

Tuesday, 20 November, 12



dS_G/dt
I
N
F
L
A
T
I
O
N
dS/dt > 0

the nonlinear
COSMIC WEB

primary anisotropies

- linear perturbations: scalar/density, tensor/gravity wave
- tightly-coupled photon-baryon fluid: oscillations $\delta\gamma$ $v\gamma$ $\pi\gamma$
- viscously damped
- polarization $\pi\gamma$
- gravitational redshift

dS/dt > 0

Decoupling LSS

17 kpc
(19 Mpc)

secondary anisotropies

dS/dt > 0

- nonlinear evolution
- weak lensing
- thermal SZ + kinetic SZ
- $d\Phi/dt$
- dusty/radio galaxies, dGs

L_{sound}/k_{sound}

M
I
L
K
E
Y
W
A
Y



z=0



Bayesian flow prior to posterior via likelihood

DarkE

reionization

dS_{astro} < 0

z ~ 1100 redshift **z**

z ~ 10

13.7-10⁻⁵⁰ Gyrs

13.7 Gyrs

time t

10 Gyrs

today

Let There Be Heat: the Shock-in-Times of Post-inflation Preheating

Probing the Cosmic Theory of Early & Late Universe Physics: from Simplicity to Complexity

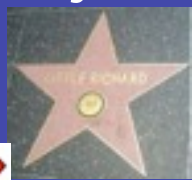
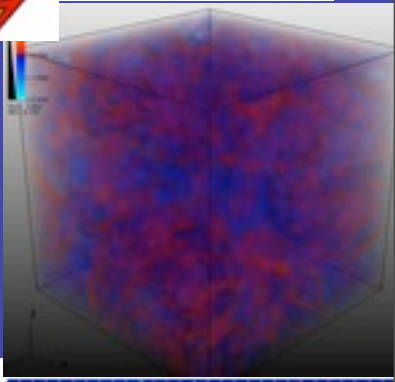
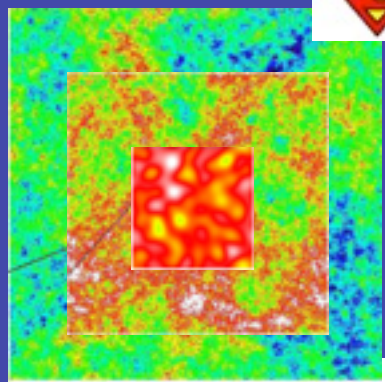
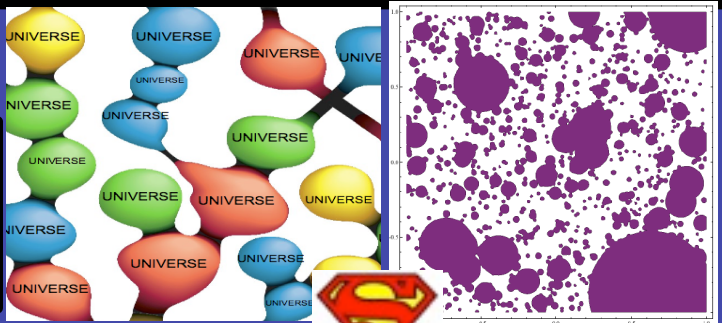
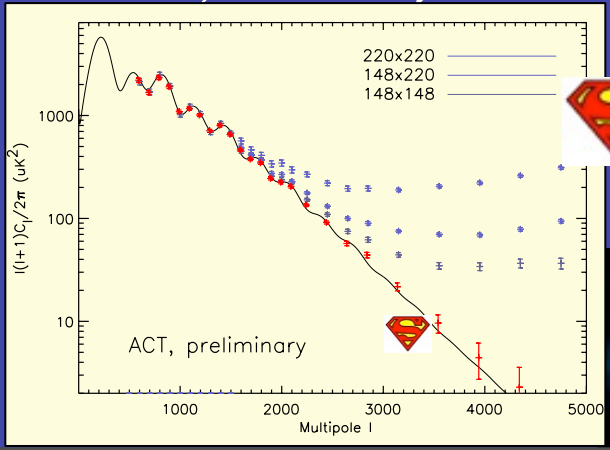
IT from BIT from BITs in IT
information quantity = entropy Shannon 1948
information quality = IQ essence

info& primarily-earlyU
=Bond@IAP 12.09.28

info& primarily-clusters/SZ
=Bond@IAS 12.10.04

info& primarily-primaryCMB
=Bond@APC 12.10.30; @Imperial 12.11.02

Damping Tail & Recombination History
new SPT12+,ACT12+,Planck13



the coherent & the entropic, in all its forms, from the ultra-early-U to Now to the ultra-late-U

Dick Bond CIFAR@CITA with CITA aka *Cosmic Information Theory & Analysis*

Probing the Cosmic Theory of Early & Late Universe Physics: from Simplicity to Complexity

the **nonlinear**
COSMIC WEB



dS_G/dt

primary anisotropies

- linear perturbations: scalar/density, tensor/gravity wave

$dS/dt > 0$



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Φ SW $d\Phi/dt$



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DarkE

MILKYWAY



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$z \sim 10$

$dS/dt > 0$

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13.7 Gyrs

time t

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today

Universe = System(s)+Reservoir

~ Signal(s)+Residual noise

~ Effective Theory+Hidden variables

~ Data+Theory

~ observer(s)+observed

the coherent and the entropic, in all its forms, from ultra-early-U to ultra-late-U

$S_{U,m+r} \sim 10^{88.6}$ cf. $S_G \sim 10^{121.9}$ asymptotic DE

$S_{th,cl} \sim 10^{76}$ Studying the Cosmic Tango en-TANGO-ment the dance of $U=R_{U}S$

our Cosmoticians' Agenda: Statistical Paths in Cosmic Theory & Data via the Bayesian chain drawing what we know of It from Its Bits

**$P(q|D,T) = P(D|q,T)P(q|T)P(T)/P(D|T)$ $D=CMB,LSS,SN,...,complexity, life$
 $T=baryon, dark matter, vacuum mass-energy densities,...,$
early & late inflation as low energy flows/trajectories on a (string) landscape**

entropy = <information-content> Quantity Shannon 1948

generalized parameter space $\{q\}$ ~phase space

$$S_f(D,T) = \int dq P_f \ln[P_f^{-1}]$$

relative Shannon entropy = - Kullback Leibler divergence

$$S_{fi}(D,T) = \int dq P_f \ln[P_f^{-1} P_i] \quad \text{cf. } S_f - S_i$$

= relative RENYI entropy of order 1; use order n for clustering & clumping

$IQ=information\ quality$

**$IQ \sim \{\text{minimal length messages/codes} \mid \text{error tolerance}\}$ Planck(E/T),
genetic code, recipes, axioms, algorithms, IC/BC/evolution eqⁿs**

cat information_overload.txt | grep fundamental | grep physics > exec_summary.tex

filter, compress, reduce, marginalize



early U applications of "CITA" to cosmic-complexity



☆ *the superhorizon measure problem & the Lambda-scape*



☆ *the emergence of the collective from the random!*
coherence from driven zero-point vacuum fluctuations $\Rightarrow V$
inflaton, gravity waves; decohere



☆ *let there be heat:* entropy generation in **preheating** from the coherent inflaton (origin of all "matter")



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*Studying the
Cosmic
Tango*



some non-early U applications of "CITA" to cosmic-complexity



➤ information in **nearly-Gaussian** density/potential random fields of U, & in weakly and strongly non-linear fields. *ergodic theorem & constrained fields*



➤ spatial coarse-grained **CMB entropy** & how we capture it



➤ dark matter entropy, cluster & **protocluster** & **cosmic web** entropy



MHD turbulence entropy with cooling & grain polarized emission - CMB fgnd

➤ *How Shannon info-entropy flows from CMB bolometer timestreams to marginalized cosmic parameters via Bayesian chains from prior to posterior. 1D & 2D & ... $\Delta S(q,DT)$ (cf. ACT10), $q=r, w, n_s, \dots$*



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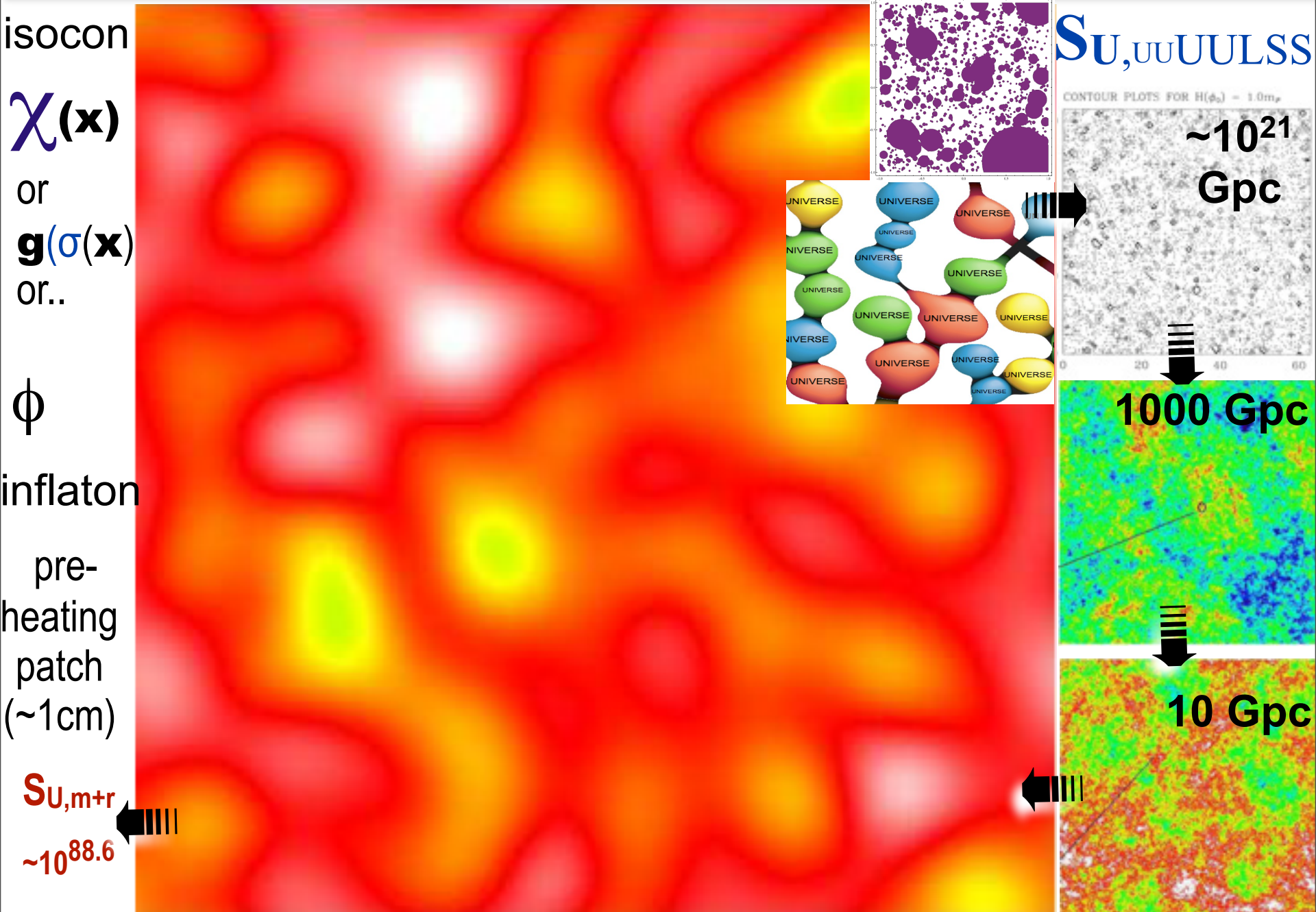


$P(q|D,T) = P(D|q,T)P(q|T)P(T)/P(D|T)$ $D=CMB,LSS,SN,...$ **complexity**, life
 $T=baryon, dark matter, vacuum mass-energy densities,....$
early & late inflation as low energy flows/trajectories on a (string) landscape

Old: Theory prior = delta function of THE correct one&only

New: Theory prior = probability distribution of
late-ish-flows on a **LANDSCAPE**

modulating post-inflation entropy generation shocks *via* longrange fields



how (most of) the **entropy** in matter

=> *GUT plasma/quark soup* => $S(\gamma, \nu)$ was

generated (through a *shock-in-time*)

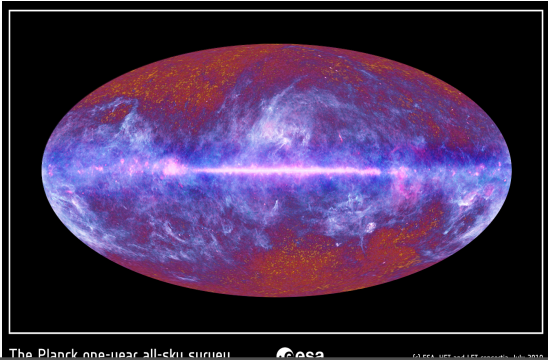
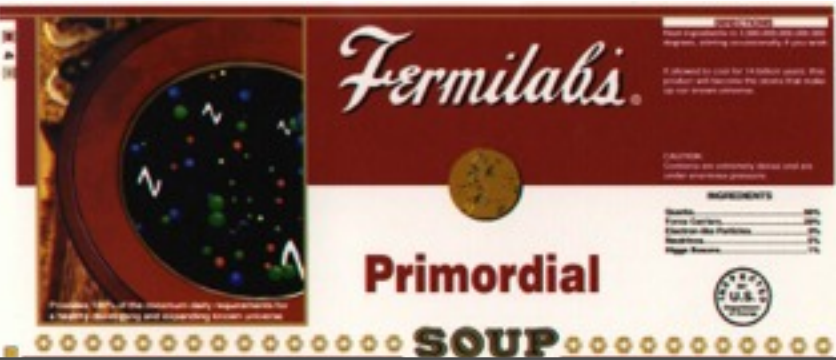
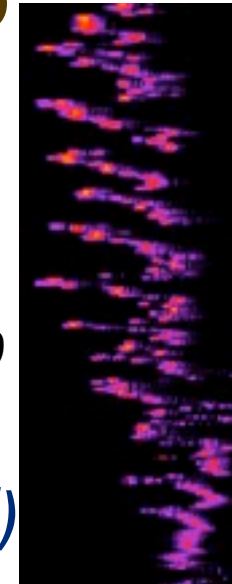
via *nonlinear coupling* of the *inflaton* to

new interaction channels g, χ_a ultimately to *standard model degrees of freedom*

∃ a role for *decaying particles, 1st order phase transitions?*

exactly who, what, where, when, why?

we search for fossil "non-Gaussian" structures from this period with Planck +WMAP9



$a_{shock}(g)$

non-Gaussianity (WMAP, Planck, LSS) spiky nG preheating

modulating post-inflation entropy generation shocks via longrange fields

isocon
 $\chi(\mathbf{x})$

or
 $g(\sigma(\mathbf{x}))$
or..

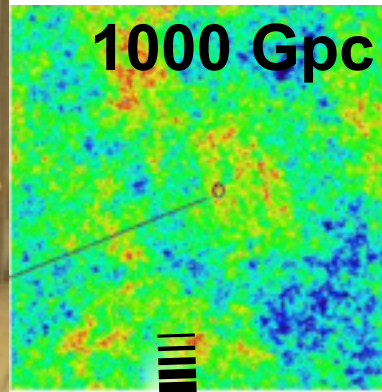
pre-
heating
patch
(~1cm)



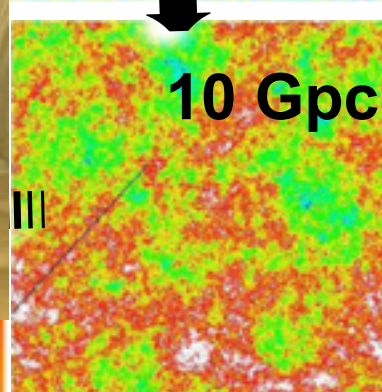
Parametric
Resonance
 $g^2 / \lambda \sim 1$



BB12



1000 Gpc

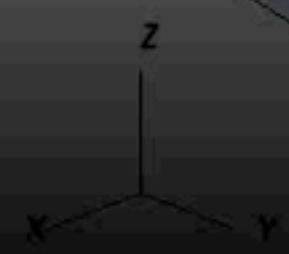
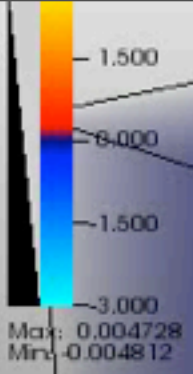


10 Gpc



B²FH12 @ifaUH aka Waikiki Feb12

$$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2 \chi^2$$



preheating
patch ~1cm

$\ln \text{energy density} / \langle \text{energy density} \rangle = -\mathcal{S}$

B+Braden12 using Frolov/Huang/Braden, Defrost/HLattice/Bsymplectic

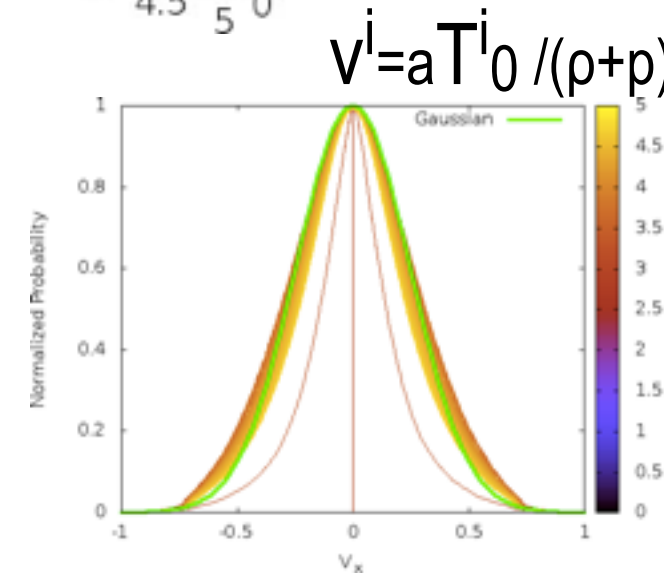
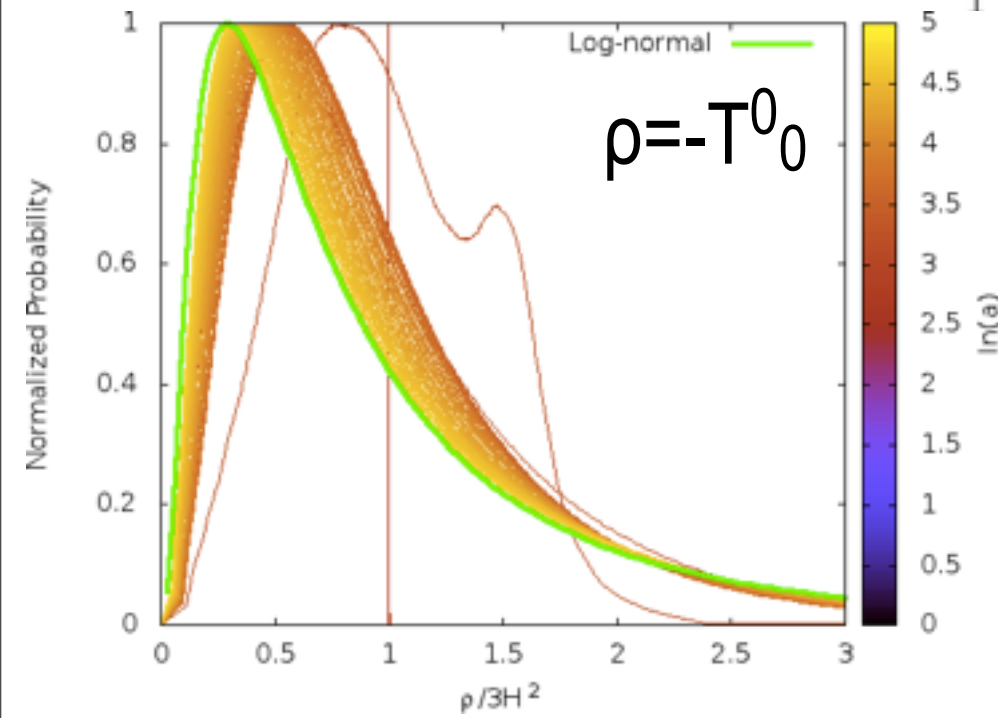
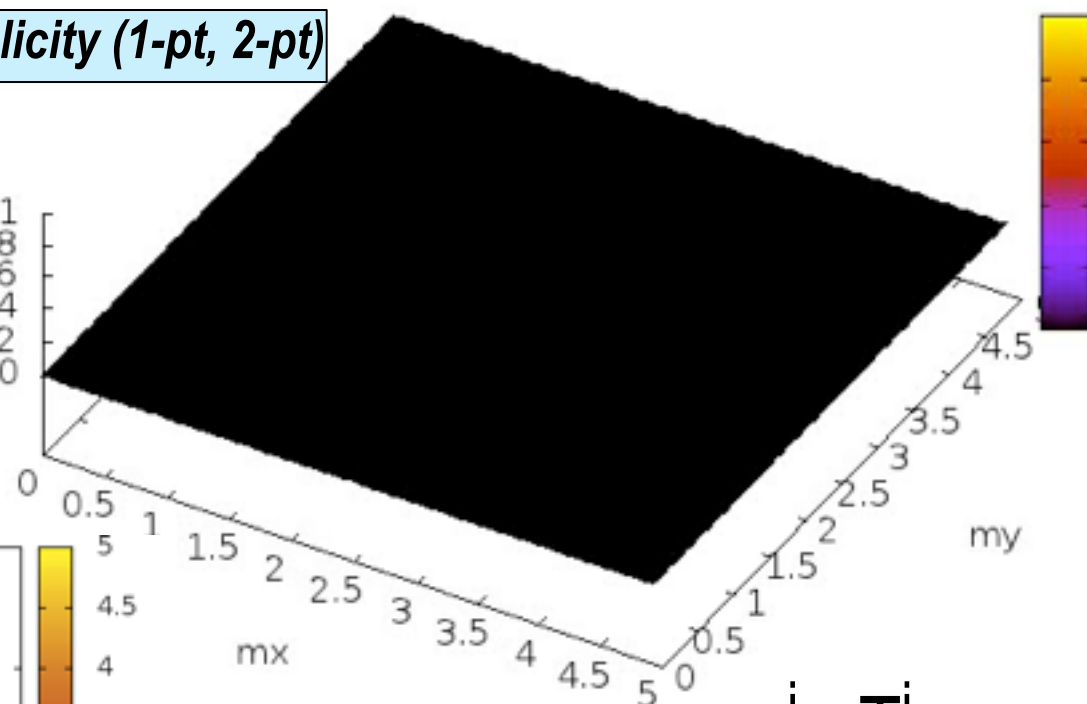
$$T^a_b = \rho_{(c)} U^a U_b + U^a J_{(e)b} + U_b J_{(e)}^a + p_{(c)} (\delta^a_b + U^a U_b) + \Pi^a_b \quad \log(a) = 0$$

spatial complexity but \exists statistical simplicity (1-pt, 2-pt)

post-shock \Rightarrow total stress-energy T^a_b

hydrodynamics description phonons
entangled primary fields $(\phi, \Pi_\phi, \chi, \Pi_\chi)$
 \Rightarrow *not good post-shock descriptors*

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2$$



nearly Gaussian in $\ln \rho / \langle \rho \rangle$ & in k -bands! B+Braden12

nearly Gaussian in v

Shannon entropy $S_f(D,T) = - \int dq P_f \ln P_f = \text{information}$ with no Quality measure on the bits **IQ**
 ~ von-Neumann entropy = Trace $\rho \ln \rho^{-1}$, $\rho(U) = \rho(S,R) = \rho(R|S) \rho(S)$ entanglement of phase & probability

Gaussian random field with correlation function **C** weight matrix **C⁻¹**
 $S = (\text{Trace } \ln C + N_{\text{dof}} \ln 2\pi + N_{\text{dof}}) / 2 = \langle \ln V_{\text{phase-space}} \rangle + N_{\text{dof}} / 2$
 = Shannon entropy subject to the **constraint** $\int dq P_f \delta q^i \delta q^j = C^{ij}$
 relative Shannon entropy $S_{fi} = \text{Tr} \{ \ln C_f C_i^{-1} + 1 - C_f C_i^{-1} \} / 2$



cf. grand canonical ensemble: constrained E_{tot} & N_A & V

Lagrange multipliers (conjugate variables) $\beta = 1/T$ & $-\beta\mu_A$ & β^ pressure; in LTE, functions of (x)*

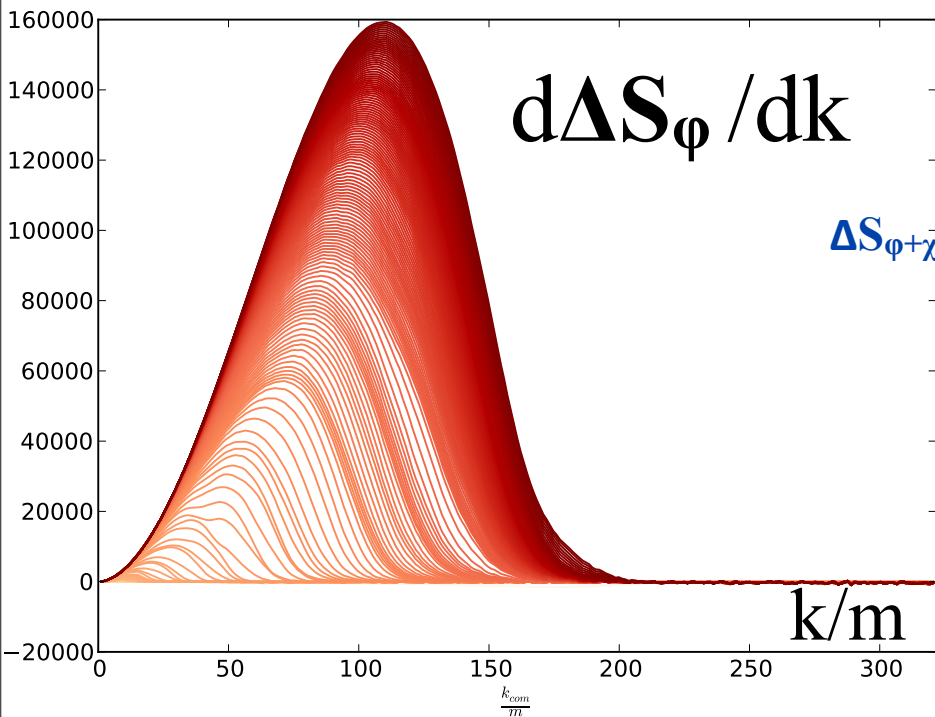
non-eq thermodynamics: flux $J_{(e)}^i(x)$ $J_{(N)}^{Ai}(x)$ conjugate thermodynamical forces B_i ($\sim \partial_i \beta$)

*more constraints (e.g., higher point correlations & more complexity) reduce entropy by limiting the freedom of the degrees of freedom q : **non-Gaussian distributions have lower S***

Lagrange multipliers: out-of-equilibrium drivers κ_i for $\langle \delta q^i \rangle$ and K_{ij} for $C^{ij} \langle \delta q^i \delta q^j \rangle$

problem: Dimensional Reduction when eigenvalues of $C \sim 0$, $S \sim -\infty$: but cold degrees of freedom should have $S=0$ (3rd). Bose-Einstein & Fermi-Dirac statistics - indistinguishable cf. distinguishable. Condensates form when too much N for E .

eU S: $\Delta s = \Delta 1/2 \text{Tr } C_{\ln p / \ln p}$ info-content in phonons $S = - \ln [\rho V/E]$



$$\Delta S_\phi \sim 1/2 \sum_k \ln \det \langle (\phi, \Pi_\phi) (\phi, \Pi_\phi)^\dagger \rangle$$

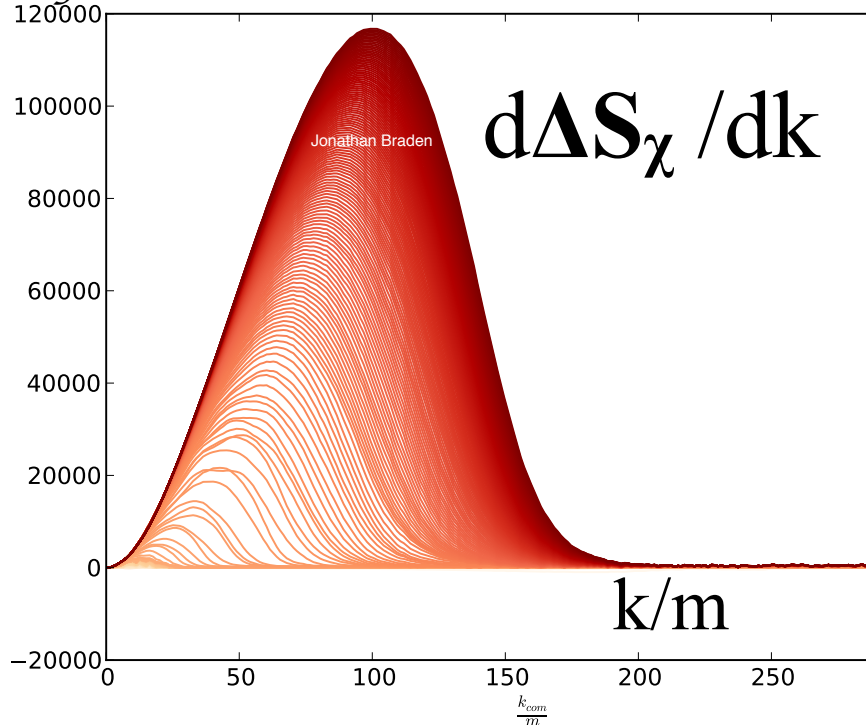
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Gaussian entropies for the “fundamental” interacting fields, ϕ, χ , subject to correlated 2-point measurements: $4N^3$ dof. $\phi_A = \phi_{Ab} + \phi_{Af}$
how good are $M^2_{AB}(\phi_{Ab}(x))$ -f-quasiparticles?
 post-shock fields become well-entangled,

hydrodynamic conserved quantities: N^3 dof in S

$S_k = \text{phonons}$



$$\Delta S_{\ln \rho} \sim 1/2 \sum_k \ln \det \langle S S^\dagger \rangle,$$

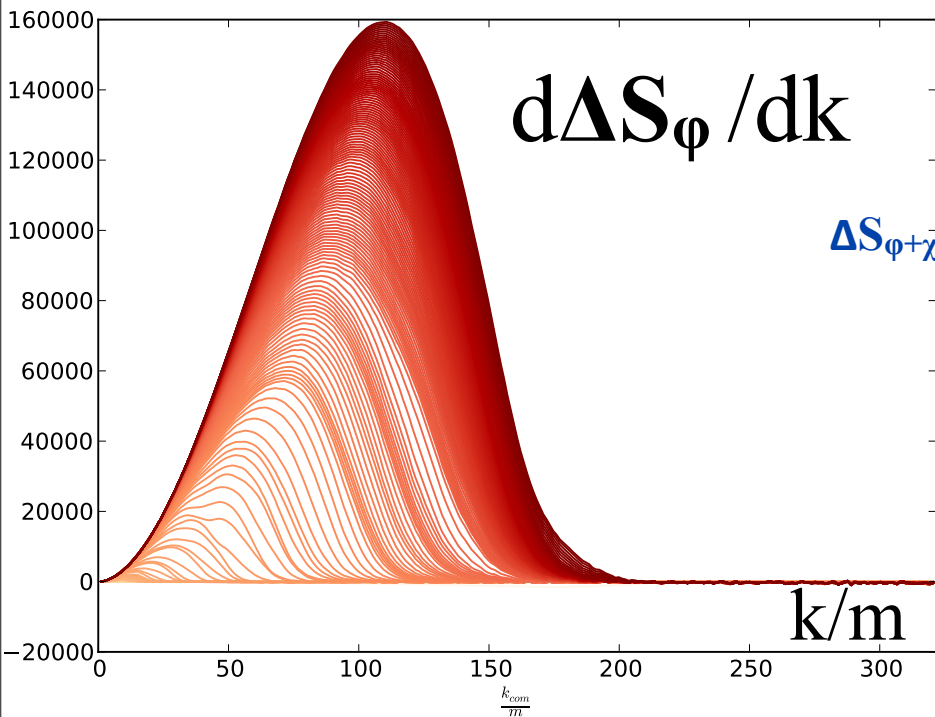
$S = \ln \rho^{-1} E/V = \text{an information content}$

$D..S/dt = \nabla_U ..S \sim -(1+w)..Tr \delta\sigma + \text{higher}$
 $\sigma_{a;b} = \text{shear} = 1/2 (U_{a;b} + U_{b;a})$

TBD: identify shear viscosity, thermal conductivity & bulk viscosity via correlation function measures

$$\Pi = -2\eta \sigma', \quad J_{(e)} = -C \nabla S$$

phonons = isotropic-shear waves = longitudinal velocities
anisotropic-shear waves: viscous damping



$$\Delta S_\phi \sim 1/2 \sum_k \ln \det \langle (\phi, \Pi_\phi) (\phi, \Pi_\phi)^\dagger \rangle$$

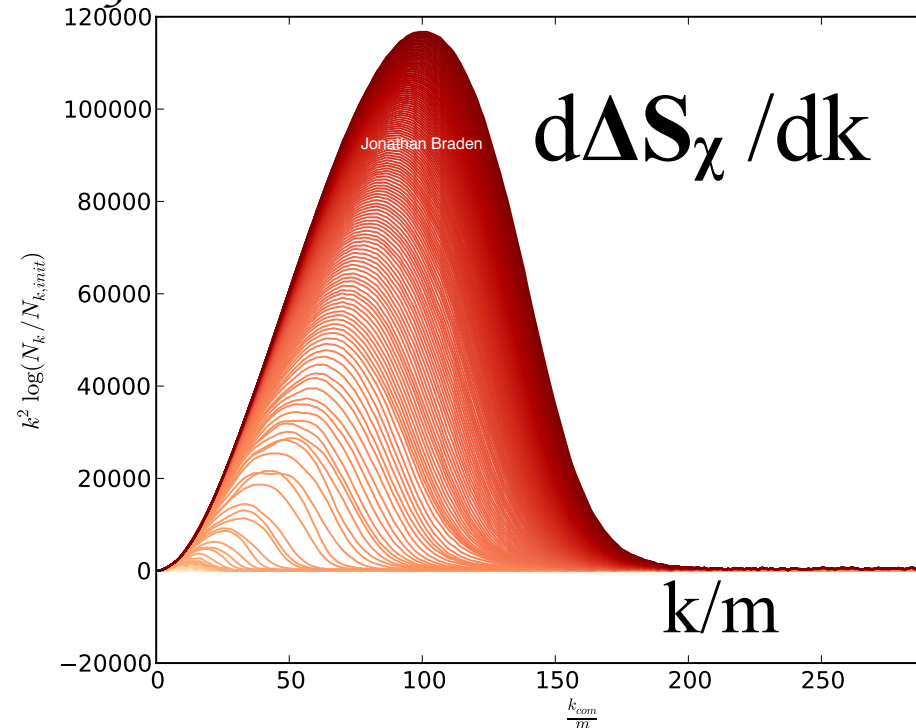
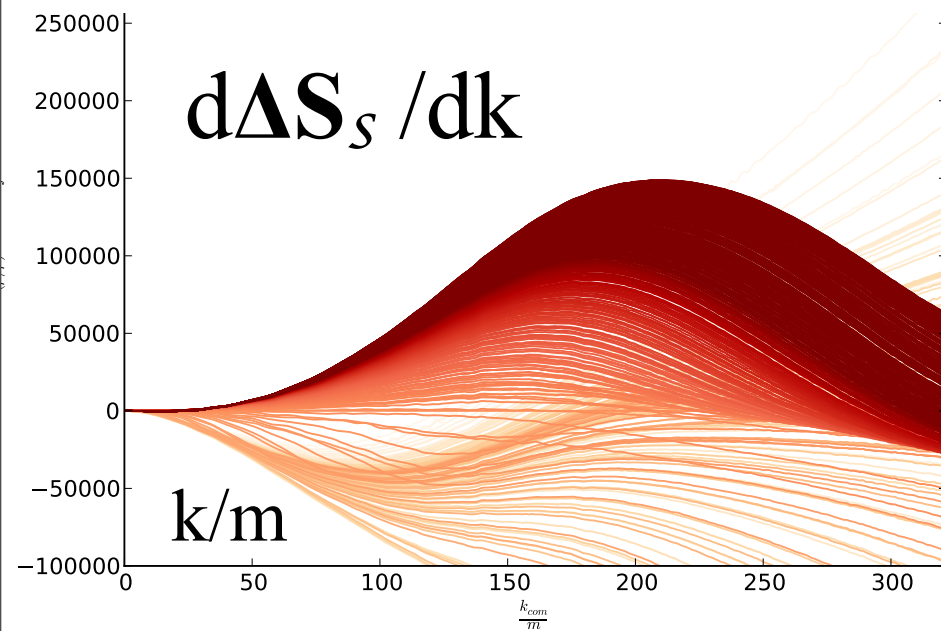
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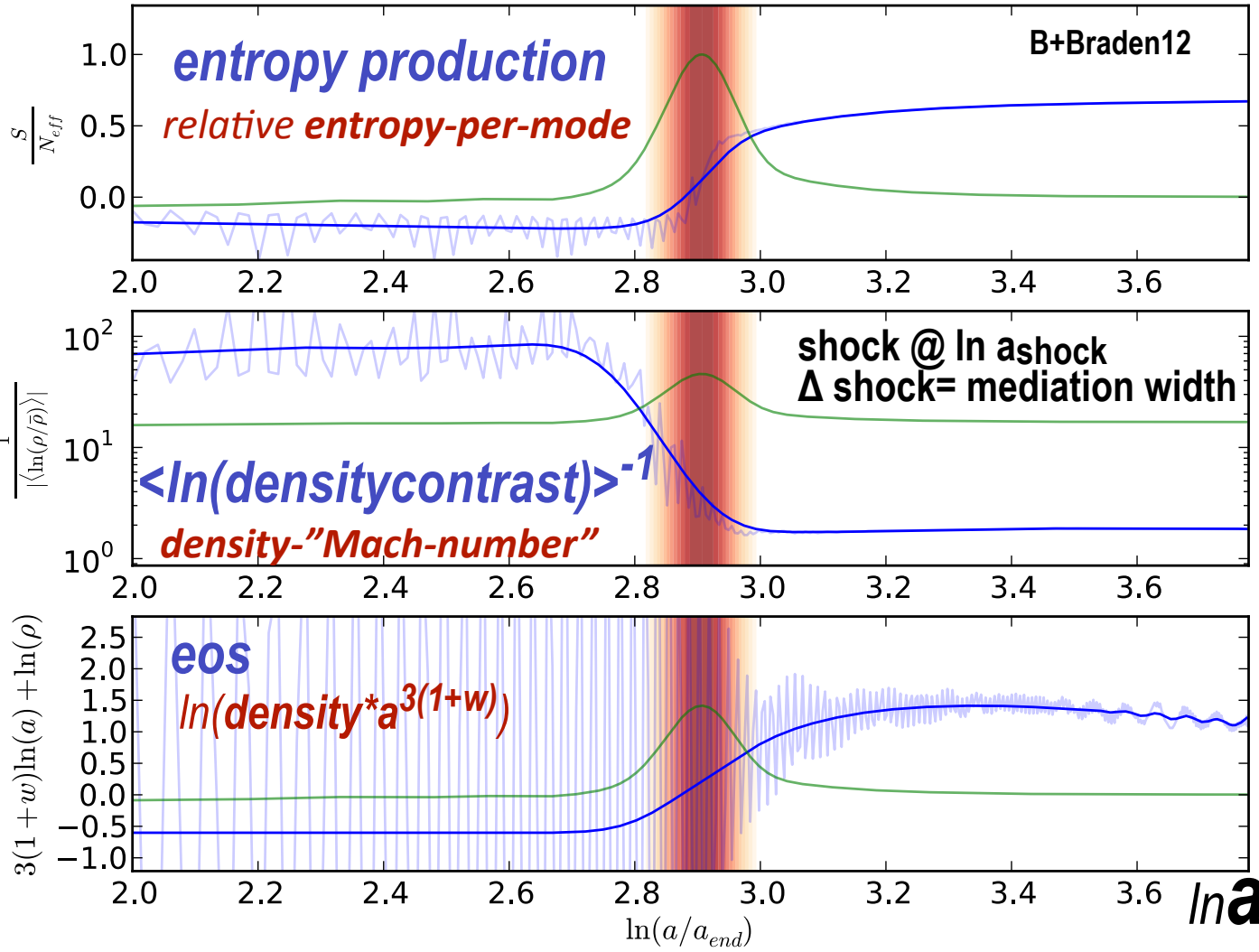
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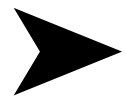
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true thermal equilibrium far off



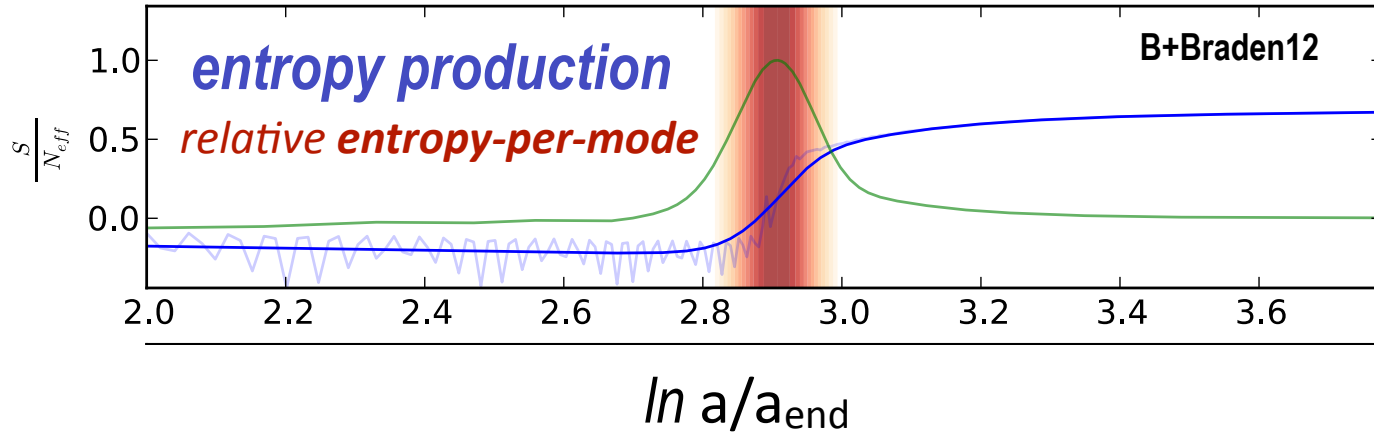
& on to coupling to standard model degrees of freedom

the Shock-in-time: constrained coarse-grained **Shannon-entropy($\ln a$)** minus the initial Gaussian random field entropy (from band-limited quantum fluctuations)

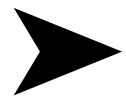
there is indeed a spike of entropy production at the shock front.

$V(\phi, \chi) = 1/2 m^2 \phi^2 + 1/2 g^2 \phi^2 \chi^2$ **post-shock \Rightarrow Hydrodynamics phonon description nearly Gaussian in $\ln \rho / \langle \rho \rangle(x)$ $\ln \rho / \langle \rho \rangle(k) \& v$**

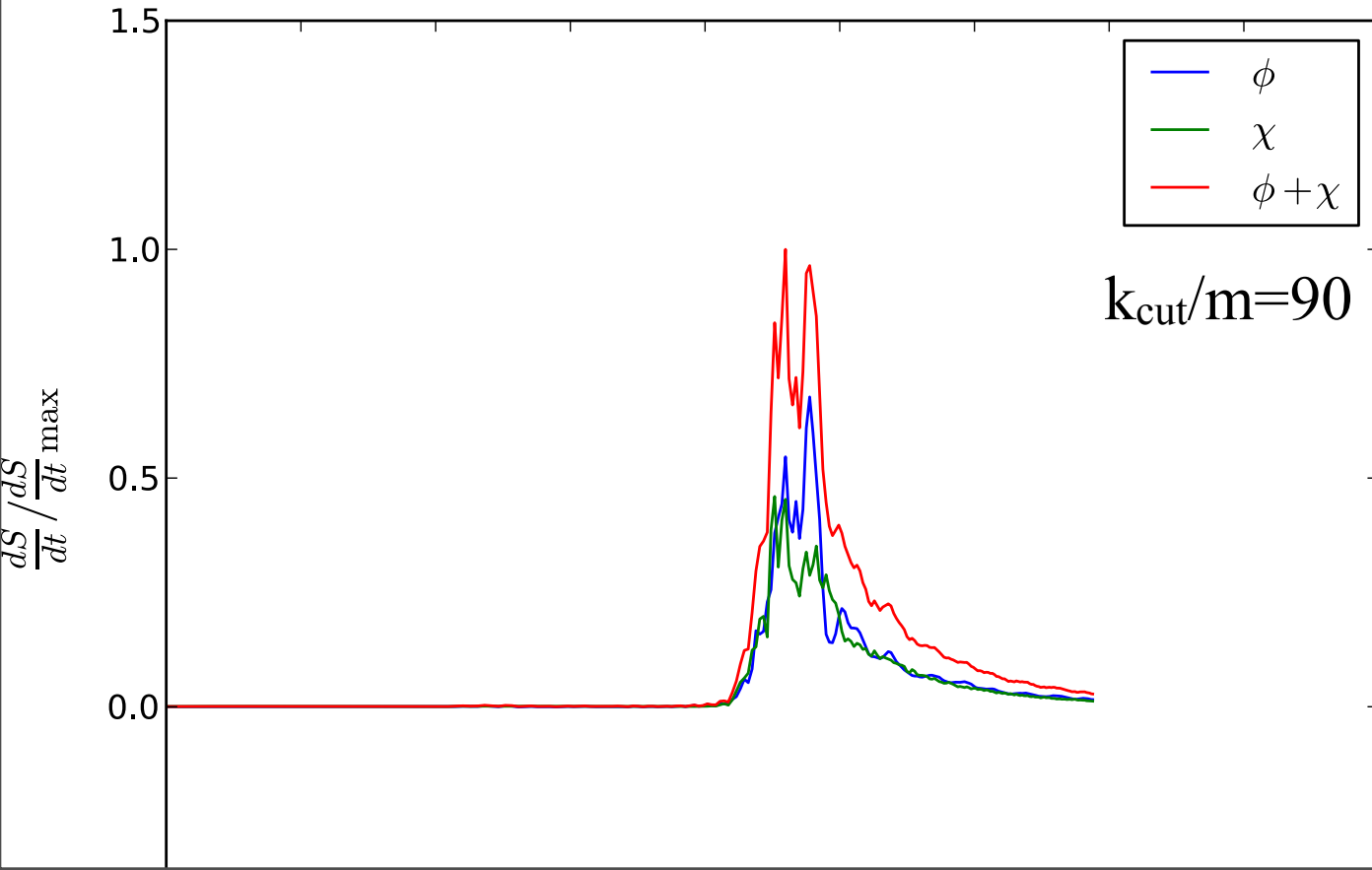
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true
thermal
equilibrium
far off



& on to
coupling to
standard
model
degrees of
freedom



non description
 $\rho > (k) \& v$

the Shock-in-Times of Post-inflation Preheating B+Braden12

Initial State = Nearly Homogeneous Inflaton

low entropy (coherent ϕ + vac fluctuations), *information encoded in a few parameters*

Preheating

Instabilities result in nonlinear transition to an incoherent state, resonances?

KLS 94, 97, e.g. Tkachev, Felder, Garcia-Bellido, ...

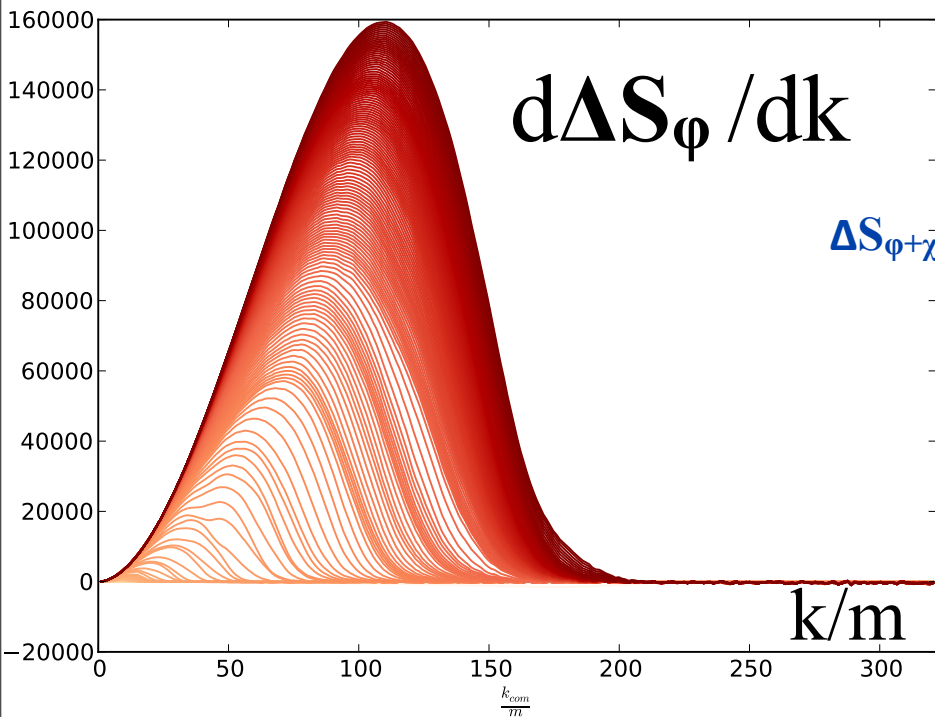
***the shock-in-time is the sharp mediator between the linear & the highly nonlinear transition
a fascinating non-Gaussianity can arise if there is a spatial modulator field varying the shock time***

(Near Adiabatic) Transition Regime

Complex slowly evolving nonlinear, nonequilibrium state e.g. Micha and Tkachev 2004,
turbulence analogy??? ***the evolution is NOT a Kolmogorov-like turbulent cascade to higher modes***

Final State = Thermal Equilibrium

= maximum spreading of information in modes subject to energy & particle number
constraints. *How to couple to standard model dofs to accelerate the power
spectrum evolution to a thermal bose-einstein distribution function?*



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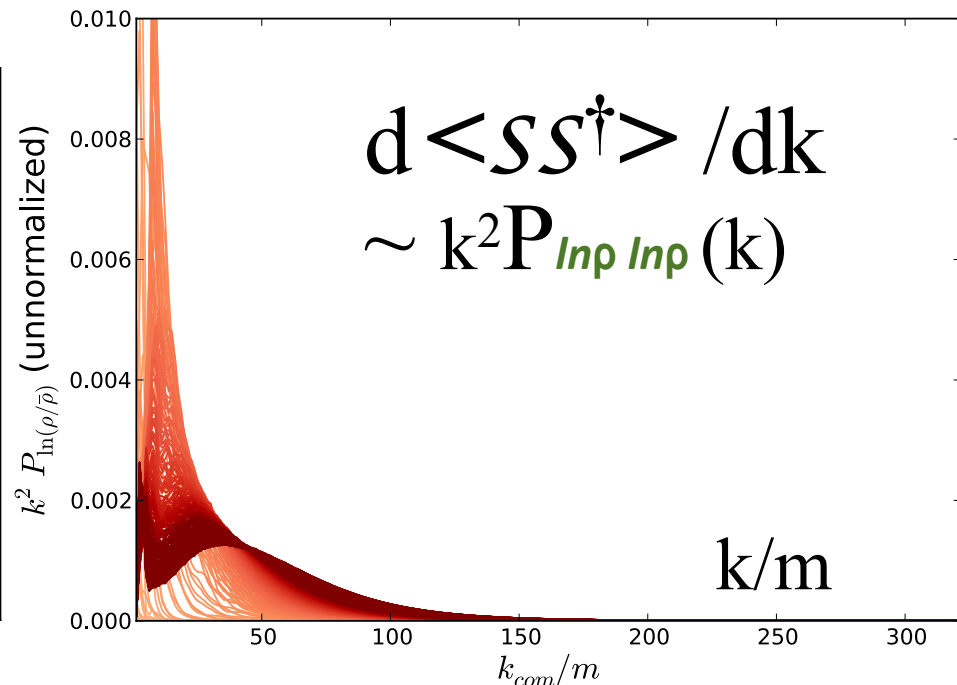
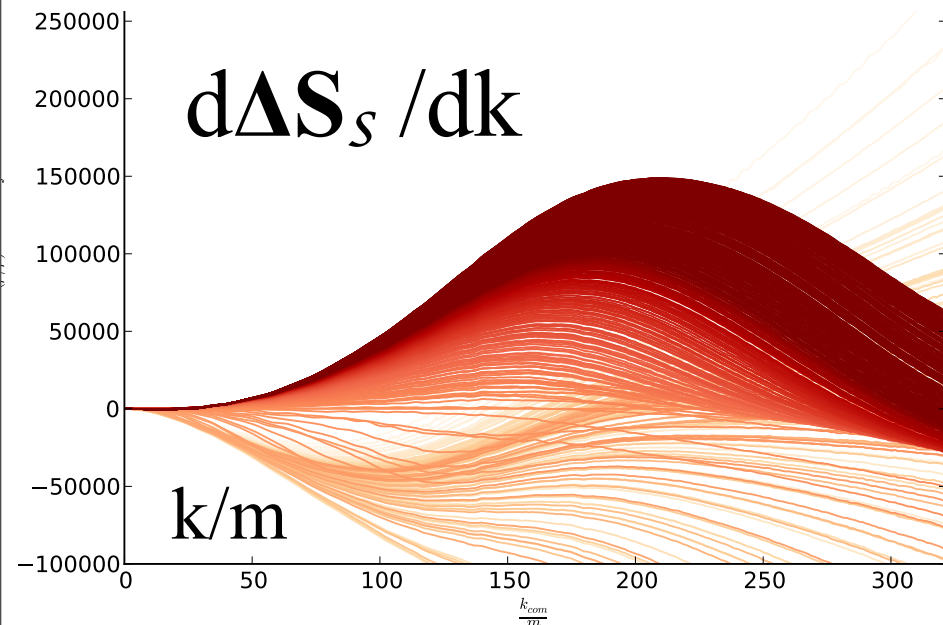
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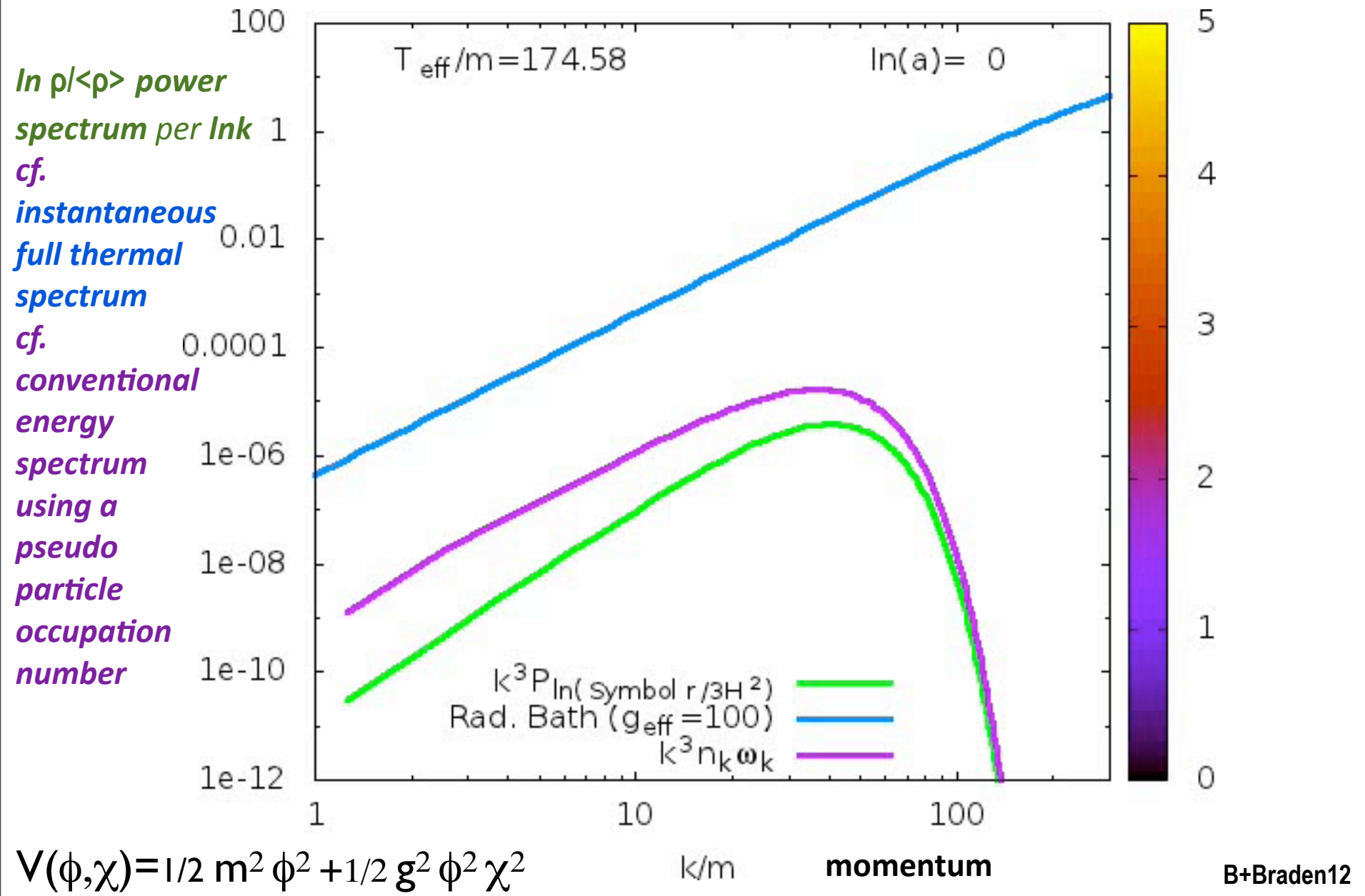
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coherent inflaton => incoherent mode cascade of fields thru a shock-in-time to thermal equilibrium

$S_{U_i} \sim 0$; $S_{U_{tot,m+r}}/n_b \sim 1.66 \times 10^{10}$ bits/b; $s_\gamma/n_\gamma = 5.2$ bits/ $\Upsilon = 2130/411$; $s_v = 21/22 s_\gamma$

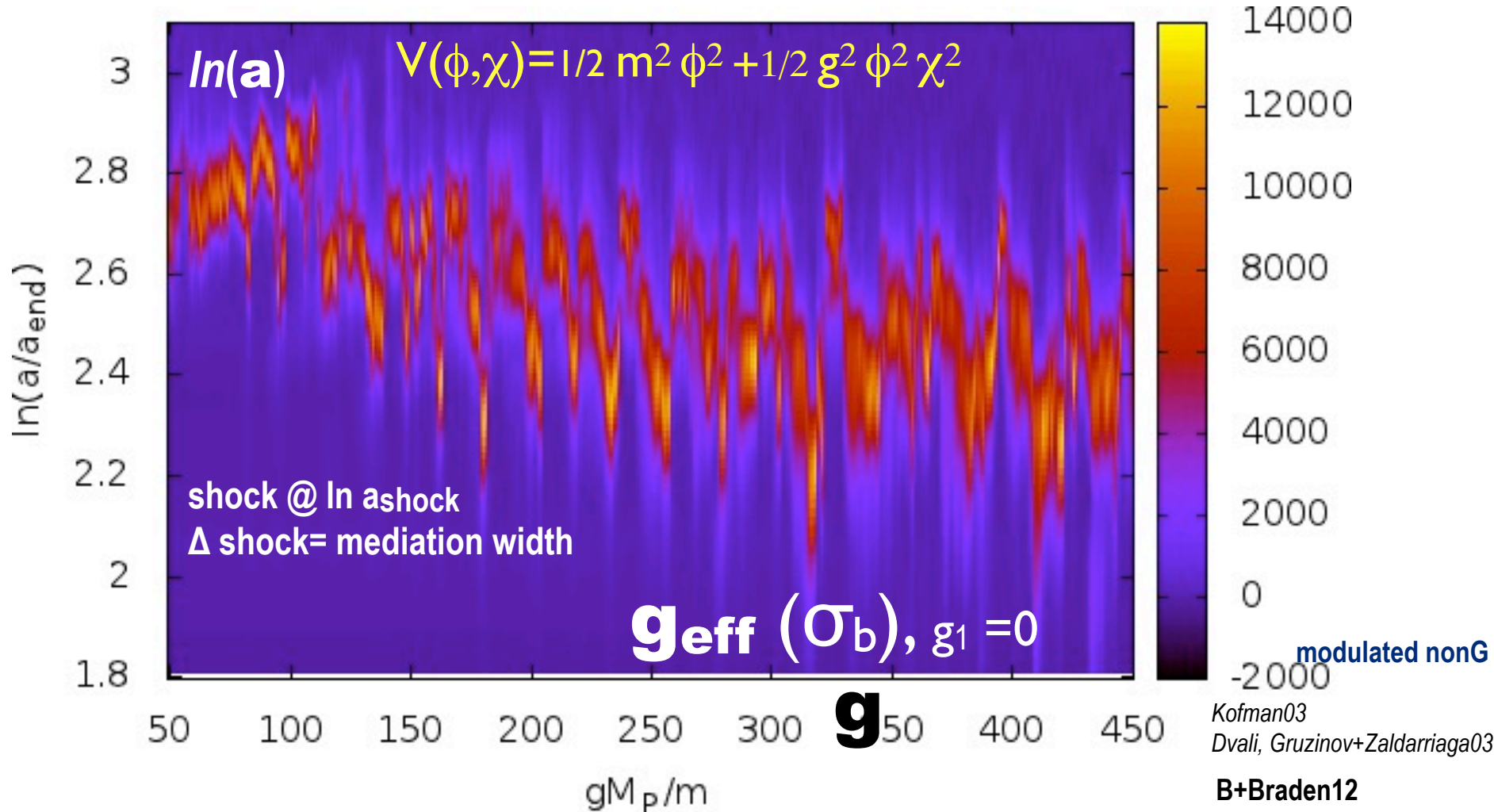


$$dS/dt(t, \mathbf{g}) \Rightarrow$$

the Shock-in-time: entropy production rate

non-Gaussianity
(WMAP, Planck, LSS)
spiky nG preheating

$\delta \ln a_{\text{shock}}(\mathbf{g}(\sigma(\mathbf{x}))) \Rightarrow$ modulated non-Gaussianity from preheating!



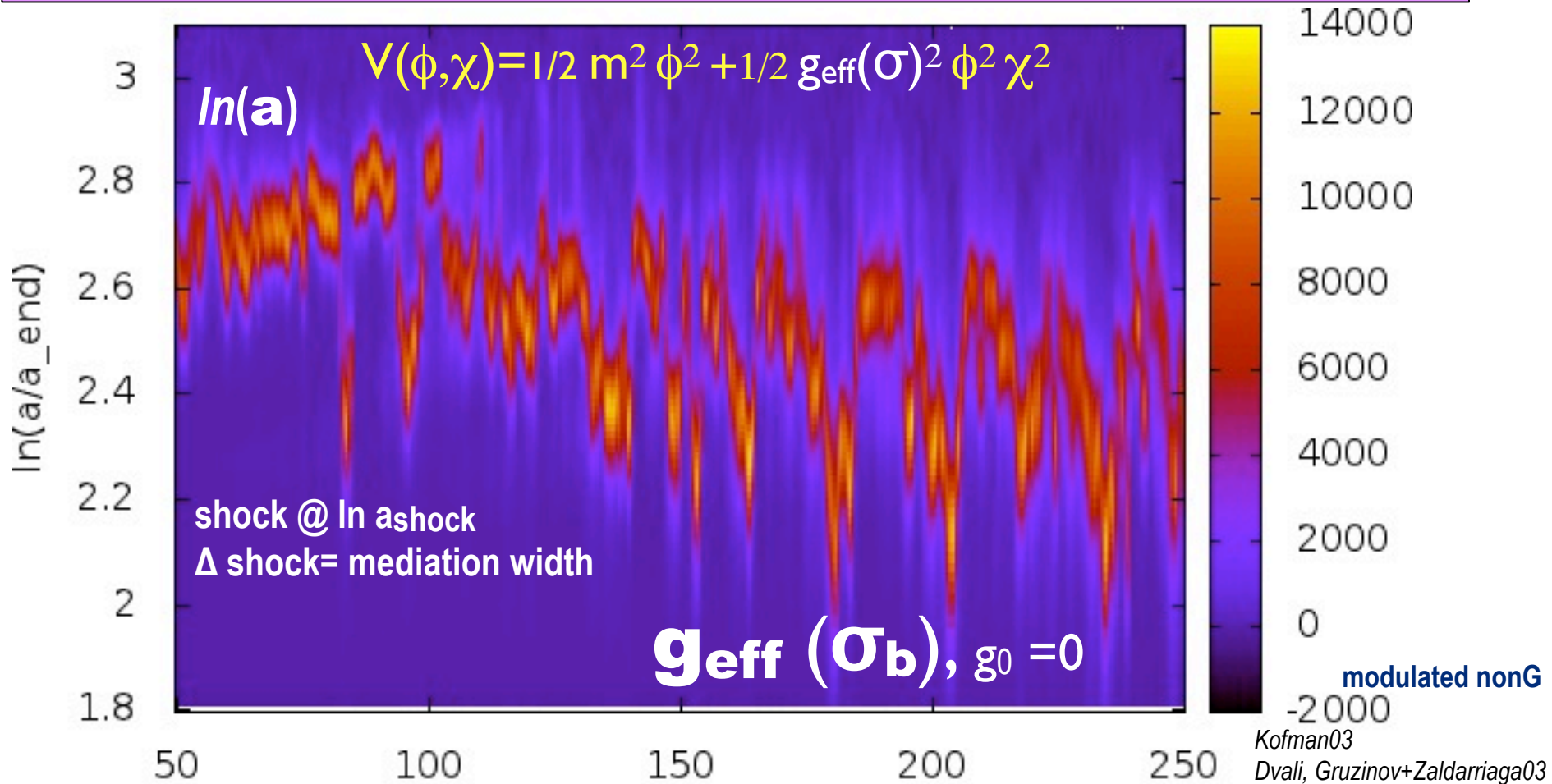
$\mathbf{g} = \mathbf{g}_{\text{eff}}(\sigma_b(\mathbf{x}))$ with frozen large scale $\sigma_b(\mathbf{x})$

$$dS/dt(t, \mathbf{g}) \Rightarrow$$

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$$g_{\text{eff}}(\sigma) = g_0 + g_1 \sigma/M_P, g_0 \exp[\gamma_1 \sigma/M_P], ..$$

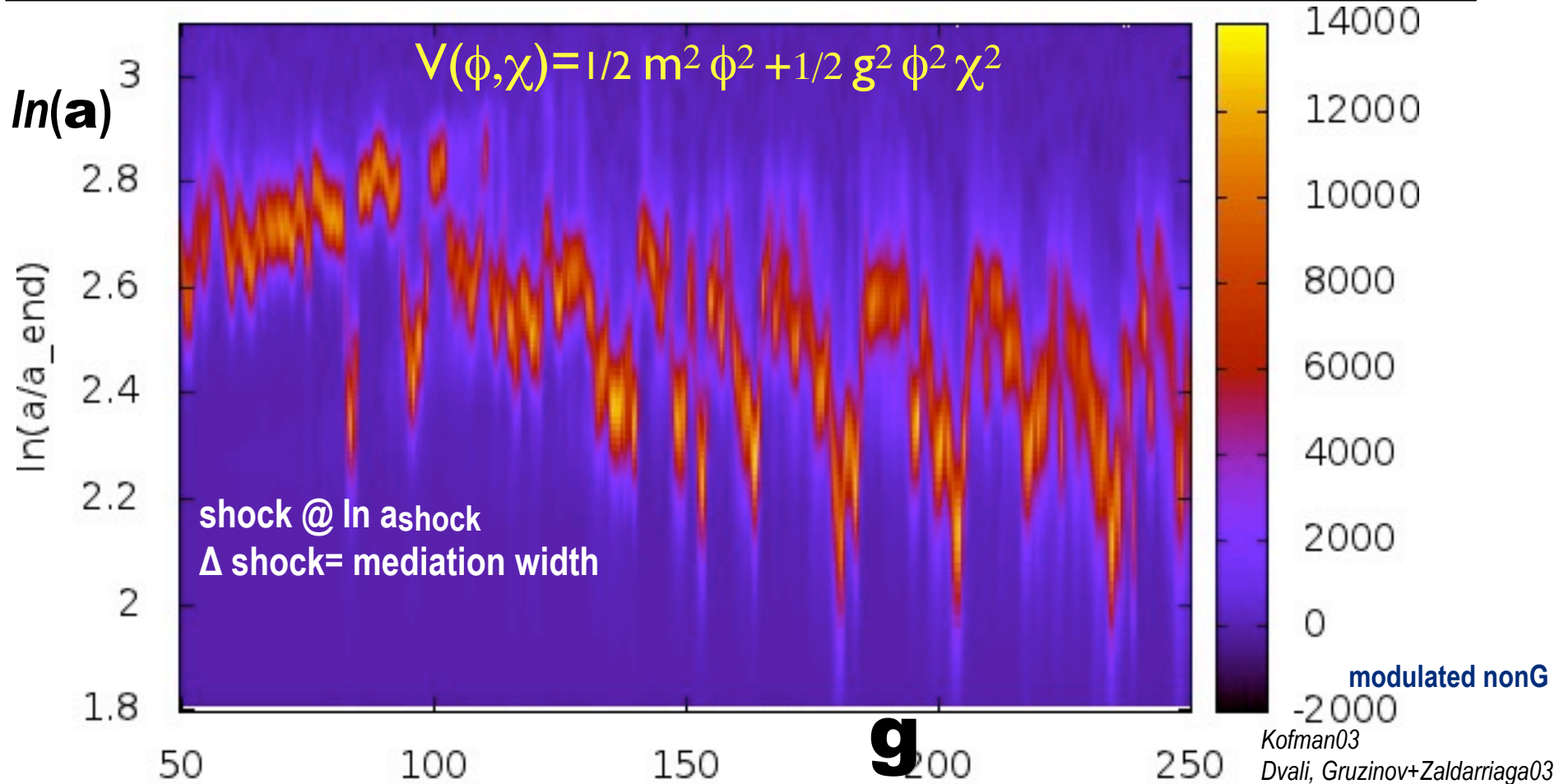
dynamical $\sigma_b(x, t) = \sigma - \sigma_f$ cf. frozen $\sigma_b(x)$ cf. $\chi_b(x) = \chi_i$

$$dS/dt(t, \mathbf{g}) \Rightarrow$$

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$$\delta \ln a_{\text{shock}}(\mathbf{g}(\sigma(\mathbf{x}))) \Rightarrow \text{modulated non-Gaussianity from preheating!}$$



Chaotic Billiards NonG

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

B+Frolov, Huang, Kofman 09

B+Braden12

B+Braden, Frolov, Huang 12

B+Braden+Mersini 2012

$$\delta \ln a_{\text{shock}}(\chi_i(\mathbf{x}) | g^2/\lambda) \Rightarrow \text{NonG of cold spots + BBM12: 3D Oscillons \& Colliding Bubbles?}$$

$$dS/dt(t, g) \Rightarrow$$

the Shock-in-time: entropy production rate

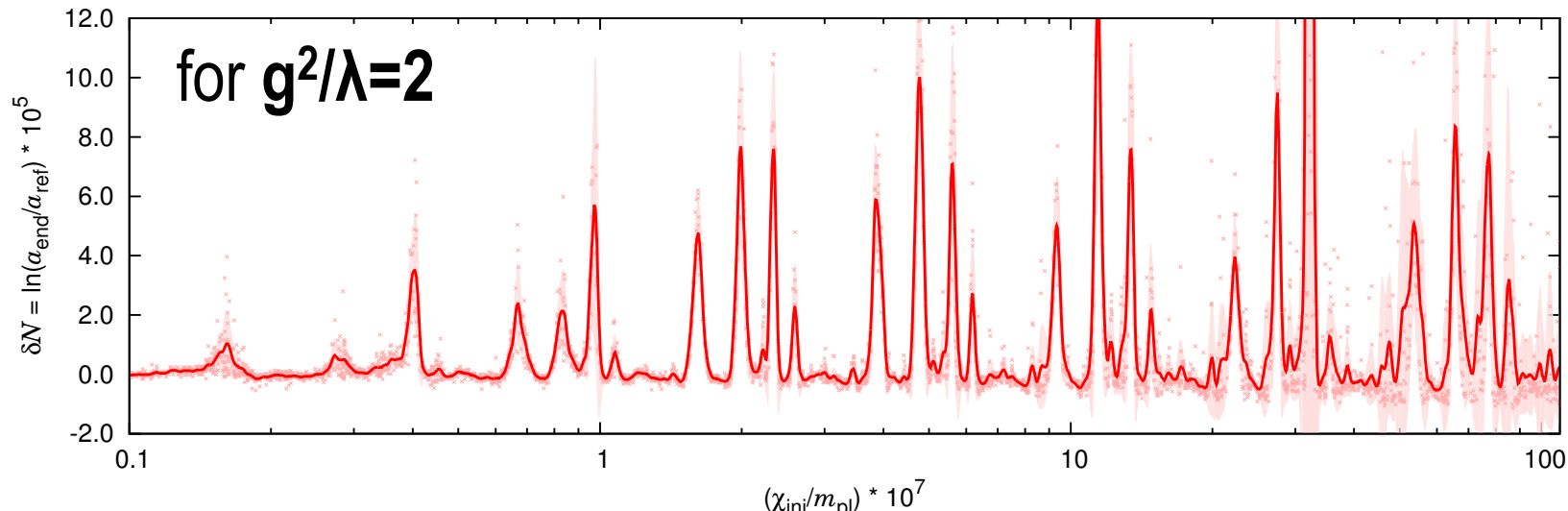
non-Gaussianity
(WMAP, Planck, LSS)
spiky nG preheating

$$\delta \ln a_{\text{shock}}(\chi_i(\mathbf{x}) | g^2/\lambda) \Rightarrow \text{Chaotic Billiards: NonG from Parametric Resonance in Preheating}$$

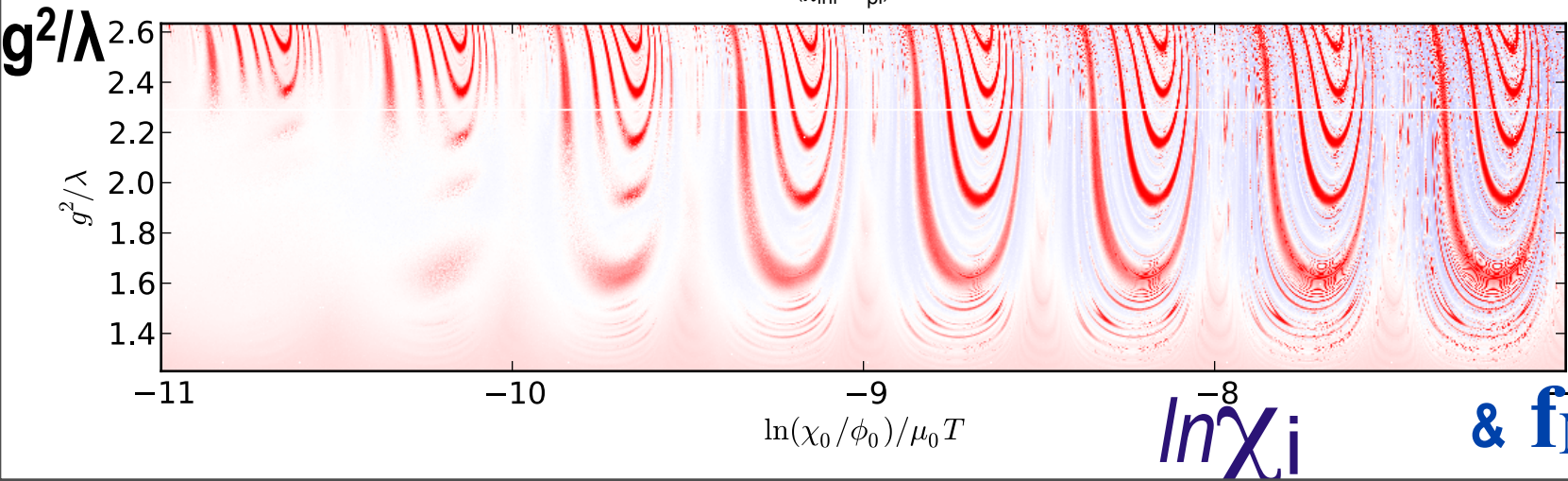
B+Frolov, Huang, Kofman 09

B+Braden, Frolov, Huang 12

$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$



huge number of
64^3 sims to
show the
wondrous
complexity of
 $\ln a(\chi_i, g^2/\lambda)$



$\ln \chi_i$ & f_{NL}^7 equiv

$$dS/dt(t, g) \Rightarrow$$

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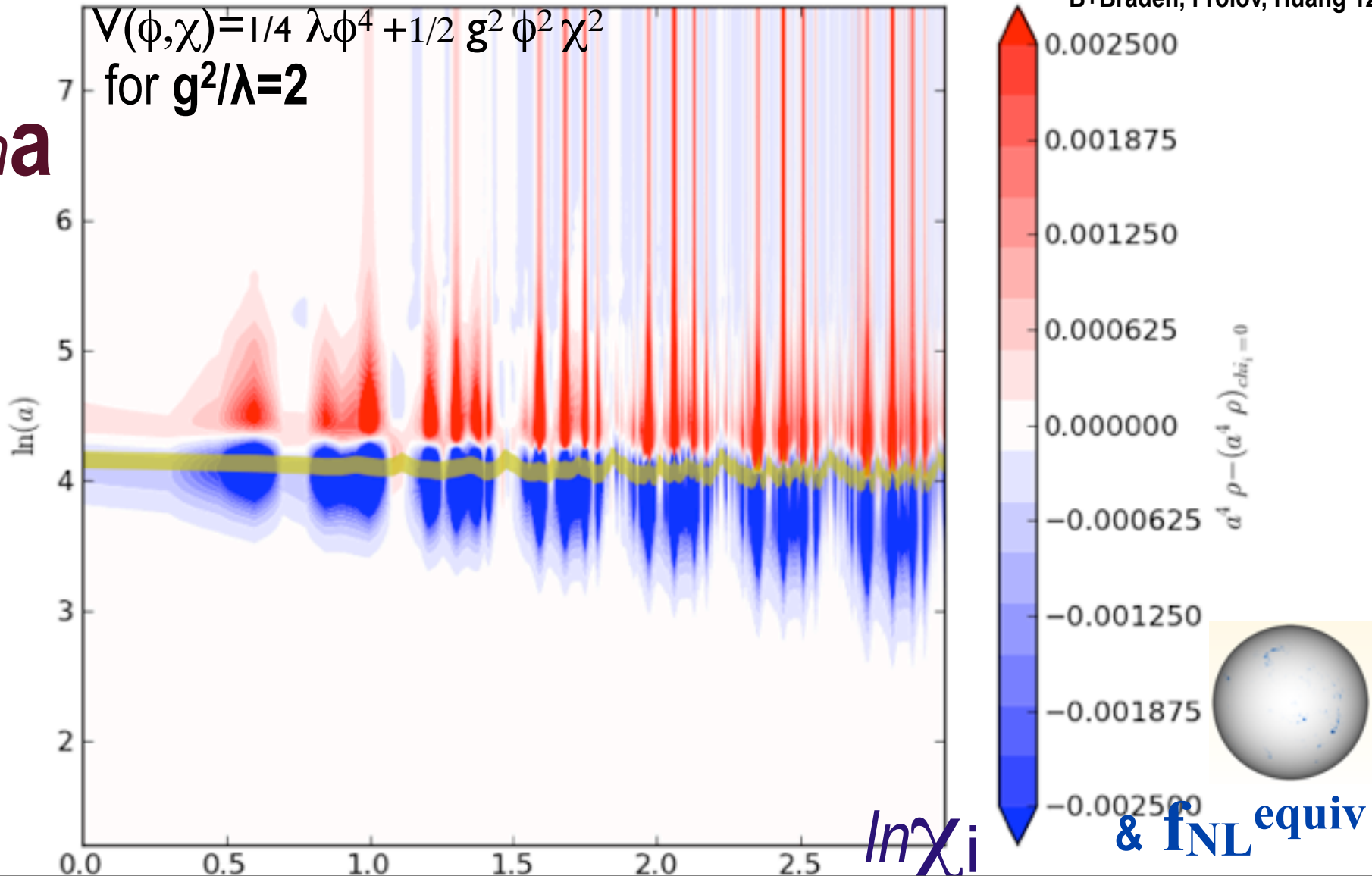
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$$V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$$

for $g^2/\lambda=2$

$\ln a$



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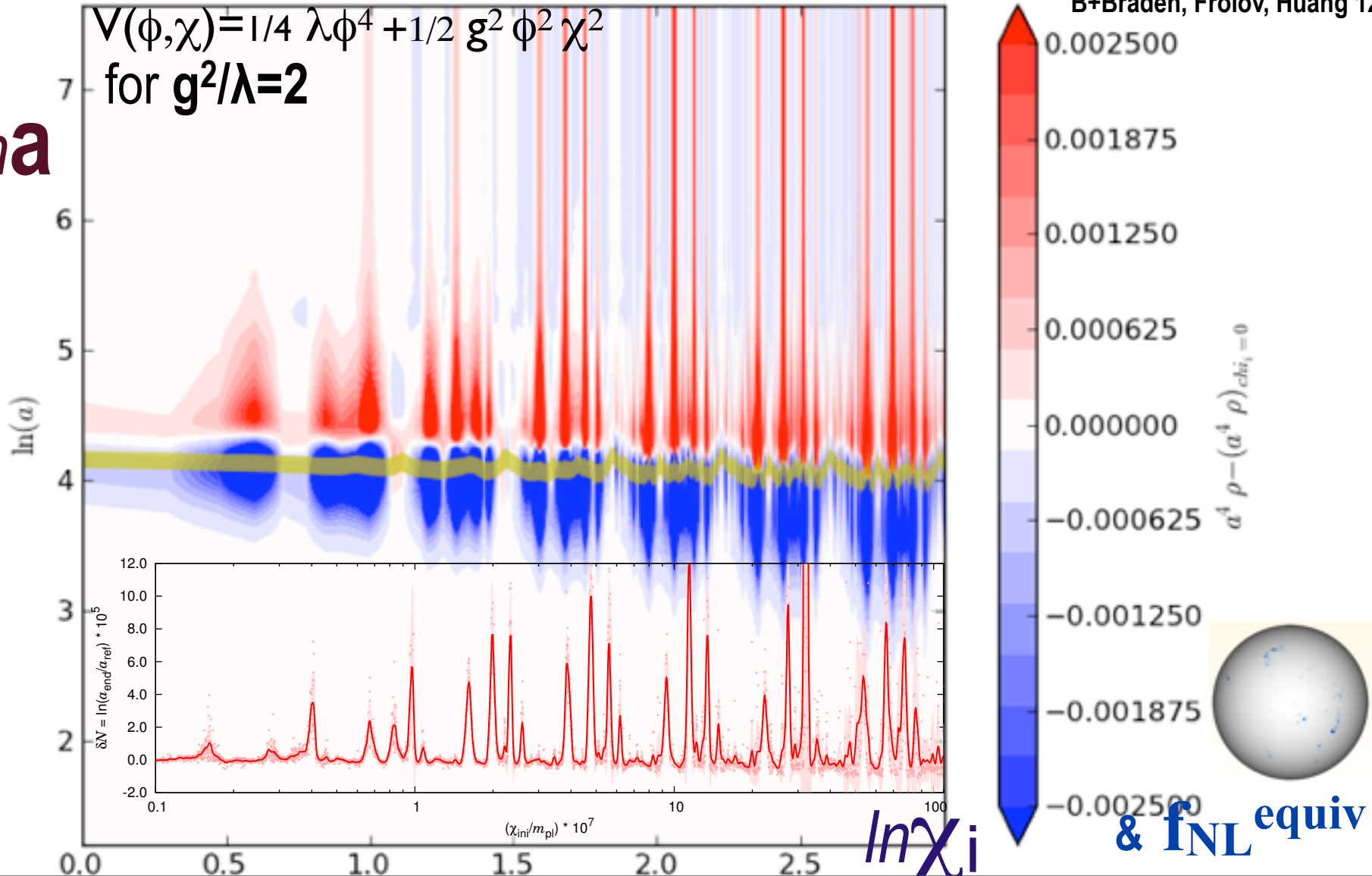
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B+Frolov, Huang, Kofman 09
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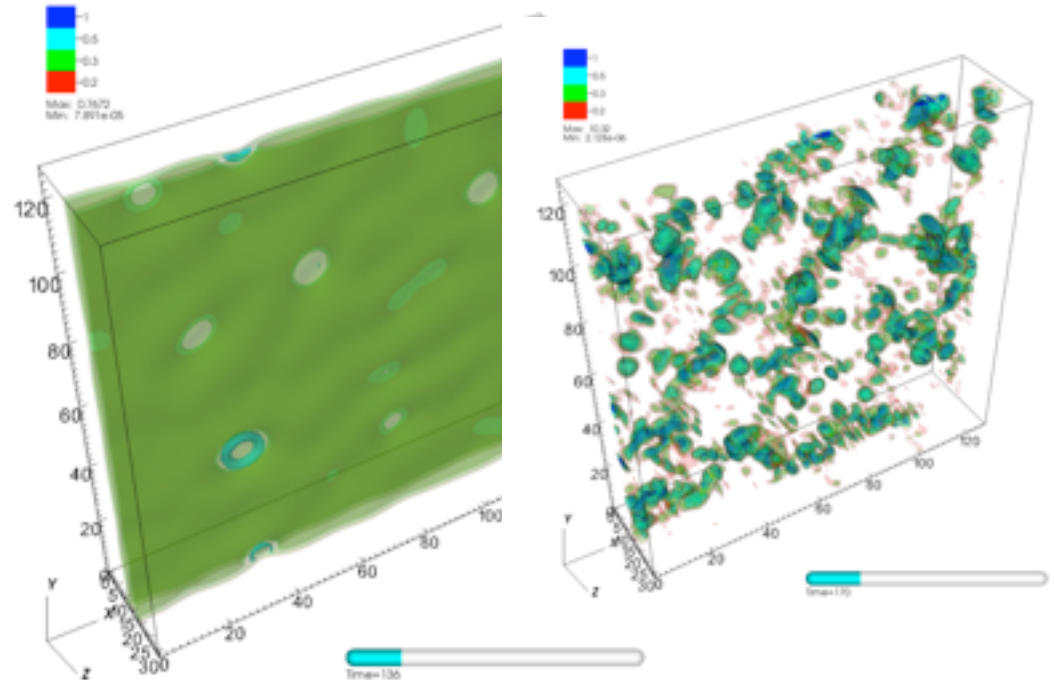
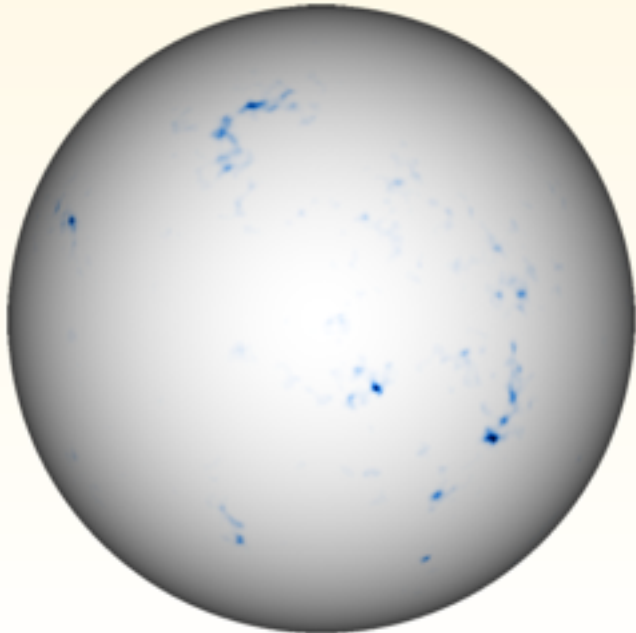


$$dS/dt(t, \mathbf{g}) \Rightarrow$$

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$$\delta \ln a_{\text{shock}}(\mathbf{g}(\sigma(\mathbf{x}))) \Rightarrow \text{modulated non-Gaussianity from preheating!}$$



& f_{NL} equiv

*when "vacuum" bubbles collide in full 3D lattice sims
with tiny zero point & wall fluctuations
 \Rightarrow burst of scalar radiation at c + long-lived oscillons, $\sim m^{-1}$*

modulated nonG

Chaotic Billiards NonG $V(\phi, \chi) = 1/4 \lambda \phi^4 + 1/2 g^2 \phi^2 \chi^2$ B+Frolov, Huang, Kofman 09
B+Braden, Frolov, Huang 12

$$\delta \ln a_{\text{shock}}(\chi_i(\mathbf{x}) | g^2/\lambda) \Rightarrow \text{NonG of cold spots + } \text{BBM12: 3D Oscillons \& Colliding Bubbles?}$$

B+Braden+Mersini 2012

Dick Bond CIFAR@CITA with CITA aka *Cosmic Information Theory & Analysis*

Probing the Cosmic Theory of Early & Late Universe Physics: from Simplicity to Complexity

the **nonlinear**
COSMIC WEB



dS_G/dt

primary anisotropies

- linear perturbations: scalar/density, tensor/gravity wave
- tightly-coupled photon-baryon fluid: oscillations $\delta_\gamma v_\gamma \pi_\gamma$
- viscously damped
- polarization π_γ
- gravitational redshift

$dS/dt > 0$



Decoupling LSS

17 kpc
(19 Mpc)

secondary
anisotropies

$dS/dt > 0$



• nonlinear evolution

• weak lensing

• thermal SZ
+ kinetic SZ

• $d\Phi/dt$

• dusty/radio galaxies, dGs



M
I
L
K
Y



$z=0$



Bayesian flow prior to posterior via likelihood

W
A
Y

DarkE

reionization

$dS_{astro} < 0$

$z \sim 1100$ redshift z

$z \sim 10$

$dS/dt > 0$

13.7-10⁻⁵⁰ Gyrs

13.7 Gyrs

time t

10 Gyrs

today