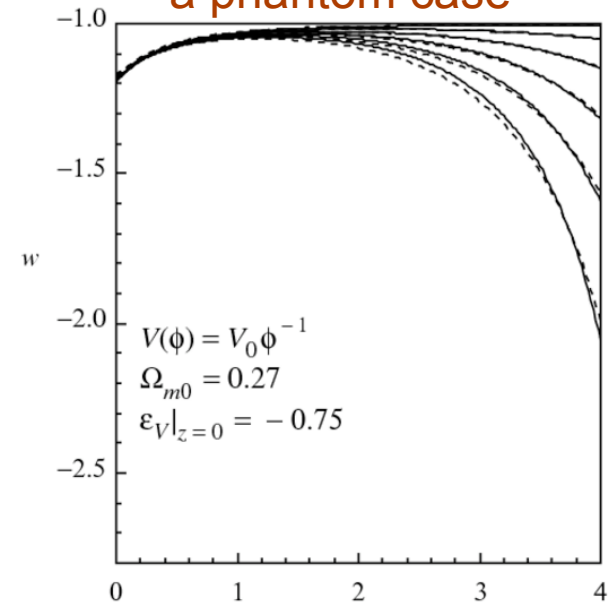
a offset-quadratic mass case



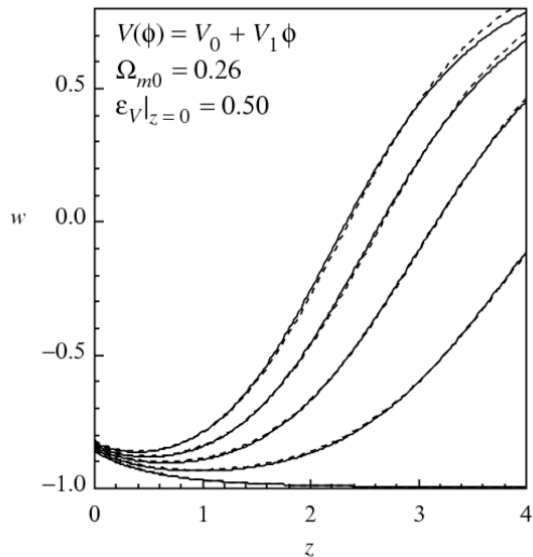
a pNGB phase case



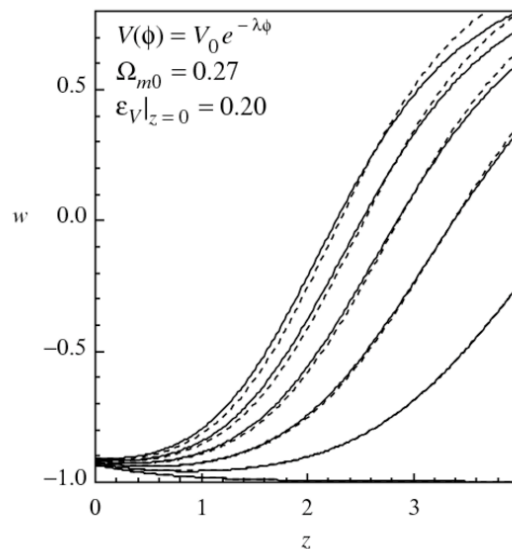
a phantom case



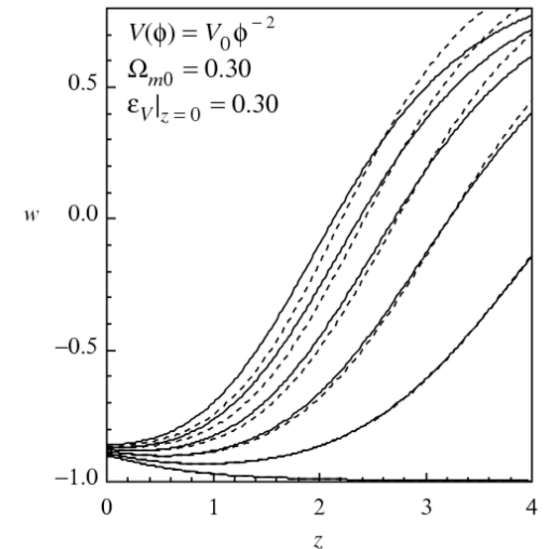
offset-linear



a Ratra-Peebles exp potential

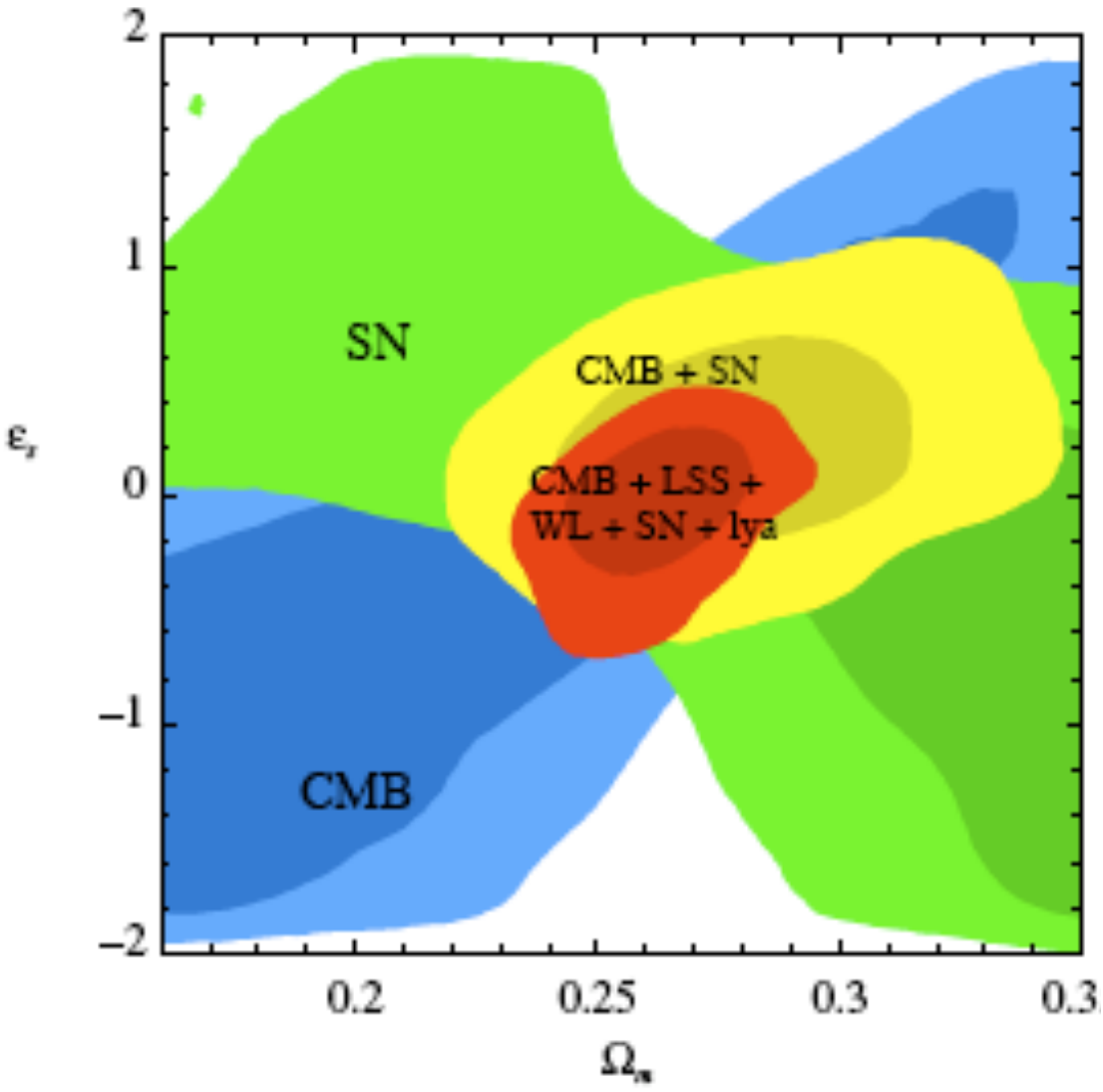


a dropping power law



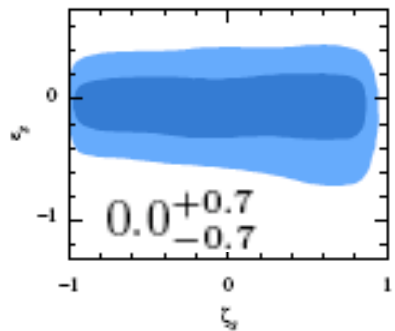
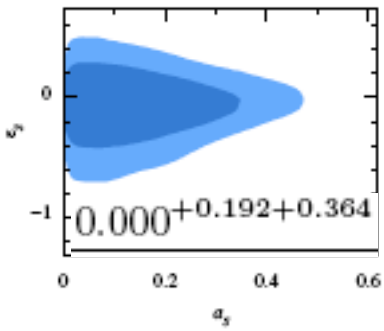
measuring ϵ_s a_s ζ_s scaling+tracking SNe_{union}+CMB

wmap5+acbar+cbi5yr+b03+**+WL**_{cfhtls+cosmos}**+LSS**_{sdssRG+2dF}**+Lya**)



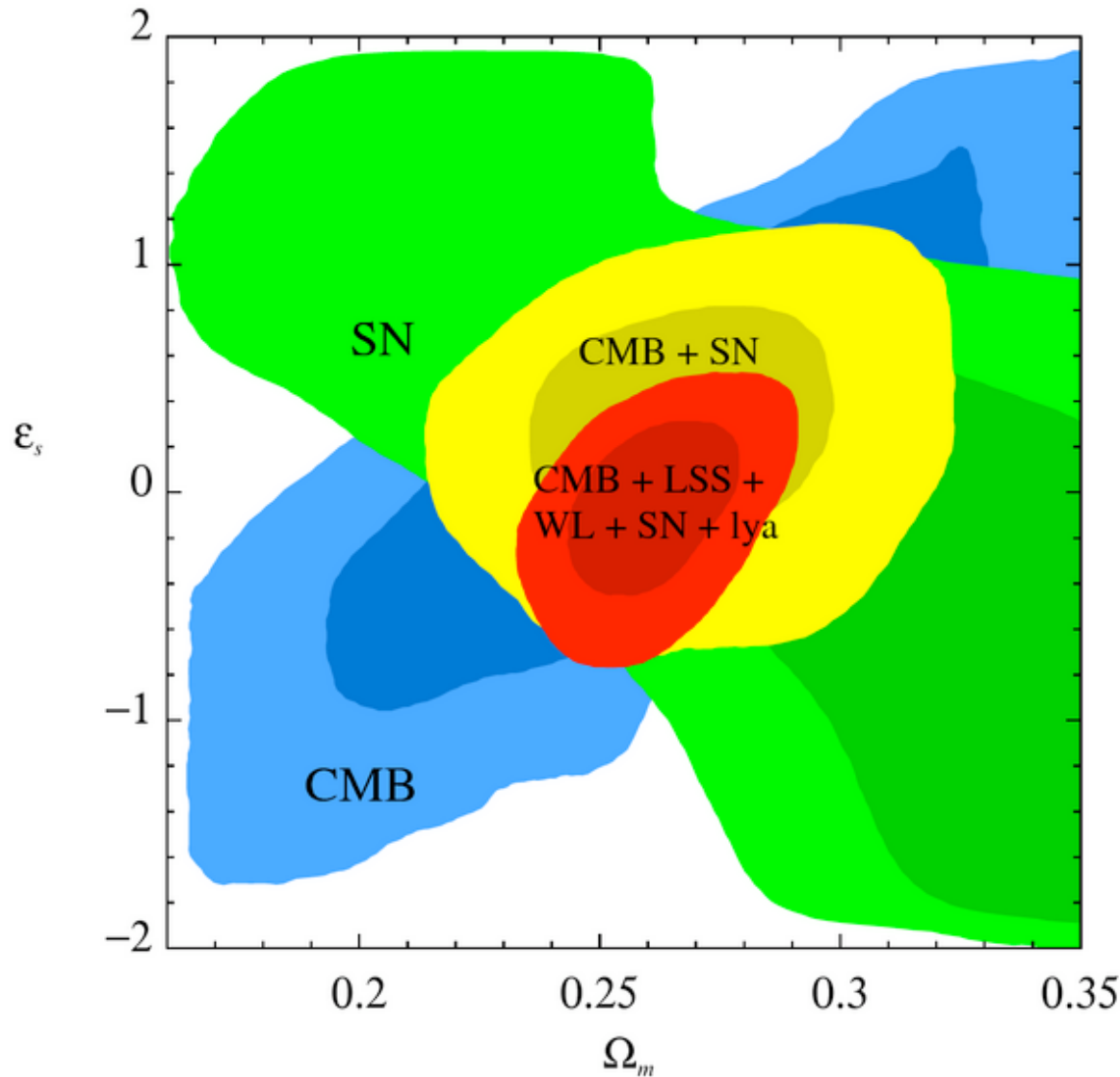
modified CosmoMC with Weak Lensing, SZ, SN, CMB, bias & w(a) slow-to-moderate-roll trajectories with various priors

ϵ_s $.01 + .25 - .28 \quad 1$
 $-.03 + .21 - .25 \quad 3$
 $-.03 + .26 - .30 \quad 2$



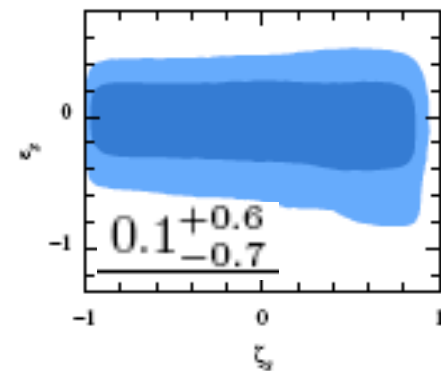
measuring ϵ_s ζ_s $\mathbf{a}_s=0$ tracking (SNe_{union}+CMB

wmap5+acbar+cbi5yr+b03+**+WL**_{cfhtls+cosmos}**+LSS**_{sdssRG+2dF+Lya})



modified CosmoMC
with Weak Lensing,
SZ, SN, CMB, bias &
w(a) slow-to-moderate-
roll trajectories with
various priors

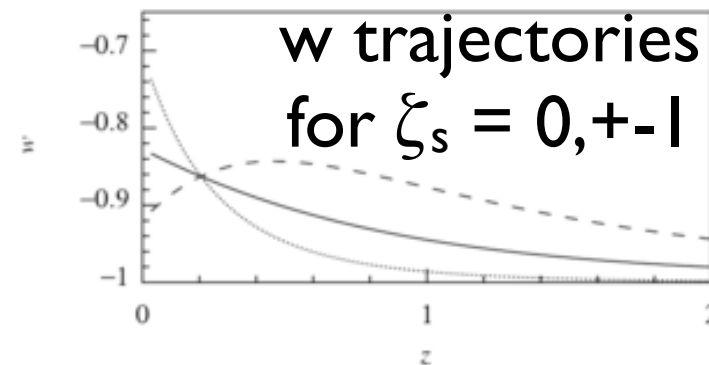
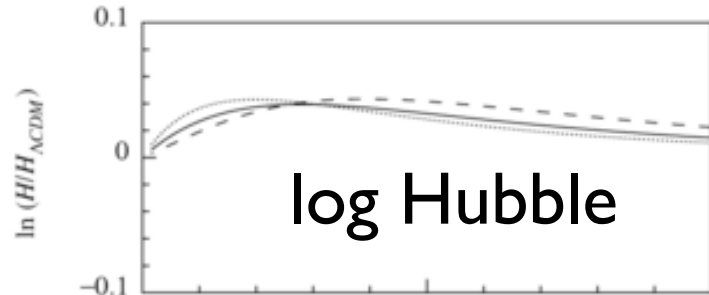
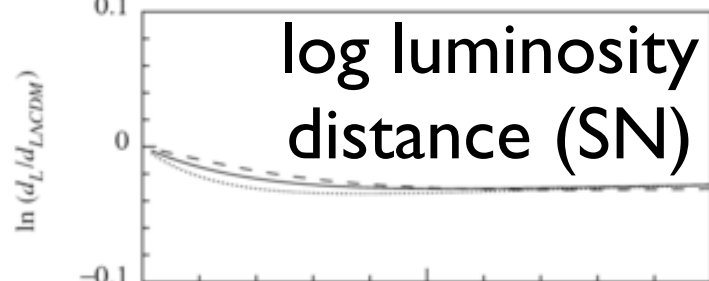
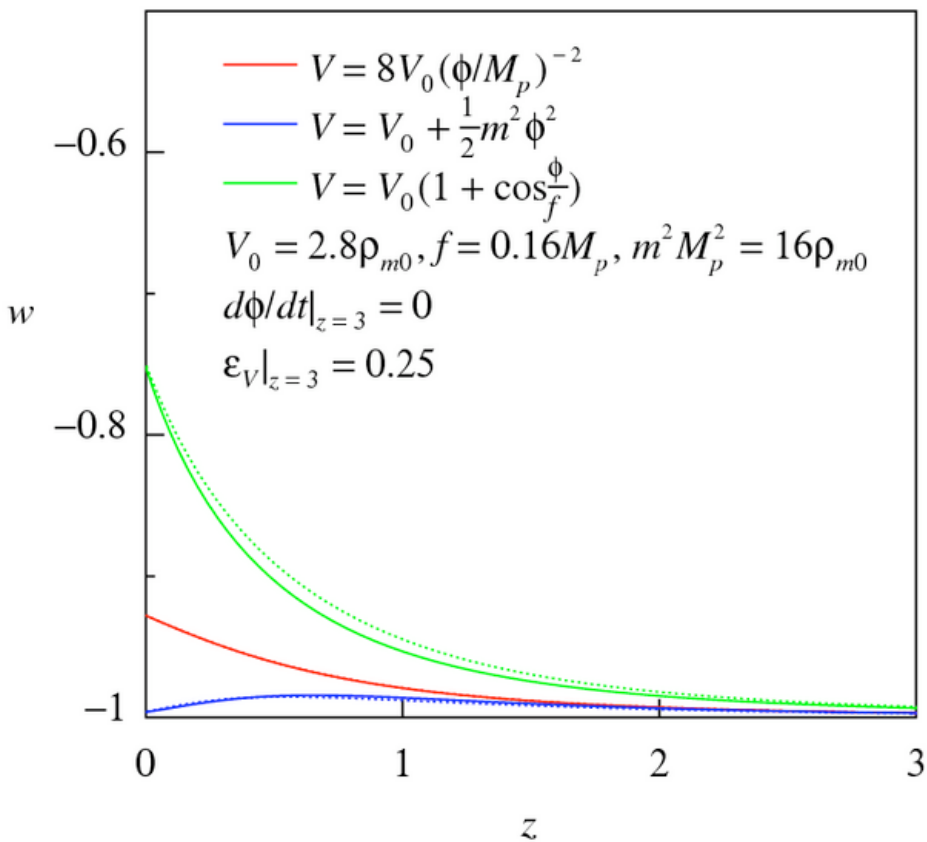
$$\epsilon_s \begin{matrix} .01 + .25 - .28 & 1 \\ -.03 + .21 - .25 & 3 \\ -.03 + .26 - .30 & 2 \end{matrix}$$



Why can't we measure the change of the slope, i.e., the effective mass of the potential? **w changes but the luminosity distance is 2 integrals of it.**

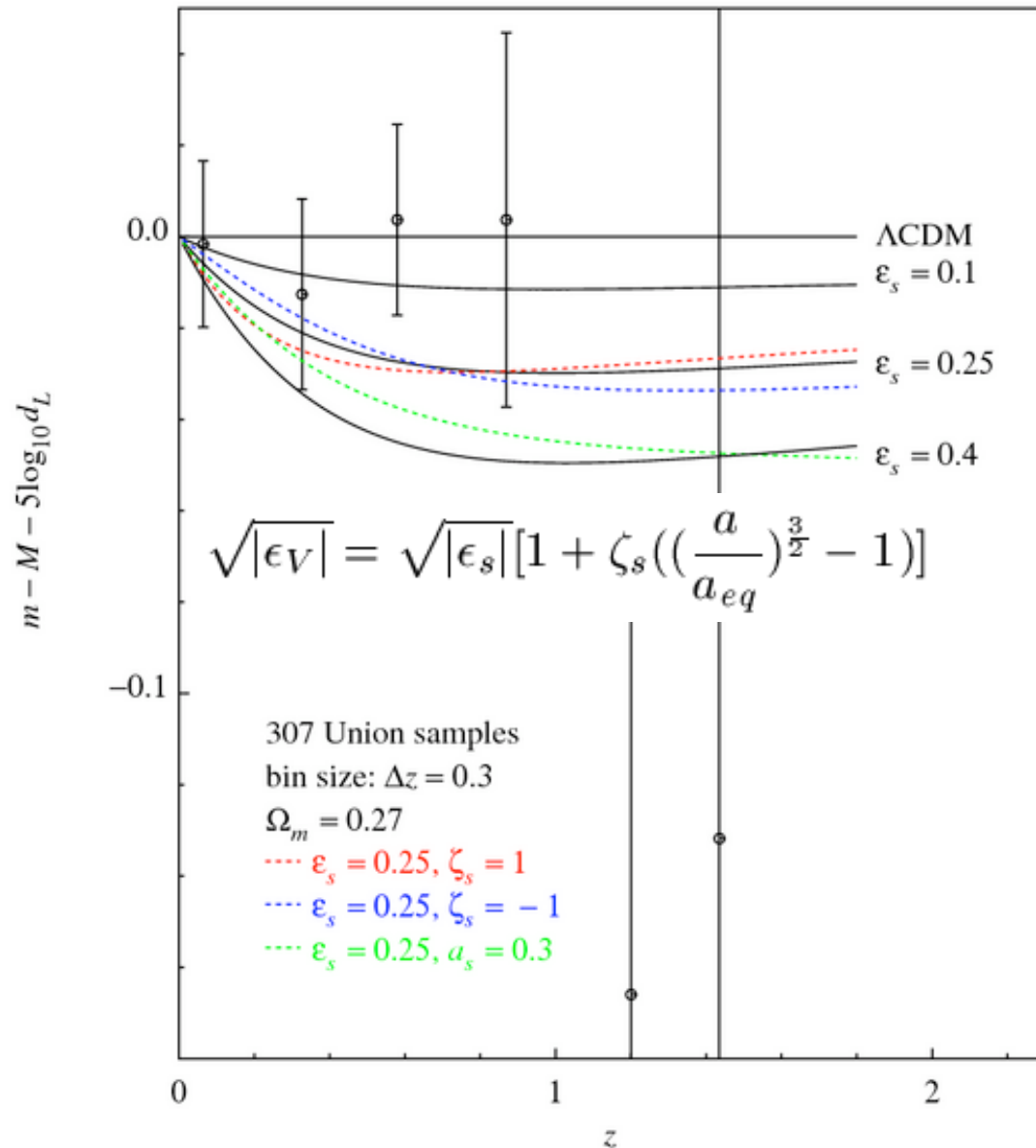
we fit $w(z)$ for tracker potentials very well

$$\sqrt{|\epsilon_V|} = \sqrt{|\epsilon_s|} \left[1 + \zeta_s \left(\left(\frac{a}{a_{eq}} \right)^{\frac{3}{2}} - 1 \right) \right]$$



Why we can measure the 1st but not the 2nd derivative of the log-potential.

potential reconstruction very partial



DE interaction & 5th force?

e.g., action $\sim F(\phi, R) + L_m$, Jordan frame, cf. Einstein frame action $F = M_P^2/2 R$,

Jordan-Brans-Dicke/scalar-tensor $F = f(\phi)R/2 + d\phi d\phi/2 - V(\phi)$, dilaton $f = e^{2\phi/M_P}$

conformal transformation $\Omega^{-2} = dF / dM_P^2/2 R$ to Einstein frame

order parameter field $\psi = -\sqrt{6} \ln \Omega$ (replaces ϕ if $\Omega^{-2}(\phi)$ only)

ψ couples to $\rho_m - 3p_m$

chameleon is the dilaton-motivated one (Khouri and Weltman 04, ..., Kaloper 07)

general dilaton-motivated coupling $\exp(2\beta_i \psi) L_{mi}$

phantom mimic: ρ_m has a correction to a^{-3} , interpret it as an addition to DE w ,
which can give an apparent $w < -1$

solar system tests are an issue. strong constraints on $\beta_{i,j}$

$m_i(\psi)$ (modified mass, dynamical (very low energy) higgs + std one). couples to ρ_m

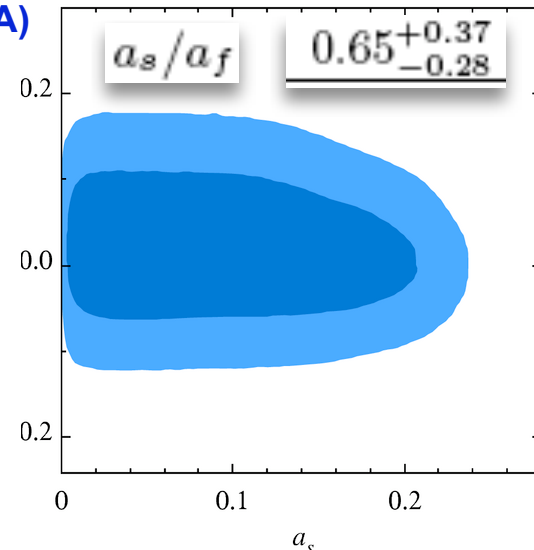
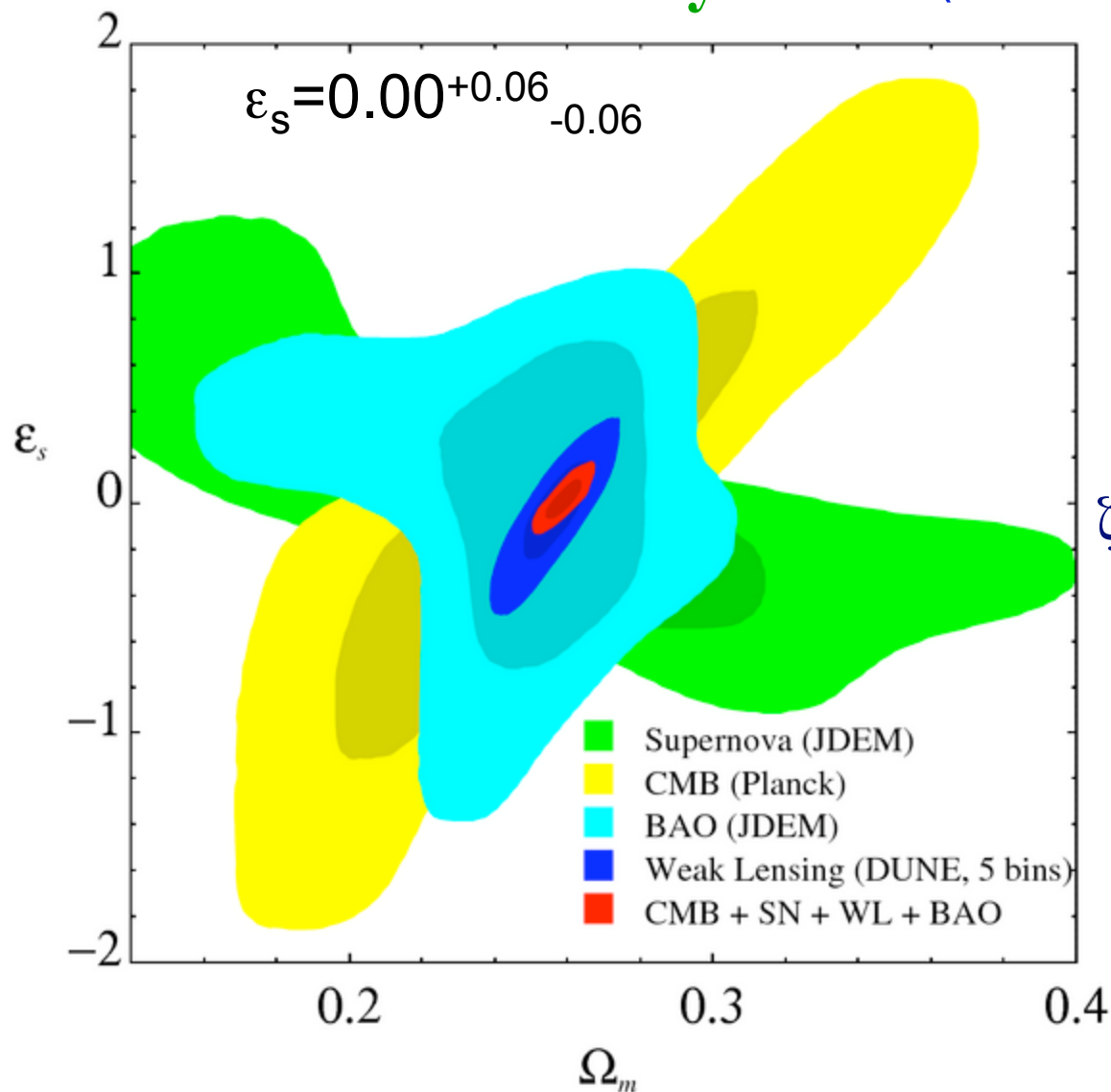
**INFLATION
NOW**

**PROBES
THEN**

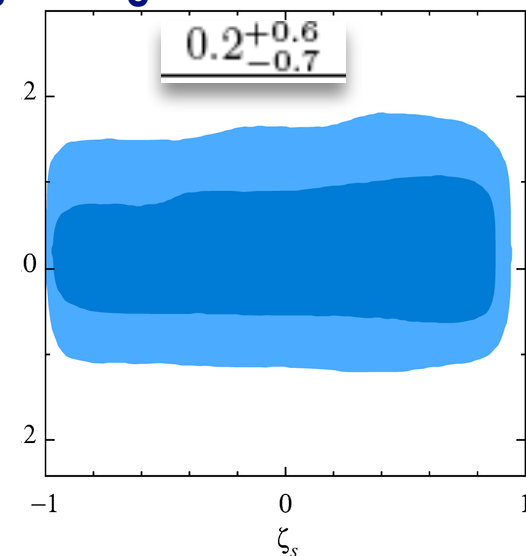
Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)

+ **DUNE-WL** (50% sky, gals @z = 0.1-1.1, 35/min²) +

Planck1yr **ESA (+NASA/CSA)**

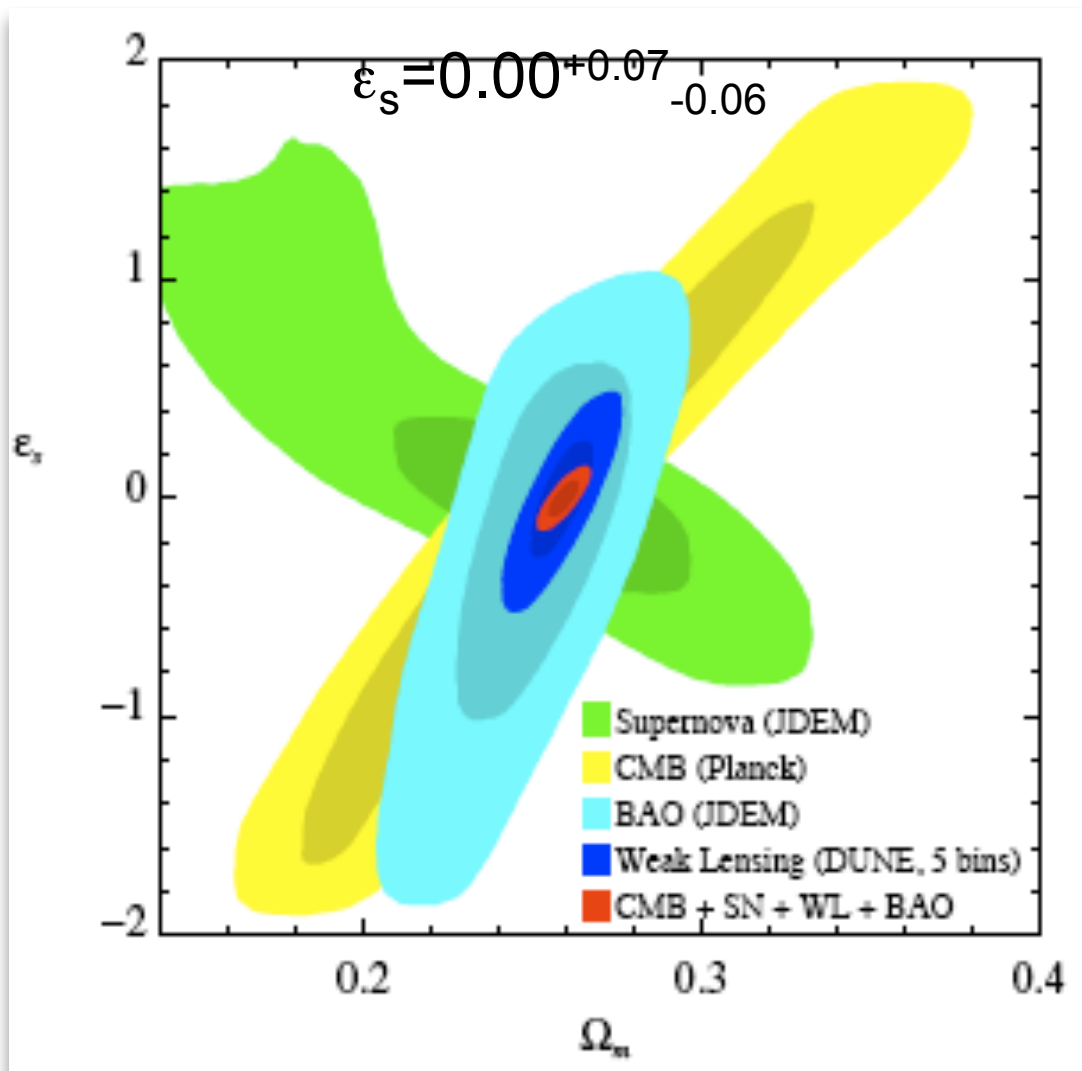


$\zeta_s \sim -d \ln \epsilon_s / d \ln a_s$ ill-determined



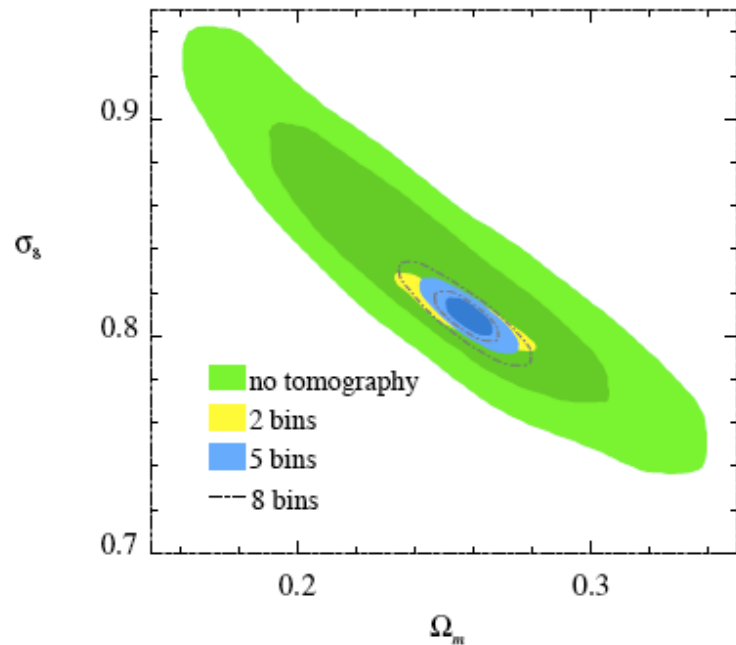
Forecast: **JDEM-SN** (2500 hi-z + 500 low-z)
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Planck1yr **ESA (+NASA/CSA)**

$a_s=0$ case



$\zeta_s \sim d \ln \epsilon_s / d \ln a \approx 2$ ill-determined

$0.1^{+0.6}_{-0.7}$



Inflation now summary

- the data cannot determine more than 2 w-parameters (+ c_sound?). general higher order Chebyshev or spline expansion in $1+w$ as for “inflation-then” $\epsilon=(1+q)$ is not that useful. **Parameter eigenmodes** show what is probed
- Any $w(a)$ leads to a viable DE model. The $w(a)=w_0+w_a(1-a)$ phenomenology requires baroque potentials
- Philosophy of HBK08: **backtrack from now (z=0) all w-trajectories arising from quintessence ($\epsilon_s > 0$) and the**

phantom equivalent ($\epsilon_s < 0$); use a 3-parameter model $\epsilon_\phi = (1+w(a))^{3/2} = \epsilon_s f(a/a_{\Lambda eq}; a_s/a_{\Lambda eq}; \zeta_s)$ to well-approximate even rather baroque w-trajectories, as well as thawing & freezing trajectories.

- We ignore constraints on Q-density from photon-decoupling and BBN because further trajectory extrapolation is needed. Can include via a prior on $\Omega_Q(a)$ at z_{dec} and z_{bbn} .**
- For general slow-to-moderate rolling 2 “dynamical parameters” (a_s, ϵ_s) & Ω_Q describe w to a few %. In early-scaling-exit, the information stored in a_s is erased by Hubble drag over the observable range & w can be described by a single parameter ϵ_s . for baroque w-trajectories, add a 3rd param ζ_s ($d \ln \epsilon_s / d \ln a / 2$) - not-determined now & then. freeze-out w at high z, 4th param

$$\begin{matrix} -0.00^{+0.09} \\ -0.13 \end{matrix}$$

$$\begin{matrix} 0.00^{+0.20+0.42} \\ \dots \end{matrix}$$

- prior-dependence e.g. $\sqrt{\epsilon_s}$, a_s near 0, $\epsilon_s > 0$ since $\epsilon_\phi < 0$ of phantom energy, negative kinetic energy is baroque
- Apr08 observations well-centered around a cosmological constant $\epsilon_s = -0.03 \pm 0.28$ $a_s < 0.36$ ($z_s > 2.0$)
cf. $\epsilon_{\phi 0} = -0.00 \pm 0.09$ if constant, $\epsilon_{\phi 0} = -0.015 \pm 0.30$ if a-linear model
- in Planck1yr-CMB+JDEM-SN+DUNE-WL future ϵ_s to ± 0.07 , a_s to < 0.21 ($z_s > 3.7$)**
- cannot reconstruct the quintessence potential**, just the slope ϵ_s & hubble drag info
- late-inflaton field is $<$ Planck mass, but not by a lot
- DE may couple to matter, 5th force constraints are strong, maybe best hope in determining more about DE (chameleon example of dilaton a la Khoury and Weltman 04)

end

Inflation Then $\epsilon(k) \sim r/16$

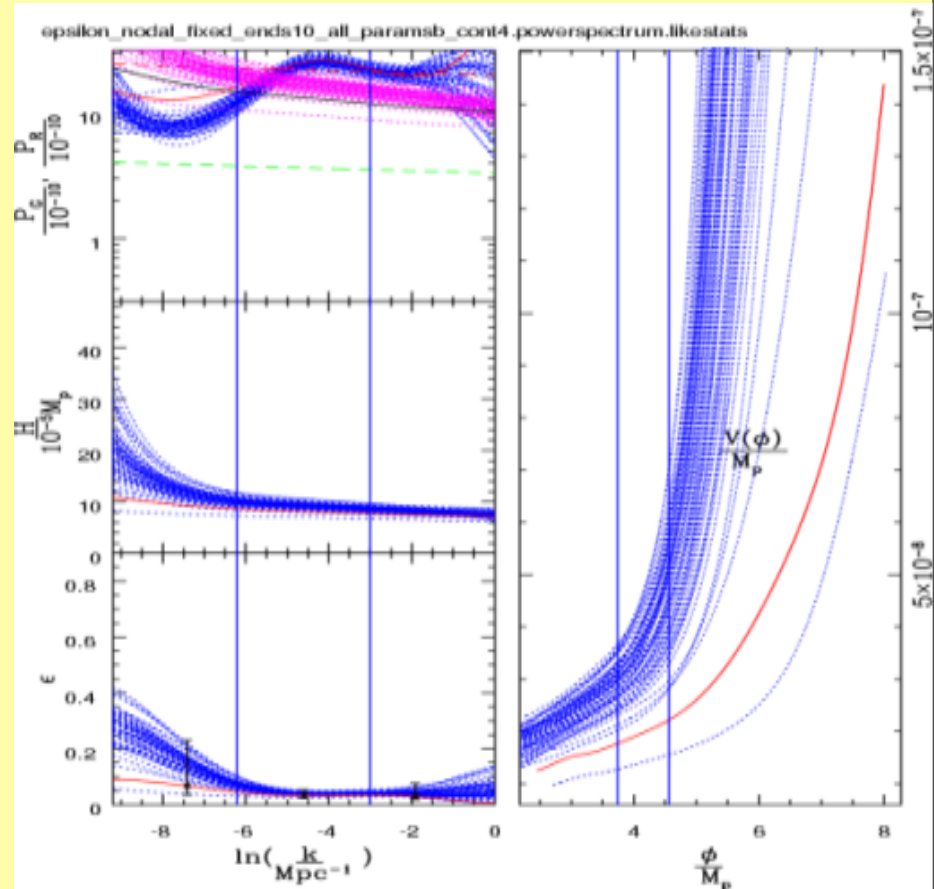
= mode expansion in $\ln H a \sim \ln k$

be blind: all $\epsilon < 1$ trajectories give allowed potential & kinetic energies

~ 10 good e-folds $k \sim 10^{-4} \text{Mpc}^{-1}$ to $\sim 1 \text{Mpc}^{-1}$

$\sim 10+$ parameters? $H(\phi)$, $V(\phi)$

Bond, Contaldi, Huang, Kofman, Vaudrevange 08



Inflation Now all $\epsilon_\phi < 1$ trajectories give allowed potential & kinetic energies but... do not be blind:... ~ 1 good e-fold. only ~ 2 params

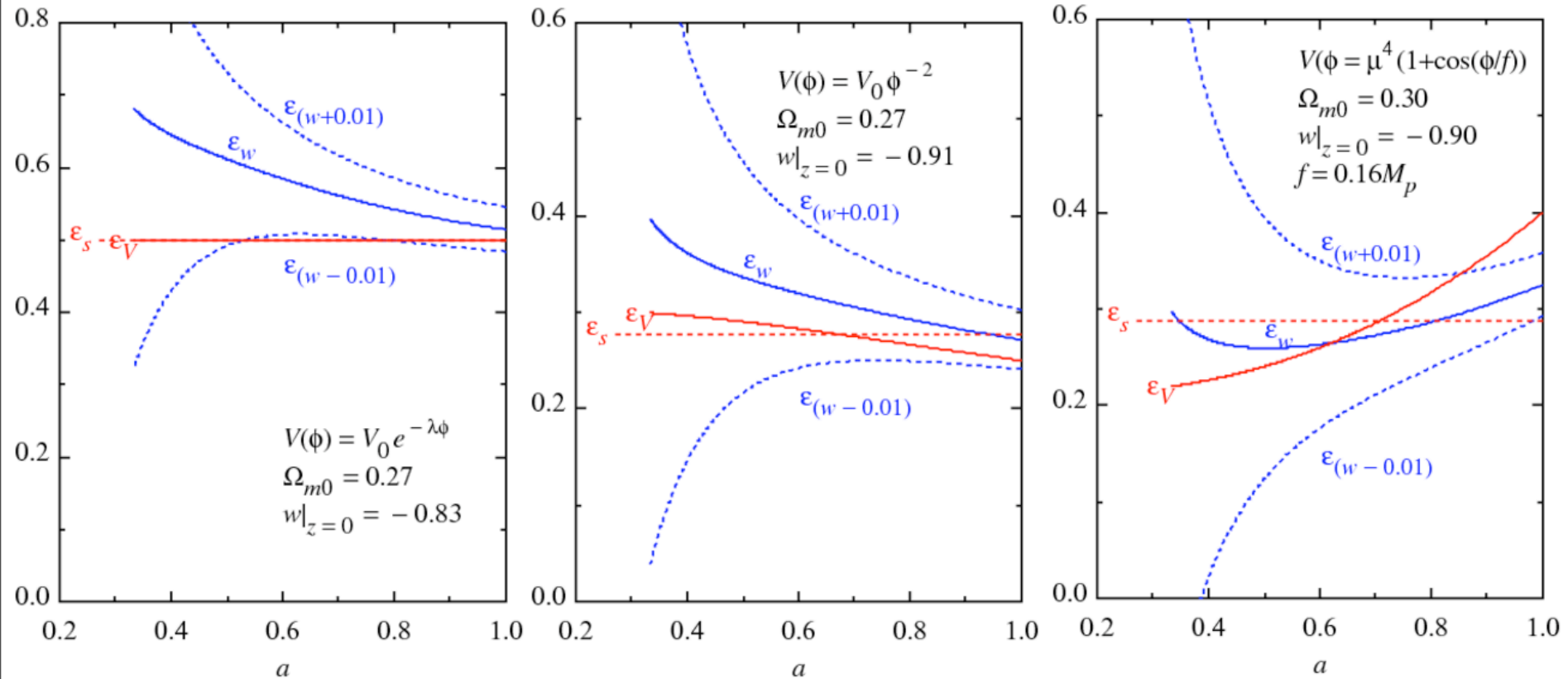
get $\epsilon_s = (d \ln V / d \psi)^2 / 4$ @ pivot pt

Huang, Bond & Kofman 08

ϵ_V trajectories are slowly varying: why the fits are good

Dynamical $\epsilon_w = \epsilon_\phi \epsilon_s / \epsilon_{\phi\text{-approx}}$ cf. shape $\epsilon_V = (V'/V)^2$ (a) / (16πG)

& ϵ_s is ϵ_V uniformly averaged over $0 < z < 2$ in a



the quintessence field is below the reduced Planck mass

