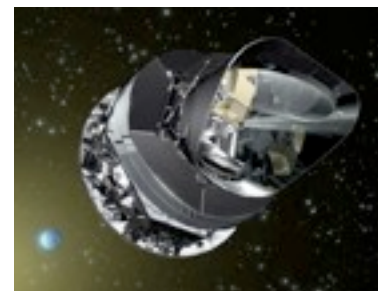
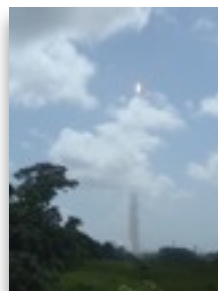
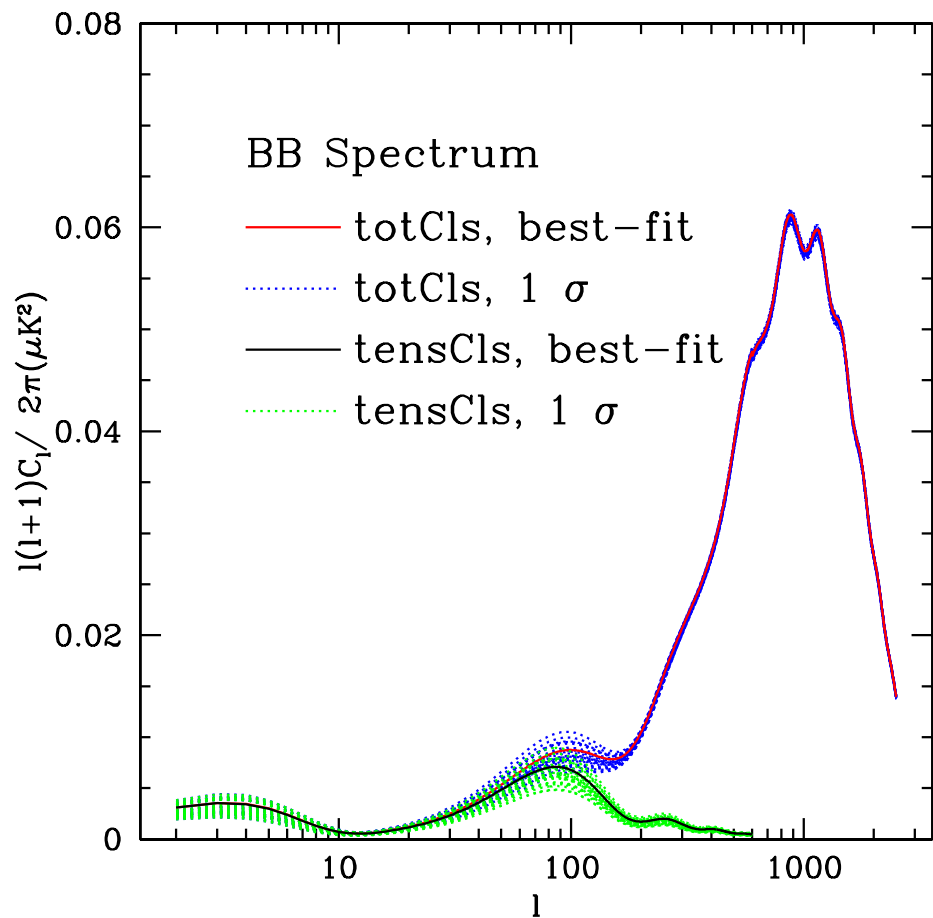
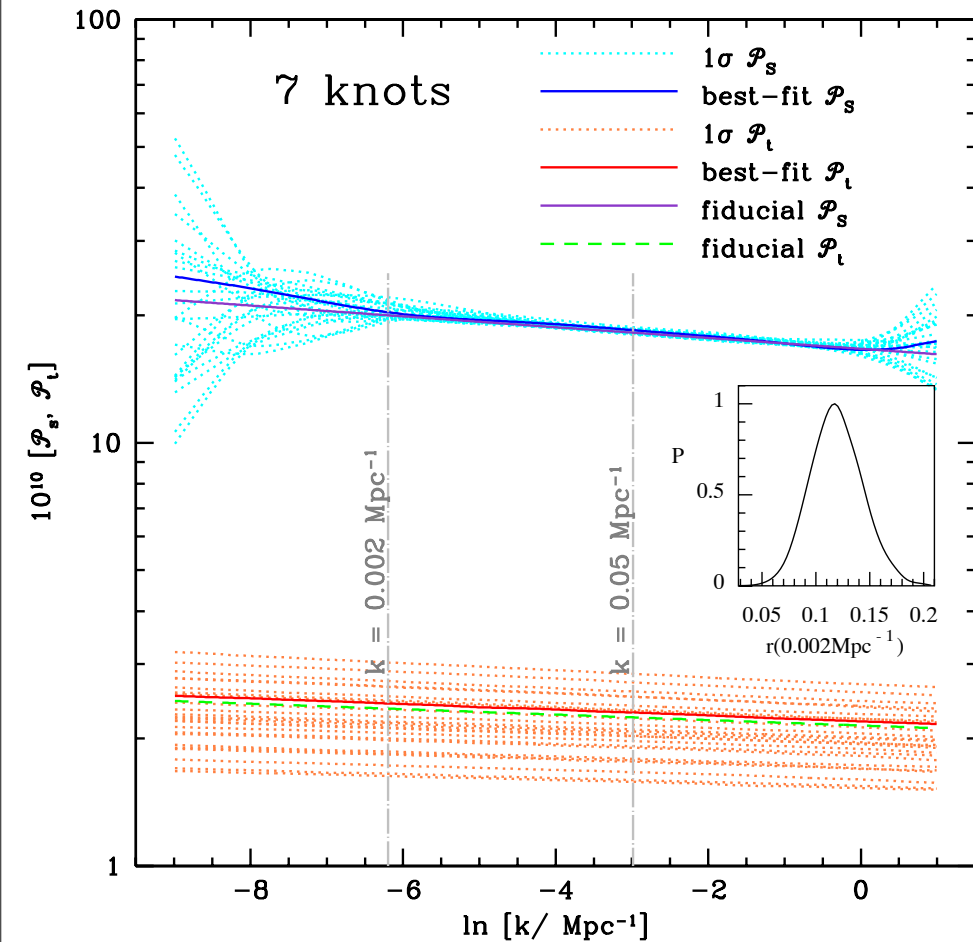


# compress data onto non-top-hat k-modes

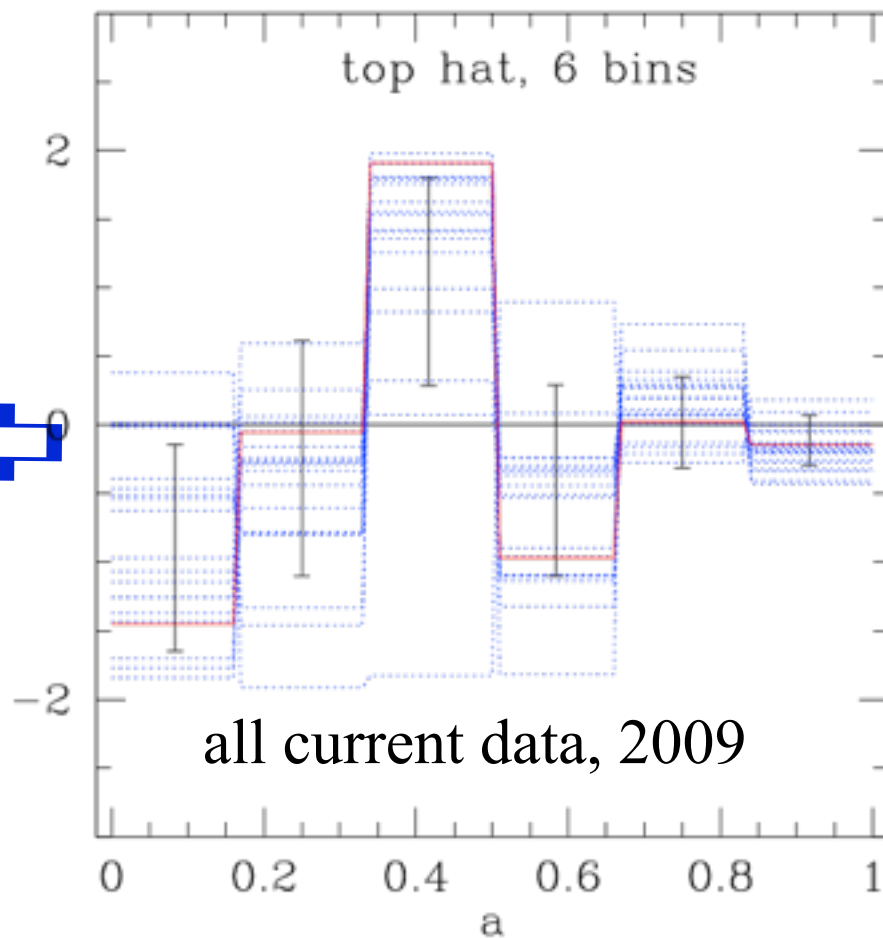
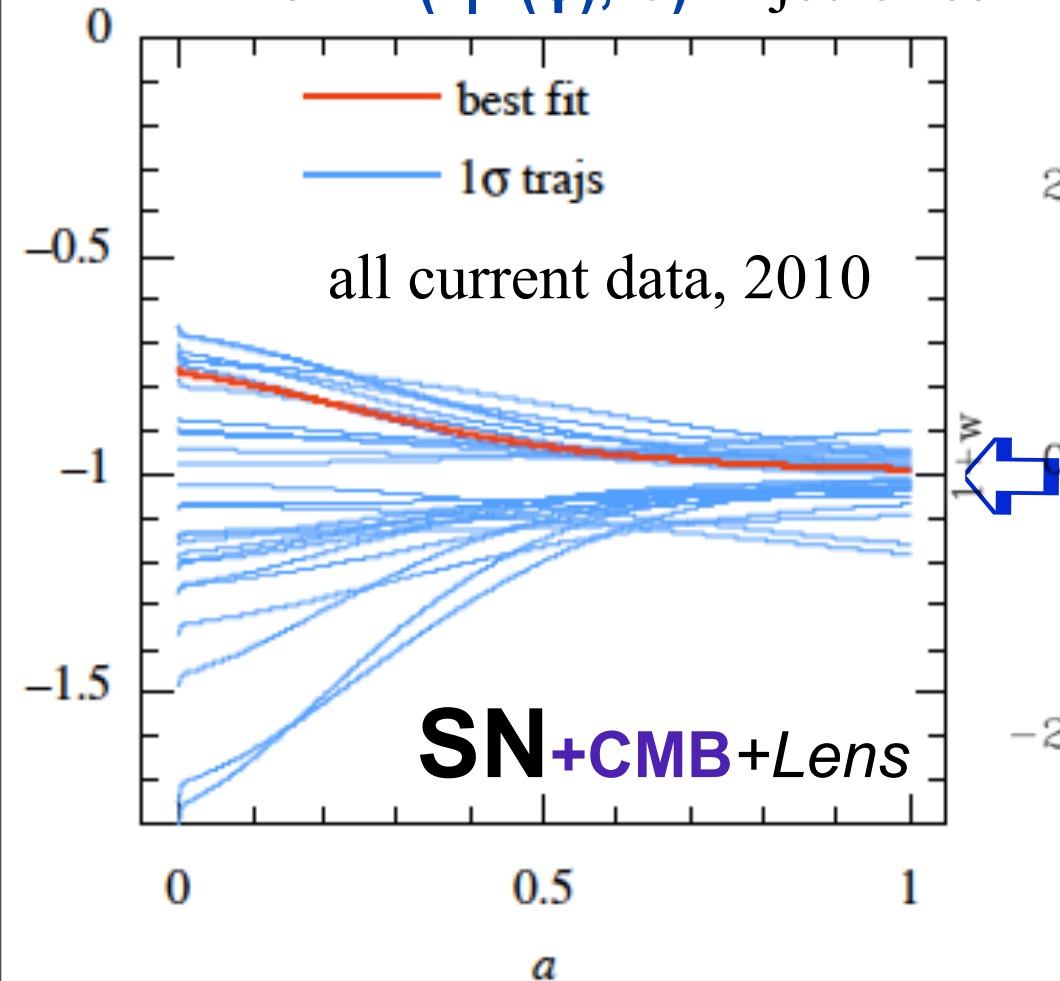
Planck2.5 7 knot forecast with inflation consistency; input  $r=0.12 m^2\phi^2$



# is the dark energy “vacuum potential energy” ?

3-parameter paves even wild late-inflaton  $w(z|V(\psi), IC)$  trajectories

semi-blind mode expansion



TEST: within errors, energy-density does not change with expansion  $\Rightarrow$  Einstein's cosmological constant is best fit so far

# ***Early & Late U Inflation: Cosmic Sports with Lev Kofman***

the horizon seen from the 70s, 80s, 90s, 00s

**\*\* the high resolution frontier: the insides of clusters via SZ (SuZie,..., Acbar, QUaD, ... CCAT, CARMA++,ALMA,GBT,... ACT, SPT, Planck)**

**the polarization frontier: down the damping tail, through Planck (and ACTpol, SPTpol, ...)**

**the CMB computational horizon: simulations & Monte Carlos**

**the CMB computational horizon: optimal de-nuisanced maps from large-format arrays; algorithmic advances, foreground/source issues**

**\*\* Theory of inflation & dark energy: the non-Gaussian frontier (beyond  $f_{NL}$  templates  $-4 < f_{NL} < 80$  now to  $f_{NL} \sim \pm 5$  Planck; will Gravity Wave  $B$  be big enough to detect  $r(k)$ ? DE w  $(z|V(\psi), IC)$  trajectories**

***beyond the SM: in quest of the sub-dominant & the anomalous***

**\*\* the polarization frontier: the quest for B-modes and primordial gravity waves - small-sky (Bicep, KECK, Spider), Planck+small-sky, need for a CMBpol??**

standard inflation space:  $n_s$   $dn_s/d\ln k$   $r = T/S$  @k-pivots

# What can be observed?

*forecasting QU not EB*

*Spider  $2\sigma_r \sim 0.02$  for  $0.02 < f_{\text{sky}} < 0.15$*

*Planck 2.5yr  $2\sigma_r \sim 0.02 \Rightarrow \sim 0.05$  (foregrounds)*

Marzieh Fahrang, Bond, Dore & Netterfield 2010

## What is predicted? ???

$0 < r < 0.5$ ,  $-12 < \log(r) < -0.3$

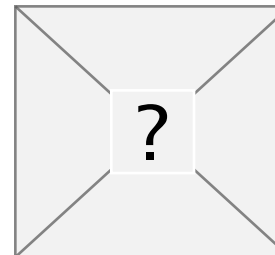
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## WHAT IS PREDICTED?

Smoothly broken scale invariance  
by nearly uniform braking (standard  
of 80s/90s/00s)  $r \sim 0.03-0.5$

large field inflation (field moves  $>$  Planck mass)  
or highly variable braking  $r$  tiny

(stringy cosmology)  $r < 10^{-10}$



small field inflation (field moves  $<$  Planck mass  $\Rightarrow r < .007$ )

Bond, Kofman, Prokushkin, Vaudrevange 07, Roulette Inflation with Kahler Moduli and their Axions

Barnaby, Bond, Zhiqi Huang, Kofman 09, Preheating after Modular Inflation

*monodromy (V=cosine+linear) & fibre inflation give larger r*

current  $r$  constraints (95%CL) - prior sensitive

$r < 0.16$  (no running, all data sets)

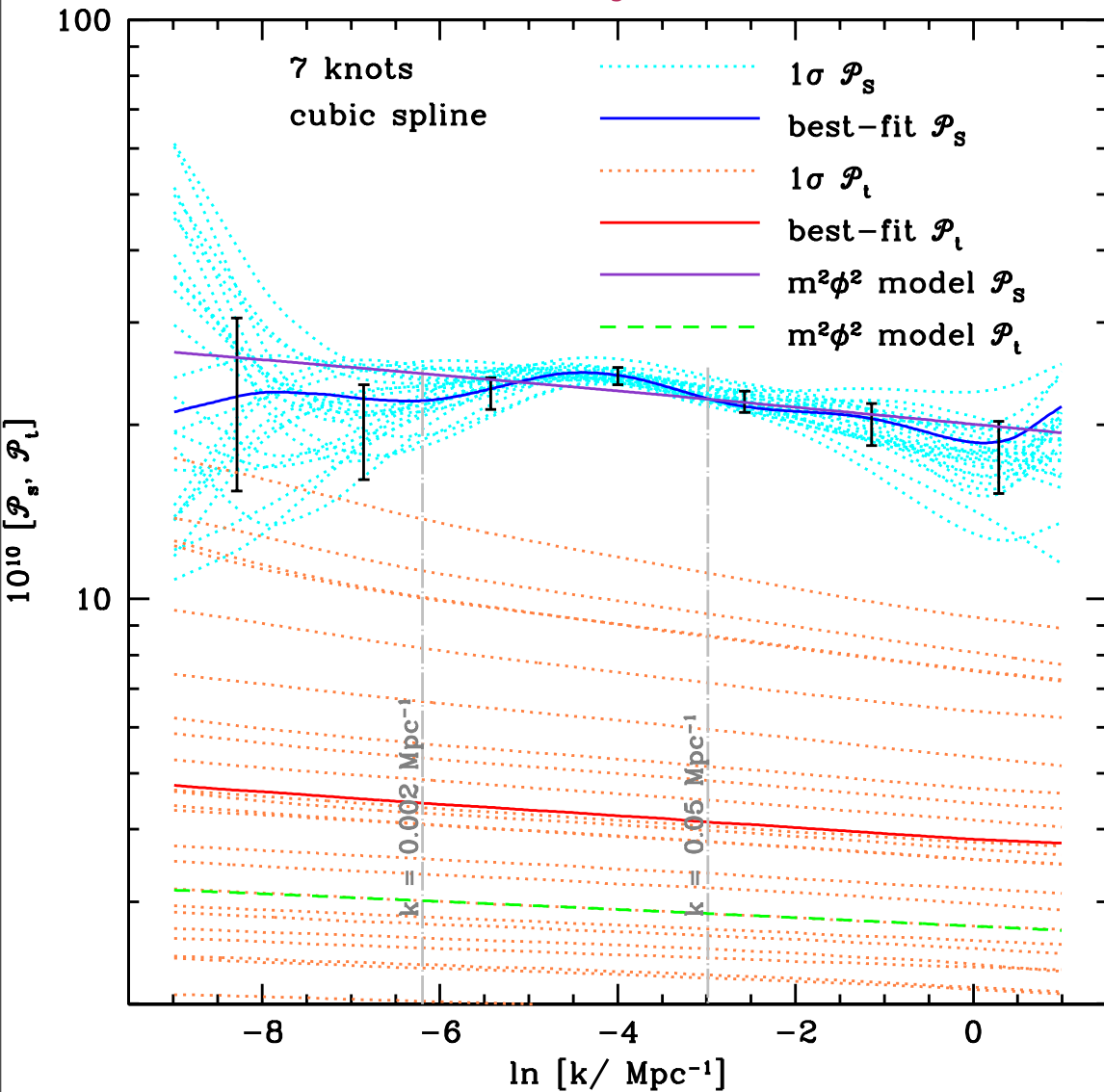
$r < 0.32$  (no running, CMB-only data sets)

$r < 0.27$  (with running, all data sets)

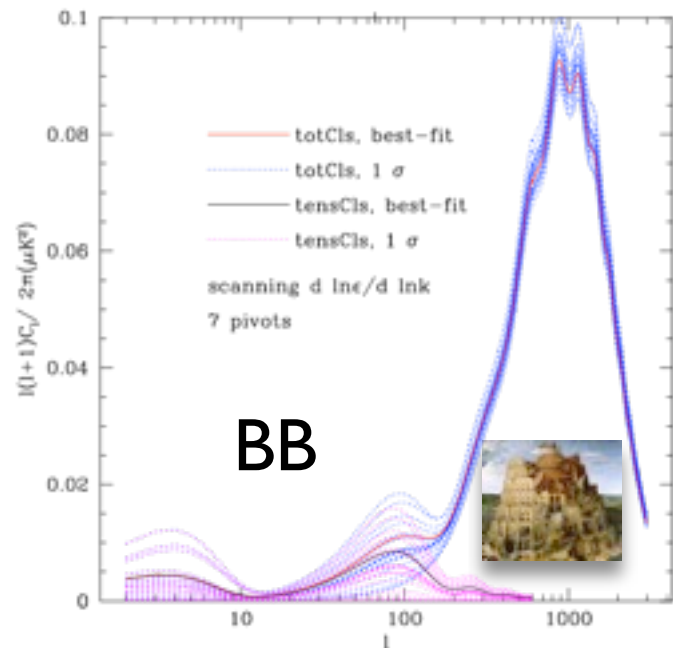
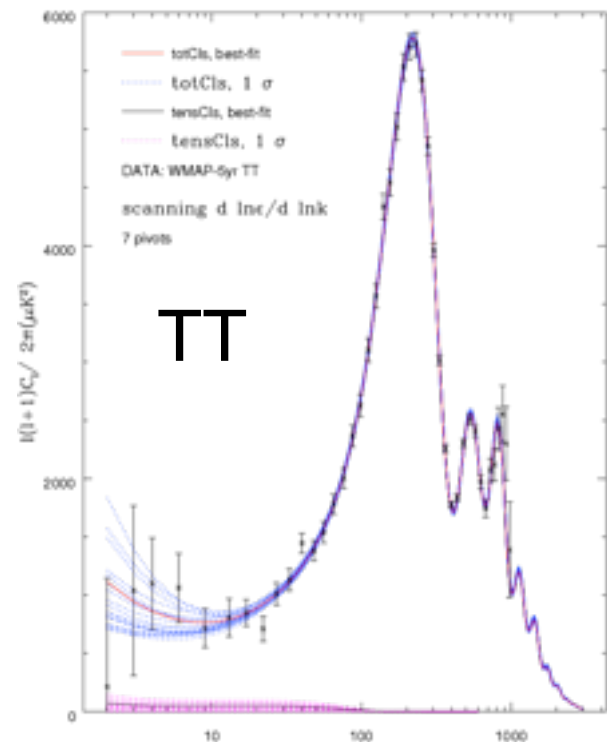
inflation consistency  
 $-n_t \approx r/8 \approx 2\varepsilon(k)$   
 $1-n_s \approx 2\varepsilon + d\ln\varepsilon/d\ln H a$

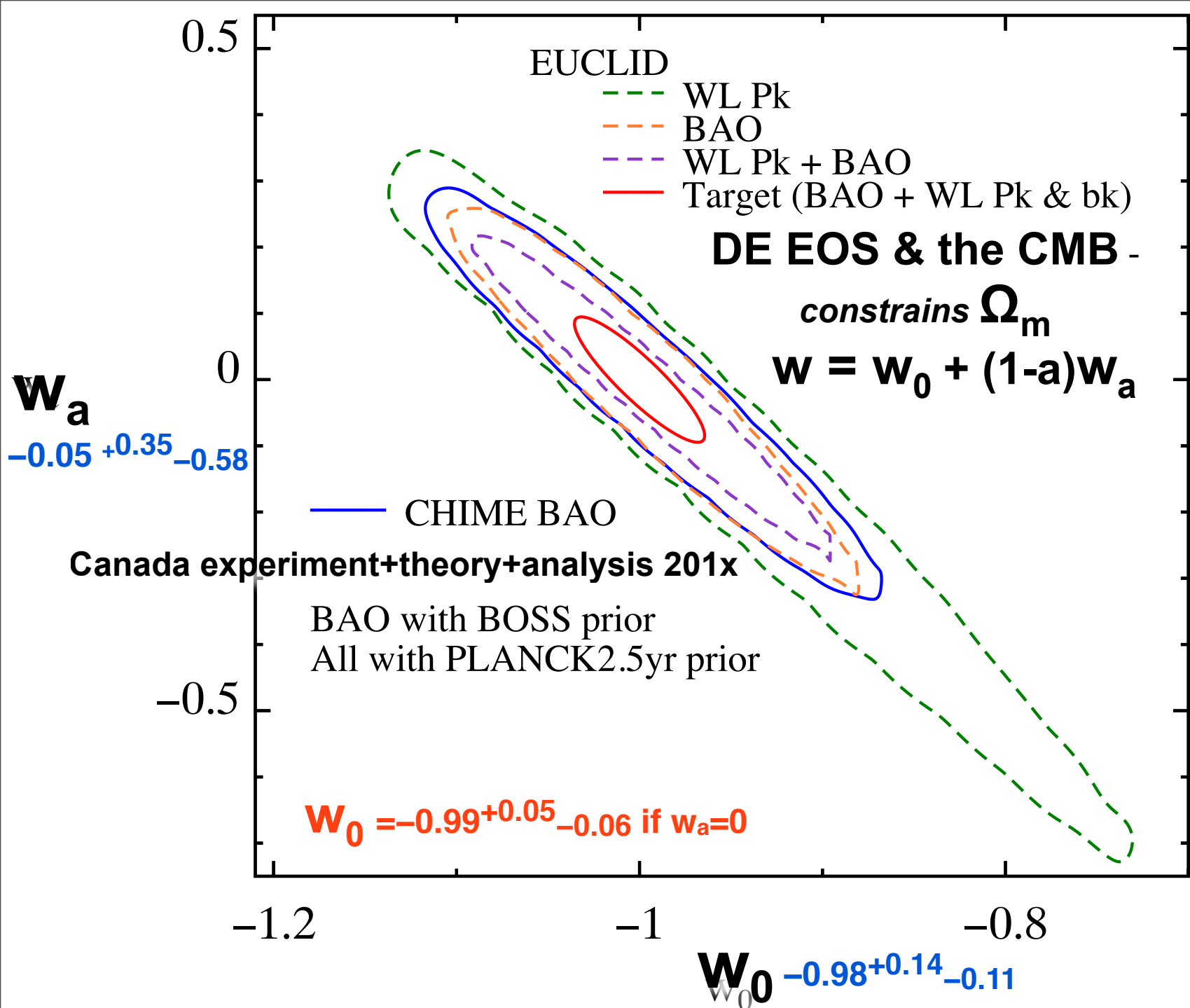
# compress data onto non-top-hat k-modes

*partially-blind acceleration trajectories obeying tensor/scalar consistency relation. Nov09 data*



Bond, Contaldi, Huang, Kofman, Vaudrevange 2010





# *the Cosmotician's Agenda: Statistical Paths in Cosmic Theory & Data*

**Dick Bond** Canadian Institute for Theoretical Astrophysics, University of Toronto

**Cosmotician**  $P(\text{cosmic parameters}|D,T)$ ,  $P(D|T)$   $D=\text{CMB,LSS,SN,...,complexity}$ ,  $T=\text{baryon, dark matter, vacuum mass-energy densities,...,early and late inflation,structure of manifolds (extra compactifying } 7 + 3+1), \text{holes, branes, fibres, strings,vacuua landscape, physical coupling 'constants'}$  **Anthrostatician**

Cosmic history: what is U made of?  $\Rightarrow \rho_{\text{dm}}/\rho_{\text{b}} = 5.1 \Rightarrow \rho_{\text{m}}/\rho_{\text{de}} = .30$   
and  $\Omega_{\text{m}} = 0.268 \pm 0.012$ ,  $\Omega_{\Lambda} = 0.736 \pm 0.012 \Rightarrow (0.294 \pm 0.011, 0.706 \pm 0.011)$

How Structure in the Universe Arose?: *from nearly Gaussian early Inflation vacuum fluctuations in curvature, isocurvature & Gravity Wave fields morphs into the nonlinear Cosmic Web: clusters, filaments, voids; galaxies*

What is the fate of U: dark energy properties driving late inflation

**CMBology &  $\Lambda$ CDM,  $\Lambda$ +tilt**: the cosmic standard model, status@Nov09:  
**Boomerang, CBI, Acbar, WMAP**, DASI, QuAD, ..  $P(D|T)$  paths for early & late inflation

**is there a y to x? @2011-12 from new expts: ACT, Planck, Spider, Keck, ACTpol**  
SPT, EBEX, Bicep, Quiet, SPTpol,.. acceleration paths for B-modes, dark energy probes



# What is the Universe made of?

**NOW:** baryons + (cold-ish) dark matter + dark energy/inflaton + tiny curvature energy (+light neutrinos+photons). ??a bit of strings/textures/PBHs?? *web of galaxies/clusters*

**THEN:** coherent inflaton / "vacuum" energy plus **zero-point fluctuations** in all fields ( $\approx$  Gaussian RF) & then preheat via mode coupling to incoherent cascade to thermal equilibrium aka quark-gluon plasma  
**& how was it, is it & will it be distributed?**

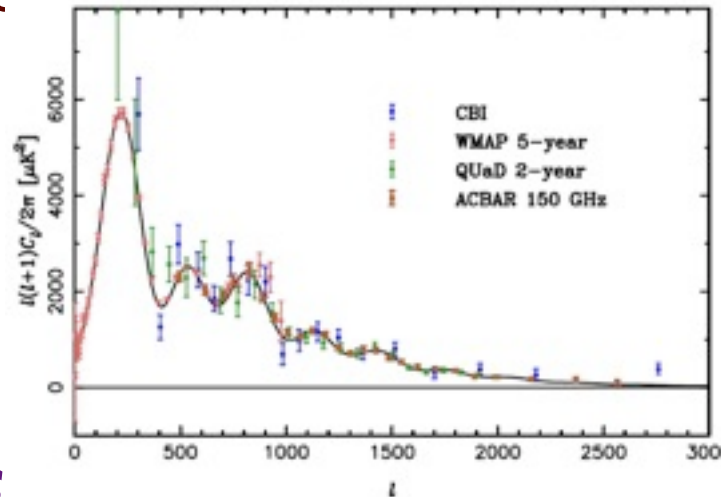
**very early U**      early to middle to now U      **very late U**

*string theory/landscape/higher dimensions*

**inflation** cyclic    baryogenesis    dark matter    BBN     $\nu$ dec    **dark energy**

$V_{\text{eff}}(\psi_{\text{inf}}) ?$

$K_{\text{eff}}(\psi_{\text{inf}}) ?$



$V_{\text{eff}}(\psi_{\text{inf}}) ?$

$K_{\text{eff}}(\psi_{\text{inf}}) ?$

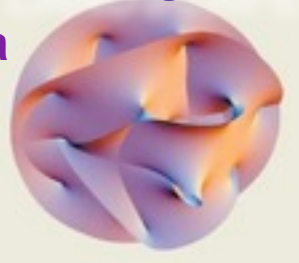
**cosmic mysteries**

$n_b/n_\gamma$   $\rho_{\text{dm}}/\rho_b$   $z_{\text{eq}}/z_{\text{rec}}$   $\rho_{\text{curv}}$   $\rho_{\text{de}}/\rho_{\text{dm}}$   $\rho_{\text{de}} \sim H^2 M_{\text{Planck}}^2$   $\rho_{\text{m}\nu} / \rho_{\text{stars}}$

**Old view:** Theory prior = delta function of THE correct one and only theory

**New:** Theory prior = probability distribution of late-flows on an energy LANDSCAPE

6/7 tiny extra dimensions



1980

$R^2$ -inflation

Old Inflation

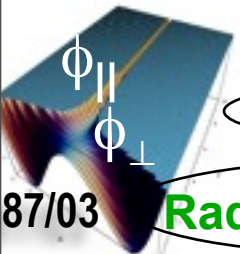
Chaotic inflation

New Inflation

Double Inflation

Power-law inflation

SUGRA inflation



87/03

Radical BSI inflation

running (nee variable  $M_P$ ) inflation

Extended inflation

1990

Natural pMGB inflation

Hybrid inflation

KLS94 preheating

SUSY F-term inflation

SUSY D-term inflation

Assisted inflation

Brane inflation

2000

SUSY P-term inflation

Super-natural Inflation

K-flation

2003 KKL

N-flation

D3,D7 brane inflation

DBI inflation

ekpyrotic/cyclic

moving brane separations

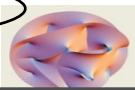
Racetrack inflation

Tachyon inflation

Warped Brane inflation

moduli fields

monodromy

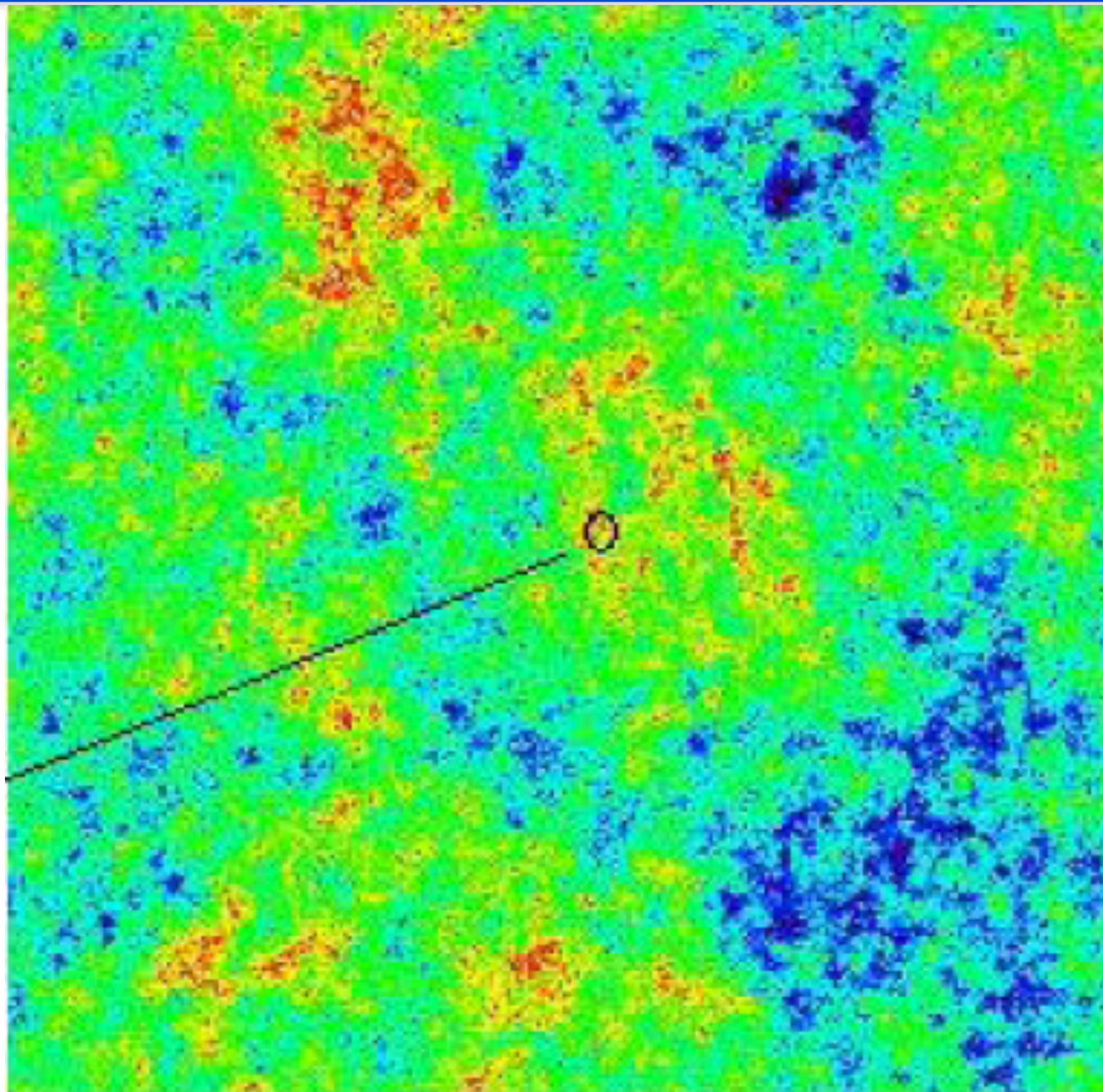


Roulette inflation Kahler moduli/axion

fiber inflation

**fluctuations in the early universe “vacuum” grow to *all* structure**

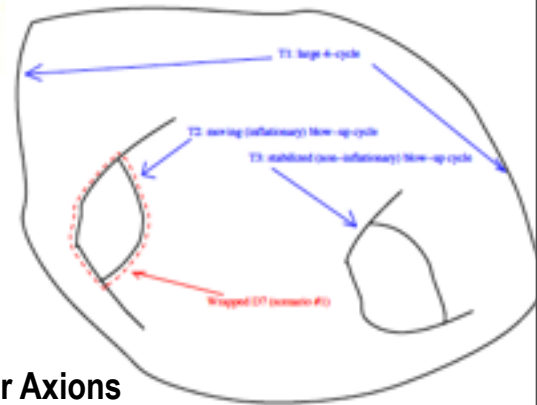
$\chi$



patterns  
in the  
quantum  
jitter  
evolve  
under  
gravity  
  
(& gas  
dynamics)

current  
Hubble  
patch  
~10 Gpc  
  
speed  
limit  
horizon

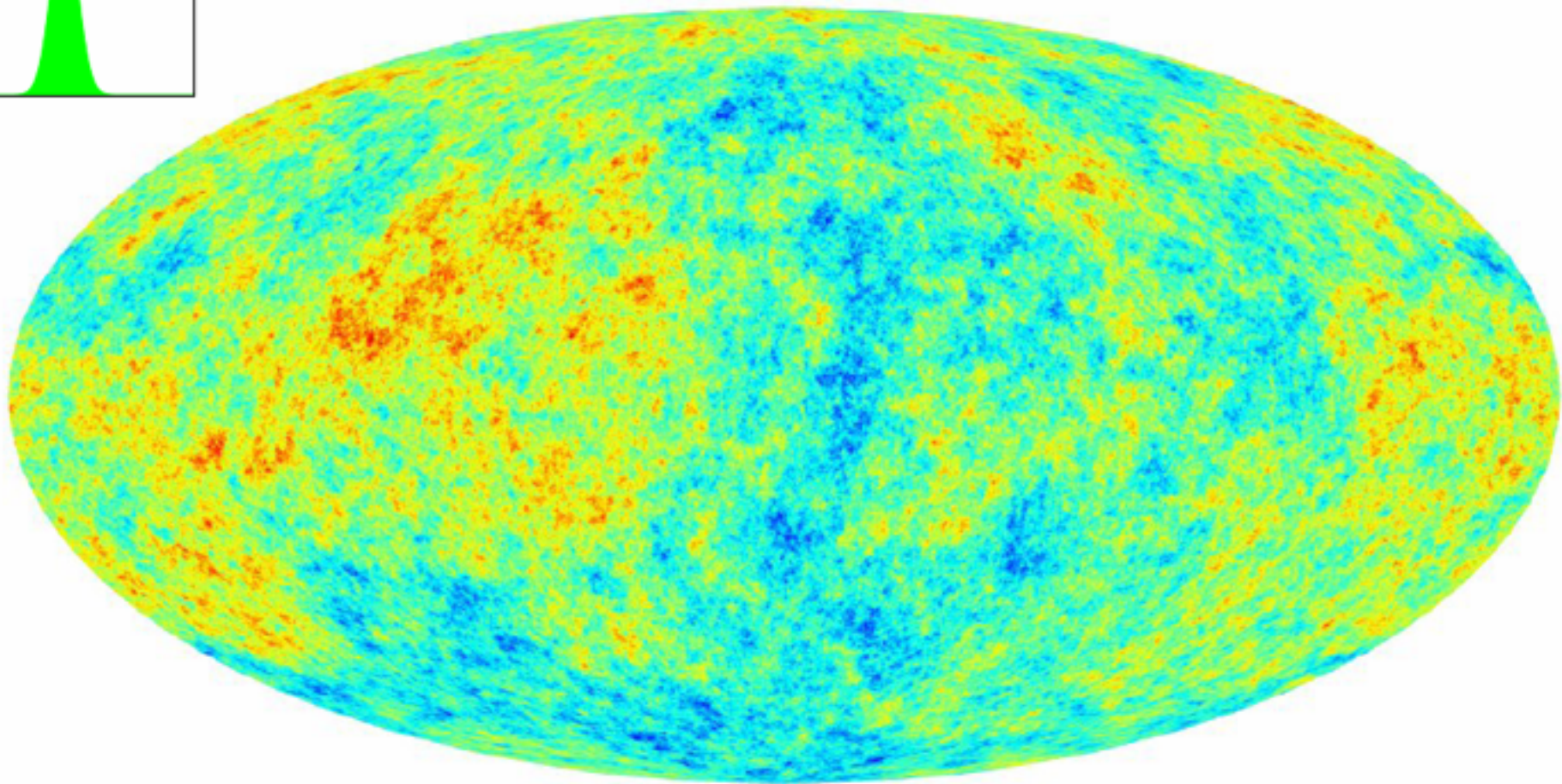
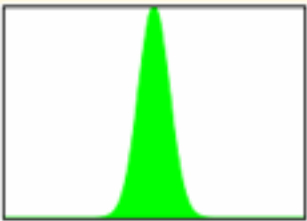
1000 Gpc

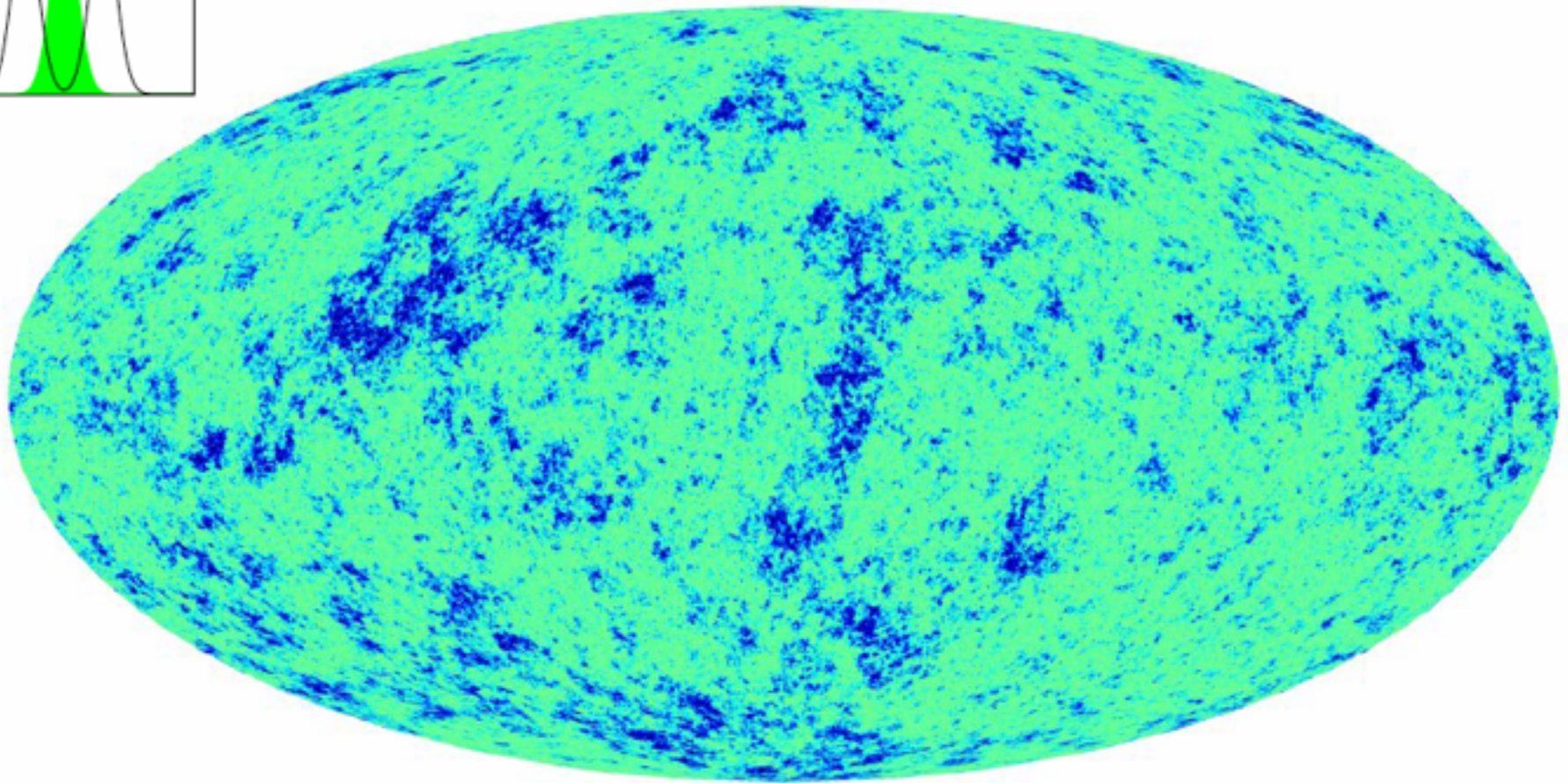
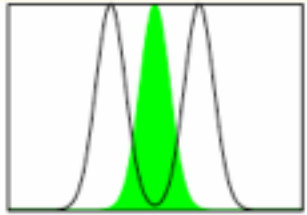


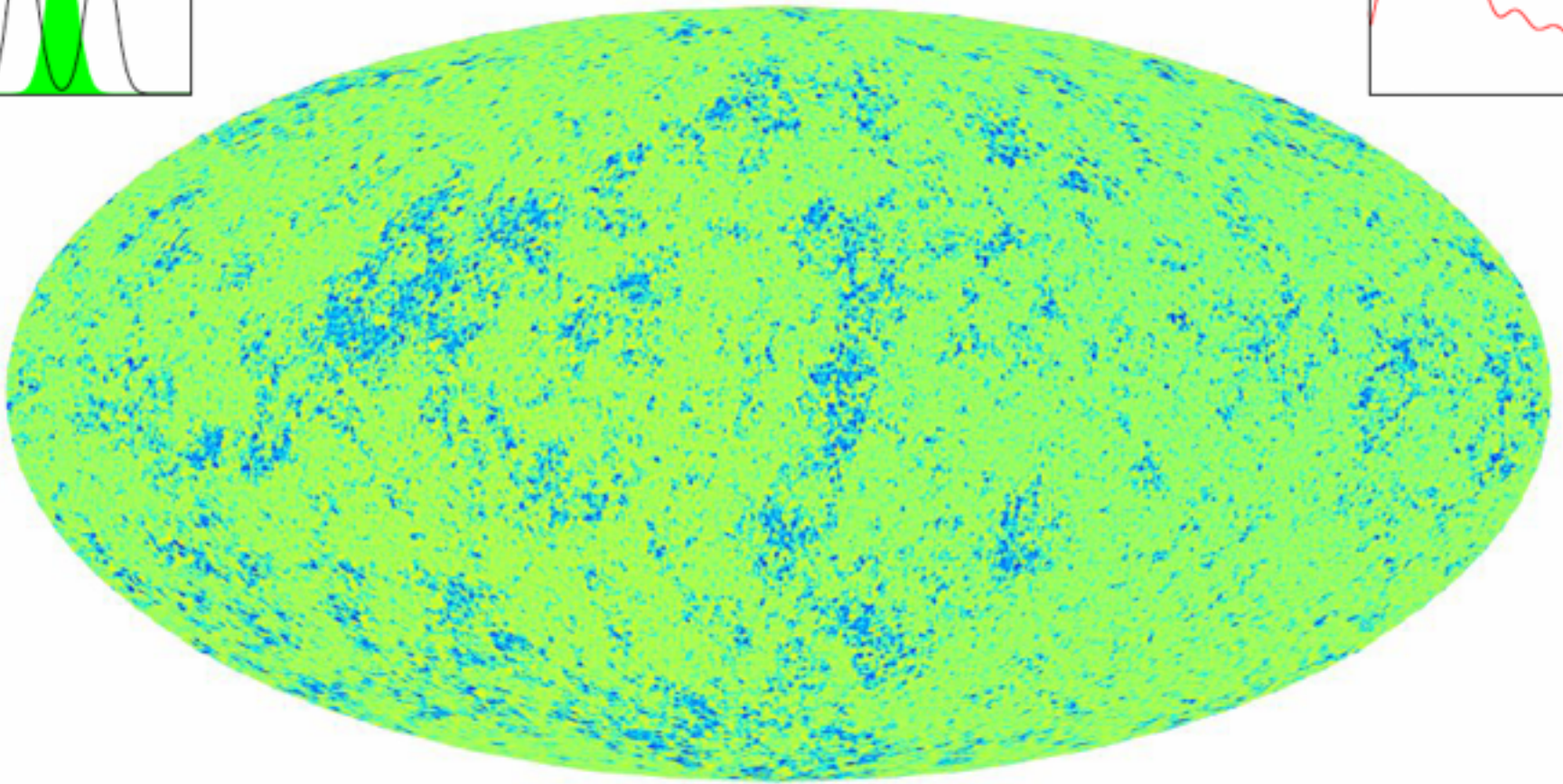
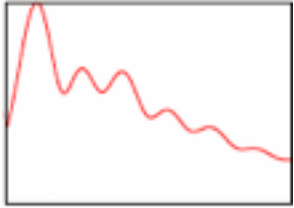
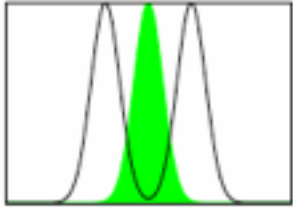
Balasubramanian, Berlund, Conlon, Quevedo, . . .

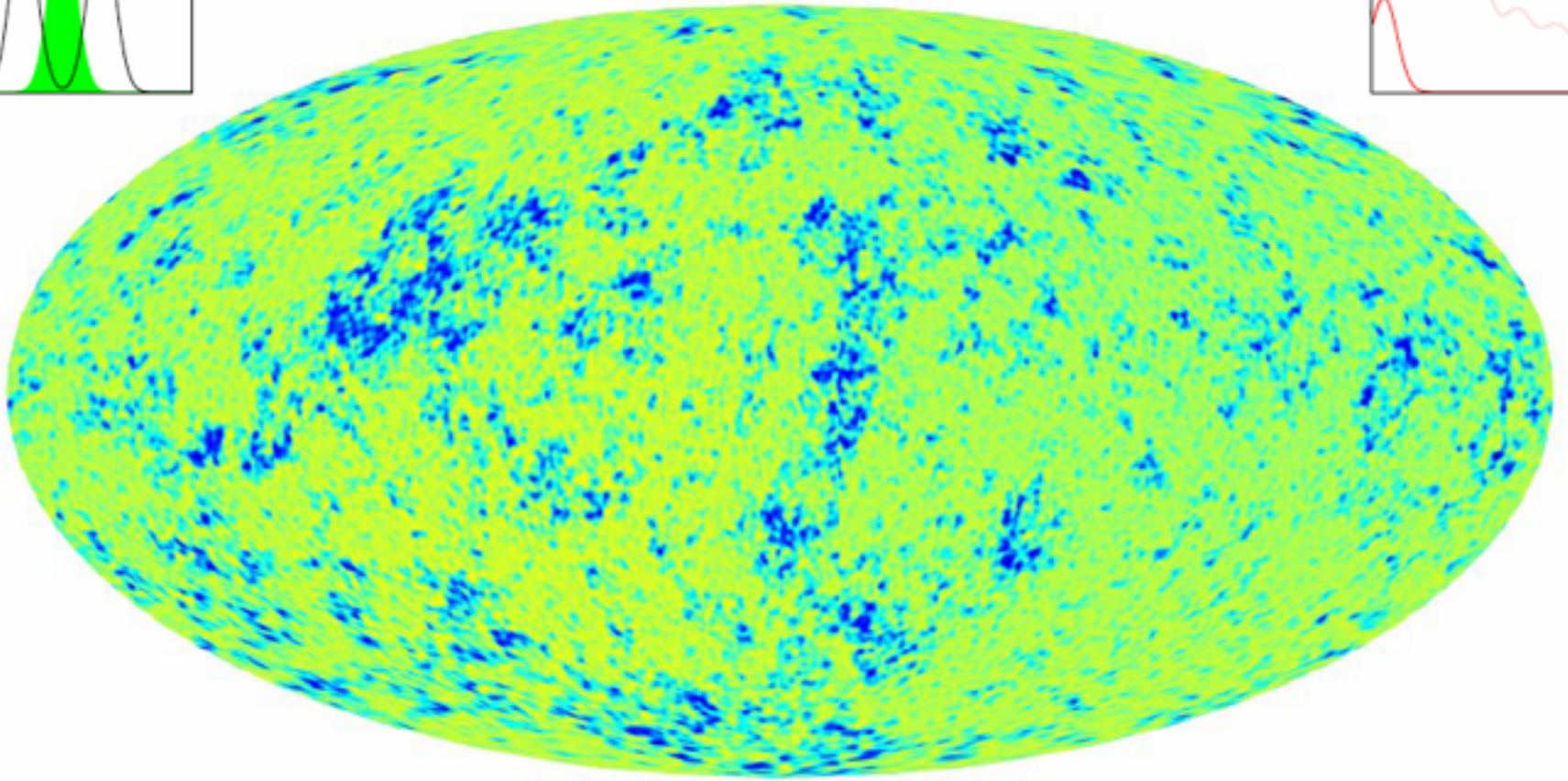
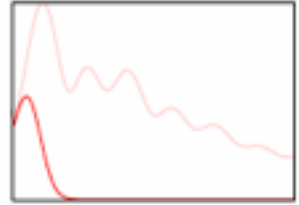
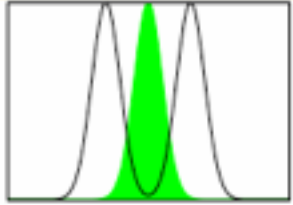
Bond, Kofman, Prokushkin, Vaudrevange 2007, Roulette Inflation with Kahler Moduli and their Axions

Neil Barnaby, Bond, Zhiqi Huang, Kofman, hep-th/0909.0503, Preheating after Modular Inflation

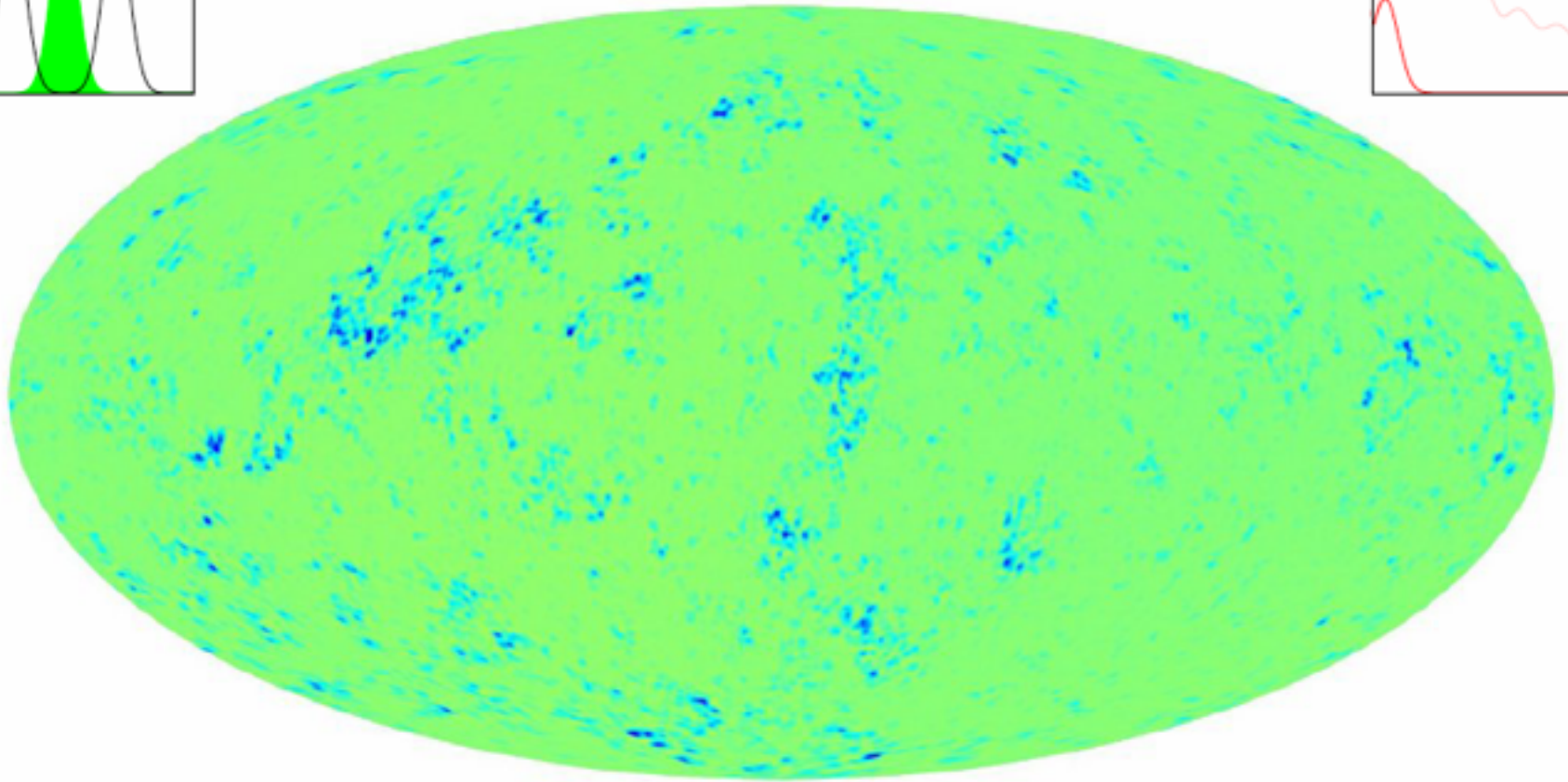
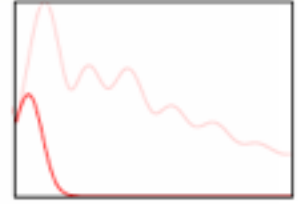
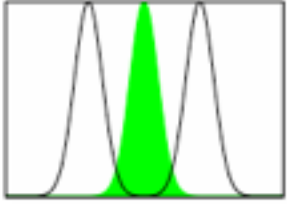




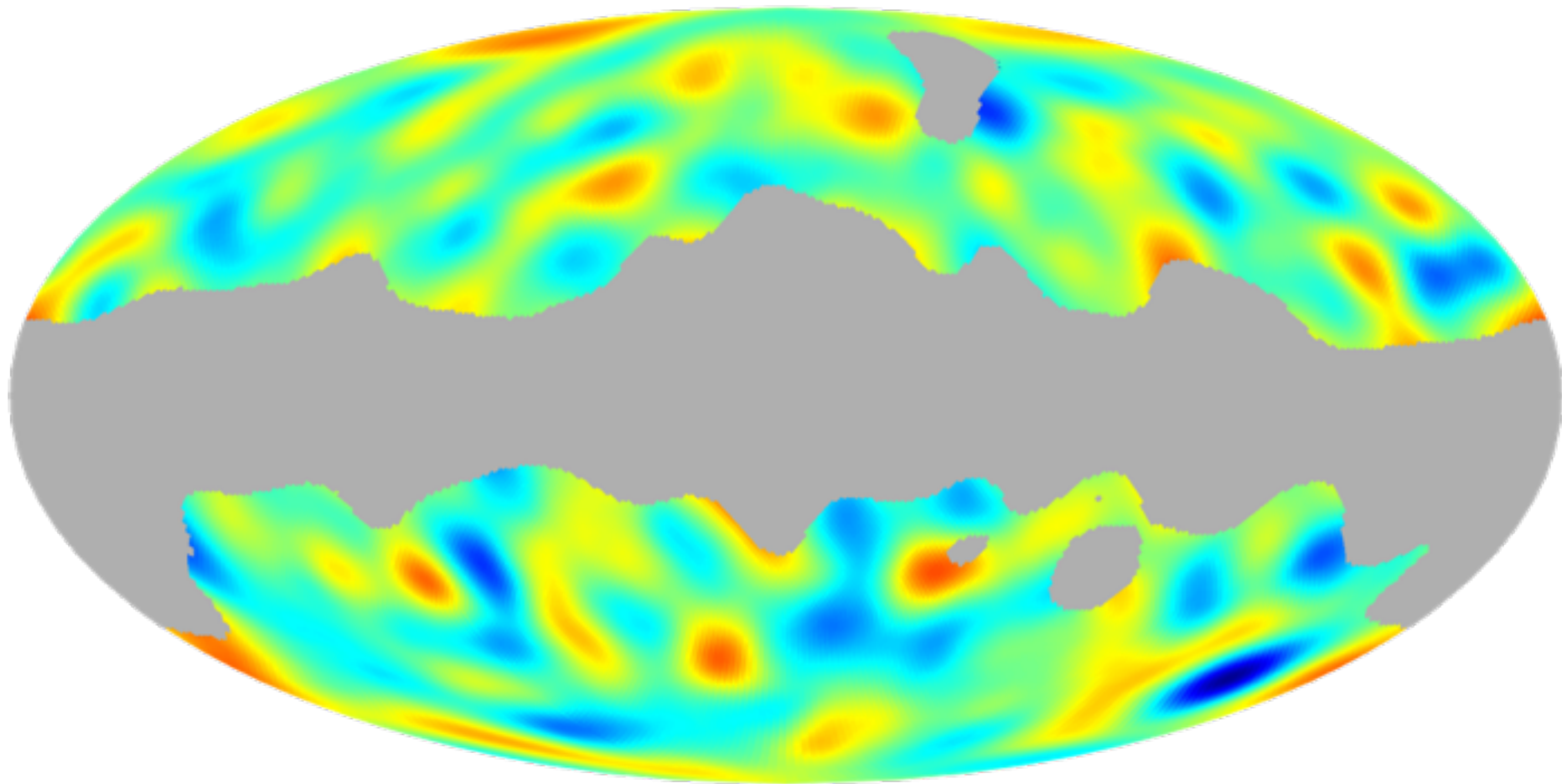






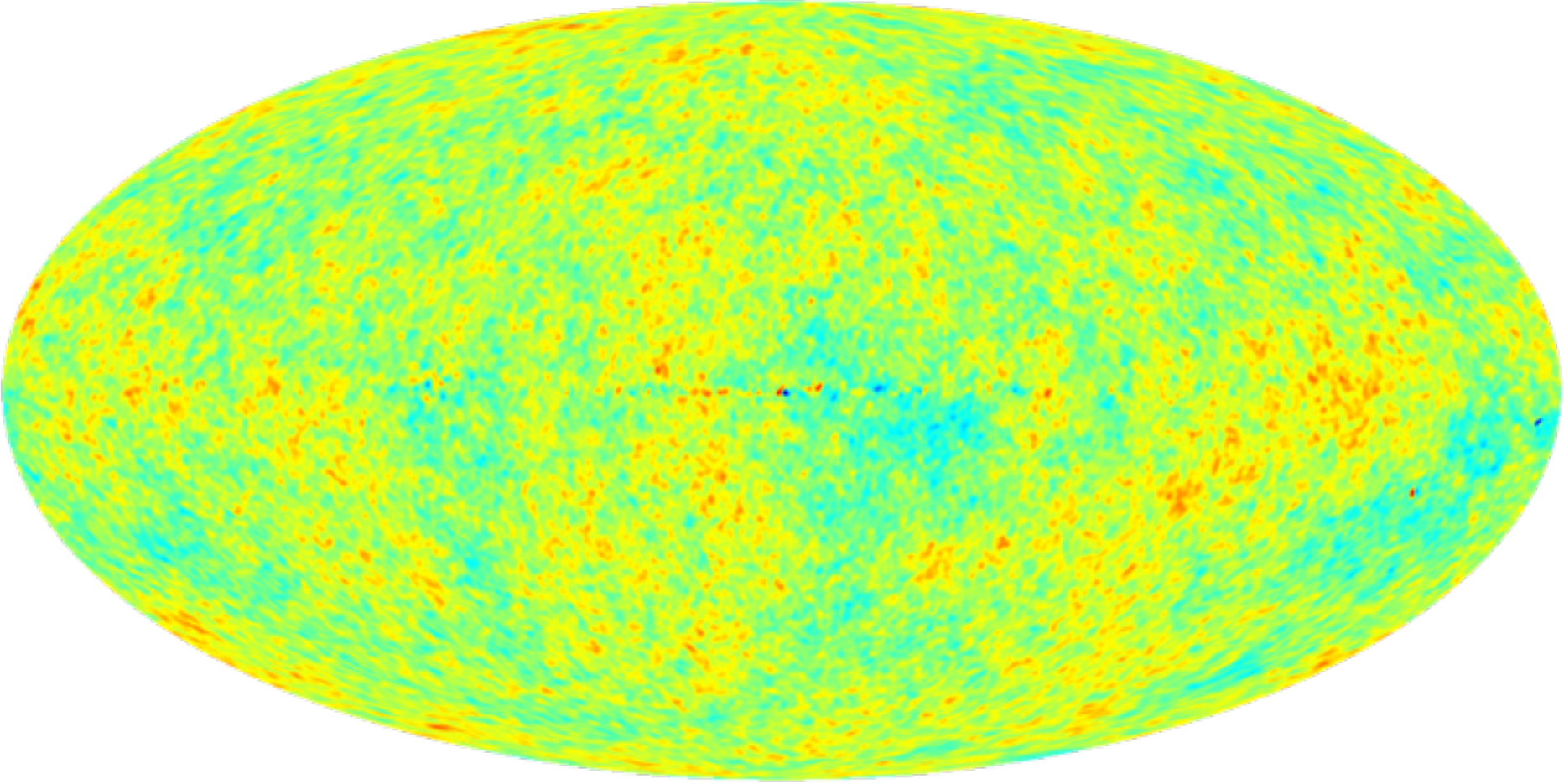


the WMAP Cold Spot: Vielva, Martinez-Gonzalez, Barr, Sanz, Cayon 2004 wavelets in WMAP1, ... Cruz et al 07 in WMAP3, & in WMAP5: needlets, steerable wavelets:  $\sim 4.5\sigma$ , others  $\sim 3\sigma$ ; Zhang & Huterer 09, not as significant with other filters 20%



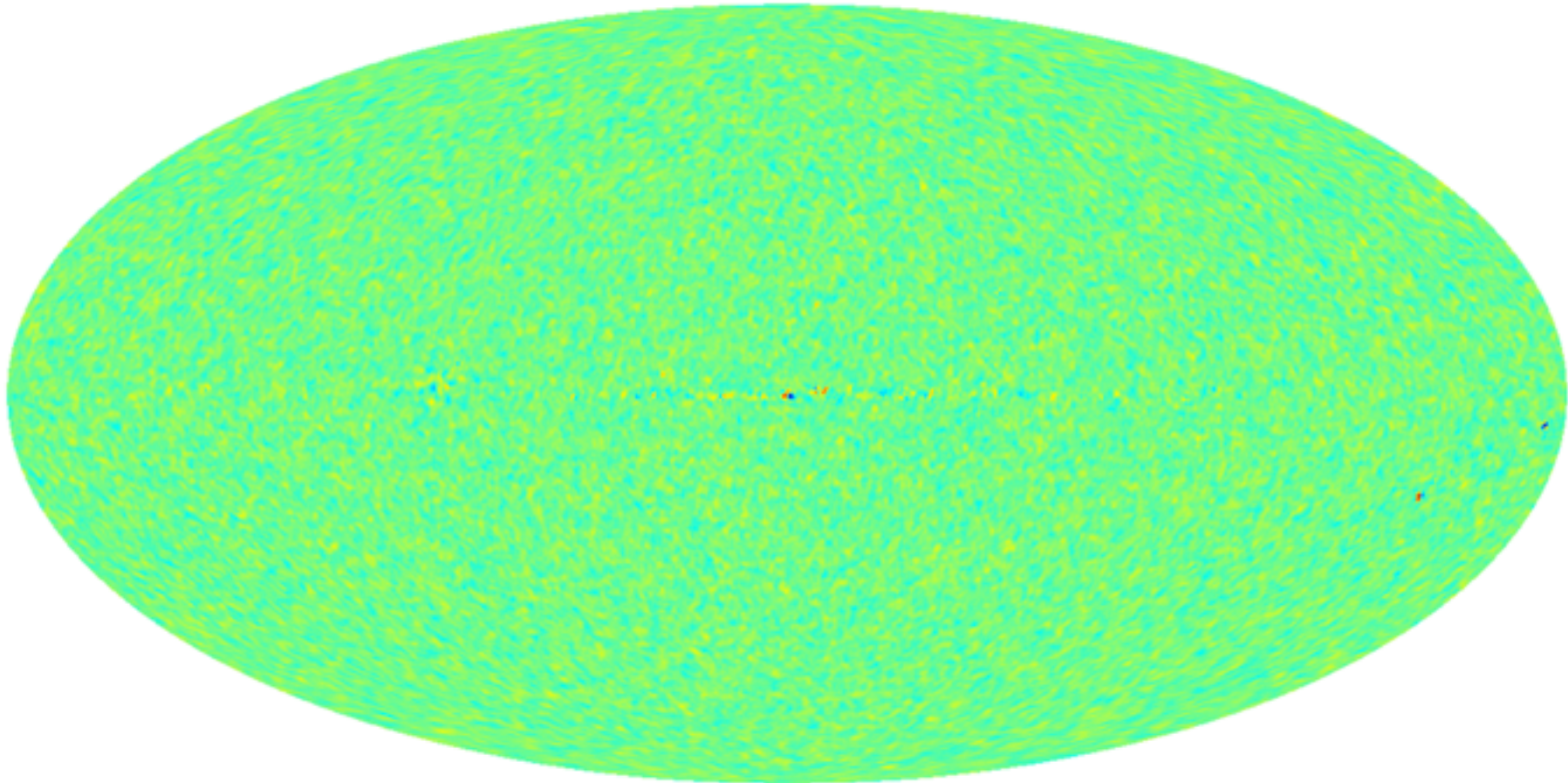
Bond, Frolov, Huang, Kofman, Nolta: Cold Spot testing: spherical SavitzkyGolay filters (compact polynomials) on pre-whitened WMAP5 data:  $-5.02\sigma$ , at 831 arcmin fwhm, 149 peaks, 1/1099 significance

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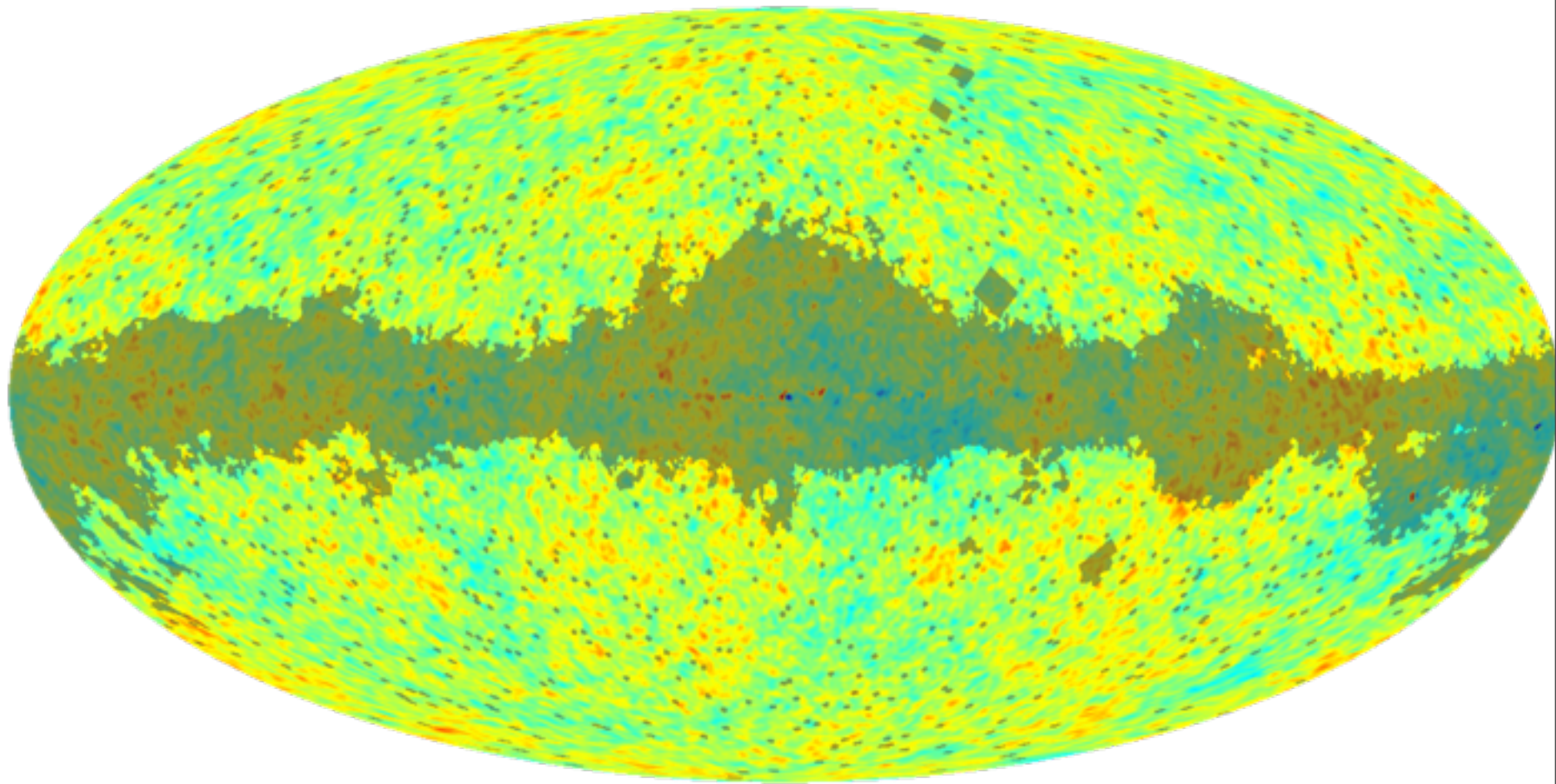
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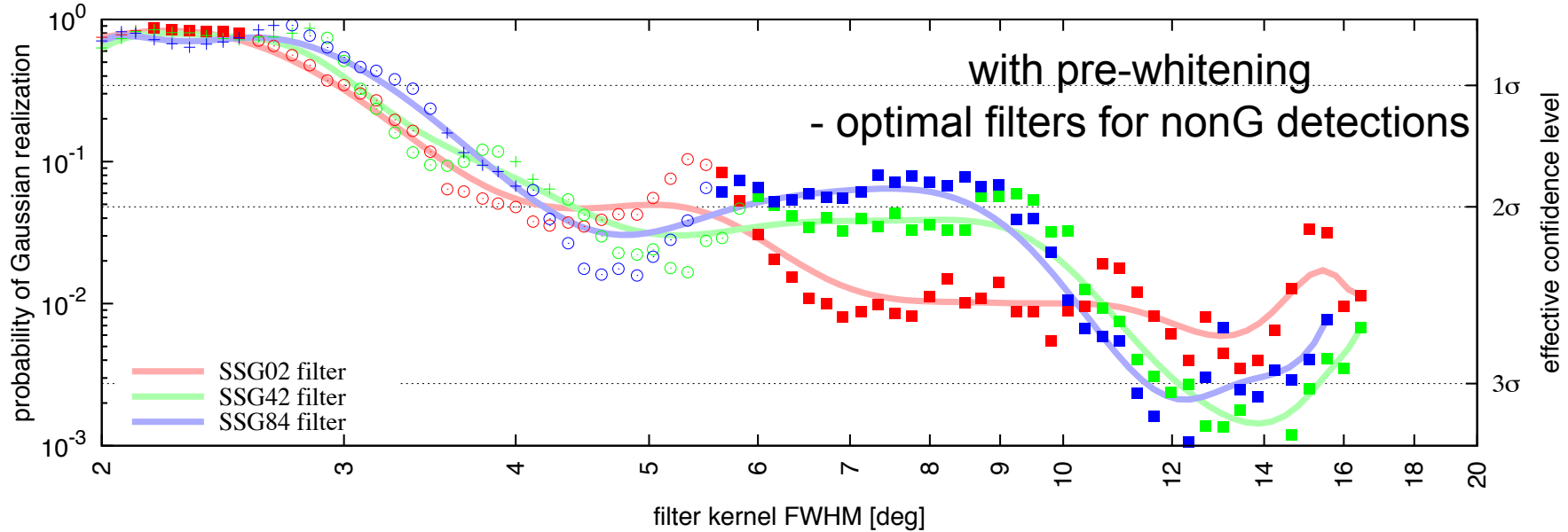
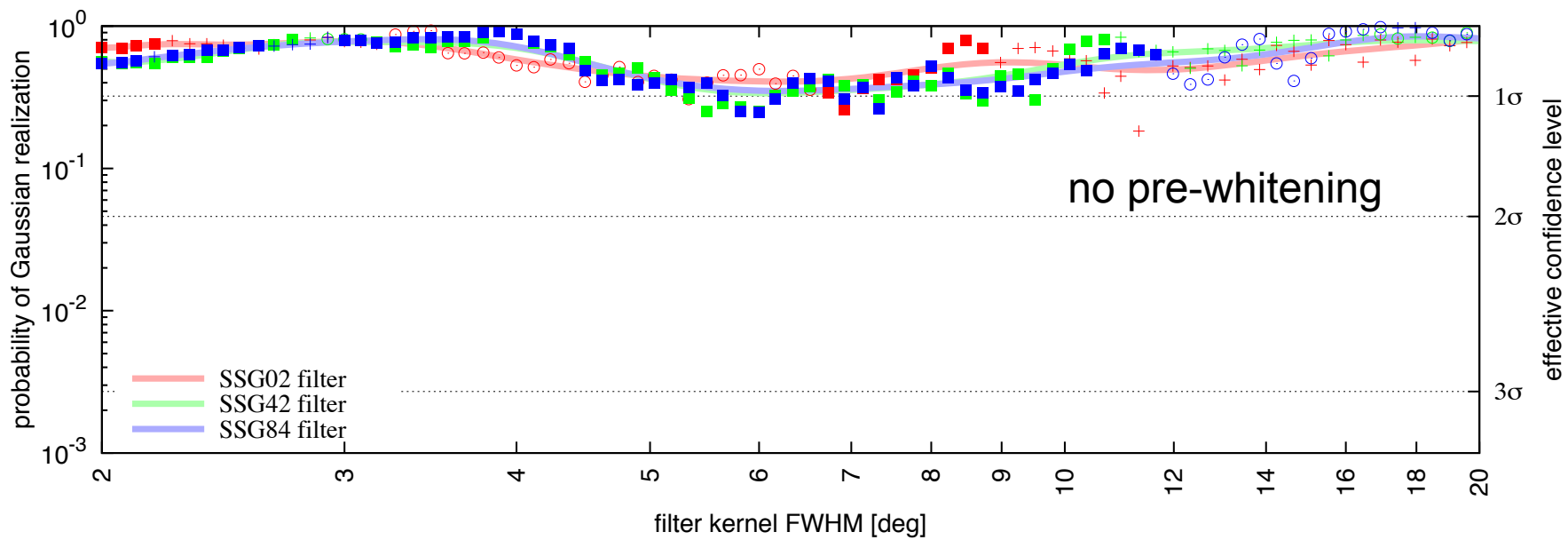
-0.665  +0.670

Bond, Frolov, Huang, Kofman, Nolta: Cold Spot testing: spherical SavitzkyGolay filters (compact polynomials) on pre-whitened WMAP5 data:  $-5.02\sigma$ , at 831 arcmin fwhm, 149 peaks, 1/1099 significance



-0.703  +0.531

**Bond, Frolov, Huang, Kofman, Nolta: Cold Spot testing: spherical SavitzkyGolay filters (compact polynomials) on pre-whitened WMAP5 data:  $-5.02\sigma$ , at 831 arcmin fwhm, 149 peaks, 1/1099 significance**



## November 2009 data

**Cosmic Microwave Background (CMB):** WMAP5yr (09), Acbar (09), QUAD (09), BICEP (09), CBI (08), Boomerang (06), DASI (05), VSA (04), MAXIMA (00)

**Type Ia Supernova (SN):** LOWZ + SDSS + ESSENCE + SNLS1yr + HST (Kessler et al 09) (**soon will + SNLS3yr**)

**Weak Lensing (WL):** COSMOS + CFHTLS-wide + RCS + VIRMOS + GaBoDS (Massey et al 07, Lesgourgues et al 07, Benjamin et al 07)

**Large Scale Structure (LSS):** SDSS-DR7 LRG (Reid et al 09)

**Lya Forest (Lya):** SDSS Lya (McDonald et al 05, 06)

**Others:** HST constraint on Hubble parameter (Riess et al 09); Cluster x-ray gas mass fraction (Allen et al 08)

## COSMOMC plug-ins (Zhiqi Huang)

### Decaying dark matter

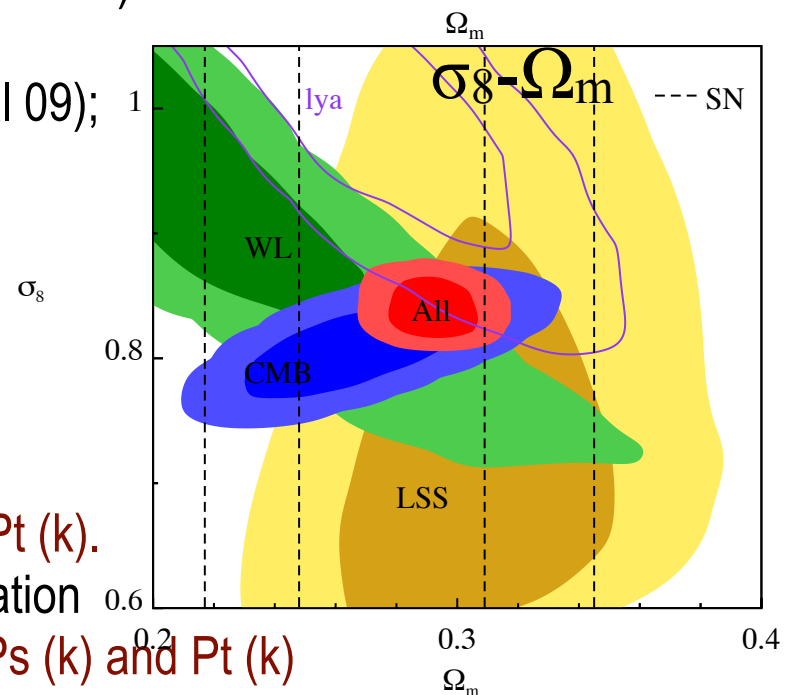
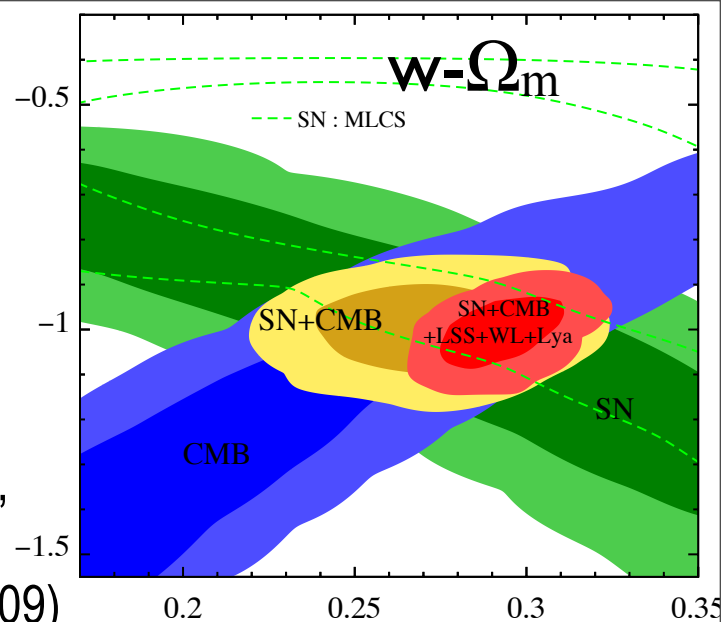
CMB, WL, SN, BAO mock data simulator

arbitrary Primordial Power spectra functions  $P_s(k)$  and  $P_t(k)$ .

full  $P_s(k)$  &  $P_t(k)$  integrator for arbitrary single-field inflation

automatic adjust  $L, k$  interpolations for more oscillatory  $P_s(k)$  and  $P_t(k)$

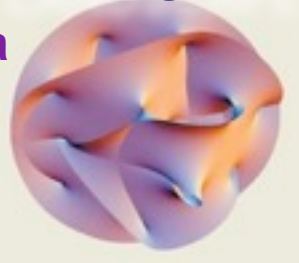
Dark energy equation of state: arbitrary  $w(z)$ , with built-in analytic quintessence/phantom parametrization.



**Old view:** Theory prior = delta function of THE correct one and only theory

**New:** Theory prior = probability distribution of late-flows on an energy LANDSCAPE

6/7 tiny extra dimensions



1980

$R^2$ -inflation

Old Inflation

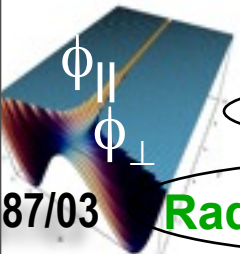
Chaotic inflation

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87/03

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Extended inflation

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Hybrid inflation

KLS94 preheating

SUSY F-term inflation

SUSY D-term inflation

Assisted inflation

Brane inflation

2000

SUSY P-term inflation

Super-natural Inflation

K-flation

2003 KKL

N-flation

D3,D7 brane inflation

DBI inflation

ekpyrotic/  
cyclic

moving brane separations

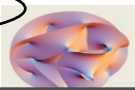
Racetrack inflation

Tachyon inflation

Warped Brane inflation

moduli fields

monodromy



Roulette inflation Kahler moduli/axion

fiber inflation



# INFLATION THEN

“standard inflation space”:  $n_s$   $dn_s/d\ln k$   $r$  @k-pivots

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Smoothly broken scale invariance  
by nearly uniform braking (standard  
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(stringy cosmology)  $r < 10^{-10}$

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*monodromy & fiber inflation give larger  $r$*

**current constraints on  $r$  (95%CL) - prior sensitive**

**$r < 0.16$  (no running, all data sets)**

**$r < 0.32$  (no running, CMB-only data sets)**

**$r < 0.27$  (with running, all data sets)**

**very early U**

early to middle to now U

**very late U**

**inflation**

*string theory/landscape/higher dimensions*

**dark energy**

$V_{\text{eff}}(\psi_{\text{inf}})$  ? partial shape reconstruction  
 $K_{\text{eff}}(\psi_{\text{inf}})$  ?

reconstruct gradient  
 $1+W_0 = -0.0 \pm 0.06$

$V_{\text{eff}}(\psi_{\text{inf}})$  ?  
 $K_{\text{eff}}(\psi_{\text{inf}})$  ?

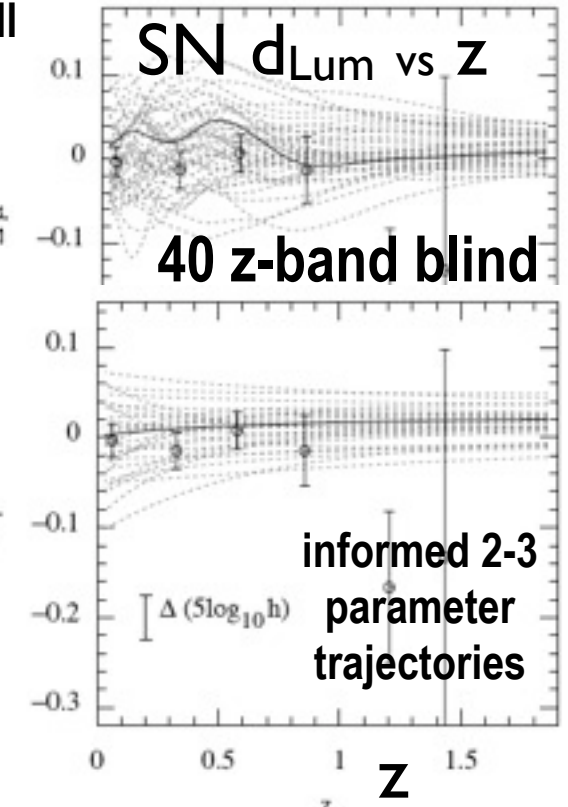
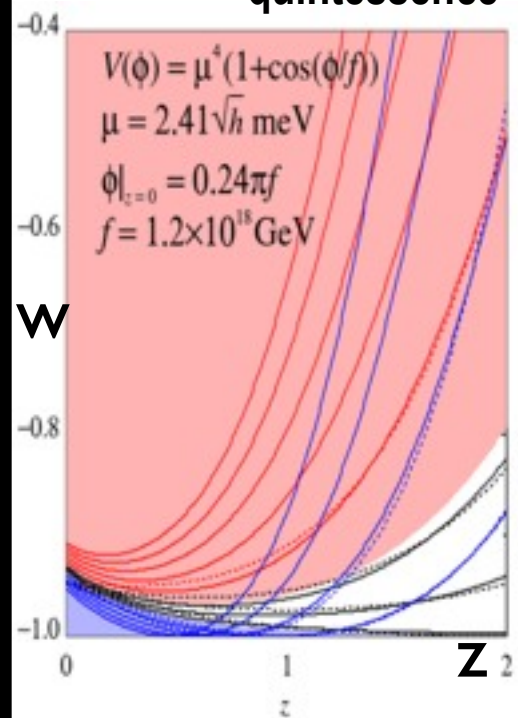
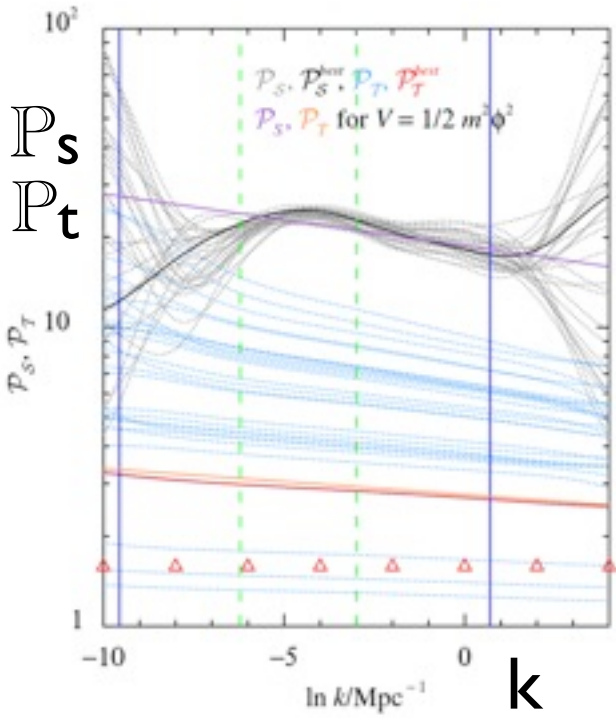
trajectory probability  
 $-d \ln \rho_{\text{tot}} / d \ln a$  / 2  
 $= \mathcal{E}(k) = 1 + q, k \sim H a$

$\Rightarrow P_s, P_t$   
 $V_{\text{eff}}(k),$   
 $\psi_{\text{inf}}(k)$

trajectory probability  
 $-d \ln \rho_{\psi} / d \ln a$  / 2  $\Rightarrow$   
 $= \mathcal{E}_{\psi}(a) = (1+w)^{2/3}$

$\epsilon_V = (d \ln V / d \psi)^2 / 4$   
 @pivot  $a_{\text{eq}}$   $\epsilon_S$  yes  
 $d^2 \ln V / d \psi^2 / 4$  no

slow-to-moderate roll  
 quintessence



**Semi-blind phenomenology**: mode function expansions of  $lnP_s (lnk)$  &  $P_t (lnk)$ : generalized running via Chebyshev; nodal-point Cheb, splines, physical shapes @ knots

**Inflation functional Consistency** built in: solve  $P_s (lnk)$  &  $P_t (lnk)$  exactly for mode function expansions of possible acceleration histories  $\mathcal{E}(lnHa)$

*results depend on prior measure for expansion coefficients for current data, less so with CMB experiments targeting the B-mode of polarization*

*Reconstruction has been much explored over the years, since the 90s. recent examples:*

**Simple binning techniques**: Bridle et al 03; Hannestad 04; Bridges et al 06, 07; Spergel et al 07;

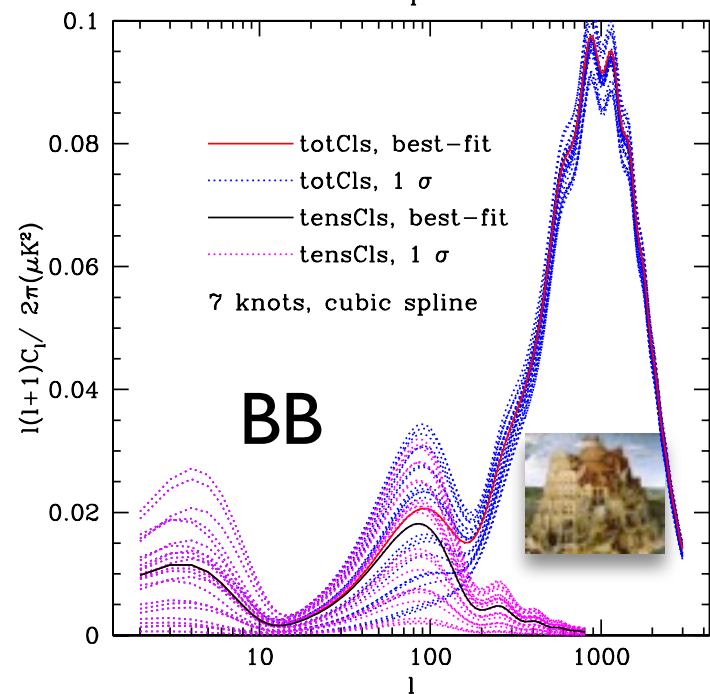
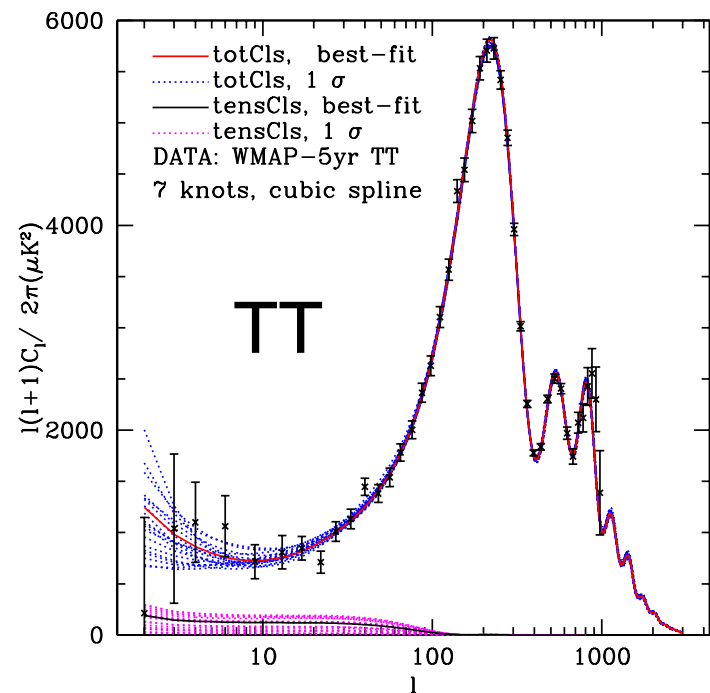
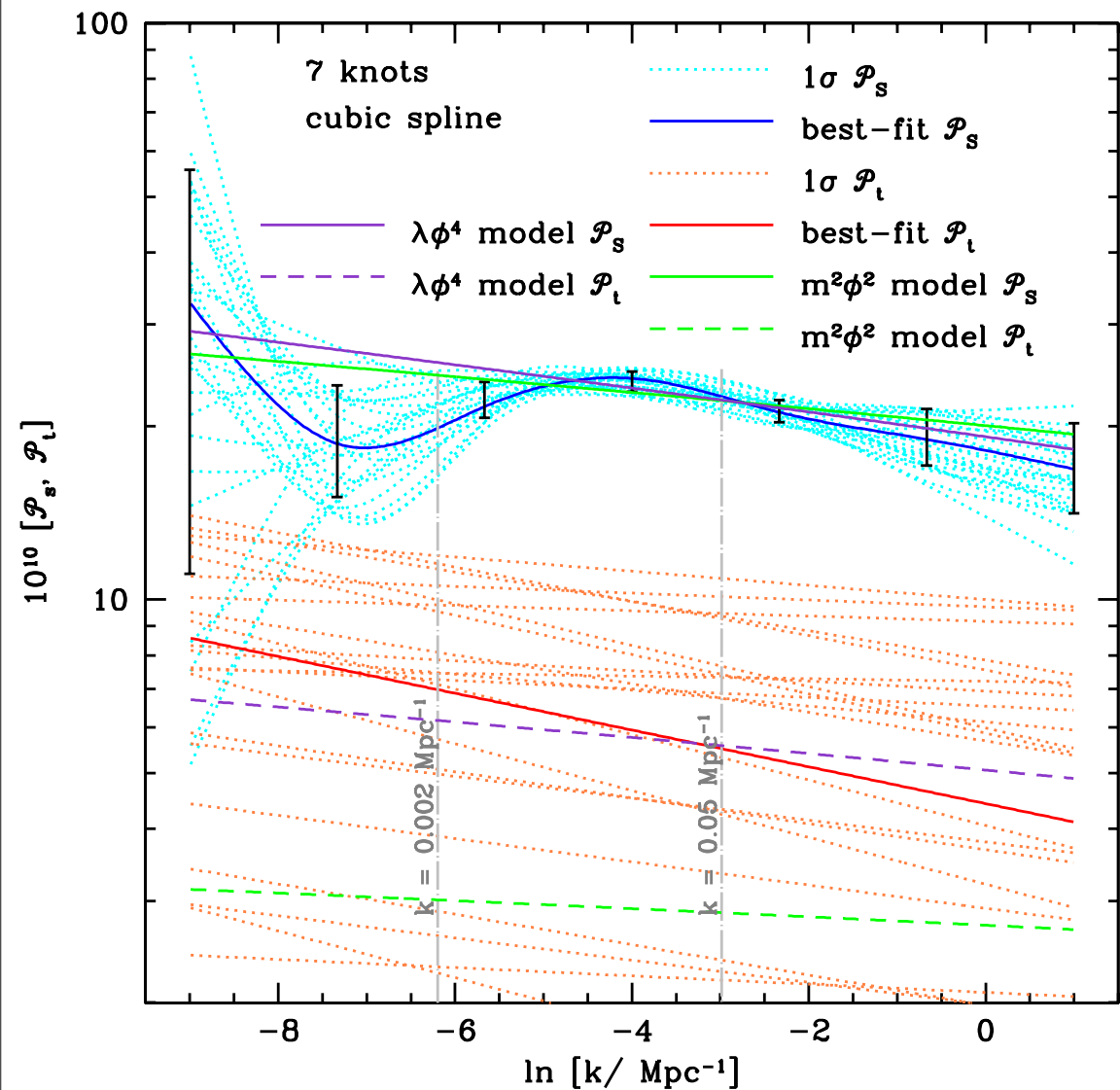
**Direct inversion**: Shafieloo et al 04,08; Kogo et al 04; Tocchini-Valentini et al 05 06; Nagata et al 08; Nicholson et al 09a,09b;

**Basis function expansion**: Mukherjee 05; Leach 06;

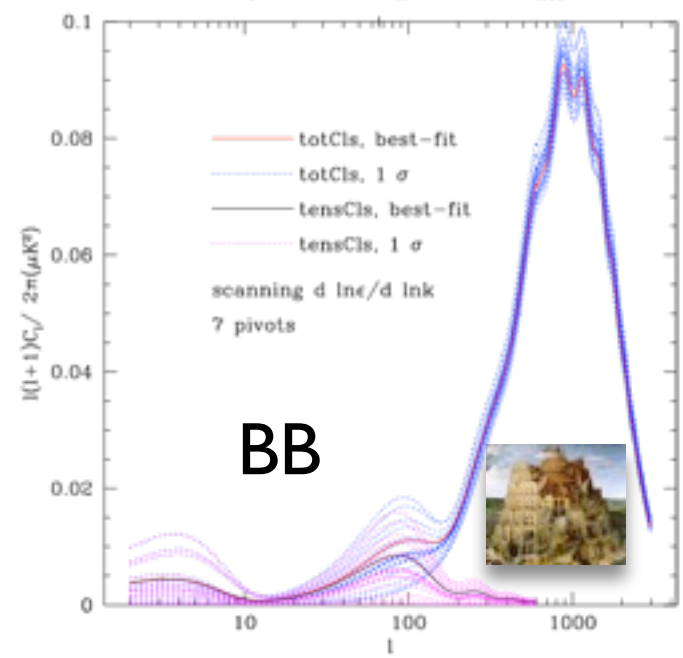
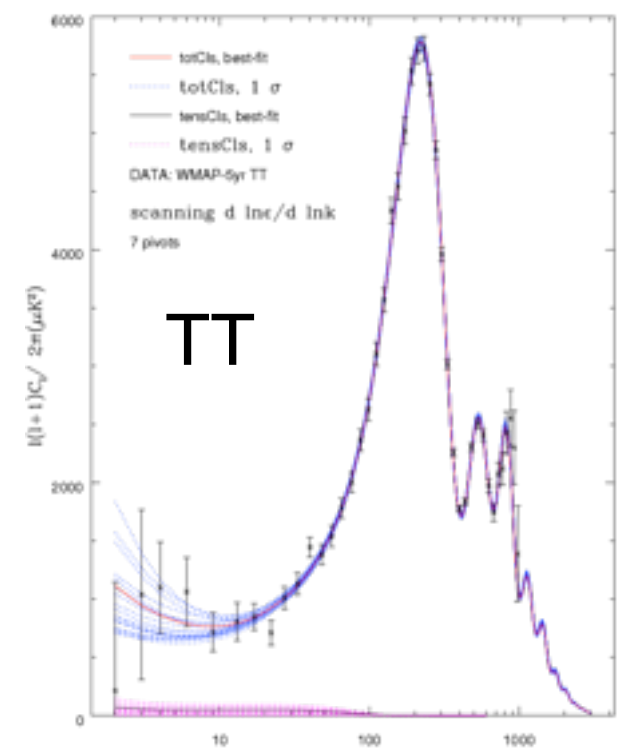
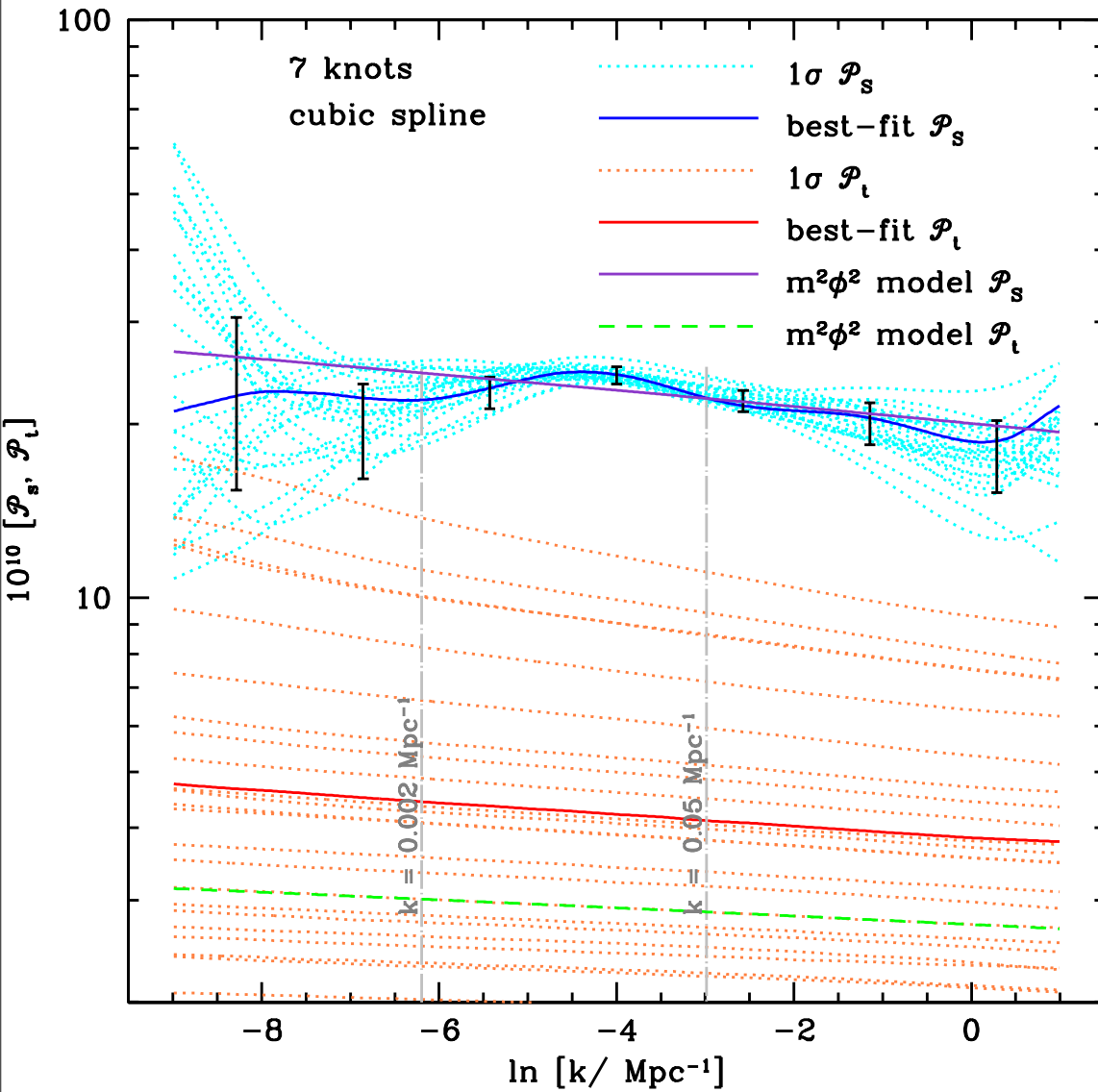
**Cubic spline interpolation**: Sealton et al 05; Peiris et al 08 09;

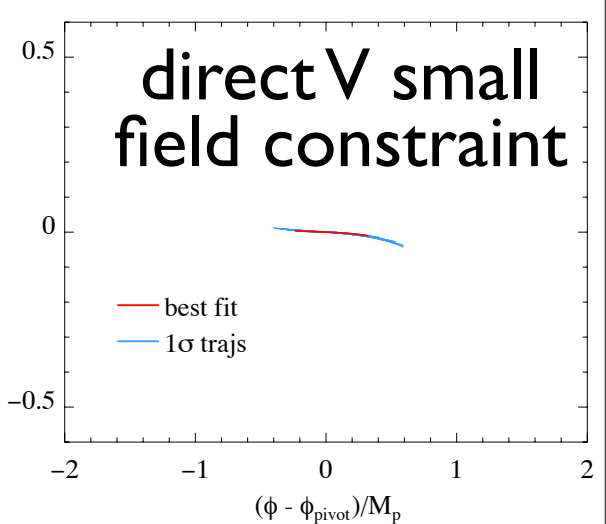
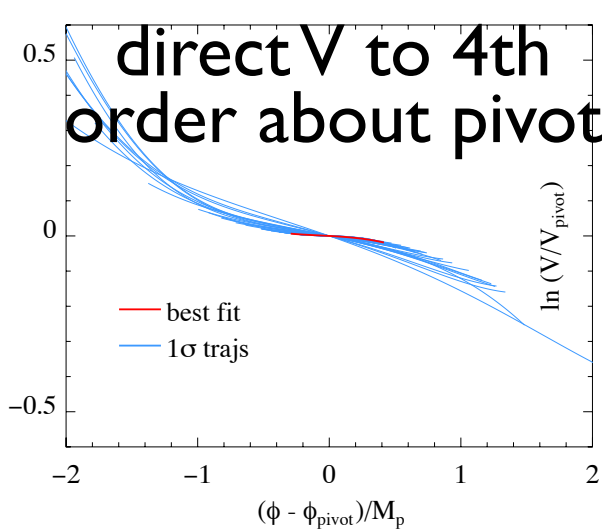
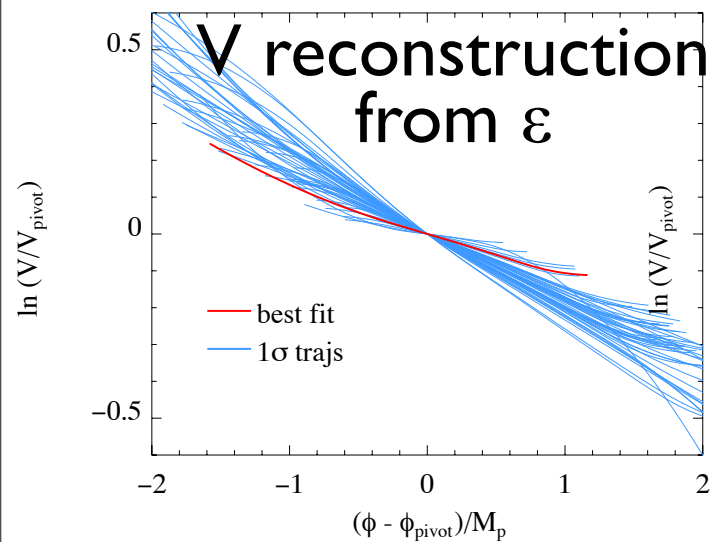
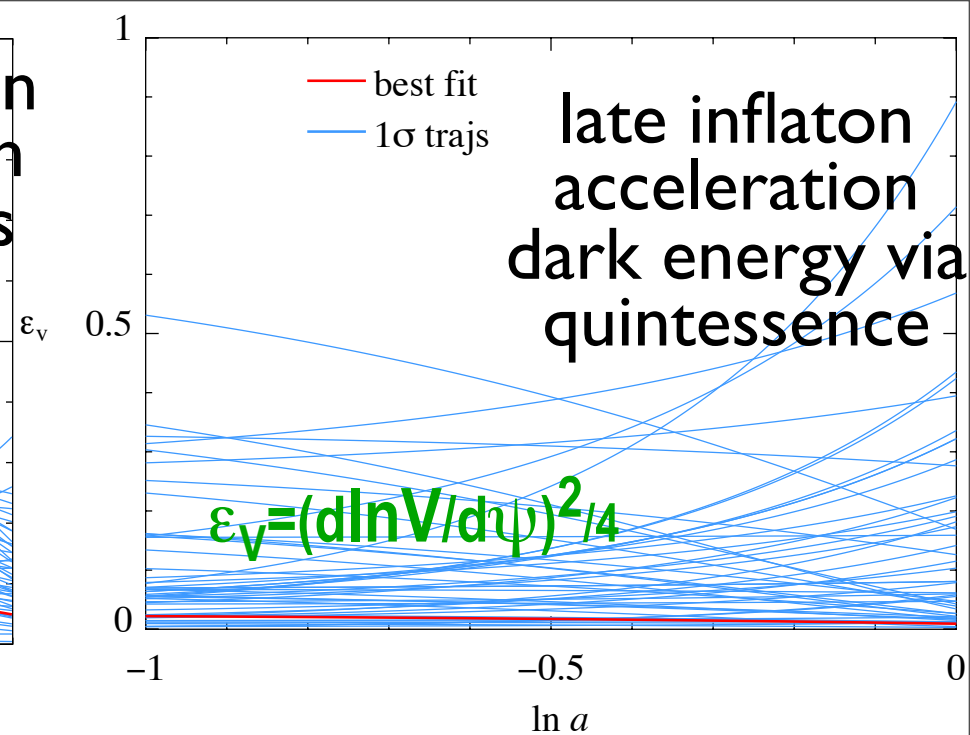
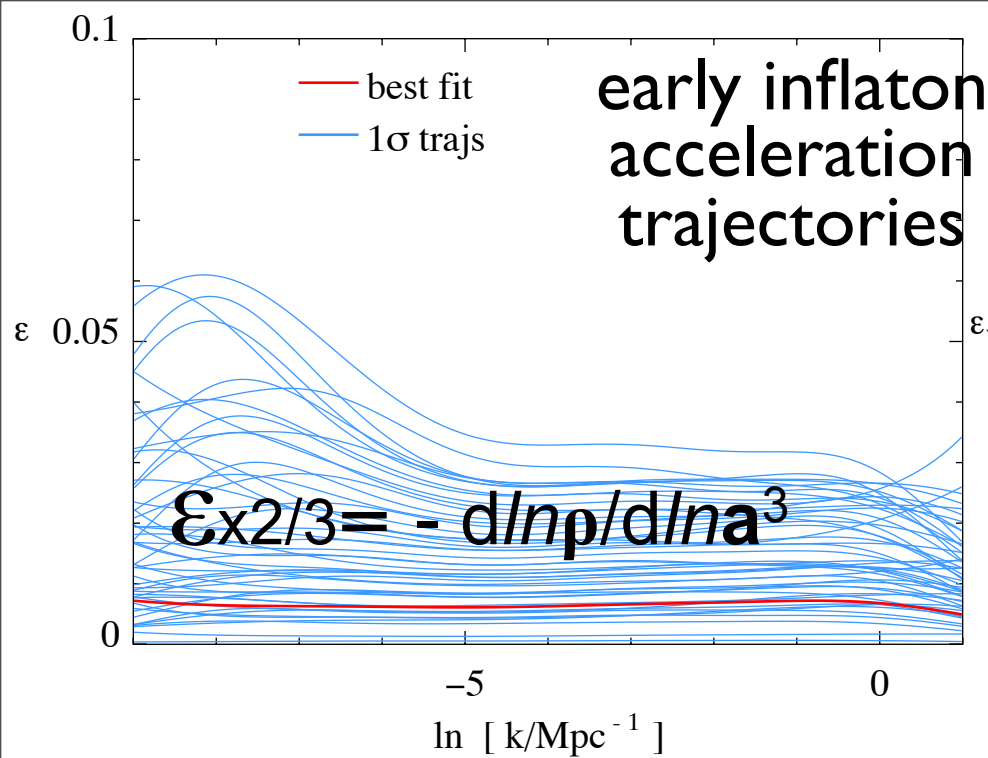
**Slow-roll reconstruction (flow equations)**: Peiris et al 03,06a,06b; Easter 06; Adshead et al 09;

*partially-blind scalar power trajectories & usual  $r$ - $n_t$  tensor - no consistency relation. Nov09 data*



# partially-blind acceleration trajectories obeying tensor/scalar consistency relation. Nov09 data





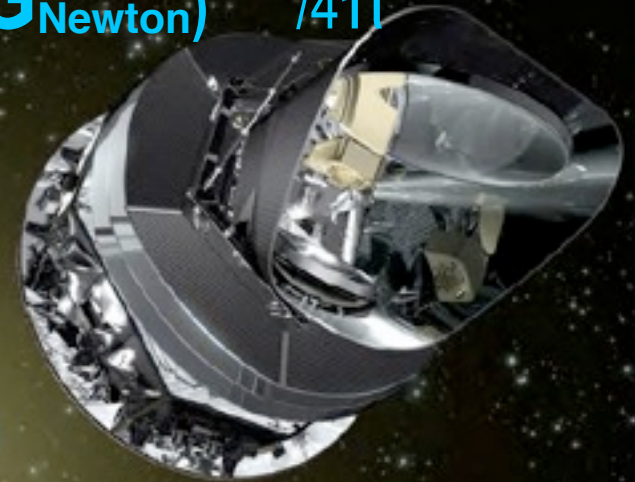
# Entering the Planck Era > May 14, 2009

*status A-OK, first all sky survey finishes Feb 2010; 5 in all*



**Launch May 14, 2009**  
**FrenchGuiana, @L2 early July,**  
**Survey Began Aug 09**

$$M_P = (ch/G_{\text{Newton}})^{1/2} / 4\pi$$



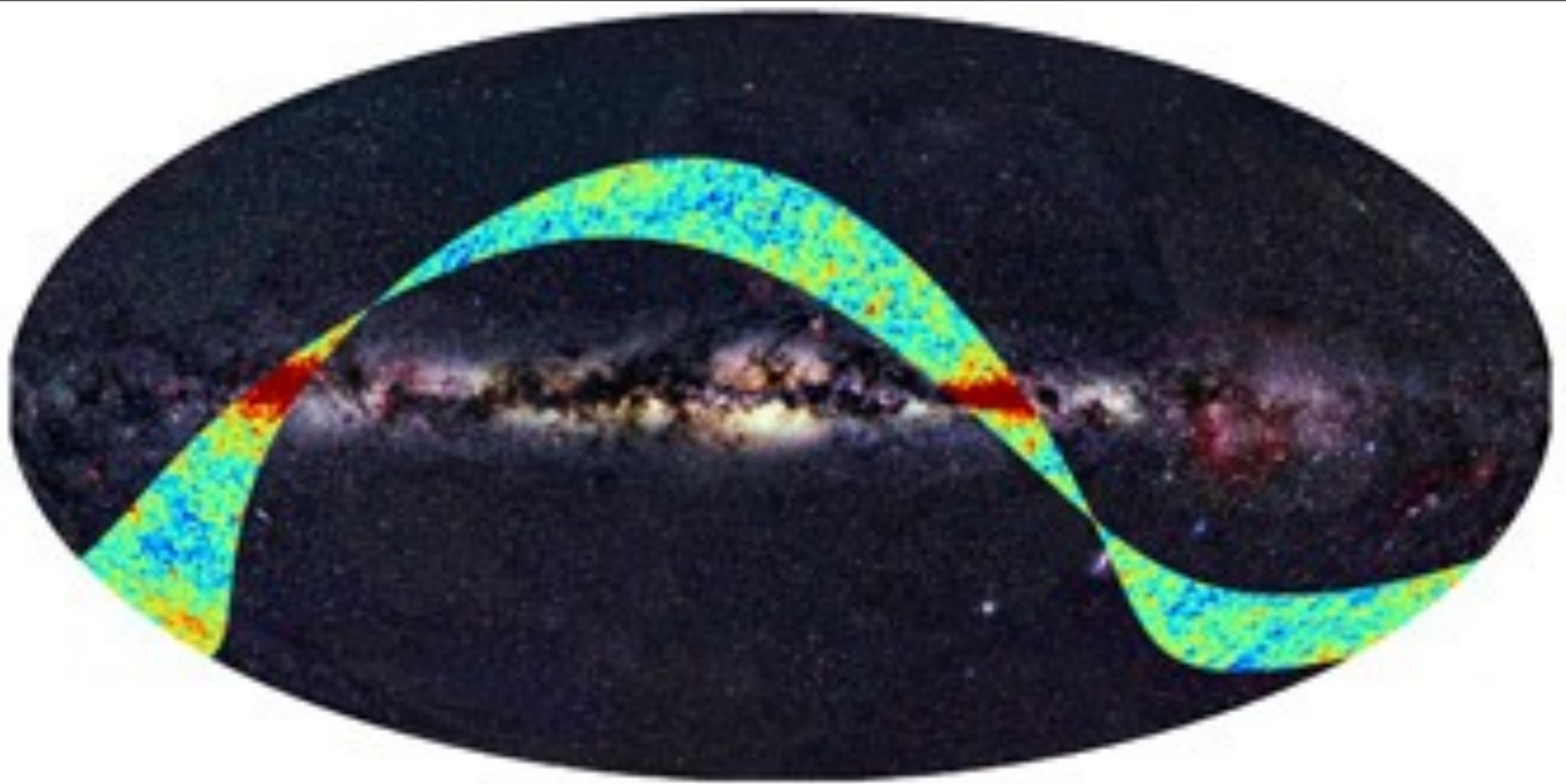
*Planck on Planck era physics: impact on early inflation & on late inflation (Dark Energy), aka mysteries of the vacuum*

**$n_s(k)$ , GW: Tensor(k)**

subdominant isocurvature, cosmic strings, textures,

***nonGaussian*  $F_{NL}(x)$**

ESA /NASA /CSA Toronto HFI QLA/KST, TA, ... Barth & Dick, Marc-Antoine Miville-Deschenes, Carrie MacTavish, Brendan Crill, Olivier Dore, Carlo Contaldi, Mike Nolta, Peter Martin, Francine Marleau, UBC LFI

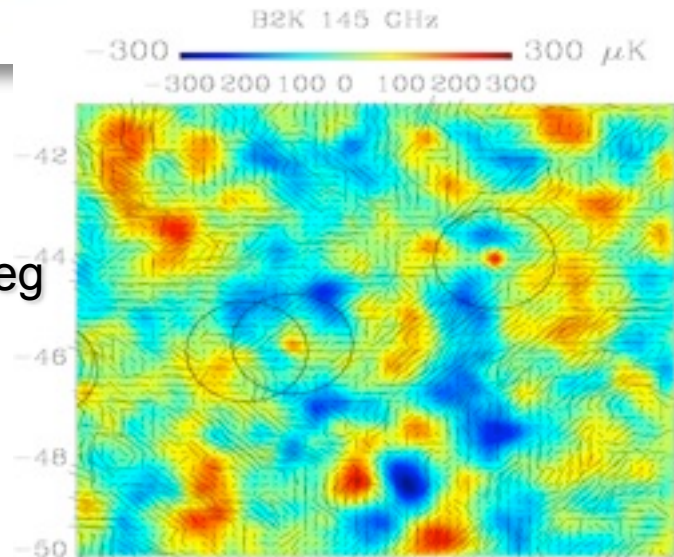


## Planck "First Light" Survey Aug 2009



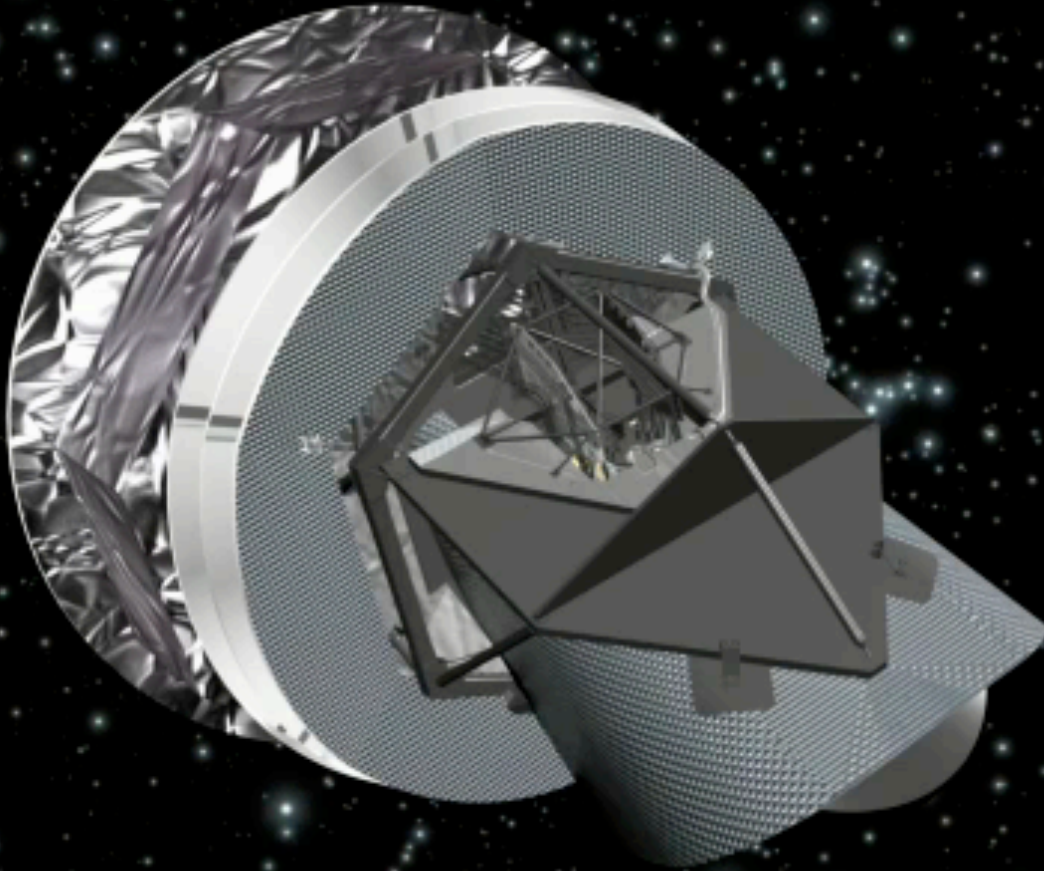
**BoomPol deep**  
**2003.1, Jul05, Dec09**  
 125 hours,  $f_{\text{sky}}=0.28\%$  115sq deg

**Planck is ~ as deep,  
 but all sky, with similar  
 bolometers (but more)  
 and better resolution**





# Planck 1st of 5 all Sky Surveys 09.7-10.1



# Future Forecasts

**CMB: Planck2.5yr**, using 3 channels (70GHz, 100GHz, 143GHz), *assuming 5% foreground residual (synchrotron + dust)*, fsky = .75, Lmax = 2500.

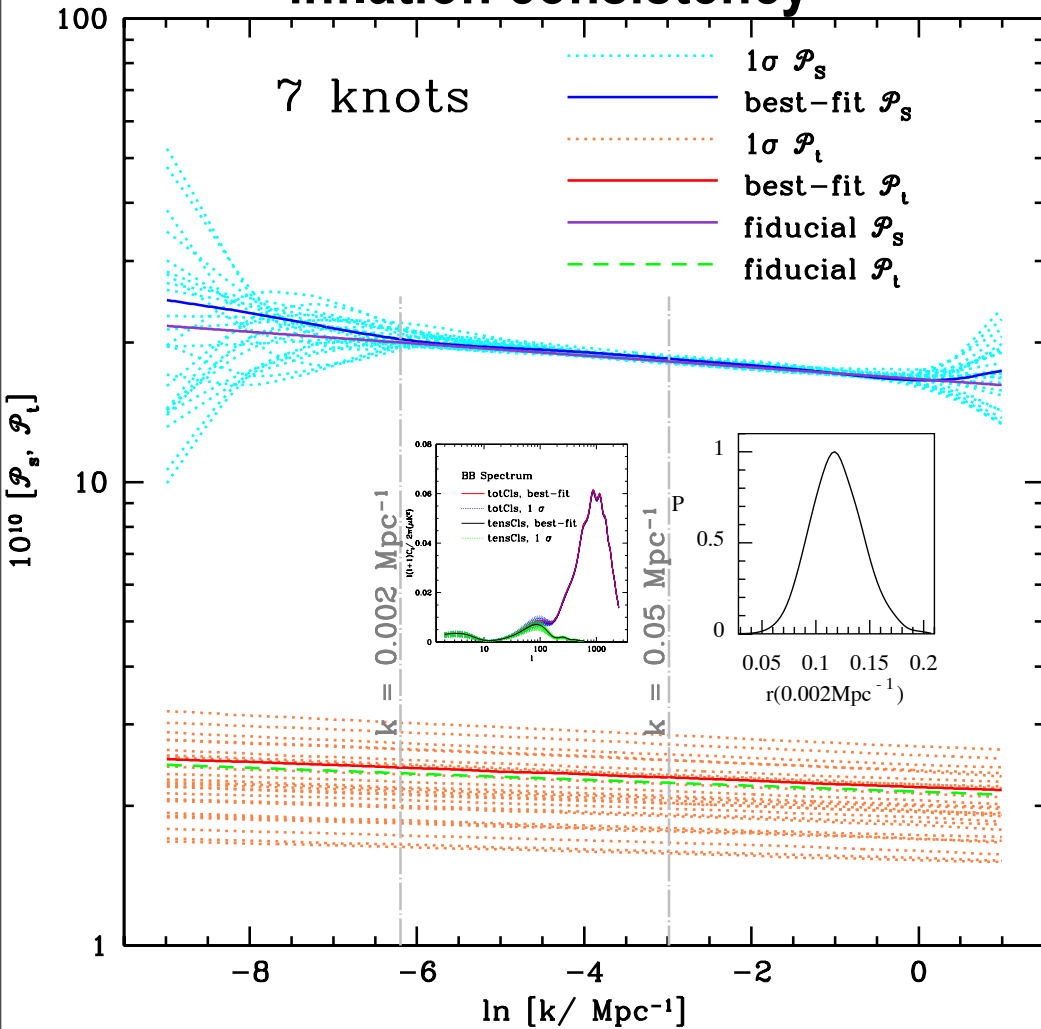
other future polarization experiments: **SPIDER**, EBEX, QUIET, KECK, ...  
**CMBPol**

**WL: DUNE-like weak lensing tomography**, 20000 sq deg, depth  $z \sim 1$ , 35 galaxies/arcmin<sup>2</sup>, two redshift bins, Lmax = 1500. → Euclid  
other proposed deep and wide WL surveys: JDEM, PanStarrs, LSST, ...

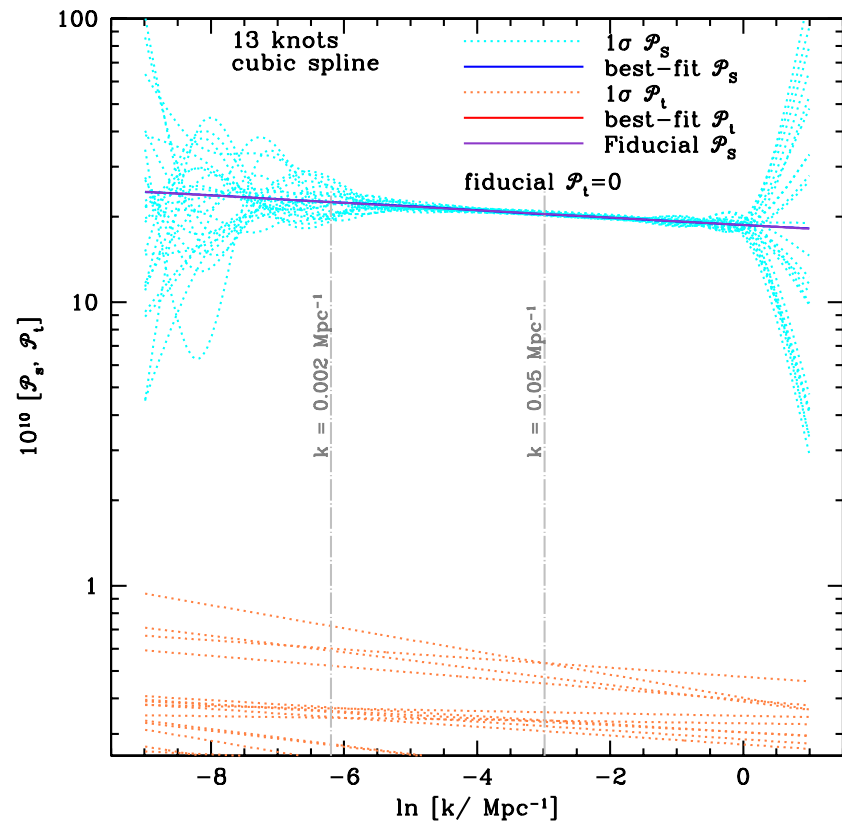
**SN: JDEM-like**, 500 LOWZ ( $z < 0.03$ ) + 2500 HIGHZ ( $0.03 < z < 1.7$ )  
other ongoing/future SN surveys: SNLS, SDSS, LSST ...

**BAO: JDEM**, 10000 degree<sup>2</sup>,  $0.5 < z < 2$ , 10 redshift bins  
other ongoing/future BAO surveys: WIGGLEZ, **CHIME**, BOSS, LSST, ...

# Planck2.5 forecast with inflation consistency



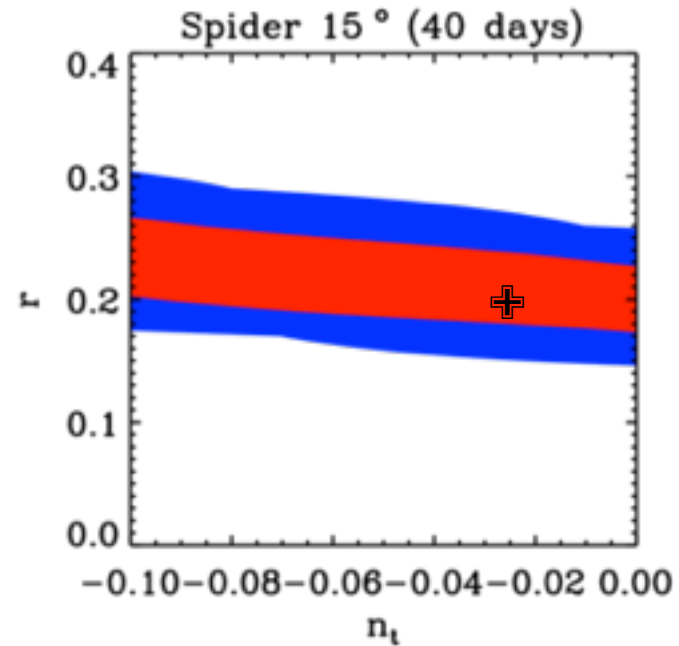
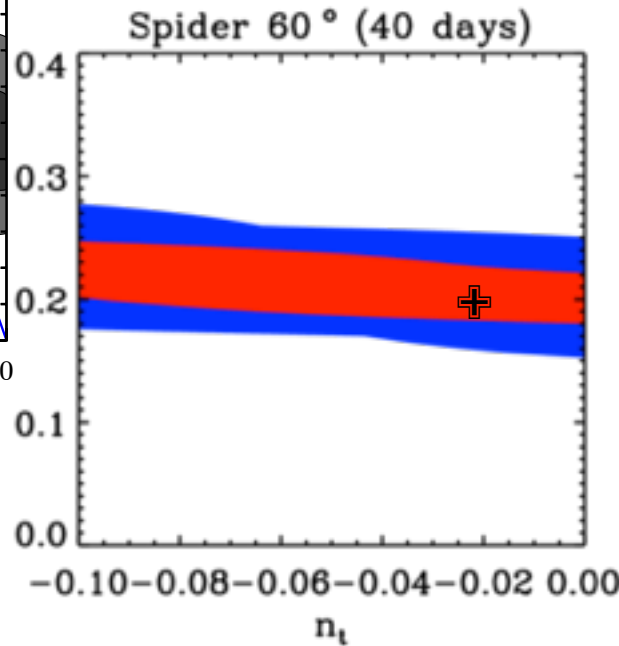
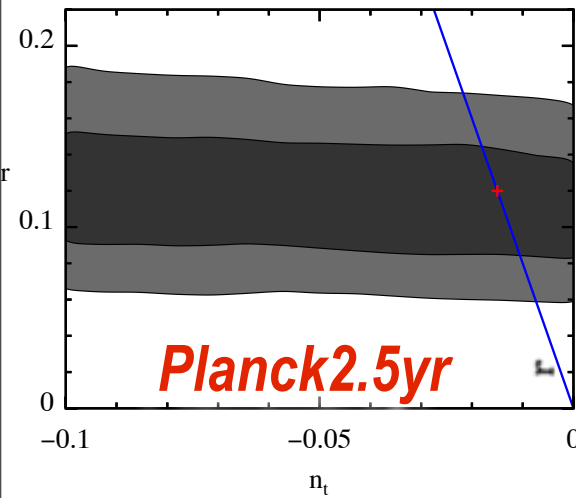
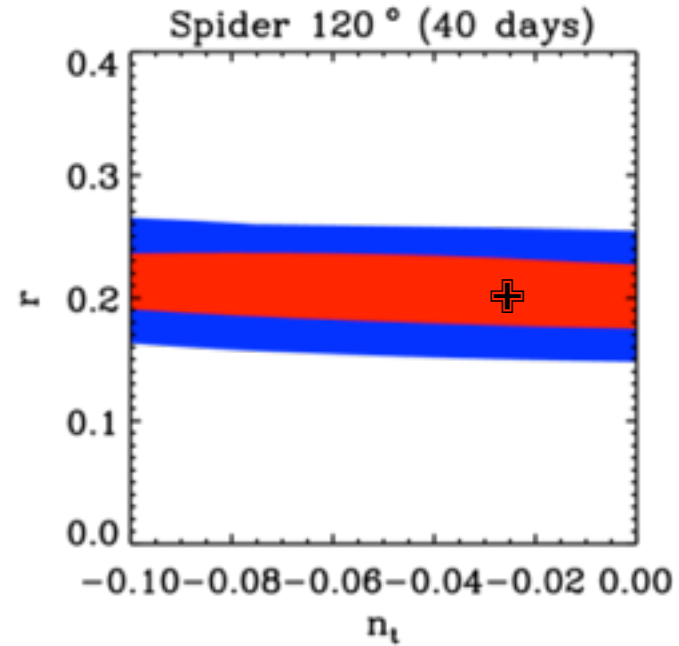
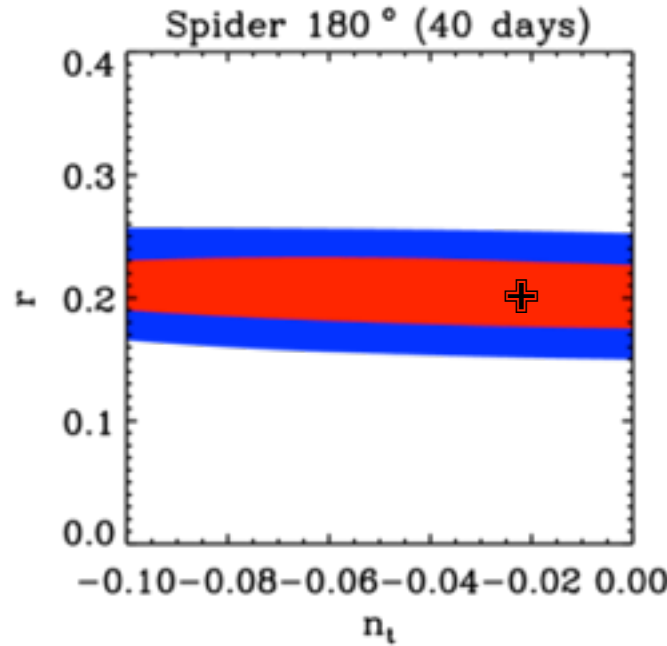
# Planck2.5 r=0 forecast for 13 knot semi-blind $\mathcal{P}_s + r\text{-}n_t$



$$r \approx -8n_t$$

poor  $n_t \Rightarrow$

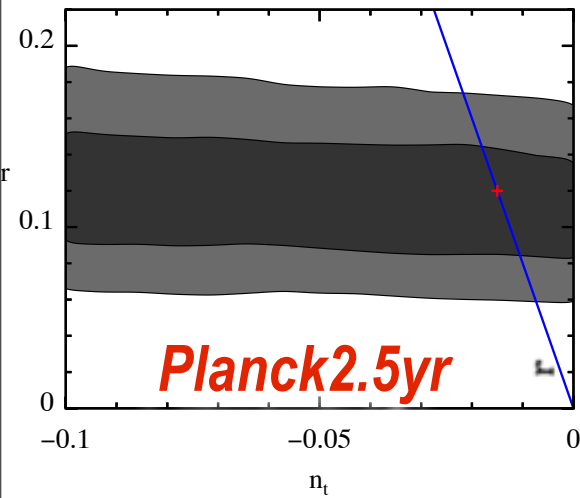
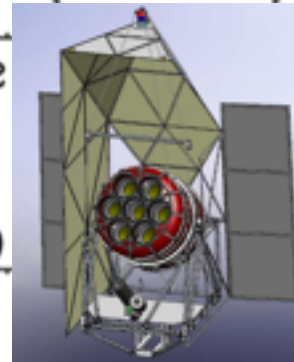
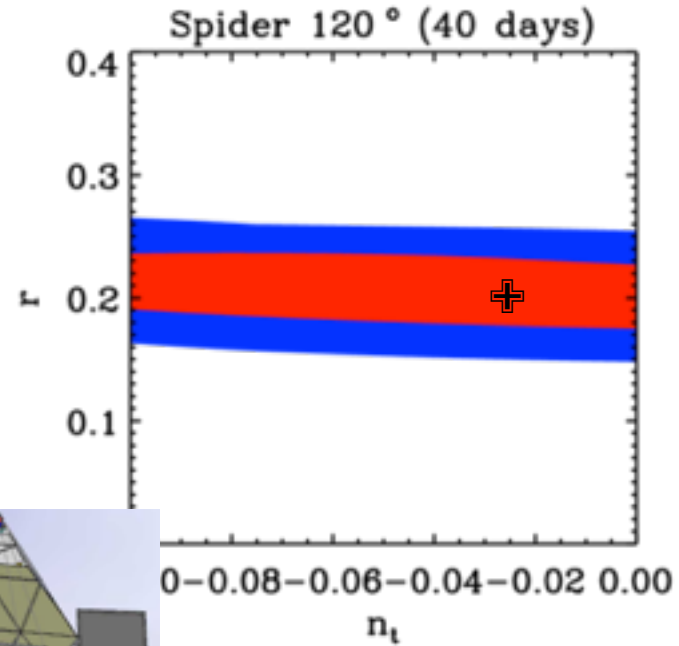
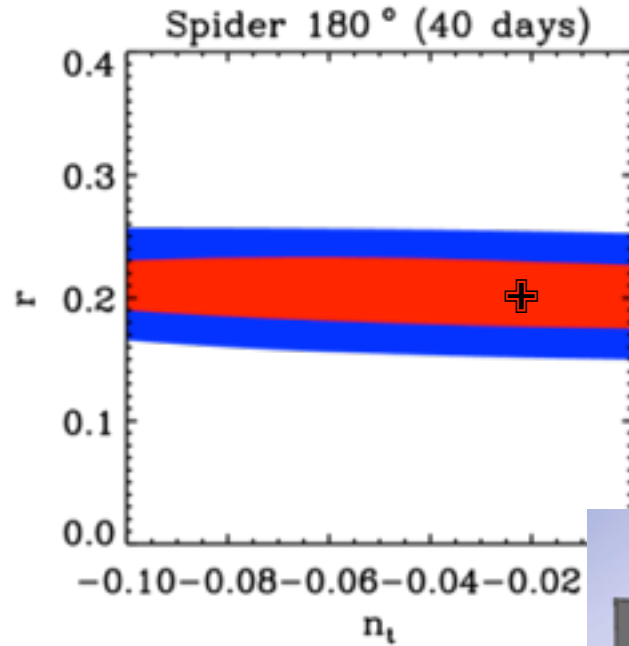
*inflation consistency cannot be checked with Spider or Planck2.5yr*



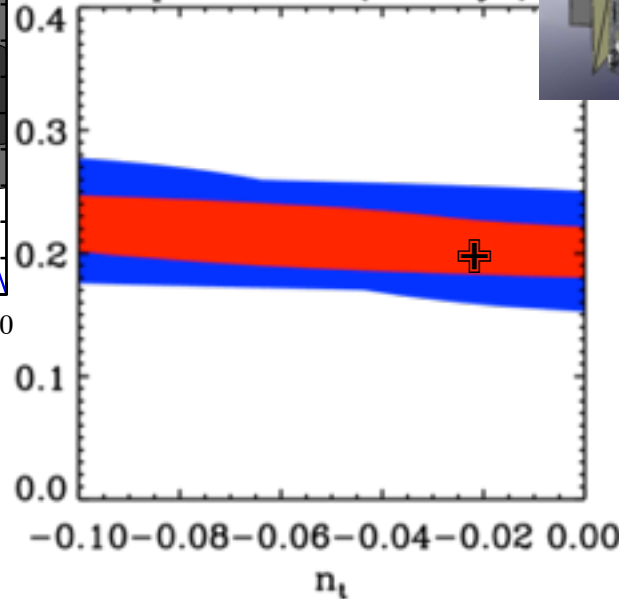
$$r \approx -8n_t$$

poor  $n_t \Rightarrow$

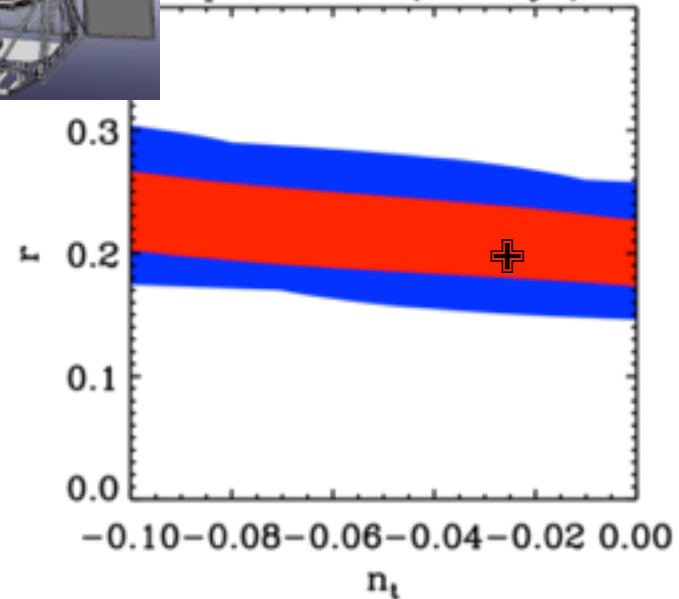
*inflation consistency cannot be checked with Spider or Planck2.5yr*



Spider 60° (40 days)



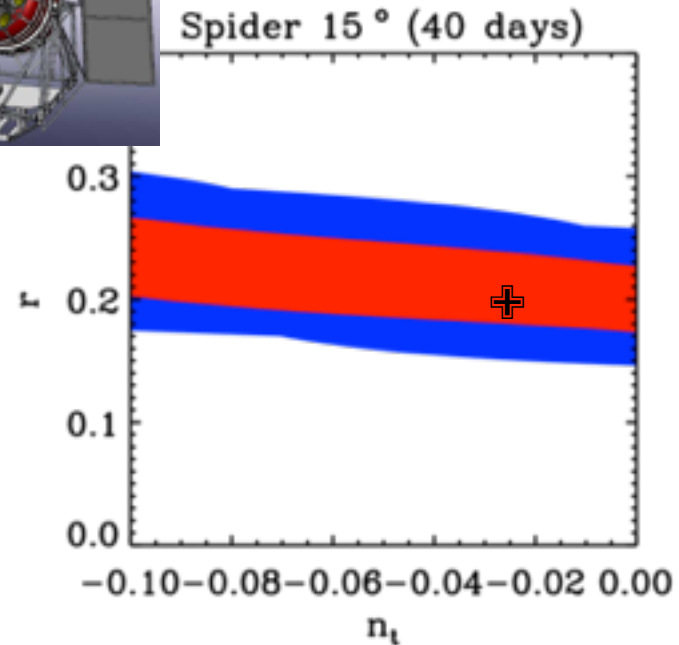
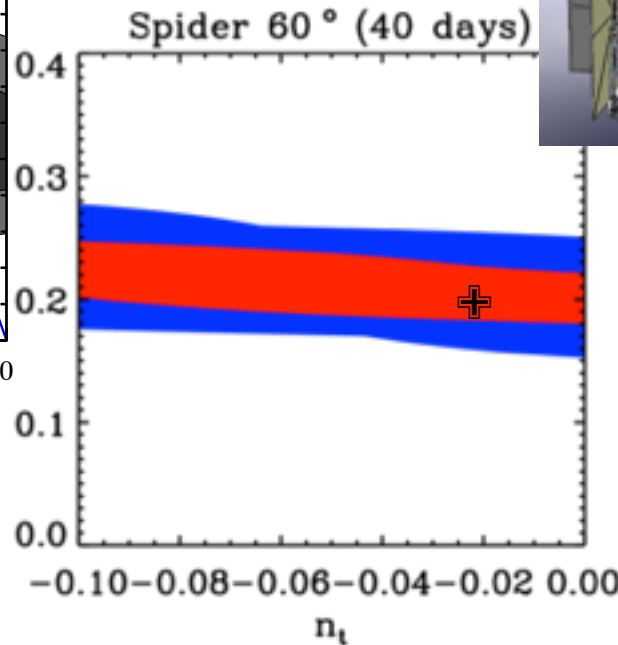
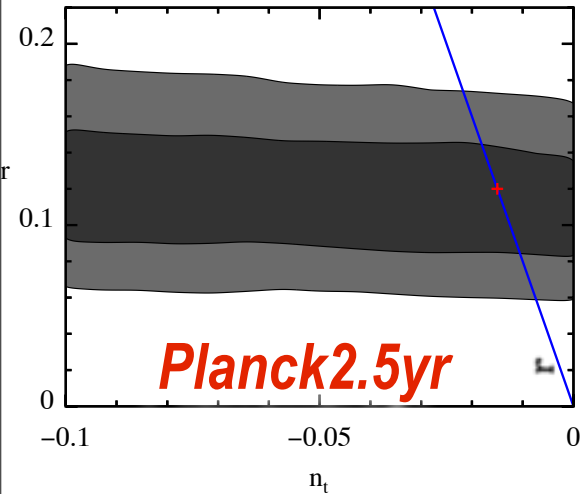
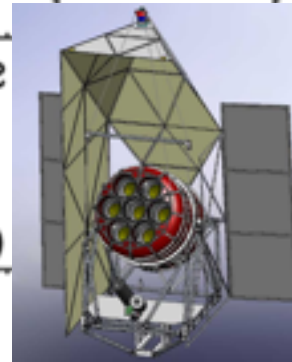
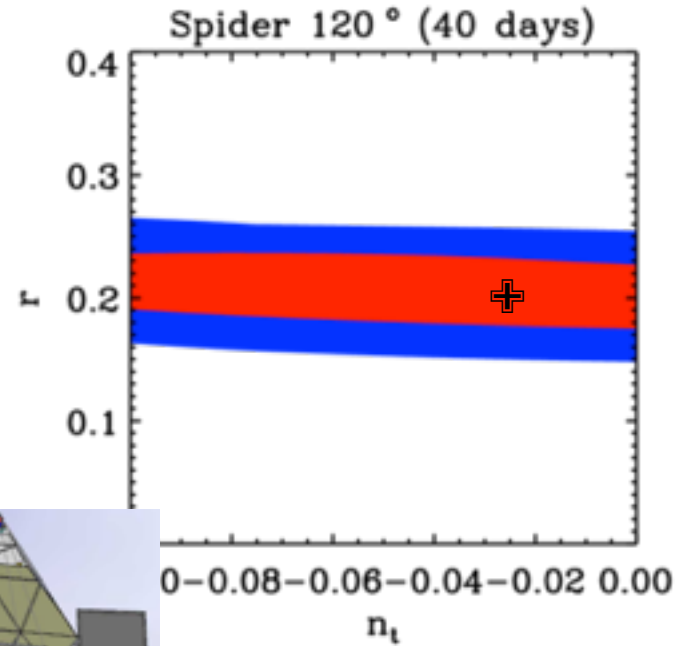
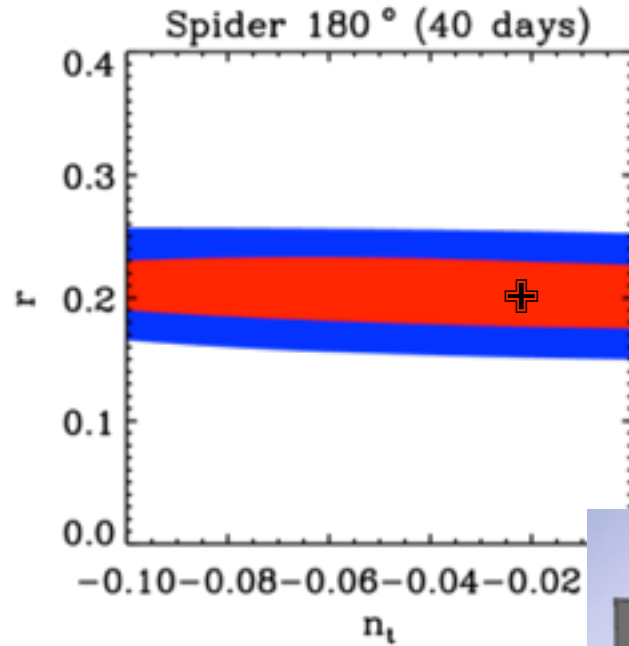
Spider 15° (40 days)



$$r \approx -8n_t$$

poor  $n_t \Rightarrow$

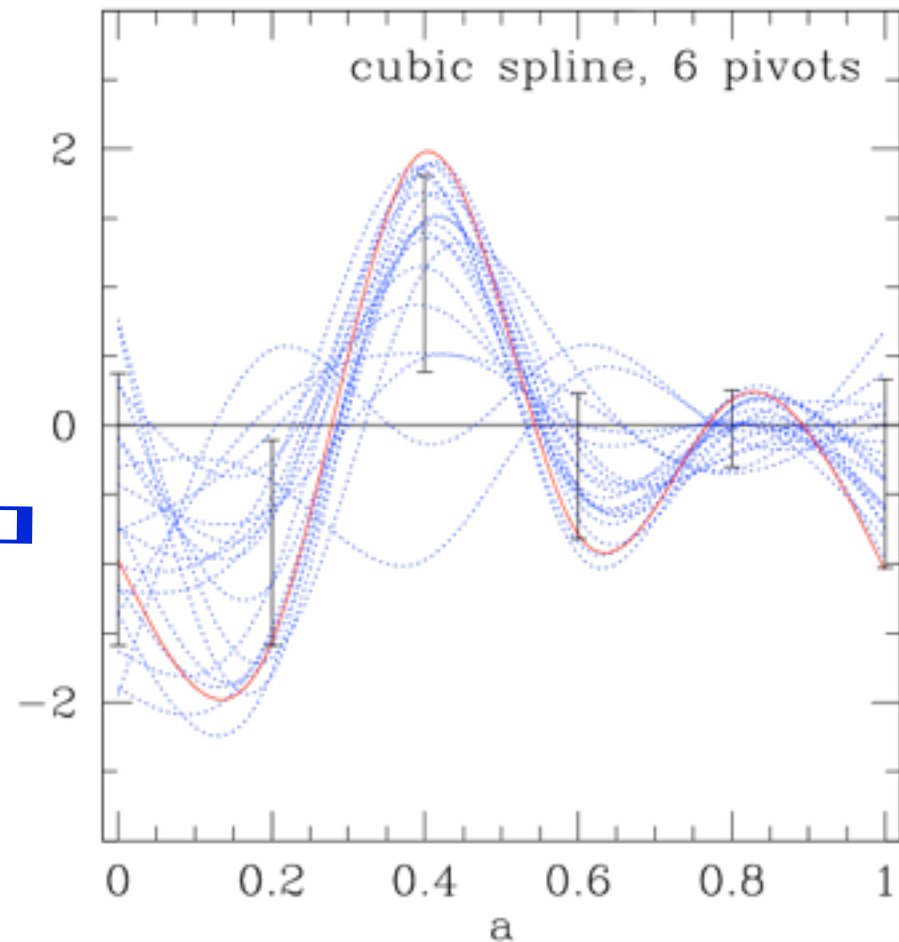
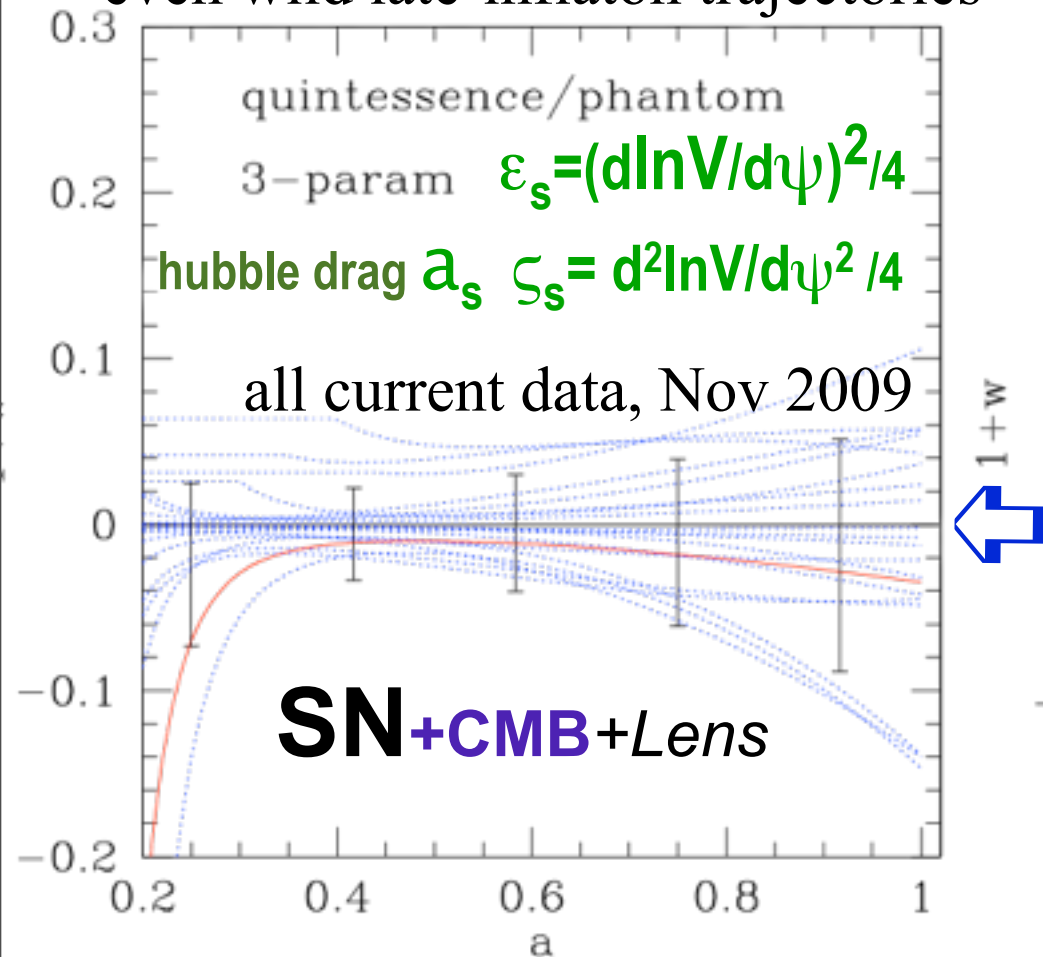
*inflation consistency cannot be checked with Spider or Planck2.5yr*



# is the dark energy “vacuum potential energy” ?

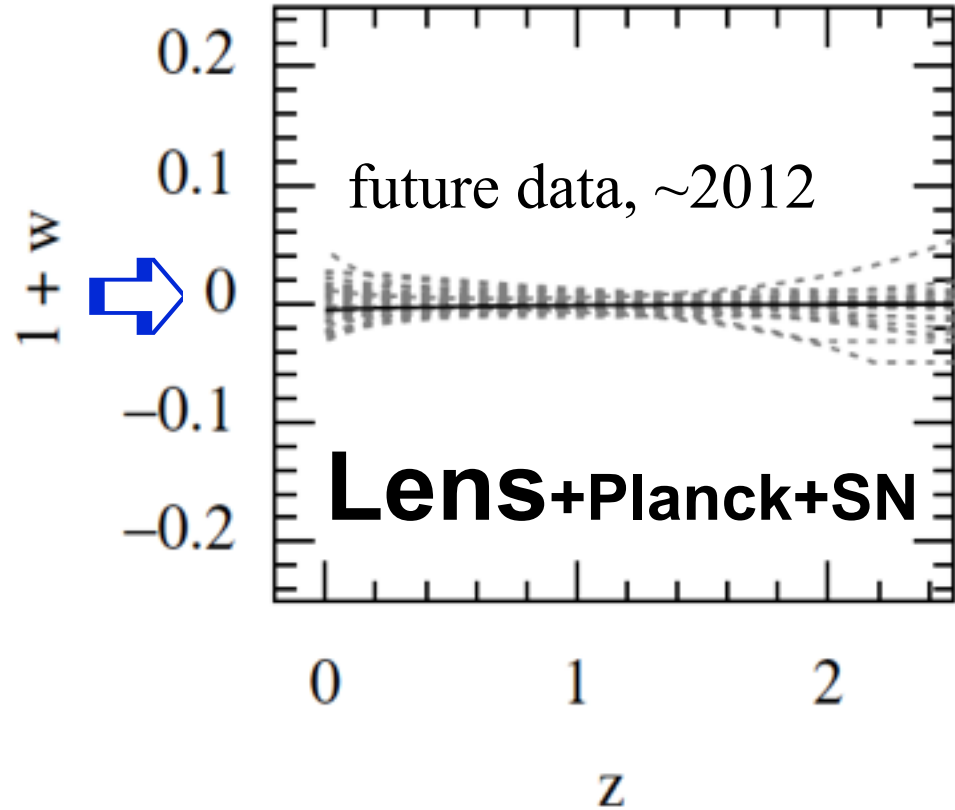
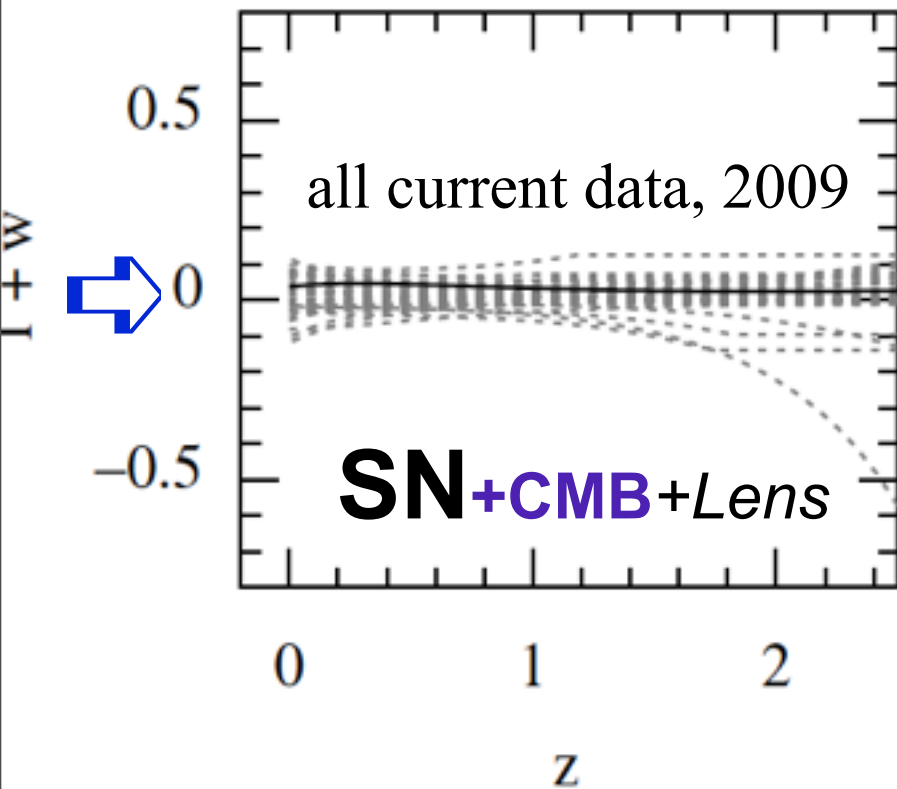
a 3-parameter expansion paves even wild late-inflaton trajectories

semi-blind mode expansion



TEST: within errors, energy-density does not change with expansion  $\Rightarrow$  Einstein's cosmological constant is best fit so far  
cannot reconstruct the quintessence potential, just the slope  $\epsilon_s$  &  $\sim$ hubble drag

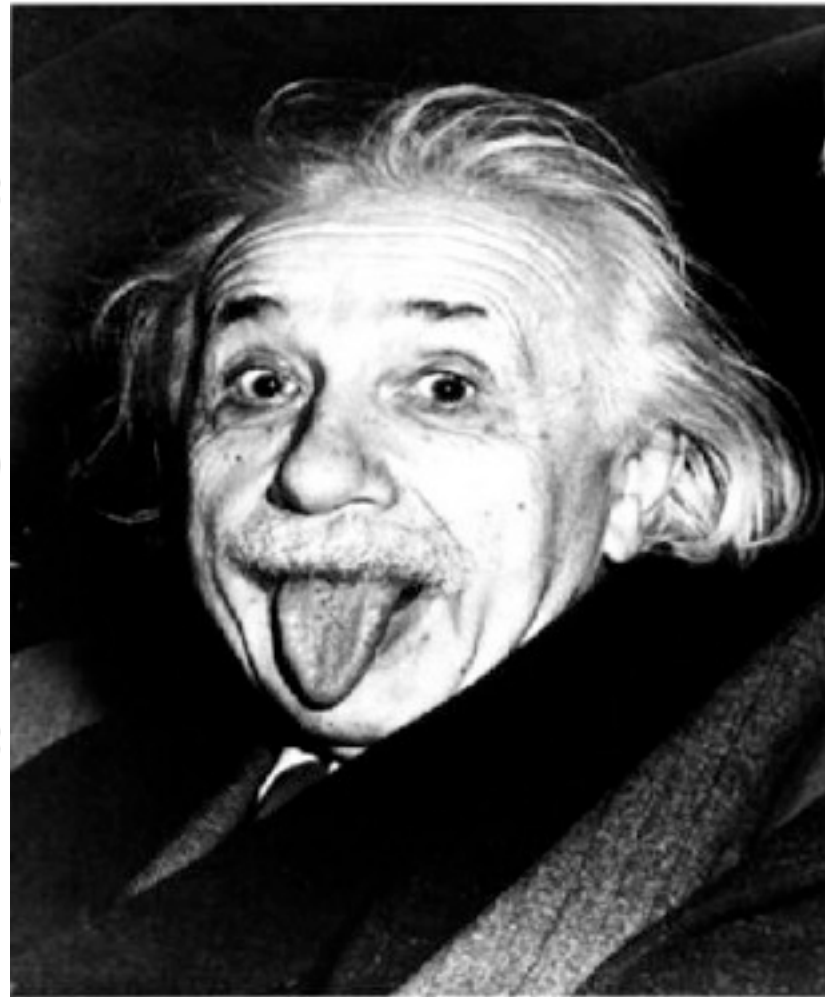
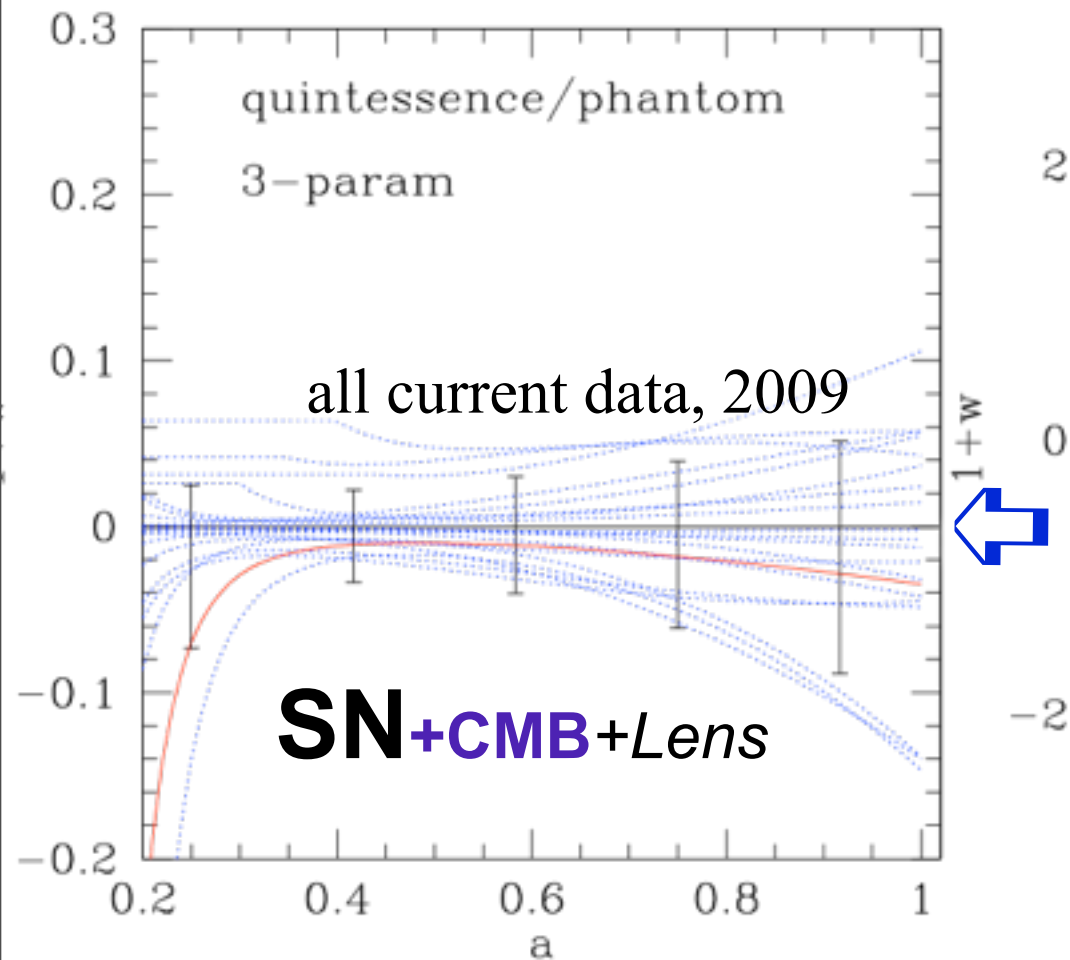
# is the **dark energy** “vacuum potential energy” ?



TEST: within errors, energy-density does not change with expansion  $\Rightarrow$  Einstein's cosmological constant is best fit so far



# is the dark energy “vacuum potential energy” ?



TEST: within errors, energy-density does not change with expansion  $\Rightarrow$  Einstein's cosmological constant is best fit so far

CITA/PI/CIFAR Dec 8 2009; UPenn Centre Dec12 2009; CIFAR10 Feb 19;  
CITA@25/BOND@60 - his idea, worked on it into Oct 2009!

## ***Physics Today June 2010: Lev Kofman's Obituary***

*Lev's graduate students remember him as a cosmic soccer player—and a gifted real one—deftly moving the research ball forward with his team and scoring often. The ball is now passed to us. In his final year, undaunted by his spreading illness, he grew to become an impressively wise acting director of CITA. It is the indomitable, fun-loving, deeply philosophical spirit who felt physics to his very core, a gourmand of life in all its manifestations, whom we miss so much.*



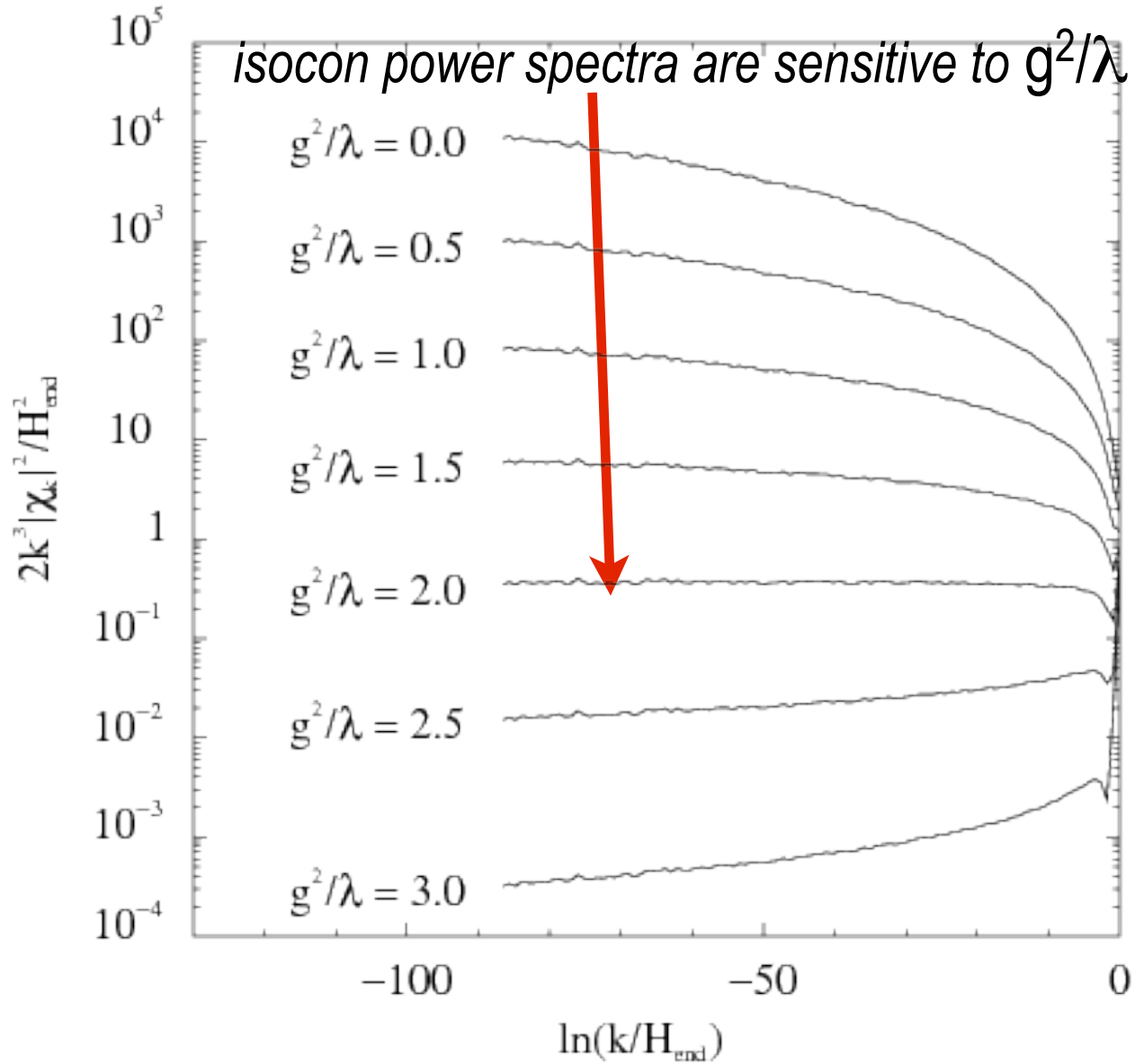
*May 10, 2010 email: For **Classical and Quantum Gravity**, **David Wands** and I are editing a special issue on **nonlinear cosmological perturbations**, and we thought it would be a good idea to **dedicate this issue to Lev**, and we'd like to include an image of Lev on the front page. What I'd like to ask you is to give us a permission to use a picture you gave me a while ago just before he died. I attach it with this mail. Best regards, **Misao Sasaki***

**& the w-paper with Zhiqi is about to go out, and trajectories with Zhiqi and Pascal too, and Andrei on non-G spikes**

# 80s-90s arena for BSI & **non-Gaussianity** near EOI, isocon fields couple in

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

$\chi_i(x,t)$  power



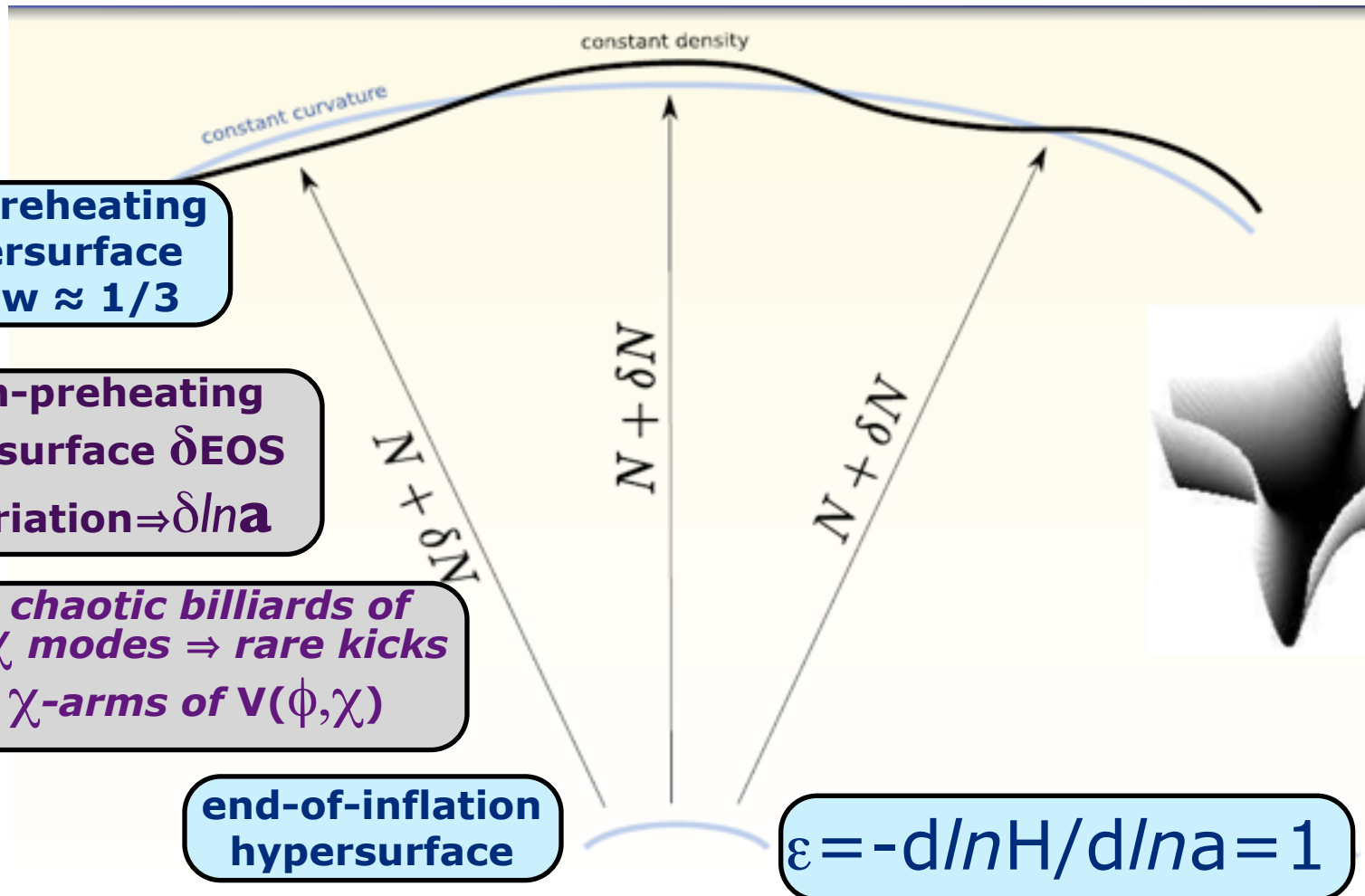
*expected  $k \sim H a$  rule would apply. pre-heating surprise!*

**$\ln a[\chi_i(x,t)]$**  from “subgrid”  $\propto H e^{-1}$  lattice simulations of  $\Phi_{\text{UHF}} \chi_{\text{UHF}}$

*Bond, Frolov, Huang, Kofman 09:*

*calculate how the expansion factor from the end of accelerated expansion (end of inflation) through preheating (copious mode-mode-coupling aka particle creation) to the onset of thermal equilibrium depends on  $\chi_i(x,t)$*

$$\delta N = \delta \ln a|_H = \text{curvature fluctuation}$$



calculate how the expansion factor from the end of accelerated expansion (end of inflation) through preheating (copious mode-mode-coupling aka particle creation) to the onset of thermal equilibrium depends on  $\chi_i(x,t)$

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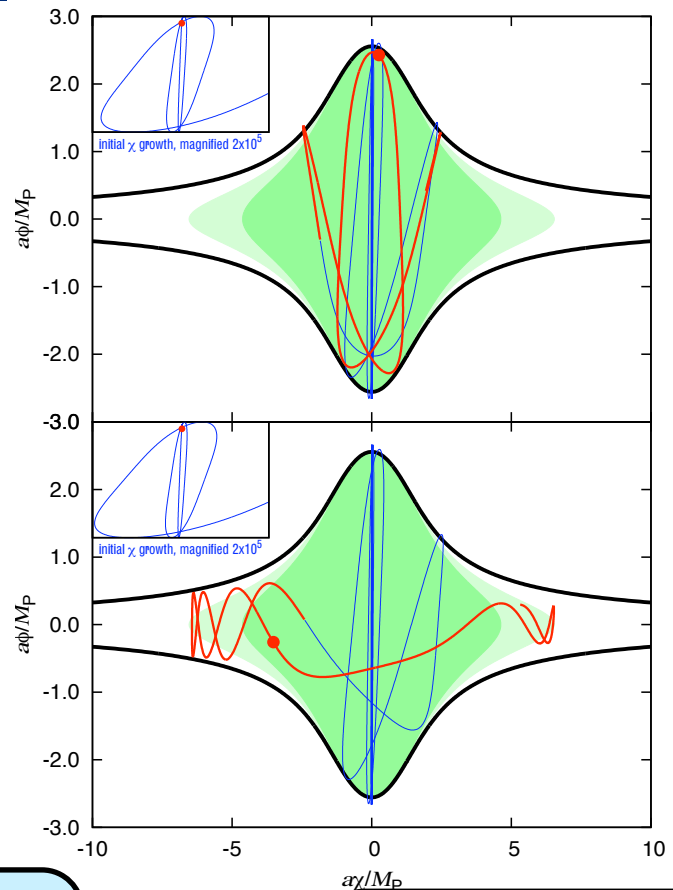
end-preheating hypersurface  
EOS  $w \approx 1/3$

begin-preheating hypersurface  $\delta$ EOS  
 $w$ -variation  $\Rightarrow \delta \ln a$

linear chaotic billiards of  $k \approx 0$   $\phi, \chi$  modes  $\Rightarrow$  rare kicks into  $\chi$ -arms of  $V(\phi, \chi)$

end-of-inflation hypersurface

$$\epsilon = -d \ln H / d \ln a = 1$$



linear regime of zero-modes:

$$\begin{aligned} \phi_0(t+T) &= \phi_0(t) \\ \chi_0(t+T) &= \chi_0(t) \exp[\mu_0 T] \\ &\Rightarrow \text{spikes are} \end{aligned}$$

$\log \chi_i$  spaced

